material into a leathery or rubberlike substance. Once the material has cooled below the glass transition temperature,  $T_{\rm r}$ , the polymer becomes stiff and brittle. At the glass transition temperature, the specific volume and enthalpy curves experience a significant change in slope. This can be seen for polystyrene in the enthalpy-temperature curve shown in Fig. 8.1. With semicrystalline thermoplastics, at a crystallization temperature near the melting temperature, the molecules start arranging themselves in small crystalline and amorphous regions, creating a very complicated morphology. During the process of crystalline structure formation, a quantum of energy, often called heat of crystallization or heat of fusion, is released and must be conducted out of the material before the cooling process can continue. The heat of fusion is reflected in the shape of the enthalpy-temperature curve as shown for polyamide 6.6, polyethylene and polypropylene in Fig. 8.1. At the onset of crystalline growth, the material becomes rubbery yet not brittle, since the amorphous regions are still above the glass transition temperature. As seen earlier, the glass transition temperature for some semi-crystalline polymers is far below room temperature, making them tougher than amorphous polymers. For common semi-crystalline polymers, the degree of crystallization can be between 30 and 70%. This means that 30-70% of the molecules form crystals and the rest remain in an amorphous state. The degree of crystallization is highest for those materials with short molecules since they can crystallize faster and more easily.

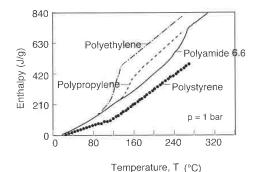
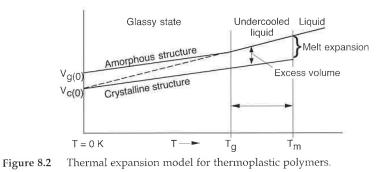


Figure 8.1 Enthalpy as a function of temperature for various thermoplastics.

Figure 8.2 [1] shows the volumetric temperature dependence of a polymer. In the melt state, the chains have "empty spaces" in which molecules can move freely. Hence, undercooled polymer molecules can still move as long as space is available. The point at which this free movement ends for a molecule or segment of chains is called the glass transition temperature or solidification point. As pointed out in Fig. 8.2, the free volume is frozen-in as well. In the case

of crystallization, ideally, the volume should jump to a lower specific volume. However even here, small amorphous regions remain which permit a slow flow or material creep. This free volume reduces to nothing at absolute zero temperature at which heat transport can no longer occur.



The specific volume of a polymer changes with pressure even at the glass transition temperature. This is demonstrated for an amorphous thermoplastic in Fig. 8.3 and for a semi-crystalline thermoplastic in Fig. 8.4.

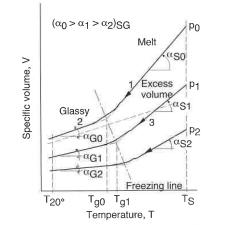
It should be noted here that the size of the frozen-in free volume depends on the rate at which a material is cooled; high cooling rates result in a large free volume. In practice this is very important. When the frozen-in free volume is large, the part is less brittle. On the other hand, high cooling rates lead to parts that are highly permeable, which may allow the diffusion of gases or liquids through container walls. The cooling rate is also directly related to the dimensional stability of the final part. The effect of high cooling rates can often be mitigated by heating the part to a temperature that enables the molecules to move freely; this will allow further crystallization by additional chain folding. This process has a great effect on the structure and properties of the crystals and is referred to as *annealing*. In general, this only signifies a qualitative improvement of polymer parts. It also affects shrinkage and warpage during service life of a polymer component, especially when thermally loaded.

All these aspects have a great impact on processing. For example, when extruding amorphous thermoplastic profiles, the material can be sufficiently cooled inside the die so that the extrudate has enough rigidity to carry its own weight as it is pulled away from the die. Semi-crystalline polymers with low molecular weights have a viscosity above the melting temperature that is too low to be able to withstand their own weight as the extrudate exits the die. Temperatures below the melting temperature,  $T_{ur}$ , however cannot be used due to solidification inside the die. Similar problems are encountered in the

#### 8 Solidification of Polymers 323



weight.



thermoforming process in which the material must be heated to a point so that it can be formed into its final shape, yet has to be able to withstand its own



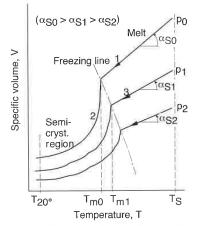


Figure 8.4 Schematic of a p-v-T diagram for semi-crystalline thermoplastics.

Semi-crystalline polymers are also at a disadvantage in the injection molding process. Because of the heat needed for crystallization, more heat must

be removed to solidify the part; and since there is more shrinkage, longer packing times and larger pressures must be employed. All this implies longer cycle times and more shrinkage. High cooling rates during injection molding of semi-crystalline polymers will reduce the degree of crystallization. However, the amorphous state of the polymer molecules may lead to some crystallization after the process, which will result in further shrinkage and warpage of the final part. It is quite common to follow the whole injection molding process in the p-v-T diagrams presented in Figs. 8.3 and 8.4, and thus predict how much the molded component has shrunk.

# 8.1.2 Morphological Structure

Morphology is the order or arrangement of the polymer structure. The possible "order" between a molecule or molecule segment and its neighbors can vary from a very ordered highly crystalline polymeric structure to an amorphous structure (i.e., a structure in greatest disorder or random). The possible range of order and disorder is clearly depicted on the left side of Fig. 8.5. For example, a purely amorphous polymer is formed only by the non-crystalline or amorphous chain structure, whereas the semi-crystalline polymer is formed by a combination of all the structures represented in Fig. 8.5.

The image of a semi-crystalline structure as shown in the middle of Fig. 8.5, can be captured with an electron microscope. A macroscopic structure, shown in the right hand side of the figure, can be captured with an optical microscope. An optical microscope can capture the coarser macromorphological structure such as the spherulites in semi-crystalline polymers.

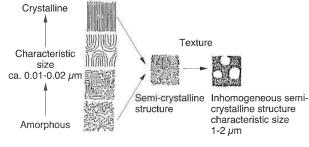
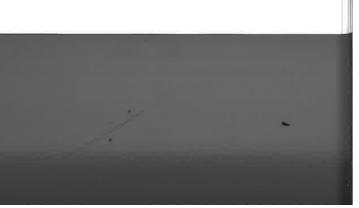


Figure 8.5 Schematic diagram of possible molecular structure which occur in thermoplastic polymers.

An amorphous polymer is defined as having a purely random structure. However it is not quite clear if a "purely amorphous" polymer as such exists. Electron microscopic observations have shown amorphous polymers that are

8 Solidification of Polymers 325



composed of relatively stiff chains, show a certain degree of macromolecular structure and order, for example, globular regions or fibrilitic structures. Nevertheless, these types of amorphous polymers are still found to be optically isotropic. Even polymers with soft and flexible macromolecules, such as polvisoprene which was first considered to be random, sometimes show bandlike and globular regions. These bundle-like structures are relatively weak and short-lived when the material experiences stresses. The shear thinning viscosity effect of polymers sometimes is attributed to the breaking of such macromolecular structures.

## 8.1.3 Crystallization

Early on, before the existence of macromolecules had been recognized, the presence of highly crystalline structures had been suspected. Such structures were discovered when undercooling or when stretching cellulose and natural rubber. Later, it was found that a crystalline order also existed in synthetic macromolecular materials such as polyamides, polyethylenes, and polyvinyls. Because of the polymolecularity of macromolecular materials, a 100% degree of crystallization cannot be achieved. Hence, these polymers are referred to as semi-crystalline. It is common to assume that the semi-crystalline structures are formed by small regions of alignment or crystallites connected by random or amorphous polymer molecules.

With the use of electron microscopes and sophisticated optical microscopes the various existing crystalline structures are now well recognized. They can be listed as follows:

- Single crystals. These can form in solutions and help in the study of crystal formation. Here, plate-like crystals and sometimes whiskers are generated.
- Spherulites. As a polymer melt solidifies, several folded chain lamellae spherulites form which are up to 0.1 mm in diameter. A typical example of a spherulitic structure is shown in Fig. 8.6 [2]. The spherulitic growth in a polypropylene melt is shown in Fig. 8.7 [3].
- Deformed crystals. If a semi-crystalline polymer is deformed while undergoing crystallization, oriented lamellae form instead of spherulites.
- Shish-kebab. In addition to spherulitic crystals, which are formed by plate- and ribbonlike structures, there are also shish-kebab, crystals which are formed by circular plates and whiskers. Shish-kebab structures are generated when the melt undergoes a shear deformation during solidification. A typical example of a shish-kebab crystal is shown in Fig. 8.8 [4].

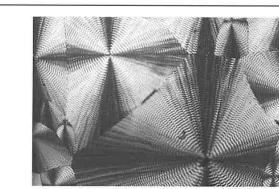






Figure 8.7 taken at 30 s intervals.

written as follows:

8 Solidification of Polymers 327

Figure 8.6 Polarized microscopic image of the spherulitic structure in polypropylene.



- Development of the spherulitic structure in polypropylene. Images were
- The crystallization fraction can be described by the Avrami equation [5],



MacNeil Exhibit 2117 Yita v. MacNeil IP, IPR2020-01139 Page 174

$$x(t) = 1 - e^{-Zt''}$$
(8.1)

where *Z* is a molecular weight and temperature dependent crystallization rate and *n* the Avrami exponent. However, since a polymer cannot reach 100% crystallization the above equation should be multiplied by the maximum possible degree of crystallization,  $x_{\infty}$ .

x(t)

$$) = x_{\infty} \left( 1 - e^{-Z t^{n}} \right) \tag{8.2}$$

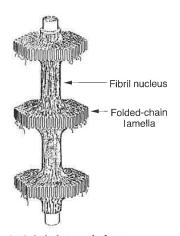


Figure 8.8 Model of the shish-kebab morphology.

The Avrami exponent, *n*, ranges between 1 and 4 depending on the type of nucleation and growth. For example, the Avrami exponent for spherulitic growth from sporadic nuclei is around 4, disclike growth 3, and rodlike growth 2. If the growth is activated from instantaneous nuclei, the Avrami exponent is lowered by 1.0 for all cases. The crystalline growth rate of various polymers differ significantly from one to another. This is demonstrated in Table 8.1 which shows the maximum growth rate for various thermoplastics. The crystalline mass fraction can be measured experimentally with a differential scanning calorimeter (DSC).

A more in-depth coverage of crystallization and structure development during processing is given by Eder and Janeschitz-Kriegl [7].

Table 8.1         Maximum Crystalline Growth Rate and Maximum Degree           Crystallinity for Various Thermoplastics						
Polymer	Growth rate (μ/min)	Maximum crystallinity (%)				
Polyethylene	>1000	80				
Polyamide 66	1000	70				
Polyamide 6	200	35				
Isotactic polypropylene	20	63				
Polyethylene terephthalate	7	50				
Isotactic polystyrene	0.30	32				
Polycarbonate	0.01	25				

# 8.1.4 Heat Transfer During Solidification

Since polymer parts are generally thin, the energy equation<sup>1</sup> can be simplified to a one-dimensional problem. Thus, using the coordinate description shown in Fig. 8.9 the energy equation can be reduced to

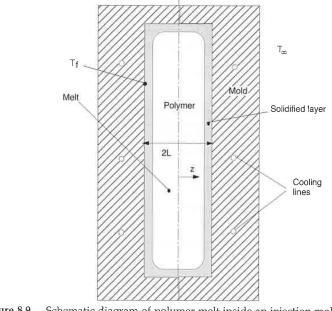
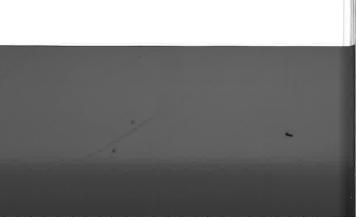


Figure 8.9 Schematic diagram of polymer melt inside an injection mold.

<sup>1</sup> The energy equation is discussed in Chapter 3 and can be found in its complete form in Appendix A.

8	Solidification	of Polymers	329



MacNeil Exhibit 2117 Yita v. MacNeil IP, IPR2020-01139 Page 175

$$\rho C_p \frac{\partial T}{\partial t} = k \frac{\partial^2 T}{\partial z^2} \tag{8.3}$$

Another assumption - and to reduce warpage, usually a requirement - is a symmetry boundary condition:

$$\frac{\partial T}{\partial z} = 0 \quad \text{at} \quad z = 0 \tag{8.4}$$

If the sheet is cooled via forced convection or the part is inside a perfectly cooled mold, the final temperature of the part can be assumed to be the second boundary condition:

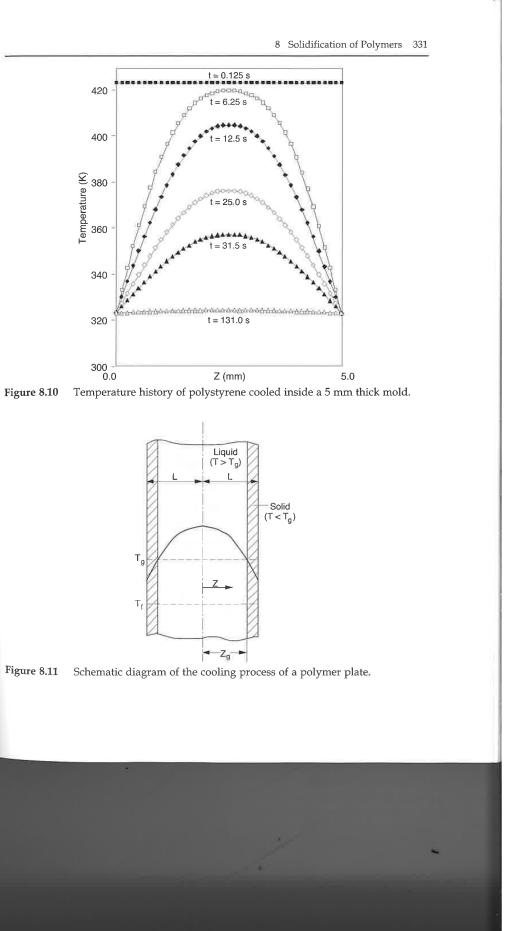
$$T = T_f \tag{8.5}$$

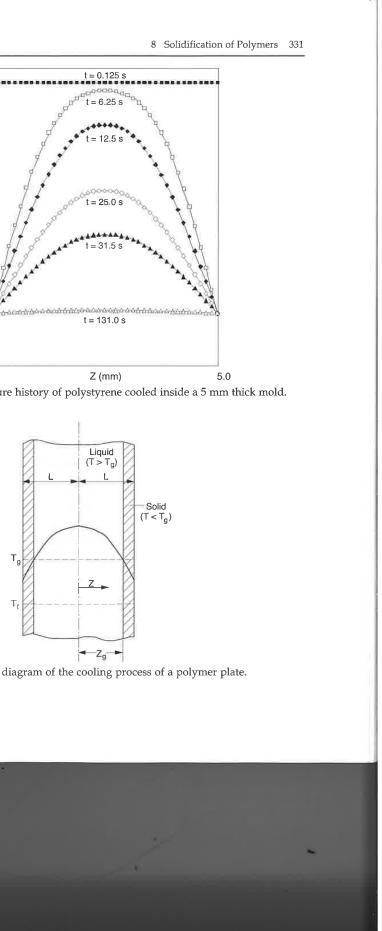
A typical temperature history for a polystyrene plate, its properties presented in Table 8.2 [8], is shown in Fig. 8.10. Once the material's temperature drops below the glass transition temperature,  $T_{g}$ , it can be considered solidified. This is shown schematically in Fig. 8.11. Of importance here is the position of the solidification front, X(t). Once the solidification front equals the plate's dimension L, the solidification process is complete. From Fig. 8.10 it can be shown that the rate of solidification decreases as the solidified front moves further away from the cooled surface. For amorphous thermoplastics, the wellknown Neumann solution can be used to estimate the growth of the glassy or solidified layer. The Neumann solution is written as

$$X(t) \propto \sqrt{\alpha t} \tag{8.6}$$

Material Properties for Polystyrene Table 8.2

	K	=	0.117 W/mK
	Ср	=	1185 J/kgK
	ρ	=	1040 kg/m <sup>3</sup>
	Тg	=	80 °C
	Е	=	3.2E9 Pa
	v	=	0.33
_			





MacNeil Exhibit 2117 Yita v. MacNeil IP, IPR2020-01139 Page 176

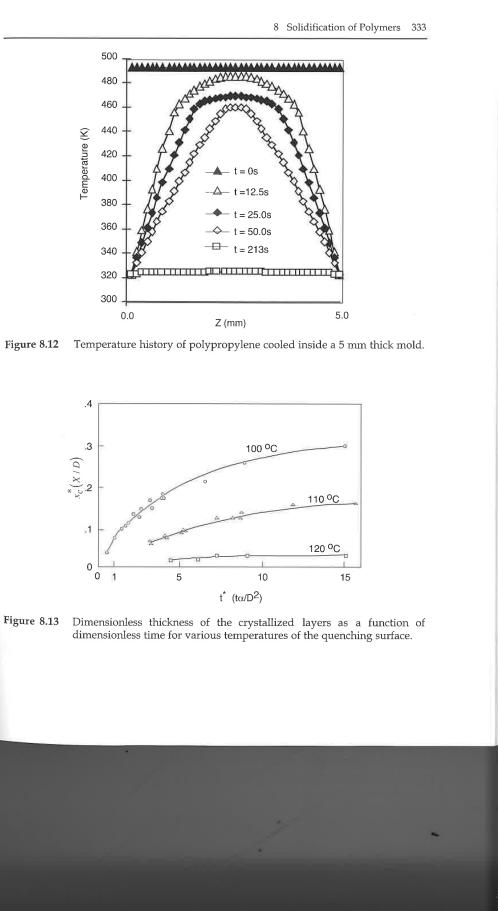
where  $\alpha$  is the thermal diffusivity of the polymer. It must be pointed out here that for the Neumann solution, the growth rate of the solidified layer is infinite as time goes to zero.

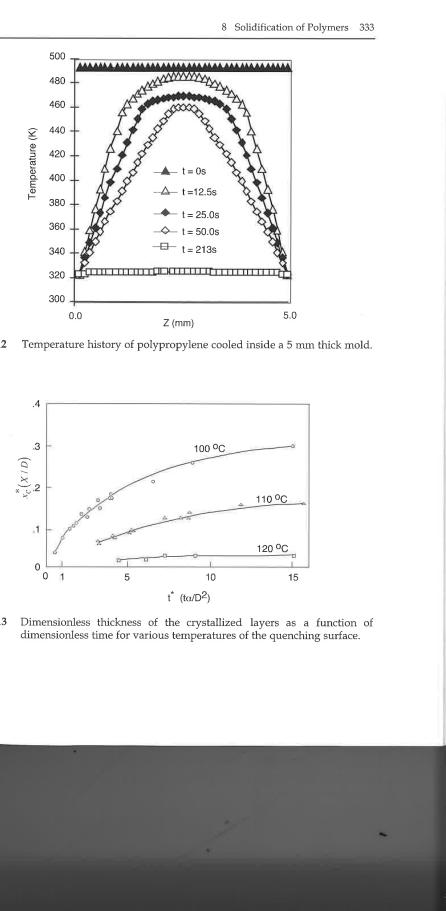
The solidification process in a semi-crystalline materials is a bit more complicated due to the heat of fusion or heat of crystallization, nucleation rate, etc. When measuring the specific heat as the material crystallizes, a peak which represents the heat of fusion is detected (see Fig. 4.12). Figure 8.12 shows the calculated temperature distribution in a semi-crystalline polypropylene plate during cooling. The material properties used for the calculations are shown in Table 8.3 [8]. Here, the material that is below the melting temperature,  $T_{w}$ , is considered solid<sup>2</sup>. Experimental evidence [9] has demonstrated that the growth rate of the crystallized layer in semi-crystalline polymers is finite. This is mainly due to the fact that at the beginning the nucleation occurs at a finite rate. Hence, the Neumann solution presented in Eq. 8.6 as well as the widely used Stefan condition [10], do not hold for semi-crystalline polymers. This is clearly demonstrated in Fig. 8.13 [10] which presents measured thickness of crystallized layers as a function of time for polypropylene plates quenched at three different temperatures. For further reading on this important topic the reader is encouraged to consult the literature [11, 12].

> Material Properties for Polypropylene Table 8.3

	-	
К		= 0.117 W/mK
C <sub>p, solid</sub>	=	1800 J/kgK
C <sub>p, melt</sub>	=	2300 J/kgK
ρ	=	930 kg/m <sup>3</sup>
Тg	=	-18 °C
Tm	=	186 °C
λ	=	209 kJ/kg

 $\overline{2}$  It is well-known that the growth of the crystalline layer in semi-crystalline polymers is maximal somewhat below the melting temperature, at a temperature  $T_c$ . The growth speed of nuclei is zero at the melting temperature and at the glass transition temperature.





MacNeil Exhibit 2117 Yita v. MacNeil IP, IPR2020-01139 Page 177

## 8.2 Solidification of Thermosets

The solidification process of thermosets, such as phenolics, unsaturated polyesters, epoxy resins, and polyurethanes is dominated by an exothermic chemical reaction called curing reaction. A curing reaction is an irreversible process that results in a structure of molecules that are more or less crosslinked. Some thermosets cure under heat and others cure at room temperature. Thermosets that cure at room temperature are those for which the reaction starts immediately after mixing two components, where the mixing is usually part of the process. However, even with these thermosets, the reaction is accelerated by the heat released during the chemical reaction, or the exotherm. In addition, it is also possible to activate cross-linking by absorption of moisture or radiation, such as ultra-violet, electron beam, and laser energy sources [13].

In processing, thermosets are often grouped into three distinct categories, namely those that undergo a heat activated cure, those that are dominated by a mixing activated cure, and those which are activated by the absorption of humidity or radiation. Examples of heat activated thermosets are phenolics; examples of mixing activated cure are epoxy resins and polyurethane.

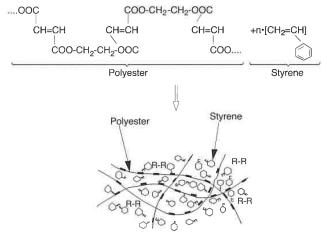
# 8.2.1 Curing Reaction

In a cured thermoset, the molecules are rigid, formed by short groups that are connected by randomly distributed links. The fully reacted or solidified thermosetting polymer does not react to heat as observed with thermoplastic polymers. A thermoset may soften somewhat upon heating and but then degrades at high temperatures. Due to the high cross-link density, a thermoset component behaves as an elastic material over a large range of temperatures. However, it is brittle with breaking strains of usually 1 to 3%. The most common example is phenolic, one of the most rigid thermosets, which consists of carbon atoms with large aromatic rings that impede motion, making it stiff and brittle. Its general structure after cross-linking is given in Figs. 3.22 and 3.23.

Thermosets can be broken down into three categories: thermosets which cure via condensation polymerization, those that undergo addition polymerization and those that cure via *free radiacal polymerization*.

Condensation polymerization is defined as the growth process that results from combining two or more monomers with reactive end-groups, and leads to by-products such as an alcohol, water, an acid, etc. A common thermoset that polymerizes or solidifies via condensation polymerization is phenol formaldehyde, discussed in Chapter 3. The by-product of the reaction when making phenolics is water. Examples of addition polymerization are polyurethanes and epoxies.

An example of a cross-linking reaction of a thermoset by free radical reaction is the co-polymerization of unsaturated polyester with styrene molecules, shown in Fig. 8.14. The molecules contain several carbon-carbon double bonds which act as cross-linking sites during curing. An example of the resulting network after the chemical reaction is shown in Fig. 8.15.





polyester.

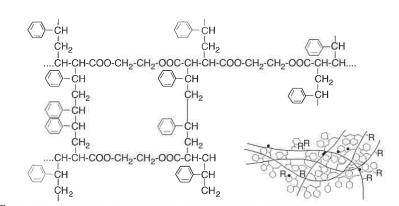
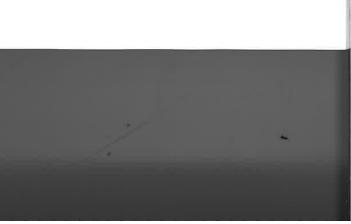


Figure 8.15 Symbolic and schematic representations of cured unsaturated polyester.

8 Solidification of Polymers 335

Figure 8.14 Symbolic and schematic representations of uncured unsaturated



MacNeil Exhibit 2117 Yita v. MacNeil IP, IPR2020-01139 Page 178

#### 8.2.2 Cure Kinetics

As discussed earlier, in processing thermosets can be grouped into two general categories: *heat activated cure* and *mixing activated cure* thermosets. However, no matter which category a thermoset belongs to, its curing reaction can be described by the reaction between two chemical groups denoted by *A* and *B* which link two segments of a polymer chain. The reaction can be followed by tracing the concentration of unreacted *As* or *Bs*, *C*<sub>A</sub> or *C*<sub>B</sub>. If the initial concentration of *As* and *Bs* is defined as *C*<sub>A0</sub> and *C*<sub>B0</sub>, the degree of cure can be described by

$$C^* = \frac{C_{A_0} - C_A}{C_{A_0}} \tag{8.7}$$

The degree of cure or conversion,  $C^*$ , equals zero when there has been no reaction and equals one when all *As* have reacted and the reaction is complete. However, it is impossible to monitor reacted and unreacted *As* and *Bs* during the curing reaction of a thermoset polymer. It is known though that the exothermic heat released during curing can be used to monitor the conversion,  $C^*$ . When small samples of an unreacted thermoset polymer are placed in a differential scanning calorimeter (DSC), each at a different temperature, every sample will release the same amount of heat,  $Q_T$ . This occurs because every cross-linking that occurs during a reaction releases a small amount of energy in the form of heat. For example, Fig. 8.16 [14] shows the heat rate released during isothermal cure of a vinyl ester at various temperatures.

The degree of cure can be defined by the following relation

$$C^* = \frac{Q}{Q_T} \tag{8.8}$$

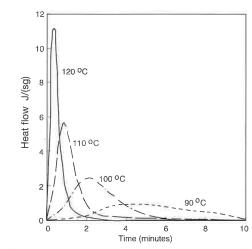
where Q is the heat released up to an arbitrary time  $\tau$ , and is defined by

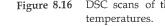
$$Q = \int_{0}^{t} \dot{Q} dt \tag{8.9}$$

DSC data is commonly fitted to empirical models that accurately describe the curing reaction. Hence, the rate of cure can be described by the exotherm,  $\dot{Q}$ , and the total heat released during the curing reaction,  $Q_T$ , as

$$\frac{dC^*}{dt} = \frac{Q}{Q_T} \tag{8.10}$$

With the use of Eq. 8.10, it is now easy to take the DSC data and find the models that describe the curing reaction.

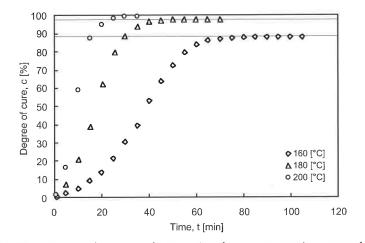


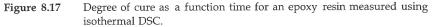


During cure, thermoset resins exhibit three distinct phases; viscous liquid, gel, and solid. Each of these three stages is marked by dramatic changes in the thermomechanical properties of the resin. The transformation of a reactive thermosetting liquid to a glassy solid generally involves two distinct macroscopic transitions: molecular gelation and vitrification. Molecular gelation is defined as the time or temperature at which covalent bonds connect across the resin to form a three-dimensional network which gives rise to long range elastic behavior in the macroscopic fluid. This point is also referred to as the gel point, where  $C^* = C_a$ . As a thermosetting resin cures, the cross-linking begins to hinder molecular movement, leading to a rise in the glass transition temperature. Eventually, when  $T_{a}$  nears the processing temperature, the rate of curing reduces significantly, eventually dominated by diffusion. At this point the resin has reached its vitrification point. Figure 8.17, which presents degree of cure as a function of time, illustrates how an epoxy resin reaches a maximum degree of cure at various processing temperatures. The resin processed at 200 °C reaches 100% cure since the glass transition temperature of fully cure epoxy is 190 °C, less than the processing temperature. On the other hand, the sample processed at 180 °C reaches 97% cure and the one processed at 160 °C only reaches 87% cure.

Figure 8.16 DSC scans of the isothermal curing reaction of vinyl ester at various

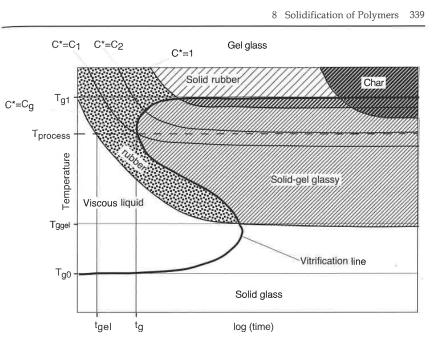






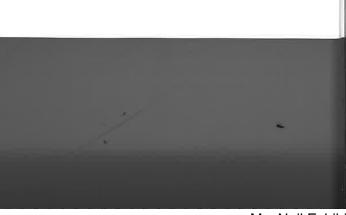
Figures 8.16 and 8.17 also illustrate how the curing reaction is accelerated as the processing temperature is increased. The curing reaction of thermally cured thermoset resins is not immediate, thus the blend can be stored in a refrigerator for a short period of time without having any significant curing reaction.

The behavior of curing thermosetting resins can be represented with the generalized time-temperature-transformation (TTT) cure diagram developed by Enns and Gillham [16]; it can be used to relate the material properties of thermosets as a function of time and the processing temperature as shown in Fig. 8.18.



The diagram presents various lines that represent constant degrees of cure. The curve labeled  $C^* = C_a$  represents the gel point and  $C^* = 1$  the fully cured resin. Both curves have their corresponding glass transition temperatures,  $T_{e_1}$ and  $T_{\text{excl}}$  for the glass transition temperature of the fully cured resin and at its gel point, respectively. The glass transition temperature of the uncured resin,  $T_{r0'}$  and an S-shaped curve labeled "vitrification line," are also depicted. The vitrification line represents the boundary where the glass transition temperature becomes the processing temperature. Hence, to the left of the vitrification curve the curing process is controlled by a very slow diffusion process. The TTTdiagram shows an arbitrary process temperature. The material being processed reaches the gel point at  $t = t_{rel}$  and the vitrification line at  $t = t_r$ . At this point the material has reached a degree of cure of  $C_1$  and glass transition temperature of the resin is equal to the processing temperature. The material continues to cure very slowly (diffusion controlled) until it reaches a degree of cure just below  $C_2$ . There are also various regions labeled in the diagram. The one labeled "viscous liquid" is the one where the resin is found from the beginning of processing until the gel point has been reached. The flow and deformation that occurs during processing or shaping must occur within this region. The region labeled "char" must be avoided during processing, since at high

Figure 8.18 Time-temperature-transformation (TTT) diagram for a thermoset



processing temperatures the polymer will eventually undergo thermal degradation.

The model that best represents the curing kinetics of thermosetting resins as reflected in a TTT-diagram is a diffusion modified Kamal-Sourour reaction model [17, 18, 19]. To model autocatalytic cure kinetics, the model can be applied as

$$\frac{dC^*}{dt} = \left(k_1 + k_2 C^{*m}\right) \left(1 - C^*\right)^{(n)}$$
(8.11)

where *m* and *n* are reaction orders, and  $k_1$  and  $k_2$  are constants defined by

$$=\frac{1}{k_{1}^{c}}+\frac{1}{k_{D}}$$
(8.12)

Here,  $k_i^c$  are Arrhenius overall rate constants defined by

$$c = a_1 e^{-h_{kr}}$$
(8.13)

and

$$k_2^c = a_{2\ell} e^{-L_2^c/_{RT}} \tag{8.14}$$

where  $a_1$  and  $a_2$  are fitting parameters,  $E_1$  and  $E_2$ , activation energies and R the ideal gas constant. The constant  $k_p$  in Eq. 8.12 is the diffusion rate constant defined as

$$k_{D} = a_{D} e^{-k_{D}} k_{T} e^{-k_{D}}$$
(8.15)

where  $a_0$  and b are adjustable parameters,  $E_0$  is the activation energy of the diffusion process, and *f* is the equilibrium fractional free volume given by

$$f = 0.00048 (T - T_s) + 0.025$$
(8.16)

where  $T_{e}$  is the instantaneous glass transition temperature during cure. Equation (8.12) shows that the overall rate constant is governed at one extreme by the Arrhenius rate constant when  $k_p >> k_i^c$ , which is the case prior to vitrification, and at the other extreme by the diffusion rate constant when  $k_0 << k_c^{i}$ , which is the case well after vitrification. For a system exhibiting a unique one-to-one relationship between the glass transition temperature and conversion, DiBenedetto's equation [20] is one of the easiest approaches for stoichiometric ratios to express this relationship using only a single parameter as

 $T_{g} = 2$ 

where  $T_{e0}$  is the glass transition temperature of the uncured resin,  $T_{e1}$  is the glass transition temperature of the fully reacted network, and  $\lambda$  is a structure dependent parameter theoretically equated to

Mixing activated cure materials such as polyurethanes will instantly start releasing exothermic heat after the mixture of its two components has occurred. The proposed Castro-Macosko curing model accurately fits this behavior and is written as [15]

$$\frac{dC}{dt}$$

# 8.2.3 Heat Transfer During Cure

A well-known problem in thick section components is that the thermal and curing gradients become more complicated and difficult to analyze since the temperature and curing behavior of the part is highly dependent on both the mold temperature and part geometry [21, 22]. A thicker part will result in higher temperatures and a more complex cure distribution during processing. This phenomenon becomes a major concern during the manufacture of thick components since high temperatures may lead to thermal degradation. A relatively easy way to check temperatures that arise during molding and curing or demolding times is desired. For example, a one-dimensional form of the energy equation that includes the exothermic energy generated during curing can be solved:

```
\rho C_{p}
```

Assuming the material is confined between two mold halves at equal temperatures, the use of a symmetric boundary condition at the center of the part is valid:

8 Solidification of Polymers 341

$$T_{g0} + \frac{\left(T_{g1} - T_{g0}\right)\lambda C^{*}}{1 - (1 - \lambda)C^{*}}$$
(8.17)

$$\lambda = \frac{\Delta C_{\rho 0}}{\Delta C_{\rho 1}} \tag{8.18}$$

The values of  $\Delta C_{a0}$  and  $\Delta C_{a1}$  are the differences in the heat capacity between the glassy and rubbery state for the uncured resin and the fully cured network, respectively. However the parameter  $\lambda$  can also be used as fitting parameter.

$$=k_0 e^{-\frac{E}{\sqrt{RT}}} \left(1 - C^*\right)^2$$
(8.19)

$$\frac{\partial T}{\partial t} = k \frac{\partial^2 T}{\partial z^2} + \rho \dot{Q}$$
(8.20)



MacNeil Exhibit 2117 Yita v. MacNeil IP, IPR2020-01139 Page 181

$$\frac{\partial T}{\partial z} = 0 \quad \text{at} \quad z = 0 \tag{8.21}$$

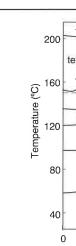
and

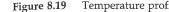
 $T = T_m$ (8.22)

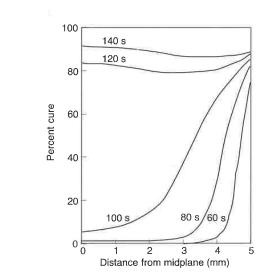
at the mold wall.

With the use of the finite difference technique and a six constant model that represents  $dC^*/dt$ , Barone and Caulk [23] solved Eqs. 8.20–8.22 for the curing of sheet molding compound (SMC). The SMC was composed of an unsaturated polyester resin with 40.7% calcium carbonate and 30% glass fiber by weight. Figures 8.19 and 8.20 show typical temperature and degree of cure distributions, respectively, during the solidification of a 10 mm thick part as computed by Barone and Caulk. In Fig. 8.19, the temperature rise resulting from exothermic reaction is obvious. This temperature rise increases in thicker parts and with increasing mold temperatures. Figure 8.21 is a plot of the time to reach 80% cure versus thickness of the part for various mold temperatures. The shaded area represents the conditions at which the internal temperature within the part exceeds 200 °C because of the exothermic reaction. Temperatures above 200 °C can lead to material degradation and high residual stresses in the final part.

Improper processing conditions can result in a non-uniform curing distribution which may lead to voids, cracks, or imperfections inside the part. It is of great importance to know the appropriate processing conditions which will both avoid the over-heating problem and speed up the manufacturing process.







8 Solidification of Polymers 343

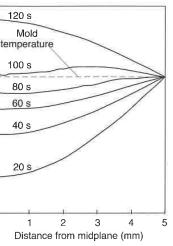
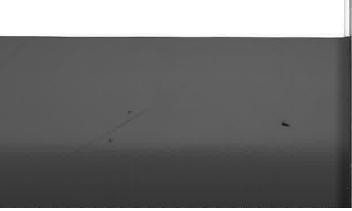
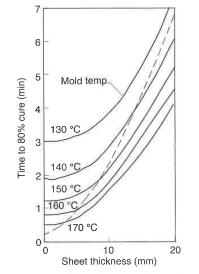


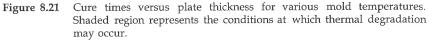
Figure 8.19 Temperature profile history of a 10 mm thick SMC plate.

Figure 8.20 Curing profile history of a 10 mm thick SMC plate.



MacNeil Exhibit 2117 Yita v. MacNeil IP, IPR2020-01139 Page 182





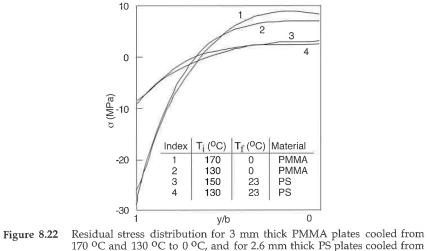
# 8.3 Residual Stresses and Warpage of Polymeric Parts

Some major problems encountered when molding polymeric parts are the control and prediction of the component's shape at room temperature. For example, the resulting sink marks in the final product are caused by the shrinkage of the material during cooling<sup>3</sup> or curing. A common geometry that usually leads to a sink mark is a ribbed structure. The size of the sink mark, which is often only a cosmetic problem, is not only related to the material and processing conditions but also to the geometry of the part. A rib that is thick in relation to the flange thickness will result in significant sinking on the flat side of the part.

Warpage in the final product is often caused by processing conditions that cause unsymmetric residual stress distributions through the thickness of the part. Thermoplastic parts most affected by residual stresses are those that are manufactured with the injection molding process. The formation of residual stresses in injection molded parts is attributed to two major coupled factors:

3 In injection molding one can mitigate this problem by continuously pumping polymer melt into the mold cavity as the part cools until the gate freezes shut.

cooling and flow stresses. The first and most important factor is the residual stress that is formed because of the rapid cooling or quenching of the part inside the mold cavity. As will be discussed and explained later in this chapter, this dominant factor is the reason why most thermoplastic parts have residual stresses that are tensile in the central core of the part and compressive on the surface. Typical residual stress distributions are shown in Fig. 8.22 [24], which presents experimental<sup>4</sup> results for PMMA and PS plates cooled at different conditions.



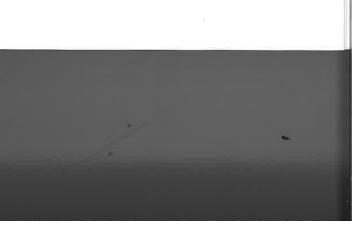
150 °C and 130 °C to 23 °C.

