

MASITC\_01080381

**SPIE Terms of Use:** This SPIE eBook is DRM-free for your convenience. You may install this eBook on any device you own, but not post it publicly or transmit it to others. SPIE eBooks are for personal use only. For details, see the SPIE <u>Terms of Use</u>. To order a print version, <u>visit SPIE</u>.



## Field Guide to

# Illumination

Angelo V. Arecchi Tahar Messadi R. John Koshel

> SPIE Field Guides Volume FG11

John E. Greivenkamp, Series Editor



Bellingham, Washington USA

#### Introduction to the Series

to the SPIE Field Guides—a series Welcome publications written directly for the practicing engineer or scientist. Many textbooks and professional reference books cover optical principles and techniques in depth. The aim of the SPIE Field Guides is to distill this information, providing readers with a handy desk or reference that provides basic. information about optical principles, techniques, phenomena, including definitions and descriptions, key equations, illustrations, application examples, design considerations, and additional resources. A significant effort will be made to provide a consistent notation and style between volumes in the series.

Each SPIE Field Guide addresses a major field of optical science and technology. The concept of these Field Guides is a format-intensive presentation based on figures and equations supplemented by concise explanations. In most cases, this modular approach places a single topic on a page, and provides full coverage of that topic on that page. Highlights, insights, and rules of thumb are displayed in sidebars to the main text. The appendices at the end of each Field Guide provide additional information such as related material outside the main scope of the volume, key mathematical relationships, and alternative methods. While complete in their coverage, the concise presentation may not be appropriate for those new to the field.

The *SPIE Field Guides* are intended to be living documents. The modular page-based presentation format allows them to be easily updated and expanded. We are interested in your suggestions for new *Field Guide* topics as well as what material should be added to an individual volume to make these *Field Guides* more useful to you.

John E. Greivenkamp, Series Editor College of Optical Sciences The University of Arizona

#### The Field Guide Series

Field Guide to Geometrical Optics, John E. Greivenkamp (FG01)

Field Guide to Atmospheric Optics, Larry C. Andrews (FG02)

Field Guide to Adaptive Optics, Robert K. Tyson & Benjamin W. Frazier (FG03)

Field Guide to Visual and Ophthalmic Optics, Jim Schwiegerling (FG04)

Field Guide to Polarization, Edward Collett (FG05)

Field Guide to Optical Lithography, Chris A. Mack (FG06)

Field Guide to Optical Thin Films, Ronald R. Willey (FG07)

Field Guide to Spectroscopy, David W. Ball (FG08)

Field Guide to Infrared Systems, Arnold Daniels (FG09)

Field Guide to Interferometric Optical Testing, Eric P. Goodwin & James C. Wyant (FG10)

#### Field Guide to Illumination

In writing this *Field Guide* to Illumination, the first task was to decide what topics to include. Illumination tends to mean different things to different people. Certainly any subject matter under the purview of the CIE, Commission Internationale de l'Eclairage (the International Commission Illumination) on or the Illuminating Engineering Society of North America (IESNA) must be considered. Some particular areas pertaining to imaging optics systems and nonimaging are potentially overlooked. Thus, we chose to address a number of topics that fall under the following three categories: imaging system illumination, nonimaging optics for illumination, and architectural illumination, which all call upon principles of radiometry and photometry. Although this is not a guide to radiometry, enough information on the subject is included to make this manual a self-contained document. Additionally, those optical properties materials that are pertinent to illumination, such as surface color, scattering, and retroreflection are described.

The content in this Field Guide starts with traditional illumination in imaging systems, followed by the recent advances in computer-aided design of high efficiency nonimaging illumination optics, along with the modern source models that support these techniques. Sections on the illumination of visual displays are included.

There was not enough room for a complete treatment of architectural illumination, but some important topics are included at the end of this *Field Guide* such as indoor and outdoor architectural illumination.

The notation and terminology are consistent throughout this *Guide*, but we do not lose sight of the fact that they may not be consistent in the field. Examples of alternate notation and terminology are presented.

Angelo Arecchi Tahar Messadi R. John Koshel Hebron, NH Favetteville, AR Tucson, AZ

### **Table of Contents**

Glossary	ix
Basic Quantities in Illumination	1
Flux and Irradiance	1
Solid Angle	2
Intensity, Radiance, Projected Solid Angle	3
Solid Angle and Projected Solid Angle	4
Spectroradiometric and Radiometric Quantities	5
Photometric Quantities	6
Matrix of Basic Quantities	7
Photopic and Scotopic Vision	8
Luminous Efficacy	9
Typical Values of Illumination Quantities	10
Averaged LED Intensity	11
Color	12
Light Source Color	12
Chromaticity Diagram	13
Color Temperature and CCT	14
Dominant Wavelength and Purity	15
Surface Color	16
Color of Fluorescent Surfaces	17
Color Rendering and CRI	18
Calculating CRI and Problems with CRI	19
Sources for Illumination	20
Typical Source Parameters	20
Tungsten Lamps	21
Tungsten and Sunlight	22
Fluorescent Lamps	23
H.P. Sodium and Metal Halide	24
Xenon and White LED	25
Light Emitting Diodes (LEDs)	26
Illumination Properties of Materials	27
Transmittance, Reflectance, and Absorptance	27
Reflectance Factor and BRDF	28
Harvey / $ABg$ Scatter Model	29
Directional Properties of Materials	30

