CLAIMS

What is claimed is:

1.   A method implemented by a network node (10) for signaling to a wireless
communication device (14) which precoders in a codebook are restricted from being used, the
method characterized by:

   generating (210) codebook subset restriction signaling that, for each of one or more
      groups of precoders, jointly restricts the precoders in the group by restricting a
      certain component that the precoders in the group have in common, and wherein
      the precoders are Kronecker product precoders and wherein the signaling is
      rank-agnostic so as to restrict precoders irrespective of their transmission rank;
      and

   sending (220) the generated signaling from the network node (10) to the wireless
      communication device (14).

2.   A method implemented by a wireless communication device (14) for decoding signaling
from a network node (10) indicating which precoders in a codebook are restricted from being
used, the method characterized by:

   receiving (400) codebook subset restriction signaling that, for each of one or more
      groups of precoders, jointly restricts the precoders in the group by restricting a
      certain component that the precoders in the group have in common, and wherein
      the precoders are Kronecker product precoders and wherein the signaling is
      rank-agnostic so as to restrict precoders irrespective of their transmission rank;
      and

   decoding (410) the received signaling as jointly restricting precoders in each of the one
      or more groups of precoders.

3.   The method of any of claims 1-2, wherein the certain component comprises a beam
precoder.

4.   The method of any of claims 1-3, wherein a precoder comprising one or more beam
precoders is restricted if at least one of its one or more beam precoders is restricted.

5.   The method of any of claims 3-4, wherein a beam precoder is a Kronecker product of
different beamforming vectors associated with different dimensions of a multi-dimensional
antenna array.

| Deleted: 3.   The method of any of claims 1-2, wherein the codebook subset restriction signaling is rank-agnostic signaling that jointly restricts the precoders in a group without regard to the precoders' transmission rank.¶ ¶ 4 |
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6. The method of claim 5, wherein the different beamforming vectors comprise Discrete Fourier Transform (DFT) vectors.

7. The method of any of claims 3-6, wherein a beam precoder is a beamforming vector used to transmit on a particular layer of a multi-layer transmission, wherein different scaled versions of that beamforming vector are transmitted on different polarizations;

8. The method of any of claims 3-6, wherein a beam precoder is a beamforming vector used to transmit on:

   multiple different layers of a multi-layer transmission;

   multiple different layers of a multi-layer transmission, wherein the layers are sent on orthogonal polarizations; or

   a particular layer and on a particular polarization.

9. The method of any of claims 1-8, wherein the codebook subset restriction signaling comprises a bitmap, with different bits in the bitmap respectively dedicated to indicating whether or not different beam precoders are restricted from being used.

10. The method of any of claims 1-8, wherein a beam precoder is a Kronecker product of first and second beamforming vectors with first and second indices, wherein the first and second beamforming vectors are associated with different dimensions of a multi-dimensional antenna array, and wherein the codebook subset restriction signaling jointly restricts the precoders in a group of precoders that have the same pair of values for the first and second indices.

11. The method of any of claims 1-9, wherein each precoder comprises one or more beam precoders, wherein each beam precoder comprises multiple different components corresponding to different dimensions of a multi-dimensional antenna array, and wherein said certain component comprises a component of a beam precoder.

12. The method of any of claims 1-11, wherein the codebook subset restriction signaling jointly restricts the precoders in a group of precoders that transmit at least in part towards a certain angular pointing direction, by restricting a certain component which has that angular pointing direction.

13. A network node (10, 600) for signaling to a wireless communication device (14, 800) which precoders in a codebook are restricted from being used, the network node (10, 600) configured to:

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generate codebook subset restriction signaling that, for each of one or more groups of precoders, jointly restricts the precoders in the group by restricting a certain component that the precoders in the group have in common, and wherein the precoders are Kronecker product precoders and wherein the signaling is rank-agnostic so as to restrict precoders irrespective of their transmission rank; and
send the generated signaling from the network node (10, 600) to the wireless communication device (14, 800).

14.   The network node of claim 13, configured to perform the method of any of claims 3-12.

15.   A network node (10, 600) for signaling to a wireless communication device (14, 800) which precoders in a codebook are restricted from being used, the network node (10, 600) characterized by:
a generating module (640) for generating codebook subset restriction signaling that, for each of one or more groups of precoders, jointly restricts the precoders in the group by restricting a certain component that the precoders in the group have in common, and wherein the precoders are Kronecker product precoders and wherein the signaling is rank-agnostic so as to restrict precoders irrespective of their transmission rank; and
a sending module (650) for sending the generated signaling from the network node (10, 600) to the wireless communication device (14, 800).

16.   A wireless communication device (14, 800) for decoding signaling from a network node (10, 600) indicating which precoders in a codebook are restricted from being used, the wireless communication device (14, 800) configured to:
receive codebook subset restriction signaling that, for each of one or more groups of precoders, jointly restricts the precoders in the group by restricting a certain component that the precoders in the group have in common, and wherein the precoders are Kronecker product precoders and wherein the signaling is rank-agnostic so as to restrict precoders irrespective of their transmission rank; and
decode the received signaling as jointly restricting precoders in each of the one or more groups of precoders.

17.   The wireless communication device of claim 16, configured to perform the method of any of claims 3-12.

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18. A wireless communication device (14, 800) for decoding signaling from a network node (10, 600) indicating which precoders in a codebook are restricted from being used, the wireless communication device (14, 800) characterized by:

    a receiving module (840) for receiving codebook subset restriction signaling that, for
5   each of one or more groups of precoders, jointly restricts the precoders in the group by restricting a certain component that the precoders in the group have in common, and wherein the precoders are Kronecker product precoders and wherein the signaling is rank-agnostic so as to restrict precoders irrespective of their transmission rank; and

10   a decoding module (850) for decoding the received signaling as jointly restricting precoders in each of the one or more groups of precoders.

19. A computer program comprising instructions which, when executed by at least one
15   processor of a node (10, 14), causes the node (10, 14) to carry out the method of any of embodiments 1-12.

20. A carrier containing the computer program of embodiment 19, wherein the carrier is one of an electronic signal, optical signal, radio signal, or computer readable storage medium.
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P45698-WO1 / 4015-9362

CLAIMS

What is claimed is:

1.   A method implemented by a network node (10) for signaling to a wireless communication device (14) which precoders in a codebook are restricted from being used, the method characterized by:

    generating (210) codebook subset restriction signaling that, for each of one or more groups of precoders, jointly restricts the precoders in the group by restricting a certain component that the precoders in the group have in common, and wherein the precoders are Kronecker product precoders and wherein the signaling is rank-agnostic so as to restrict precoders irrespective of their transmission rank; and

    sending (220) the generated signaling from the network node (10) to the wireless communication device (14).

2.   A method implemented by a wireless communication device (14) for decoding signaling from a network node (10) indicating which precoders in a codebook are restricted from being used, the method characterized by:

    receiving (400) codebook subset restriction signaling that, for each of one or more groups of precoders, jointly restricts the precoders in the group by restricting a certain component that the precoders in the group have in common, and wherein the precoders are Kronecker product precoders and wherein the signaling is rank-agnostic so as to restrict precoders irrespective of their transmission rank; and

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3.   The method of any of claims 1-2, wherein the certain component comprises a beam precoder.

4.   The method of any of claims 1-3, wherein a precoder comprising one or more beam precoders is restricted if at least one of its one or more beam precoders is restricted.

5.   The method of any of claims 3-4, wherein a beam precoder is a Kronecker product of different beamforming vectors associated with different dimensions of a multi-dimensional antenna array.

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6. The method of claim 5, wherein the different beamforming vectors comprise Discrete Fourier Transform (DFT) vectors.

