

## Software Modeling Discussion

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Outside the laboratory, software programs are used to model, optimize, and tolerance optical systems. Two types of codes exist in the optical design arena: **lens design codes** and **optics analysis codes**. The former are used primarily to design the lenses used in optical systems. They include robust analysis tools such as point spread function graphs, spot diagrams, and modular transfer function curves; optimization tools to improve upon the performance of the imaging system; and tolerancing tools to ensure manufacturability. Increasingly, these lens design codes include **nonsequential ray tracing**. Nonsequential ray tracing is required for a number of illumination systems, especially those based on nonimaging optics. In standard lens design, rays follow a prescribed sequence of optical interfaces. Thus, the traced rays know the sequence of surface intercepts, which reduces the computation load since the algorithm does not need to determine which surface is struck next by a ray.

Optics analysis codes are based around nonsequential ray tracing such that computation time must be spent to determine which surfaces are struck by each ray. Nonsequential ray tracing is inherently slower than sequential ray tracing. Analysis codes are further broken down into two geometry types: **surface-based geometry** and **solid-based geometry**. Surface-based codes require the user to generate each surface, assigning the optical properties on the two sides of each interface. Solid-based codes develop enclosed objects that allow the user to assign volume-based properties such as the type of material (e.g., BK7) and surface-based properties (e.g., a silver mirror).

Optical design codes incorporate more **computer-aided design (CAD)** into their capabilities. This feature allows the codes to import mechanical design formats such as IGES and STEP. Certain industries such as the automotive and architectural industries have specialized codes. The list of codes is extensive and always changing.

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## Role of Light in Architecture

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The illumination of buildings is a design process aimed at orchestrating light for the user's well-being. The layering and patterning of light is considered successful when complex physiological and psychological responses are satisfied. Such responses are centrally conditioned by vision: the medium through which information and perceptions about a given space are recorded and interpreted. Economics and energy efficiency play a critical role in design decisions, but the satisfaction of vision requirements is of overriding importance.

The characteristic features of an architectural space only come to life with light. Hence, no light no architecture. At the same time, light is not neutral: The way it is arranged gives a particular appreciation of the space and generates specific emotive and aesthetic responses.

The electric illumination of an architectural space is simply the result of transmitted or reflected light emanating from distant and immediate surrounding surfaces. Therefore, the lighting designer can influence the interface between light and matter to meet these visual requirements and sensations. Hence, only with a proper understanding of physiological and psychological factors and a familiarity with available technologies can lighting decisions be made for proper effect.

Despite some setbacks in the 1970s caused by an advocacy for windowless buildings to save energy, light available from the sun and sky has regained the attention of lighting designers for the many benefits it brings to users. When available and well controlled, daylight is by far the preferred source of illumination. Today, the common design approach combines the contribution of both electric and natural lights for increased work productivity, and reduced absenteeism or visual fatigue.

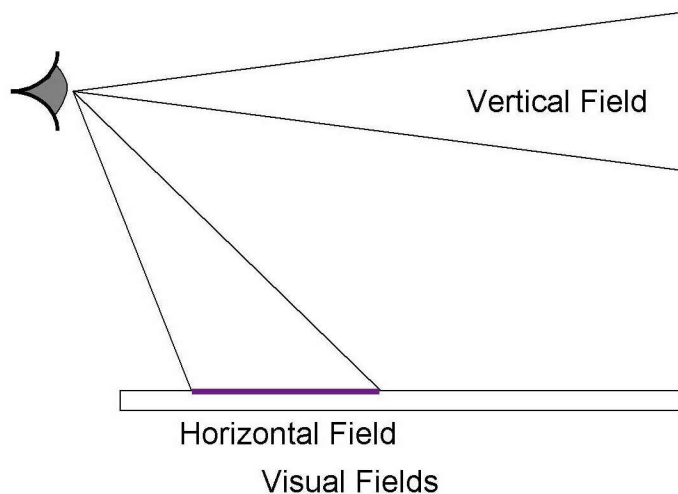
## Eye Adaptation and Visual Fields

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**Eye adaptation** to the visual environment is the eye's response and sensitivity to the ambient light level as the person moves from one environment to the next, such as walking from the bright and sunny outdoors to the dark indoors. If the difference between the two light levels is extreme, the person may feel like he or she has moved into a totally black environment. Slowly, the sensitivity of the eye attunes itself to the dark environment and details become increasingly distinguished. It takes 20 to 30 minutes for the eyes to completely adapt to a dark environment and grasp the details. Conversely, eyes adapt to a sunny environment in 2 to 3 minutes.

**Transient adaptation** is the ability of the visual system to adapt in short intervals to the different luminances prevailing in a fixed visual field, for instance, when looking through a bright window and down to a desk. Due to such variations, the iris constantly adjusts the aperture to control the light entering the eye. Large variations between luminances in a scene are considered detrimental to visual comfort and lead to eye fatigue.

**Visual fields** refer to the direction of the eyes' line of sight. When looking down, the viewer apprehends a **horizontal field**, and when looking up, a **vertical field**.

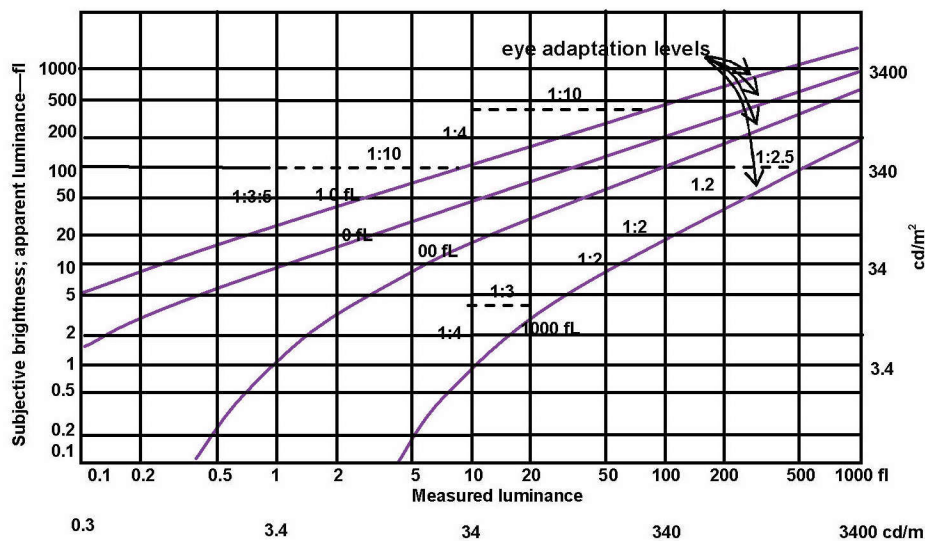




## Apparent Brightness

Vision is stimulated by brightness mapped on the retina as a byproduct of light reflected from an opaque surface or transmitted through a transparent medium (the glass bulb of a lamp, for example). A distinction must be made, however, between **photometric brightness** or luminance and **apparent brightness**. Luminance or photometric brightness is calibrated in relation to the eye's sensitivity to various wavelengths, while apparent brightness is perceived in the context of the ambient light level to which the eye is adapted. Hence, the brightness of an object relative to the retinal image is by no means a complete specification of its visual appearance. This may be understood by considering the blinding brightness of a car's headlights during the night that is barely perceivable during the day, even though a light meter will register the same photometric brightness.

At an ambient surrounding of 3.4 cd/m<sup>2</sup> (1 fL), a measured luminance of 34 cd/m<sup>2</sup> (10 fL) appears to be 340 cd/m<sup>2</sup> (100 fL). At a low ambient level, the difference perceived between two surfaces is also reduced from a difference of 1:10 to 1:4.



Subjective brightness versus measured luminance. (Reprinted with permission from Stein and Reynolds, copyright Wiley & Sons, 2005.)



## Lighting Design—Layering of Light

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For both energy conservation and visual variety, lighting design is implemented in layers to properly distribute light throughout the architectural space.