Retroreflectors—Geometry	31
Retroreflectors—Radiometry	32
Illumination Transfer	33
Lambertian and Isotropic Models	33
Known Intensity	34
Known Flux and Known Radiance	35
Form Factor and Average Projected Solid Angle	36
Configuration Factor	37
Useful Configuration Factor	38
Useful Form Factor	39
Irradiance from a Uniform Lambertian Disk	40
Cosine Fourth and Increase Factor	41
Known Irradiance	42
$\omega$ , $\Omega$ , NA, and f/# for a Circular Cone	43
Invariance of Radiance	44
Illumination in Imaging Systems	45
Image Radiance	45
Limitations on Equivalent Radiance	46
Image Irradiance	47
f/#, Working f/#, T/#, NA, Ω	48
Flux and Étendue	49
Illumination in Nonimaging Systems	50
Generalized Étendue	50
Concentration	51
Skew Invariant	52
Fibers, Lightpipes, and Lightguides	53
Fibers—Basic Description	53
Numerical Aperture and Étendue	54
Fiber Bundles	55
Tapered Fibers and Bundles	56
Classical Illumination Designs	57
Spherical Reflector	57
Abbe Illumination	58
Köhler Illumination	59

viii

Ellipsoidal and Paraboloidal Mirrors	60
Spectral Control and Heat Management	61
Illumination in Visual Afocal Systems	62
Uniform Illumination	63
Searchlight	63
Source at a Distance	64
Mixing Rod	65
Bent Lightpipes	66
Integrating Sphere	67
Lenslet Arrays	68
Small Reflectors, Lenslet Arrays, and Facets	69
Source Models	70
Source Modeling Overview	70
Source Modeling Methods	71
LED Modeling	72
Incandescent Lamp Modeling	73
Arc and Fluorescent Lamp Modeling	74
The dia Flactocoom Edin Modeling	
Nonimaging Compound Concentrators	<b>75</b>
Nonimaging Compound Concentrators	75
Concentrators as Luminaires	76
Compound Parabolic Concentrators	77
Compound Elliptical and Hyperbolic Concentrators	78
Tailored-Edge-Ray Design	79
Faceted Reflector Design	80
Advanced Nonimaging Optic Design	81
Displays	82
Displays—Overview	82
Backlit Display Components	83
Backlit Display: Source and Injector	84
Backlit Display: Bource and Injector Backlit Display: Lightguides, Features, Reflectors	85
Backlit Display: Polarizers, LC, and BEF	86
Projection Displays	87
1 Tojection Displays	01
<b>Characterizing Illumination Systems</b>	88
Mapping Flat-Fielding Sources	88

Goniophotometers	89
Types A, B, C Goniometer Coordinate Systems	90
"Snapshot" Goniophotometers	91
Shapshot domophotometers	O I
Software Modeling	92
Software Modeling Discussion	92
Architectural Illumination	93
Role of Light in Architecture	93
Light and Visual Performance	94
Eye Adaptation and Visual Fields	94
Apparent Brightness	95
Apparent Brightness	00
Lighting Design	96
Lighting Design—Layering of Light	96
Luminaire for Open-Plan Office	97
Photometric Report and VCP	97
Spacing Criteria and Coefficient of Utilization	98
Daylight Compensation	99
Daylight Factor	99
Daylight Strategies	100
Exterior Lighting	101
Exterior Lighting	(3)
Nighttime Visibility Criteria	101
Recommended Illuminance for Façades	102
Façade Floodlighting for Uniform Illumination	103
Illumination of Outdoor Areas	104
Special Considerations for Outdoor Fixtures	105
Parking	106
Outdoor Luminaire—Transverse Light	100
Distribution	106
Outdoor Luminaire—Lateral Light Distribution	$100 \\ 107$
Caracor Daminanc Dateral Digit Distribution	101
Roadway Lighting	108
Criteria for Roadway Lighting	108

Small Target Visibility Recommended Roadway Luminaires Recommended Lamps for Roadway Luminaires	109 110 111
Appendix Equation Summary CIE Illuminants A and D65 $\bar{x}, \bar{y}, \bar{z}, V(\lambda)$ , and $V'(\lambda)$ Archaic and Arcane Units of Illumination	112 112 119 122 125
Bibliography	127
Index	133

## Glossary

α	Absorptance
α	Observation angle (in retroreflection)
$a_i$	Input area to a compound concentrator
$a_o$	Output area of a compound concentrator
$\boldsymbol{A}$	Absorbance
$A_i$	Illuminated area
$A_r$	Radiating area
$a_x$	Area of plane $x$
$a\Omega$	Throughput, étendue
C	Concentration ratio
CCT	Correlated color temperature
CIE	International Commission on Illumination
CRI	Color rendering index
$d_i$	Diameter of input aperture to a CPC
$d_o$	Diameter of output aperture of a CPC
$d_s$	Diameter of small aperture of a CPC
$D(\mu,\lambda)$	Donaldson matrix
$\boldsymbol{E}$	Irradiance
$E_{\perp}$	Illuminance normal to the illumination
$E_0$	Axial irradiance
$oldsymbol{E}_e$	Edge irradiance
$oldsymbol{E}_i$	Image irradiance
$oldsymbol{E}_{i0}$	Axial image irradiance
$oldsymbol{E}_{\lambda}$	Spectral irradiance
<i>f</i> /#	F-number
$f/\#_{ m w}$	Working F-number
F'	Increase factor
$F_{a \ { m to} \ b}$	Form factor from $a$ to $b$
$f_{ m skew}$	Skew invariant
I	Intensity
$m{I}_{ ext{LED A}}$	Averaged LED intensity, CIE condition A
$I_{ m LEDB}$	Averaged LED intensity, CIE condition B
$oldsymbol{I}_{\lambda}$	Spectral intensity
L	Radiance
	CIE 1976 (L*a*b*) color space; CIELAB
	CIE 1976 (L*u*v*) color space; CIELUV
$L_i$	Image radiance
$L_o$	Object radiance
$L_{\lambda}$	Spectral radiance