7. The method of any of claims 3-6, wherein a beam precoder is a beamforming vector used to transmit on a particular layer of a multi-layer transmission, wherein different scaled versions of that beamforming vector are transmitted on different polarizations;

8. The method of any of claims 3-6, wherein a beam precoder is a beamforming vector used to transmit on:

multiple different layers of a multi-layer transmission;

multiple different layers of a multi-layer transmission, wherein the layers are sent on orthogonal polarizations; or

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11. The method of any of claims 1-2, wherein each precoder comprises one or more beam precoders, wherein each beam precoder comprises multiple different components corresponding to different dimensions of a multi-dimensional antenna array, and wherein said certain component comprises a component of a beam precoder.

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send the generated signaling from the network node (10, 600) to the wireless communication device (14, 800).

14.   The network node of claim 13, configured to perform the method of any of claims 3-12.

15.   A network node (10, 600) for signaling to a wireless communication device (14, 800) which precoders in a codebook are restricted from being used, the network node (10, 600) characterized by:

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decode the received signaling as jointly restricting precoders in each of the one or more groups of precoders.

17.   The wireless communication device of claim 16, configured to perform the method of any of claims 3-12.

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19. A computer program comprising instructions which, when executed by at least one processor of a node (10, 14), causes the node (10, 14) to carry out the method of any of embodiments 1-12.

20. A carrier containing the computer program of embodiment 19, wherein the carrier is one of an electronic signal, optical signal, radio signal, or computer readable storage medium.

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(Not for submission under 37 CFR 1.99)

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Filing Date	2016-06-17
First Named Inventor	Faxér
Art Unit	
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Attorney Docket Number	4015-9595 / P45698-US2

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	Application Number	15105648	
INFORMATION DISCLOSURE	**Filing Date**	2016-06-17	
STATEMENT BY APPLICANT	**First Named Inventor**	Faxér	
(Not for submission under 37 CFR 1.99)	**Art Unit**		
	Examiner Name		
	Attorney Docket Number	4015-9595 / P45698-US2	

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Please see 37 CFR 1.97 and 1.98 to make the appropriate selection(s):

That each item of information contained in the information disclosure statement was first cited in any communication from a foreign patent office in a counterpart foreign application not more than three months prior to the filing of the information disclosure statement. See 37 CFR 1.97(e)(1).

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The fee set forth in 37 CFR 1.17 (p) has been submitted herewith.

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A signature of the applicant or representative is required in accordance with CFR 1.33, 10.18. Please see CFR 1.4(d) for the form of the signature.

Signature	/Justin J. Leonard, Reg. No. 60986/	Date (YYYY-MM-DD)	2016-08-02
Name/Print	Justin Leonard	Registration Number	60986

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5.   A record related to an International Application filed under the Patent Cooperation Treaty in this system of records may be disclosed, as a routine use, to the International Bureau of the World Intellectual Property Organization, pursuant to the Patent Cooperation Treaty.

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ASYMPTOTIC EQUIPARTITION PROPERTY

In information theory, the analog of the law of large numbers is the asymptotic equipartition property (AEP). It is a direct consequence of the weak law of large numbers. The *law of large numbers* states that for independent, identically distributed (i.i.d.) random variables, $\frac{1}{n}\sum_{i=1}^{n} X_i$ is close to its expected value EX for large values of n. The AEP states that $\frac{1}{n}\log\frac{1}{p(X_1, X_2, \ldots, X_n)}$ is close to the entropy H, where $X_1, X_2, \ldots, X_n$ are i.i.d. random variables and $p(X_1, X_2, \ldots, X_n)$ is the probability of observing the sequence $X_1, X_2, \ldots, X_n$. Thus, the probability $p(X_1, X_2, \ldots, X_n)$ assigned to an observed sequence will be close to 2^{-nH}.

This enables us to divide the set of all sequences into two sets, the *typical set*, where the sample entropy is close to the true entropy, and the nontypical set, which contains the other sequences. Most of our attention will be on the typical sequences. Any property that is proved for the typical sequences will then be true with high probability and will determine the average behavior of a large sample.

First, an example. Let the random variable $X \in \{0, 1\}$ have a probability mass function defined by $p(1) = p$ and $p(0) = q$. If $X_1, X_2, \ldots, X_n$ are i.i.d. according to $p(x)$, the probability of a sequence $x_1, x_2, \ldots, x_n$ is $\prod_{i=1}^{n} p(x_i)$. For example, the probability of the sequence $(1, 0, 1, 1, 0, 1)$ is $p^{\sum x_i} q^{n-\sum x_i} = p^4 q^2$. Clearly, it is not true that all 2^n sequences of length n have the same probability.

However, we might be able to predict the probability of the sequence that we actually observe. We ask for the probability $p(X_1, X_2, \ldots, X_n)$ of the outcomes $X_1, X_2, \ldots, X_n$, where $X_1, X_2, \ldots$ are i.i.d. $\sim p(x)$. This is insidiously self-referential, but well defined nonetheless. Apparently, we are asking for the probability of an event drawn according to the same

probability distribution. Here it turns out that $p(X_1, X_2, \ldots, X_n)$ is close to 2^{-nH} with high probability.

We summarize this by saying, "Almost all events are almost equally surprising." This is a way of saying that

$$\Pr\left\{(X_1, X_2, \ldots, X_n) : p(X_1, X_2, \ldots, X_n) = 2^{-n(H \pm \epsilon)}\right\} \approx 1 \quad (3.1)$$

if $X_1, X_2, \ldots, X_n$ are i.i.d. $\sim p(x)$.

In the example just given, where $p(X_1, X_2, \ldots, X_n) = p^{\sum X_i} q^{n - \sum X_i}$, we are simply saying that the number of 1's in the sequence is close to np (with high probability), and all such sequences have (roughly) the same probability $2^{-nH(p)}$. We use the idea of convergence in probability, defined as follows:

Definition (*Convergence of random variables*). Given a sequence of random variables, $X_1, X_2, \ldots,$ we say that the sequence $X_1, X_2, \ldots$ converges to a random variable X:

1. *In probability* if for every $\epsilon > 0$, $\Pr\{|X_n - X| > \epsilon\} \to 0$
2. *In mean square* if $E(X_n - X)^2 \to 0$
3. *With probability 1* (also called *almost surely*) if $\Pr\{\lim_{n \to \infty} X_n = X\} = 1$

3.1 ASYMPTOTIC EQUIPARTITION PROPERTY THEOREM

The asymptotic equipartition property is formalized in the following theorem.

Theorem 3.1.1 *(AEP)   If $X_1, X_2, \ldots$ are i.i.d. $\sim p(x)$, then*

$$-\frac{1}{n} \log p(X_1, X_2, \ldots, X_n) \to H(X) \quad \textit{in probability.} \quad (3.2)$$

Proof: Functions of independent random variables are also independent random variables. Thus, since the X_i are i.i.d., so are $\log p(X_i)$. Hence, by the weak law of large numbers,

$$-\frac{1}{n} \log p(X_1, X_2, \ldots, X_n) = -\frac{1}{n} \sum_i \log p(X_i) \quad (3.3)$$

$$\to -E \log p(X) \quad \text{in probability} \quad (3.4)$$

$$= H(X), \quad (3.5)$$

which proves the theorem.   □

Definition   The *typical set* $A_\epsilon^{(n)}$ with respect to $p(x)$ is the set of sequences $(x_1, x_2, \ldots, x_n) \in \mathcal{X}^n$ with the property

$$2^{-n(H(X)+\epsilon)} \leq p(x_1, x_2, \ldots, x_n) \leq 2^{-n(H(X)-\epsilon)}, \tag{3.6}$$

As a consequence of the AEP, we can show that the set $A_\epsilon^{(n)}$ has the following properties:

Theorem 3.1.2

1. If $(x_1, x_2, \ldots, x_n) \in A_\epsilon^{(n)}$, then $H(X) - \epsilon \leq -\frac{1}{n} \log p(x_1, x_2, \ldots, x_n) \leq H(X) + \epsilon$.
2. $\Pr\{A_\epsilon^{(n)}\} > 1 - \epsilon$ *for n sufficiently large.*
3. $|A_\epsilon^{(n)}| \leq 2^{n(H(X)+\epsilon)}$, *where $|A|$ denotes the number of elements in the set A.*
4. $|A_\epsilon^{(n)}| \geq (1 - \epsilon)2^{n(H(X)-\epsilon)}$ *for n sufficiently large.*

Thus, the typical set has probability nearly 1, all elements of the typical set are nearly equiprobable, and the number of elements in the typical set is nearly 2^{nH}.