Residual stresses in injection molded parts are also formed by the shear and normal stresses that exist during flow of the polymer melt inside the mold cavity during the filling and packing stage. These tensile flow induced stresses are often very small compared to the stresses that build up during cooling. However, at low injection temperatures, these stresses can be significant in size, possibly leading to parts with tensile residual stresses on the surface. Figure 8.23 [25] demonstrates this concept with PS plates molded at different injection temperatures. The figure presents residual stress distributions through the thickness of the plate perpendicular and parallel to the flow direction. Isayev [24, 25] has also demonstrated that flow stresses are maximum near the gate. The resulting tensile residual stresses are of particular concern since they may lead to stress cracking of the polymer component.

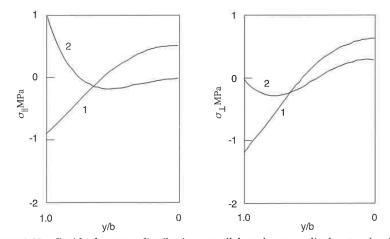
8 Solidification of Polymers 345

170 °C and 130 °C to 0 °C, and for 2.6 mm thick PS plates cooled from

4 The experimental residual stress distributions where directly computed from curvature measurements



obtained by the layer removal method.



**Figure 8.23** Residual stress distribution parallel and perpendicular to the flow direction for a 2.54 mm thick PS plate cooled from 244 °C (1) and 210 °C (2) to 60 °C

The development of models and simulations to predict shrinkage and warpage in the manufacturing of plastic parts is necessary to understand and control the complex thermomechanical behavior the material undergoes during processing. Shrinkage and warpage result from material inhomogeneities and anisotropy caused by mold filling, molecular or fiber orientation, curing or solidification behavior, poor thermal mold lay-out, and improper processing conditions. Shrinkage and warpage are directly related to residual stresses. Transient thermal or solidification behavior as well as material anisotropies can lead to the build-up of residual stresses during manufacturing. Such process-induced residual stresses can significantly affect the mechanical performance of a component by inducing warpage or initiating cracks and delamination in composite parts. It is hoped that an accurate prediction of the molding process and the generation of residual stresses will allow for the design of better molds with appropriate processing conditions.

This section presents basic concepts of the thermomechanical behavior during the manufacturing process of polymeric parts. The formation of residual stresses during the fabrication of plastic parts is introduced first, followed by a review of simple models used to compute residual stresses and associated warpage of plates and beams under different thermal loadings. Several models, which characterize the transient mechanical and thermomechanical behavior of thermoplastic polymers will be reviewed and discussed next. Using these existing models, residual stresses, shrinkage, and warpage of injection molded thermoplastic parts can be predicted. Furthermore, results from the literature are presented. Since thermoset polymers behave quite differently from thermoplastic polymers during molding, other models need to be introduced to compute the thermomechanical behavior of thermoset polymers. Based on these models, results for predicting residual stresses and the resulting shrinkage and warpage for both thin and thick thermoset parts are also discussed.

# 8.3.1 Residual Stress Models

The formation of residual stresses is most critical during the solidification of polymer components inside injection molds. To illustrate residual stress buildup during injection molding, the plate shaped injection molding cavity shown in Fig. 8.9 is considered. As a first order approximation, it can be assumed that a hard polymer shell forms around the melt pool as the material is quenched by the cool mold surfaces. Neglecting the packing stage during the injection molding cycle, this rigid frame contains the polymer as it cools and shrinks during solidification. The shrinkage of the polymer is, in part, compensated by the deflection of the rigid surfaces, a deformation that occurs with little effort. In fact, if the packing stage is left out, it is a common experimental observation that between 85 to 90% of the polymer's volumetric changes are compensated by shrinkage through the thickness of the part [26]. To understand which material properties, boundary conditions, and processing conditions affect the residual stresses in a solidified polymer component, the cooling process of an injection molded amorphous polymer plate, as it cools inside the mold cavity, will be considered. For simplicity, in the following analysis we include only the thermal stresses which result from the solidification of an injection molded article as it is quenched from an initial temperature,  $T_i$ , to a final temperature,  $T_{\ell}$  (Fig. 8.9). However, it is important to point out again that, in injection molded parts, the solidification process starts during mold filling, and that flow continues during the post-filling or packing stage. This results in frozen-in flow stresses that are of the same order as the thermal stresses. Baaijens [27] calculated the residual stresses in injection molded parts, including the viscoelastic behavior of the polymer and the flow and thermal stresses. With his calculations, he demonstrated that the flow induced stresses are significant and that a major portion of them stems back to the post-filling stage during injection molding. This is in agreement with experimental evidence from Isayev [24] and Wimberger-Friedl [28].

In Fig. 8.9 the plate thickness, 2L, denotes the characteristic dimension across the z-direction and is considered to be much smaller than its other dimensions. This is a common assumption for most polymer parts. It is assumed that the polymer behaves as a viscous liquid above  $T_g$  and as an elastic solid below  $T_g$ . The resulting residual stresses form because the cooling of the plate, from the outside to the inside, cause the outer layers to solidify first

8 Solidification of Polymers 347



without any resistance from the hot liquid core. As the inner layers solidify and cool, their shrinkage is resisted by the solidified outer surface, thus, leading to a residual stress which is tensile in the center and compressive at the surface. Hence, the residual stress build-up must depend on material and process dependent temperatures, space, thermal properties, elastic properties, and on time. This can be expressed as

$$\sigma = \sigma \{ T_i - T_f, T_g - T_f, L, z, \beta, k, h, \alpha, E, \nu, t \}$$

$$(8.23)$$

where  $\beta$  is the thermal expansion coefficient, *k* the thermal conductivity,  $\alpha$  the thermal diffusivity, E the elastic modulus, v Poisson's ratio, and t time. Using the dimensional analysis and assuming that stress relaxation effects are negligible, the final residual stress can be written as

$$\frac{\sigma(1-\nu)}{E} = f\left(Bi, \hat{z}, \varepsilon_T\right) \tag{8.24}$$

where  $\hat{z}$  is a dimensionless coordinate defined by z/L and  $B_i$  is the Biot number defined by the ratio of convective heat removal to heat conduction and is calculated with

$$Bi = \frac{hL}{k} \tag{8.25}$$

A large Biot number signifies a process where the heat is removed from the surface of the part at a high rate. This is typical of fast quench processes, which result in both high temperature gradients and residual stresses. Predicted temperature distributions in a process with a large Biot number is shown in Fig. 8.24a. On the other hand, a low Biot number describes a process where the heat is removed from the part's surface at a very low rate, resulting in parts with fairly constant temperatures. Predicted temperature fields, for low Biot number processes, as shown in Fig. 8.24b, will lead to low residual stresses in the final part.

The third quantity,  $\varepsilon_r$ , found in Eq. 8.24 is the thermal strain that will lead to residual stress. It is a quantity that measures the influence of processing conditions on residual stress formation and is defined by

$$A = \beta \left( T_g - T_f \right) \tag{8.26}$$

The limits of the thermal strain are described by

$$\varepsilon_T = 0 \tag{8.27}$$

if  $T_f = T_g$  and

if  $T_i = T_g$ 

(8.28)  $\varepsilon_{T} = Maximun$ 

380

370

360

350

340

330

320

425

400

375

350

325

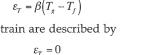
300

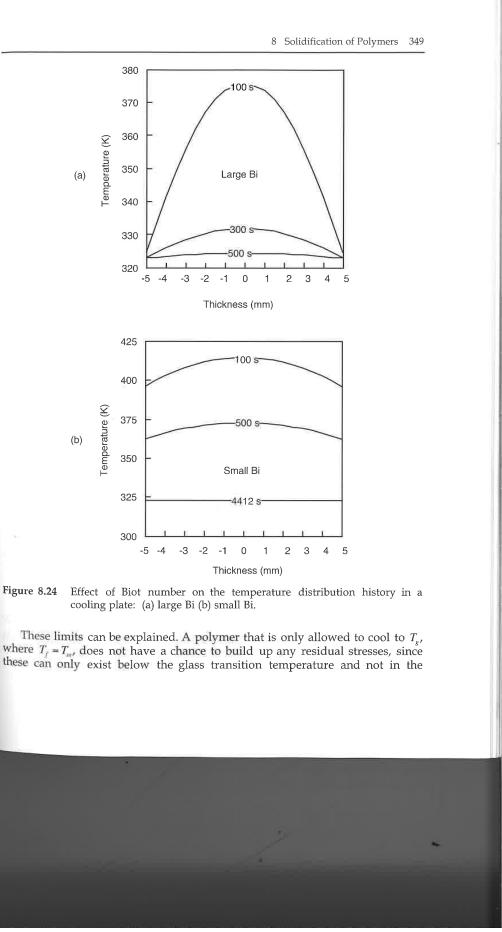
£

(b)

£

(a)





MacNeil Exhibit 2117 Yita v. MacNeil IP, IPR2020-01139 Page 185

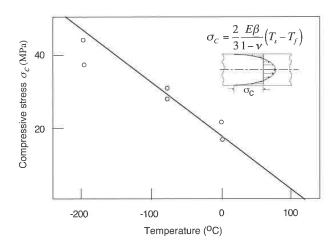
liquid state. On the other hand, a polymer that is initially at the glass transition temperature and cools to another temperature perceives all its strain in the solid state, hence, conceivably translating them completely into stresses.

### 8.3.1.1 Residual Stress Model Without Phase Change Effects

The parabolic temperature distribution which is present once the part has solidified will lead to a parabolic residual stress distribution that is compressive in the outer surfaces of the component and tensile in the inner core. Assuming no residual stress build-up during phase change, a simple function based on the parabolic temperature distribution, can be used to approximate the residual stress distribution in thin sections [28]:

$$\sigma = \frac{2}{3} \frac{E\beta}{1 - \nu} \left( T_s - T_f \right) \left( \frac{6z^2}{4L^2} - \frac{1}{2} \right)$$
(8.29)

Here,  $T_s$  denotes the solidification temperature: the glass transition temperature for amorphous thermoplastics, or the melting temperature for semi-crystalline polymers. Equation 8.29 was derived by assuming static equilibrium (e.g., the integral of the stresses through the thickness must be zero). The full derivation is left out here, since a more general approach is presented in the next section. Figure 8.23 [29] compares the compressive stresses measured on the surface of PMMA samples to Eq. 8.29.



**Figure 8.25** Comparison between computed, Eq. (8.29), and measured compressive stresses on the surface (z = L) of injection molded PMMA plates.

# 8.3.1.2 Model to Predict Residual Stresses with Phase Change Effects

As the plate shown in Fig. 8.9 cools, it develops a solidified layer that continues to grow until the whole plate hardens. Figure 8.11 shows a cross-section of the plate at an arbitrary point in time. At any instance of time, t, the location that has just reached  $T_g$  is defined as  $Z_g(t)$ . To solve for the residual stress distribution, the energy equation, Eq. 8.3, must be solved while satisfying the force balance equation within the solidified material. At the centerline, the symmetry boundary condition can be used, Eq. 8.4, and a convective boundary condition on the outer surface of the plate is needed.

$$h(T_s - T_f) = -k \frac{\partial T}{\partial z}$$
 at  $z = L$  (8.30)

The strain at any time and position is usually defined as the sum of its elastic, thermal, and viscous strain components:

#### E( i

where  $\varepsilon_{E}$  is the elastic strain,  $\varepsilon_{v}$  the viscous strain and  $\varepsilon_{th}$  the thermal strain, which occurs only after the material is below the glass transition temperature. The thermal strain can be written as

# $\varepsilon_{\iota h}$

The viscous strain is the strain the layer undergoes just before solidifying, caused by thermal contraction and viscous flow. The viscous strain occurs under a negligible stress and is not felt by the layer that has just solidified. Each layer has a different viscous strain equal to the overall strain of the plate,  $\varepsilon(t)$ , the instant that layer has solidified, which makes the viscous strain a function of space. Solving for the elastic strain results in

$$\sigma(z,t) = \frac{E}{1-v}$$

To solve for the total strain of and add up to zero, as

Since the plate can be considered symmetric and the stresses are zero above the glass transition temperature, we can write

8 Solidification of Polymers 351

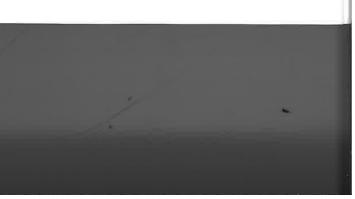
$$t) = \varepsilon_E + \varepsilon_{vh} + \varepsilon_v \tag{8.31}$$

$$=\beta(T(z,t)-T_g) \tag{8.32}$$

$$\varepsilon(t) - \beta \left( T(z,t) - T_{g} \right) - \varepsilon_{\nu}(z) \right)$$
(8.33)

To solve for the total strain of the plate, the stresses must approach equilibrium

$$\int_{L} \sigma(z,t) dz = 0 \tag{8.34}$$



MacNeil Exhibit 2117 Yita v. MacNeil IP, IPR2020-01139 Page 186

$$\int_{z_0(t)}^{L} \sigma(z,t) dz = 0 \tag{8.35}$$

Substituting Eq. 8.33 into Eq. 8.35 gives

 $z_e(t)$ 

$$\int_{(t)}^{t} \left( \varepsilon(t) - \beta \left( T(z,t) - T_g \right) - \varepsilon_v(z) \right) dz = 0$$
(8.36)

However, the plate's total strain is constant through the thickness and can be integrated out and solved for as

$$\varepsilon(t) = \frac{1}{L - z_g(t)} \int_{z_g(t)}^{L} \left( \beta \left( T(z, t) - T_g \right) + \varepsilon_v(z) \right) dz \tag{8.37}$$

The total strain  $\varepsilon(t)$  and its viscous component  $\varepsilon_{v}$  are unknown but equal to each other and can be found by solving both Eq. 8.37 and the energy equation, Eq. 8.3, with a convective boundary condition. The energy equation can be solved numerically by using the finite difference method. The same grid points used for the energy equation can be used for the integration of Eq. 8.37. The solution is achieved in successive time steps from the beginning of cooling until the whole plate has reached the glass transition temperature, at which point the whole viscous strain distribution is known. Now, the part needs to be cooled until its final temperature distribution of  $T = T_f$  has been reached. The final residual stress distribution can be computed as

$$\sigma(z) = \frac{E}{1-\nu} \Big( \varepsilon_{\nu\nu} - \beta \Big( T_f - T_g \Big) - \varepsilon_{\nu}(z) \Big)$$
(8.38)

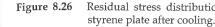
The total strain of the plate is unknown and can be found by solving the equilibrium equation, Eq. 8.34, using the final residual stress distribution as

$$\varepsilon_{tot} = \frac{1}{L} \int_{0}^{L} \left( \beta \left( T_{f} - T_{g} \right) - \varepsilon_{v}(z) \right) dz$$
(8.39)

Figures 8.24 and 8.25 show residual stress distributions for several Biot numbers and values of  $\Theta_{g'}$  respectively. The value  $\Theta_{g}$  is the dimensionless temperature that leads to a residual stress build-up and is defined by

$$\Theta_g = \frac{T_g - T_f}{T_i - T_f} \tag{8.40}$$

In Figure 8.25 the model described in this section is also compared to the residual stress distribution of Eq. 8.29. In this comparison, the influence of phase change effects becomes evident.



0.2

0.1

-0.1 -0.2

-0.3

-0.4 -0.5 -0.6

 $\hat{\sigma}$ 

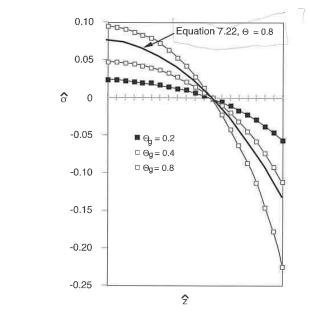
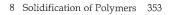


Figure 8.27



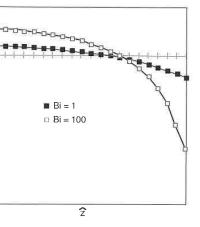
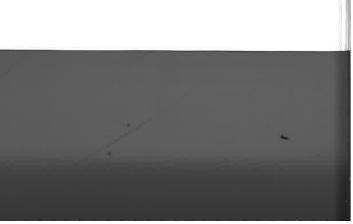


Figure 8.26 Residual stress distributions as a function of Biot number in a poly-

Residual stress distributions as a function of thermal boundary conditions in a polystyrene plate after cooling.



MacNeil Exhibit 2117 Yita v. MacNeil IP, IPR2020-01139 Page 187

Equations 8.37-8.39 can be modified and solved together with the energy equation for thermosets, Eq. 8.20, to compute the residual distributions in thermosetting parts. Here,  $T_e$  must be replaced with the temperature of the material at the time it solidified (e.g., when its conversion was 80%).

## 8.3.2 Other Simple Models to Predict Residual Stresses and Warpage

In practice, the complexity of part geometry and cooling channel design in the manufacture of plastic parts can result in unsymmetric mold wall temperature variations which in turn lead to warpage of the part after it is ejected from the mold. Here, a simple model is presented to evaluate residual stress and warpage of a flat plate caused by uneven mold temperatures (Fig. 8.26a), temperature rise due to exothermic curing reaction in thermoset parts (Fig. 8.26b), and by unsymmetric stress distributions in laminated composites (Fig. 8.26c). In general, the stress distribution has to satisfy the equilibrium equation as defined in Eq. 8.33 where the stress-strain relation is defined as

$$\sigma(z) = \frac{E}{(1-\nu)} \left( \varepsilon_{tot} - \beta \Delta T(z) - \varepsilon_{\nu}(z) \right)$$
(8.41)

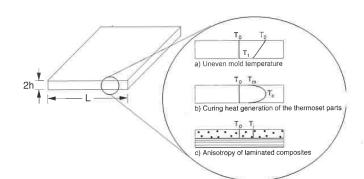


Figure 8.28 Possible causes of residual stress build-up across the thickness of a part.

Here,  $\epsilon_{tot}$  is the total or actual shrinkage of the plate,  $\Delta T$  the change in temperature, E Young's modulus, v Poisson's ratio, and  $\beta$  the thermal expansion coefficient. For simplicity, the viscous strain is often neglected, assuming the part is thin enough that it solidifies at once. Based on classical shell theory and using the stress distribution, one can additionally compute a thermal moment as follows:

Λ

where w is the width of the plate. In the following analyses the above Eqs. 8.39-8.42 will be used to compute residual stress and warpage for various cases. If the part is fixed as it is cooled to its final temperature, the total strain,  $\varepsilon_{ee}$ , is zero. În such a case, residual stress is dominated by thermal strain.

# 8.3.2.1 Uneven Mold Temperature

During molding, the mold wall surface temperatures may vary due to improper thermal mold layout (Fig. 8.26a) with variations typically in the order of 10 °C. Furthermore, the temperatures on the mold surface may vary depending on where the heating or cooling lines are positioned. However, in the current example, we assume that this effect is negligible. The amount of warpage caused by temperature variations between the two mold halves can easily be computed using the equations of the last section. The temperature field across the thickness of a part can be described by

$$T = \left[\frac{1}{2}\right]$$

After substituting Eqs. 8.34 and 8.43 into Eq. 8.41, the stress distribution throughout the thickness can be obtained:

$$\sigma = \frac{1}{2}$$

Substituting Eq. 8.44 into Eq. 8.42, the thermal moment *M* becomes

# M =

For a part whose width, w, is much smaller than its length,  $\ell$ , we can assume a cantilevered geometry as shown in Fig. 8.27. For this geometry the deflection,  $\delta$ , that results from a moment, *M*, can be written as

8 Solidification of Polymers 355

$$\mathcal{A} = w \int_{-L}^{L} \sigma(z) z dz \tag{8.42}$$

$$(8.43)$$

$$\frac{\beta E}{2(1-\nu)} \left[ (T_2 - T_1) \frac{z}{L} \right] \tag{8.44}$$

$$=\frac{w\beta EL^2}{3(1-v)}(T_2 - T_1)$$
(8.45)

$$\delta = \frac{M\ell^2}{2EI} \tag{8.46}$$



where the area moment of inertia, *I*, is written as

 $\varepsilon_{tot} =$ 

 $\sigma(z) = \frac{1}{1}$ 

Substituting Eq. 8.51 into Eq. 8.39, the residual stress distribution becomes

$$\sigma(z) = \frac{\beta E}{(1-\nu)} \left[ \frac{1}{3} (T_c - T_m) - (T_c - T_m) \frac{z^2}{L^2} \right]$$
(8.52)

After defining the non-dimensional parameters,  $\hat{\sigma}$  and  $\hat{z}$ , as

 $\hat{\sigma}$ 

and

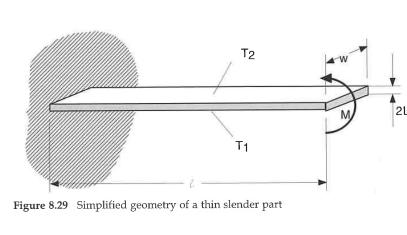
Eq. 8.52 can be normalized as

The non-dimensional residual stress distribution across the thickness of the part is depicted in Fig. 8.27. The stresses in the outer layer are compressive while tensile stresses are found in the inner layers. A maximum compressive non-dimensional stress of 2/3 is located on the surface and a maximum tensile stress of 1/3 occurs at the center of the part.

In addition to uneven mold temperatures, the exothermic curing reaction is a known problem when manufacturing thermoset parts. Heat release during such reactions can cause the transient temperature inside the part to be higher than the mold wall temperatures. Typical temperature and curing history plots are shown in Figs. 8.17 and 8.18. Note that such a temperature distribution dominates the final residual stress distribution. Here, a simple elastic model is presented to approximate the residual stress distribution. The temperature field in the calculation can be described by a parabolic curve

$$T(z) = T_c + (T_m - T_c) \frac{z^2}{L^2}$$
(8.49)

where  $T_c$  and  $T_m$  are the temperature at the center of the plate and the mold surface, respectively.



 $I = \frac{1}{12} w (2L)^3$ 

$$\delta = \frac{\beta\ell^2}{4L} (T_2 - T_1) \tag{8.48}$$

Substituting Eqs. 8.45 and 8.47 into Eq. 8.46 we get

$$\delta = \frac{\beta\ell^2}{4L} \left( T_2 - T_1 \right) \tag{8.48}$$

8 Solidification of Polymers 357

We assume the part to be cooled elastically to room temperature,  $T_0$ . Using Eq. 8.41, the stress distribution can be expressed by

$$\frac{E}{-\nu} \Big[ \varepsilon_{\iota o \iota} - \beta \big( T_0 - T(z) \big) \Big]$$
(8.50)

Since the above equation has to satisfy the equilibrium equation, Eq. 8.34, the total strain can be obtained by integrating the stress field across the thickness

$$\frac{\beta}{L} \left[ T_0 - \frac{2}{3} T_c - \frac{1}{3} T_m \right]$$
(8.51)

$$=\frac{(1-\nu)\sigma}{E\beta(T_c-T_m)}$$
(8.53)

$$\hat{z} = \frac{z}{L} \tag{8.54}$$

$$\hat{\sigma}(\hat{z}) = \frac{1}{3} - \hat{z}^2 \tag{8.55}$$

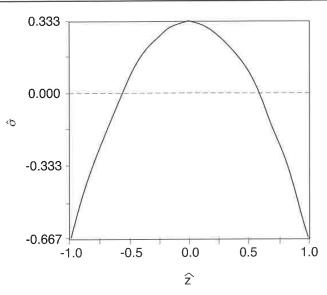


Figure 8.30 Normalized residual stress distribution in a thin thermoset part.

### 8.3.2.3 Anisotropy Induced Curvature Change

In the manufacturing of large and thin laminate structures or fiber reinforced composite parts with a large fiber–length/part–thickness ratio, the final part exhibits a higher thermal expansion coefficient in the thickness direction than in the surface direction. If the part is curved, it will undergo an angular distortion, as shown in Fig. 8.28, which is a consequence of the anisotropy of the composites. This phenomenon is usually called the *spring-forward* effect or *anisotropy induced curvature change* [32]. Through–thickness thermal strains, which are caused by different thermal expansion coefficients, can lead to an angle distortion of a cylindrical shell experiencing a temperature change. As demonstrated in Fig. 8.28, when a curved part undergoes a temperature change of  $\Delta T$ , the curved angle,  $\theta$ , will change by  $\Delta \theta$ . The resulting  $\Delta \theta$ , therefore, is dependent on the angle  $\theta$ , the temperature change  $\Delta T$ , and the difference of the thermal expansion coefficients in the *r* and  $\theta$  directions [33]

$$\Delta \theta = (\beta_r - \beta_\theta) \theta \Delta T = \Delta \beta \, \theta \, \Delta T \tag{8.56}$$

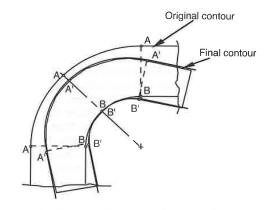


Figure 8.31 Schematic diagram of the spring-forward effect.

In plate analysis, the inclusion of anisotropies that lead to curvature changes is very involved. Hence, it is easier to introduce the curvature change by an equivalent thermal moment [34]:

*M* =

where R represents the local radius of curvature.

# 8.3.3 Predicting Warpage in Actual Parts

Shrinkage and warpage are directly related to residual stresses which result from locally varying strain fields that occur during the curing or solidification stage of a manufacturing process. Such strain gradients are caused by nonuniform thermomechanical properties and temperature variations inside the mold cavity. Shrinkage due to cure can also play a dominant role in the residual stress development in thermosetting polymers and becomes important for fiber reinforced thermosets when are a concern sink marks appearing in thick sections or ribbed parts.

When processing thermoplastic materials, shrinkage and warpage in a final product depend on the molecular orientation and residual stresses that form during processing. The molecular or fiber orientation and the residual stresses inside the part in turn depend on the flow and heat transfer during the mold filling, packing, and cooling stage of the injection molding process. Kabanemi

8 Solidification of Polymers 359

$$=\frac{E}{(1-\nu)}\frac{\Delta\beta\Delta T}{R}\frac{L^3}{12}$$
(8.57)



et al. [35] used a three-dimensional finite element approach to solve the thermal history and residual stress build-up in injection molded parts. To predict the residual stress in the finished part, they characterized the thermomechanical response of the polymer from melt to room temperature, or from the p-v-T behavior to stress-strain behavior. Bushko and Stokes [36, 37] used a thermorheologically simple thermo-viscoelastic material model to predict residual stresses and warpage in flat plates. With their model, they found that packing pressure had a significant effect on the shrinkage of the final part but little effect on the residual stress build-up. Wang and co-workers have developed unified simulation programs to model the filling and post-filling stages in injection molding [38-41]. In their models they perform a simultaneous analysis of heat transfer, compressible fluid flow, fiber orientation, and residual stress build-up in the material during flow and cooling using finite element/control volume approach for flow, finite difference techniques for heat transfer, and finite element methods for fiber orientation and thermomechanical analysis.

The shrinkage and warpage in thin compression molded fiber reinforced thermoset plates were predicted by various researchers [42] using fully threedimensional finite element models and simplified finite element plate models. More recently [4, 44], the through-thickness properties, temperature, and curing variations that led to warpage have been represented with equivalent moments. By eliminating the thickness dimensions from their analysis, they significantly reduced computation costs and maintained agreement with experimental results. At the same time, they were able to use the same finite element meshes used in common commercial codes to predict the mold filling and the fiber orientation in the final part.

The governing equations used for the stress analysis of polymer components are derived using the principle of virtual work. Here, the stresses are represented as a function of local strain and residual stress { $\sigma_0$ }.

$$\{\sigma\} = [E]\{\varepsilon\} - [E]\{\varepsilon_{tot}\} + \{\sigma_0\}$$

$$(8.58)$$

In Eq. 8.58 the material tensor [E] is anisotropic and temperature or degree of cure dependent and  $\{\varepsilon_{tot}\}$  is the total internal strain that occurs due to curing, cooling or heating during a time step. Two kinds of internal strains should be included when simulating the thermomechanical behavior of polymer parts. One is a thermal strain caused by temperature change and the other is a curing strain resulting from cross-linking polymerization of thermoset resins. Thus, the total internal strain can be expressed by

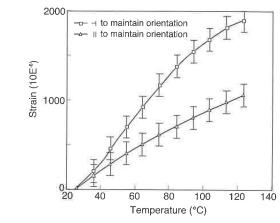
 $\left\{\varepsilon_{\mu\nu}\right\} = \left\{\varepsilon_{0}^{\mu}\right\} + \left\{\varepsilon_{0}^{c}\right\} \tag{8.59}$ 

The thermal shrinkage was measured from a rectangular plate molded with a charge that covered 25% of the mold surface and that was allowed to flow only in one direction.

Here, superscript th denotes the thermal strain and c the curing strain. The thermal strains can be represented in terms of temperature change and thermal expansion coefficients

 $\left\{\varepsilon_0^{th}\right\}T = 1$ 

The anisotropic thermal expansion coefficient, caused by fiber orientation, is perhaps the largest cause of warpage in fiber reinforced parts. Figure 8.29 demonstrates how, for typical thermoset composite parts, the thermal shrinkage parallel to the main orientation direction is about half of that normal to the main orientation direction<sup>5</sup>.

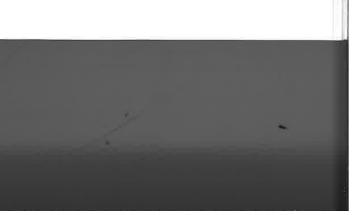


**Figure 8.32** Experimentally measured thermal strains in an SMC plate with a fiber orientation distribution that resulted from a 25% initial mold coverage charge.

To calculate the residual stress development during the manufacturing process, the heat transfer equation is coupled to the stress-strain analysis through constitutive equations. Figure 8.30 compares the mold geometry with part geometry for the truck fender shown in Chapter 7, after mold removal and cooling, computed using the above model. The fiber content by volume in the part was 21% ( $\phi$ =0.21) and the material properties for the glass fiber and the unsaturated polyester resin are listed in Table 8.4.

#### 8 Solidification of Polymers 361

$$\Delta T \left\{ \alpha_{xx} \alpha_{yy} \alpha_{zz} 0 \ 0 \ 0 \right\}$$
(8.60)



5.0 x 10<sup>-6</sup>

 $\beta$  (mm/mm/K)

Table 8.4	Mechanical and Thermomechanical Properties for Various Materials				
	Fiberglass	Polyester	Ероху	_	
E (MPa)	$7.3 \times 10^{4}$	2.75 x 10 <sup>3</sup>	$4.1 \times 10^{3}$		
υ	0.25	0.34	0.37		

3.7 x 10<sup>-5</sup>

5.76 x 10<sup>-5</sup>

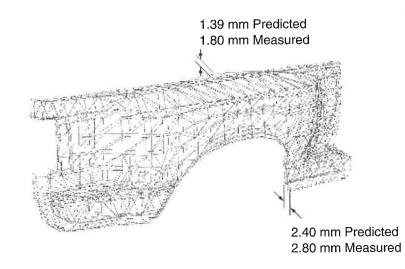


Figure 8.33 Simulated displacements of an automotive body panel. Displacements were magnified by a factor of 20.

Minimizing warpage is one of the biggest concerns for the design engineer. One way to reduce warpage is by introducing a temperature gradient between the upper and lower mold halves. Again, this through-thickness temperature gradient will introduce a thermal moment which increases or decreases the warpage. Also, by changing the formulation of the polyester resin, the coefficient of thermal expansion of the matrix can be reduced, making it similar to the coefficient of the glass fiber. Theoretically, reduction of the coefficients for the matrix would decrease the in-plane differential shrinkage, which in turn could help reduce the final warpage. Furthermore, the fiber content also has a great effect on the deformation of a body panel. Here, although the warpage is actually caused by the existence of fibers inside the resin, the increase of fiber content adds to the stiffness of the part which in turn reduces warpage. Further reduction in warpage can also be achieved by changing the size and location of the initial charge, a trial-and-error solution, which is still the most feasible with today's technology.

# Examples

a function of time.

8.8

where

and

where *n* is the total number of data points and  $\Delta t$  is the time step. Since the data are given in terms of temperature, we must transform the temperature step to time using the heating rate 2.78 K/min using

The above leads to a total heat of reaction,  $Q_{T}$ , of 785.4 J/g or 785.4 kJ/kg. The degree of cure as a function of temperature is plotted in Fig. 8.31.

8.1 Three small samples of an epoxy resin were subjected to a temperature rise from 50 °C to 300 °C in a differential scanning calorimeter using three different heating rates: 2.78 K/min (5F/min), 5.66 K/min (10 F/min) and 11.11 K/min (20 F/min). Table 8.5 presents the exothermal heat released during the tests. Determine the total heat of reaction using the data measured with the 2.78 K/min heating rate. Plot the degree of cure as

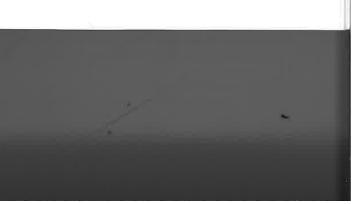
In order to compute the degree of cure as a function of time we use Eq.

$$C_i^* = \frac{Q_i}{Q_T}$$

$$Q_i = \int_0^{\tau_i} \dot{Q} dt = \sum_{j=1}^{\bar{i}} \dot{Q}_j \Delta t$$

$$Q_T = \int_0^\infty \dot{Q} dt = \sum_{j=1}^n \dot{Q}_j \Delta t$$

$$\Delta t = \frac{10\mathrm{K}}{2.78\mathrm{K}\,/\mathrm{min}}$$

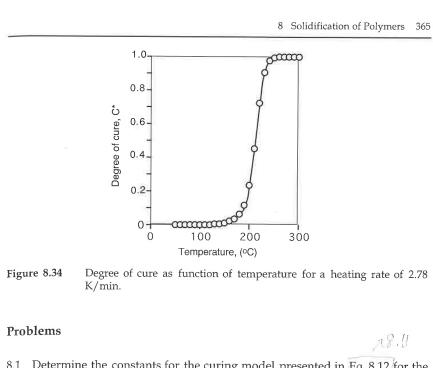


MacNeil Exhibit 2117 Yita v. MacNeil IP, IPR2020-01139 Page 192



Table 8.5 DSC Data for an Epoxy Resin

<i>T</i> (°C)	$\dot{Q}$ $\left(\frac{J}{g \cdot \min}\right)$				
	2.78 K/min	5.66 K/min	11.11 K/min		
$\begin{array}{c} 50\\ 60\\ 70\\ 80\\ 90\\ 100\\ 110\\ 120\\ 130\\ 140\\ 150\\ 160\\ 170\\ 180\\ 190\\ 200\\ 210\\ 220\\ 230\\ 240\\ 250\\ 260\\ \end{array}$	2.78 K/min 0. 0. 0.01 0.02 0.03 0.06 0.12 0.22 0.38 0.65 1.11 1.91 3.38 6.23 12.21 24.97 47.10 60.09 39.40 15.0 4.29 0.98	5.66 K/min 0. 0. 0.01 0.02 0.04 0.09 0.16 0.28 0.49 0.82 1.35 2.23 3.69 6.23 10.86 19.76 37.23 68.36 103.36 100.09 55.65	11.11 K/min 0. 0.01 0.02 0.03 0.06 0.12 0.21 0.37 0.62 1.03 1.66 2.668 4.24 6.76 10.94 18.08 30.79 53.89 94.37 152.83 196.48		
270 280 290 300	0.17 0.018 0. 0.	19.99 5.17 0.92 0.09	168.68 90.54 31.62 7.06		



- vinyl ester presented in Fig. 8.15. -7 3 16
- effects of phase change.
- change effects.

8 Solidification of Polymers 365

18.11

8.1 Determine the constants for the curing model presented in Eq. 8.12 for the

8.2 Write a finite difference program to solve for the transient temperature distribution in a cooling amorphous polymer plate. Test the program with the data given for polystyrene in Table 8.2 for a 2 mm thick plate.

8.3 Using the momentum balance presented in Eq. 8.43, derive the residual stress distribution, Eq. 8.38, in a cooling polymer plate neglecting the

8.4 A 1 mm thick polystyrene ruler is injection molded. For a resin with a glass transition temperature around 100 °C and a final ambient temperature of 20 °C, estimate the residual stress at the surface of the part shortly after demolding. Assume a Young's modulus of 3200 MPa and a thermal expansion coefficient of 7x10-5 mm/mm/°C. Neglect phase

8.5 For a standard 30 cm long, 3 cm wide, and 1 mm thick ruler, how much warpage would occur with a 5 °C temperature difference between the



mold halves? Assume a Young's modulus of 3200 MPa and a thermal expansion coefficient of  $7x10^{-5} \text{ mm/mm/}^{\circ}\text{C}$ .

- 8.6 Write a finite difference program to solve for the transient temperature distribution in a cooling amorphous polymer plate. Solve Eqs. 8.31-8.39 along with the predicted temperatures to estimate the residual stress in the final plate. Compare the residual stress distribution for a 2 and a 5 mm thick polystyrene plate.
- 8.7 A long and thin unsaturated polyester unidirectional glass fiber composite plate (1000x20x2 mm) is molded in a thermally unbalanced mold. One mold side is a 140 °C and the other at 150 °C. Assuming the temperature distribution is at steady state the instant the part solidifies, what is the residual stress distribution in the plate before it is allowed to warp.  $E_{composite} = 20$ GPa. Towards which direction would the plate warp, the hot side or cooler side?
- 8.8 Figure 8.31 presents a schematic of the cross-section of an SMC pick-up truck box. In the finished product, the average through the thickness thermal expansion coefficient,  $\beta_3$ , is  $2x10^{-5}$  mm/mm/K, and the average planar thermal expansion coefficient,  $\beta_1$  or  $\beta_2$  is  $8 \times 10^{-6} \text{ mm/mm/K}$ . Estimate the amount and direction that the side walls will warp, if any.

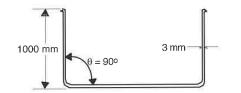


Figure 8.35 Schematic of an SMC pick-up truck cross-section.

8.9 Using the data given in Example 8.1, plot the degree of cure for heating rates of 5.66 K/min and 1.11 K/min. What are the characteristic curing times for all three heating rates.