## Glossary (cont.)

M	Integrating sphere multiplier
m	Lateral image magnification
n	Index of refraction
NA	Numerical aperture
OD	Optical density
$p_e$	Purity
$\overline{pf}$	Packing fraction
psa	Projected solid angle
R	Reflectance factor
$R_A$	Coefficient of retroreflection
$R_a$	General color rendering index
$R_I$	Coefficient of retroreflected luminous intensity
$R_L$	Coefficient of retroreflected luminance
$S_{\lambda}(\lambda)$	Spectral density of a light source
T	Transmittance factor
T/#	T-number
u, v	CIE 1960 UCS chromaticity coordinates
u', v'	CIE 1976 UCS chromaticity coordinates
$V(\lambda)$	Photopic luminous efficiency
$V'(\lambda)$	Scotopic luminous efficiency
$W^*U^*V^*$	CIE 1964 uniform space coordinates
<i>x</i> , <i>y</i>	CIE 1931 chromaticity coordinates
X, Y, Z	CIE tristimulus values
$\overline{x}, \overline{y}, \overline{z}$	CIE color matching functions
В	Entrance angle (in retroreflection)
ξ	Generalized étendue
λ	Wavelength, emission wavelength
$\lambda_{0.5 ext{m}}$	Center wavelength (for LED)
$\lambda_c$	Centroid wavelength (for LED)
$\lambda_d$	Dominant wavelength
$\lambda_{p}$	Peak wavelength (for LED)
μ	Excitation wavelength
$\underline{\mathbf{\rho}}$	Reflectance
$\frac{ ho}{ ho}$	Average reflectance
τ	Transmittance
υ	Viewing angle (in retroreflection)
Φ	Flux
$\Phi_{\lambda}$	Spectral flux
Ω	Projected solid angle (psa)

## Glossary (cont.)

$\frac{\omega}{\overline{z}}$	Solid angle
$\overline{\Omega}_{a \text{ to } b}$	Average projected solid angle from $a$ to $b$
$\Omega_i$	Input psa to a compound concentrator
$\Omega_o$	Output psa from a compound concentrator
$\Omega_x$	Projected solid angle viewed from plane <i>x</i>
$\Theta_i$	Input half-angle of compound concentrator
$\Theta_o$	Output half-angle from compound concentrator
$\theta_{max}$	Maximum output half-angle from CPC

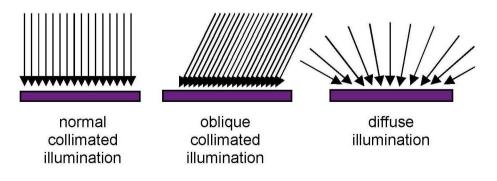
#### Flux and Irradiance

In examining terminology for illumination, it is useful to separate the spatial considerations from the spectral concerns. In many cases, the spatial and spectral issues are independent and can be separated without losing any generality. In other cases, the spatial and spectral issues cannot be separated physically, but it is useful to separate them conceptually. The commonly used spatial quantities are flux, irradiance, intensity, and radiance.

Flux,  $\Phi$ , is the optical power or rate of flow of radiant energy.

Irradiance, E, is the flux per unit area striking a surface. Occasionally, the flux per unit area leaving a surface, called **exitance**, M, is important. However, the geometry is the same as for irradiance, so it will not be treated separately here. Furthermore, when exitance is used, it is often the flux leaving a nonphysical surface such as the exit port of an integrating sphere or the real image in an imaging system, where it is identical to the irradiance onto the surface.

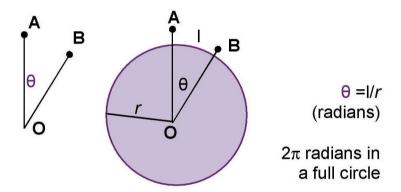
The irradiance quantity itself says absolutely nothing about the directionality of the flux. For example, if the three cases in the figure below all have the same flux per unit area striking the surface, then they all have the same irradiance. Because of this ambiguity, specifications for illumination systems often qualify the irradiance quantity with an added description of the desired directional properties.



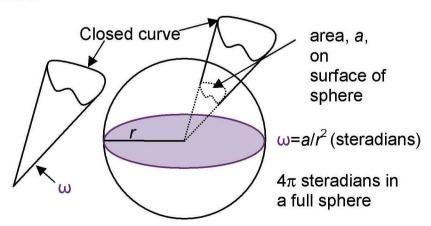
#### Solid Angle

The definition of intensity involves the concept of a solid angle. A solid angle is a 3D angular volume that is defined analogously to the definition of a plane angle in two dimensions.

A plane angle,  $\theta$ , made up of the lines from two points meeting at a vertex, is defined by the arc length of a circle subtended by the lines and by the radius of that circle, as shown below. The dimensionless unit of plane angle is the radian, with  $2\pi$  radians in a full circle.



A solid angle,  $\omega$ , made up of all the lines from a closed curve meeting at a vertex, is defined by the surface area of a sphere subtended by the lines and by the radius of that sphere, as shown below. The dimensionless unit of solid angle is the **steradian**, with  $4\pi$  steradians in a full sphere.



#### Intensity, Radiance, and Projected Solid Angle

Intensity, *I*, is the flux per unit solid angle. It is the amount of flux from a point source contained in a small angular volume. A source can be considered a point source for this application if the irradiance falls off as the **inverse square** of the distance from the source. Intensity, for a given source, can vary with direction.