Proof: The proof of property (1) is immediate from the definition of $A_\epsilon^{(n)}$. The second property follows directly from Theorem 3.1.1, since the probability of the event $(X_1, X_2, \ldots, X_n) \in A_\epsilon^{(n)}$ tends to 1 as $n \to \infty$. Thus, for any $\delta > 0$, there exists an n_0 such that for all $n \geq n_0$, we have

$$\Pr\left\{ \left| -\frac{1}{n} \log p(X_1, X_2, \ldots, X_n) - H(X) \right| < \epsilon \right\} > 1 - \delta. \tag{3.7}$$

Setting $\delta = \epsilon$, we obtain the second part of the theorem. The identification of $\delta = \epsilon$ will conveniently simplify notation later.

To prove property (3), we write

$$1 = \sum_{x \in \mathcal{X}^n} p(\mathbf{x}) \tag{3.8}$$

$$\geq \sum_{x \in A_\epsilon^{(n)}} p(\mathbf{x}) \tag{3.9}$$

$$\geq \sum_{x \in A_\epsilon^{(n)}} 2^{-n(H(X)+\epsilon)} \tag{3.10}$$

$$= 2^{-n(H(X)+\epsilon)} |A_\epsilon^{(n)}|. \tag{3.11}$$

where the second inequality follows from (3.6). Hence

$$|A_\epsilon^{(n)}| \leq 2^{n(H(X)+\epsilon)} \qquad (3.12)$$

Finally, for sufficiently large n, $\Pr\{A_\epsilon^{(n)}\} > 1 - \epsilon$, so that

$$1 - \epsilon < \Pr\{A_\epsilon^{(n)}\} \qquad (3.13)$$

$$\leq \sum_{x \in A_\epsilon^{(n)}} 2^{-n(H(X)-\epsilon)} \qquad (3.14)$$

$$= 2^{-n(H(X)-\epsilon)}|A_\epsilon^{(n)}|, \qquad (3.15)$$

where the second inequality follows from (3.6). Hence,

$$|A_\epsilon^{(n)}| \geq (1 - \epsilon)2^{n(H(X)-\epsilon)}, \qquad (3.16)$$

which completes the proof of the properties of $A_\epsilon^{(n)}$. $\square$

3.2   CONSEQUENCES OF THE AEP: DATA COMPRESSION

Let $X_1, X_2, \ldots, X_n$ be independent, identically distributed random variables drawn from the probability mass function $p(x)$. We wish to find short descriptions for such sequences of random variables. We divide all sequences in $\mathcal{X}^n$ into two sets: the typical set $A_\epsilon^{(n)}$ and its complement, as shown in Figure 3.1.
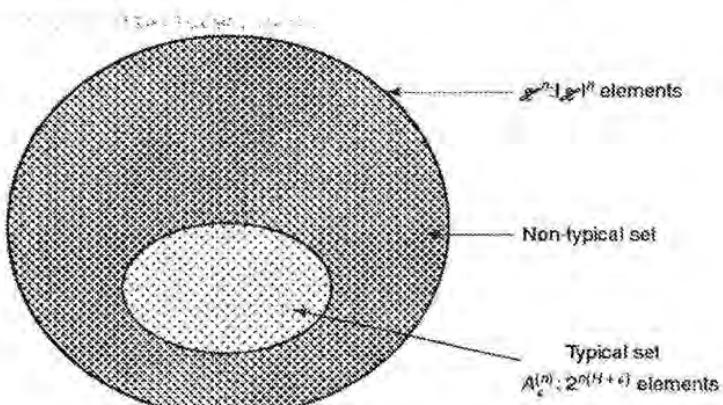
FIGURE 3.1. Typical sets and source coding.
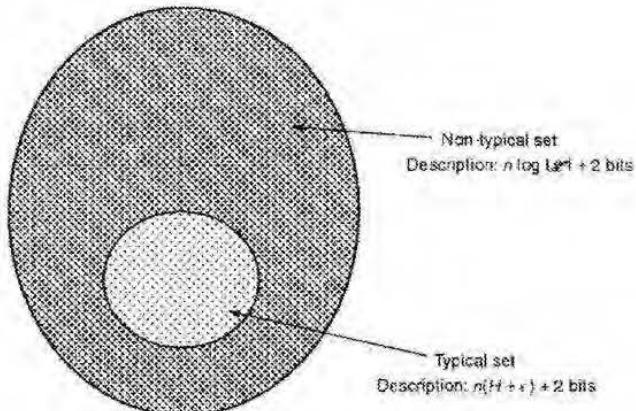
FIGURE 3.2. Source code using the typical set.

We order all elements in each set according to some order (e.g., lexicographic order). Then we can represent each sequence of $A_\epsilon^{(n)}$ by giving the index of the sequence in the set. Since there are $\leq 2^{n(H+\epsilon)}$ sequences in $A_\epsilon^{(n)}$, the indexing requires no more than $n(H + \epsilon) + 1$ bits. [The extra bit may be necessary because $n(H + \epsilon)$ may not be an integer.] We prefix all these sequences by a 0, giving a total length of $\leq n(H + \epsilon) + 2$ bits to represent each sequence in $A_\epsilon^{(n)}$ (see Figure 3.2). Similarly, we can index each sequence not in $A_\epsilon^{(n)}$ by using not more than $n \log |\mathcal{X}| + 1$ bits. Prefixing these indices by 1, we have a code for all the sequences in $\mathcal{X}^n$.

Note the following features of the above coding scheme:

- The code is one-to-one and easily decodable. The initial bit acts as a flag bit to indicate the length of the codeword that follows.
- We have used a brute-force enumeration of the atypical set $A_\epsilon^{(n)c}$ without taking into account the fact that the number of elements in $A_\epsilon^{(n)c}$ is less than the number of elements in $\mathcal{X}^n$. Surprisingly, this is good enough to yield an efficient description.
- The typical sequences have short descriptions of length $\approx nH$.