# References

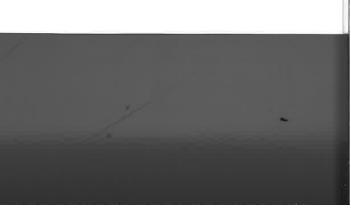
- van Krevelen, D.W., and Hoftyzer, P.J., Properties of Polymers, Elsevier Scientific 1. Publishing Company, Amsterdam, (1976).
- 2 Wagner, H., Internal report, AEG, Kassel, Germany, (1974).
- Menges, G., and Winkel, E., Kunststoffe, 72, 2, 91, (1982). 3.
- Tadmor, Z., and Gogos, C.G., Principles of Polymer Processing, John Wiley & Sons, 4. New York, (1979).
- Avrami, M., J. Chem. Phys., 7, 1103, (1939). 5 6
- Sharples, A., Polymer Science, A Materials Science Handbook, Chapter 4, A.D. Jenkins, Ed., North Holland Publishing Company, Amsterdam, (1972).
- 7. H.E.H. Meijer, Verlag Chemie, Weinheim, (1995).
- Brandrup, J., and Immergut, E.H., Polymer Handbook, John Wiley & Sons, New 8. York, (1975).
- 9. (1985).
- 10.
- 13. Randell, D.R., Radiation Curing Polymers, Burlington House, London, (1987).
- MI, ASM International, Material Park, (1994).
- Munich, (1989)
- 2567 (1983).
- Sci., 14 (3), 231 (1974).
- 18. Rabinowitch, E., Trans. Faraday Soc., 33, 1225 (1937). 19 Eds., Walter de Gruyter, New York (1987)

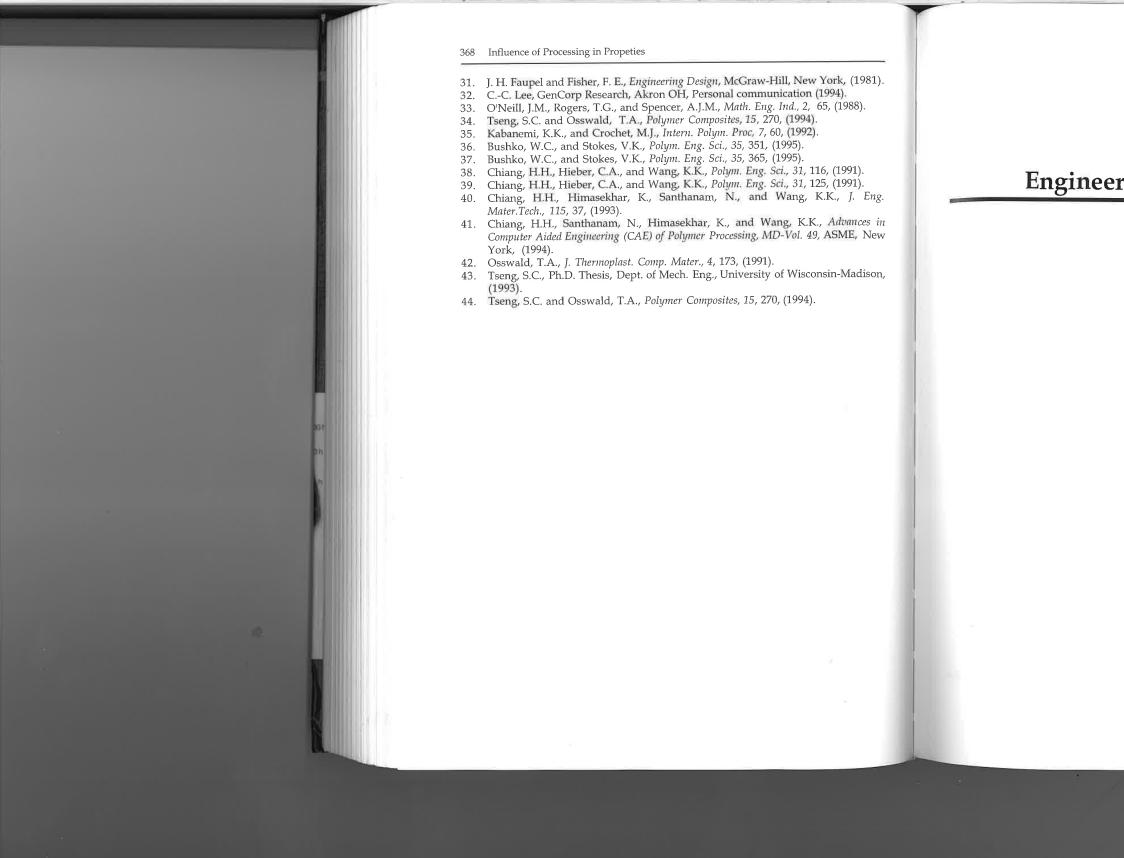
- 22.
- 23. Barone, M.R. and Caulk, D.A., Int. J. Heat Mass Transfer, 22, 1021, (1979).
- 24. Isayev, A.I., and Crouthamel, D.L., Polym. Plast. Technol., 22, 177, (1984). 25. Isayev, A.I., Polym. Eng. Sci., 23, 271, (1983).
- 26.
- Wübken, G., Ph.D. Thesis, IKV, RWTH-Aachen, Germany, (1974). 27. Baaijens, F.P.T., Rheol. Acta, 30, 284, (1991).
- 28.
- 29.
- - Hill, New York, (1959).

### 8 Solidification of Polymers 367

- Eder., G., and Janeschitz-Kriegl, H., Material Science and Technology, Vol. 18., Ed.
- Krobath, G., Liedauer, S., and Janeschitz-Kriegl, H., Polymer Bulletin, 14, 1,
- Stefan, J., Ann. Phys. and Chem., N.F., 42, 269, (1891).
- 11. Eder, G., and Janeschitz-Kriegl, H., Polymer Bulletin, 11, 93, (1984).
- 12. Janeschitz-Kriegl, H., and Krobath, G., Intern. Polym. Process., 3, 175, (1988).
- 14. Palmese, G.R., Andersen, O., and Karbhari, V.M., Advanced Composites X: Proceedings of the 10th Annual ASM/ESD Advance Composites Conference, Dearborn,
- 15. Macosko, C.W., RIM Fundamentals of Reaction Injection Molding, Hanser Publishers,
- 16. Enns, J.B. and Gillham, J.K., "Time-Temperature-Transformation (TTT) Cure Diagram: Modeling the Cure Behavior of Thermosets", J. Appl. Polym. Sci., 28,
- 17. Kamal, M.R., "Thermoset Characterization for Moldability Analysis", Polym. Eng.

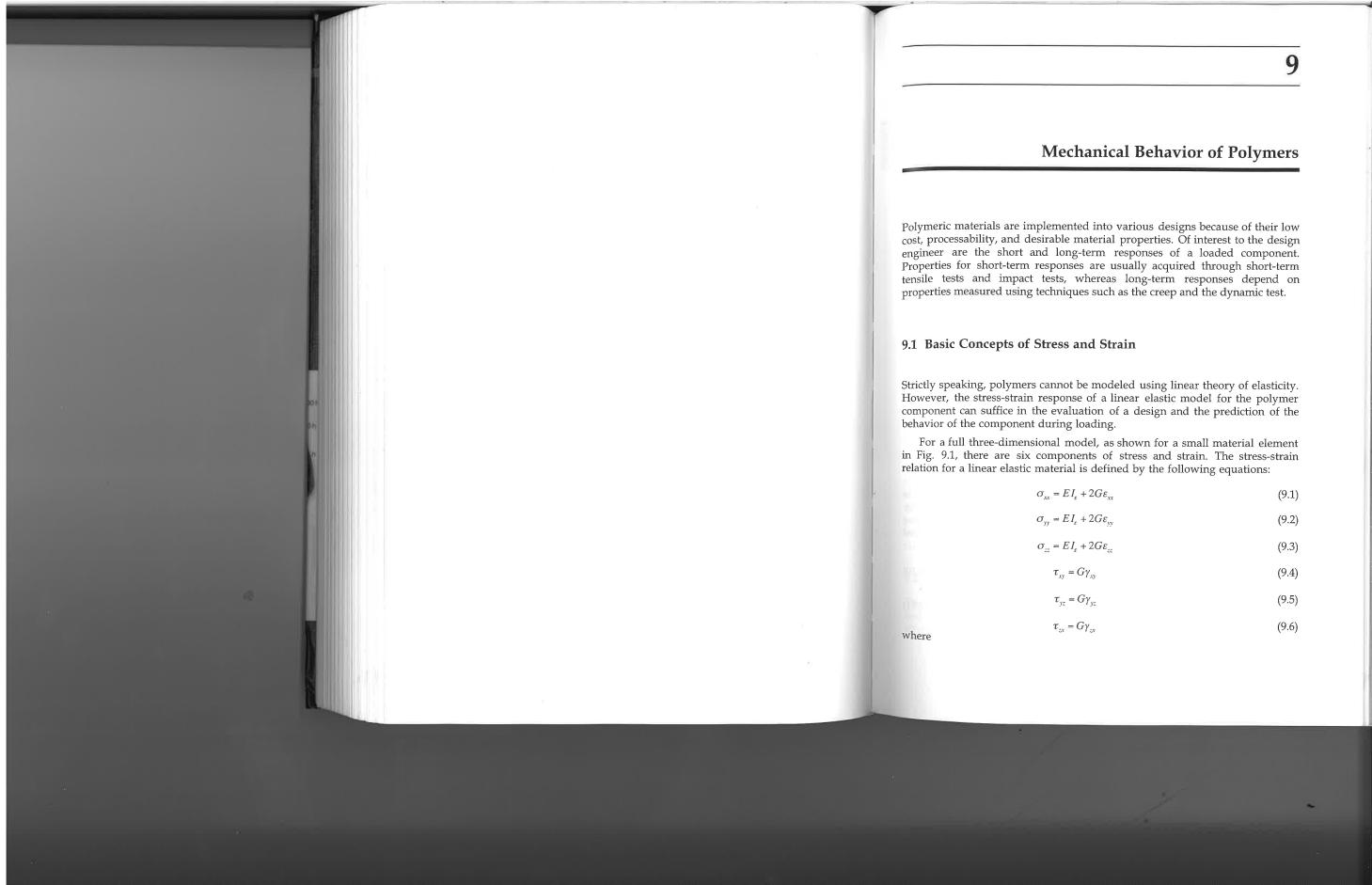
  - Havlicek, I and Dusek, K., in Crosslinked Epoxies, 417, B. Sedlacek and J. Kahovec,
- 20. DiBenedetto, A.T., J. Polym. Sci. Polym. Phys., ed., 25, 1949 (1987).
- 21. Bogetti, T.A. and Gillespie, J.W., 45th SPI Conf. Proc., (1990).
  - Bogetti, T.A. and Gillespie, J.W., 21st Int. SAMPE Tech. Conf., (1989).
  - Wimberger-Friedl, R., Polym. Eng. Sci., 30, 813, (1990).
  - Ehrenstein, G.W., Polymer-Werkstoffe, Hanser Publishers, Munich, (1978).
- 30. S. P. Timoshenko and Krieger, S. W., Mechanics of Composite Materials, McGraw-





# Part III

# **Engineering Design Properties**



$= EI_{\varepsilon} + 2G\varepsilon_{xx}$	(9.1)
$= EI_{\varepsilon} + 2G\varepsilon_{yy}$	(9.2)

$E = EI_{\varepsilon} + 2G\varepsilon_{zz}$	(9.3)
$E = E I_{\varepsilon} + 2G \varepsilon_{zz}$	(9.3

$ au_{xy} = G \gamma_{xy}$	(9.4)
$ au_{yz} = G \gamma_{yz}$	(9.5)

MacNeil Exhibit 2117 Yita v. MacNeil IP, IPR2020-01139 Page 196

$$E = \frac{vE}{(1+v)(1-2v)}$$
(9.7)

and  $I_{\varepsilon}$  is the first invariant of the strain tensor and represents the volumetric expansion of the material which is defined by

$$I_{\varepsilon} = \varepsilon_{xx} + \varepsilon_{yy} + \varepsilon_{zz} \tag{9.8}$$

The elastic constants E, v and G represent the modulus of elasticity, Poisson's ratio and shear modulus, respectively. The shear modulus, or modulus of rigidity, can be written in terms of *E* and *v* as

$$G = \frac{E}{2(1+\nu)} \tag{9.9}$$

The above equations can be simplified for different geometries and load cases. Two of the most important simplified models, the plane stress and plane strain models, are discussed below.

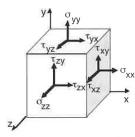


Figure 9.1 Differential material element with coordinate and stress definition.

#### 9.1.1 Plane Stress

A common model describing the geometry and loading of many components is the plane stress model. The model reduces the problem to two dimensions by assuming that the geometry of the part can be described on the x-y plane with a relatively small thickness in the z direction. In such a case  $\sigma_{zz} = \tau_{zz} = \tau_{yz} = 0$  and Eqs. 9.1-9.6 reduce to

$$\sigma_{xx} = \frac{E}{1 - \nu^2} \left( \varepsilon_{xx} + \nu \varepsilon_{yy} \right) \tag{9.10}$$

$$\sigma_{yy} = \frac{E}{1 - v^2} \left( v \varepsilon_{xx} + \varepsilon_{yy} \right) \quad \text{and} \tag{9.11}$$

#### 9.1.2 Plane Strain

Another common model used to describe components is the plane strain model. Similar to the plane stress model, the geometry can be described on an x-y plane with an infinite thickness in the z direction. This problem is also twodimensional, with negligible strain in the z direction but with a resultant  $\sigma_{zz}$ . For this case, Eqs. 9.1–9.8 reduce to

$$\sigma_{xx} = \frac{E}{(1+v)}$$
$$\sigma_{yy} = \frac{E(1-v)}{(1+v)(1-v)}$$

# 9.2 The Short-Term Tensile Test

The most commonly used mechanical test is the short-term stress-strain tensile test. Stress-strain curves for selected polymers are displayed in Fig. 9.2 [1]. For comparison, the figure also presents stress-strain curves for copper and steel. It becomes evident from Fig. 9.2 that although they have much lower tensile strengths, many engineering polymers exhibit much higher strains at break.

The next two sections discuss the short-term tensile test for elastomers and thermoplastic polymers separately. The main reason for identifying two separate topics is that the deformation of a cross-linked elastomer and an uncross-linked thermoplastic vary greatly. The deformation in a cross-linked polymer is in general reversible, whereas the deformation in typical uncrosslinked polymers is associated with molecular chain relaxation, which makes the process time-dependent, and sometimes irreversible.

# 9.2.1 Rubber Elasticity

The main feature of elastomeric materials is that they can undergo very large and reversible deformations. This is because the curled-up polymer chains stretch during deformation but are hindered in sliding past each other by the

9 Mechanical Behavior of Polymers 373

$$\tau_{xy} = G\gamma_{xy} \tag{9.12}$$

$$\frac{(1-\nu)}{\nu(1-2\nu)} \left( \varepsilon_{xx} + \frac{\nu}{1-\nu} \varepsilon_{yy} \right)$$
(9.13)

$$\frac{v}{-2v}\left(\frac{v}{1-v}\varepsilon_{xx}+\varepsilon_{yy}\right)$$
 and (9.14)

$$\tau_{xy} = G\gamma_{xy} \tag{9.15}$$



cross-links between the molecules. Once a load is released, most of the molecules return to their coiled shape. As an elastomeric polymer component is deformed, the slope of the stress-strain curve drops significantly as the uncurled molecules provide less resistance and entanglement, allowing them to move more freely. Eventually, at deformations of about 400%, the slope starts to increase since the polymer chains are fully stretched. This is followed by polymer chain breakage or crystallization which ends with fracture of the component. Stress-deformation curves for natural rubber (NR) [2] and a rubber compound [3] composed of 70 parts of styrene-butadiene-rubber (SBR) and 30 parts of natural rubber are presented in Fig. 9.3. Because of the large deformations, typically several hundred percent, the stress-strain data are usually expressed in terms of extension ratio,  $\lambda$ , defined by

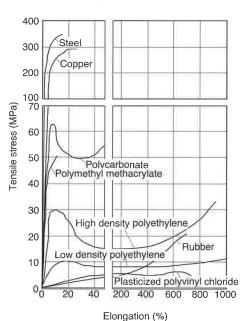


Figure 9.2 Tensile stress-strain curves for several materials.

where L represents the instantaneous length and  $L_0$  the initial length of the specimen.

 $\lambda = \frac{L}{L_0}$ 

(MPa)

Figure 9.3 Experimental stress-extension curves for NR and a SBR/NR compound.

Based on kinetic theory of rubber elasticity [2, 4] simple expressions can be derived to predict the stress as a function of extension. For a component in uniaxial extension, or compression, the stress can be computed as<sup>1</sup>

 $\sigma$ 

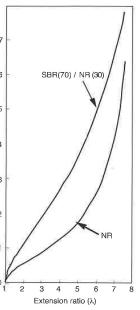
approximated by

with  $E_0$  as the elastic tensile modulus at zero extension.

Figure 9.4 [2] compares the kinetic theory model with the experimental data for natural rubber, presented in Fig. 9.3. The agreement is good up to about 50% extension ( $\lambda$  = 1.5). However, Eq. 9.17 can be used to approximate the

follows  $\sigma = G_0 \left( \lambda^2 - 1 / \lambda^4 \right).$ 

9 Mechanical Behavior of Polymers 375



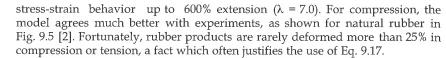
$$=G_0\left(\lambda - \frac{1}{\lambda^2}\right) \tag{9.17}$$

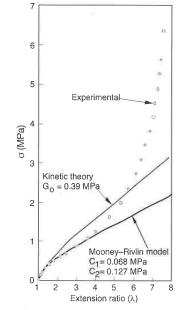
where  $G_0$  is the shear modulus at zero extension, which for rubbers can be

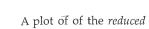
$$G_0 = \frac{E_0}{3}$$
(9.18)

1 A similar equation exists for equibiaxial extension (inflation) of thin sheets. This equation is written as









0.8

0.4

0.0

-0.4 -0.8 -1.2 -1.6 -2.0

-2.4 -2.8

for natural rubber.

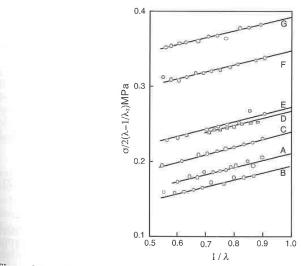
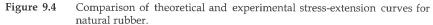


Figure 9.6 Mooney plots for rubber with various degrees of vulcanization.



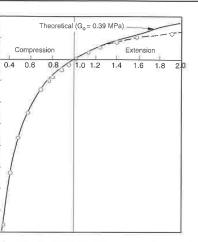
A more complex model representing the deformation behavior of elastomers in the region in which the stress-strain curve is reversible is the Mooney-Rivlin equation [5, 6] written as

$$\sigma = 2\left(\lambda - \frac{1}{\lambda^2}\right)\left(C_1 + \frac{C_2}{\lambda}\right) \tag{9.19}$$

which can be rearranged to give

$$\frac{\sigma}{2\left(\lambda - \frac{1}{\lambda^2}\right)} = C_1 + \frac{C_2}{\lambda} \tag{9.20}$$

# 9 Mechanical Behavior of Polymers 377





A plot of of the *reduced stress*,  $\sigma/2(\lambda - 1/\lambda^2)$ , versus  $1/\lambda$  is usually referred to as a *Mooney plot* and should be linear with a slope of  $C_2$  and an ordinate of  $(C_1 + C_2)$  at  $1/\lambda = 1$ . A typical Mooney plot is presented in Fig. 9.6 [7] for a natural rubber with different formulations and times of vulcanization.



MacNeil Exhibit 2117 Yita v. MacNeil IP, IPR2020-01139 Page 199

The description of the various rubber formulations tested are presented in Table 9.1 [7]. It can be seen that  $C_2$  shows little change, even with different rubber composition, and is approximately 0.1 Mpa. On the other hand,  $C_1$  changes with degree of vulcanization and composition. A comparison between the Mooney-Rivlin model, the kinetic theory model, and experimental data for natural rubber is found in Fig. 9.4. For this material, the Mooney-Rivlin model represents the experimental data quite well up to extension ratios of 3.5.

Table 9.1	Compounding Details of the	e Vulcanizates Used by Gumbrell et al. <sup>a</sup>
-----------	----------------------------	-----------------------------------------------------

· · · · · · · · · · · · · · · · · · ·	0				5		
Mix	А	В	С	D	Е	F	G
Rubber	100	100	100	100	100	100	100
Sulfur	3.0	3.0	3.0	3.0	3.25	4.0	4.0
Zinc oxide	5.0	5.0	5.0	5.0	5.0	5.0	5.0
Stearic acid	1.0	1.0	1.0	1.0	1.0	1.0	1.0
Benzthiazyl disulphide	0.5	0.5	0.5	0.75		1.0	0.5
Mercaptobenz-thiazyl- disulphide		0.5	0.5	0.25		0.3	
Zinc dimethyl dithiocarbamate				0.1		0.15	
Diphinyl guanidine					1.25		1.0
Antioxidant	1.0	1.0	1.0	1.0	1.0	1.0	1.0
Time of vulcanization at 141.5 <sup>o</sup> C (min)	45	10	30	20	60	10	12

<sup>a</sup> Reference [7.]

Finally, it should be noted that the stiffness and strength of rubber is increased by filling with carbon black. The most common expression for describing the effect of carbon black content on the modulus of rubber was originally derived by Guth and Simha [8] for the viscosity of particle suspensions, and later used by Guth [9] to predict the modulus of filled polymers. The Guth equation can be written as

$$\frac{G_f}{G_0} = 1 + 2.5\phi + 14.1\phi^2 \tag{9.21}$$

where  $G_f$  is the shear modulus of the filled material and  $\phi$  the volume fraction of particulate filler. The above expression is compared to experiments [10, 11] in Fig. 9.7.

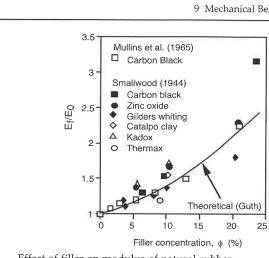


Figure 9.7 Effect of filler on modulus of natural rubber.

# 9.2.2 The Tensile Test and Thermoplastic Polymers

Of all the mechanical tests done on thermoplastic polymers, the tensile test is the least understood, and the results are often misinterpreted and misused. Since the test was inherited from other materials that have linear elastic stressstrain responses, it is often inappropriate for testing polymers. However, standardized tests such as DIN 53457 and ASTM D638 are available to evaluate the stress-strain behavior of polymeric materials.

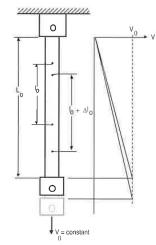
The DIN 53457, for example, is performed at a constant elongational strain rate of 1% per minute, and the resulting data are used to determine the *short-term modulus*. The ASTM D638 test also uses one rate of deformation per material to measure the modulus; a slow speed for brittle materials and a fast speed for ductile ones. However, these tests do not reflect the actual rate of deformation experienced by the narrow portion of the test specimen, making it difficult to maintain a constant speed within the region of interest.

Extensive work was done by Knausenberger and Menges [12] where the rate of deformation of the test specimen is maintained constant. This is achieved by optically measuring the deformation on the specimen itself, as schematically demonstrated in Fig. 9.8 [12], and using that information as a feedback to control the elongational speed of the testing machine. The Knausenberger-Menges technique allows the testing engineer to measure the stress-strain response at various strain rates, where in each test the rate of deformation in the narrow section of the test specimen is accurately controlled. The resulting data can be used to determine the viscoelastic properties of

9 Mechanical Behavior of Polymers 379



polymers ranging from impact to long-term responses. A typical test performed on PMMA at various strain rates at room temperature is shown in Fig. 9.9. The increased curvature in the results with slow elongational speeds suggests that stress relaxation plays a significant role during the test.



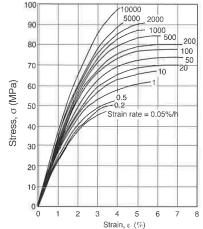
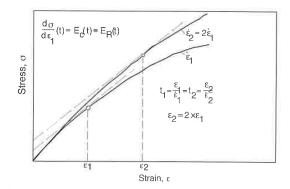


Figure 9.9 Stress-strain behavior of PMMA at various strain rates.

It can be shown that for small strains, or in linear viscoelasticity, the secant modulus, described by

and the tangent modulus, defined by

are independent of strain rate and are functions only of time and temperature. This is demonstrated in Fig. 9.10 [13]. The figure shows two stress-strain responses: one at a slow elongational strain rate,  $\dot{\epsilon}_{i}$ , and one at twice the speed, defined by  $\dot{\epsilon}_2$ . The tangent modulus at  $\epsilon_1$  in the curve with  $\dot{\epsilon}_1$  is identical to the tangent modulus at  $\varepsilon_2$  in the curve with  $\dot{\varepsilon}_2$ , where  $\varepsilon_1$  and  $\varepsilon_2$  occurred at the same time. For small strains the tangent modulus,  $E_t$ , is identical to the relaxation modulus,  $E_r$ , measured with a stress relaxation test. This is important since the complex stress relaxation test can be replaced by the relatively simple shortterm tensile test by plotting the tangent modulus versus time.

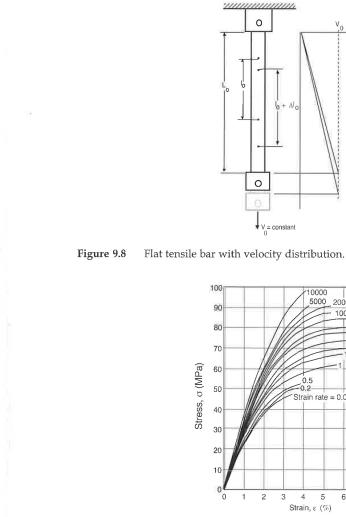


rates of deformation.

Generic stress-strain curves and stiffness and compliance plots for amorphous and semi-crystalline thermoplastics are shown in Fig. 9.11 [14]. For amorphous thermoplastics one can usually approximate the stress-strain behavior in the curves of Fig. 9.11 by

> $\sigma(T,t) = E_0(T,t)(1-D_1(T,t)\varepsilon)\varepsilon$ (9.24)

and in a short-term test a semi-crystalline polymer would behave more like



9 Mechanical Behavior of Polymers 381

$$E_s = \frac{\sigma}{\varepsilon} \tag{9.22}$$

$$E_{i} = \frac{d\sigma}{d\varepsilon} \tag{9.23}$$

Figure 9.10 Schematic of the stress-strain behavior of a viscoelastic material at two



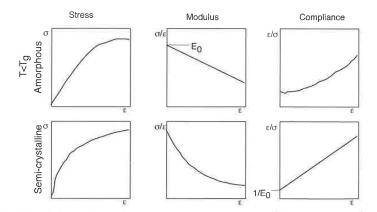
$$\sigma(T,t) = E_0(T,t)\frac{\varepsilon}{1+D_2(T,t)\varepsilon}$$
(9.25)

where  $E_0$ ,  $D_1$  and  $D_2$  are time- and temperature-dependent material properties. However, below the glass transition temperature, the stress-strain curve of an amorphous polymer has a long and much steeper rise, with less relaxation effects, as shown in Fig. 9.10 and Eq. 9.24. In the stress-strain response of semicrystalline polymers, on the other hand, the amorphous regions make themselves visible in long-term tensile tests. Hence, Eqs. 9.24 and 9.25 can be written in a more general form as

$$\sigma = E_0 \varepsilon \frac{1 - D_1 \varepsilon}{1 + D_2 \varepsilon} \tag{9.26}$$

The coefficients in Eq. 9.26 can be determined for various rates of deformation. For example, the curves in Fig. 9.12 [15] show the coefficient  $E_0$  for an amorphous unplasticized PVC measured at various strain rates,  $\dot{\epsilon}$ , and temperatures. The curves in the figure suggest that there is a direct relationship between temperature and strain rate or time. It can be seen that the curves, separated by equal temperature differences, are shifted from each other at equal distances,  $\log(a_r)$ , where

$$a_T = \frac{\dot{\varepsilon}_{ref}}{\dot{\varepsilon}} \tag{9.27}$$



**Figure 9.11** Schematic of the stress-strain response, modulus and compliance of amorphous and semi-crystalline thermoplastics at constant rates of deformation.

Since strain rate is directly related to time, one can make use of Arrhenius' relation between relaxation time,  $\lambda$ , and a reference relaxation time,  $\lambda_{ref}$ , stated by

.

where *A* is the activation energy, *T* temperature and *K* a material property. The modified form of the Arrhenius equation for shifting the data can be written as

# $\log(a_T)$

where  $T_{ref}$  is the reference temperature. The material constant *K* can be calculated by using data from Fig. 9.12, as shown in the sample graphical shift displayed in the figure. The coefficient *K*, which can be solved for by using

# K

turns out to be 10,000 for the conditions shown in Fig. 9.12. This is true unless the test temperature is above the glass transition temperature, at which point the shift factor,  $a_T$ , and the coefficient *K* become functions of strain rate, as well as time and temperature. This is demonstrated for unplasticized PVC in Fig. 9.13 [15]. For the temperature range below  $T_g$ , displayed in Fig. 9.12, the data can easily be shifted, allowing the generation of a *master curve* at the reference temperature,  $T_{ref}$ . Figure 9.14 [15] shows such master curves for the three coefficients  $E_0$ ,  $D_1$  and  $D_2$  in Eq. 9.26 for the amorphous PVC shown in Figs. 9.12 and 9.13. For comparison, Fig. 9.15 [15] shows  $E_0$  and  $D_2$  for a high density polyethylene at 23 °C as a function of strain rate.

The values of  $E_0$ ,  $D_1$  and  $D_2$  can be easily calculated for each strain rate from the stress-strain diagram [16]. The modulus  $E_0$  simply corresponds to the tangent modulus at small deformations where

9 Mechanical Behavior of Polymers 383

$$\frac{\lambda}{\lambda_{ref}} = e^{-\Lambda/KT} \tag{9.28}$$

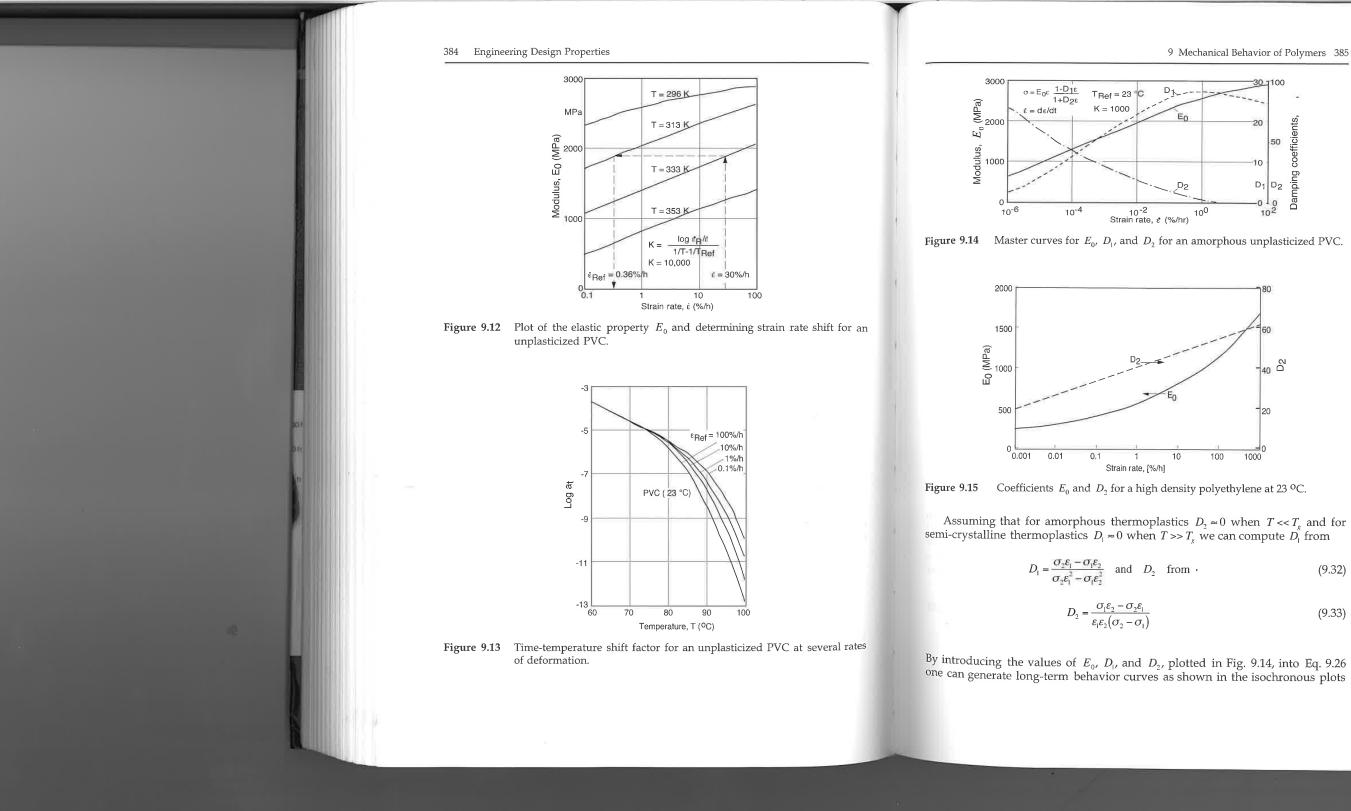
$$T_{T} = K \left( \frac{1}{T} - \frac{1}{T_{ref}} \right)$$

$$\tag{9.29}$$

$$=\frac{\log(\dot{\epsilon}_{ref} / \dot{\epsilon})}{1/T - 1/T_{ref}}$$
(9.30)

$$\sigma \approx E_0 \varepsilon$$

(9.31)



$$\sigma_1 \varepsilon_2 = \sigma_2 \varepsilon_1$$
 and  $D_2$  from  $\cdot$  (9.32)  
 $\sigma_1 \varepsilon_2 = \sigma_2 \varepsilon_1$  (9.32)

$$=\frac{1}{\varepsilon_1\varepsilon_2(\sigma_2-\sigma_1)}$$
(9.55)



MacNeil Exhibit 2117 Yita v. MacNeil IP, IPR2020-01139 Page 203

in Fig. 9.16 [15]. Here, the stress-strain behavior of unplasticized PVC is presented at constant times from 0.1 to 1000 hours of loading time. This is done by simply determining which strain rate results in a certain value of strain for a specific isochronous curve (time), then reading the values of  $E_0$ ,  $D_1$ , and  $D_2$ from the graphs and computing the corresponding stress using Eq. 9.26. When one uses this technique and furthermore applies the time-temperature superposition on short-term tests, one can approximate the long-term behavior of polymers which is usually measured using time consuming creep or relaxation tests.

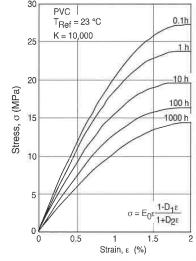
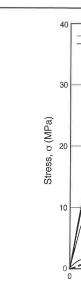
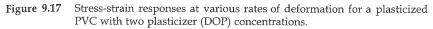
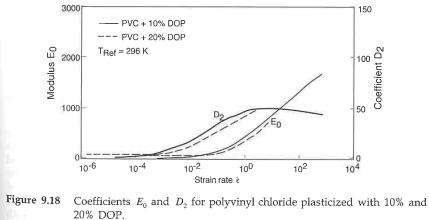


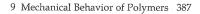
Figure 9.16 Isochronous stress-strain curves for an unplasticized PVC.

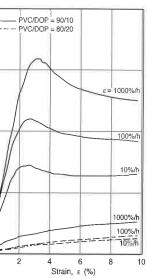
As a final note, similar to the effect of a rise in temperature, a solvent can increase the overall toughness of the material at the sacrifice of its strength and stiffness. This is shown in Fig. 9.17 [15] for a PVC plasticized with 10 and 20% dioctylphthalate (DOP). Figure 9.18 [15] shows the coefficients  $E_0$  and  $D_2$  for a PVC plasticized with 10 and 20% DOP. Figure 9.19 [15] demonstrates the similar effects of temperature and plasticizer.

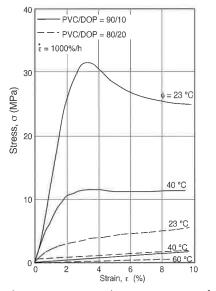


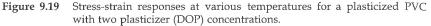












# 9.3 Long-Term Tests

The stress relaxation and the creep test are well-known long-term tests. The stress relaxation test, discussed in Chapter 2, is difficult to perform and is therefore often approximated by data acquired through the more commonly used creep test. The stress relaxation of a polymer is often thought of as the inverse of creep.

The creep test, which can be performed either in shear, compression, or tension, measures the flow of a polymer component under a constant load. It is a common test that measures the strain,  $\varepsilon$ , as a function of stress, time, and temperature. Standard creep tests such as DIN 53 444 and ASTM D2990 can be used. Creep tests are performed at a constant temperature using a range of applied stress, as shown in Fig. 9.20 [17], where the creep responses of a polypropylene copolymer are presented for a range of stresses in a graph with a log scale for time. When plotting creep data in a log-log graph, in the majority of the cases, the creep curves reduce to straight lines as shown for polypropylene in Fig. 9.21 [1]. Hence, the creep behavior of most polymers can be approximated with a power-law model represented by

ε(

where M and n are material-dependent properties.

plasticized PVC.

Figure 9.23 [19] presents the creep modulus for various materials as a function of time.

deformation speeds.

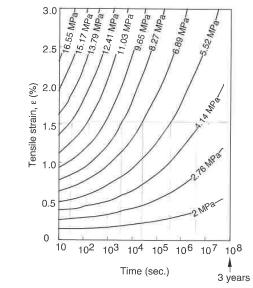


Figure 9.20 Creep response of a propylene-ethylene copolymer at 20 °C.

9 Mechanical Behavior of Polymers 389

$$f(t) = M(\sigma, T)t^n \tag{9.34}$$

Similar to the stress relaxation test, the creep behavior of a polymer depends heavily on the material temperature during testing, having the highest rates of deformation around the glass transition temperature. This is demonstrated in Fig. 9.22 [18], which presents the creep compliance of

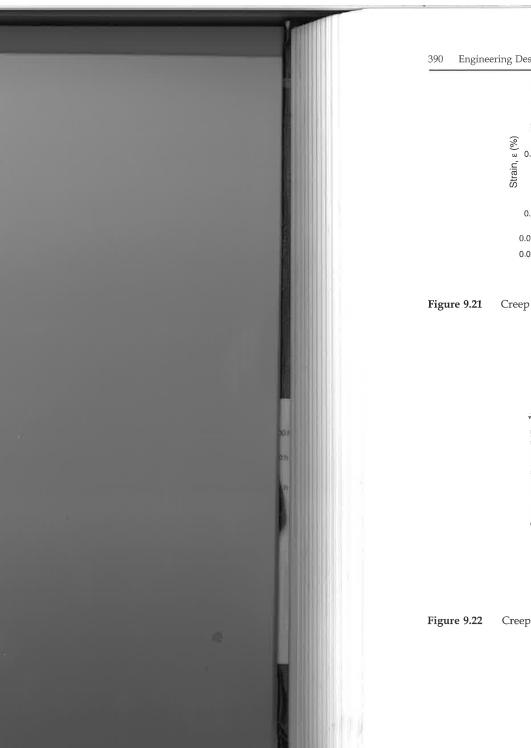
Creep data is very often presented in terms of creep modulus,  $E_{c}$ , defined by

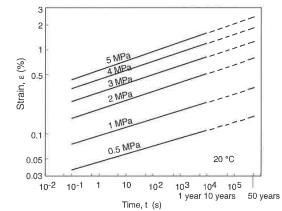
$$E_{\varepsilon} = \frac{\sigma_0}{\varepsilon(t)} \tag{9.35}$$

Depending on the time scale of the experiment, a property that also varies considerably during testing is Poisson's ratio, v. Figure 9.24 [14] shows Poisson's ratio for PMMA deformed at rates (%/h) between 10-2 (creep) and 10<sup>3</sup> (impact). The limits are v = 0.5 (fluid) for high temperatures or very slow deformation speeds and v = 0.33 (solid) at low temperatures or high



MacNeil Exhibit 2117 Yita v. MacNeil IP, IPR2020-01139 Page 205







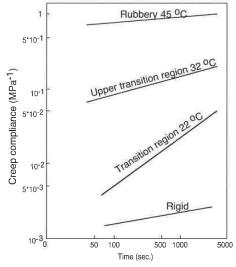


Figure 9.22 Creep compliance of a plasticized PVC at different temperatures.