The **horizontal ambient layer** is maintained to 1/3 to 2/3 the task illumination level. Lower bound levels (1/3) for horizontal ambient light may be appropriate for a museum or boutique store to emphasize a display. Upper bound levels (2/3) are more relaxing for most casual activities where a 25- to 35-fc ambient light level is sufficient and relates well to tasks requiring 50 to 60 fc.

The **vertical ambient layer** is critical in keeping vertical tasks glare free, such as washout of video display terminals (VDTs). In addition, when people look away from a task, the line of sight is then the vertical average luminance from the walls and ceiling. **Wall washing** and **grazing** are some of the techniques used to reinforce the sensation of spaciousness, clarity, and pleasantness.

A **task layer** supplements the ambient illumination to fulfill lighting requirements for critical activities. Energy is saved by (1) locating the source near the task to provide the light level recommended by the Illuminating Engineering Society of North America (IESNA), (2) reducing ambient light levels, and (3) turning off the task light when not in use. The scene presents varied lighting instead of the monotonous atmosphere, resulting from the **general illumination approach**.

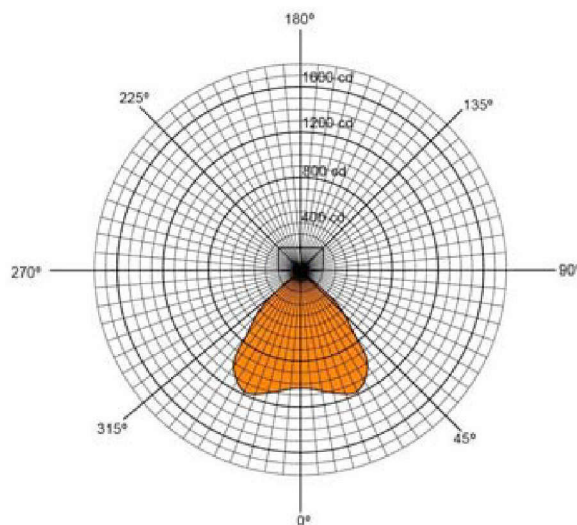
The **accent** or **focal layer** gives the space its identity and mood by highlighting or spotlighting certain architectural elements and objects, such as paintings, sculptures, and landscapes. **Downlighting**, **accent lighting**, and **backlighting** are some techniques used to produce such effects on various elements in the space.

The **ornamental layer** introduces elements that add sparkle to the space with effects similar to those of Christmas lights. Chandeliers, candles, and sconces can be considered for this purpose.

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## Photometric Report and VCP

Manufacturers provide a **photometric report** that details the optical performance and characteristic light distribution patterns of a luminaire. The **candela distribution curve (CDC)**, presented in either polar (figure below) or rectilinear plots and in tables, shows the luminous intensity distribution measured at different angles, from 0 to 360 deg in increments of 5 deg. Using the plot below, the luminous intensity can be found for a specific direction. Rectangular luminaires (2 x 4 or 1 x 4) require candela distribution curves in at least three planes: crosswise, longitudinal, and 45 deg. These luminous intensities can quickly reveal the potential for glare.



Candela distribution curve.

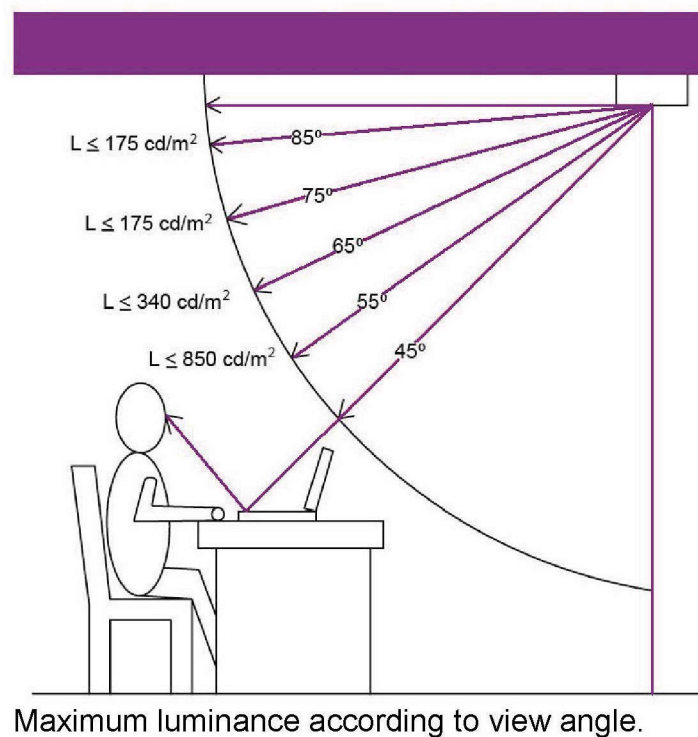
The **visual comfort probability (VCP)**, a rating system for evaluating direct discomfort glare, is expressed as the percent of occupants of a space who will be bothered by direct glare. Standard data provided for a luminaire specification include tables of its VCP ratings for various room geometries, based on IESNA standard conditions. These include a uniformly distributed illumination level of 1000 lux (~100 fc), luminaire height, observer position, and room surface reflectances (ceiling, 80%; walls, 50%; and floor, 20%). In general, a minimum VCP of 70 is the established limit for the viable use of a luminaire.

## The Layered Approach

**Spacing criteria (SC)** to achieve uniform ambient illumination is the ratio of the spacing (S) distance between the respective axis of parallel luminaires and their mounting height (MH), i.e.,  $SC = S/MH$ . For a rectangular luminaire, SC is given along both axes, lengthwise and crosswise. The distance between walls and adjacent light fixtures is set at no more than one-half S.

The **coefficient of utilization (CU)** specifies the proportion of lumens that reach the workplane from the fixture for given room geometries and surface reflectances. The CU gives some indication of the luminaire's efficiency.

When located in the field of view, bright light sources can cause discomfort and disability glare. However, the severity of glare depends on the angle at which the luminaire is seen. The *IESNA Handbook* provides as maxima the following **luminances from a direct luminaire** according to the view or cut-off angle:



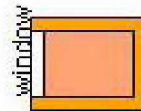


## Daylight Factor

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Windows and skylights admit daylight as free illumination, and the viewers have visual contact with the outside. However, only a portion of outdoor light is received inside a building. The sky's condition, along with the size, placement, and orientation of the window(s) opening, the glazing type and transmittance, and shading as well as room proportions, affect the quantity and quality of received light.

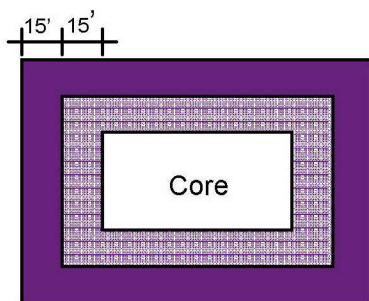
The **daylight factor (DF)** accounts for these parameters and is used to determine the percentage of outside light that can be received inside a room with a specific configuration. DF is the ratio of interior illuminance at a given point on a given plane (usually the work plane) to the exterior illuminance under minimal light conditions of an overcast sky, e.g., the CIE overcast sky distribution. For parallelepipedic-room buildings with windows on one side only, a minimum DF of 2% is generally recommended throughout the work plane.



The DF general equation is

$$DF = E_i/E_o,$$

where  $E_i$  and  $E_o$  are the indoor and outdoor horizontal illuminances, respectively.



Daylight should be allowed to reach through side windows for the tasks performed at the rear of the space. Shelves in side windows can help reflect light deep into interior spaces and shade the vision portion of the window.

Office tasks can be lit at a depth of up to 15 feet from the window. The next 15 feet may need to be supplemented by electric light. Beyond 30 feet, little or no daylight is available unless the space has windows on opposite sides. Evenly distributed roof skylights provide uniform light but for one story only, assuming proper glazing transmittance and sunlight control.