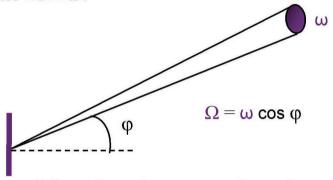
The term "intensity" is used in many disciplines, some even closely related to optics, to mean things other than flux per unit solid angle. Use caution and rely on context to determine the meaning of the word in a particular situation.

Radiance, L, applies to extended sources and surfaces. It is the flux per unit solid angle per unit projected area of the source or surface. The projected area is the projection of the area onto a surface normal to the direction of view and is equal to the actual area times the cosine of the angle between the surface normal and the direction of view. Radiance can vary with position on a surface, and like intensity, it can vary with direction. A source or surface with constant radiance in all directions is called Lambertian. A Lambertian source or surface has intensity that varies with the cosine of the angle with the surface normal.

In many cases, the angle of view changes over the extent of the receiver. These cases require an alternate definition of radiance: radiance is the flux per unit area per unit **projected solid angle**. (In fact, this is the more general definition and covers the simpler case where the entire surface of the extended source is at essentially the same angle as the direction of view.)

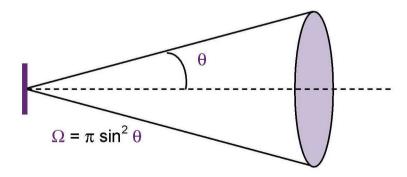
#### Solid Angle and Projected Solid Angle

The relationship between solid angle and projected solid angle can be confusing. Projected solid angle has meaning primarily for a small Lambertian source, which has intensity that varies as the cosine of the angle with the surface normal. The **projected solid angle**,  $\Omega$ , is the **solid angle**,  $\omega$ , weighted by the cosine of the angle with the surface normal.



When the solid angle is large enough so that the angle with the surface normal is not the same over the entire solid angle, the total projected solid angle must be computed by integrating the incremental projected solid angles. See the reference by Bartell for a more detailed explanation.

For some special cases, the integration results in simple expressions, such as for a large circular cone that is normal to a surface and subtends a half angle,  $\theta$ .



A hemisphere has  $2\pi$  steradians (solid angle) but  $\pi$  projected steradians (projected solid angle).

#### Spectroradiometric and Radiometric Quantities

In the spectral dimension of illumination, the most general view looks at the spectral density—the amount of radiation per unit wavelength interval. In terms of the four spatial quantities already considered, the spectral quantities are **spectral flux**,  $\Phi_{\lambda}$ ; **spectral irradiance**,  $E_{\lambda}$ ; **spectral intensity**,  $I_{\lambda}$ ; and **spectral radiance**,  $L_{\lambda}$ . These quantities, usually written with a subscript to indicate that they are integrable, must be integrated to determine the amount of radiation in a particular spectral band. For example, the **total radiant flux**,  $\Phi$  (in units of watts), in the band between wavelength  $\lambda 1$  and wavelength  $\lambda 2$  is

$$\Phi(\lambda 1, \lambda 2) = \int_{\lambda 1}^{\lambda 2} \Phi_{\lambda}(\lambda) \cdot d\lambda.$$

Similar expressions can be written for the total irradiance, E (watts/m<sup>2</sup>); total radiant intensity, I (watts/sr); and total radiance, L (watts/m<sup>2</sup>·sr).

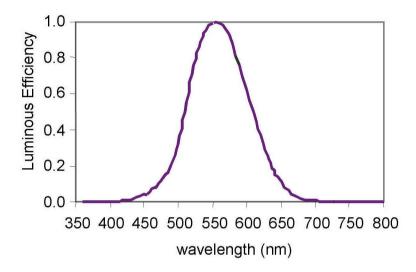
Photometry measures the response of the human eye to light. Although not everyone has exactly the same the standardized CIE 1924 luminous response, efficiency function works very well for most people. (The CIE is the International Commission Illumination.) This function, shown on the following page, is designated  $V(\lambda)$ . The values for this function, in 5-nm increments, are given in the Appendix. Not coincidentally, this function is identical to the CIE color matching function, y. The unit of luminous (photopic) flux is the lumen. The luminous flux is found from the spectral flux and the  $V(\lambda)$  function from the following relationship:

luminous flux = 
$$683 \int \Phi_{\lambda}(\lambda) \cdot V(\lambda) \cdot d\lambda$$
.

The factor of 683 in this equation comes directly from the definition of the fundamental unit of luminous intensity, the candela.

#### **Photometric Quantities**

## CIE 1924 Luminous Efficiency $(V\lambda)$



#### Notes on notation:

- The photopic quantities of flux, irradiance, intensity, and radiance are called luminous flux, illuminance, luminous intensity, and luminance, respectively.
- These quantities are sometimes notated with a subscript "v" (for visual), as  $\Phi_v$ ,  $E_v$ ,  $I_v$ , and  $I_v$ . But often the subscript is omitted since the meaning is usually clear from the context, and it could be confused with the subscript notation often reserved for integrable quantities.
- The designations  $\Phi$ , E, I, and L are common but not universally standard. Another set of symbols sometimes used is P, H, J, and N, respectively, for radiometric quantities;  $P_{\lambda}$ ,  $H_{\lambda}$ ,  $J_{\lambda}$ , and  $N_{\lambda}$  for spectral quantities; and F, E, I, and B for the corresponding photometric quantities.
- Solid angle and projected solid angle are not always distinguished by  $\omega$  and  $\Omega$ , respectively.