We use the notation x^n to denote a sequence $x_1, x_2, \ldots, x_n$. Let $l(x^n)$ be the length of the codeword corresponding to x^n. If n is sufficiently large so that $\Pr\{A_\epsilon^{(n)}\} \geq 1 - \epsilon$, the expected length of the codeword is

$$E(l(X^n)) = \sum_{x^n} p(x^n) l(x^n) \tag{3.17}$$

$$= \sum_{x^n \in A_\epsilon^{(n)}} p(x^n) l(x^n) + \sum_{x^n \in A_\epsilon^{(n)c}} p(x^n) l(x^n) \qquad (3.18)$$

$$\leq \sum_{x^n \in A_\epsilon^{(n)}} p(x^n)(n(H + \epsilon) + 2)$$

$$+ \sum_{x^n \in A_\epsilon^{(n)c}} p(x^n)(n \log |\mathcal{X}| + 2) \qquad (3.19)$$

$$= \Pr\left\{A_\epsilon^{(n)}\right\} (n(H + \epsilon) + 2) + \Pr\left\{A_\epsilon^{(n)c}\right\} (n \log |\mathcal{X}| + 2) \qquad (3.20)$$

$$\leq n(H + \epsilon) + \epsilon n(\log |\mathcal{X}|) + 2 \qquad (3.21)$$

$$= n(H + \epsilon'), \qquad (3.22)$$

where $\epsilon' = \epsilon + \epsilon \log |\mathcal{X}| + \frac{2}{n}$ can be made arbitrarily small by an appropriate choice of ϵ followed by an appropriate choice of n. Hence we have proved the following theorem.

Theorem 3.2.1   *Let X^n be i.i.d. $\sim p(x)$. Let $\epsilon > 0$. Then there exists a code that maps sequences x^n of length n into binary strings such that the mapping is one-to-one (and therefore invertible) and*

$$E\left[\frac{1}{n}l(X^n)\right] \leq H(X) + \epsilon \qquad (3.23)$$

for n sufficiently large.

Thus, we can represent sequences X^n using $nH(X)$ bits on the average.

3.3   HIGH-PROBABILITY SETS AND THE TYPICAL SET

From the definition of $A_\epsilon^{(n)}$, it is clear that $A_\epsilon^{(n)}$ is a fairly small set that contains most of the probability. But from the definition, it is not clear whether it is the smallest such set. We will prove that the typical set has essentially the same number of elements as the smallest set, to first order in the exponent.

Definition   For each $n = 1, 2, \ldots$, let $B_\delta^{(n)} \subset \mathcal{X}^n$ be the smallest set with

$$\Pr\{B_\delta^{(n)}\} \geq 1 - \delta. \qquad (3.24)$$

Computer Sciences Department

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Abstract

With the widening gap between processor and memory speeds, memory system designers may find cache compression beneficial to increase cache capacity and reduce off-chip bandwidth. Most hardware compression algorithms fall into the dictionary-based category, which depend on building a dictionary and using its entries to encode repeated data values. Such algorithms are effective in compressing large data blocks and files. Cache lines, however, are typically short (32-256 bytes), and a per-line dictionary places a significant overhead that limits the compressibility and increases decompression latency of such algorithms. For such short lines, significance-based compression is an appealing alternative.

We propose and evaluate a simple significance-based compression scheme that has a low compression and decompression overhead. This scheme, Frequent Pattern Compression (FPC) compresses individual cache lines on a word-by-word basis by storing common word patterns in a compressed format accompanied with an appropriate prefix. For a 64-byte cache line, compression can be completed in three cycles and decompression in five cycles, assuming 12 FO4 gate delays per cycle. We propose a compressed cache design in which data is stored in a compressed form in the L2 caches, but are uncompressed in the L1 caches. L2 cache lines are compressed to predetermined sizes that never exceed their original size to reduce decompression overhead. This simple scheme provides comparable compression ratios to more complex schemes that have higher cache hit latencies.

1 Introduction

As semiconductor technology continues to improve, the rising disparity between processor and memory speed increasingly dominates performance. Modern processors use two or more levels of cache memories to reduce effective memory latency and bandwidth. Effectively using the limited on-chip cache resources becomes increasingly important as memory latencies continue to increase relative to processor speeds. Cache compression has previously been proposed to improve performance, since compressing data stored in on-chip caches increases their effective capacity, potentially reducing misses.

Most previous proposals in hardware cache or memory compression (Section 2) are hardware implementations of dictionary-based software compression algorithms (e.g., LZ77 [32]). Such hardware dictionary-based schemes depend mainly on maintaining a per-block dictionary and encoding words (or bytes) that match in the dictionary, while keeping words (bytes) that do not match in their original form with an appropriate prefix.

Schemes such as the Block-Referential Compression with Lookahead (BRCL) used in the IBM MXT memory compression depend on having long enough lines / pages to increase the overall compression ratio [14]. BRCL provides a

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good compression ratio for 1K-byte or longer blocks. However, cache lines are typically much shorter and BRCL does not perform as well for shorter lines. In addition, decompression latency is high, since the parallel implementation of BRCL decompresses data at a speed of 8 bytes per cycle [26], or 8 cycles for a 64-byte cache line. The X-Match compression scheme [18] tries to compress more data with a small dictionary by allowing partial matches of data words to dictionary entries. Frequent-value cache designs [29, 31] achieve better compression for cache lines by constructing a single dictionary (the Frequent-Value Cache, FVC) for the whole cache, which increases the chance of a single word to be found and compressed. These designs are based on the observation that a few cache values are frequent and thus can be compressed to a fewer number of bits. However, a large FVC requires an increased decompression latency due to the increased FVC access time.

Significance-based compression is based on the observation that most data types (e.g., 32-bit integers) can be stored in a fewer number of bits than the maximum allowed. For example, sign-bit extension is a commonly implemented technique to store small integers (e.g., 8-bit) into 32-bit words, while all the information in the word is stored in the least-significant few bits. In contrast with dictionary-based compression schemes, significance-based compression [9, 11, 12] does not incur a per-line dictionary overhead, which makes it more suitable for the typically-short cache lines. In addition, compression and decompression hardware is faster than dictionary-based encoding and decoding. However, compressibility can be significantly impaired for long cache lines.

In this document, we propose a significance-based compression scheme that provides reasonable compressibility for the typically short cache lines with a relatively fast hardware compression and decompression (Section 3). This scheme, the Frequent Pattern Compression (FPC) compresses a cache line on a word-by-word basis. For each word, FPC detects whether it falls into one of the patterns that can be stored in a smaller number of bits, and stores it in a compressed form with an appropriate prefix. We discuss the implementation of a hardware decompression pipeline that decompresses a 64-byte cache line in five cycles (Section 4). We evaluate this scheme and compare it with other hardware compression schemes in Section 5.

2 Related Work

Several researchers used hardware-based compression to increase effective memory size, reduce memory address and data bandwidth, and increase effective cache size.

IBM's Memory Compression. IBM's MXT technology [26] employs real-time main-memory content compression that can be used to effectively double the main memory capacity without a significant added cost. It was first implemented in the Pinnacle chip [25], a single-chip memory controller. Franaszek, et al. [13], described the design of a compressed random access memory (C-RAM), which formed the basis for the memory organization for the MXT technology, and studied the optimal line size for such an organization. Data in main memory is compressed using a hardware parallelized derivative of the Lempel-Ziv (LZ77) sequential algorithm [32]. This parallel algorithm, Parallel Block-Referential Compression with Directory Sharing, divides the input data block (1 KB in MXT) into sub-blocks (four 256-byte sub-blocks), and cooperatively constructs dictionaries while compressing all sub-blocks in parallel [14]. MXT is shown to have a negligible performance penalty compared to standard memory, and memory contents for many applications and web servers can be compressed by a factor of two to one [1].

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Other Hardware Memory Compression Designs. Kjelso, et al. [18], demonstrated that hardware main memory compression is feasible and worthwhile. They used the X-Match hardware compression algorithm that maintains a dictionary and replaces each input data element (whose size is fixed at four bytes) with a shorter code in case of a total or partial match with a dictionary entry. Communication bandwidth is reduced by "compacting" cache-to-memory address streams [12] or data streams [11]. Benini, et al. [8], propose a data compression/decompression scheme to reduce memory traffic in general purpose processor systems. Data is stored uncompressed in the cache, and compressed on the fly when transferred to memory. Memory-to-cache traffic is also decompressed on the fly. They used a differential compression scheme described in [7] that is based on the assumption that it is likely for data words in the same cache line to have some bits in common. Zhang and Gupta [30] introduce a class of common-prefix and narrow-data transformations for general-purpose programs that compress 32-bit addresses and integer words into 15-bit entities. They implemented these transformations by augmenting six data compression extension (DCX) instructions to the MIPS instruction set.

