

Library of Congress Cataloging in Publication Data Johnson, David E Basic electric circuit analysis. Includes index. Includes index.
I. Electric circuits. I. Hilburn, John L., 1938joint author. II. Johnson, Johnny Ray, joint
author. III. Title.
TK454,J56 621.319'2 77-24210
ISBN 0-13-060137-3 © 1978 by Prentice-Hall, Inc., Englewood Cliffs, N.J. 07632 All rights reserved. No part of this book may be reproduced in any form or by any means without permission in writing from the publisher. Printed in the United States of America 10 9 8 7 6 5 4 3 PRENTICE-HALL INTERNATIONAL, INC., London PRENTICE-HALL OF AUSTRALIA PTY. LIMITED, Sydney PRENTICE-HALL OF CANADA, LTD., Toronto PRENTICE-HALL OF INDIA PRIVATE LIMITED, New Delhi PRENTICE-HALL OF JAPAN, INC., Tokyo PRENTICE-HALL OF SOUTHEAST ASIA PTE. LTD., Singapore WHITEHALL BOOKS LIMITED, Wellington, New Zealand



Find authenticated court documents without watermarks at <u>docketalarm.com</u>.

EXERCISES

10.6.1 Using phasors, find the ac steady-state current i if $v=12\cos{(1000t+30^\circ)}$ V in (a) Fig. 10.9(a) for R=4 k Ω , (b) Fig. 10.11(a) for L=20 mH, and (c) Fig. 10.13(a) for C=1 μ F.

Ans. (a) $3 \cos (1000t + 30^\circ) \text{ mA}$, (b) $0.6 \cos (1000t - 60^\circ) \text{ A}$, (c) $12 \cos (1000t + 120^\circ) \text{ mA}$

10.6.2 In Ex. 10.6.1, find i in each case at t = 1 ms. Ans. (a) 0.142 mA, (b) 0.599 A, (c) -11.987 mA

10.7 IMPEDANCE AND ADMITTANCE

Let us now consider a general phasor circuit with two accessible terminals, as shown in Fig. 10.15. If the time-domain voltage and current at the terminals are given by (10.38), then the phasor quantities at the terminals are

$$V = V_m/\underline{\theta}$$

$$I = I_m/\underline{\phi}$$
(10.46)

We define the ratio of the phasor voltage to the phasor current as the impedance of the circuit, which we denote by Z. That is,

$$Z = \frac{V}{I} \tag{10.47}$$

which by (10.46) is

$$\mathbf{Z} = |\mathbf{Z}| \underline{\theta_z} = \frac{V_m}{I_m} \underline{\theta - \phi}$$
 (10.48)

where $|\,{\bf Z}\,|$ is the magnitude and θ_Z the angle of ${\bf Z}.$ Evidently,

$$|\mathbf{Z}| = \frac{V_m}{I_m}, \quad \theta_Z = \theta - \phi$$

Impedance, as is seen from (10.47), plays the role, in a general circuit, of resistance in resistive circuits. Indeed, (10.47) looks very much like Ohm's law; also like resistance,

impedance is measured in ohms, being a ratio of volts to amperes. It is important to stress that impedance is a complex number, being the ratio of two complex numbers, but it is not a phasor. That is, it has no corresponding sinusoidal time-domain function of any physical meaning, as current and voltage phasors have. The impedance \mathbf{Z} is written in polar form in (10.48); in rectangular form it is

generally denoted by

$$\mathbf{Z} = R + jX \tag{10.49}$$

where $R=\operatorname{Re} \mathbf{Z}$ is the resistive component, or simply resistance, and $X=\operatorname{Im} \mathbf{Z}$ is the reactive component, or reactance. In general, $\mathbf{Z}=\mathbf{Z}(j\omega)$ is a complex function of $j\omega$, but $R=R(\omega)$ and $X=\overline{X}(\omega)$ are real functions of ω . Both R and X, like Z, are measured in ohms. Evidently, comparing (10.48) and (10.49) we may write

$$|\mathbf{Z}| = \sqrt{R^2 + X^2}$$

$$\theta_z = \tan^{-1} \frac{X}{R}$$

Chap. 10

$$R = |\mathbf{Z}| \cos \theta_z$$
$$X = |\mathbf{Z}| \sin \theta_z$$

These relations are shown graphically in Fig. 10.16. As an example, suppose in Fig. 10.15 that $V=10/\underline{56.1^\circ}\ V$ and $I=2/\underline{20^\circ}\ A$. Then

$$\mathbf{Z} = \frac{10/56.1^{\circ}}{2/20^{\circ}} = 5/36.1^{\circ}\,\Omega$$

In rectangular form this is

$$\mathbf{Z} = 5(\cos 36.1^{\circ} + j \sin 36.1^{\circ})$$

= $4 + j3 \Omega$

The impedances of resistors, inductors, and capacitors are readily found from their V-I relations of (10.40), (10.43), and (10.45). Distinguishing their impedances with subscripts R, L, and C, respectively, we have, from these equations and (10.47),

$$Z_{R} = R$$

$$Z_{L} = j\omega L = \omega L/90^{\circ}$$

$$Z_{C} = \frac{1}{j\omega C} = -j\frac{1}{\omega C} = \frac{1}{\omega C}/-90^{\circ}$$
(10.50)





FIGURE 10.15 General phasor circuit

FIGURE 10.16 Graphi