#### Matrix of Basic Quantities

	SPECTRAL			
		Radio- metric	Spectral	Photopic
	Flux	Power	Power/ wavelength interval	Luminous flux
		watts (W)	watts/nm	lumens (lm)
		Irradiance	Spectral	Illuminance
$\boldsymbol{S}$	Flux/		irradiance	$ m lm/m^2$
$\boldsymbol{P}$	area	$ m W/m^2$	$ m W/m^2 \cdot nm$	or lux
$egin{array}{c} A \ T \ I \end{array}$	Flux/	(Radiant) intensity	Spectral intensity	(Luminous) intensity
$\boldsymbol{A}$	solid	,	3	m lm/sr
$oldsymbol{L}$	angle			or
		W/sr	W/sr nm	candela (cd)
		Radiance	Spectral radiance	Luminance
	Flux/			lm/m² ∙sr
	area·			or
	solid			$\mathrm{cd}/\mathrm{m}^2$
	angle			or
		W/m <sup>2</sup> sr	W/m <sup>2</sup> sr nm	nit

The table above shows the four spatial quantities and the three spectral categories that are discussed in the preceding pages. These create 12 distinct cells that cover the vast majority of specifications for illumination systems.

With two exceptions, both used mainly in the United States, work in illumination is almost always done in SI units. The two exceptions (both deprecated) are:

#### Illuminance

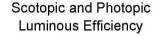
1 footcandle  $(lm/ft^2) = 10.764 lux (lm/m^2)$ 

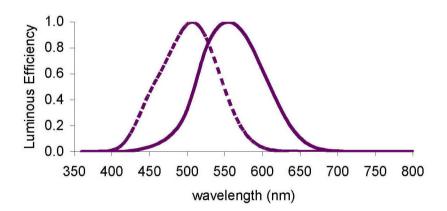
#### Luminance

1 footlambert (candela/ $\pi$ ft²) = 3.426 nit (candela/m²)

#### Photopic and Scotopic Vision

The human visual system responds to light over a wide dynamic range, in excess of 6 orders of magnitude. To achieve this dynamic range, the mechanisms for high-light-level vision and low-light-level vision are different. The high-level region, called the **photopic region**, is active at luminance levels above about 3 cd/m². The low-level region, called the **scotopic region**, is active below approximately  $0.01 \text{ cd/m}^2$ . The region between pure photopic and pure scotopic is called the **mesopic region**, where the visual response is a mixture of the two. The **photopic efficiency**, usually designated  $V(\lambda)$ , peaks at 555 nm, while the **scotopic efficiency**, usually designated  $V(\lambda)$ , peaks at 507 nm.





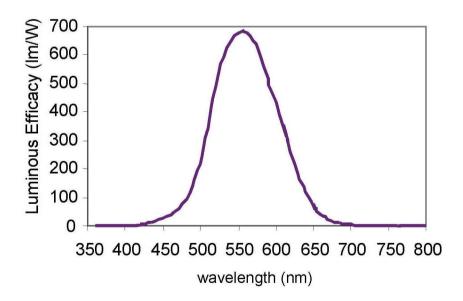
The values for photopic efficiency and scotopic efficiency, both in 5-nm increments, are given in the Appendix.

#### **Luminous Efficacy**

Luminous efficacy, quantified in lumens per watt, is a measure of the ability of a light source to produce a visual response from its power. In the photopic region, luminous efficacy peaks at 683 lumens per watt at 555 nm. In fact, the lumen is defined in terms of the power at 555 nm (frequency of  $540 \times 10^{12}$  Hz). Specifically, the definition (adopted in 1979) is in terms of the candela (lumen per steradian).

The candela is the luminous intensity, in a given direction, of a source that emits monochromatic radiation at a frequency of  $540 \times 10^{12}$  Hz and that has a radiant intensity in that direction of 1/683 watt per steradian.

## Luminous Efficacy (photopic)



It is usually clear from the context whether the power is the radiated power (as in the discussion above) or, often for lamps, the "wall-plug" power.

#### Typical Values of Illumination Quantities

Direct sunlight 1000 W/m² (250–250		
	nm)	
Direct sunlight	100,000 lux	
Shade	10,000 lux	
Overcast day	1,000 lux	
Office space	300–600 lux	
Full moon	0.2 lux	
Quarter moon	0.01 lux	
Moonless clear night	0.001 lux	
Luminous	Intensity	
Automobile headlight	$5{,}000-20{,}000~\mathrm{cd}$	
Household flashlight	100–1,000 cd	
100-W tungsten lightbulb	$100 \mathrm{\ cd}$	
LED traffic signal	$250 – 700 \mathrm{\ cd}$	
Single LED	$1~\mathrm{mcd}{-25}~\mathrm{cd}$	
Radiance and	d Luminance	
Sun	$2  imes 10^7  \mathrm{W/m^2  sr}$	
	(250–2500nm)	
Sun	$2 \times 10^9 \text{ nit}$	
Frosted lightbulb	100,000 nit	
Fluorescent lamp	5,000 nit	
Computer screen	100 nit	

Wavelength Ranges for Illumination			
UV-C*	250 to 280 nm		
UV-B	280 to 315 nm		
UV-A	315 to 400 nm		
Visible	$\sim$ 360–400 to $\sim$ 760–800 nm		
Near-infrared (NIR)†	760 nm to 1.1 μm		

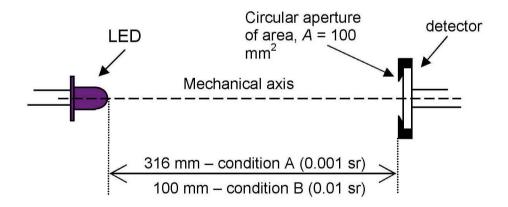
<sup>\*</sup> Actual definition of UV-C is 100 to 280 nm. However, the range from 100 to 250 nm is not of interest for illumination systems.

 $<sup>^{\</sup>dagger}$  Actual definition of NIR is to 1.4  $\mu m.$  However, 1.1  $\mu m$  is the upper limit for silicon-based detectors.