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## Daylight Strategies

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IESNA RP-5-99 Recommended Practice of **daylighting** emphasizes the following illumination practices:

1. Block direct sunlight in the vicinity of tasks. Blocking direct sunlight at the window (e.g., with louvers) is the first step toward glare control by allowing only light from the sky and that reflected from the ground to pass through the window glass.
  2. Design windows to minimize direct glare. East, west, or south facing windows can have too much glare if excessive sunlight strikes the glass. With 100,000 lux of light available on the outside on a sunny day, a glass pane, with typically only 2% transmittance, can reach a luminance up to 2000 cd/m<sup>2</sup>, which exceeds the tolerated average of 850 cd/m<sup>2</sup>. Internal blinds (structurally stable external shading devices with adjustable louvers) can block direct sunlight and reduce the luminance of the window or skylight. And glazing that has a visible light transmittance of 25% can be an acceptable trade-off of daylight availability, the view to the outside, and minimize glare.
  3. Zone electric lighting for daylight responsive control. The electric light distribution system should be zoned according to daylight availability inside an open-plan office. Daylight zoning depends on the room configuration, sky condition, and solar exposure. Large open-plan offices are often subdivided into the perimeter zones, the intermediate zone, and the core zones based on daylight availability as indicated in item 1.
  4. Provide responsive lighting controls. Controls are at the heart of efficient electric light operation and daylight harvesting, specifically to accommodate the time-dependent electric light demand. The variables governing control strategies include the space layout, configuration, orientation, the occupancy patterns, lighting usage, and daylight availability. Controls include tuning to reduce electric power while still meeting each user's needs, and adaptive compensation to lower the light levels at night.
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## Nighttime Visibility Criteria

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The eye is capable of adapting to a wide range of light levels but not at the same time. To function well, it must be adapted to the prevailing light conditions. As previously indicated for daytime conditions, our eyes use **photopic vision**, which utilizes the eye's cones and the center of the visual field. The eye works differently when it is adapted to low light levels. Under very dark, moonlit conditions, our eyes use **scotopic vision**, which primarily utilizes the eye's rods, resulting in greater acuity in the peripheral visual field.

For **nighttime visibility** in most urban and suburban environments, our eyes use **mesopic vision**, which is a combination of both photopic and scotopic. In nighttime environments, the goal of the lighting design is to keep the eye adapted to mesopic or scotopic vision, and not to introduce high light levels that will create an imbalance in the visual field and cause the eye to try to use photopic vision. Recent research indicates that light sources rich in blue and green (metal halide or fluorescent) improve peripheral mesopic vision, clarity, and depth of field better than sources rich in red and yellow, such as incandescent and high-pressure sodium.

Extreme **glare** leads to loss of visibility. Glare is caused by a high luminance ratio between the glare source and the prevailing light conditions to which the eye is adapted. In other words, insufficiently shielded light sources generate direct glare. The following measures reduce the luminance ratio and control nighttime glare:

- **Uniform light distribution** in a visual scene and brightness ratios kept to 1:5 between average and maximum luminance;
  - **Reduction of light levels** and **source brightness** using fixtures with low wattage;
  - **Shielding the light source** and **locating fixtures** to avoid glare. Fixtures near the property line should have "house-side shielding" to prevent glare to residential neighbors.
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### Recommended Illuminance for Façades

**Façade illumination** aims to reproduce at night a building's aesthetic and formal characteristics that are perceived during the day for the purpose of attracting attention and creating a good impression. To this effect, **floodlighting** is one technique employed, which treats a building as a giant piece of sculpture for visual display. Luminaires are typically mounted in close proximity to buildings and are aimed to illuminate the structure. Lighting the building from the top down reduces stray uplight, and precisely aimed fixtures minimize trespass light.

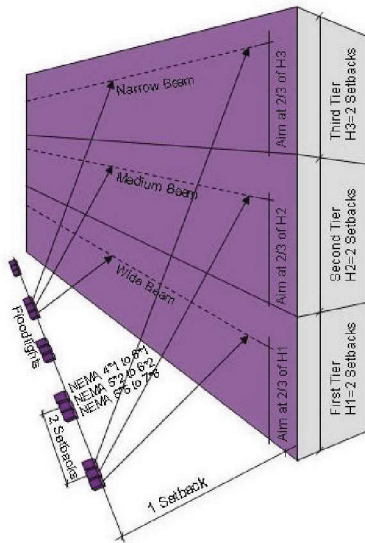
Effective illumination of facades is a complex and subjective task. Results depend heavily upon surrounding light levels, the surface finish of the intended target, the spectral color distribution of the lamp source, mounting location allowances, and viewers' perceptions.

The following table lists the IESNA's recommended illuminance levels for the floodlighting of buildings and monuments.

Area Description	Target Surface Finish	Average Target Illuminance
Bright	Light	5 (50)
Bright	Medium light	7(70)
Bright	Dark	10(100)
Dark	Light	2(20)
Dark	Medium light	3(30)
Dark	Medium dark	4(40)
Dark	Dark	5(50)

Adapted from *IESNA Hand-book*, 9<sup>th</sup> Edition, copyright IESNA, 2000.

## Façade Floodlighting for Uniform Illumination



Adapted from *IESNA Handbook*, 9<sup>th</sup> Edition, copyright IESNA, 2000.

(IESNA RP-33). The further away the luminaire is from the facade, the narrower the light beam must be. Aiming and positioning ground-mounted floodlights for uniform illumination depend first on the available **setback** in relation to the building height. If the height is 2 times the setback dimension, the center of a “wide beam” floodlight aimed at  $2/3$  the height of the building is recommended. If a building is 30 feet high, the recommended aiming point is 20 feet high. Floodlight **spacing** along the facade should not exceed 2 times the setback distance. If the setback is 22.5 feet, the floodlights should be placed no more than 45 feet apart, with the first floodlight at  $1/2$  to 1 of the setback dimension. As the building height increases to 4 times the setback, a medium-beam floodlight with the same aiming elevation is recommended. Buildings with up to 6 times the setback require more narrow-beam floodlights. Thus, one location on the ground may hold multiple floodlights, each aimed at different building elevations. The illumination from the ground of façades with more than 6 times the setback is not recommended due to the difficulty of achieving uniformity.

**Floodlighting** fixtures can be mounted at ground level, or on stands and poles. They can also be attached to the building itself or to adjacent structures. The key lights are set up for a modeling effect but should be combined with other color sources to soften the strong effects of shadows.

Floodlight categories are **narrow beam** (types 1, 2, 3), **medium beam** (types 4, 5) and **wide beam** (types 6, 7)

## Illumination of Outdoor Areas

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Lighting **building entries** at night provides (1) vertical illumination to comfortably light people's faces, and (2) horizontal illumination to light the pathway and any changes in the light level. Such a pool of light comes from a mounting position high on the building, on a pedestrian-scaled post lantern, or on the underside of a canopy.

**Emergency egress doors** are provided with lighting on the outside of the door threshold and extended for a distance at least equal to the width of the door opening.

**Softscape lighting** is for private yards, patios, parks, gardens, boulevards, entry markers, and other natural features such as water. They are softly illuminated and emit a minimum of glare, contrast, or spill light to the neighbors. Some techniques used to light trees to achieve the desired effect are **frontlighting** to highlight details, texture, and color; **backlighting** to show form and separate the plant from the background; **sidelighting** to emphasize plant texture and create shadows; **uplighting** to make branches glow; and **downlighting** for accent details, colors, and texture. The illumination of tree trunks along with canopies helps anchor them to the landscape.

**Hardscape lighting** is for outdoor sculptures, fountains, or vertical displays. A 3D sculpture is illuminated from two directions to provide highlights and soften shadows. The key light is focused on the mass of the sculpture with light added to relieve shadows.

**Stairs** and **ramps** are hazardous in low light, so contrast is essential for their safe use. Illuminated handrails, step lights, or small fixtures in the balustrade provide light differentiation between the step risers and threads. Other techniques to complement light effects are coloring of the step nosing and color differentiation between threads and risers.

**Walkways, sidewalks, and bikeways** are illuminated at levels recommended by the IESNA with lights placed to provide visual information.

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### Special Considerations for Outdoor Fixtures

**Controls** using astronomical time switches and/or photosensors are deployed to ensure that exterior lighting is not operated when sufficient daylight is available or during nighttime except those fixtures for security.