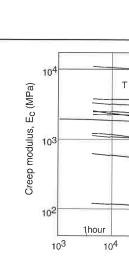
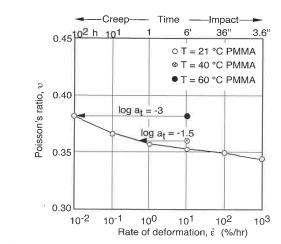


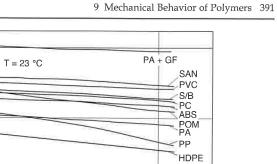
Figure 9.23 Time dependence of creep moduli for several polymer,



temperatures.

9.3.1 Isochronous and Isometric Creep Plots

Typical creep test data, as shown in Fig. 9.20, can be manipulated to be displayed as short-term stress-strain tests or as stress relaxation tests. These manipulated creep-test-data curves are called isochronous and isometric graphs.



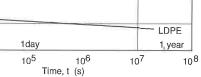


Figure 9.24 Poisson's ratio as a function of rate of deformation for PMMA at various



An isochronous plot of the creep data is generated by cutting sections through the creep curves at constant times and plotting the stress as a function of strain. The isochronous curves of the creep data displayed in Fig. 9.20 are presented in Fig. 9.25 [17]. Similar curves can also be generated by performing a series of *short creep tests*, where a specimen is loaded at a specific stress for a short period of time, typically around 100 s [20]. The load is then removed, and the specimen is allowed to relax for a period of 4 times greater than the time of the creep test. The specimen is then reloaded at a different stress, and the test is repeated until a sufficient number of points exists to plot an isochronous graph. This procedure is less time-consuming than the regular creep test and is often used to predict the short-term behavior of polymers. However, it should be pointed out that the short-term tests described in Section 9.2.2 are more accurate and are less time consuming and cheaper to perform.

The isometric or "equal size" plots of the creep data are generated by taking constant strain sections of the creep curves and by plotting the stress as a function of time. Isometric curves of the polypropylene creep data presented in Fig. 9.20 are shown in Fig. 9.26 [17]. This plot resembles the stress relaxation test results and is often used in the same manner. When we divide the stress axis by the strain, we can also plot the modulus versus time.

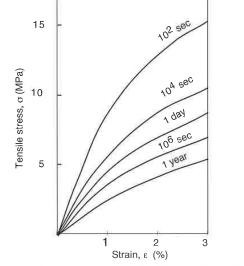
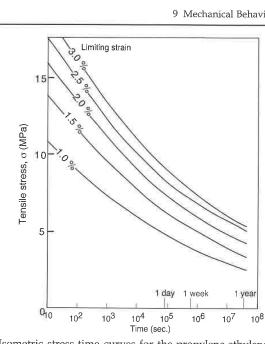


Figure 9.25 Isochronous stress-strain curves for the propylene-ethylene copolymer creep responses shown in Fig. 9.20.



responses shown in Fig. 9.20.

# 9.4 Dynamic Mechanical Tests

#### 9.4.1 Torsion Pendulum

The simplest dynamic mechanical test is the torsion pendulum. The standard procedure for the torsional pendulum, schematically shown in Fig. 9.27 [21], is described in DIN 53445 and ASTM D2236. The technique is applicable to virtually all plastics, through a wide range of temperatures; from the temperature of liquid nitrogen, -180 °C to 50-80 °C above the glass transition temperature in amorphous thermoplastics and up to the melting temperature in semi-crystalline thermoplastics. With thermoset polymers one can apply torsional tests up to the degradation temperatures of the material.

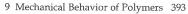
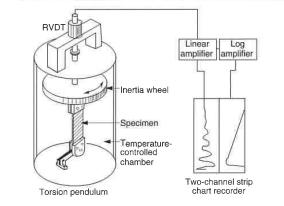


Figure 9.26 Isometric stress-time curves for the propylene-ethylene copolymer creep







The torsion pendulum apparatus is made up of an inertia wheel, grips, and the specimen contained in a temperature-controlled chamber. The rectangular test specimen can be cut from a polymer sheet or part, or it can be made by injection molding. To execute the test the inertia wheel is deflected, then released and allowed to oscillate freely. The angular displacement or twist of the specimen is recorded over time. The frequency of the oscillations is directly related to the elastic shear modulus of the specimen, G', and the decay of the amplitude is related to the damping or *logarithmic decrement*,  $\Delta$ , of the material. The elastic shear modulus (Pascals) can be computed using the relation<sup>2</sup>

$$G' = \frac{6.4\pi^2 I L f^2}{\mu b t^3}$$
(9.36)

where I is the polar moment of inertia  $(g/cm^2)$ , L the specimen length (cm), f the frequency (Hz), b the width of the specimen, t the thickness of the specimen, and  $\mu$  a shape factor which depends on the width-to-thickness ratio. Typical values of  $\mu$  are listed in Table 9.2 [18]. The logarithmic decrement can be computed using

$$\Delta = \ln \left( \frac{A_n}{A_{n+1}} \right) \tag{9.37}$$

where *A*<sub>n</sub> represents the amplitude of the nth oscillation.<sup>3</sup> Although the elastic shear modulus, G', and the logarithmic decrement,  $\Delta$ , are sufficient to characterize a material, one can also compute the loss modulus G" by using

<sup>2</sup> For more detail, please consult ASTM D2236.

3 When  $\Delta > 1$ , a correction factor must be used to compute *G*'. See ASTM D2236.

Table 9.2	Table 9.2         Shape Factor µ for Various Rectangular Cross-Sections				
Ratio of	specimen width to thickness	μ			
	1.0	2.249			
	1.2	2.658			
	1.4	2.990			
	1.6	3.250			
	1.8	3.479			
	2.0	3.659			
	2.5	3.990			
	3.0	4.213			
	4.0	4.493			
	5.0	4.662			
	10.0	4.997			
	50.0	5.266			
	$\infty$	5.333			

The logarithmic decrement can also be written in terms of *loss tangent*, tan  $\delta$ , where  $\delta$  is the out-of-phase angle between the strain and stress responses. The loss tangent is defined as

tar

Figures 9.28 [1] and 9.29 [1] show the elastic shear modulus and the loss tangent for high impact polystyrene, and various polypropylene grades, respectively. In the graph for high impact polystyrene, the glass transition temperatures for polystyrene at 120 °C and for butadiene at -50 °C, are visible. For the polypropylene grades, the glass transition temperatures and the melting temperatures can be seen. The vertical scale in plots such as Figs. 9.28 and 9.29 is usually a logarithmic scale. However, a linear scale better describes the mechanical behavior of polymers in design aspects. Figure 9.30 [1] presents the elastic shear modulus on a linear scale for several thermoplastic polymers as a function of temperature.

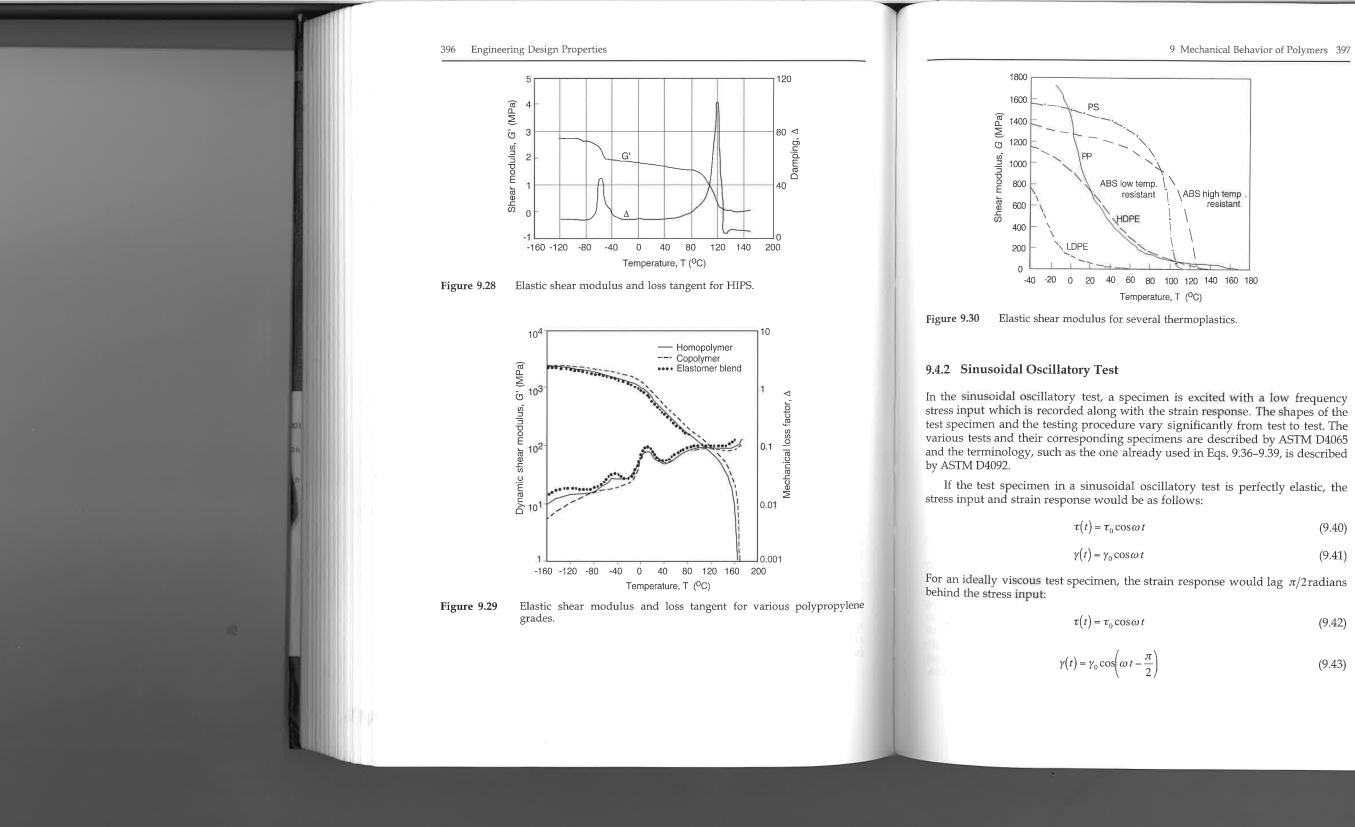
9 Mechanical Behavior of Polymers 395

$$G'' = \left(\frac{G'\Delta}{\pi}\right)$$

(9.38)

$$\delta = \frac{G''}{G'} = \frac{\Delta}{\pi} \tag{9.39}$$





9 Mechanical Behavior of Polymers 397

$(t) = \tau_0 \cos \omega t$	(9.40)
------------------------------	--------

(9.41)

(9.42)

$$=\gamma_0 \cos\left(\omega t - \frac{\pi}{2}\right) \tag{9.43}$$



Polymers behave somewhere in between the perfectly elastic and the perfectly viscous materials and their response is described by

$$\tau(t) = \tau_0 \cos \omega t \quad \text{and} \tag{9.44}$$

$$\gamma(t) = \gamma_0 \cos(\omega t - \delta) \tag{9.45}$$

The shear modulus takes a complex form of

$$G^* = \frac{\tau(t)}{\gamma(t)} = \frac{\tau_0 e^{i\delta}}{\gamma_0} = \frac{\tau_0}{\gamma_0} (\cos\delta + i\sin\delta) = G' + G''$$
(9.46)

which is graphically represented in Fig. 9.31. G' is usually referred to as storage *modulus* and *G*<sup>"</sup> as *loss modulus*. The ratio of loss modulus to storage modulus is referred to as *loss tangent*:

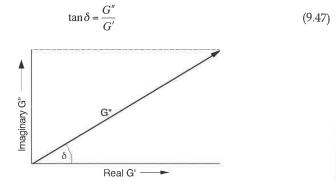


Figure 9.31 Vector representation of the complex shear modulus.

#### Viscoelastic Behavior of Polymers 9.5

Linear viscoelastic models were already introduced in Chapter 2. The main assumptions made in linear viscoelasticity is that the deformations must be small and that various loadings at different times are simply superimposed on one another as stated by Boltzmann's superposition principle. Several models exist to simulate the linear viscoelastic behavior of polymers. These physical models are generally composed of one or several elements such as dashpots, springs, or friction elements that represent viscous, elastic, or yielding properties,

respectively. All models must satisfy the momentum balance and continuity or deformation equation, along with the appropriate constitutive laws. The most commonly used constitutive equations are the viscous or Newtonian model, which is written as

and the linear elastic or Hookean model, which is represented by

where  $\eta$  and *E* are the viscosity and Young's modulus, respectively.

#### 9.5.1 Kelvin Model

The Kelvin model, sometimes also called the Kelvin-Voigt model, is shown in Fig. 9.32. It is the simplest model that can be used to represent the behavior of a solid polymer component at the beginning of loading.

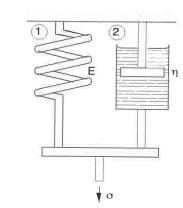


Figure 9.32 Schematic diagram of the Kelvin model. The momentum balance for the Kelvin model is stated as  $\sigma = \sigma_1 + \sigma_2$ and the continuity equation is represented by  $\varepsilon = \varepsilon_1 = \varepsilon_2$ 

governing equation, Eq. 9.50, can be rewritten as

9 Mechanical Behavior of Polymers 399

 $\sigma = \eta \dot{\varepsilon}$ (9.48)

 $\sigma = E\varepsilon$ (9.49)

Using Eq. 9.51 with the constitutive relations in Eqs. 9.48 and 9.49, the



MacNeil Exhibit 2117 Yita v. MacNeil IP, IPR2020-01139 Page 210

(9.50)

(9.51)



$$E\varepsilon + \eta\dot{\varepsilon}$$
 (9.52)

#### 9.5.1.1 Kelvin Model Creep Response

Using Eq. 9.52, the strain in a creep test in the Kelvin model can be solved for as

$$\varepsilon(t) = \frac{\sigma_0}{E} \left( -e^{-t/\lambda} \right) \tag{9.53}$$

where  $\lambda$ , (*E*/ $\eta$ ), is the relaxation time. The creep modulus is defined as

$$E_c(t) = \frac{E}{\left(1 - e^{-t/\lambda}\right)} \tag{9.54}$$

The creep response of the Kelvin model is shown in Fig. 9.33.

 $\sigma = 1$ 

#### 9.5.1.2 Kelvin Model Stress Relaxation

In the Kelvin model the stress does not relax and remains constant at

$$\sigma = E\varepsilon_0 \tag{9.55}$$

Time

This is shown in Fig. 9.33.

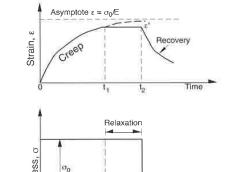


Figure 9.33 Creep, relaxation, and recovery response of the Kelvin model.

t.

# 9.5.1.3 Kelvin Model Strain Recovery

written as

and is represented in Fig. 9.33.

#### 9.5.1.4 Kelvin Model Dynamic Response

strain given by

### εĺ

where  $\varepsilon_0$  is the strain amplitude and  $\omega$  is the frequency. Differentiating Eq. 9.57 and substituting into Eq. 9.52 results in

$$\sigma(t) = E\varepsilon_0$$

Dividing Eq. 9.58 by the strain amplitude results in the complex modulus, which is formed by the storage modulus defined by

and the loss modulus given by

# 9.5.2 Jeffrey Model

The momentum balance equations as

as is the continuity equation by

9 Mechanical Behavior of Polymers 401

Since the stresses do not relax in a Kelvin model, the full shape of the original component or specimen can be recovered. The strain recovery response can be

$$\varepsilon(t) = \varepsilon_0 e^{-t/\lambda} \tag{9.56}$$

We can also consider the response of a Kelvin model subjected to a sinusoidal

$$(t) = \varepsilon_0 \sin(\omega t) \tag{9.57}$$

 $\varepsilon_0 \sin(\omega t) + \eta \omega \varepsilon_0 \cos(\omega t)$ (9.58)

$$E' = E \tag{9.59}$$

 $E'' = \eta \omega$ (9.60)

As shown in Fig. 9.34, the Jeffrey model is a Kelvin model with a dashpot. This extra feature adds the missing long-term creep to the Kelvin model.

of the Jeffrey model is re	epresented by two
----------------------------	-------------------

$\sigma = \sigma_3$ and	(9.61)
$\sigma = \sigma_1 + \sigma_2$	(9.62)



$$\varepsilon_1 = \varepsilon_2$$
 and (9.63)

$$\varepsilon = \varepsilon_2 + \varepsilon_3 \tag{9.64}$$

Combining Eq. 9.61–9.64 and applying the constitutive equations gives

$$\sigma + \left(\frac{\eta_1 + \eta_3}{E_2}\right)\dot{\sigma} = \eta_3 \dot{\varepsilon} + \left(\frac{\eta_3 \eta_1}{E_2}\right)\ddot{\varepsilon}$$
(9.65)

which is sometimes written as

$$\sigma + \lambda_1 \dot{\sigma} = \eta_0 (\dot{\varepsilon} + \lambda_2 \ddot{\varepsilon}) \tag{9.66}$$

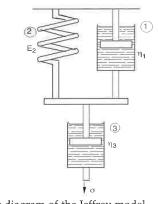


Figure 9.34 Schematic diagram of the Jeffrey model.

9.5.2.1 Jeffrey Model Creep Response

Using Eq. 9.66, the strain in a creep test in the Jeffrey model can be solved for as

$$\varepsilon(t) = \frac{\sigma_0}{E} \left( 1 - e^{-t/\lambda_2} \right) + \frac{\sigma_0}{\eta_0} t \tag{9.67}$$

and is depicted in Fig. 9.35. The creep modulus of the Jeffrey model is written as

$$E_{c}(t) = \left(\frac{\left(1 - e^{-t/\lambda_{2}}\right)}{E} + \frac{t}{\eta_{3}}\right)^{-1}$$
(9.68)

Figure 9.35 Creep, relaxation and recovery response of the Jeffrey model.

### 9.5.2.2 Jeffrey Model Stress Relaxation

equation, Eq. 9.66 as

and is also represented in Fig. 9.35.

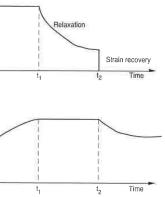
9.5.2.3 Jeffrey Model Strain Recovery

The unrelaxed stress is recovered in the same way as in the Kelvin model

9.5.3 Standard Linear Solid Model

The standard linear solid model, shown in Fig. 9.36, is a commonly used model to simulate the short-term behavior of solid polymer components. The momentum balance of the standard linear solid model is expressed with two equations as

9 Mechanical Behavior of Polymers 403



The stress relaxation of the Jeffrey model is derived from the governing

 $\sigma = \sigma_0 e^{-t/\lambda_1}$ (9.69)

 $\varepsilon(t) = \varepsilon_0 e^{-t/\lambda}$ (9.70)

 $\sigma = \sigma_1 + \sigma_2$ 

(9.71)



Continuity or deformation is represented with

$$\varepsilon = \varepsilon_1 + \varepsilon_3 \tag{9.73}$$

(9.72)

and

(9.74)

When we combine Eqs. 9.71–9.74 and use the constitutive equations for the spring and dashpot elements, we get the governing equation for the standard linear solid model:

 $\sigma_1 = \sigma_3$ 

 $\varepsilon = \varepsilon_2$ 

$$\eta \dot{\sigma} + E_1 \sigma = \eta (E_1 + E_2) \dot{\varepsilon} + E_1 E_2 \varepsilon$$
(9.75)

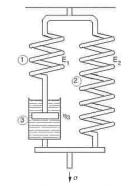


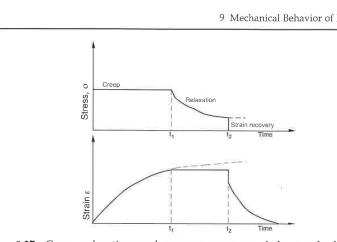
Figure 9.36 Schematic diagram of the standard linear solid model.

#### 9.5.3.1 Standard Linear Solid Model Creep Response

Using Eq. 9.75, the strain in a creep test in the standard linear solid model can be solved for as

$$\varepsilon = \frac{\sigma_0}{E_2} + \left(\frac{\sigma_0}{E_1 + E_2} - \frac{\sigma_0}{E_2}\right) e^{-(E_1 E_2 / \eta (E_1 + E_2))/2}$$
(9.76)

and is plotted in Fig. 9.37.



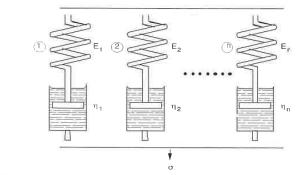
model.

# 9.5.3.2 Standard Linear Solid Model Stress Relaxation

The stress relaxation of the standard linear solid model can be derived by integrating Eq. 9.75 and is represented by

# 9.5.4 Maxwell-Wiechert Model

The Maxwell-Wiechert model, shown in Fig. 9.38, is a generalized model which consists of an arbitrary number of Maxwell models connected in parallel.



9 Mechanical Behavior of Polymers 405

Figure 9.37 Creep, relaxation, and recovery response of the standard linear solid

 $\sigma = \varepsilon_0 (E_2 + E_1) e^{-(E_1/\eta)t}$ (9.77)

Figure 9.38 Schematic diagram of the Maxwell-Wiechert model.



MacNeil Exhibit 2117 Yita v. MacNeil IP, IPR2020-01139 Page 213

The momentum balance in the ith Maxwell element of the Maxwell-Wiechert model is expressed as

$$=\sigma_{i1} + \sigma_{i2} \tag{9.78}$$

and the full momentum balance for a model with n elements is written as

 $\sigma_1$ 

$$\sigma = \sum_{i=1}^{n} \sigma_i \tag{9.79}$$

Continuity or deformation for the ith Maxwell element is expressed as

$$\varepsilon_i = \varepsilon_{i1} + \varepsilon_{i2} \tag{9.80}$$

and for the full model

$$\varepsilon = \varepsilon_1 = \varepsilon_2 = \varepsilon_i \dots \tag{9.81}$$

The governing equation for the Maxwell-Wiechert model is written as

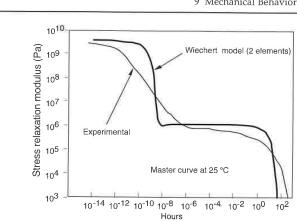
$$\dot{\varepsilon} = \frac{\dot{\sigma}_i}{E_i} + \frac{\sigma_i}{\eta_i} \tag{9.82}$$

#### 9.5.4.1 Maxwell-Wiechert Model Stress Relaxation

The stress relaxation of the Maxwell-Wiechert model can be derived by integrating Eq. 9.82 and substituting the resulting stress into Eq. 9.79. Dividing by the applied strain  $\varepsilon_0$  results in an expression for the relaxation model which is written as

$$E(t) = \sum_{i=1}^{n} E_{i} e^{-(1/\lambda_{i})t}$$
(9.83)

which represents a model with *n* relaxation times and where  $\lambda_i = \eta_i / E_i$ . As an example, we can approximate the relaxation behavior of the polyisobutylene shown in Fig. 2.29 by using a Maxwell-Wiechert model having two Maxwell elements with  $\lambda_1 = 10^{-8}$  h and  $\lambda_2 = 100$  h, and  $E_1 = 3 \times 10^9$  Pa and  $E_2 = 10^6$  Pa. Figure 9.39 compares the experimental relaxation modulus with the model. One can see that although there are big differences between the two curves, the model, with its two relaxation times, does at least qualitatively represent the experimental values.



# 9.5.4.2 Maxwell-Wiechert Model Dynamic Response

We can also consider the response of a Maxwell-Wiechert model subjected to a sinusoidal strain given by Eq. 9.57. In a similar analysis to that presented for the Kelvin model and for the Maxwell model in Chapter 2, the storage modulus is given by

$$E' = \sum_{i=1}^{n} \left( \frac{E_i (\omega_i \lambda_i)^2}{1 + (\omega_i \lambda_i)^2} \right)$$
(9.84)

and the viscous term or the loss modulus, is given by

$$E'' =$$

#### 9.6 Effects of Structure and Composition on Mechanical Properties

The shear modulus versus temperature diagram is a very useful description of the mechanical behavior of certain materials. It is possible to generate a general shear modulus versus temperature diagram for all polymers by using a reduced temperature described by

#### 9 Mechanical Behavior of Polymers 407

Figure 9.39 Comparison of the experimental stress relaxation for polyisobutylene to a two-component Maxwell-Wiechert model response.

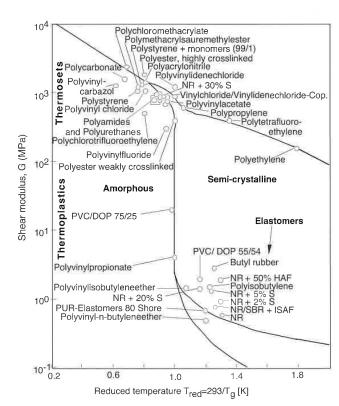
$$\sum_{i=1}^{n} \left( \frac{E_i \omega_i \lambda_i}{1 + (\omega_i \lambda_i)^2} \right)$$
(9.85)



MacNeil Exhibit 2117 Yita v. MacNeil IP, IPR2020-01139 Page 214

$$T_{red} = \frac{293K}{T_g}$$
 (9.86)

Fig. 9.40 [22] shows this diagram with the shear modulus of several polymers. The upper left side of the curve represents the stiff and brittle cross-linked materials, and the upper right side represents the semi-crystalline thermoplastics whose glass transition temperature is below room temperature. The lower right side of the curve represents elastomers, positioned accordingly on the curve depending on their degree of cross-linkage.



**Figure 9.40** Shear modulus of several polymers as a function of reduced glass transition temperature.

## 9.6.1 Amorphous Thermoplastics

Amorphous thermoplastics exhibit "useful" behavior below their glass transition temperature. Figure 9.41 shows the shear modulus of an unplasticized PVC with respect to temperature. In this figure we observe that the material solidifies at the glass transition temperature, between 80 and 90 °C. We note that one cannot exactly pinpoint T<sub>g</sub> but only a range within which it will occur. In fact, already at 60 °C the stiffness dramatically drops as the U-PVC starts to soften. Below -10 °C, the U-PVC becomes very stiff and brittle, making it useful only between -10 °C and 60 °C for most applications. As mentioned before, the properties of thermoplastics can be modified by adding plasticizing agents. This is shown for PVC in Fig. 9.42 where the shear modulus drops at much lower temperatures when a plasticizing agent is added.

Often the tensile stress and strain at failure are plotted as a function of temperature. Figure 9.43 shows this for a typical amorphous thermoplastic. The figure shows how the material is brittle below the glass transition temperature and, therefore, fails at low strains. As the temperature increases, the strength of the amorphous thermoplastic decreases, since it becomes leathery in texture and is able to withstand larger deformations. Above  $T_{\rm g}$ , the strength decreases significantly, as the maximum strain continues to increase, until the flow properties have been reached at which point the mechanical strength is negligible. This occurs around the "flow temperature" marked as  $T_{\rm f}$  in the diagram. If the temperature is further increased, the material will eventually thermally degrade at the degradation temperature,  $T_{\rm d}$ .

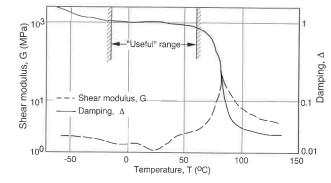
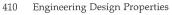
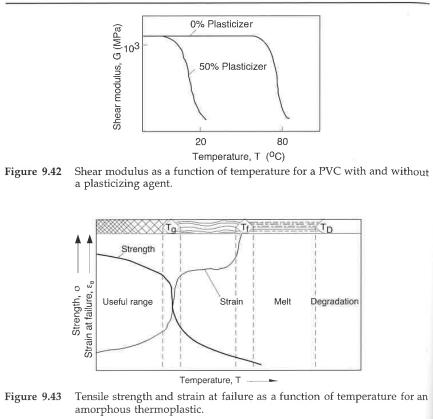


Figure 9.41 Shear modulus and mechanical damping for an unplasticized PVC.

9 Mechanical Behavior of Polymers 409







Some amorphous thermoplastics can be made high impact resistant (less brittle) through copolymerization. The most common example is acrylonitrilebutadiene-styrene, also known as ABS. Since butadiene chains vitrify at temperatures below -50 °C, ABS is very tough at room temperature in contrast to polystyrene and acrylics by themselves. Due to the different glass transition temperatures present in the materials which form the blend, ABS shows two general transition regions, one around -50 °C and the other at 110 °C, visible in both the logarithmic decrement and the shear modulus.

#### 9.6.2 Semi-Crystalline Thermoplastics

The properties of semi-crystalline thermoplastics can also be analyzed by plotting mechanical properties with respect to temperature. An interesting example is shown in Fig. 9.44, which presents plots of shear modulus versus temperature of a polystyrene with different molecular structures after having gone through different stereo-specific polymerization techniques: low molecular weight PS (A), a high molecular weight PS (B), a semi-crystalline PS (C), and a cross-linked PS (D). In Fig. 9.44 we can see that the low molecular weight material flows before the high molecular weight one, simply due to the fact that the shorter chains can slide past each other more easily- reflected in the lower viscosity of the low molecular weight polymer. The semi-crystalline PS shows a certain amount of stiffness between its glass transition temperature at around 100 °C and its melting temperature at 230 °C. Since a semi-crystalline polystyrene is still brittle at room temperature, it is not very useful to the polymer industry. Figure 9.44 also demonstrates that a cross-linked polystyrene will not melt.

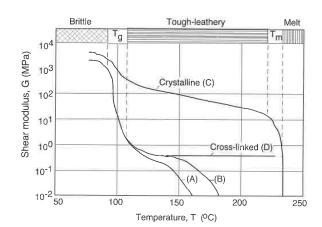


Figure 9.44

Semi-crystalline thermoplastics are leathery and tough at room temperature since their atactic and amorphous regions vitrify at much lower temperatures. Figure 9.45 shows the shear modulus plotted versus temperature for polypropylene at various degrees of crystallinity. In each case the amorphous regions "solidify" at around 0 °C, whereas the melting temperature goes up significantly with increasing degree of crystallinity. The brittle behavior of polypropylene at 0 °C can sometimes pose a problem in design. This problem can be mitigated through copolymerization - in this case PP copolymerized with ethylene or in elastomers such as ethylene-propylenediene terpolymer (EPDM).

9 Mechanical Behavior of Polymers 411

Shear modulus curves for amorphous, semi-crystalline and cross-linked polystyrene. (A) low molecular weight amorphous, (B) high molecular weight amorphous, (C) semi-crystalline, (D) cross-linked.



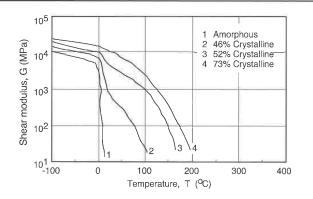
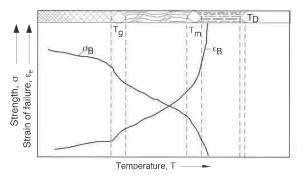
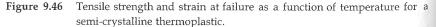


Figure 9.45 Shear modulus for polypropylene with various degrees of crystallinity.

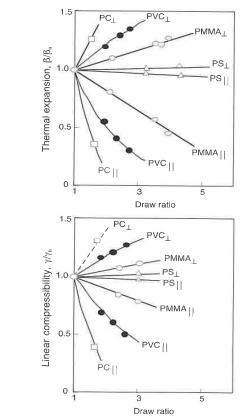
The tensile stress and the strain at failure for a common semi-crystalline thermoplastic is shown in Fig. 9.46. The figure shows an increase in toughness between the glass transition temperature and the melting temperature. The range between  $T_g$  and  $T_m$  applies to most semi-crystalline thermoplastics.

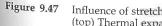




#### 9.6.3 Oriented Thermoplastics

If a thermoplastic is deformed at a temperature high enough so that the polymer chains can slide past each other but low enough such that the relaxation time is much longer than the time it takes to stretch the material, then the orientation generated during stretching is retained within the polymer component. We note that the amount of stretching,  $L/L_0$ , is not always proportional to the degree of orientation within the component; for example, if the temperature is too high during stretching, the molecules may have a chance to fully relax, resulting in a component with little or no orientation. Any degree of orientation results in property variations within thermoplastic polymers. Figure 9.47 [23] shows the influence stretching has on various properties of common amorphous thermoplastics. The stretching will lead to decreased strength and stiffness properties perpendicular to the orientation and increased properties parallel to the direction of deformation. In addition, highly oriented materials tend to split along the orientation direction under small loads.



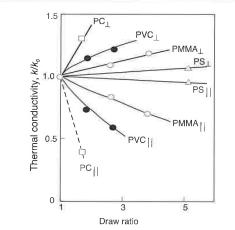


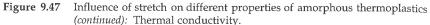
9 Mechanical Behavior of Polymers 413

Influence of stretch on different properties of amorphous thermoplastics: (top) Thermal expansion, (bottom) Linear compressibility (continued).

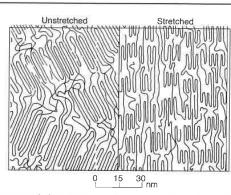


MacNeil Exhibit 2117 Yita v. MacNeil IP, IPR2020-01139 Page 217





In amorphous thermoplastics the stretching that leads to permanent property changes occurs between 20 and 40 °C above the glass transition temperature,  $T_{g}$ , whereas with semi-crystalline thermoplastics they occur between 10 and 20 °C below the melting temperature, Tm. After having stretched a semi-crystalline polymer, one must anneal it at temperatures high enough that the amorphous regions relax. During stretching the spherulites break up as whole blocks of lamellae slide out, shown schematically in Fig. 9.48 [24]. Whole lamellae can also rotate such that by sufficiently high stretching, all molecules are oriented in the same direction. The lamellae blocks are now interconnected by what is generally called tie molecules. If this material is annealed in a fixed position, a very regular, oriented structure can be generated. This highly oriented material becomes dimensionally stable at elevated temperatures, including temperatures slightly below the annealing or fixing temperature. However, if the component is not fixed during the annealing process, the structure before stretching would be recovered. Figure 9.49 has stress-strain plots for polyethylene with various morphological structures. If the material is stretched such that a needle-like or fibrilic morphological structure results, the resulting stiffness of the material is very high. Obviously, a more realistic structure that would result from stretching would lead to a stacked platelike structure with lower stiffness and ultimate strength. An unstretched morphological structure would be composed of spherulites and exhibit much lower stiffness and ultimate strength. The strength of fibrilic structures is taken advantage of when making synthetic fibers. Figure 9.50 shows theoretical and achievable elastic moduli of various synthetic fiber materials.



crystalline thermoplastics.

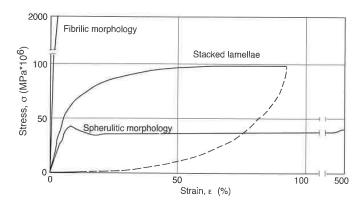
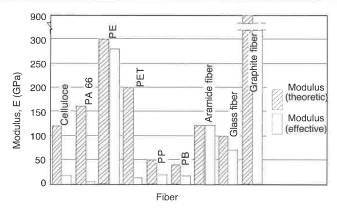
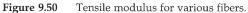


Figure 9.49 Stress-strain behavior of polyethylene with various morphologies.

9 Mechanical Behavior of Polymers 415

Figure 9.48 Schematic of the sliding and re-orientation of crystalline blocks in semi-

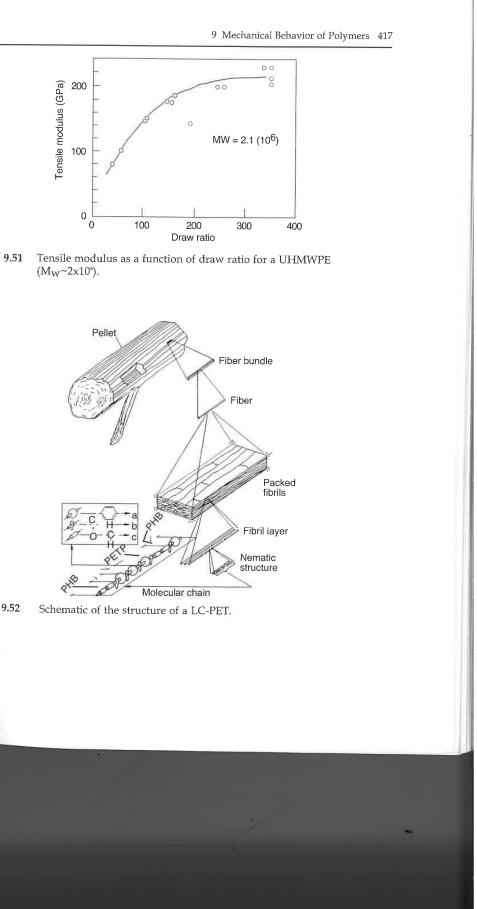


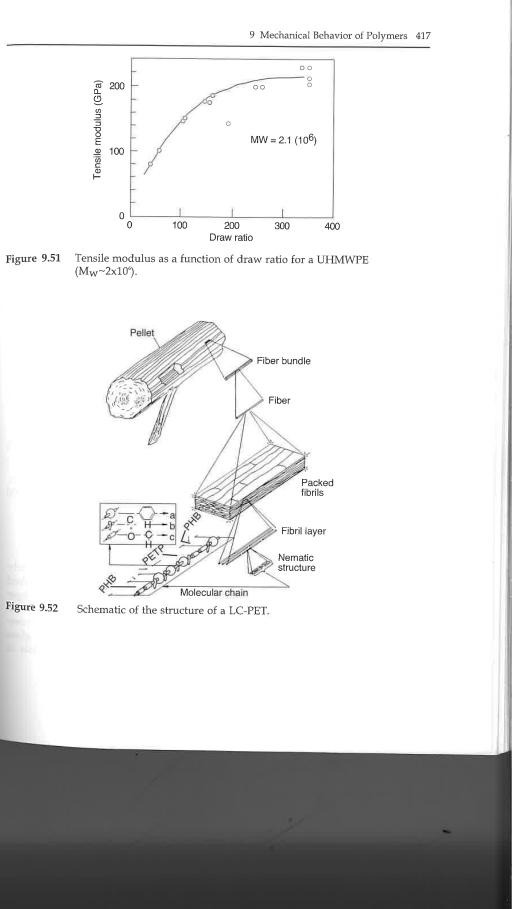


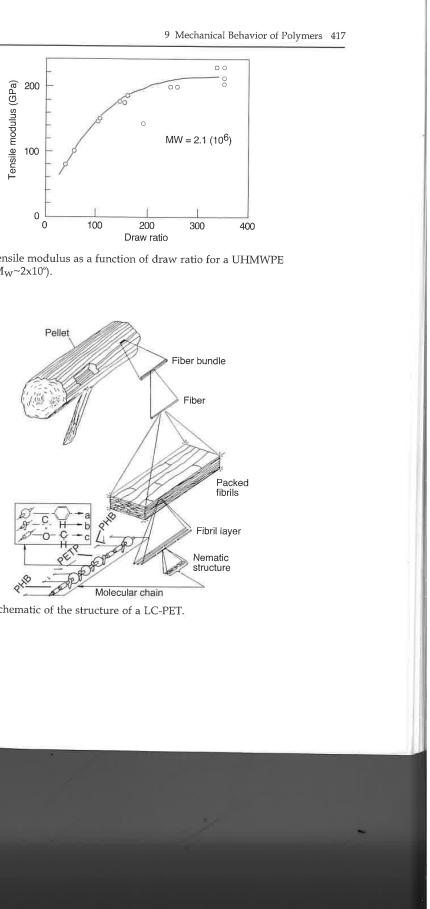
High-stiffness and high-strength synthetic fibers are becoming increasingly important for lightweight high-strength applications. Extended-chain ultrahigh molecular weight polyethylene fibers have only been available commercially since the mid 1980s. The fibers are manufactured by drawing or extending fibers of small diameters at temperatures below the melting point. The modulus and strength of the fiber increase with the drawing ratio or stretch. Due to intermolecular entanglement, the natural draw ratio of high molecular weight high-density polyethylene is only 5<sup>4</sup>. To increase the draw ratio by a factor of 10 or 100, polyethylene must be processed in a solvent such as paraffin oil or paraffin wax.