Cache Compression and Related Designs. Lee, et al. [21, 19, 20], propose a compressed memory hierarchy model that selectively compresses L2 cache and memory blocks if they can be reduced to half their original size. Their selective compressed memory system (SCMS) use a hardware implementation of the X-RL compression algorithm [18], a variant of the X-Match algorithm that gives a special treatment for runs of zeros. They propose several techniques to hide decompression overhead, including parallel decompression, selective adaptive compression for blocks that can be compressed to below a certain threshold, and the use of a decompression buffer to be accessed on L1 misses in parallel with L2 access. Ahn, et al. [2], propose several improvements on the X-RL technique that capture common values. Chen, et al. [10], propose a scheme that dynamically partitions the cache into sections of different compressibility, and they use a variant of the LZ compression algorithm. Pomerene, et al. [22], used a shadow directory scheme with more address tags than data blocks to improve upon LRU replacement.

Frequent-Value-Based Compression. Yang and Gupta [28] found out from an analysis of the SPECint95 benchmarks that a small number of distinct values occupy a large fraction of memory access values. This value locality phenomenon enabled them to design energy-efficient caches [27] and data compressed caches [29]. In their compressed cache design, each line in the L1 cache can be either one uncompressed line or two lines compressed to at least half their original sizes based on frequent values [29]. Zhang, et al., designed a value-centric data cache design called the frequent value cache (FVC) [31], which is a small direct-mapped cache dedicated to holding frequent benchmark values. They showed that augmenting a direct mapped cache with a small frequent value cache can greatly reduce the cache miss rate.

Significance-Based Compression. Farrens and Park [12] make use of the fact that many address references transferred between processor and memory have redundant information in their high-order (most significant) portions. They cached these high order bits in a group of dynamically allocated base registers and only transferred small register indexes rather than the high-order address bits between the processor and memory. Citron and Rudolph [11] store common high-order bits in address and data words in a table and transfer only an index plus the low order bits between the processor and memory. Canal, et al. [9], proposed a scheme that compresses data, addresses and instruc-

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tions into their significant bytes while maintaining a two or three extension bits to maintain significant byte positions. They use this method to reduce dynamic power consumption in a processor pipeline. Kant and Iyer [16] studied the compressibility properties of address and data transfers in commercial workloads, and report that the high-order bits can be predicted with high accuracy in address transfers but with less accuracy for data transfers.

3 Frequent Pattern Compression (FPC)

We propose a compression scheme that builds on significance-based compression schemes [9, 11, 12]. It is also based on the observation that some data patterns are frequent and also compressible to a fewer number of bits. For example, many small-value integers can be stored in 4, 8 or 16 bits, but are normally stored in a full 32-bit word (or 64-bits for 64-bit architectures). These values are frequent enough to merit special treatment, and storing them in a more compact form can increase the cache capacity. In addition, special treatment is also given to runs of zeros since they are very frequent, which is similar to the special treatment in X-RL [18]. The insight behind FPC is that we want to get most of the benefits of dictionary-based schemes, while keeping the per-line overhead at a minimum.

The Frequent Pattern Compression (FPC) compresses / decompresses on a cache line basis. Each cache line is divided into 32-bit words (e.g., 16 words for a 64-byte line). Each 32-bit word is encoded as a 3-bit prefix plus data. Table 1 shows the different patterns corresponding to each prefix.

Each word in the cache line is encoded into a compressed format if it matches any of the patterns in the first six rows of Table 1. These patterns are: a zero run (one or more all-zero words), 4-bit sign-extended (including one-word zero runs), one byte sign-extended, one halfword sign-extended, one halfword padded with a zero halfword, two byte-sign-extended halfwords, and a word consisting of repeated bytes (e.g. "0x20202020", or similar patterns that can be used for data initialization). These patterns are selected based on their high frequency in many of our integer and commercial benchmarks. A word that doesn't match any of these categories is stored in its original 32-bit format. All prefix values as well as the zero-run length data bits are stored at the beginning of the line to speed up decompression.

3.1 Segmented Frequent Pattern Compression (S-FPC)

To exploit compression, the L2 cache must be able to pack more compressed cache lines than uncompressed lines into the same space. One approach is to decouple the cache access, adding a level of indirection between the address

Table 1. Frequent Pattern Encoding

Prefix	Pattern Encoded	Data Size
000	Zero Run	3 bits (for runs up to 8 zeros)
001	4-bit sign-extended	4 bits
010	One byte sign-extended	8 bits
011	halfword sign-extended	16 bits
100	halfword padded with a zero halfword	The nonzero halfword (16 bits)
101	Two halfwords, each a byte sign-extended	The two bytes (16 bits)
110	word consisting of repeated bytes	8 bits
111	Uncompressed word	Original Word (32 bits)

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tag and the data storage. Seznec's decoupled sector cache does this on a per-set basis to improve the utilization of sector (or sub-block) caches [23]. Hallnor and Reinhardt's Indirect-Index Cache (IIC) does this across the whole cache, allowing fully-associative placement and a software managed replacement policy [15]. Lee, et al.'s selective compressed caches use this technique to allow two compressed cache blocks to occupy the space required for one uncompressed block [21, 19, 20]. Decoupled access is simpler if we serially access the cache tags before the data. Fortunately, this is increasingly necessary to limit power dissipation [17].

In theory, a cache line can be compressed into any number of bits. This can be achieved in a completely decoupled design across the whole cache (e.g., IIC). However, such design adds more complexity to cache management. In our compressed cache design, the decoupled variable segment cache [5], each cache line is stored as a group of one or more 8-byte *segments*. For example, a 64-byte line can be stored in 1-8 segments. A compressed line is padded with zeros till its size becomes a multiple of the segment size, and these extra zeros (that do not correspond to any tags) are ignored during decompression. While this approach doesn't permit high compression ratios for some cache lines (e.g., all zero lines), it allows for a more practical and faster implementation of cache accesses.

4 Compression and Decompression

We propose a compressed cache design in which data is stored uncompressed in the level-1 caches and compressed in the level-2 caches [5]. This helps reduce many of the costly L2 cache misses that hinder performance, while not affecting the common case of an L1 hit. However, such a design adds the overhead of compressing or decompressing cache lines when moved between the two levels. FPC allows a relatively fast implementations of both of these functions.

Compression. Cache line compression occurs when data is written back from the L1 to the L2 cache. A cache line is compressed easily using a simple circuit that checks each word (in parallel) for pattern matches. If a word matches any of the seven compressible patterns, a simple encoder circuit is used to encode the word into its most compact form. If no match was found, the whole word is stored with the prefix '111'. This can be performed in one cycle, assuming 12 FO4 delays. For zero runs, we need to detect such runs of consecutive zeros, and increment the data value of the first occurrence to represent their count. Since zero runs are limited in our design to eight zeros, this can be implemented in a single cycle using a simple multiplexer/adder circuit.

Cache line compression can be implemented in a memory pipeline, by allocating three pipeline stages on the L1-to-L2 write path (one for pattern matching, one for zero run encoding, and one for gathering the compressed line). A small victim cache that contains a few entries in both compressed and uncompressed form can be used to hide the compression latency on L1 writebacks.