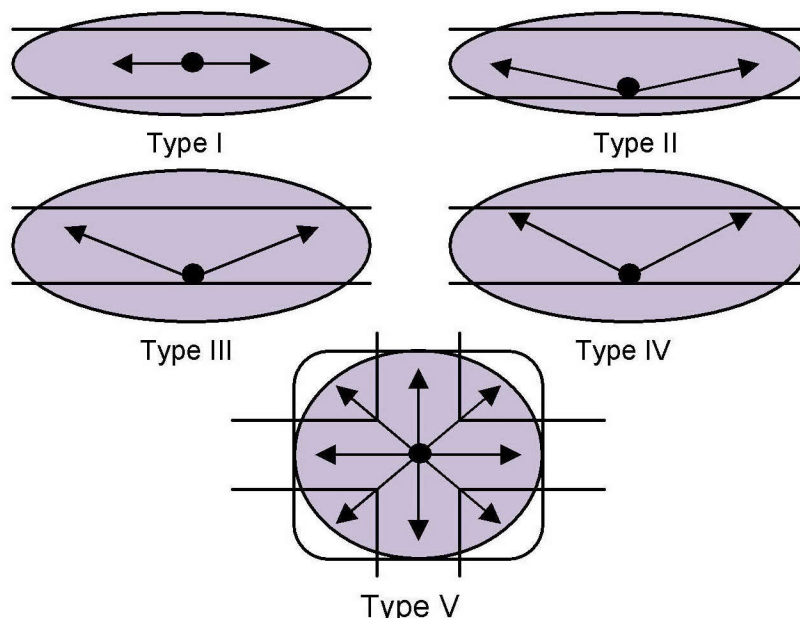
Special considerations must be given to proper installation of luminaires exposed to the outdoor environment. If installed on ground they must have the “**wet location rated**” label and if placed under canopies but still exposed to the elements, they must be “**damp location rated.**” In addition, durable with vandal-resistant components and regularly maintained luminaires to minimize dirt accumulation or to prevent obstruction by grass, leaves, mud, and other debris, ensure steady operation of exterior lighting. Separate security fixtures are exclusively used to provide low light levels for security cameras (.01 footcandle). The table below summarizes the illuminance and luminance ratios for various outdoor areas.

Outdoor space type	Horiz. Avg. Illuminance (fc)	Vert. Avg. Illuminance (fc)	Lum. Ratio
Building entrance (Active/Inactive)	5.0 / 3.0	3.0 / 3.0	
Emergency lighting: Egress Path	1		
Roadside sidewalks & Type A bikeways: commercial, intermediate, residential areas	1; 0.6; 0.2	2.2; 1.1; 0.5	4:1 to 5:1
Walkways distant from roadside & Type B bikeways	0.5	0.5	4:1 to 5:1
General parking and pedestrian areas	3.6; 2.4; 0.8		4:1 to 5:1
Loading docks	10	3	
Storage yards, active-inactive	10	3	

(Adapted from *IESNA Hand-book*, 9<sup>th</sup> Edition, copyright IESNA, 2000.)

## Outdoor Luminaire—Transverse Light Distribution

Luminaires' **beam pattern distributions** are classified by IESNA according to transverse and lateral projections. (see the next two figures). Five types, shown below, are illustrated according to the maximum candlepower and the trace of the half-maximum value. A **luminaire's transverse reach** is expressed in MH units: **type I** (1 MH), **type II** (1.75 MH), **type III** (2.75 MH), **type IV** (6 MH), and **type V** (symmetric distribution in four quadrants). Type V is usually best at the center of parking lots. Type IV or forward-throw distribution is best for wide, multilane roads and parking lot perimeters. Type I has a long and narrow distribution that can be applied to narrow roadways, walkways, or bike paths. It also can be located at or near the center of a pathway, approximately two MHs in width, or used as overhead lighting in areas such as parking lots, plazas, courtyards, and along walkways. Types II and III distribute light to one side of the light source. These luminaires should generally be used for street lighting to direct light to the street side of the lamp but not shining into the building side.

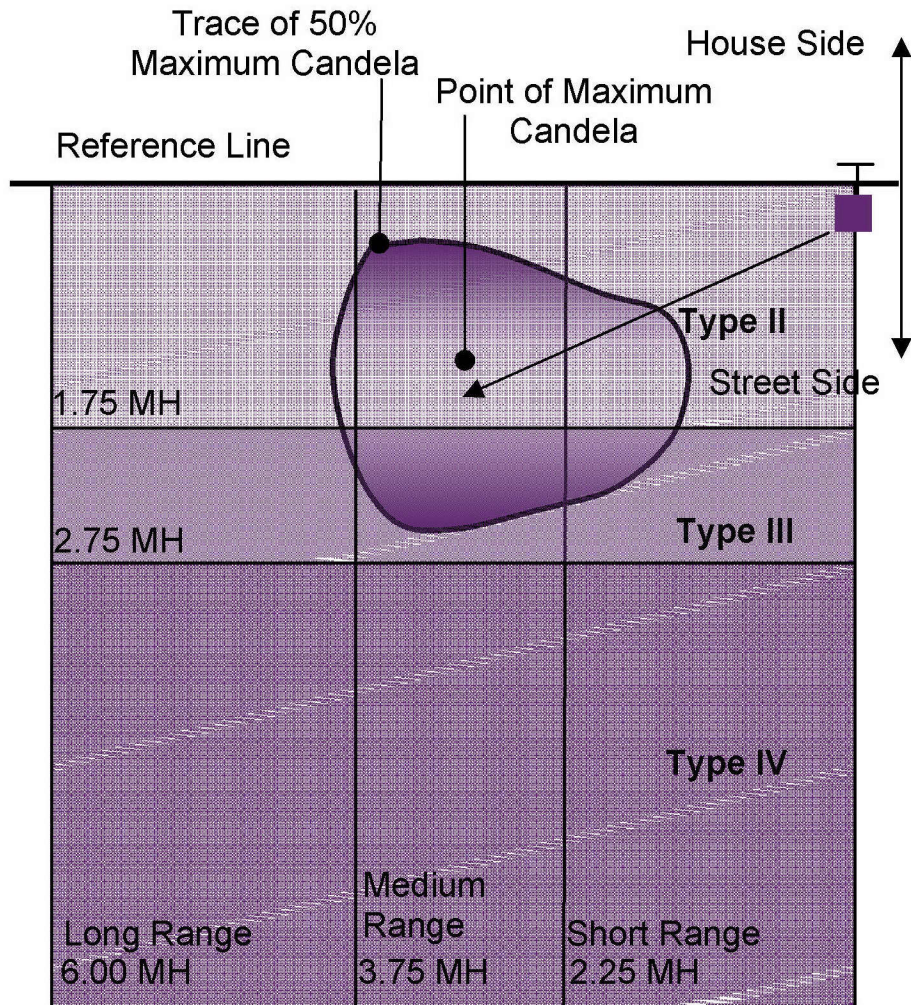


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### Outdoor Luminaire—Lateral Light Distribution

Fixtures for roadway and parking applications are further classified as **short**, **medium**, or **long lateral distribution**. This classification relates the types of fixtures, the spacing between them according to the point of maximum candelas, and the MH. For a short-range lateral throw, the maximum luminaire spacing is generally less than 4.5 times the MH. A medium throw allows a maximum spacing of generally less than 7.5 times the MH, and a long throw is generally less than 12 times the MH (see figure below).



Type III distribution of a luminaire. Half-maximum candelas trace falls within 2.75MH. (Adapted from *IESNA Handbook*, 9<sup>th</sup> Edition, copyright IESNA, 2000.)



## Criteria For Roadway Lighting

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Three principal criteria are used to design major roadway lighting systems: **luminance**, **illuminance**, and the newer concept of **small target visibility (STV)**. The illuminance **inverse square law calculations** are well known. It was found, however, that illuminance levels do not correlate well with visibility or driver performance. IESNA Standard RP-8-00 addresses one shortcoming of the illuminance method by adding a maximum **veiling luminance ratio (VLR)** that is specifically intended to limit glare from a luminaire. The luminance determination is necessary to calculate the VLR. Luminance describes the reflected light from the pavement as seen when driving, so evaluating the quality of a lighting system by how it looks at night is actually the same as evaluating its luminance.