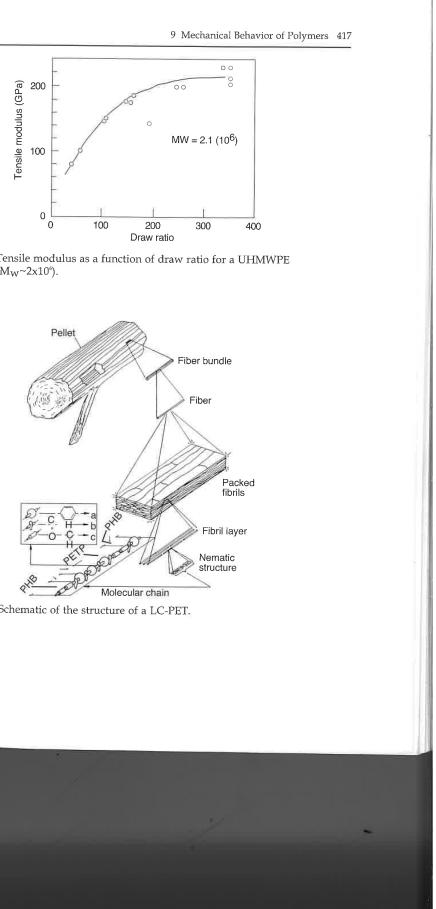
Figure 9.51 [25] presents the tensile modulus of super-drawn ultra-high molecular weight high-density polyethylene fibers as a function of draw ratio. It can be seen that at draw ratios of 250, a maximum modulus of 200 GPa is reached. In addition to amorphous and semi-crystalline thermoplastics, there is a whole family of thermoplastic materials whose molecules do not relax and, thus, retain their orientation even in the melt state. This class of thermoplastics is the liquid crystalline polymers. One such material is the aramid fiber, most commonly known by its tradename, Kevlar<sup>®</sup>, which has been available in the market for several years. To demonstrate the structure of liquid crystalline polymers, successive enlargement of an aramid pellet is shown in Fig. 9.52 [26]. For comparison, Table 9.3 presents mechanical properties of aramid and polyethylene fibers and other materials.

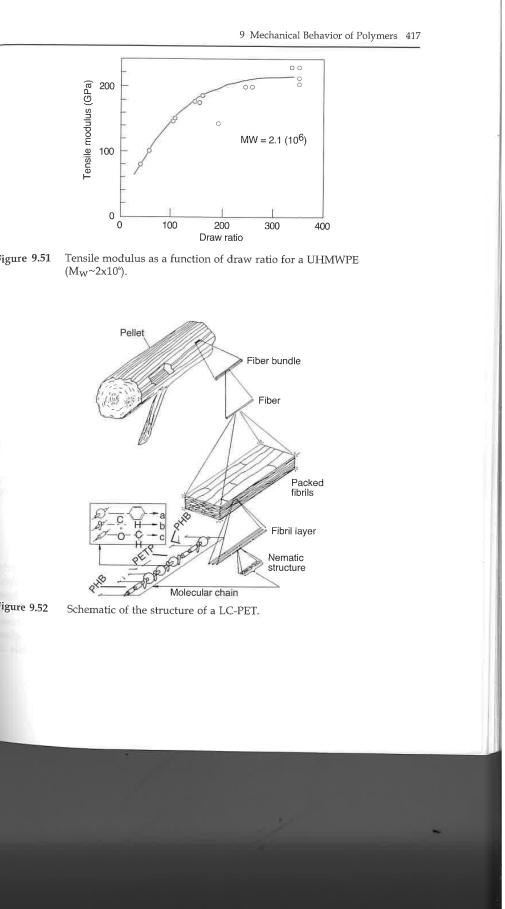
4 It is interesting that a semi-crystalline thermoplastic stretches more at low molecular weights than at high molecular weights. This contradicts what we expect from theory that longer molecules allow the component to stretch following the relation  $\lambda_{m} \approx M^{0.5}$ . An explanation for this may be the trapped entanglements found in high molecular weight, semi-crystalline polymers that act as semi-permanent cross-links which rip at smaller deformations.











MacNeil Exhibit 2117 Yita v. MacNeil IP, IPR2020-01139 Page 219

Table 9.3 Mec	Table 9.3         Mechanical Properties of Selected Fibers			
Fiber	Tensile strength (MPA)	Tensile modulus (GPa)	Elongation to break (%)	Specific gravity
Polyethylene	3000	172	2.7	0.97
Aramid	2760	124	2.5	1.44
Graphite	2410	379	0.6	1.81
S-glass	4585	90	2.75	2.50

The anisotropy of the oriented material can be approximated by assuming that there are covalent bonds joining the molecular chains along the orientation direction, whereas only van der Waals forces act in the two directions perpendicular to the main orientation. With this so called 1:2 rule, we can write

$$a_{\parallel} + 2a_{\perp} = 3a_{o} \quad \text{and} \tag{9.87}$$

$$a_1 + 2a_2 = 3a_0 \tag{9.88}$$

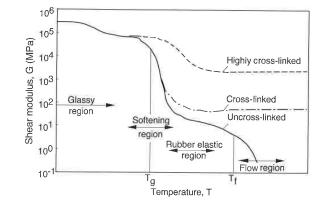
where  $a_0$  is the property for the isotropic material,  $a_1$  and  $a_2$  are the values for the fully oriented material, and  $a_{\parallel}$  and  $a_{\parallel}$  are the values that correspond to the parallel and perpendicular directions with respect to the main orientation. The actual degree of orientation in the above analysis is unknown. The 1:2 rule can be applied to strength properties such as elastic modulus and Poisson's ratio as well as to thermal expansion coefficient and thermal diffusivity. For the elastic modulus, we can write

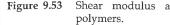
$$\frac{1}{E_{\parallel}} + \frac{2}{E_{\perp}} = \frac{3}{E_{0}}$$
(9.89)

This rule can be used to approximate mechanical properties of synthetic fibers. For example, a polypropylene fiber will have a tensile elastic modulus of 700 MPa compared to an elastic modulus of 30 MPa for the isotropic material.

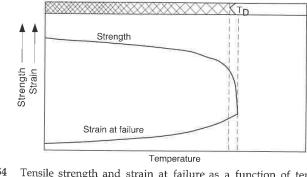
#### 9.6.4 Cross-Linked Polymers

Cross-linked polymers, such as thermosets and elastomers, behave completely differently than their counterparts, thermoplastic polymers. In cross-linked systems, the mechanical behavior is also best reflected by the plot of the shear modulus versus temperature. Figure 9.53 compares the shear modulus between highly cross-liked, cross-linked, and uncross-linked polymers. The coarse crosslinked system, typical of elastomers, has a low modulus above the glass transition temperature. The glass transition temperature of these materials is usually below -50 °C, so they are soft and flexible at room temperature. On the other hand, highly cross-linked systems, typical in thermosets, show a smaller decrease in stiffness as the material is raised above the glass transition temperature; the decrease in properties becomes smaller as the degree of crosslinking increases. Figure 9.54 shows ultimate tensile strength and strain curves plotted versus temperature. It is clear that the strength remains fairly constant up to the thermal degradation temperature of the material.





typical thermosets.



## 9 Mechanical Behavior of Polymers 419

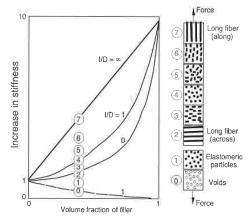
Figure 9.53 Shear modulus and behavior of cross-linked and uncross-linked

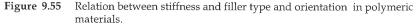
Figure 9.54 Tensile strength and strain at failure as a function of temperature for

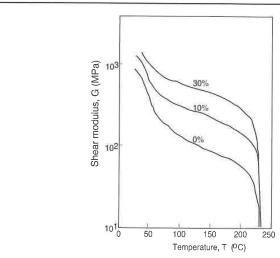
# 9.7 Mechanical Behavior of Filled and Reinforced Polymers

When we talk about fillers, we refer to materials that are intentionally placed in polymers to make them stronger, lighter, electrically conductive, or cheaper. Any filler will affect the mechanical behavior of a polymeric material. For example, long fibers will make it stiffer but usually denser, whereas foaming will make it more compliant but much lighter. On the other hand, a filler such as calcium carbonate will decrease the polymer's toughness while making it considerably cheaper. Figure 9.55 [27] shows a schematic plot of the change in stiffness as a function of volume fraction for several types of filler materials.

Figure 9.56 shows the increase in dynamic shear modulus for polybutylene terephthalate with 10 and 30% glass fiber content. However, fillers often decrease the strength properties of polymers - this is discussed in more detail in the next chapter.





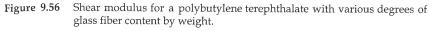


glass fiber content by weight.

However, when we refer to reinforced plastics, we talk about polymers (matrix) whose properties have been enhanced by introducing a reinforcement (fibers) of higher stiffness and strength. Such a material is usually called a fiber reinforced polymer (FRP) or a fiber reinforced composite (FRC). The purpose of introducing a fiber into a matrix is to transfer the load from the weaker material to the stronger one. This load transfer occurs over the length of the fiber as schematically represented in Fig. 9.57. The length it takes to complete the load transfer from the matrix to the fiber, without fiber or matrix fracture, is usually referred to as critical length, L<sub>c</sub>. For the specific case where there is perfect adhesion between fiber and matrix, the critical length can be computed as

where *D* is the fiber diameter,  $\sigma_{uf}$  is the tensile strength of the fiber and  $\tau_{um}$  is the shear strength of the matrix. Although Eq. 9.90 predicts L/D as low as 10, experimental evidence suggests that aspect ratios of 100 or higher are required to achieve maximum strength [28]. If composites have fibers that are shorter than their critical length they are referred to as short fiber composites, and if the fibers are longer they are referred to as long fiber composites [29].

9 Mechanical Behavior of Polymers 421



$$L_c = D \frac{\sigma_{if}}{2\tau_{max}} \tag{9.90}$$



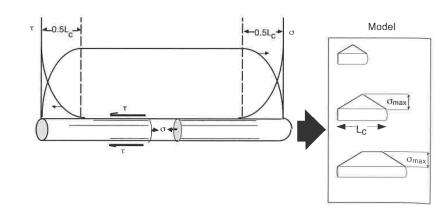


Figure 9.57 Schematic diagram of load transfer from matrix to fiber in a composite.

### 9.7.1 Anisotropic Strain-Stress Relation

.

As discussed in Chapter 6, filled polymers are often anisotropic, and the relations presented in Eqs. 9.1-9.15 are not valid. The three-dimensional anisotropic strain-stress relation where, for simplicity, x, y, and z have been replaced by 1, 2, and 3, respectively, is often written as

$$\varepsilon_{11} = \frac{1}{E_{11}} \sigma_{11} - \frac{\nu_{21}}{E_{22}} \sigma_{22} - \frac{\nu_{31}}{E_{33}} \sigma_{33}$$
(9.91)

$$\varepsilon_{22} = -\frac{\nu_{12}}{E_{11}}\sigma_{11} + \frac{1}{E_{22}}\sigma_{22} - \frac{\nu_{32}}{E_{33}}\sigma_{33}$$
(9.92)

$$\varepsilon_{33} = -\frac{v_{13}}{E_{11}}\sigma_{11} - \frac{v_{23}}{E_{22}}\sigma_{22} + \frac{1}{E_{33}}\sigma_{33}$$
(9.93)

$$\gamma_{12} = \frac{1}{G_{12}} \tau_{12} \tag{9.94}$$

$$\gamma_{23} = \frac{1}{G_{23}} \tau_{23} \tag{9.95}$$

and in matrix form for the more general case:

	2 3		2	
	$\varepsilon_{11}$		$S_{11}$	$S_{12}$
	$\varepsilon_{22}$		$S_{21}$	$S_{22}$
ļ	$\varepsilon_{33}$	_	$S_{31}$	$S_{32}$
	$\gamma_{12}$		$S_{41}$	$S_{42}$
	$\gamma_{23}$		$S_{51}$	$S_{52}$
	γ <sub>31</sub>		$S_{61}$	$S_{62}$

where coupling between the shear terms and the elongational terms can be introduced.

# 9.7.2 Aligned Fiber Reinforced Composite Laminates

The most often applied form of the above equations is the two-dimensional model used to analyze the behavior of aligned fiber reinforced laminates, such as that shown schematically in Fig. 9.58. For this simplified case, Eqs. 9.91-9.96 reduce to

$$\varepsilon_L = \frac{1}{E_L} \sigma_L - \frac{\nu_{TL}}{E_T} \sigma_T \tag{9.98}$$

 $\mathcal{E}_T = \cdot$ 

#### 2

which can also be written as

### $\{\varepsilon_{LT}\}$

matrix.

9 Mechanical Behavior of Polymers 423

$$\gamma_{31} = \frac{1}{G_{31}} \tau_{31} \tag{9.96}$$

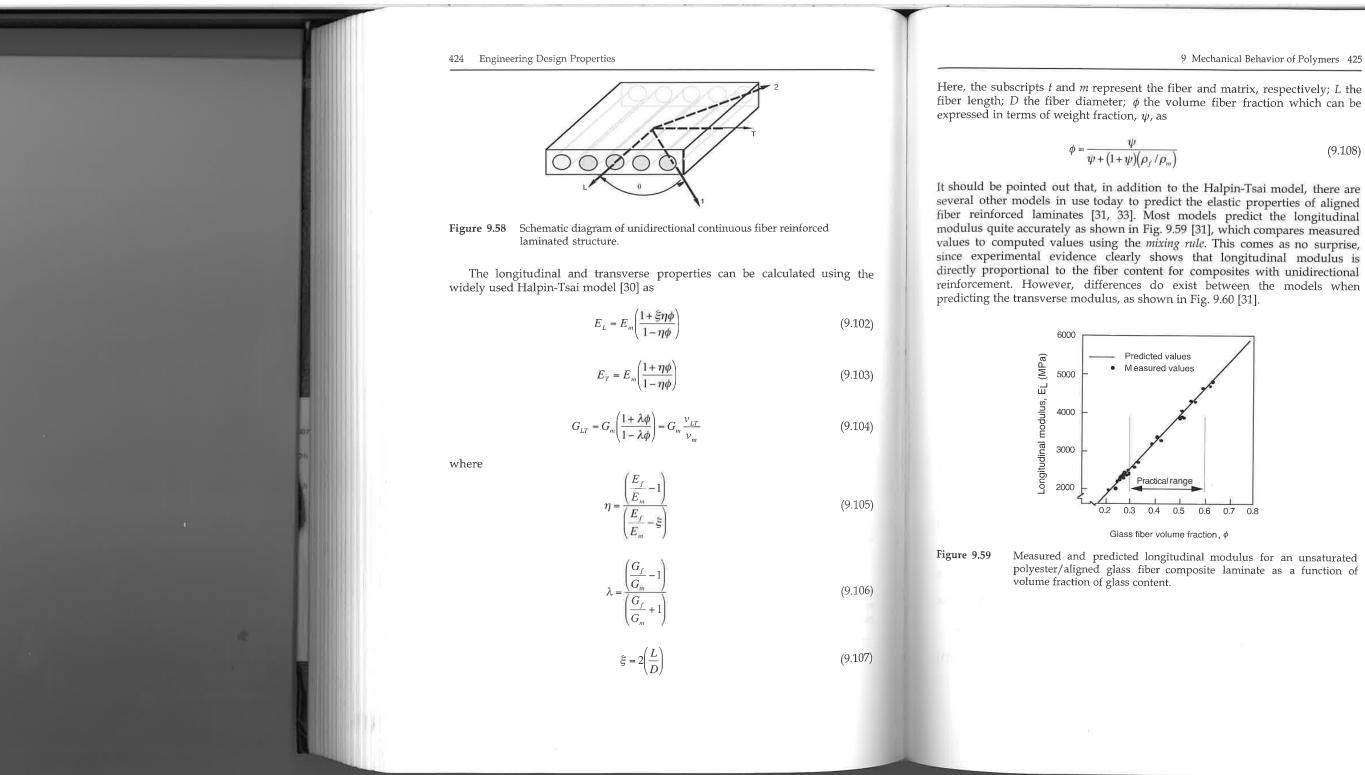
$$-\frac{\nu_{LT}}{E_L}\sigma_L + \frac{1}{E_T}\sigma_T \tag{9.99}$$

$$\} = [S_{LT}]\{\sigma_{LT}\}$$
(9.101)

where the subscripts *L* and *T* define the longitudinal and transverse directions, respectively, as described in Fig. 9.58, and  $[S_{LT}]$  is referred to as the compliance



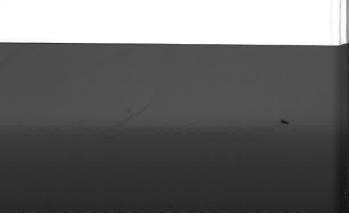
MacNeil Exhibit 2117 Yita v. MacNeil IP, IPR2020-01139 Page 222



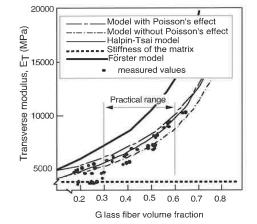
9 Mechanical Behavior of Polymers 425

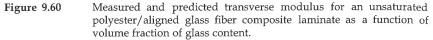
$$\frac{\psi}{\psi + (1+\psi)(\rho_f/\rho_m)} \tag{9.108}$$

polyester/aligned glass fiber composite laminate as a function of



MacNeil Exhibit 2117 Yita v. MacNeil IP, IPR2020-01139 Page 223





# 9.7.3 Transformation of Fiber Reinforced Composite Laminate Properties

The loading in a laminated structure is not always aligned with the transverse and longitudinal directions of the reinforcement. Hence, it is often necessary to rotate the laminate and its properties by an angle  $\theta$ . Figure 9.58 depicts the laminate's material coordinate system L-T and a rotated arbitrary coordinate system 1-2. If we rotate the axes from the 1-2 system to the L-T system, we can transform the stress components using

$$\begin{cases} \sigma_{L} \\ \sigma_{T} \\ \tau_{LT} \end{cases} = \begin{bmatrix} c^{2} & s^{2} & 2sc \\ s^{2} & c^{2} & -2sc \\ -sc & sc & (c^{2} - s^{2}) \end{bmatrix} \begin{bmatrix} \sigma_{11} \\ \sigma_{22} \\ \tau_{12} \end{bmatrix} \quad \text{or}$$
(9.109)

$$\{\sigma_{LT}\} = [T_{\sigma}]\{\sigma_{12}\} \tag{9.110}$$

The transformation of the strain components carry an extra 1/2 term for the shear strains and is written as

$$\begin{cases} \varepsilon_L \\ \varepsilon_T \\ \gamma_{LT} \end{cases} = \begin{bmatrix} c^2 & s^2 & sc \\ s^2 & c^2 & -sc \\ -2sc & 2sc & (c^2 - s^2) \end{bmatrix} \begin{bmatrix} \varepsilon_{11} \\ \varepsilon_{22} \\ \gamma_{12} \end{bmatrix}$$
 or (9.111)

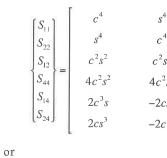
{ε,

Combining Eq. 9.101 with the above transformations, we can write

or

$$\left\{\varepsilon_{12}\right\} = \left[T_{\varepsilon}\right]^{-1} \left[S_{LT}\right] \left[T\sigma\right] \left\{\sigma_{12}\right\}$$
(9.114)

The compliance matrix in the L-T coordinate system has four independent components and the 1-2 system has six. The inverse of  $[T_{\varepsilon}]$  is equivalent to rotating the coordinates back by -θ. This leads to



 $\{S_{12}\} = \left\lceil R(\theta) \right\rceil \{S_{LT}\}$ 

9 Mechanical Behavior of Polymers 427

$$\{\boldsymbol{\varepsilon}_{LT}\} = [\boldsymbol{T}_{\varepsilon}]\{\boldsymbol{\varepsilon}_{12}\}$$
(9.112)

 $[T_{\varepsilon}]{\varepsilon_{12}} = [S_{LT}][T\sigma]{\sigma_{12}}$ (9.113)

$$\begin{array}{ccccc} & & & & & & & & \\ & & & & & & & & \\ & & & & & & & & \\ s^2 & & & & & & & & \\ c^3 s^2 & & & & & & & & \\ c^3 s & & & & & & & \\ s^3 s & & & & & & & \\ \end{array} \left\{ \begin{array}{c} S_{LL} \\ S_{TT} \\ S_{LT} \\ S_{SS} \end{array} \right\}$$
(9.115)

(9.116)

The engineering elastic constants in the 1-2 system can easily be computed:

$E_{11} = \frac{1}{S_{11}}$	(9.117)
$E_{22} = \frac{1}{S_{22}}$	(9.118)
$G_{12} = \frac{1}{S_{44}}$	(9.119)
$v_{12} = -\frac{S_{12}}{S_{11}}$	(9.120)
$v_{21} = -\frac{S_{12}}{S_{22}}$	(9.121)



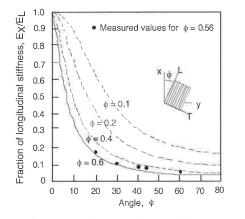
$$\eta_{14} = \frac{S_{14}}{S_{11}} \tag{9.122}$$

$$\eta_{24} = \frac{S_{24}}{S_{22}} \tag{9.123}$$

(9.124)

(9.125)

Figure 9.61 [33] shows how the stiffness decreases as one rotates away from the longitudinal axis for an aligned fiber reinforced composite with different volume fraction fiber content. From the figure it is evident that for high volume fraction fiber contents only a slight misalignment of the fibers from the loading direction results in a drastic reduction of the properties. Along with the predicted stiffness properties, the figure also presents the stiffness for a composite with 0.56 volume fraction of fibers measured at various angles from the longitudinal axis of the composite. The measured and the predicted values agree quite well.



Measured and predicted elastic modulus in a unidirectional fiber Figure 9.61 reinforced laminate as a function of angle between loading and fiber direction.

# 9.7.4 Reinforced Composite Laminates with a Fiber Orientation **Distribution Function**

The above transformation can be used to compute the properties of planar systems with a fiber orientation distribution function. This is done by superposing aligned fiber laminates rotated away from the principal 1-2 coordinate system by an angle  $\theta$  and with a volume fiber fraction given by  $\psi(\theta)$ . The transformation is written as

$$\{S_{12}\} = \int_{-2}^{2}$$

which can be written in discrete terms to be used with fiber orientation distribution function attained from computer simulation:

$$\left\{S_{12}\right\} = \sum_{i=1}^{N}$$

Using Eq. 9.126, one can easily predict the stiffness properties of a part with randomly oriented fibers, where  $\psi(\theta) = 1/\pi$ , using<sup>5</sup>

$$\frac{1}{E_{11}} = \frac{1}{E_{22}} = \frac{1}{E_{random}}$$

#### 9.8 Strength Stability Under Heat

As mentioned earlier, polymers soften and eventually flow as they are heated. It is, therefore, important to know what the limiting temperatures are at which a polymer component can still be loaded with moderate deformations. Three tests are commonly performed on polymer specimens to determine this limiting temperature for that material. They are the Vicat temperature test (DIN 53460), shown in Fig. 9.62, the Martens temperature test (DIN 53458 or 53462), and the heat-distortion temperature (HDT) test (ASTM D 648-72) shown in Fig. 9.636.

- 6 Courtesy of BASF.

9 Mechanical Behavior of Polymers 429

$$\int_{\frac{1}{2}}^{\frac{1}{2}} \left( \left[ R(\theta) \right] \{ S_{LT} \} \psi(\theta) \right) d\theta \tag{9.126}$$

$$\left(\left[R(\theta_i)|\{S_{LT}\}\psi(\theta_i)\right]\Delta\theta\right)$$
(9.127)

$$=\frac{3}{8}\frac{1}{E_L} + \frac{3}{8}\frac{1}{E_T} - \frac{2}{8}\frac{v_{LT}}{E_L} + \frac{1}{8}\frac{1}{G_{LT}}$$
(9.128)

5 The incorrect expression  $E_{Rouber} = 3 / 8E_L + 5 / 8E_T$  is often successfully used, for low fiber content, to approximate the stiffness of the composite with randomly oriented fibers. However, using this equation for composites with large differences between  $E_L$  and  $E_T$ , the stiffness can be overestimated by 50%.



In the Vicat temperature test, a needle loaded with weights is pushed against a plastic specimen inside a glycol bath. This is shown schematically in Fig. 9.62. The uniformly heated glycol bath rises in temperature during the test. The Vicat number or Vicat temperature is measured when the needle has penetrated the polymer by 1 mm. The advantage of this test method is that the test results are not influenced by the part geometry or manufacturing technique. The practical limit for thermoplastics, such that the finished part does not deform under its own weight, lies around 15 K below the Vicat temperature.

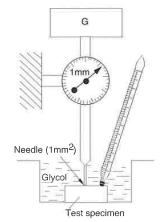


Figure 9.62 Apparatus to determine a material's shape stability under heat [BASF] using the Vicat temperature test.

To determine the heat distortion temperature, the standard specimen lies in a fluid bath on two knife edges separated by a 10 cm distance. A bending force is applied on the center of the specimen. Similar to the Vicat temperature test, the bath's temperature is increased during the test. The HDT is the temperature at which the rod has bent 0.2 mm to 0.3 mm (see Fig. 9.63). The Vicat temperature is relatively independent of the shape and type of part, whereas the heat-distortion-data are influenced by the shaping and pretreatment of the test sample. Table 9.4 shows the heat distortion temperature for selected thermoplastics measured using ASTM D648.

In the Martens temperature test, the temperature at which a cantilevered beam has bent 6 mm is recorded. The test sample is placed in a convection oven with a constantly rising temperature. In Europe, the HDT test has replaced the Martens temperature test.

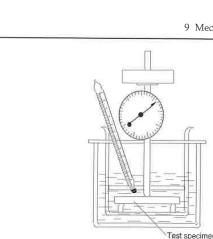


Figure 9.63 Apparatus to determine a material's shape stability under heat using the heat-distortion-temperature test (HDT).

It is important to point out that these test methods do not give enough information to determine the allowable operating temperature of molded plastic components subjected to a stress. Heat distortion data is excellent when comparing the performance of different materials and should only be used as a reference not as a direct design criterion.

Material	HDT ( <sup>o</sup> C) 1.86 MPa	0.45 MPa
HDPE	50	50
PP	45	120
uPVC	60	82
PMMA	60	100
PA66	105	200
PC	130	145

#### Examples

component.

9 Mechanical Behavior of Polymers 431

 Table 9.4
 Heat Distorsion Temperature for Selected Thermoplastics

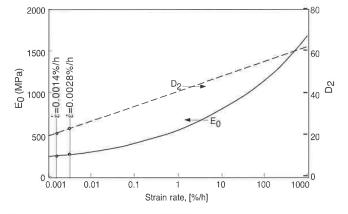
9.1 A loaded high-density polyethylene component is not to exceed 4% strain after 60 days of loading at room temperature. Using the short term data presented in Fig. 9.64 estimate the maximum allowable stress within the

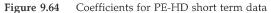


Figure 9.64 presents constants  $E_0$  and  $D_2$  as a function of rate of the deformation  $\dot{\epsilon}$ . The time given in this design is 60 days (1440 h) and the strain is 4%. Therefore the average rate of deformation is 4%/1440h = 0.0028%/h. At that rate, we read  $E_0 = 250MPa$  and  $D_2 = 28$ . We can now use Eq. 9.25 to compute the allowable stress

$$\sigma = \frac{E_0 \varepsilon}{1 + D_2 \varepsilon} = \frac{250 \text{MPa}(0.04)}{1 + 28(0.04)} = 4.72 \text{MPa}$$

It should be noted that the prescribed strain of 4% is quite high. As a rule of thumb, a component that is subjected to a long term load should not have strains larger than 2%, to avoid creep rupture. Hence, if we reduce our allowable strain to 2%, the rate of deformation during the 60 days should be  $\dot{\varepsilon} = 2\% / 1440h = 0.0014\% / h$ . At the new rate we read  $E_0 = 245$ MPa and  $D_2 = 26$  from Fig. 9.64. Using the new constants, the maximum allowable stress for a 2% strain in 60 days is 3.22 MPa.





9.2 In a special laboratory experiment, a PMMA pipe is used to cap a tank that is pressurized at 2 MPa, as shown in Fig. 9.65. The 3 mm thick pipe has a 50 mm internal diameter and is 300 mm long. Estimate the diameter change of the pipe after one year of testing? Use the creep data given below [34].

To solve this problem we can use the thin pressure vessel approximation, working with an average diameter,  $\overline{D} = 53$  mm. This is a  $\sigma_{\rm A}$ , defined by

 $\sigma_H = \frac{p}{\sigma}$ 

where, p is the pressure and h is the thickness. These stresses are constant and will cause the pipe to creep. Using the PMMA creep data we can generate a 1 year isochronous curve, which is presented in Fig.9.67. The strains that correspond to stresses of 17.67 MPa and 8.83 MPa are  $\varepsilon_{H} = 1.32\%$  and  $\varepsilon_{A} = 0.6\%$ , respectively. Since this is a biaxial case we must correct the hoop strain using Poisson's effect, before computing the diameter change. For this we use

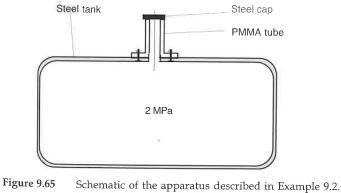
value of 1/3. Thus,



To compute the diameter change we use

Hence,

 $\Delta D = (53 \text{ mm})(0.0112) = 0.594 \text{ mm}$ 



#### 9 Mechanical Behavior of Polymers 433

case of biaxial stress, composed of a hoop stress,  $\sigma_{\mu}$ , and an axial stress,

$$\frac{\overline{D}}{2h} = 17.67 \text{ MPa} \text{ and } \sigma_A = \frac{p\overline{D}}{4h} = 8.83 \text{ MPa}$$

$$\varepsilon'_{H} = \varepsilon_{H} - v\varepsilon_{A}$$

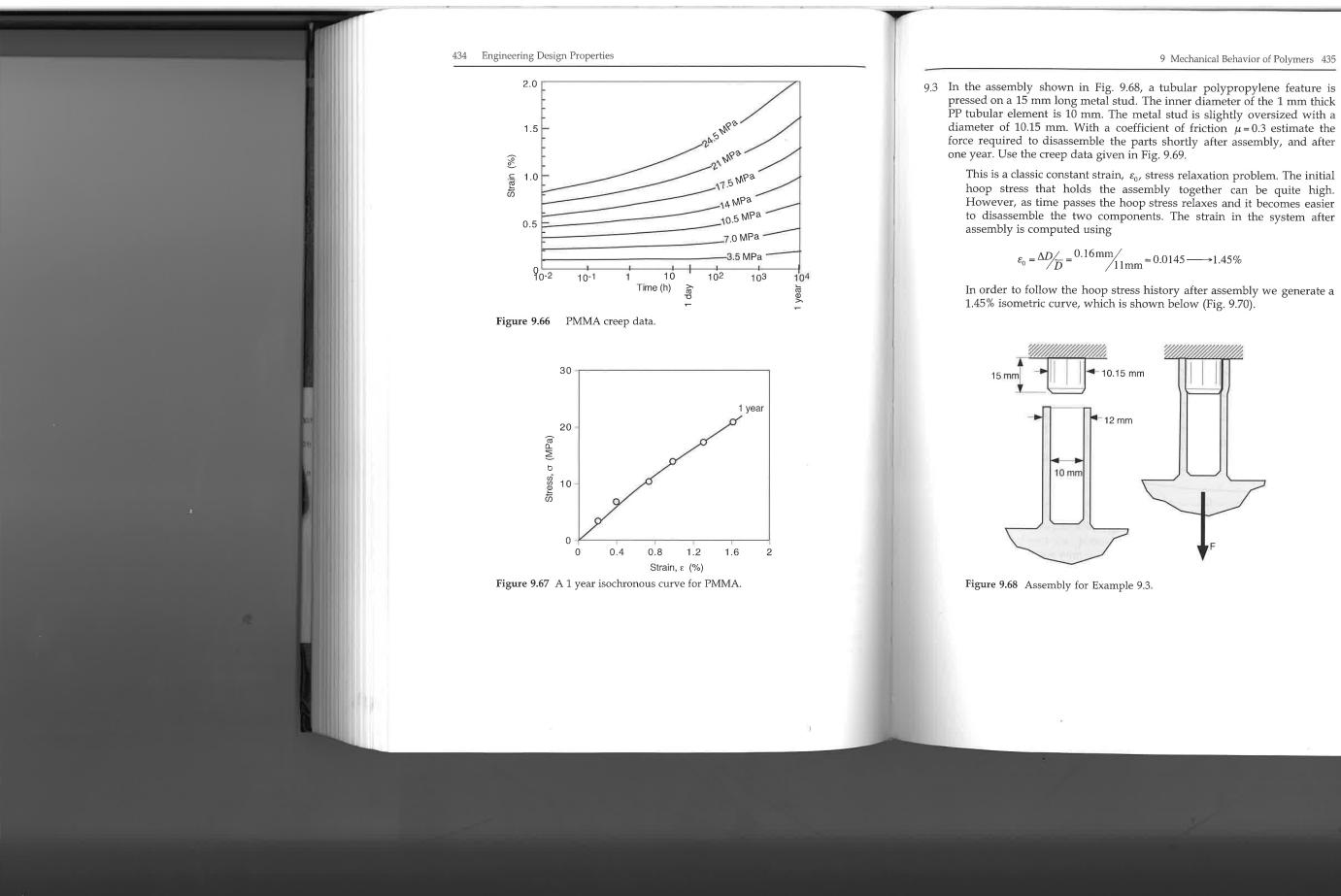
However, since we were not given Poisson's ration, v, we assume a

$$f_{H} = 1.32 - (\frac{1}{3})0.6 = 1.12\%$$

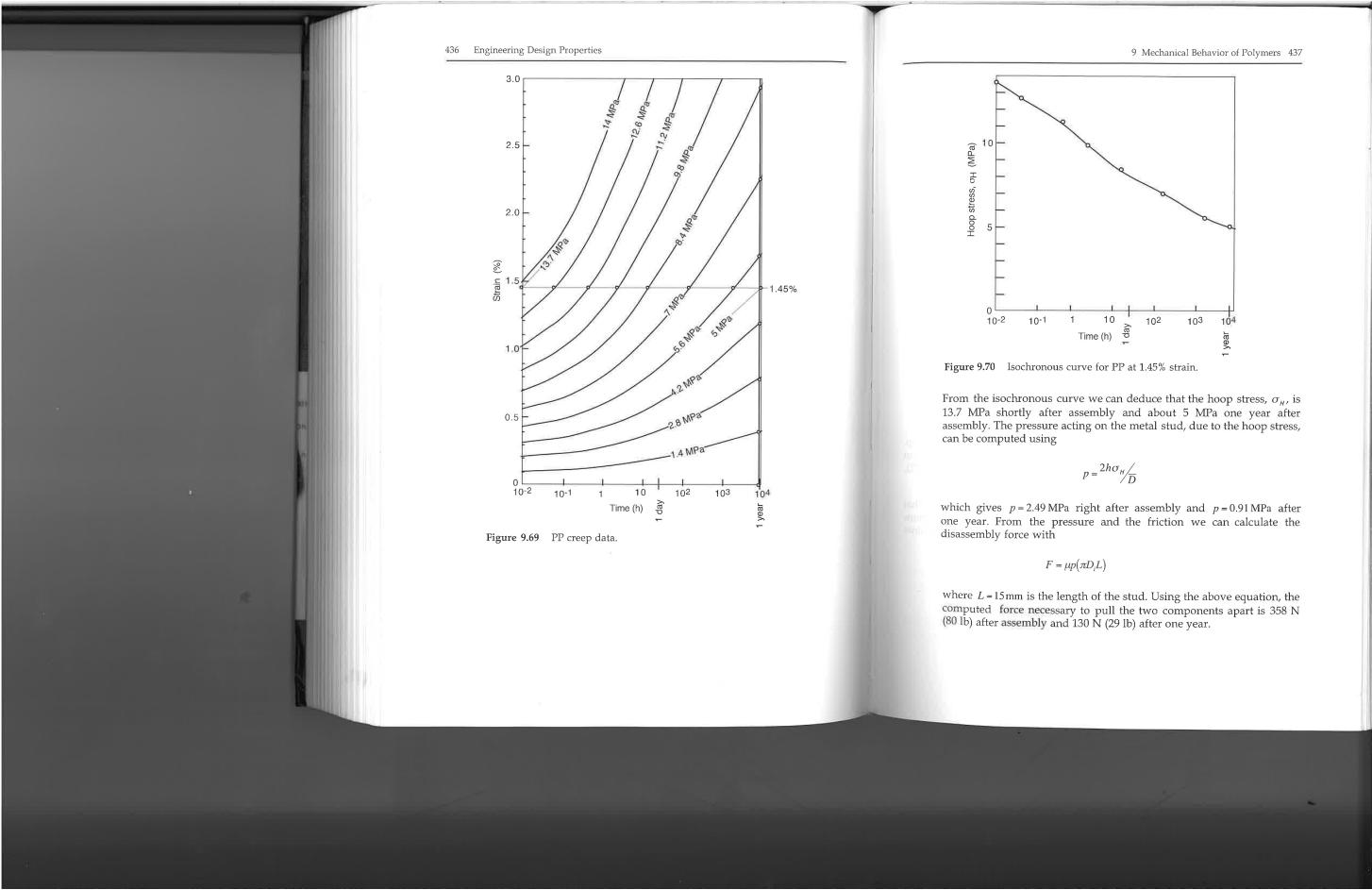
$$\varepsilon'_{H} = \Delta D / D$$



MacNeil Exhibit 2117 Yita v. MacNeil IP, IPR2020-01139 Page 227

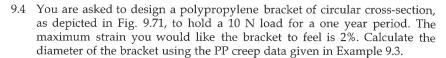


9 Mechanical Behavior of Polymers 435



$$p = \frac{2h\sigma_H}{D}$$

MacNeil Exhibit 2117 Yita v. MacNeil IP, IPR2020-01139 Page 229



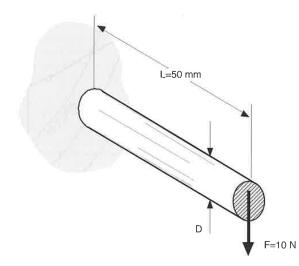
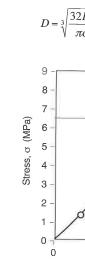


Figure 9.71 Cantilevered bracket of circular cross-section.