#### **Averaged LED Intensity**

In 1997 the CIE established a special quantity for lightemitting diodes (LEDs) called the **averaged LED intensity**. This was introduced because, as stated in CIE Publication 127:2007, *Measurement of LEDs*, "There are significant differences between LEDs and other light sources which made it necessary for the CIE to introduce a new quantity for their characterization with precisely defined measurement conditions."

To obtain **averaged LED intensity**, the LED is measured on its mechanical axis (in line with the package) by a circular detector of area  $100 \text{ mm}^2$  at a prescribed distance from the front tip of the LED package. Two distances are used: 316 mm (condition A) and 100 mm (condition B), with the solid angles defined as 0.001 sr and 0.01 sr, respectively. The measurements made are notated as  $I_{\text{LED A}}$  and  $I_{\text{LED B}}$  in units of intensity (candela or W/sr). Since the entire measurement geometry is completely defined, the measurements should be repeatable.



#### **Light Source Color**

The perceived color of a light source is quantified by its **chromaticity**. Chromaticity is calculated from the spectral density of the light source,  $S_{\lambda}$ , and the CIE **color matching functions**,  $\overline{x}$ ,  $\overline{y}$ , and  $\overline{z}$  as follows:

$$\begin{split} X &= \int S_{\lambda}(\lambda) \cdot \overline{x}(\lambda) \cdot d\lambda, & x &= \frac{X}{X + Y + Z}, \\ Y &= \int S_{\lambda}(\lambda) \cdot \overline{y}(\lambda) \cdot d\lambda, & y &= \frac{Y}{X + Y + Z}, \end{split}$$

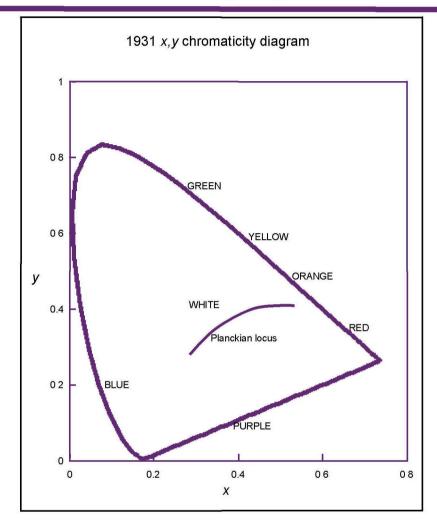
where X, Y, and Z are called **tristimulus values**, and x and y are the CIE **1931 chromaticity coordinates**. The integrals above are usually calculated as block summations from 360 to 830 nm, generally at 1-nm or 5-nm intervals. A table of  $\overline{x}$ ,  $\overline{y}$ , and  $\overline{z}$ , in 5-nm intervals can be found in the Appendix.

The 1931 chromaticity coordinates (x, y) are common coordinates for light-source colors and are represented graphically by the familiar "horseshoe" graph. All of the possible colors of light are contained inside the horseshoe shape, with the pure monochromatic spectral colors around the curved perimeter, the purples along the straight line at the bottom, and less-saturated colors in the interior. The various shades of white, which are of the most interest in illumination systems, occupy the central region.

Those white lights that have near-blackbody spectra (such as tungsten incandescent lamps) lie along the **Planckian locus**. The lower blackbody temperatures lie toward the red, and the higher temperatures toward the blue.

Color 13

#### **Chromaticity Diagram**



Two other coordinate systems are used to describe the chromaticity of light sources: the CIE 1960 UCS coordinate system (u, v), and the CIE 1976 UCS coordinate system (u', v'). Both attempt to portray equal perceived color differences by equal distances.

$$u = 4X/(X+15Y+3Z) = 4x/(-2x+12y+3),$$

$$v = 6Y/(X+15Y+3Z) = 6y/(-2x+12y+3),$$

$$u' = 4X/(X+15Y+3Z) = 4x/(-2x+12y+3),$$

$$v' = 9Y/(X+15Y+3Z) = 9y/(-2x+12y+3).$$

The CIE 1960 UCS coordinate system is obsolete except for calculating correlated color temperature.

#### Color Temperature and CCT

Any light source whose chromaticity coordinates fall directly on the Planckian locus has a **color temperature** equal to the blackbody temperature of the Planckian radiator with those coordinates. Color temperature is usually expressed in Kelvins (K). The concept of color temperature is especially useful for incandescent lamps, which very closely approximate a blackbody spectrum throughout the visible region. For these lamps, the color temperature also defines the spectrum in this region.

For white lights that don't have chromaticity coordinates that fall exactly on the Planckian locus but do lie near it, the **correlated color temperature (CCT)** is used. The CCT of a light source, also expressed in Kelvins, is defined as the temperature of the blackbody source that is closest to the chromaticity of the source in the CIE 1960 UCS (u, v) system. CCT is an essential metric in the general lighting industry to specify the perceived color of fluorescent lights and other nonincandescent white-light sources such as LEDs and high intensity discharge HID lamps.

The difference in perceived color is closely related to the reciprocal of CCT. The reciprocal is expressed in reciprocal megakelvin (MK)-1, with one (MK)-1 approximately equal to a just-noticeable color difference:

$$(MK)^{-1} = 10^6 / CCT$$
.