Decompression. Cache line decompression occurs when data is read from the L2 to the L1 caches. This is a frequent event for most benchmarks whose working sets do not fit in the L1 cache. Decompression latency is critical since it is directly added to the L2 hit latency. Decompression is a slower process than compression, since prefixes for all words in the line have to be accessed in series, because each prefix is used to determine the length of its corresponding encoded word and therefore the starting location of all the subsequent compressed words. Figure 1 presents a sche-
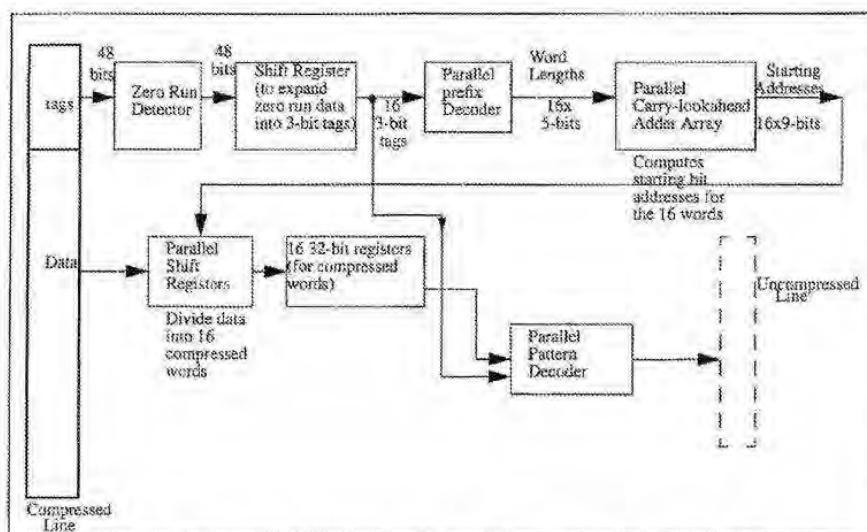
Figure 1. Cache line decompression pipeline for a 64-byte (16-word) cache line.

This is a five-stage pipeline used to decompress a compressed cache line, where each stage contains 12 FO4 gate delays or less. The first pipeline stage (containing the zero run detector, shift register and parallel prefix decoder) decodes the prefix array to determine the length in bits of each word. The second and third stages (Parallel Prefix adder array) compute the starting bit address for each data word by adding the length fields of the preceding words in a hierarchical fashion. The fourth stage (parallel shift registers) contains 16 registers each of which is shifted by the starting address of its word. The fifth and last stage contains the pattern decoder, which decodes the content of each 32-bit register into an uncompressed word according to its corresponding prefix.

matic diagram for a five-stage hardware pipeline that can be used to decompress 64-byte cache lines. Each pipeline stage is 12 FO4 delays or less, assuming the parallel resources required are available for the parallel adder, shift register and pattern decoder. Assuming one processor cycle requires 12 FO4 gate delays, this means that the decompression latency is limited to 5 processor cycles.

5 Evaluation

We evaluate our FPC scheme in terms of its achieved compressibility compared to other compression schemes. We show compression results for our frequent patterns, and demonstrate that zero runs are the most frequent. We also analyze the performance of segmented compression, and the effect of restricting compressed lines to segment boundaries on compression ratios.

5.1 Workloads

To evaluate our design against alternative schemes, we used several multi-threaded commercial workloads from the Wisconsin Commercial Workload Suite [3]. We also used six of the SPEC [24] benchmarks, three from the integer suite (SPECint2000) and three from the floating point suite (SPECfp2000). All of these workloads run under the

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Table 2. Workload Descriptions

Online Transaction Processing (OLTP): DB2 with a TPC-C-like workload. The TPC-C benchmark models the database activity of a wholesale supplier, with many concurrent users performing transactions. Our OLTP workload is based on the TPC-C v3.0 benchmark using IBM's DB2 v7.2 EEE database management system. We use a 5 GB database with 25,000 warehouses stored on eight raw disks and an additional dedicated database log disk. We reduced the number of districts per warehouse, items per warehouse, and customers per district to allow more concurrency provided by a larger number of warehouses. There are 16 simulated users, and the database is warmed up for 100,000 transactions.
Java Server Workload: SPECjbb. SPECjbb2000 is a server-side java benchmark that models a 3-tier system, focusing on the middleware server business logic. We use Sun's HotSpot 1.4.0 Server JVM. Our experiments use two threads and two warehouses, a data size of ~44 MB, and a warmup interval of 200,000 transactions.
Static Web Serving: Apache. We use Apache 2.0.43 for SPARC/Solaris 9, configured to use pthread locks and minimal logging as the web server. We use SURGE [6] to generate web requests. We use a repository of 20,000 files (totalling ~500 MB), and disable Apache logging for high performance. We simulate 400 clients each with 25 ms think time between requests, and warm up for 50,000 requests.
Static Web Serving: Zeus. Zeus is another static web serving workload driven by SURGE. Zeus uses an event-driving server model. Each processor of the system is bound by a Zeus process, which is waiting for web serving event (e.g., open socket, read file, send file, close socket, etc.). The rest of the configuration is the same as Apache (20,000 files of ~500 MB total size, 400 clients, 25 ms think time, 50,000 requests for warmup).
SPEC. We use three integer benchmarks (bzip, gcc, and mcf) and three floating point benchmarks (applu, equake, and swim) from the SPECcpu2000 set to cover a wide range of compressibility properties and working set sizes. We use the first reference input for each benchmark. We warm up caches of each benchmark run for 1 billion instructions.

Solaris 9 operating system. These workloads are briefly described in Table 2. For each data point in our results, we present the average and the 95% confidence interval of multiple simulations to account for space variability [4].

5.2 Compression Ratio

To evaluate the success of our compression scheme, we estimated the compressibility properties of our set of benchmarks. A snapshot is taken of the L2 cache contents for each of these benchmarks after a warm-up interval. Assuming variable-length cache lines that can occupy any number of bits, we compare the compression ratio from our Frequent Pattern Compression scheme (FPC) with two other memory compression schemes:

- The X-RL algorithm [18] used in some compressed cache implementations [21, 19, 20].
- The Block-Referential Compression with Lookahead (BRCL) scheme [14], which is an upper bound for the parallel compression scheme used for memory compression in the IBM MXT technology [26]. We apply it here to cache lines.

We also compare against the "Deflate" algorithm used in the gzip unix utility, which combines an LZ-variant implementation with Huffman encoding of codewords in the dictionary. For this algorithm, we run the gzip utility on the whole cache snapshot file (as opposed to 64-byte lines individually compressed by the other three schemes). The "Deflate" algorithm is used to provide a practical bound on compressibility of dictionary-based schemes for arbitrarily long cache lines.

Figure 2 shows results that compare the four compression schemes. While FPC is faster to implement in hardware, it provides comparable compression ratios to the dictionary-based XRL and BRCL, and even approaches gzip for some benchmarks. FPC is slightly better than XRL and BRCL for the four commercial benchmarks.