In this design, the instant the bracket is loaded it will begin to creep. Since the life of the system is designed to be one year, with a maximum strain of 2%, we will work with a 1 year isochronous curve(Fig.9.72), generated using Fig.9.69.

From the isochronous curve we find that 6.5 MPa is the stress that corresponds to a 2% strain. In a cantilevered beam the maximum stresses occur in the upper (tensile) and lower (compressive) points where the bracket joins the wall. For a cantilevered system we use

$$\sigma = \frac{Mc}{I} \text{, where } \begin{cases} c = D/2\\ M = FL\\ I = \frac{\pi D^4}{64} \end{cases}$$



At this point it is important to mention that this design has many flaws. First a solid cross-section such as this will result in a long cycle time during manufacturing due to the slow cooling. In addition, thick crosssections result in large amounts of shrinkage, especially with a semicrystalline material such as polypropylene. Finally, the bending strength of a solid circular cross-section is only a fraction (lower than 20%) of the bending strength that an I-beam could deliver. This means that by changing the cross-sectional geometry of the beam, we would only need 20% or less of the material required for the present design.

9 Mechanical Behavior of Polymers 439

Hence, we can solve for *D* using

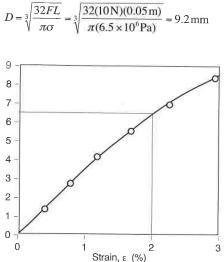


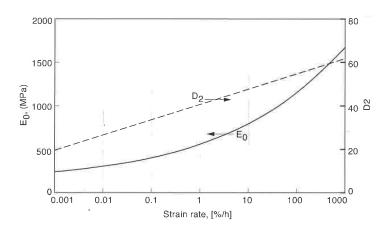
Figure 9.72 A 1 year isochronous curve for PP.



MacNeil Exhibit 2117 Yita v. MacNeil IP, IPR2020-01139 Page 230

#### Problems

9.1 Using the coefficients  $E_0$  and  $D_2$  for the high-density polyethylene presented in Fig. 9.73 compute the stress for 0%, 2%, 4%, and 6% strain and reconstruct the stress-strain curve for a specimen tested at 23 °C with a 100%/h deformation rate.



**Figure 9.73** Coefficients  $E_0$  and  $D_2$  for a high density polyethylene at 23 °C.

- 9.2 For the above material calculate the 1% strain secant modulus for 6 min, 1 h, 10 h, and 100 h. Plot the data and comment on your results.
- 9.3 Using the time-temperature superposition principle described below, plot the stress-strain curve of Problem 9.1 for T = 40 °C.

$$\operatorname{Log}(\dot{\varepsilon}_{ref} / \dot{\varepsilon}) = k(1 / T - 1 / T_{ref}), \quad \text{with} \quad k = 10400 \,\mathrm{K}$$

- 9.4 Generate a 2 year isochronous curve for the polypropylene curve presented in Fig. 9.21. Using this curve estimate the thickness of a 50 mm diameter polypropylene pipe whose maximum allowable strain in a 2 year period should be 2%, while subjected to a 200 kPa internal pressure. Note: neglect effect of biaxial state of stress.
- After a continuos 1 year operation, what is the diameter change of a cast 9.5 acrylic tube which is part of a fluids experimental set-up that transports

- Tube inside diameter = 50 mm, • Tube thickness = 3 mm,
- Tube length = 300 mm.

Use the 20 °C creep curves given below.

- 9.6
- 9.7
- 9.8

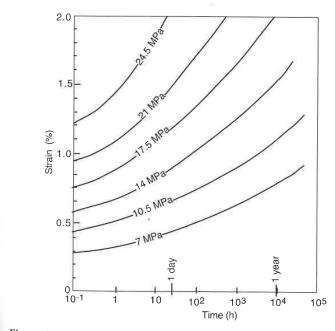


Figure 9.74 Creep data for polyacetal.

9 Mechanical Behavior of Polymers 441

air at a pressure of 10 bar. Use the following

You are to re-design the 50 mm long solid polypropylene circular bracket described in Example 9.4 using a hollow circular cross-section with a 2 mm thickness. How much material are you saving?

A cast iron pump housing has a polypropylene cover. The cover is tightened with steel bolts causing a compressive strain of 1.5% on the edge of the plate. When will the pump start leaking if it generates internal pressures of up to 4 MPa. Use the creep data given in Fig. 9.20.

Rework Example 9.3 using polyacetal data given in Fig. 9.74.

MacNeil Exhibit 2117 Yita v. MacNeil IP, IPR2020-01139 Page 231

Two metal pipes are to be connected using a polypropylene fitting as 9.9 shown in Fig. 9.75. The tubes are inserted onto the fitting causing a 1% hoop strain.

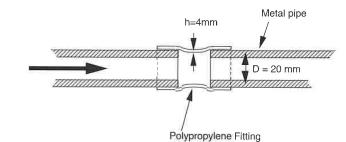


Figure 9.75 Polypropylene snap-fit assembly.

Using the creep curves given in Fig. 9.69, estimate the initial hoop stress in the polypropylene fitting.

The pressure of the water inside the tubes is 5 MPa. Estimate how long will this design be water-proof?

What initial hoop strain do you recommend to make the design water proof for 1 year?

Draw a 1 day isochronous stress-strain curve.

- 9.10 Derive the equation given for Young's modulus, E<sub>random</sub>, for a plate with randomly oriented fibers. Assume that the fiber length is much larger than the thickness of the plate.
- 9.11 Similar to the Halpin-Tsai model, the mixing rule is another common technique to compute the properties of a unidirectional fiber reinforced composite part. The mixing rule for the longitudinal modulus is written as

$$E_L = \phi E_f + (1 - \phi) E_m$$

Plot  $E_{\rm L}$  as a function of  $\phi$  for  $E_f/E_m = 2,10$  and 20.

- be loaded in torsion.
- your components. Why?
- [20].

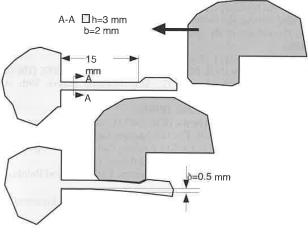


Figure 9.76 Polyacetal snap-fit assembly.

9 Mechanical Behavior of Polymers 443

9.12 You are to design two long fiber reinforced cylindrical structural components. Component A is to be loaded axially. Component B is to

• What is the ideal orientation of the fibers for each component? • If you were to choose between pultrusion, filament winding, and injection molding, which process would you choose to manufacture

9.13 You are asked to design a polyacetal snap-fit as depicted in Fig. 9.76. Find the maximum force between the two components shortly after assembly, and after one year. Use the creep data presented in Fig. 9.74

9.14 In a certain design, in which creep plays a significant role, you need to decide between a polyacetal and a polypropylene component. Your maximum allowable strain is 2% after one year. Which one would you choose if cost plays a major role in your design decision. To help you solve this problem, use the creep data presented in Figs. 9.76 and 9.69, for POM and PP, respectively, and the cost data presented in Chapter 1.



9.15 In Problem 9.13, how would your decision be if weight played a higher role than cost?

#### References

- 1. Domininghaus, H., Plastics for Engineers, Hanser Publishers, Munich, (1993).
- 2. Treloar, L.R.G., The Physics of Rubber Elasticity, 3rd. Ed., Clarendon Press, Oxford, (1975).
- 3. Courtesy ICIPC, Medellín, Colombia.
- 4. Ward, I.M., and Hadley, D.W., An Introduction to Mechanical Properties of Solid Polymers, John Wiley & Sons, Chichester, (1993).
- 5. Mooney, M., J. Appl. Phys., 11, 582, (1940).
- 6. Rivlin, R.S., and Saunders, D.W., Phil. Trans. Roy. Soc., A243, 251, (1951).
- Gumbrell, S.M., Mullins, L., and Rivlin, R.S., Trans. Faraday Soc., 49, 1495, (1953). 7.
- 8. Guth, E., and Simha, R., Kolloid-Zeitschrift, 74, 266, (1936).
- 9. Guth, E., Proceedings of the American Physical Society, (1937): Physical Review, 53, 321, (1938).
- 10. Smallwood, H.M., J. Appl. Phys., 15, 758, (1944).
- 11. Mullins, L., and Tobin, N.R. N.R., J. Appl. Polym. Sci., 9, 2993, (1965).
- 12. Knausenberger, R., and Menges, G., SPE Technical Papers, 39th ANTEC, 240, (1981).
- 13. Retting, W., Rhelogica Acta, 8, 258, (1969).
- 14. Schmachtenberg, E., Ph.D. Thesis, IKV, RWTH-Aachen, Germany, (1985).
- 15. Krämer, S., Ph.D. Thesis, IKV, RWTH-Aachen, Germany, (1987).
- 16. Weng, M., Ph.D. Thesis, IKV, RWTH-Aachen, Germany, (1988).
- 17. ASTM, Plastics (II), 08.02, ASTM, Philadelphia, (1994).
- Nielsen, L.E., Mechanical Properties of Polymers, Van Nostrand Reinhold, New York, 18. (1962).
- 19. Menges, G., (after Retting, W. and Lörtsch), Werkstoffkunde Kunststoffe, 3<sup>rd</sup>. Ed., Hanser Publishers, Munich, (1989),
- Crawford, R.J., Plastics Engineering, 2nd ed., 47, Pergamon Press, Oxford, (1987). 20.
- 21. O'Toole, J.L., Modern Plastics Encyclopedia, McGraw Hill, New York, (1983).
- Thimm, Th., Plastomere, Elastomere, Duromere, Kautschuk und Gummi, 14, 8, 233, 22. (1961).
- 23. Henning, F., Kunststoffe, 65, 401, (1975).
- 24. Hosemann, R., Kristall und Technik, 11, 1139, (1976).
- 25. Zachariades, A.E., and Kanamoto, T., High Modulus Polymers, A.E. Zachariades, and R.S. Porter, Eds., Marcel Dekker, Inc., New York, (1988).
- Becker, H., Diploma Thesis, IKV, RWTH-Aachen, Germany, (1986). 26.
- Wende, A., Glasfaserverstärkte Plaste, VEB Deutscher Verlag für die Grundstoff-27. Industrie, Leipzig, (1969).
- Nielsen, L.E., and Landel, R.F., Mechanical Properties of Polymers and Composites, 28. 2nd Ed., Marcel Dekker, Inc., New York, (1994).

- New York, (1993).
- Technomic Publishing Co., Stamford, (1968).
- 31. 32.
- 33.
- Verlag Stuttgart, (1984).

9 Mechanical Behavior of Polymers 445

29. Krishnamachari, S.I., Applied Stress Analysis of Plastics, Van Nostrand Reinhold,

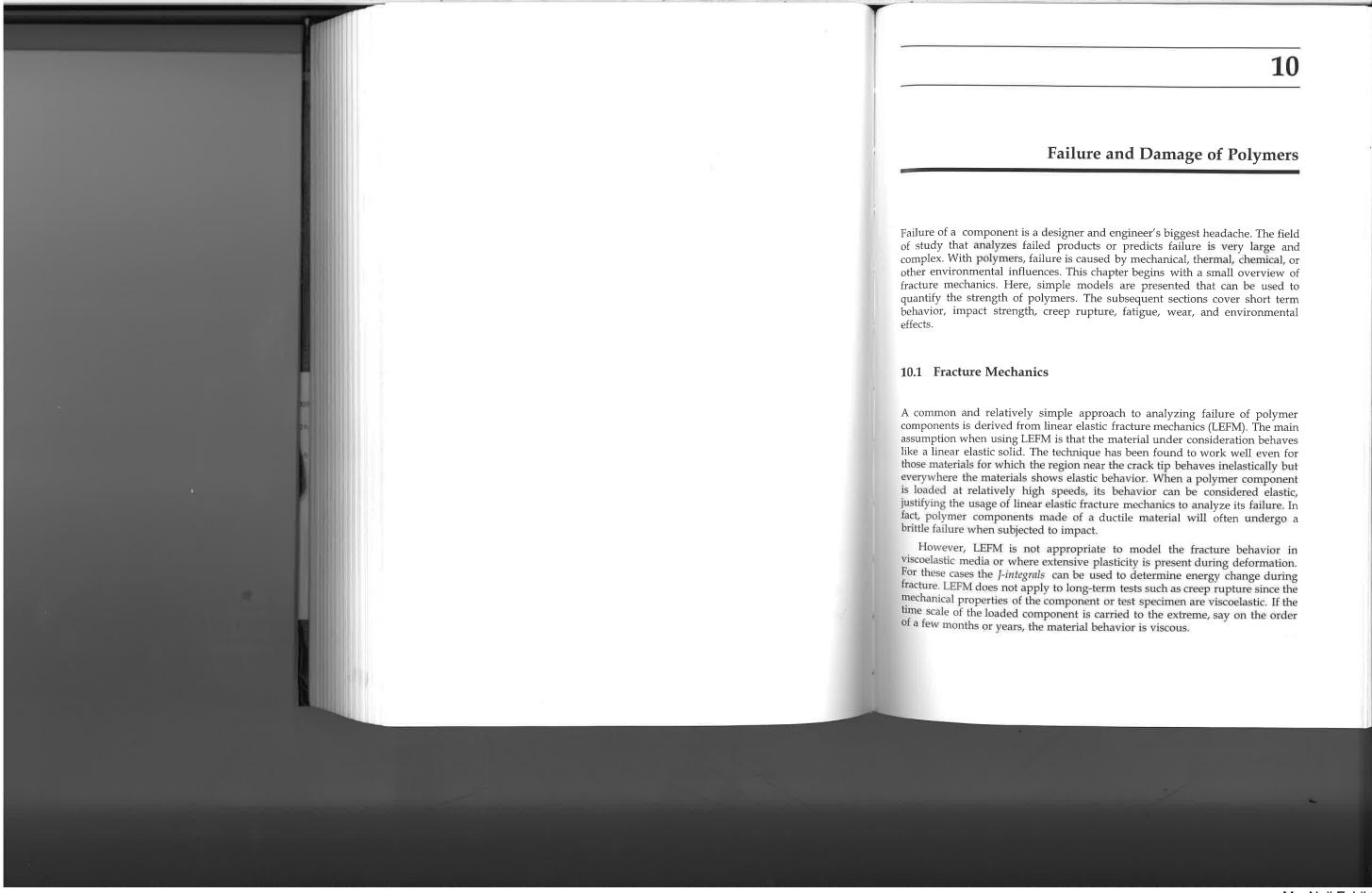
30. Tsai, S.W., Halpin, J.C., and Pagano, N.J., Composite Materials Workshop,

Brintrup, H., Ph.D. Thesis, IKV, RWTH-Aachen, Germany (1974).

Ehrenstein, G.W., Faserverbundkunststoffe, Hanser Verlag, München, (1992).

Menges, G., and Bintrup, H., Chapter 4 in Polymere Wrkstoffe, Georg Thieme

34. Powell, P.C., "Engineering with Polymers," Chapman and Hall, London, (1983).



The next sections will discuss linear elastic as well as linear viscoelastic fracture mechanics, applying them to quantitatively analyze strength properties of cracked polymer components or parts with sharp notches or stress concentrators.

### **10.1.1** Fracture Predictions Based on the Stress Intensity Factor

From the basic three crack growth modes of failure, shown in Fig. 10.1, mode I most resembles an internal crack growing under a tensile load. For the analysis, consider the cracked body displayed in Fig. 10.2 with a crack length of 2a and an applied stress  $\sigma$ . Near but not at the crack tip, the stress in the direction of loading can be approximated by

$$\sigma_{y} = \frac{K_{Ic}}{\sqrt{2\pi r}} \tag{10.1}$$

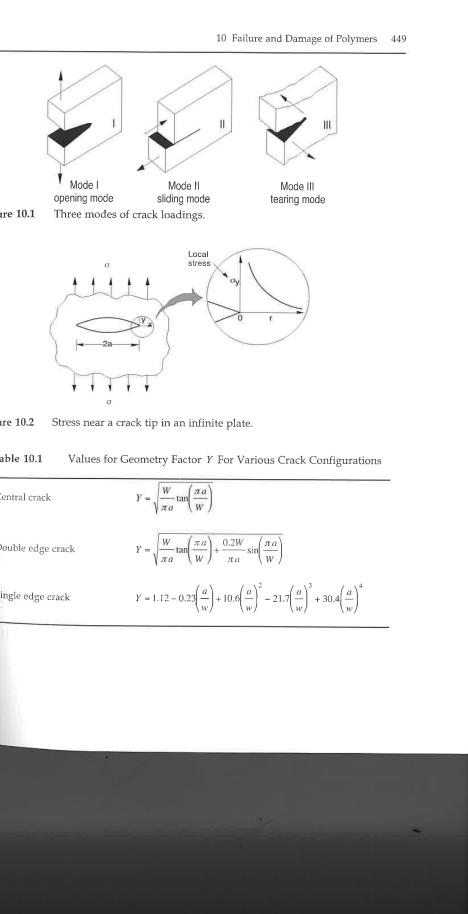
where r is the distance from the crack tip and  $K_{tc}$  is the critical stress intensity *factor* needed for mode *I* crack growth and failure, defined by

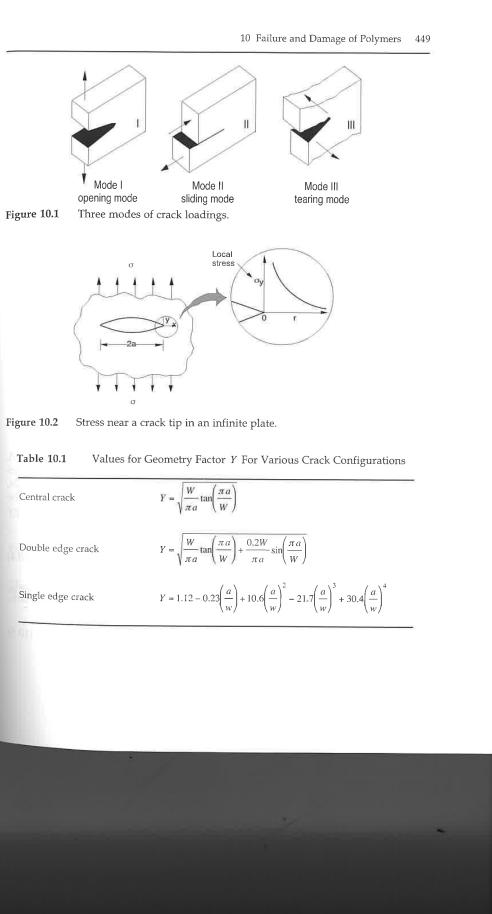
$$X_{lc} = \sigma \sqrt{\pi a} \tag{10.2}$$

This stress intensity factor depends on crack size relative to component size, crack shape, boundary conditions, etc. Hence, a more general form of Eq. 10.2 is given by

$$K_{lc} = Y\sigma\sqrt{\pi a} \tag{10.3}$$

where Y is a dimensionless correction factor tabulated for various geometries in Table 10.1. In a linear elastic solid, fracture occurs instantaneously at a combination of stress and crack size that results in a critical stress intensity factor,  $K_{lc}$ . The critical stress intensity factor is a material property that depends on the temperature, grade of polymer, orientation, etc., where a large value implies a tough material. Table 10.2 [1, 2] shows stress intensity factors, also called *fracture toughness*, for common polymers.





MacNeil Exhibit 2117 Yita v. MacNeil IP, IPR2020-01139 Page 235

various materia	various materials		
Material	KIc(MN/m <sup>3/2</sup> )	$G_{Ic}(kJ/m^2)$	
ABS	2-4	5	
Acetal	4	1.2-2	
Ероху	0.3-0.5	0.1-0.3	
LDPE	1	6.5	
MDPE-HDPE	0.5-5	3.5-6.5	
Polyamide 66	3	0.25-4	
Polycarbonate	1-2.6	5	
Polyester-glass reinforced	5-7	5-7	
Polypropylene copolymer	3-4.5	8	
Polystyrene	0.7-1.1	0.3-0.8	
PMMA	1.1	1.3	
uPVC	1-4	1.3-1.4	
Aluminum-alloy	37	20	
Glass	0.75	0.01-0.02	
Steel-mild	50	12	
Steel-alloy	150	107	
Wood	0.5	0.12	

#### Table 10.2 Values of Plane Stress Intensity Factor and Strain Toughness for Various Materials

### 10.1.2 Fracture Predictions Based on an Energy Balance

To analyze a mode I crack growth case using an energy balance and LEFM, consider the cracked body used in the previous analysis, where the actual forces are used instead of stresses, as displayed in Fig. 10.3. The crack width is also 2a, and the body is subjected to a load F. The load-displacement behavior of the cracked body is described by the solid line in Fig. 10.4. The elastic energy stored in the loaded component is given by the area under the curve:

$$U_c = \frac{1}{2}FX \tag{10.4}$$

As the crack grows by an amount  $\Delta a$ , the stiffness of the component decreases as shown by the dashed line in Fig. 10.4, and the elastic energy changes to

$$U_c' = \frac{1}{2} \left( F + \Delta F \right) \left( X + \Delta X \right) \tag{10.5}$$

described by

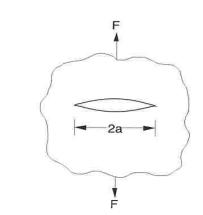


Figure 10.3 Load applied on a cracked specimen.

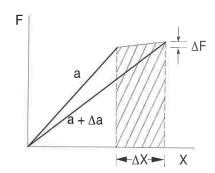


Figure 10.4 Linear elastic behavior of a cracked specimen.

The external work done as the crack grows the distance  $\Delta a$  is defined by the shaded area in Fig. 10.4 and can be written as

 $\Delta U_c$ 

### 10 Failure and Damage of Polymers 451

The change in stored elastic energy for the body with the growing crack is

 $\Delta U = U_c - U'_c$ (10.6)

$$= \left(F + \frac{\Delta F}{2}\right) \Delta X \tag{10.7}$$



MacNeil Exhibit 2117 Yita v. MacNeil IP, IPR2020-01139 Page 236

By subtracting Eq. 10.6 from Eq. 10.7 we can compute the energy required to generate new surfaces during fracture:

$$\Delta U_c - \Delta U = \frac{1}{2} (F \Delta X - X \Delta F)$$
(10.8)

Griffith's hypothesis [3], commonly used as a fracture criterion, states that for a crack to increase in size, the rate of stored elastic energy decrease must be larger or equal to the rate at which surface energy is created during crack growth. Griffith's hypothesis can be related to the expression in Eqs. 10.6 and 10.7 as

$$\frac{\partial (U_c - U)}{\partial a} \ge G_{l_c} \tag{10.9}$$

where  $G_{lc}$  defines the energy required to increase a crack by a unit length in a component of unit width and is usually referred to as the elastic energy release rate, the toughness or the critical energy release rate. Equations 10.6, 10.7, and 10.9 can be combined to give

$$G_{lc} = \frac{1}{2} \left( F \frac{\partial x}{\partial a} - X \frac{\partial F}{\partial a} \right)$$
(10.10)

Making use of the compliance defined by

$$J = \frac{X}{F} \tag{10.11}$$

and defining the force at the onset of crack propagation by  $F_{c'}$  we can rewrite Eq. 10.10 as

$$S_{Ic} = \frac{F_c^2}{2t} \frac{\partial J}{\partial a} \tag{10.12}$$

This equation describes the fundamental material property,  $G_{ic}$ , as a function of applied force at fracture and the rate at which compliance changes with respect to crack size. Equation 10.12 is more useful if it is written in terms of stress as

$$G_{lc} = \frac{\pi G_c^2 a}{E} \tag{10.13}$$

This equation only applies for plane stress and must be redefined for the plane strain case as

 $G_{lc}$ 

Table 10.2 also displays typical values of toughness for common materials.

for the plane stress case and

 $G_{k}$ 

for the plane strain case.

# 10.1.3 Linear Viscoelastic Fracture Predictions Based on J-Integrals

Because of the presence of viscous components and the relatively large cracktip plastic zone during deformation, the elastic energy release rate,  $G_{le'}$  is not an appropriate measure of the energy release or toughness during fracture of many thermoplastic polymers. The J-integral concept was developed by Rice [4] to describe the strain energy transfer into the crack tip region and, using the notation in Fig. 10.5, is defined by

$$J_{ic} =$$

specimen of thickness *t* can be computed by

which gives

10 Failure and Damage of Polymers 453

$$a = \frac{\pi \sigma_c^2 a}{E} \left( 1 - \nu^2 \right)$$
 (10.14)

By substituting Eq. 10.3 into Eqs. 10.13 and 10.14, we can relate the stress intensity factor  $K_{lc}$  and the toughness  $G_{lc}$  with

$$G_{lc} = \frac{K_{lc}^*}{Y^2 E}$$
(10.15)

$$L = \frac{K_{lc}^2}{Y^2 E} \left(1 - \nu^2\right) \tag{10.16}$$

$$\int W dy - \int_{\Gamma} \underline{\mathbf{T}} \frac{\partial \underline{\mathbf{u}}}{\partial \mathbf{x}} ds \tag{10.17}$$

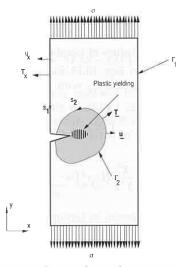
where W represents the strain energy density,  $\underline{\mathbf{T}}$  the traction vector, and  $\underline{\mathbf{u}}$  the displacement vector. As with  $G_{lc}$ ,  $J_{lc}$  is a measure of the energy release rate, thus, analogous to Fig. 10.4. We can consider Fig. 10.6 to determine the energy release in a viscoelastic material with a growing crack. Again, the shaded area in the curve represents the energy release rate which, apart from second order effects, is the same for constant load and constant deformation and for a

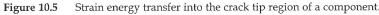
$$\Delta U = J_{lc} t \Delta a \tag{10.18}$$

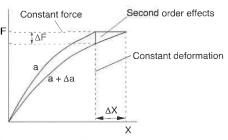
$$T_{lc} = -\frac{1}{t} \left( \frac{\partial U}{\partial a} \right)$$

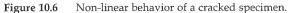
MacNeil Exhibit 2117 Yita v. MacNeil IP, IPR2020-01139 Page 237

(10.19)









At fracture,  $J_{ic}$  can be related to the crack opening displacement,  $\delta$ , and the yield stress,  $\sigma_{\rm v}$ , by

$$J_{lc} = \sigma_y \delta \tag{10.20}$$

One important feature of the J-integral as defined in Eq. 10.17 is that it is path independent, so any convenient path can be chosen where stresses and displacements are known. A good choice for a path is one that completely encloses the crack tip with the plastic region but which lies within the elastic region of the body. Another property of the J-integral is that for linear elastic cases,  $J_{lc} = G_{lc}$ .

# 10.2 Short-Term Tensile Strength

As discussed in the previous chapter, short-term tensile tests DIN 53457 and ASTM D638 are available to test the stress-strain behavior of polymeric materials at room temperature  $(23 \text{ }^{\circ}\text{C})^1$ . The resulting data is plotted in a stressstrain curve that reflects the type of material and the mode of failure associated with the test polymer. When regarding polymeric materials from the failure mode point of view, there are two general types of fracture: brittle and ductile. However, depending on the temperature, environment, and whether a component is notched or not, a material can fail either way. Figure 10.7 shows a diagram developed by Vincent [5] which helps the engineer to distinguish between the different modes of failure of various thermoplastics. The figure represents a plot of brittle stress at about -180 °C ( $\sigma_{\scriptscriptstyle B}$ ) versus yield stress at -20 °C (A) and 20 °C (O). The data points to the right of line A represent polymers that are brittle unnotched. The points that are between lines A and B are those polymers that are ductile unnotched but brittle notched, and those to the left of line B represent polymers that are ductile even when notched.

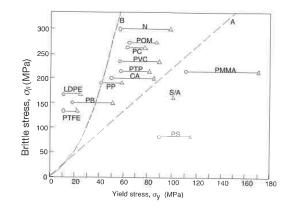


Figure 10.7 Brittle stress at -180  $^{\circ}$ C versus yield stress at -20  $^{\circ}$ C ( $\Delta$ ) and 20  $^{\circ}$ C (o) for various polymers.

10 Failure and Damage of Polymers 455

1 We believe that it is imperative that the rate of deformation within the tensile specimen be maintained constant. In Chapter 9 we presented the Knausenberger-Menges technique that maintains this condition

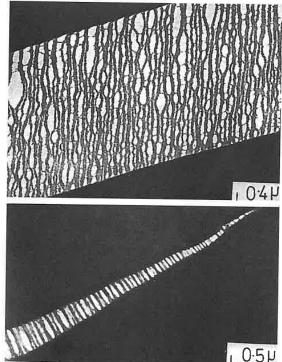


using optical techniques.

#### 10.2.1 Brittle Failure

Brittle failure usually occurs with thermoplastics below their glass transition temperature, T<sub>e</sub>, and with highly cross-linked polymers. However, as discussed later in this chapter, brittle failure also occurs in creep rupture and fatigue tests performed at temperatures above the glass transition temperature of the polymer. Typically, it occurs at very small strains - perhaps 1% or less - and it is generally associated with amorphous thermoplastics below their glass transition temperature. Figure 10.8 shows the stress-strain curve for the injection molded polystyrene ASTM D638M type I test specimen shown in Fig. 10.9. The stress strain curve has a constant slope until the point where small microcracks form just before failure. These small microcracks form in the plane perpendicular to the maximum principal stress and are nucleated at points of high stress concentrations such as scratches, dust particles in the material and material inhomogeneities. These cracks, which are more commonly known ascrazes, impair clarity and reflect light, which makes them particularly obvious in transparent materials.

Figure 10.10 [6] shows electron micrographs of the center and edge of a craze in a polystyrene specimen. As can be seen in the micrograph, the craze boundaries are connected with load bearing fibrils which make them less dangerous than actual cracks. Crazing is directly related to the speed at which the component or test specimen is being deformed. At high deformation speeds, the crazes are small and form shortly before failure, which makes them difficult to detect. At slow rates of deformation, crazes tend to be large and occur early on during loading. A typical craze is about 0.5  $\mu m$  wide at the center and 200 µm long.<sup>2</sup> However, the length and width of a craze is materialdependent.



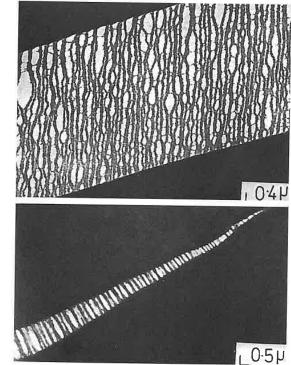


Figure 10.10

specimen.

2 The length of a craze will vary between 10  $\mu m$  and 1000  $\mu m.$ 

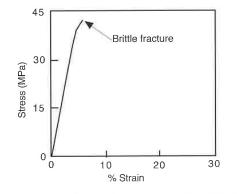
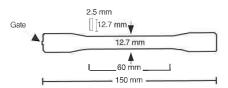
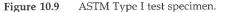


Figure 10.8 Stress-strain curve for a polystyrene at room temperature.





10 Failure and Damage of Polymers 457

Electron micrographs of the center and edge of a craze in a polystyrene

Figure 10.11 [7] shows the relation between stress, strain, craze size formation and failure. By extrapolating the craze formation line, one can see that at high stress crazes form at the same time as failure. When crazes form under static loading, they do not pose immediate danger to the polymer component. However, crazes are irreversible, and they imply a permanent damage within the material. It should also be noted that once crazes and microcracks have formed, the material no longer obeys the laws of linear viscoelasticity. The limit strain at which microcracks will form is sometimes depicted by EFX. Complex models exist, beyond the scope of this book, which relate the critical strain to the surface energy within a craze [8].

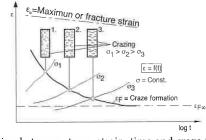


Figure 10.11 Relation between stress, strain, time and craze formation.

Figure 10.12 [7] shows the relationship between strain, time, and damage for PMMA. The bottom of the figure shows the time-temperature superposition. For example, the damage that occurs at 10 hours for 23 °C will occur at 105 hours for a component at 60 °C. It is interesting to see how the critical strain,  $\epsilon_{F^{\times}}$ , is delayed as the temperature of the polymer component rises.

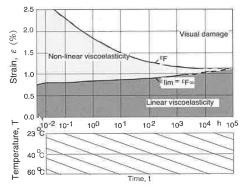
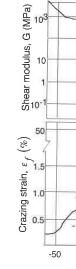


Figure 10.12 Strain limits for linear viscoelasticity.

Figure 10.13 [7] shows a plot of critical strain versus temperature for an impact resistant polystyrene and compares the damage behavior curve to the shear modulus. The two curves are almost a mirror images of each other and demonstrate that the formation of microcracks is inversely proportional to the stiffness of the material. The figure also demonstrates the influence of orientation on the onset of microcracks. As expected, in a component loaded perpendicular to the orientation, or across the polymer chains, the microcracks form earlier than in one loaded parallel to the orientation direction.



high impact polystyrene.

#### 10.2.2 Ductile Failure

A ductile failure takes place with semi-crystalline thermoplastics at temperatures between the glass transition temperature,  $T_{e}$ , and the melting temperature,  $T_m$ . A ductile failure is a succession of several events, as is clearly shown in the stress-strain diagram for polypropylene, shown in Fig. 10.14 and explained in the following paragraphs.

At first, the semi-crystalline polymer behaves like an elastic solid whose deformation is reversible. For the polypropylene sample test results shown in Fig. 10.14, this linear elastic behavior holds for deformations of up to 0.5%. This

### 10 Failure and Damage of Polymers 459

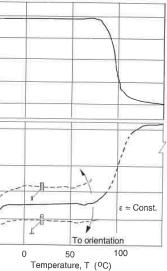


Figure 10.13 Shear modulus and crazing strain as a function of temperature for a



MacNeil Exhibit 2117 Yita v. MacNeil IP, IPR2020-01139 Page 240

behavior takes place when the component's load is applied and released fairly quickly, without causing a permanent damage to the material and allowing the component to return to its original shape. This is graphically depicted in Fig. 10.15 [7].

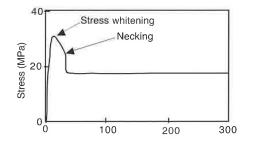


Figure 10.14 Stress-strain curve for a polypropylene at room temperature.

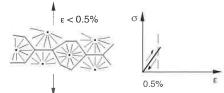


Figure 10.15 Elastic deformation within a spherulitic structure.

If the load is increased or the process is slowed, the stress-strain curve becomes non-linear, reflected by the reduction of rate of stress increase. At this point, microcracks form in the interface between neighboring spherulites, as shown in the photograph of Fig. 10.16 [9] and schematically in Fig. 10.17 [7].



propylene).

Figure 10.16

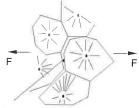
Split spherulite Figure 10.17 Schematic of crack formation at inter-spherulitic boundaries.

The formation of such microcracks, also called *stress whitening*, is an irreversible process, causing a permanent deformation in the polymer component. Other than the white coloration that makes itself noticeable in the stressed component, the cracks are not visible to the naked eye. These microcracks are fairly constant in length, about the size of the spherulites. Their formation and growth, and their relation to the stress-strain behavior of a semi-crystalline polymer, are depicted in Fig. 10.18 [7].

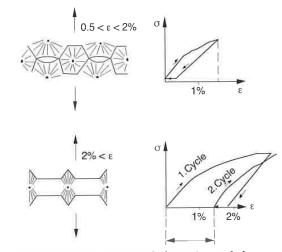
10 Failure and Damage of Polymers 461



Micrograph of crack formation at inter-spherulitic boundaries (poly-







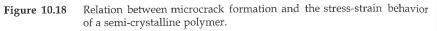
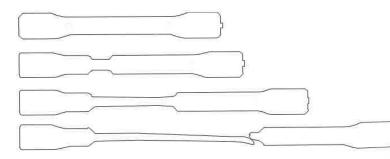


Figure 10.14 shows that by further deforming the specimen, the stress-strain curve reaches a maxima called the yield point or yield strength. Beyond the yield point the stress drops, an event that is followed by necking, a localized reduction in cross-sectional area. Once necking has occurred, the specimen or component continues a long cold drawing process where the spherulitic structure is first deformed and then broken up, creating highly oriented regions within the polymer component. Figure 10.19 shows the progression of the necked region during tensile tests of polypropylene samples. This mode of failure is common in semi-crystalline components, such as the one shown in Fig. 10.20 for a polyethylene automotive fan blade.



**Figure 10.19** Necking progression of a polypropylene specimen during a tensile test.

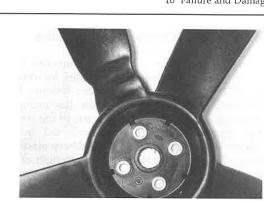
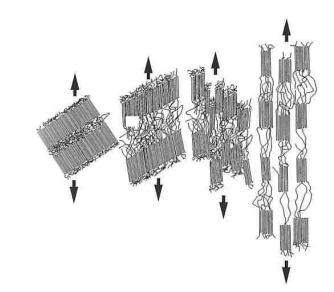


Figure 10.20 Necking of a polyethylene automotive fan blade [11].

Necking and cold drawing can be explained with the molecular model [10] shown in Fig. 10.21. Once the amorphous ties between lamellae have been completely extended, a slip-tilting of the lamellae is induced. As deformation continues, lamellae fragments get aligned in the direction of draw, forming fibrils of alternating crystal blocks and stretched amorphous regions.



tensile test.

10 Failure and Damage of Polymers 463

Figure 10.21 Molecular model used to represent necking and drawing during a



## 10.2.3 Failure of Highly Filled Systems or Composites

A polymer that usually fails under a brittle fracture can be toughened by adding filler particles. The most common examples for this effect are high impact polystyrene (HIPS) and ABS. In both these systems, brittle polymers, acrylic, and polystyrene, were toughened with the inclusion of rubbery particles into the material as shown in the schematic of the structure of HIPS in Fig. 10.22 [12]. This increase in toughness is reflected in the stress-strain behavior of HIPS shown in Fig. 10.23, where the rubbery elastic behavior of the rubber particles lowered the stiffness and ultimate strength of the material but increased its toughness. The rubber particles halt the propagation of a growing craze. Characteristic lengths of crazes that form in such systems are only as large as the characteristic gap between filler particles. This creates a system that has a large number of small crazes instead of the small number of large crazes present in the unfilled polymer. Table 10.3 [2] presents the effect of volume fraction of rubber particles on the mechanical and fracture properties of rubbermodified polystyrene. The impact strength and the fracture strain are maximized at a rubber particle volume fraction of about 20%.

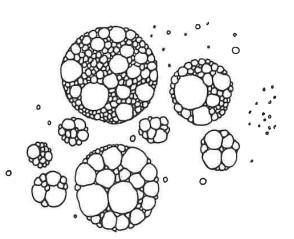
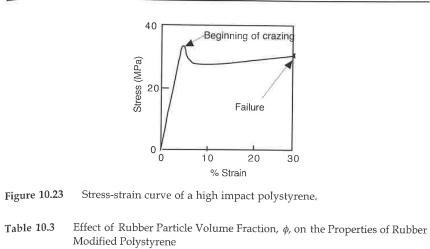


Figure 10.22 Schematic of the structure of a high impact polystyrene.