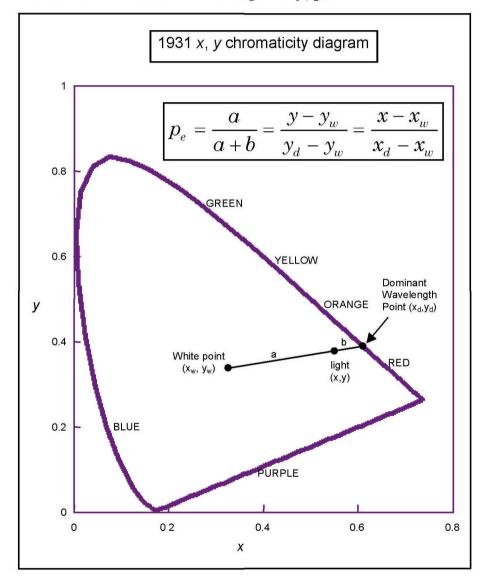
There are limitless different spectra, all with the same CCT, that may have little or no resemblance to the blackbody curve for that temperature or to each other.

There is no approved method for computing CCT nor is there a simple and accurate closed-form expression. One simple and accurate method is to use a program such as Excel with *solver* to find the blackbody temperature that minimizes the distance between its (u, v) coordinates and those of the light in question.

Color 15

#### **Dominant Wavelength and Purity**

Colored light sources can be modeled as a mixture of a monochromatic source and a white light. The wavelength of this theoretical monochromatic source is called the **dominant wavelength**,  $\lambda_d$ , and is the perceived color of the light. The percent of the total power provided by the monochromatic source is the **purity**,  $p_e$ .



The choice of the "white point" is arbitrary. Very often, the default choice is an "equal energy white" (x = 0.3333), y = 0.3333).

#### **Surface Color**

The color of a surface, like that of a light source, can be quantified. The **reflectance factor**,  $R(\lambda)$ , of the surface is combined with the spectral density of the illumination,  $S_{\lambda}$ , and the CIE color matching functions,  $\bar{x}$ ,  $\bar{y}$ , and  $\bar{z}$ , in the calculation of tristimulus values:

$$\begin{split} X &= k \int S_{\lambda}(\lambda) \cdot R(\lambda) \cdot \overline{x}(\lambda) \cdot d\lambda, \\ Y &= k \int S_{\lambda}(\lambda) \cdot R(\lambda) \cdot \overline{y}(\lambda) \cdot d\lambda, \\ Z &= k \int S_{\lambda}(\lambda) \cdot R(\lambda) \cdot \overline{z}(\lambda) \cdot d\lambda, \\ k &= \frac{100}{\int S_{\lambda}(\lambda) \cdot \overline{y}(\lambda) \cdot d\lambda}. \end{split}$$

Or, in summation form:

$$Y = k \sum_{\lambda=380}^{780} S_{\lambda}(\lambda) \ R(\lambda) \ \overline{y}(\lambda), \qquad \qquad X = k \sum_{\lambda=380}^{780} S_{\lambda}(\lambda) \ R(\lambda) \ \overline{x}(\lambda),$$

$$Z = k \sum_{\lambda=380}^{780} S_{\lambda}(\lambda) \; R(\lambda) \; \overline{z}(\lambda) \; , \qquad \quad k = 100 / \sum_{\lambda=380}^{780} S_{\lambda}(\lambda) \; \overline{y}(\lambda) \; .$$

The chromaticity of light sources is 2D, with the photometric value of luminous flux, illuminance, luminous intensity, or luminance playing the role of the third "dimension." However, the chromaticity of surfaces is 3D, with a "lightness" dimension included. Common 3D surface-color spaces are derived from the tristimulus values.

 $x,\,y,\,Y-{\rm CIE}$ 1931 chromaticity plus Ytristimulus value

$$L^*,a^*,b^*-CIE$$
 1976 ( $L^*a^*b^*$ ) color space; CIELAB

W\*U\*V\*- CIE 1964 uniform space coordinates (obsolete except for the calculation of color rendering index)

Color 17

#### Color of Fluorescent Surfaces

The phenomenon of **fluorescence** is characterized by the absorption of light at one wavelength and the nearly instantaneous emission at a longer wavelength. Various surfaces of interest in illumination systems, such as road signs designed to convert the blue-rich skylight at twilight to more visible yellow, also exhibit intentional fluorescent properties to make them brighter or more detectable.

The calculation of the chromaticity of fluorescent surfaces has a degree of complexity that is not present for nonfluorescent surfaces. For fluorescent surfaces, the reflectance factor  $R(\lambda)$  is replaced by the **Donaldson matrix**,  $D(\mu,\lambda)$ , where  $\mu$  is the absorbed or excitation wavelength, and  $\lambda$  is the emission wavelength:

$$\begin{split} X &= k \sum_{\lambda=380}^{780} \sum_{\mu=300}^{780} S_{\mu}(\mu) \ D(\mu, \lambda) \ \overline{x}(\lambda), \\ Y &= k \sum_{\lambda=380}^{780} \sum_{\mu=300}^{780} S_{\mu}(\mu) \ D(\mu, \lambda) \ \overline{y}(\lambda), \\ Z &= k \sum_{\lambda=380}^{780} \sum_{\mu=300}^{780} S_{\mu}(\mu) \ D(\mu, \lambda) \ \overline{z}(\lambda). \end{split}$$

Note that for nonfluorescent surfaces, the Donaldson matrix collapses to the reflectance factor for the diagonal elements ( $\mu = \lambda$ ), and is zero everywhere else.

The normalization constant, k, is the same as for non-fluorescent surfaces.

In fact, the reflectance factor can be thought of as a special case of the Donaldson matrix.

The details of computing the chromaticity of fluorescent surfaces can be found in ASTM Standard E2152-01, Standard Practice for Computing the Colors of Fluorescent Objects from Bispectral Photometric Data.