In reference to the figure on the next page, luminance at point  $P$  is determined as the sum of contributions from all  $n$  luminaires:

$$L_P = \sum r(\beta_i, \gamma_i) I(\phi_i, \gamma_i) / 10,000 \text{ h}^2,$$

where  $r$  is the **reflectance coefficient** at angles  $\beta$  and  $\gamma$ .

The veiling luminance,  $L_v$ , and the VLR are also necessary to limit the glare effect. The  $L_v$  can be determined as follows:

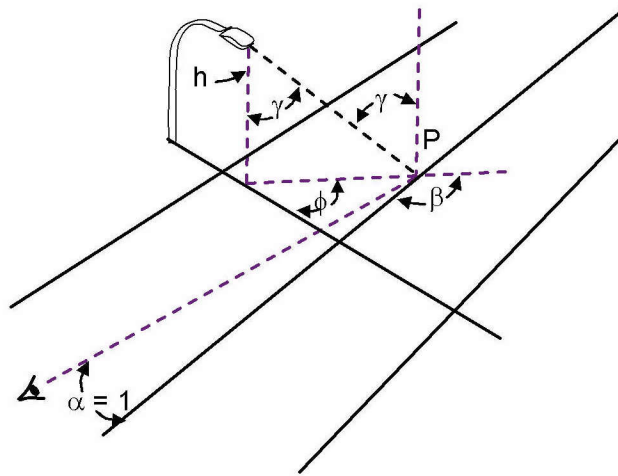
$$L_v = \sum 10 E_v / (\theta^2 + 1.5 \theta),$$

where:  $L_v$  is the veiling luminance at the observer's location, in  $\text{cd}/\text{m}^2$ ;  $E_v$  is the vertical illuminance on the plane of the observer's eye; and  $\theta$  is the angle between the line of sight and the luminaires in degrees.

Values recommended for luminance and VLR are found in the 9<sup>th</sup> Edition of the *IESNA Handbook*.

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### Small Target Visibility



Single fixture for luminance determination. (Adapted from *IESNA Hand-book*, 9<sup>th</sup> Edition, copyright IESNA, 2000.)

The **STV** method was developed to account for the contrast that must be present to allow drivers moving at high speed to quickly detect hazards and react to them. Indeed, a roadway lighting system may provide a high and uniform road surface luminance, yet the visibility threshold may be low due to the absence of contrast. Three luminance components influence the visibility of a target: the target luminance itself, the luminance of the background, and the veiling luminance or glare. Given these three luminances, all of which can be calculated, the visibility of each target in the array can be determined in terms of the **visibility level (VL)**. VL is the ratio of target contrast to the contrast of a similar target at threshold, a measure of visibility that has been widely used.

STV predicts the visibility of a standard object (18 × 18 cm) located on the roadway at a specific distance from the driver, and accounts for the contrast between the standard target and its background by considering the driver's age, viewing time, pavement reflectance, and glare from the luminaire. The larger the STV number, the more visible the object. For more details, go to IESNA RP-8-00.

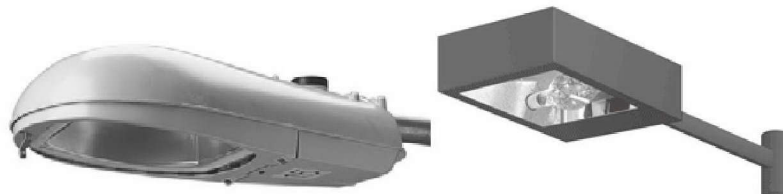
## Recommended Roadway Luminaires

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After the desired minimum illuminance and the pole height are initially set based on light spill, road cross-section, pavement type, and roadway category (*IESNA Handbook*), a few luminaires and sources can be tested to achieve a design that meets the recommended light level, uniformity, and acceptable glare. Common layouts include luminaires on one side of the road, luminaires on both sides, or luminaires in a center median. One-side and median configurations often have the additional advantage of requiring less wire and conduit, resulting in lower construction costs.

Starting with any of the five previously described types of luminaires is a convenient way to facilitate selection according to roadway width and light spill control. **Full cutoff** luminaires should be specified wherever possible to prevent light pollution. Typically, Types I, II, and III are appropriate for narrow roadways, while type IV is proper for multilane roads. Lateral-medium-throw luminaires are preferred over short-throw types because fewer poles are required and over long-throw types because then **semicutoffs** are not needed. Combining transversal and longitudinal distributions helps the designer select luminaires for even light distribution based on roadway widths and pole spacing.

The architecture of such luminaires comes in many shapes. Two are shown below. The most prevalent is the “**cobra head**” luminaire, typically mounted on a 6-ft arm. This fixture with a flat lens is recommended to minimize disability glare and light trespass. Reflectors may be formed or faceted aluminum. The **rectilinear “shoebox”** luminaire, designed as a full cutoff, is also popular. The reflector in this design is usually larger than that in a cobra head to achieve better optical control.



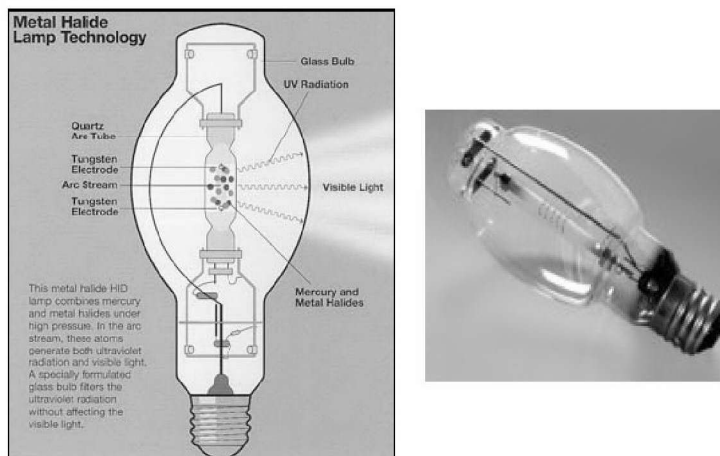
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## Recommended Lamps for Roadway Luminaires

**Metal halide, high-pressure sodium, and induction lamps** are the most common lamps, ranging from 100 to 400 W depending on the MH and roadway cross-section. Metal halide is used where color rendition is a concern or white light is desired, but this lamp also emits light in the blue-green portion of the spectrum, which enhances the driver's peripheral vision. A **light-loss factor (LLF)** accounts for the depreciation in lamp output and luminaire performance over time. Typical LLFs are 0.60 to 0.70 for **high-pressure sodium** lamps and 0.45 to 0.55 for **metal halide lamps**. Note that the LLF varies depending on environmental conditions and maintenance procedures.



Left: metal halide lamp. Above: 400W high pressure sodium BT-37. (Images reprinted with permission from Sylvania.)

The isofotcandle procedure, not covered here, can be used to determine luminaire spacing based on needed illuminance and uniformity. With the help of software programs, many iterations can be performed quickly to compare various lighting systems and determine the safest and most efficient solution.