Volume fraction $\phi$	Tensile modulus GPa	Impact strength MJ/m <sup>3</sup>	Fracture strain %
0.06	2.8	0.42	3
0.12	2.4	1.90	20
0.22	1.9	11.6	45
0.30	1.0	5.6	34
0.78	0.55	1.2	8

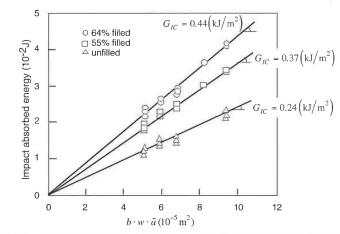
This increase in toughness can be observed even if the filler material is also brittle. Electron micrographs of such systems have shown that cracks propagate until they hit a filler particle, which often stops the propagation [2]. In thermosetting polymers, this effect is commonly referred to as crack pinning. Figure 10.24 compares plots of impact-absorbed energy as a function of specimen size for unfilled epoxy and epoxies filled with irregular-shaped silica with weight percents of 55% and 64%.

The failure of a fiber-filled material begins at the interface between filler or reinforcement and the matrix, as shown in the electron micrograph presented in Fig. 10.25 [13] . The micrograph was taken when a glass fiber filled polyester specimen was placed under loading and shows the breakage of the adhesion between imbedded glass fibers and their matrix. This breakage is generally referred to as debonding. This initial microcrack formation is reflected in a stress-strain curve by the deviation from the linear range of the elastic constants. In fact, the failure is analogous to the microcracks that form between spherulites when a semi-crystalline polymer is deformed.

10 Failure and Damage of Polymers 465







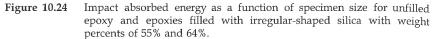




Figure 10.25 Electron micrograph of crack formation between polyester matrix and a glass fiber.

# 10.3 Impact Strength<sup>3</sup>

In practice, nearly all polymer components are subjected to impact loads. Since many polymers are tough and ductile, they are often well suited for this type of loading. However, under specific conditions even the most ductile materials, such as polypropylene, can fail in a brittle manner at very low strains. These types of failure are prone to occur at low temperatures and at very high deformation rates.

According to several researchers [14, 15] a significantly high rate of deformation leads to complete embrittlement of polymers which results in a lower threshold of elongation at break. Menges and Boden designed a special high-speed elongational testing device that was used to measure the minimum work required to break the specimens. The minimum strain,  $\varepsilon_{\min}$ , which can be measured with such a device, is a safe value to use in calculations for design purposes. One should always assume that if this minimum strain value is exceeded at any point in the component, initial fracture has already occurred. Table 10.4 [16, 17] presents minimum elongation at break values for selected thermoplastics on impact loading.

On the other hand, the stiffness and the stress at break of the material under consideration increase with the rate of deformation. Table 10.5 [16] presents data for the stress at break,  $\sigma_{\min}$ , for selected thermoplastics on impact loading. This stress corresponds to the point where the minimum elongation at break has just been reached.

#### Table 10.4 Minimu

Polym
HMW-PMMA
PA6 + 25% SFR
PP
uPVC
POM
PC + 20% SFR
PC

3 The term "impact strength" is widely misused, since one is actually referring to energy absorbed before failure.

10 Failure and Damage of Polymers 467

um	Elongation	at	Break	on	Impact	Loading
----	------------	----	-------	----	--------	---------

r	ε <sub>min</sub> (%)	
	2.2	
	1.8	
	1.8	
	2.0	
	4.0	
	4.0	
	6.0	



 Table 10.5
 Minimum Stress at Break on Impact Loading

Polymer	σ <sub>min</sub> (MPa)	
HMW-PMMA	135	
PA6 + 25% SFR	175	
uPVC	125	
POM	>130	
PC + 20% SFR	>110	
PC	>70	

Figure 10.26 summarizes the stress-strain and fracture behavior of a HMW-PMMA tested at various rates of deformation. The area under the stress-strain curves represents the volume-specific energy to fracture (w). For impact, the elongation at break of 2.2% and the stress at break of 135 MPa represent a minimum of volume-specific energy because the stress increases with higher rates of deformation, but the elongation at break remains constant. Hence, if we assume a linear behavior, the minimum volume-specific energy absorption up to fracture can be calculated using

$$w_{\min} = 0.5\sigma_{\max}\varepsilon_{\min} \tag{10.21}$$

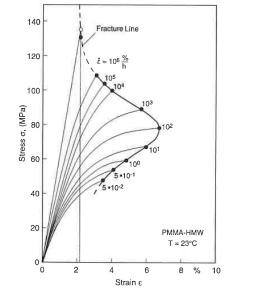
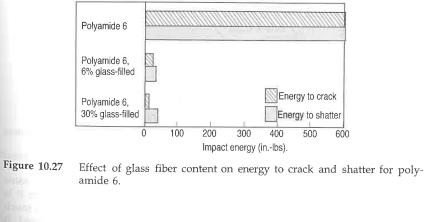


Figure 10.26 Stress-strain behavior of HMW-PMMA at various rates of deformation.

If the stress-strain distribution in the polymer component is known, one can estimate the minimum energy absorption capacity using  $w_{\min}$ . It can be assumed that failure occurs if  $w_{\min}$  is exceeded in any part of the loaded component. This minimum volume-specific energy absorption,  $w_{\min}$ , can be used as a design parameter. It was also used by Rest [18] for fiber-reinforced polymeric materials.

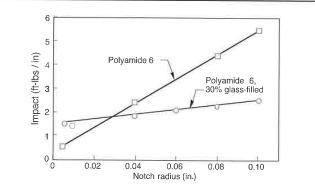
Glass fiber reinforced thermoplastics generally undergo brittle failure. Figure 10.27 [16] shows how the impact resistance of a polyamide 6 material was dramatically reduced with the addition of a glass reinforcement. Interesting to note is that the impact resistance of polyamide 6 with 6% and 30% glass reinforcement is essentially the same when compared to the unfilled material. However, a specimen with a sharp notch that resembles a crack will have a higher impact resistance if it is glass reinforced. Figure 10.28 [16] illustrates this by showing a plot of izod test data for polyamide 6 specimens and polyamide 6 specimens filled with 30% glass reinforcement as a function of notch radius. Here, the data for a small notch radius reflect the energy it takes to propagate the crack through the specimen. The data for a large notch radius approach the energy it takes to both, initiate and propagate a crack. In a filled polymer, a filler can sometimes increases the impact resistance of the component. For example, the volume fraction of crazes in a rubber particle filled polystyrene increases with increasing particle content. Figure 10.29 shows the volume fraction of craze voids as a function of rubber particle content in a high impact polystyrene. The figure also schematically depicts the relation between rubber particle content and craze geometry.



10 Failure and Damage of Polymers 469



470 Engineering Design Properties





Impact strength as a function of notch tip radius for a filled and unfilled polyamide 6.

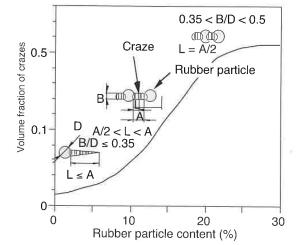
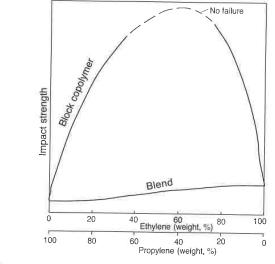


Figure 10.29 Volume fraction of craze voids as a function of rubber particle content in a high impact polystyrene.

The impact strength of a copolymer and polymer blend of the same materials can be quite different, as shown in Fig. 10.30. From the figure it is clear that the propylene-ethylene copolymer, which is an elastomer, has a much higher impact resistance than the basic polypropylene-polyethylene blend. It should be pointed out here that elastomers usually fail by ripping. The ripping

or tear strength of elastomers can be tested using the ASTM D1004, ASTM D1938, or DIN 53507 test methods. The latter two methods make use of rectangular test specimens with clean slits cut along the center. A typical tear propagation test for an elastomer composed of 75 parts of natural rubber (NR) and 25 parts of styrene butadiene rubber (SBR) is presented in Fig. 10.31.4 The tear strength of elastomers can be increased by introducing certain types of particulate fillers. For example, a well dispersed carbon black filler can double the ripping strength of a typical elastomer. Figure 10.32 [7] shows the effect that different types of fillers have on the ripping strength of a polychloroprene elastomer.

In general, one can say if the filler particles are well dispersed and have diameters between 20 nm and 80 nm, they will reinforce the matrix. Larger particles will act as microscopic stress concentrators and will lower the strength of the polymer component. A case where the filler adversely affects the polymer matrix is presented in Fig. 10.33 [7], where the strength of PVC is lowered with the addition of a calcium carbonate powder.

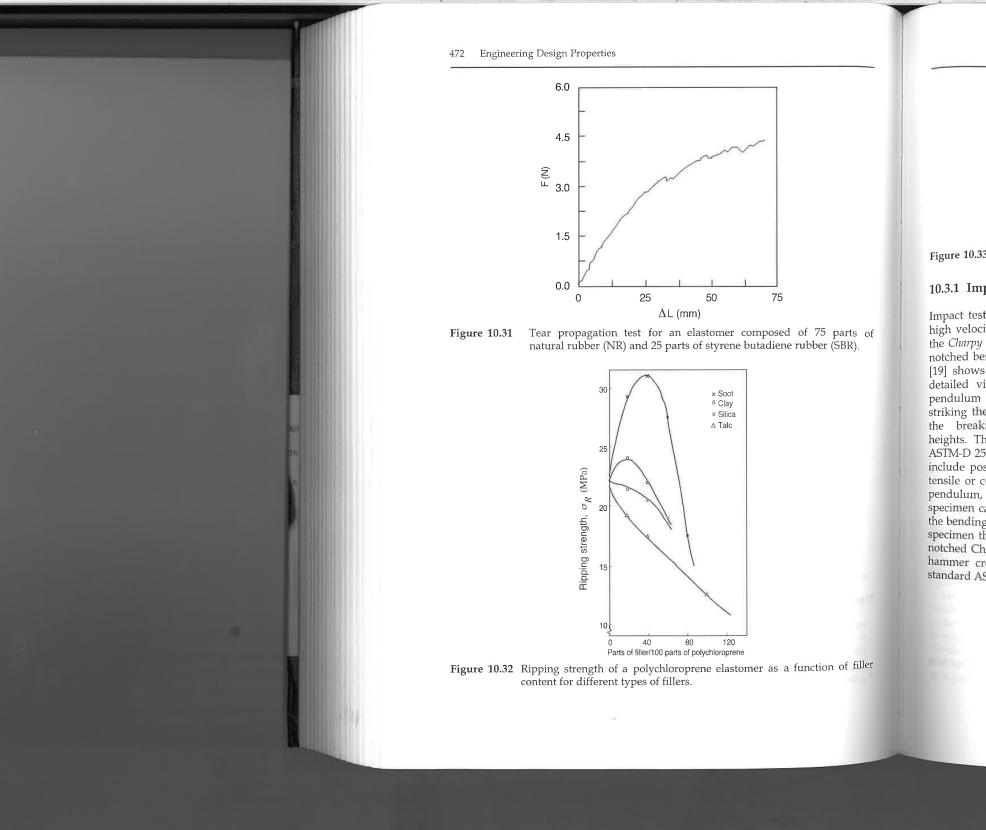


4 Courtesy of ICIPC, Medellín, Colombia.

10 Failure and Damage of Polymers 471

Figure 10.30 Impact strength of a propylene-ethylene copolymer and a polypropylene -polyethylene polymer blend.





10.3.1 Impact Test Methods Impact tests are widely used to evaluate a material's capability to withstand high velocity impact loadings. The most common impact tests are the Izod and the Charpy tests. The Izod test evaluates the impact resistance of a cantilevered notched bending specimen as it is struck by a swinging hammer. Figure 10.34 [19] shows a typical Izod-type impact machine, and Fig. 10.35 [19] shows a detailed view of the specimen, the clamp, and the striking hammer. The pendulum or hammer is released from a predetermined height and after striking the specimen, travels to a recorded height. The energy absorbed by the breaking specimen is computed from the difference between the two heights. The standard test method that describes the Izod impact test is the ASTM-D 256 test. There are several variations of the Izod test. These variations include positioning the test specimen such that the stresses in the notch are tensile or compressive by having the notch face away or toward the swinging pendulum, respectively. In addition, the clamping force exerted on the test specimen can have a great effect on the test results. The Charpy test evaluates the bending impact strength of a small notched or unnotched simply supported specimen that is struck by a hammer similar to the Izod impact tester [19]. The notched Charpy test is done such that the notch faces away from the swinging hammer creating tensile stresses within the notch, see Fig. 10.36. Both, the standard ASTM D256 and DIN 53453 tests describe the Charpy impact test.

# 10 Failure and Damage of Polymers 473

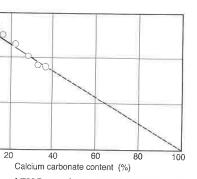
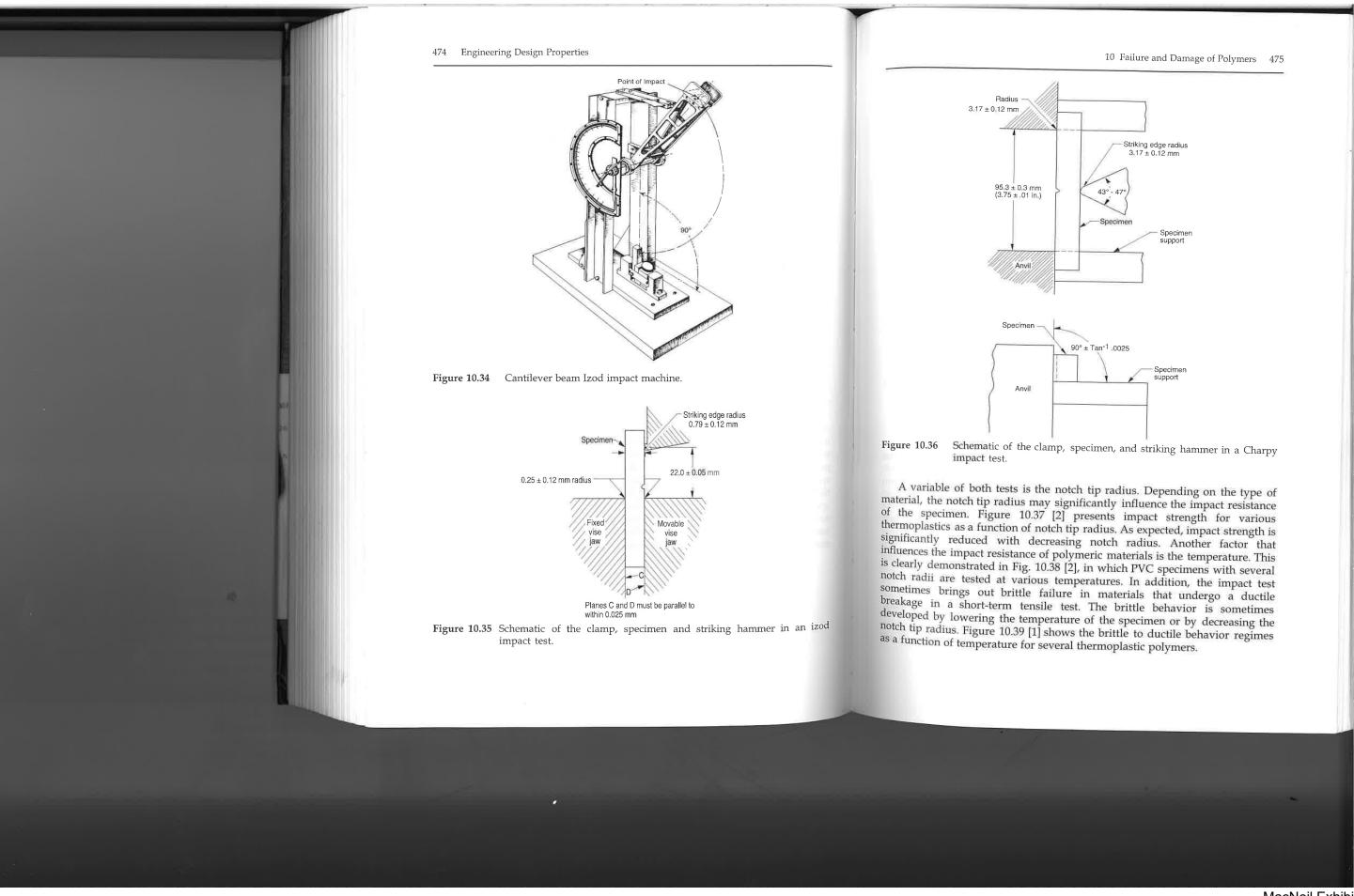


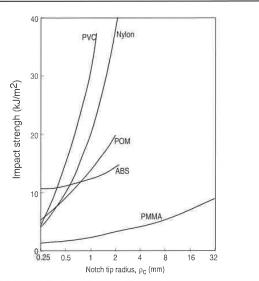
Figure 10.33 Tensile strength of PVC as a function of calcium carbonate content.

Σ

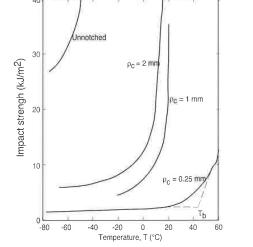
igth











Polystyrene Polymethyl methacrylate Polyamide (dry) - glass filled Methylpentene polymer Polypropylene Craze resistant acrylic Polyethylene terephthalate Polyacetal Rigid polyvinyl chloride Cellulose acetate butyrate Polyamide (dry) Polysulphones High density polyethylene Polyphenylene oxide Propylene-ethylene copolymers Acrylonitrile-butadiene-styrene Polycarbonate Polyamide (wet) Polytetrafluoroethylene Low density polyethylene

Figure 10.39 Brittle to ductile behavior regimes as a function of temperature for several thermoplastic polymers.

Another impact test worth mentioning is the *falling dart* test. This test is well suited for specimens that are too thin or flexible to be tested using the Charpy and Izod tests. This test, which is described by the ASTM 3029 and DIN 53 453 standard methods, also works well when the fracture toughness of a finished product with large surfaces is sought. Figure 10.40 shows a schematic of a typical falling dart test set-up [19]. The test consists of dropping a *tup*, with a spherical tip and otherwise variable shape and weight on a usually circular test specimen that is clamped around the periphery. The weight of the tup and the height from which it is dropped are the test variables. The energy needed to fracture the test specimen is directly computed from the potential energy of the tup before it is released; written as

where m is the mass of the tup, h the height from which it is dropped, and ggravity. It is assumed that the potential energy is fully transformed into kinetic energy and, in turn, into fracture energy. The test itself is much simpler than the Charpy and Izod tests, since Eq. 10.22 can be used to interpret the results

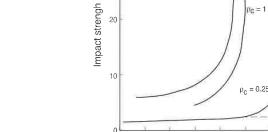
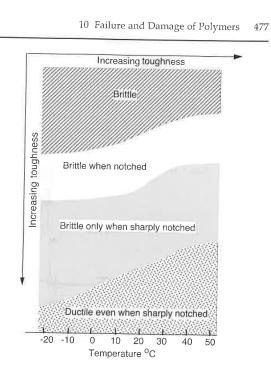


Figure 10.38 Impact strength of PVC as a function of temperature for various notch tip radii.



### $U_n = mgh$



MacNeil Exhibit 2117 Yita v. MacNeil IP, IPR2020-01139 Page 249

(10.22)

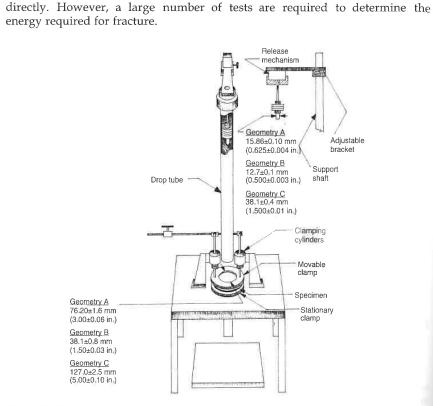


Figure 10.40 Schematic of a drop weight impact tester.

#### 10.3.2 Fracture Mechanics Analysis of Impact Failure

Although the most common interpretation of impact tests is qualitative, it is possible to use linear elastic fracture mechanics to quantitatively evaluate impact test results. Using LEFM, it is common to compute the material's fracture toughness  $G_{lc}$  from impact test results. Obviously, LEFM is only valid if the Izod or Charpy test specimen is assumed to follow linear elastic behavior and contains a sharp notch. At the onset of crack propagation, Eq. 10.4, which gives the elastic energy stored in the loaded test specimen, can be rewritten in terms of compliance, J, as

 $U_{c}$ 

given by

we can write Eq. 10.24 as

The parameter  $\tilde{a}$  is found in Table 10.6 [20] for various Charpy impact test specimens and in Table 10.7 [20] for various Izod impact test specimens. The elastic energy absorbed by the test specimen during fracture,  $U_e$ , can also be represented with energy lost by the pendulum,  $U_t$ . This allows the test engineer to relate impact test results with the fracture toughness  $G_{ic}$  of a material. When plotting  $U_e$  versus  $tw\tilde{a}$ , the kinetic effects lead to a positive intercept on the  $U_e$  axis. This can be corrected by subtracting the kinetic effects,  $U_{i}$ , from  $U_{e}$ . The kinetic effects can be computed using [20]

where m is the mass of the specimen, M the mass of the tup, V the velocity, and *e* the coefficient of restitution.

Figure 10.41 contains both Charpy and Izod test result data for a medium density polyethylene [20] as plots of  $U_e$  versus  $tw\tilde{a}$  with kinetic energy corrections. We can now calculate  $G_{lc}$  from the slope of the curve (Eq. 10.26).

However, as mentioned earlier for polymers that undergo significant plastic deformation before failure, Eq. 10.26 does not apply and the Jintegral must be used. Here, by taking the Charpy or Izod specimen and assuming full yield, having a plastic hinge, we can calculate the energy by using

 $U_{c}$ 

10 Failure and Damage of Polymers 479

$$U_c = \frac{1}{2} F_c^2 J$$
 (10.23)

Solving for  $F_c$  in Eq. 10.12 and substituting into Eq. 10.23 results in

$$G_{lc} t \left( \frac{J}{\partial J / \partial a} \right)$$
(10.24)

Introducing the test specimen's width, w, and a geometrical crack factor,  $\tilde{a}$ ,

$$\tilde{a} = \left(\frac{1}{J}\frac{\partial J}{\partial a}\right)^{-1} \tag{10.25}$$

$$U_{c} = G_{lc} w t \tilde{a} \tag{10.26}$$

$$\frac{1}{2}\frac{m}{M}(1-e)\bigg)m\bigg(\frac{M}{m+M}\bigg)V^2\tag{10.27}$$

$$=\frac{\delta}{2}\sigma_{y}t(w-a)$$

(10.28)



Table 10.	6 Charpy l	mpact Test	Geometric	Crack Facto	ors ã
	2L/D=4	2L/D=6	2L/D=8	2L/D=10	2L/D=12
a/D					
0.04	1.681	2.456	3.197	3.904	4.580
0.06	1.183	1.715	2220	2.700	3.155
0.08	0.933	1.340	1.725	2.089	2.432
0.10	0.781	1.112	1.423	1.716	1.990
0.12	0.680	0.957	1.217	1.461	1.688
0.14	0.605	0.844	1.067	1.274	1.467
0.16	0.550	0.757	0.950	1.130	1.297
0.18	0.505	0.688	0.858	1.015	1.161
0.20	0.468	0.631	0.781	0.921	1.050
0.22	0.438	0.584	0.718	0.842	0.956
0.24	0.413	0.543	0.664	0.775	0.877
0.26	0.391	0.508	0.616	0.716	0.808
0.28	0.371	0.477	0.575	0.665	0.748
0.30	0.354	0.450	0.538	0.619	0.694
0.32	0.339	0.425	0.505	0.578	0.647
0.34	0.324	0.403	0.475	0.542	0.603
0.36	0.311	0.382	0.447	0.508	0.564
0.38	0.299	0.363	0.422	0.477	0.527
0.42	0,276	0.328	0.376	0.421	0.462
0.44	0.265	0.311	0.355	0.395	0.433
0.46	0.254	0.296	0.335	0.371	0.405
0.48	0.244	0.281	0.316	0.349	0.379
0.50	0.233	0,267	0.298	0.327	0.355
0.52	0.224	0.253	0.281	0.307	0.332
0.54	0.214	0.240	0.265	0.88	0.310
0.56	0.205	0.228	0.249	0.270	0.290
0.58	0.196	0.216	0.235	0.253	0.271
0.60	0.187	0.205	0.222	0.238	0.253

a/D	2L/D=4	2L/D=6	2L/D=8	2L/D=10	2L/D=
0.06	1.540	1.744	1.850	2.040	
0.08	1.273	1.400	1.485	1.675	1.906
0.10	1.060	1.165	1.230	1.360	1.570
0.12	0.911	1.008	1.056	1.153	1.294
0.14	0.795	0.890	0.932	1.010	1.114
0.16	0.708	0.788	0.830	0.900	0.990
0.18	0.650	0.706	0.741	0.809	0.890
0.20	0.600	0.642	0.670	0.730	0.810
0.22	0.560	0.595	0.614	0.669	0.750
0.24	0.529	0.555	0.572	0.617	0.697
0.26	0.500	0.525	0.538	0.577	0.656
0.28	0.473	0.500	0.510	0.545	0.618
0.30	0.452	0.480	0.489	0.519	0.587
0.32	0.434	0.463	0.470	0.500	0.561
0.34	0.420	0.446	0.454	0.481	0.538
0.36	0.410	0.432	0.440	0.468	0.514
0.38	0.397	0.420	0.430	0.454	0.494
0.40	0.387	0.410	0.420	0.441	0.478
0.42	0.380	0.400	0.411	0.431	0.460
0.44	0.375	0.396	0.402	0.423	0.454
0.46	0.369	0.390	0.395	0.415	0.434
0.48	0.364	0.385	0.390	0.408	0.422
0.50	0.360	0.379	0.385	0.399	0.411

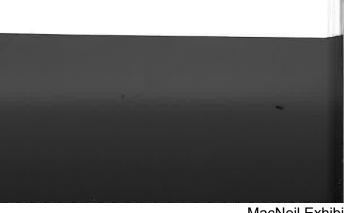
where t(w-a) was replaced by A or the cross-sectional area of the specimen where fracture occurs. Figure 10.42 gives results for  $U_e$  as a function of A for high-impact polystyrene. The results show close agreement between the Charpy and Izod test methods and a linear correlation exists, as predicted with Eq. 10.29.

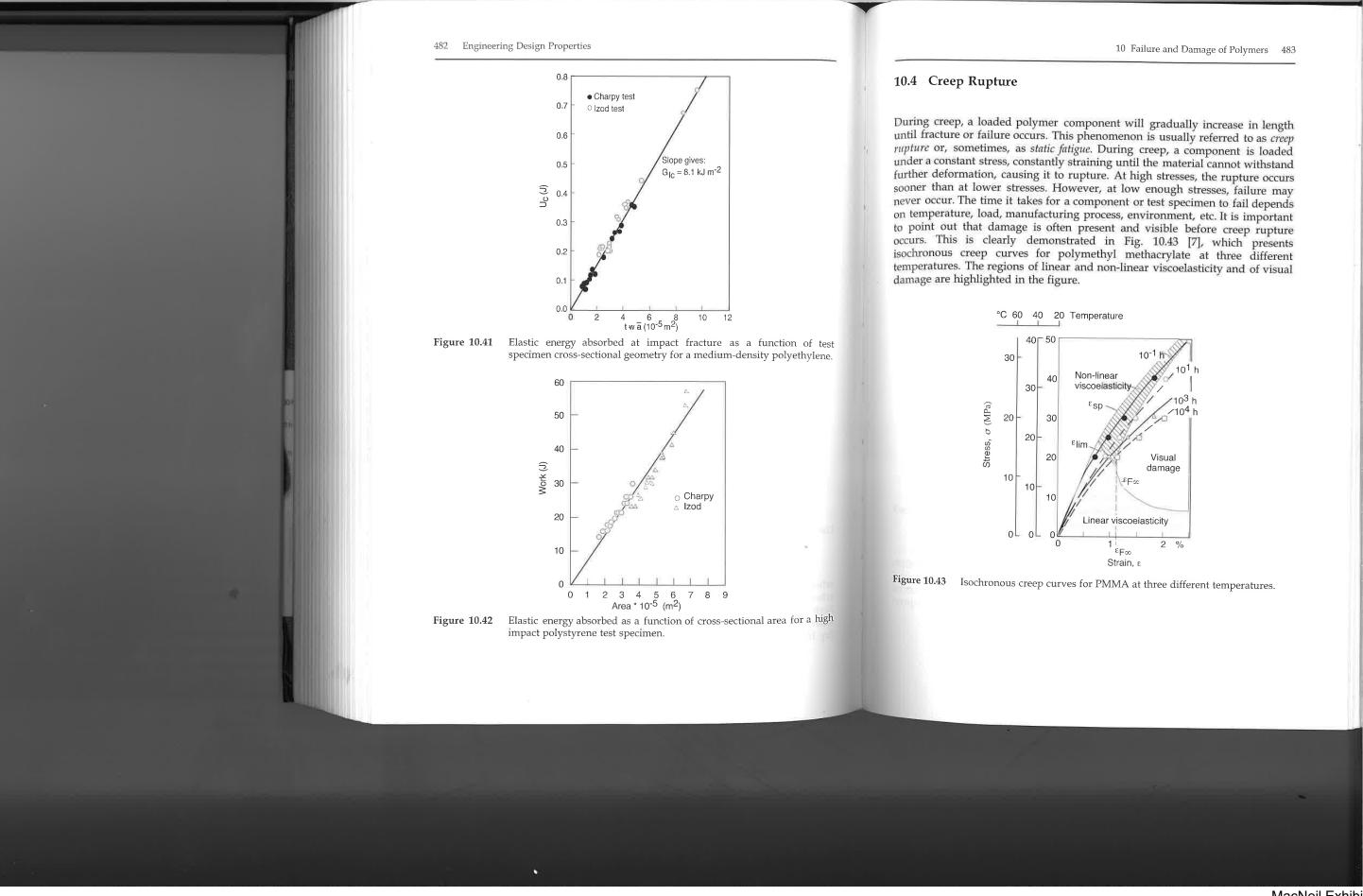
10 Failure and Damage of Polymers 481

Using the relation in Eq. 10.20 with Eq. 10.28 we can write

$$J_{lc} = \frac{2U_c}{A}$$

(10.29)





# **10.4.1** Creep Rupture Tests

The standard test to measure creep rupture is the same as the creep test discussed in the previous chapter. Results from creep rupture tests are usually presented in graphs of applied stress versus the logarithm of time to rupture. A sample of creep rupture behavior for several thermoplastics is presented in Fig. 10.44 [21]. As the scale in the figure suggests, the tests were carried out with loadings that cause the material to fail within a few weeks. An example of a creep rupture test that ran for 10 years is shown in Fig. 10.45 [22, 23]. Here, the creep rupture of high density polyethylene pipes under internal pressures was tested at different temperatures. Two general regions with different slopes become obvious in the plots. The points to the left of the knee represent pipes that underwent a ductile failure, whereas those points to the right represent the pipes that had a brittle failure. As pointed out, generating a graph such as the one presented in Fig. 10.45, is an extremely involved and lengthy task, that takes several years of testing.<sup>5</sup> Usually, these types of tests are carried out to 1,000 h (6 weeks) or 10,000 h (60 weeks) as shown in Fig. 10.466 for a polyamide 6 with 30% glass fibers tested at different temperatures. Once the steeper slope, which is typical of the brittle fracture has been reached, the line can be extrapolated with some degree of confidence to estimate values of creep rupture at future times.

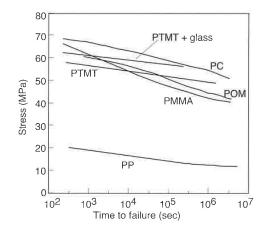
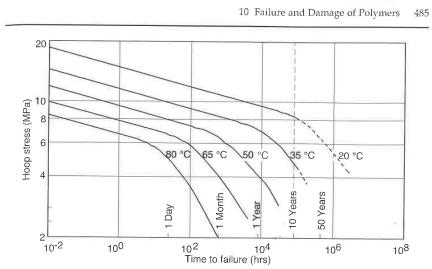
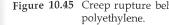


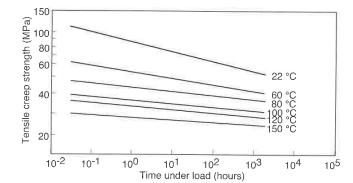
Figure 10.44 Creep rupture behavior for various thermoplastics.

5 These tests where done between 1958 and 1968 at Hoechst AG, Germany.









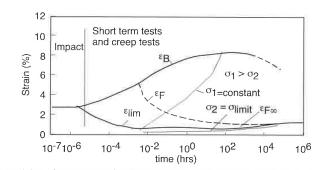
Although the creep test is considered a long term test, in principle it is difficult to actually distinguish it from monotonic stress strain tests or even impact tests. In fact, one can plot the full behavior of the material, from impact to creep, on the same graph as shown for PMMA under tensile loads at room temperature in Fig. 10.47 [7].

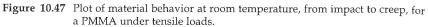
Figure 10.45 Creep rupture behavior as a function of temperature for a high density

Figure 10.46 Creep rupture behavior as a function of temperature for a polyamide 6 with 30% glass fibers (Durethan BKV 30).



MacNeil Exhibit 2117 Yita v. MacNeil IP, IPR2020-01139 Page 253





The figure represents strain as a function of the logarithm of time. The strain line that represents rupture is denoted by  $\varepsilon_{R}$ . This line represents the maximum attainable strain before failure as a function of time. Obviously, a material tested under an impact tensile loading will strain much less than the same material tested in a creep test. Of interest in Fig. 10.47 are the two constant stress lines denoted by  $\sigma_1$  and  $\sigma_2$ . The following example will help the reader interpret Fig. 10.47. It can be seen that a PMMA specimen loaded to a hypothetical stress of  $\sigma_1$  will behave as a linear viscoelastic material up to a strain of 1%, at which point the first microcracks start forming or the craze nucleation begins. The crazing appears a little later after the specimen's deformation is slightly over 2%. The test specimen continues to strain for the next 100 h until it ruptures at a strain of about 8%. From the figure it can be deduced that the first signs of crazing can occur days and perhaps months or years before the material actually fractures. The stress line denoted by  $\sigma_2$ , where  $\sigma_1 > \sigma_2$  is a limiting stress under which the component will not craze. Figure 10.47 also demonstrates that a component loaded at high speeds (i.e., impact) will craze and fail at the same strain. A limiting strain of 2.2% is shown.

Since these tests take a long time to perform, it is often useful to test the material at higher temperatures, where a similar behavior occurs in a shorter period of time. Figure 10.48 [7] shows tests performed on PMMA samples at five different temperatures. When comparing the results in Fig. 10.48 to the curve presented in Fig. 10.47, a clear time-temperature superposition becomes visible. In the applied stress versus logarithm of time to rupture curves, such as the one shown in Fig. 10.45, the time-temperature superposition is also evident.

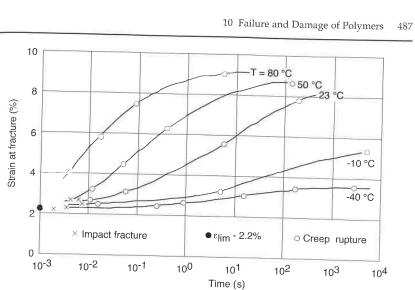


Figure 10.48 Strain at fracture for a PMMA in creep tests at various temperatures.

# 10.4.2 Fracture Mechanics Analysis of Creep Rupture

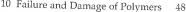
Crack growth rates during static tests have been found to have a power law relation with the stress intensity factor  $K_{k,i}$  as

where A and m are material properties and  $K_{lc}$  can be computed using Eq. 10.3 which results in

> da  $\frac{-}{dt} =$

By ignoring the time it takes for crack initiation, this equation may be used to predict a conservative time for creep rupture of a polymer component. If we integrate Eq. 10.31, we can predict the time it takes for a crack to grow from a length  $a_1$  to a length  $a_2$  by using

 $t = \frac{2(m-1)}{(m-1)}$ 



$$\frac{da}{dt} = AK_{l_c}^m \tag{10.30}$$

$$A(Y\sigma)^m(\pi a)^{m/2} \tag{10.31}$$

$$\frac{\left(a_{1}^{1-\frac{m_{2}}{2}}-a_{2}^{1-\frac{m_{2}}{2}}\right)}{\cdot 2\right)C_{1}\left(Y\sigma\sqrt{\pi}\right)^{m}$$

(10.32)

Experimental evidence shows that for slow crack growth, the value of m is large, and ranges between 7 and 25. Hence, the time it takes for a crack to grow between  $a_1$  and  $a_2$  is dominated by the initial crack length, because a small crack will grow much slower than a large one.

# 10.5 Fatigue

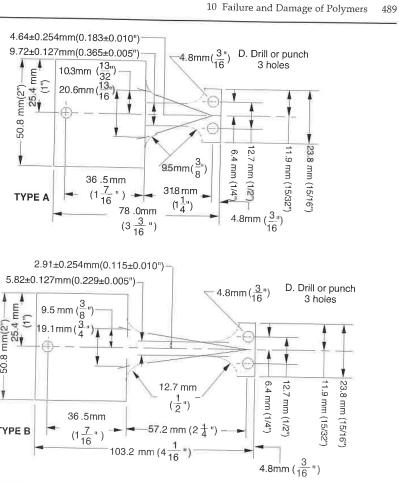
Dynamic loading of any material that leads to failure after a certain number of cycles is called fatigue or dynamic fatigue. Dynamic fatigue is of extreme importance since a cyclic or fluctuating load will cause a component to fail at much lower stresses than it does under monotonic loads.

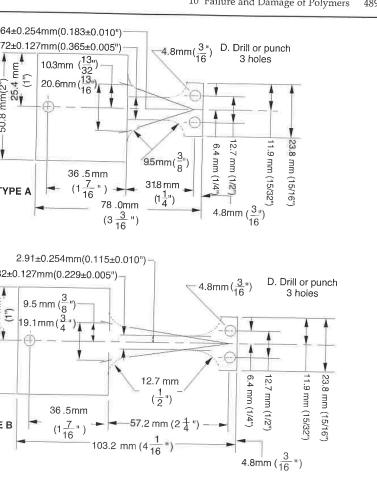
#### 10.5.1 Fatigue Test Methods

The standard fatigue tests for polymeric materials are the ASTM-D 671 test and the DIN 50100 test. In the ASTM test, a cantilever beam, shown in Fig. 10.49 [19], is held in a vise and bent at the other end by a yoke which is attached to a rotating variably eccentric shaft. A constant stress throughout the test region in the specimen is achieved by its triangular shape.

Fatigue testing results are plotted as stress amplitude versus number of cycles to failure. These graphs are usually called S-N curves, a term inherited from metal fatigue testing [24]. Figure 10.50 [25] presents S-N curves for several thermoplastic and thermoset polymers tested at a 30-Hz frequency and about a zero mean stress,  $\sigma_{\rm m}$ .

We must point out here, that most fatigue data presented in the literature and in resin supplier data sheets does not present the frequency, specimen geometry or environmental conditions at which the tests were performed. Hence, such data is not suitable for use in design. The data we present in this section is only intended to illustrate the various problems that arise when measuring fatigue life of a polymer. The information should also serve to reflect trends and as a comparison between various materials and conditions.