7
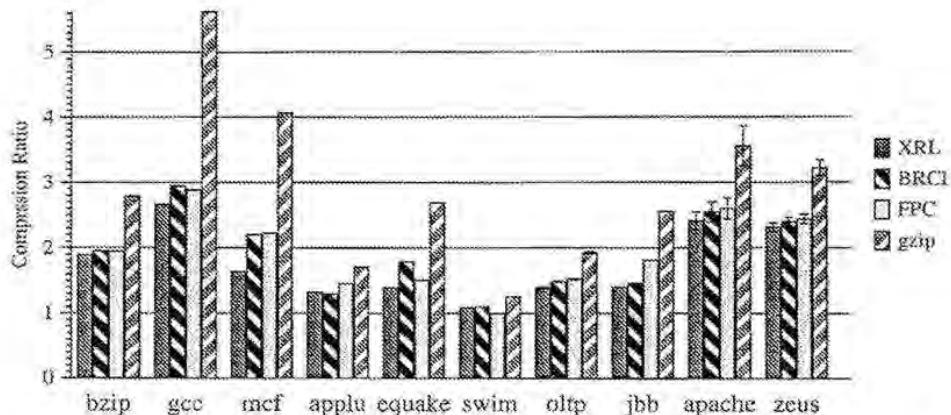
Figure 2. Compression ratios (original size / compressed size) for XRL, BRCL, FPC and gzip
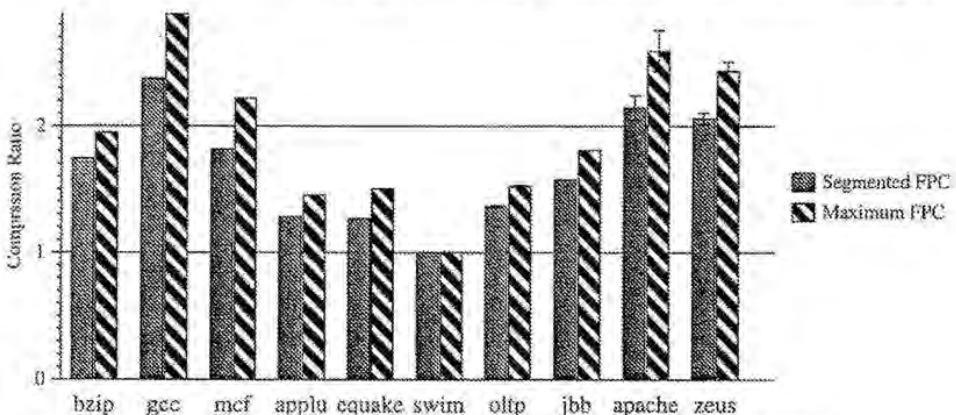

Figure 3. Compression ratios for segmented and variable-length FPC

In most practical cache designs, cache lines cannot occupy any arbitrary number of bits. Restricting the compressed line sizes to a certain subset of all possible lengths (as we do in our segmented design) partially reduces compressibility. To assess this loss in compressibility, we compare the compression ratio from our Segmented Frequent Pattern Compression scheme (Segmented-FPC) against the compression ratio from the Frequent Pattern Compression scheme assuming variable-length lines are possible (Maximum-FPC).

Figure 3 shows the compression ratios from the two schemes for our ten benchmarks. The simple scheme (Segmented-FPC) has compression ratios of 1.7-2.4 for the three SPECint2000 benchmarks, 1.0-1.3 for the three SPECfp2000 benchmarks, 1.4-2.1 for the four commercial benchmarks. OLTP had the lowest compression ratio among our set of commercial benchmarks, since its data is randomly generated. A real OLTP application would have much less randomness, and thus have a higher compression ratio.

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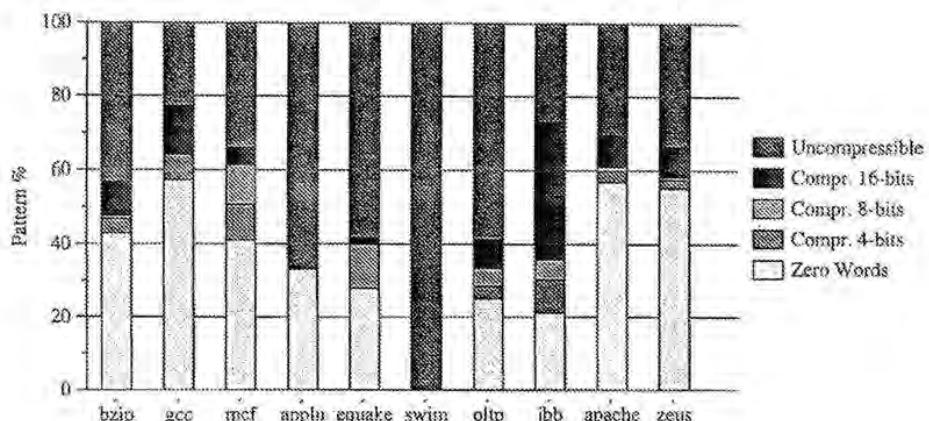
Figure 4. Frequent Pattern Histogram

Compression ratios are higher for all integer benchmarks (1.4-2.4) than floating point benchmarks. For example, only 0.4% of all cache lines in *swim* are compressible. This is because of the nature of floating point benchmarks where floating point numbers might not fit any of the frequent patterns. However, some benefit is still possible for benchmarks with lots of zero words. Segmented-FPC achieved most of the compression benefit from variable-length lines of Maximum-FPC.

5.3 Which Patterns Are Frequent?

Frequent Pattern Compression (FPC) is built on the observation that some word patterns are more frequent than others. We experimented with cache snapshots for our different benchmarks to come up with a reasonable set of frequent patterns (described in Table 1). Figure 4 shows the relative frequency of incompressible words, zero words and words compressible to 4, 8 and 16 bits. The 4-, 8-, and 16-bit patterns are present with various frequencies across our integer and commercial benchmarks. Unfortunately, most of the words in floating point benchmarks are incompressible with FPC, since our patterns are mainly integer patterns.

As Figure 4 demonstrates, zero words are the most frequent compressible pattern across all benchmarks, which is why some compression techniques (e.g., X-RL) specifically optimize for runs of zeros. Figure 5 shows the average number of zeros in a zero run for our set of benchmarks. Except for equake and jbb, the average zero run length for all benchmarks is greater than two. In developing the FPC scheme, we had two options to compress zeros. The first was to have a prefix for each zero word with no data. The second was to encode zero runs with a single prefix and save the length of the run in the data part corresponding to that prefix. However, since most zero runs have more than two (and in most cases three) words, the additional compressibility justifies having special treatment for zero runs.

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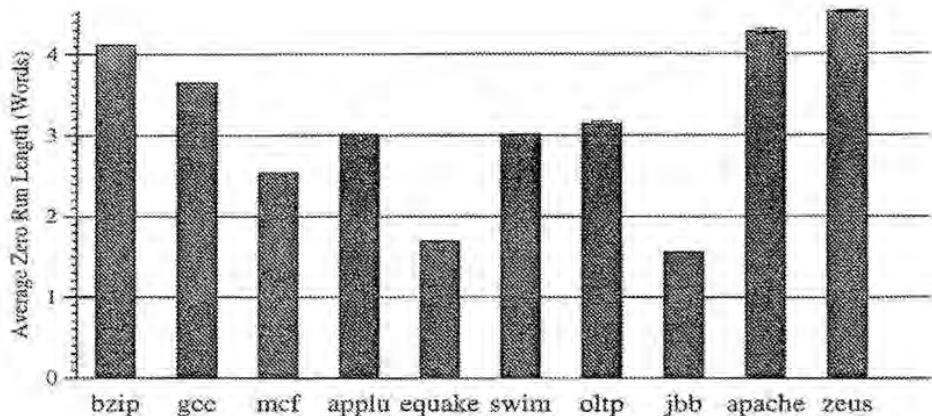
Figure 5. Average number of words in a zero run for our ten benchmarks
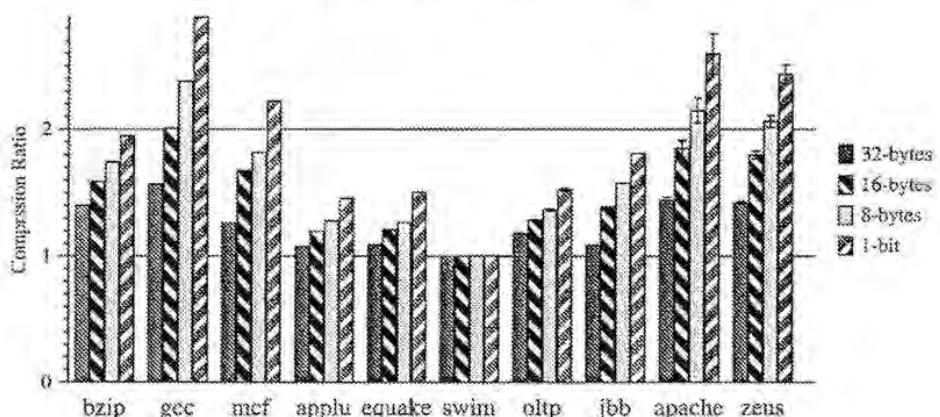
Figure 6. FPC Compression ratios for segment sizes (1 bit to 32 bytes)