## Equation Summary

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### Basic Quantities in Illumination

$$\text{photopic luminous flux} = 683 \int \Phi_{\lambda}(\lambda) \cdot V(\lambda) \cdot d\lambda$$

### Color

#### Light source color:

$$X = \int S_{\lambda}(\lambda) \cdot \bar{x}(\lambda) \cdot d\lambda \qquad x = \frac{X}{X + Y + Z}$$

$$Y = \int S_{\lambda}(\lambda) \cdot \bar{y}(\lambda) \cdot d\lambda \qquad y = \frac{Y}{X + Y + Z}$$

$$Z = \int S_{\lambda}(\lambda) \cdot \bar{z}(\lambda) \cdot d\lambda$$

$$u = 4X/(X + 15Y + 3Z) = 4x/(-2x + 12y + 3)$$

$$v = 6Y/(X + 15Y + 3Z) = 6y/(-2x + 12y + 3)$$

$$u' = 4X/(X + 15Y + 3Z) = 4x/(-2x + 12y + 3)$$

$$v' = 9Y/(X + 15Y + 3Z) = 9y/(-2x + 12y + 3)$$

#### Color temperature and CCT:

$$(MK)^{-1} = 10^6 / CCT$$

#### Surface color:

$$X = k \int S_{\lambda}(\lambda) \cdot R(\lambda) \cdot \bar{x}(\lambda) \cdot d\lambda$$

$$Y = k \int S_{\lambda}(\lambda) \cdot R(\lambda) \cdot \bar{y}(\lambda) \cdot d\lambda$$

$$Z = k \int S_{\lambda}(\lambda) \cdot R(\lambda) \cdot \bar{z}(\lambda) \cdot d\lambda$$

$$k = \frac{100}{\int S_{\lambda}(\lambda) \cdot \bar{y}(\lambda) \cdot d\lambda}$$


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### Equation Summary (cont.)

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#### Color of fluorescent surfaces:

$$X = k \sum_{\lambda=380}^{780} \sum_{\mu=300}^{780} S_{\mu}(\mu) D(\mu, \lambda) \bar{x}(\lambda)$$

$$Y = k \sum_{\lambda=380}^{780} \sum_{\mu=300}^{780} S_{\mu}(\mu) D(\mu, \lambda) \bar{y}(\lambda)$$

$$Z = k \sum_{\lambda=380}^{780} \sum_{\mu=300}^{780} S_{\mu}(\mu) D(\mu, \lambda) \bar{z}(\lambda)$$

$$k = 100 / \sum_{\lambda=380}^{780} S_{\lambda}(\lambda) \bar{y}(\lambda)$$

#### *Illumination Properties of Materials*

##### BRDF and reflectance factor:

$$\text{BRDF} = L/E \quad R = \text{BRDF} \cdot \pi$$

##### Harvey/ABg scatter model:

$$B = |\beta_{\text{rolloff}}|^g \quad \text{BSDF} = \frac{A}{B + |\beta - \beta_0|^g}$$

##### Retroreflectors:

$$R_I = \frac{I}{E_{\perp}} \quad R_A = \frac{R_I}{A} \quad R_L = \frac{R_A}{\cos v} = \frac{L}{E_{\perp}}$$

#### *Illumination Transfer*

##### Known intensity:

$$E = \frac{I \cos \xi}{d^2} \quad \Phi_i = I \omega \quad L = \frac{I}{A_r \cos \theta}$$


---



### Equation Summary (cont.)

---

**Known flux:**

$$I = \Phi_i / \omega \quad E = \Phi_i / A_i \quad L = \frac{\Phi_i}{\omega A_r \cos \theta} = \frac{\Phi_i}{\Omega A_r}$$

**Known radiance:**

$$E_0 = \frac{\Phi_i}{A_i} = \frac{L A_r \Omega}{A_i} = \frac{L A_r \cos \theta \cos \xi}{d^2} = L \Omega_i$$

**Known irradiance:**

$$I = \frac{E \cdot d^2}{\cos \xi} \quad \Phi = E \cdot A_i \quad L = \frac{R \cdot E}{\pi}$$

**Relationship of configuration factor to projected solid angle and of form factor to average projected solid angle:**

$$C = \Omega / \pi \quad F_{a \rightarrow b} = \bar{\Omega}_{a \rightarrow b} / \pi$$

**Projected solid angle of circular area from on-axis point:**

$$\Omega = \frac{\pi r^2}{r^2 + d^2} = \pi \sin^2 \theta$$

**Projected solid angle of circular area from off-axis point:**

$$\Omega = \frac{\pi}{2} \left( 1 - \frac{1 + \tan^2 \delta - \tan^2 \theta}{\left[ \tan^4 \delta + (2 \tan^2 \delta)(1 - \tan^2 \theta) + \sec^4 \theta \right]^{1/2}} \right)$$

$$\Omega = \frac{\pi}{2} \left( 1 - \frac{1 + (d/x)^2 - (r/x)^2}{\left[ \left\{ 1 + (d/x)^2 + (r/x)^2 \right\}^2 - 4(r/x)^2 \right]^{1/2}} \right)$$


---

### Equation Summary (cont.)

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**Average projected solid angle from one circular area to another, with both areas parallel and centered on the same axis:**

$$\bar{\Omega}_{r \text{ to } i} = \frac{\pi}{2} \left[ 1 + \frac{1 + \left(\frac{r_i}{d}\right)^2}{\left(\frac{r_r}{d}\right)^2} - \left\{ \left( 1 + \frac{1 + \left(\frac{r_i}{d}\right)^2}{\left(\frac{r_r}{d}\right)^2} \right)^2 - 4 \left(\frac{r_i}{r_r}\right)^2 \right\}^{\frac{1}{2}} \right]$$

**Cosine fourth and increase factor:**

$$E_i = \pi L_r \sin^2 \theta \cdot \cos^4 \delta \cdot F'$$

**$\omega$ ,  $\Omega$ , NA, and  $f/\#$  for a circular cone:**

$$\omega = 2\pi(1 - \cos\theta) \quad \Omega = \pi \sin^2 \theta$$

$$NA = n \cdot \sin \theta \quad f/\# = 1/2 \sin \theta$$

### *Illumination in Imaging Systems*

**Object and image radiance:**

$$\frac{L_i}{n_i^2} = \tau \cdot \frac{L_o}{n_o^2}$$

**Image irradiance off axis:**

$$E_i = \pi \tau L_o \sin^2 \theta \cdot \cos^4 \delta \cdot F'$$

**Image irradiance on axis:**

$$\begin{aligned} E_{i0} &= \pi \tau L_o \sin^2 \theta = \frac{\pi \tau L_o}{4(f/\#)^2} = \frac{\pi L_o}{4(T/\#)^2} \\ &= \pi \tau L_o NA^2 = \tau L_o \Omega \end{aligned}$$

**Image flux:**

$$\Phi_i = \tau L_o a_i \Omega_i = \tau L_o a_p \Omega_p$$


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### Equation Summary (cont.)

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#### *Illumination in Nonimaging Systems*

##### Generalized étendue:

$$\mathcal{E} = n^2 \iint_{\text{aperture}} \cos \theta dA_s d\omega$$

$$\Phi = \iint_{\text{aperture}} L(\mathbf{r}, \hat{\mathbf{a}}) \cos \theta dA_s d\omega,$$

$$\begin{aligned} \Phi &= L_s \iint_{\text{aperture}} \cos \theta dA_s d\omega \\ &= \frac{L_s \mathcal{E}}{n^2} \end{aligned}$$

##### Concentration:

$$C = A/A'$$

$$C_{2D} = \frac{a}{a'} = \frac{n' \sin \theta'}{n \sin \theta} \quad C_{3D} = \frac{A}{A'} = \left( \frac{n' \sin \theta'}{n \sin \theta} \right)^2$$

$$C_{2D,\text{opt}} = \frac{n'}{n \sin \theta_a} \quad C_{3D,\text{opt}} = \left( \frac{n'}{n \sin \theta_a} \right)^2$$

##### Skew invariant:

$$f_{\text{skew}}(s) = \frac{d\mathcal{E}(s)}{ds},$$

where  $s = r_{\min} k_t$

#### *Fibers, Lightpipes, and Lightguides*

##### Maximum acceptance angle:

$$\sin \theta_{\max} = \frac{1}{n_0} \sqrt{n_1^2 - n_2^2}$$

##### Numerical aperture:

$$\text{NA} = n_0 \sin \theta_{\max} = \sqrt{n_1^2 - n_2^2}$$


---



### Equation Summary (cont.)

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**Étendue:**

$$E'_{\text{tendue}} = \frac{\pi^2}{4} d^2 NA^2$$

**Tapered single fiber:**

$$a_i \cdot NA_i^2 \approx a_o \cdot NA_o^2$$

**Tapered bundle:**

$$NA_o = NA_i = NA_{\text{fiber}}$$

$$a_o \cdot pf_o = a_i \cdot pf_i$$

**Uniform Illumination**

**Bent lightpipes:**

$$R = r_2/r_1 = 1 + t/r_1 \leq n$$

**Integrating sphere radiance:**

$$L = \frac{\Phi}{\pi \cdot A_s} \cdot M \quad M = \frac{1}{1 - \bar{\rho}}$$

$$\theta(\phi) = \arctan \left[ \tan \theta_1 + \int_{\phi_1}^{\phi} I_{\text{src}}(v) dv \right]$$

$$r(\phi) = r_1 \exp \left[ \int_{\phi_1}^{\phi} \tan \left( \frac{s - \theta(s)}{2} \right) ds \right]$$

**Nonimaging Compound Concentrators**

**Preservation of étendue:**

$$a_i \Omega_i = a_o \Omega_o$$

**Maximum concentration ratio:**

$$\frac{a_i}{a_o} (\text{max}) = \frac{1}{\sin^2 \theta_i}$$


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### Equation Summary (cont.)