#### Color Rendering and CRI

The color of an object depends on both the object and the illuminating source. Some sources are better than others at rendering the colors of objects. This ability is quantified in a figure of merit called the color rendering index (CRI) for the source. The CRI is calculated by comparing chromaticity coordinates ofeight prescribed nonfluorescent test-color samples (specified by their spectral radiance factors) under the source being evaluated with the chromaticity coordinates of the same eight samples under a reference illuminant. The reference illuminant is a blackbody radiator (with the same CCT as the source) for sources with a CCT of less than 5000 K, and a phase of daylight (with the same CCT as the source) for sources with a CCT of 5000 K or higher. The distance between the two chromaticity coordinates for a particular test-color sample represents the color difference between the sample illuminated by the source being evaluated and the same sample illuminated by the reference illuminant. The general color rendering **index**, designated  $R_a$ , is the average distance (in  $W^*$ ,  $U^*$ , V\* space) between the eight pairs of chromaticity coordinates (a pair for each test-color sample). It is normalized so a source that is identical to its reference illuminant has a CRI of 100, and a "warm white" fluorescent lamp has a CRI of about 50. Here are examples of typical CRI values for several illuminating sources:

Sunlight (CIE D65)	100
Tungsten lamp (CIE A)	100
Xenon	97
White light LED (blue + YAG)	83
Compact fluorescent lamp	80
Daylight fluorescent	75
Metal halide lamp	61
Warm white fluorescent	52
High-pressure sodium lamp	20
White light from RGB LED combination	20 to 65
White light from four LED combination	up to 90

Color 19

#### Calculating CRI and Problems with CRI

Complete details for calculating **CRI** are beyond the scope of this guide. The information is available in two CIE publications (both are necessary):

- CIE 13.3-1995, Method of Measuring and Specifying Color Rendering Properties of Light Sources
- CIE Publication 15:2004, Colorimetry, 3rd Edition

With these publications comes a software disk for calculating CRI from a light source spectral density. The publications and disk can be purchased from the CIE at www.cie.co.at/cie/index.html.

Work on the CRI began in the 1940s when widespread use of fluorescent tubes began for general lighting. The figure of merit has come under criticism lately for several reasons. Among them:

- The eight test-color samples are all moderate in saturation. CRI does not produce numbers that correspond well with observations on highly saturated colors.
- The CRI is considered to be less accurate when the test illuminant and the reference illuminant differ by more than 0.0054 (in *u*, *v* space). Many real illuminants are farther away than this from their respective reference illuminants.
- Many different illuminants, such as sunlight and tungsten lamps, have "perfect" CRIs near 100, yet they render colors quite differently.
- New white light sources, such as combinations of LEDs, seem to perceptually render colors far better than is predicted by their rather low CRIs.

The CIE is expected to issue a new recommendation for quantifying color rendering within the next several years.

#### **Typical Source Parameters**

Spectral densities for several common light sources are displayed on the following pages. The table below lists some of the relevant parameters for these sources.

Typical values for common illumination sources			
Source	Approx. CCT (K)	CRI (R <sub>a</sub> )	Luminous Efficacy (lm/W)
Tungsten <sup>†</sup>	2800 to 3200	100	12 to 20
Sunlight	6500	100	$100^{\ddagger}$
Daylight fluorescent	6360	75	55
Warm white fluorescent	3000	52	60
High-pressure sodium	2030	20	115
Metal halide	4020	61	90
Xenon	5000 to 6000	97	10 to 20

<sup>&</sup>lt;sup>†</sup> Tungsten lamps allow a great deal of control over these parameters. Guidelines for controlling tungsten lamps are detailed on the next page.

LEDs are becoming common illumination sources. They produce white light by using a blue LED and one or more phosphors. Depending on the phosphor used, they can have CCTs from less than 3000 K to in excess of 9000 K. The luminous efficacies also vary over a wide range, from 40 or 50 lm/W for high-flux devices and up to and above 100 lm/W for low-flux devices, with CRIs up to about 80 ( $R_a$ ). White light is also produced from LEDs by mixing the light from several single-color LEDs. LED lighting technology is changing extremely rapidly as newer devices are developed.

<sup>‡</sup> Lumens per radiated watt. All others are "wall-plug."

#### **Tungsten Lamps**

Tungsten filament incandescent lamps, particularly tungsten halogen lamps, are often used in illumination systems. Paired with stable, current-controlled power supplies, they provide extremely stable sources. If the current is altered, the filament temperature changes, with a resulting change in filament resistance. Therefore, the voltage change is not linearly related to the current change. Similar nonlinear relationships hold for other characteristics of the lamp, such as power consumed, luminous flux output, efficacy (lumens/Watt), color temperature, and lifetime.

Tungsten halogen lamps should be operated between 95% and 105% of their rated current. Within this operating envelope, the relationships between the operating parameters are approximately exponential. Modifying the current to a value different from the rated current changes the other parameters according to the exponents shown in the table below:

Parameter	Exponent
Color temperature (K)	0.80
Lifetime (hours)	-25
Luminous efficacy	3.6
(lumens/Watt)	
Luminous flux (lumens)	6.5
Power (Watts)	2.9
Voltage (volts)	1.9

An example of a lamp operated at 5% over its rated current is shown below:

Parameter	Rated	Operated
Current	6.02 A	$6.02 \times 1.05 = 6.32$
Color temperature	$2900~\mathrm{K}$	$2900 \times 1.05^{08} = 3015$
Lifetime	$1000~\mathrm{hrs}$	$1000 \times 1.05^{-25} = 295$
Luminous efficacy	16 lm/W	$16 \times 1.05^{36} = 19$
Luminous flux	1040 lm	$1040 \times 1.05^{6} = 1428$
Power	$65~\mathrm{W}$	$65 \times 1.05^{29} = 75$
Voltage	10.8 V	$10.8 \times 1.05^{19} = 11.8$