5.4 Analysis of Segmented Frequent Pattern Compression

In designing a practical compressed cache implementation, selecting a specific base segment size is critical. A compressed line can only be stored in a size that is an integer multiple of the base segment size. Smaller segments allow for higher compression ratios. On the other hand, larger segments decrease the cache design complexity. Cache design should balance the tradeoff between these two conflicting issues. We selected a base segment size of 8-bytes (i.e., up to 8 segments for 64-byte lines) in our Segmented FPC design.

Figure 6 shows the sensitivity of our compression schemes to the base segment size. The four bars for each benchmark represent compression ratios if we have two possible sizes, i.e., an uncompressed line occupying two segments (32-byte segments), four (16-byte segments), eight (8-byte segments, which is the same as Segmented-FPC in

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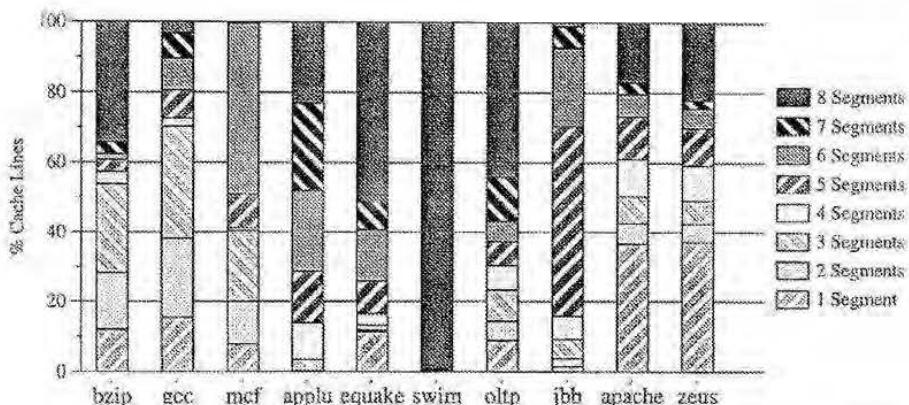
Figure 7. Segment Length Histogram: Percentage of cache lines compressed into 1-8 Segments

Figure 3), and all possible sizes (1-bit segments, the same as Maximum-FPC). Our 8-byte-segment design increases the compression ratio by up to 52% vs. 32-byte segments, and up to 19% vs. 16-byte segments. Figure 7 shows the percentage of lines that can be compressed into 1-8 segments. We show a more detailed distribution in Figure 8, demonstrating the cumulative distribution of compressed cache line sizes (1-512 bits) for our ten benchmarks, as well as the 25th, 50th and 75th percentiles.

6 Conclusion

Cache designers might consider using cache compression to increase cache capacity and reduce off-chip bandwidth. In this document, we propose and evaluate a simple significance-based compression scheme suitable for cache lines, since it has a low compression and decompression overhead. This scheme, Frequent Pattern Compression (FPC) compresses individual cache lines on a word-by-word basis by storing common word patterns in a compressed format accompanied with an appropriate prefix. This simple scheme provides comparable compression ratios to more complex schemes that have higher cache hit latencies.

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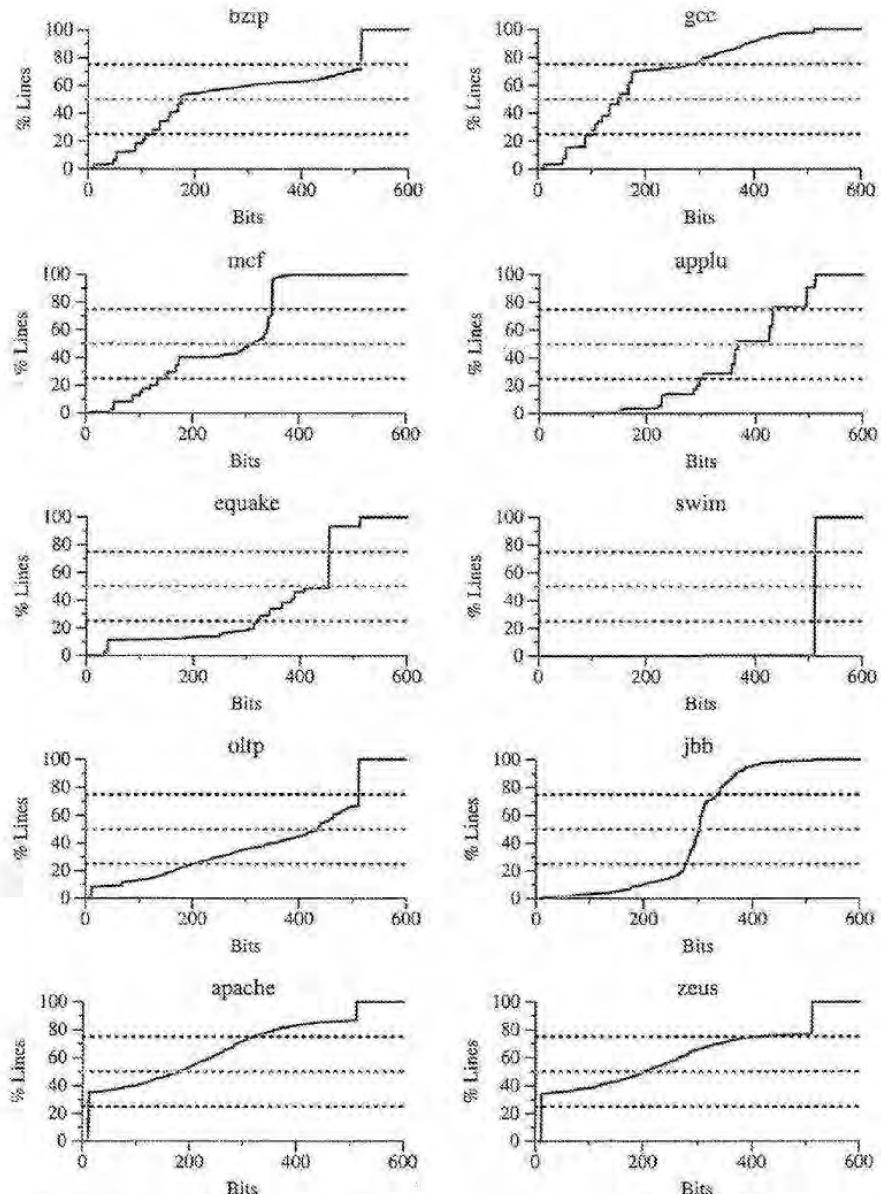
Figure 8. Cumulative Distribution of Compressed Line Lengths (1 to 512 bits). These graphs highlight the 25th, 50th and 75th percentile values.

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