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**Diameter of CPC used as a collimator:**

$$\frac{d_o}{d_i} = \frac{1}{\sin \theta_{\max}}$$

**Length of CPC:**

$$\text{Length} = \frac{d_o + d_i}{2 \tan \theta_{\max}}$$

**Equation for surface of CPC:**

$$\begin{aligned} & (r \cos \theta_{\max} + z \sin \theta_{\max})^2 \\ & + r d_s (1 + \sin \theta_{\max})^2 \\ & - z d_s \cos \theta_{\max} (2 + \sin \theta_{\max}) \\ & - \frac{d_s^2}{4} (1 + \sin \theta_{\max})(3 + \sin \theta_{\max}) \\ & = 0, \end{aligned}$$

where:

$r$  is the radius of the cone, perpendicular to the axis,

$z$  is the axial position measured from the small end,

$d_s$  is the diameter of the small end, and

$\theta_{\max}$  is the maximum field angle at the large end.

**Tailored edge ray design:**

$$\begin{aligned} \theta(\phi) &= \arctan \left[ \tan \theta_1 + \int_{\phi_1}^{\phi} I_{src}(v) dv \right] \\ r(\phi) &= r_1 \exp \left\{ \int_{\phi_1}^{\phi} \tan \left[ \frac{s - \theta(s)}{2} \right] ds \right\} \end{aligned}$$

## CIE Illuminants A and D65

$\lambda$ (nm)	CIE Ill. A Tungsten at 2856 K	CIE Ill. D65 Sunlight
300	0.930483	0.03410
305	1.128210	1.66430
310	1.357690	3.29450
315	1.622190	11.76520
320	1.925080	20.23600
325	2.269800	28.64470
330	2.659810	37.05350
335	3.098610	38.50110
340	3.589680	39.94880
345	4.136480	42.43020
350	4.742380	44.91170
355	5.410700	45.77500
360	6.144620	46.63830
365	6.947200	49.36370
370	7.821350	52.08910
375	8.769800	51.03230
380	9.795100	49.97550
385	10.899600	52.31180
390	12.085300	54.64820
395	13.354300	68.70150
400	14.708000	82.75490
405	16.148000	87.12040
410	17.675300	91.48600
415	19.290700	92.45890
420	20.995000	93.43180
425	22.788300	90.05700
430	24.670900	86.68230
435	26.642500	95.77360
440	28.702700	104.86500
445	30.850800	110.93600
450	33.085900	117.00800
455	35.406800	117.41000
460	37.812100	117.81200
465	40.300200	116.33600
470	42.869300	114.86100



**CIE Illuminants A and D65 (cont.)**

$\lambda$ (nm)	CIE Ill. A	CIE Ill. D65
475	45.517400	115.39200
480	48.242300	115.92300
485	51.041800	112.36700
490	53.913200	108.81100
495	56.853900	109.08200
500	59.861100	109.35400
505	62.932000	108.57800
510	66.063500	107.80200
515	69.252500	106.29600
520	72.495900	104.79000
525	75.790300	106.23900
530	79.132600	107.68900
535	82.519300	106.04700
540	85.947000	104.40500
545	89.412400	104.22500
550	92.912000	104.04600
555	96.442300	102.02300
560	100.000000	100.00000
565	103.582000	98.16710
570	107.184000	96.33420
575	110.803000	96.06110
580	114.436000	95.78800
585	118.080000	92.23680
590	121.731000	88.68560
595	125.386000	89.34590
600	129.043000	90.00620
605	132.697000	89.80260
610	136.346000	89.59910
615	139.988000	88.64890
620	143.618000	87.69870
625	147.235000	85.49360
630	150.836000	83.28860
635	154.418000	83.49390
640	157.979000	83.69920
645	161.516000	81.86300
650	165.028000	80.02680

**CIE Illuminants A and D65 (cont.)**

$\lambda$ (nm)	CIE Ill. A	CIE Ill. D65
655	168.510000	80.12070
660	171.963000	80.21460
665	175.383000	81.24620
670	178.769000	82.27780
675	182.118000	80.28100
680	185.429000	78.28420
685	188.701000	74.00270
690	191.931000	69.72130
695	195.118000	70.66520
700	198.261000	71.60910
705	201.359000	72.97900
710	204.409000	74.34900
715	207.411000	67.97650
720	210.365000	61.60400
725	213.268000	65.74480
730	216.120000	69.88560
735	218.920000	72.48630
740	221.667000	75.08700
745	224.361000	69.33980
750	227.000000	63.59270
755	229.585000	55.00540
760	232.115000	46.41820
765	234.589000	56.61180
770	237.008000	66.80540
775	239.370000	65.09410
780	241.675000	63.38280
785	243.924000	63.84340
790	246.116000	64.30400
795	248.251000	61.87790
800	250.329000	59.45190
805	252.350000	55.70540
810	254.314000	51.95900
815	256.221000	54.69980
820	258.071000	57.44060
825	259.865000	58.87650
830	261.602000	60.31250

$\bar{x}, \bar{y}, \bar{z}, V(\lambda), \text{ and } V'(\lambda)$ 

Note: The photopic efficiency function,  $V(\lambda)$ , is identical to the  $\bar{y}$  standard observer function.

$\lambda$ (nm)	$\bar{x}$	$\bar{y}, V$	$\bar{z}$	$V'$
360	0.000130	0.000004	0.000606	0.000000
365	0.000232	0.000007	0.001086	0.000000
370	0.000415	0.000012	0.001946	0.000000
375	0.000742	0.000022	0.003486	0.000000
380	0.001368	0.000039	0.006450	0.000000
385	0.002236	0.000064	0.010550	0.001108
390	0.004243	0.000120	0.020050	0.002209
395	0.007650	0.000217	0.036210	0.004530
400	0.014310	0.000396	0.067850	0.009290
405	0.023190	0.000640	0.110200	0.018520
410	0.043510	0.001210	0.207400	0.034840
415	0.077630	0.002180	0.371300	0.060400
420	0.134380	0.004000	0.645600	0.096600
425	0.214770	0.007300	1.039050	0.143600
430	0.283900	0.011600	1.385600	0.199800
435	0.328500	0.016840	1.622960	0.262500
440	0.348280	0.023000	1.747060	0.328100
445	0.348060	0.029800	1.782600	0.393100
450	0.336200	0.038000	1.772110	0.455000
455	0.318700	0.048000	1.744100	0.513000
460	0.290800	0.060000	1.669200	0.567000
465	0.251100	0.073900	1.528100	0.620000
470	0.195360	0.090980	1.287640	0.676000
475	0.142100	0.112600	1.041900	0.734000
480	0.095640	0.139020	0.812950	0.793000
485	0.057950	0.169300	0.616200	0.851000
490	0.032010	0.208020	0.465180	0.904000
495	0.014700	0.258600	0.353300	0.949000
500	0.004900	0.323000	0.272000	0.982000
505	0.002400	0.407300	0.212300	0.998000
510	0.009300	0.503000	0.158200	0.997000



$\bar{x}$ ,  $\bar{y}$ ,  $\bar{z}$ ,  $V(\lambda)$ , and  $V'(\lambda)$  (cont.)

$\lambda$ (nm)	$\bar{x}$	$\bar{y}, V$	$\bar{z}$	$V'$
515	0.029100	0.608200	0.111700	0.975000
520	0.063270	0.710000	0.078250	0.935000
525	0.109600	0.793200	0.057250	0.880000
530	0.165500	0.862000	0.042160	0.811000
535	0.225750	0.914850	0.029840	0.733000
540	0.290400	0.954000	0.020300	0.650000
545	0.359700	0.980300	0.013400	0.564000
550	0.433450	0.994950	0.008750	0.481000
555	0.512050	1.000000	0.005750	0.402000
560	0.594500	0.995000	0.003900	0.328800
565	0.678400	0.978600	0.002750	0.263900
570	0.762100	0.952000	0.002100	0.207600
575	0.842500	0.915400	0.001800	0.160200
580	0.916300	0.870000	0.001650	0.121200
585	0.978600	0.816300	0.001400	0.089900
590	1.026300	0.757000	0.001100	0.065500
595	1.056700	0.694900	0.001000	0.046900
600	1.062200	0.631000	0.000800	0.033150
605	1.045600	0.566800	0.000600	0.023120
610	1.002600	0.503000	0.000340	0.015930
615	0.938400	0.441200	0.000240	0.010880
620	0.854450	0.381000	0.000190	0.007370
625	0.751400	0.321000	0.000100	0.004970
630	0.642400	0.265000	0.000050	0.003335
635	0.541900	0.217000	0.000030	0.002235
640	0.447900	0.175000	0.000020	0.001497
645	0.360800	0.138200	0.000010	0.001005
650	0.283500	0.107000	0.000000	0.000677
655	0.218700	0.081600	0.000000	0.000459
660	0.164900	0.061000	0.000000	0.000313
665	0.121200	0.044580	0.000000	0.000215
670	0.087400	0.032000	0.000000	0.000148
675	0.063600	0.023200	0.000000	0.000103
680	0.046770	0.017000	0.000000	0.000072

$\bar{x}$ ,  $\bar{y}$ ,  $\bar{z}$ ,  $V(\lambda)$ , and  $V'(\lambda)$  (cont.)

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$\lambda$ (nm)	$\bar{x}$	$\bar{y}$ , $V$	$\bar{z}$	$V'$
685	0.032900	0.011920	0.000000	0.000050
690	0.022700	0.008210	0.000000	0.000035
695	0.015840	0.005723	0.000000	0.000025
700	0.011359	0.004102	0.000000	0.000018
705	0.008111	0.002929	0.000000	0.000013
710	0.005790	0.002091	0.000000	0.000009
715	0.004106	0.001484	0.000000	0.000007
720	0.002899	0.001047	0.000000	0.000005
725	0.002049	0.000740	0.000000	0.000003
730	0.001440	0.000520	0.000000	0.000003
735	0.001000	0.000361	0.000000	0.000002
740	0.000690	0.000249	0.000000	0.000001
745	0.000476	0.000172	0.000000	0.000001
750	0.000332	0.000120	0.000000	0.000001
755	0.000235	0.000085	0.000000	0.000001
760	0.000166	0.000060	0.000000	0.000000
765	0.000117	0.000042	0.000000	0.000000
770	0.000083	0.000030	0.000000	0.000000
775	0.000059	0.000021	0.000000	0.000000
780	0.000042	0.000015	0.000000	0.000000
785	0.000029	0.000011	0.000000	0.000000
790	0.000021	0.000007	0.000000	0.000000
795	0.000015	0.000005	0.000000	0.000000
800	0.000010	0.000004	0.000000	0.000000
805	0.000007	0.000003	0.000000	0.000000
810	0.000005	0.000002	0.000000	0.000000
815	0.000004	0.000001	0.000000	0.000000
820	0.000003	0.000001	0.000000	0.000000
825	0.000002	0.000001	0.000000	0.000000
830	0.000001	0.000000	0.000000	0.000000

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## Archaic and Arcane Units of Illumination

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### Luminous Intensity

The unit of luminous intensity is, and has been, the base unit of photometry. Until recently, it suffered from a lack of stable, reproducible standards. Over the past century and a half, standards have ranged from actual candles (wax or whale fat), gas lamps (pentane, isopropyl acetate), vegetable oil lamps (colza, i.e. canola oil), carbon filament lamps, blackbody furnaces, and finally, in 1979, a radiometric standard. Because of the past difficulty in realizing the standard, most of these expressions for intensity are approximate at best.

- 1 Hefner candle  $\approx$  0.9 cd
- 1 candlepower\* = 1 candela (cd)
- 1 new candle = 1 bougie nouvelle = 1 cd
- 1 candle (UK)  $\approx$  1 cd
- 1 decimal candle = 1 bougie decimal = 1.02 cd
- 1 international candle = 1.02 cd
- 1 Vereinskerze (German candle)  $\approx$  1.1 cd
- 1 pentane candle  $\approx$  10 cd
- 1 Munich candle  $\approx$  1.2 cd
- 1 carcel unit  $\approx$  9.8 cd
- 1 Violle  $\approx$  20.4 cd

### Luminous Flux

- 1 spherical candlepower\* (SCP) =  $4\pi$  lumens (lm)
- 1 mean spherical candlepower\* (MSCP) =  $4\pi$  lm

### Illuminance

- 1 nox = 0.001 lux
- 1 milliphot = 10 lux
- 1 footcandle\* =  $1 \text{ lm/ft}^2 = 10.764 \text{ lux}$
- 1 flame = 43.06 lux
- 1 cm-candle = 1 phot = 10,000 lux

\* still in occasional use

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## Archaic and Arcane Units of Illumination (cont.)

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### Luminance

Several units of luminance have the number  $\pi$  in the denominator. This was done before the availability of calculators and computers to facilitate the calculation of the luminance of a **Lambertian** surface, which radiates uniform **luminance** over a projected solid angle of  $\pi$  steradians. For example, a Lambertian surface with **reflectance**,  $\rho$ , receiving an **illuminance** of  $x$  lux has a **luminance** of  $\rho x$  apostilbs.

$$1 \text{ bril} = 3.183 \times 10^{-8} \text{ nit}$$

$$1 \text{ skot} = 3.183 \times 10^{-4} \text{ nit}$$

$$1 \text{ apostilb} = 1 \text{ Blondel} = 1 \text{ cd}/\pi\text{m}^2 = 0.3183 \text{ nit}$$

$$1 \text{ millilambert} = 3.183 \text{ nit}$$

$$1 \text{ foot-Lambert}^* = 1 \text{ cd}/\pi\text{ft}^2 = 3.426 \text{ cd}/\text{m}^2 = 3.426 \text{ nit}$$

$$1 \text{ cd}/\text{ft}^2 = 10.76 \text{ nit}$$

$$1 \text{ Lambert} = 1 \text{ cd}/\pi\text{cm}^2 = 3183 \text{ nit}$$

$$1 \text{ stilb} = 1 \text{ cd}/\text{cm}^2 = 10,000 \text{ nit}$$

### CCT

$$1 \text{ mired}^* \text{ (microreciprocal degree)} = 1 \text{ reciprocal megaKelvin (MK)}^{-1}$$

$$1 \text{ mirek}^* \text{ (microreciprocal Kelvin)} = 1 \text{ reciprocal megaKelvin (MK)}^{-1}$$

### Photons

$$1 \text{ Einstein}^\ddagger = \text{Avagadro's number of photons}$$

$$1 \text{ Einstein}^\ddagger = 6.022 \times 10^{23} \text{ photons}$$

$$1 \text{ micromole}^\ddagger = 6.022 \times 10^{17} \text{ photons in the 400- to 700-nm band}$$

### Photon Radiance

$$1 \text{ Rayleigh}^\ddagger = 7.96 \times 10^{-8} \text{ photons}/\text{sec}\cdot\text{m}^2\cdot\text{sr}$$

### Wavelength

$$1 \text{ millimicron}^* = 1 \text{ nanometer}$$

\* still in occasional use

‡ still in occasional use in fields other than illumination or optics

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