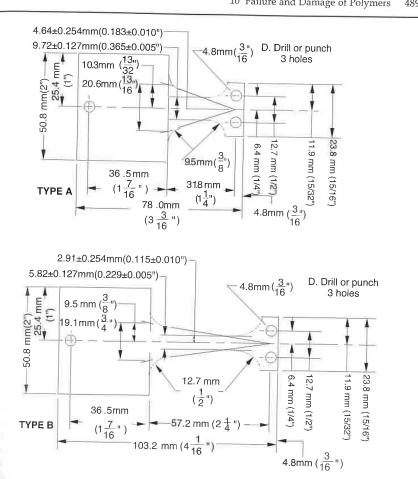


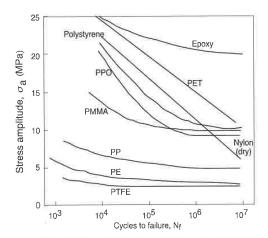
Figure 10.49 ASTM constant force fatigue test specimens.

Fatigue in plastics is strongly dependent on the environment, the temperature, the frequency of loading, the surface, etc. For example, due to surface irregularities and scratches, crack initiation at the surface is more likely in a polymer component that has been machined than in one that was injection molded. As mentioned in Chapter 5, an injection molded article is formed by several layers of different orientation. In such parts the outer layers act as a protective skin that inhibits crack initiation. In an injection molded article, cracks are more likely to initiate inside the component by defects such as weld



MacNeil Exhibit 2117 Yita v. MacNeil IP, IPR2020-01139 Page 255

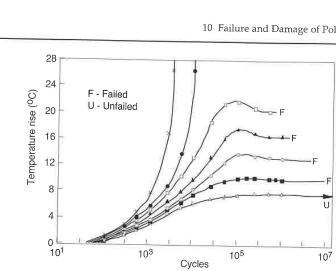
lines and filler particles. The gate region is also a prime initiator of fatigue cracks. Corrosive environments also accelerate crack initiation and failure via fatigue. Corrosive environments and weathering will be discussed in more detail later in this chapter.

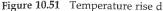




Stress-life (S-N) curves for several thermoplastic and thermoset polymers tested at a 30-Hz frequency about a zero mean stress.

It is interesting to point out in Fig. 10.50 that thermoset polymers show a higher fatigue strength than thermoplastics. An obvious cause for this is their greater rigidity. However, more important is the lower internal damping or friction, which reduces temperature rise during testing. Temperature rise during testing is one of the main factors that lead to failure when experimentally testing thermoplastic polymers under cyclic loads. The heat generation during testing is caused by the combination of internal frictional or hysteretic heating and low thermal conductivity. At a low frequency and low stress level, the temperature inside the polymer specimen will rise and eventually reach thermal equilibrium when the heat generated by hysteretic heating equals the heat removed from the specimen by conduction. As the frequency is increased, viscous heat is generated faster, causing the temperature to rise even further. This phenomenon is shown in Fig. 10.51 [21] in which the temperature rise during uniaxial cyclic testing of polyacetal is plotted. After thermal equilibrium has been reached, a specimen eventually fails by conventional brittle fatigue, assuming the stress is above the endurance limit.



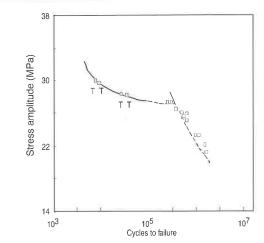


However, if the frequency or stress level is increased even further, the temperature will rise to the point at which the test specimen softens and ruptures before reaching thermal equilibrium. This mode of failure is usually referred to as thermal fatigue. This effect is clearly demonstrated in Fig. 10.52 [21]. The points marked T denote those specimens that failed due to thermal fatigue. The other points represent the specimens that failed by conventional mechanical fatigue. A better picture of how frequency plays a significant role in fatigue testing of polymeric materials is generated by plotting results such as those shown in Fig. 10.52 [21] for several frequencies (Fig. 10.53 [21]). The temperature rise in the component depends on the geometry and size of test specimen. For example, thicker specimens will cool slower and are less likely to reach thermal equilibrium. Similarly, material around a stress concentrator will be subjected to higher stresses which will result in temperatures that are higher than the rest of the specimen leading to crack initiation caused by localized thermal fatigue. To neglect the effect of thermal fatigue, cyclic tests with polymers must be performed at very low frequencies that make them much lengthier than those performed with metals and other materials which have high thermal conductivity.

10 Failure and Damage of Polymers 491

Figure 10.51 Temperature rise during uniaxial cycling under various stresses at 5-Hz.







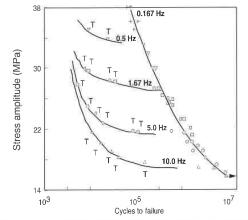
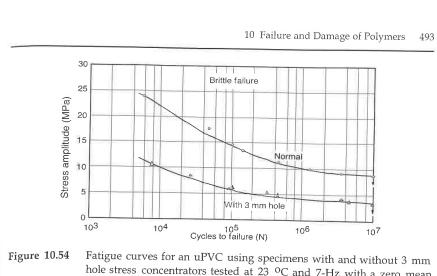
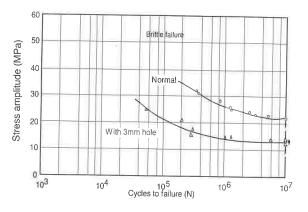


Figure 10.53 Fatigue and thermal failures in acetal tested at various frequencies.

As mentioned earlier, stress concentrations have a great impact on the fatigue life of a component. Figures 10.547 and 10.556 compare S-N curves for uPVC and polyamide 66, respectively, for specimens with and without a 3 mm

7 All courtesy of Bayer AG, Germany.



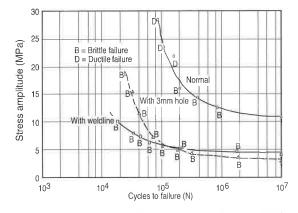


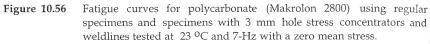
stress.

Figure 10.55 Fatigue curves for polyamide 66 (Durethan A30S) using specimens with and without 3 mm hole stress concentrators tested at 23 °C and 7-Hz with a zero mean stress.

hole stress concentrators tested at 23 °C and 7-Hz with a zero mean

circular hole acting as a stress concentrator. Material irregularities caused by filler particles or by weld lines also affect the fatigue of a component. Figures 10.566 and 10.576 compare S-N curves for regular PC and ABS test specimens to fatigue behavior of specimens with a weld line and specimens with a 3-mm circular hole.





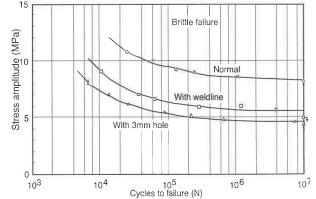
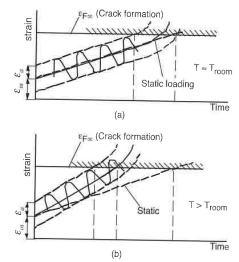


Figure 10.57 Fatigue curves for ABS (Novodur PH/AT) using regular specimens and specimens with 3 mm hole stress concentrators and weldlines tested at 23 °C and 7-Hz with a zero mean stress.

Up to this point, we assumed a zero mean stress,  $\sigma_{\rm m}$ . However, many polymer components that are subjected to cyclic loading have other loads and stresses applied to them, leading to non-zero mean stress values. This superposition of two types of loading will lead to a combination of creep, caused by the mean stress, and fatigue, caused by the cyclic stress,  $\sigma_a$ . Test results from experiments with cyclic loading and non-zero mean stresses are complicated by the fact that some specimens fail due to creep and others due to conventional brittle fatigue. Figure 10.58 illustrates this phenomenon for both cases with and without thermal fatigue, comparing them to experiments in which a simple static loading is applied. For cases with two or more dynamic loadings with different stress or strain amplitudes, a similar strain deformation progression is observed. Figure 10.59 [26] presents the strain progression in polyacetal specimens in which two stress amplitudes, one above and one below the linear viscoelastic range of the material, are applied. The strain progression,  $\Delta \varepsilon$ , is the added creep per cycle caused by different loadings, similar to ratcheting effects in metal components where different loadings are combined.

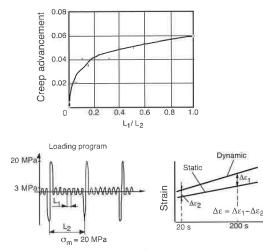


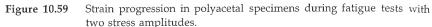
# 10 Failure and Damage of Polymers 495

Figure 10.58 Creep and thermal fatigue effects during cyclic loading.

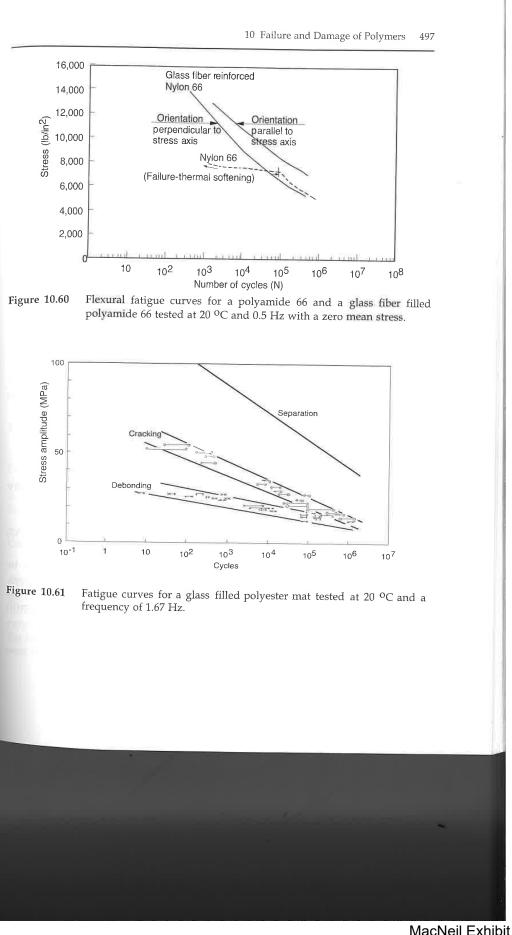


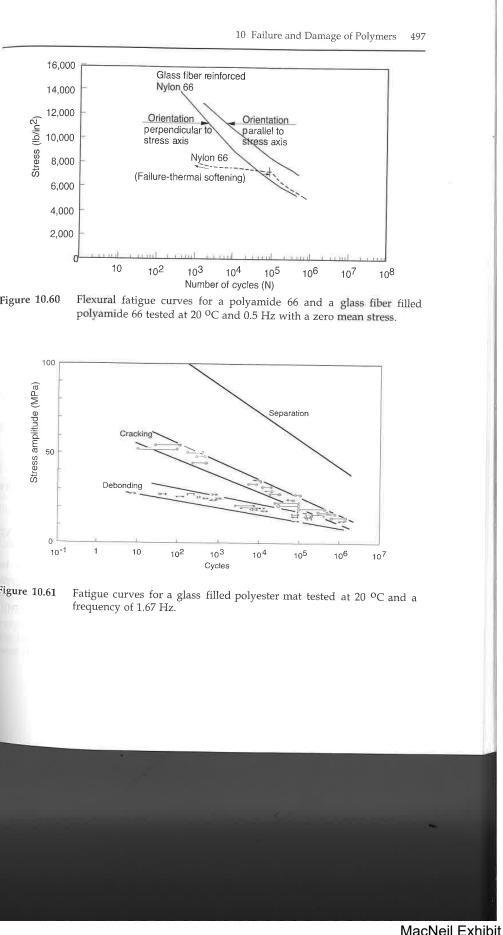
MacNeil Exhibit 2117 Yita v. MacNeil IP, IPR2020-01139 Page 258

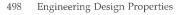


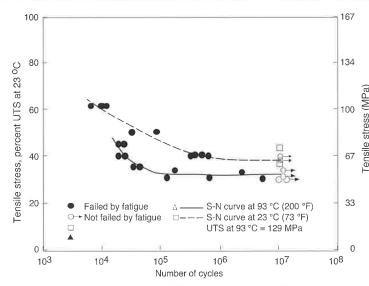


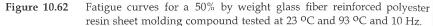
Fiber-reinforced composite polymers are stiffer and less susceptible to fatigue failure. Reinforced plastics have also been found to have lower hysteretic heating effects, making them less likely to fail by thermal fatigue. Figure 10.60 [27] presents the flexural fatigue behavior for glass fiber filled and unfilled polyamide 66 tested at 20 °C and a 0.5 Hz frequency with a zero mean stress. Parallel to the fiber orientation, the fatigue life was greater than the life of the specimens tested perpendicular to the orientation direction and the unfilled material specimens. The fatigue life of the unfilled specimen and the behavior perpendicular to the orientation direction were similar. However, the unfilled material failed by thermal fatigue at high stresses, whereas both the specimens tested perpendicular and parallel to the orientation direction failed by conventional fatigue at high stress levels. Fiber reinforced systems generally follow a sequence of events during failure consisting of debonding, cracking, and separation [28]. Figure 10.61 [29] clearly demonstrates this sequence of events with a glass-filled polyester mat tested at 20 °C and a frequency of 1.67 Hz. In most composites, debonding occurs after just a few cycles. It should be pointed out that often reinforced polymer composites do not exhibit an endurance limit, making it necessary to use factors of safety between 3 and 4. The fracture by fatigue is generally preceded by cracking of the matrix material, which gives a visual warning of imminent failure. It is important to mention that the fatigue life of thermoset composites is also affected by temperature. Figure 10.62 [30] shows the tensile strength versus











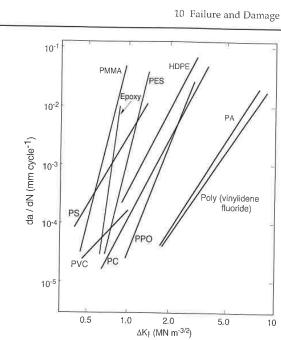
number of cycles to failure for a 50% glass fiber filled unsaturated polyester tested at 23 °C and 93 °C. At ambient temperature, the material exhibits an endurance limit of about 65 MPa, which is reduced to 52 MPa at 93 °C.

# **10.5.2** Fracture Mechanics Analysis of Fatigue Failure

Crack growth rates during cyclic fatigue tests are related to the stress intensity factor difference,  $\Delta K_{lc}$ ,

$$\frac{da}{dt} = B\left(\Delta K_{lc}\right)^n \tag{10.3}$$

where *B* and *n* are material properties and  $\Delta K_{lc} = K_{lcmax} - K_{lemin}$  can be computed using Eq. 10.3 with the maximum and minimum alternating stresses. Crack growth behavior for several polymers is shown in Fig. 10.63 [29, 31]. Hertzberg and Manson [29] also show that for some materials, the crack growth rate is reduced somewhat with increasing test frequency.



#### 10.6 Friction and Wear

Friction is the resistance that two surfaces experience as they slide or try to slide past each other. Friction can be dry (i.e., direct surface-surface interaction) or lubricated, where the surfaces are separated by a thin film of a lubricating fluid.

The force that arises in a dry friction environment can be computed using Coulomb's law of friction as

where *F* is the force in surface or sliding direction, *N* the normal force, and  $\mu$ the coefficient of friction. Coefficients of friction between several polymers and different surfaces are listed in Table 10.8 [7]. However, when dealing with polymers, the process of two surfaces sliding past each other is complicated by the fact that enormous amounts of frictional heat can be generated and stored near the surface due to the low thermal conductivity of the material. The



Figure 10.63 Crack growth rate during fatigue for various polymers.

 $F = \mu N$ 

(10.34)



analysis of friction between polymer surfaces is complicated further by environmental effects such as relative humidity and by the likeliness of a polymer surface to deform when stressed, such as shown in Fig. 10.64 [7]. The top two figures illustrate metal-metal friction, wheareas the bottom figures illustrate metal-polymer friction.

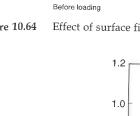
Table 10.8	Coefficient of Friction for Various Polymers
Lable 10.0	Coefficient of Friction for Various Forymers

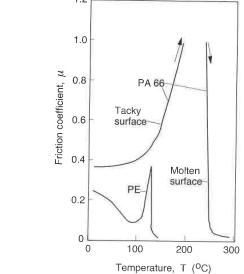
				5					
Specimen	Partner			Velocity (mm/s)					
		0.03	0.1	0.4	0.8	3.0	10.6		
Dry friction									
PP'	$PP^{*}$	0.54	0.65	0.71	0.77	0.77	0.71		
PA	PA	0.63	1921	0.69	0.70	0.70	0.65		
PP	PP'	0.26	0.29	0.22	0.21	0.31	0.27		
PA	$PA^{m}$	0.42	(#)	0.44	0.46	0.46	0.47		
Steel	$PP^{\circ}$	0.24	0.26	0.27	0.29	0.30	0.31		
Steel	$PA^{m}$	0.33	-	0.33	0.33	0.30	0.30		
PP⁵	Steel	0.33	0.34	0.37	0.37	0.38	0.38		
PA"	Steel	0.39	1990 1990	0.41	0.41	0.40	0.40		
Water lubricated									
PP	$PP^{s}$	0.25	0.26	0.29	0.30	0.28	0.31		
PA''	$PA^m$	0.27	153	0.24	0.22	0.21	0.19		
Steel	$PP^{\circ}$	0.23	0.25	0.26	0.26	0.26	0.22		
PP <sup>s</sup>	Steel	0.25	0.25	0.26	0.26	0.25	0.25		
PA <sup>m</sup>	Steel	0.20	-	0.23	0.23	0.22	0.18		
Oil lubricated									
PP*	PP	0.29	0.26	0.24	0.25	0.22	0.21		
PA <sup>m</sup>	$PA^{m}$	0.22	-	0.15	0.13	0.11	0.08		
Steel	$PP^{s}$	0.17	0.17	0.16	0.16	0.14	0.14		
Steel	PA	0.16	548	0.11	0.09	0.08	0.08		
PP <sup>*</sup>	Steel	0.31	0.30	0.30	0.29	0.27	0.25		
PA <sup>m</sup>	Steel	0.26	100	0.15	0.12	0.07	0.04		

Note i = injection molded, s = sandblasted, m = machined.

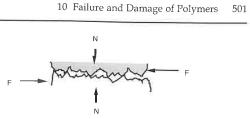
Temperature plays a significant role on the coefficient of friction  $\mu$  as clearly demonstrated in Fig. 10.65 for polyamide 66 and polyethylene. In the case of polyethylene, the friction first decreases with temperature. At 100 °C the friction increases because the polymer surface becomes tacky. The friction coefficient starts to drop as the melt temperature is approached. A similar behavior is encountered with the polyamide curve.

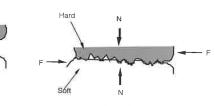






high density polyethylene.





After loading

Figure 10.64 Effect of surface finish and hardness on frictional force build-up.

Figure 10.65 Temperature effect on coefficient of friction for a polyamide 66 and a



As mentioned earlier, temperature increases can be caused by the energy released by the frictional forces. A temperature increase in time, due to friction between surfaces of the same material, can be estimated using

$$\Delta T = \frac{2\dot{Q}\sqrt{t}}{\sqrt{\pi}\sqrt{k\rho C_p}} \tag{10.35}$$

where k is the thermal conductivity of the polymer,  $\rho$  the density,  $C_{p}$  the specific heat and the rate of energy created by the frictional forces which can be computed using

$$\hat{Q} = Fv \tag{10.36}$$

where v is speed between the sliding surfaces.

Wear is also affected by the temperature of the environment. Figure 10.668 shows how wear rates increase dramatically as the surface temperature of the polymer increases, causing it to become tacky.

Table 10.9 [32] presents relative volumetric wear values for selected polymers and beechwood using the volumetric wear of steel St 37 as a reference.

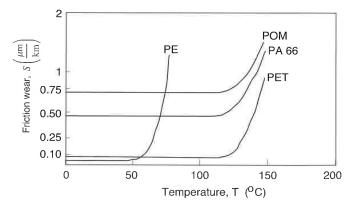


Figure 10.66 Wear as a function of temperature for various thermoplastics.

8 Courtesy of BASF.

Table 10.9
Polymer
Steel
Beechwood
PMMA
PVC-U
HDPE
PP
HDPE
PA 66
UHMW-HDPE

# 10.7 Stability of Polymer Structures

The failure of certain structures is often determined by the stiffness of the structural element and not by the strength of the material. Such a failure is commonly referred to as buckling. The common example of buckling is the failure of a slender column under compressive loads. Slender columns with hinged ends have a critical load,  $F_{crit}$ , defined by

F<sub>crit</sub> Α

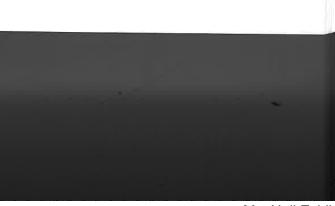
Relative Volumetric Wear					
Density (g/cm <sup>3</sup> )	Wear/Wear <sub>steel</sub>				
7.45	1.0				
0.83	17.9				
1.31	11.2				
1.33	5.8				
0.92	3.8				
0.90	2.8				
0.95	2.1				
1.13	1.0				
0.94	0.6				

10 Failure and Damage of Polymers 503

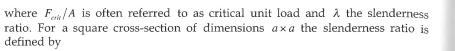
$$\vec{r}_{crit} = \frac{\pi^2 EI}{L^2} \tag{10.37}$$

where E is the modulus, I the area moment of inertia and L the length of the column. If we use the relation  $I = Ar^2$ , where A is the cross-sectional area of the column and r is the radius of gyration, we can rewrite Eq. 10.37 as

$$=\frac{\pi^2 EI}{\left(\frac{L}{\gamma}\right)^2} = \frac{\pi^2 EI}{\lambda^2}$$
(10.38)



MacNeil Exhibit 2117 Yita v. MacNeil IP, IPR2020-01139 Page 262



$$\lambda = \frac{L}{\sqrt{12}} \tag{10.39}$$

Menges and Dolfen performed a series of compression tests on glass fiber reinforced unsaturated polyester specimens of square cross-section. Figure 10.67 [33] presents the unit loads and compressive strains at failure of the composite columns as a function of slenderness ratio. Their experiments demonstrated that at slenderness ratios smaller than 20 the columns failed by a shear delamination mode, while columns with slenderness ratios larger than 20 failed by buckling. Similarly, Gaube and Menges [34] performed experiments with various shell structures. Figure 10.68 presents the critical strain as a function of slenderness ratio. We can see here that in all cases buckling of polymer structures occurred below the value predicted by classical stability theory.

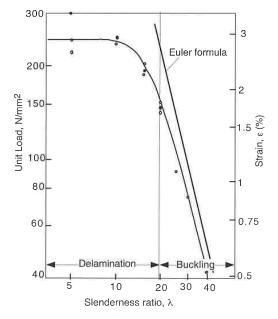
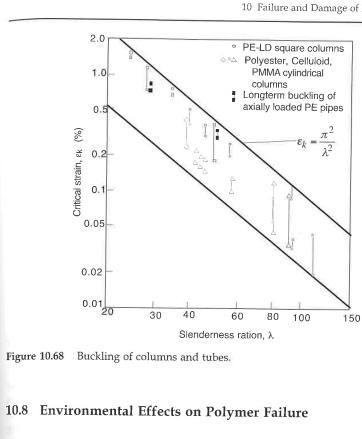


Figure 10.67 Delamination and buckling of glass reinforced UPE columns.



The environment or the media in contact with a loaded or unloaded component plays a significant role on its properties, life span, and mode of failure. The environment can be a natural one, such as rain, hail, solar ultra-violet radiation, extreme temperatures, etc., or an artificially created one, such as solvents, oils, detergents, high temperature environments, etc. Damage in a polymer component due to natural environmental influences is usually referred to as weathering.

10.8.1 Weathering

When exposed to the elements, polymeric materials begin to exhibit environmental cracks, which lead to early failure at stress levels significantly

10 Failure and Damage of Polymers 505



lower than those in the absence of these environments. Figure 10.69 [35] shows an electron micrograph of the surface of a high-density polyethylene beer crate after nine years of use and exposure to weathering. The surface of the HDPE exhibits brittle cracks, which resulted from ultra violet rays, moisture, and extremes in temperature.

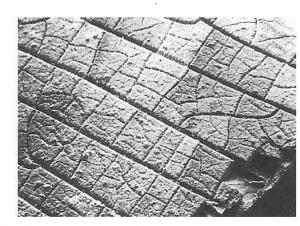


Figure 10.69 Electron micrograph of the surface of a high density polyethylene beer crate after nine years of use and exposure to weathering.

Standard tests such as the DIN 53486 test are available to evaluate effects of weathering on properties of polymeric materials. It is often unclear which weathering aspects or what combination of them influence material decay the most. Hence, laboratory tests are often done to isolate individual weathering factors such as ultra-violet radiation. For example, Fig. 10.70 shows the surface of a polyoxymethylene specimen irradiated with ultra violet light for 100 h in a laboratory environment. The DIN 53487 xenotest is a standard test to expose polymer test specimens to UV radiation in a controlled environment. Figure 10.71 is a plot of impact strength of notched PMMA specimens as a function of hours of UV radiation exposure in a controlled DIN 53487 test and years of weathering under standard DIN 53486 conditions. The correlation between the two tests is clear. The ASTM-D 4674 test evaluates the color stability of polymer specimens exposed to ultra violet radiation. Standard tests also exist to test materials for specific applications such as the ASTM-D 2561 test, which evaluates the environmental stress cracking resistance of blow molded polyethylene containers.

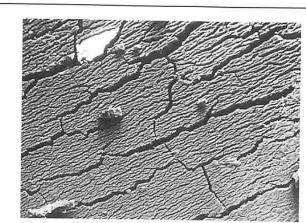
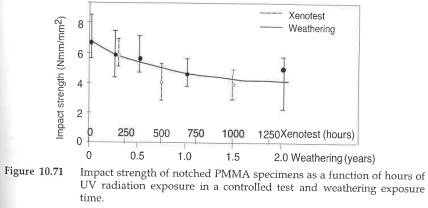


Figure 10.70



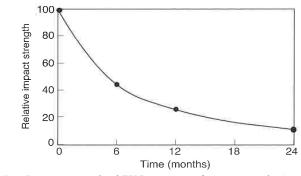
As can be seen, the effect of ultra violet radiation, moisture, and extreme temperature is detrimental to the mechanical properties of plastic parts. One example in which weathering completely destroys the strength properties of a material is shown for PVC in Fig. 10.72. The figure presents the decay of the impact strength of PVC pipes exposed to weathering in the United Kingdom [36]. As can be seen, the impact strength rapidly decreases in the first six months and is only 11% of its original value after only two years. The location and climate of a region can play a significant role on the weathering of polymer components. Figure 10.73 [36] shows the decrease in impact strength

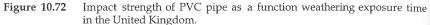
10 Failure and Damage of Polymers 507

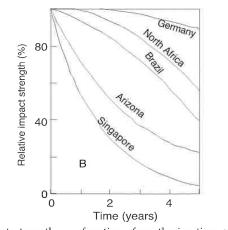
Surface of a polyoxymethylene specimen irradiated with ultra violet light for 100 h in a laboratory environment.

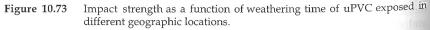


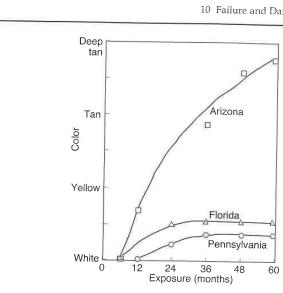
of rigid PVC as a function of time at five different sites. After five years of weathering, the PVC exposed in Germany still has 95% of its original impact strength, whereas the samples exposed in Singapore have less than 5% of their initial strength. The degradation in PVC samples is also accompanied by discoloration as presented in Fig. 10.74 [36]. The figure shows discoloration of white PVC as a function of time at various locations. The samples exposed in Arizona showed significantly higher discoloration than those exposed in Pennsylvania and Florida.







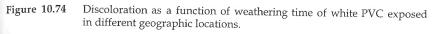




The strength losses and discoloration in a weathering process are mainly attributed to the ultra-violet rays received from sunshine. This can be demonstrated by plotting properties as a function of actual sunshine received instead of time exposed. Figure 10.75 [37] is a plot of percent of initial impact strength for an ABS as a function of total hours of exposure to sun light in three different locations: Florida, Arizona, and West Virginia. The curve reveals the fact that by "normalizing" the curves with respect to exposure to actual sunshine, the three different sites with three completely different weather conditions9 lead to the same relation between impact strength and total sunshine.

9 Florida has a subtropical coastal climate with a yearly rainfall of 952 mm and sunshine of 2750 hours. Arizona has a hot dry climate with 116 mm of rainfall and 3850 hours of sunshine. West Virginia has a milder climate with 992 mm of rainfall and 2150 hours of sunshine [28].

10 Failure and Damage of Polymers 509





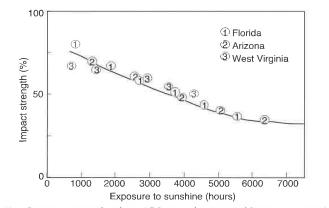


Figure 10.75 Impact strength of an ABS as a function of hours to actual sunshine exposure.

The effect of weathering can often be mitigated with the use of pigments, such as TiO<sub>2</sub> or soot, which absorb ultra violet radiation, making it more difficult to penetrate the surface of a polymer component. The most important one is soot. For example, ABS with white and black pigments exhibit a noticeable improvement in properties after exposure to ultra violet radiation. Figure 10.76 [37] shows the reduction of impact strength in ABS samples as a function of exposure time to sunshine for four pigment concentrations: 0.5%, 0.7%, 1%, and 2%. It is clear that the optimal pigment concentration is around 1%. Beyond 1% of pigmentation there is little improvement in the properties.

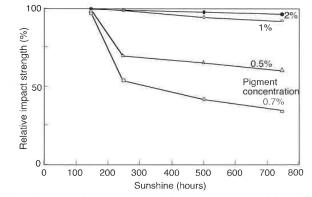
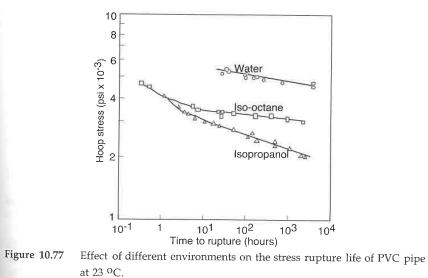


Figure 10.76 Influence of pigment concentration on the impact strength reduction of ABS specimens exposed to weathering.

# 10.8.2 Chemical Degradation

Liquid environments can have positive and negative effects on the properties of polymeric materials. Some chemicals or solvents can have detrimental effects on a polymer component. Figure 10.77 [25] shows results of creep rupture tests done on PVC tubes as a function of the hoop stress. It can be seen that the life span of the tubes in contact with the iso-octane and isopropanol has been significantly reduced as compared to the tubes in contact with water. The measured data for the pipes that contained iso-octane clearly show a slope reduction with a visible endurance limit, making it possible to do long-life predictions. On the other hand, the isopropanol samples do not exhibit such a slope reduction, suggesting that isopropanol is a harmful environment which acts as a solving agent and leads to gradual degradation of the PVC surface.



The question, of whether a chemical is harmful to a specific polymeric material is one that needs to be addressed if the polymer component is to be placed in a possibly threatening environment. Similar to polymer solutions, a chemical reaction between a polymer and another substance is governed by the Gibbs free energy equation, as discussed in Chapter 5. If the change in enthalpy, AH, is negative then a chemical reaction will occur between the polymer and the solvent.



The effect of the solubility parameter of several solvents on the fatigue response of polystyrene samples is presented in Fig. 10.78 [31]. Here, the relation in Eq. 6.24 becomes evident; as the absolute difference between the solubility parameter of polystyrene, which is 9.1  $(cal/cm^3)^{1/2}$ , and the solubility parameter of the solvent decreases, the fatigue life drops significantly.

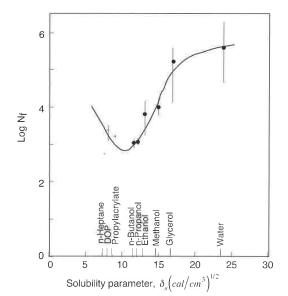


Figure 10.78 Effect of solubility parameter of the surrounding media on the fatigue life of polystyrene specimens.

It should be pointed out again that some substances are more likely to be absorbed by the polymer than others<sup>10</sup>. A polymer that is in a soluble environment is more likely to generate stress cracks and fail. This is illustrated in Fig. 10.79 [38], which shows the strain for crack formation in polyphenylene oxide samples as a function of solubility parameter<sup>11</sup> of various solutions. The specimens in solutions that were  $\pm 1$  (cal/cm<sup>3</sup>)<sup>1/2</sup> away from the solubility parameter of the polymer generated cracks at fairly low strains, whereas those specimens in solutions with a solubility parameter further away from the solubility of the polymer formed crazes at much higher strains.

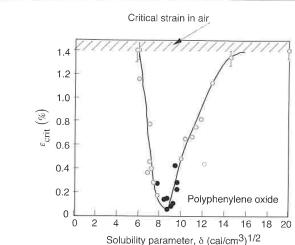


Figure 10.79

Environmental stress cracking or stress corrosion in a polymer component only occurs if crazes or microcracks exist. Hence, stress corrosion in a hostile environment can be avoided if the strain within the component is below the critical strain,  $\varepsilon_{\alpha}$ .

# **10.8.3 Thermal Degradation of Polymers**

Because plastics are organic materials, they are threatened by chain breaking, splitting off of substituents, and oxidation. This degradation generally follows a reaction which can be described by the Arrhenius principle. The period of dwell or residence time permitted before thermal degradation occurs is given by

#### t permi

where  $\Delta$  is the activation energy of the polymer, *R* the gas constant and *T* the absolute temperature.

A material that is especially sensitive to thermal degradation is PVC; furthermore, the hydrogen chloride that results during degradation attacks metal parts. Ferrous metals act as a catalyzer and accelerate degradation.

10 Failure and Damage of Polymers 513

Strains at failure as a function of solubility parameter for polyphenylene oxide specimens: (•) cracking, (O) crazing.

$$u_{ted} \sim \exp\left(\frac{\Delta}{RT}\right)$$
 (10.40)



<sup>10</sup> Please refer to Chapter 13.

<sup>11</sup> Please refer to Chapter 6-

An easy method for determining the flash point of molding batches is by burning the hydrocarbons which are released at certain temperatures. This is shown schematically in Fig. 10.8012 . For PVC one should use a vial with soda lye, instead of a flame, to determine the conversion of chlorine.

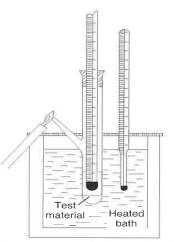


Figure 10.80 Test procedure to determine flash point of polymers.

Thermogravimetry (TGA) is another widely used method to determine the resistance to decomposition or degradation of polymers at high temperatures. For this purpose, the test sample is warmed up in air or in a protective gas while placed on a highly sensitive scale. The change in weight of the test sample is then observed and recorded (see Chapter 3). It is also very useful to observe color changes in a sample while they are heated inside an oven. For example, to analyze the effect of processing additives, polymers are kneaded for different amounts of time, pressed onto a plate, and placed inside a heated oven. The time when a color change occurs is recorded to signify when degradation occurs.

12 Courtesy of BASF.

# Examples

what is the material's fracture toughness ?

We must first compute a/D and read  $\tilde{a}$  from Table 10.6, where D = 10 mm and L = 40 mm. Next we can calculate  $tw\tilde{a}$  ( $Dw\tilde{a}$  for the notation used in Table 10.6), where w = 10 mm. Table 10.10 tabulates all the data.

We can now plot U versus  $Dw\tilde{a}$  and estimate the fracture toughness from the slope, as shown in Fig. 10.82.

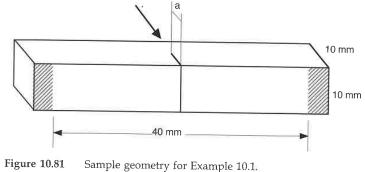


Table 10.	Table 10.10			
a	a/1			
(mm)	_			
1	0.1			
2	0.2			
3	0.3			
4	0.4			
5	0.5			

10 Failure and Damage of Polymers 515

10.1 Charpy Impact tests were performed on PVC samples with crack lengths of 1, 2, 3, 4, and 5 mm. The energy absorbed by the specimen during impact was 0.1, 0.062, 0.046, 0.037 and 0.031 J. The specimen's cross-section was 10 mm x 10 mm, and its length 40 mm. For a PVC modulus of 2 GPa

Tabulated	data	for	Example 10.1	
-----------	------	-----	--------------	--

)	ã	Dwã (m²)	U (J)
	0.781	78.1×10 <sup>-6</sup>	0.1
	0.468	$46.8 \times 10^{-6}$	0.062
	0.354	$35.4 \times 10^{-6}$	0.0465
	0.287	$28.7 \times 10^{-6}$	0.037
	0.233	$23.3 \times 10^{-6}$	0.031



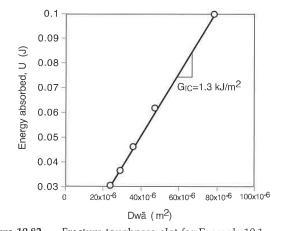


Figure 10.82 Fracture toughness plot for Example 10.1.

We can also compute the critical stress intensity factor  $K_{IC}$  using

 $K_{IC} = \sqrt{EG_{IC}} = 1.61 M N m^{-\frac{3}{2}}$ 

10.2 You are asked to design a cylindrical 200 mm diameter, 5 mm thick polycarbonate pressure vessel, as depicted in Fig. 10.83. To attach a fixture, the pressure vessel has a series of 0.5 mm deep grooves along its length. During its life, the pressure vessel will experience occasional pressure surges. Using the data given below, estimate the critical pressure inside the vessel that will result in fracture.

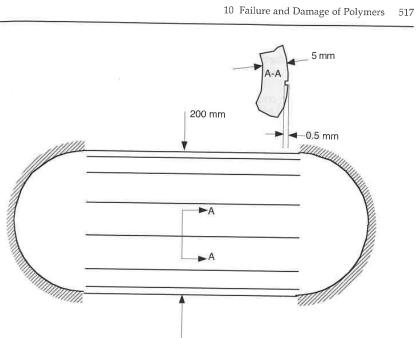
 $G_{IC} = 5 \text{ kJ} / \text{m}^2$ , E = 2.1 GPa, v = 0.33

This problem can be solved using Eq. 10.14

$$G_{lc} = \frac{\pi \sigma_c^2 a}{E} \left(1 - v^2\right)$$

where,  $\sigma_c$  is the hoop stress given by

$$\sigma_c = \frac{p\overline{D}}{2h}$$



using

Problems

Figure 10.83 Pressure vessel geometry for Example 10.2.

Note that since the vessel is axially restricted, the axial stress can be neglected. We can now solve for the pressure that will lead to failure

 $p = \left[\frac{G_{IC}}{\pi a} \frac{4Eh^2}{(1-v^2)\overline{D}^2}\right]^{1/2} = \left[\frac{5 \text{ kJ/m}^2}{\pi (0.5 \text{ mm})} \frac{4(2.1 \text{ GPa})(5 \text{ mm})^2}{(1-.33^2)(197.5 \text{ mm})^2}\right]^{1/2} = 4.39 \text{MPa} (645 \text{ psi})$ 

10.1 Is polystyrene an appropriate material to use for safety goggles? Why?

10.2 A high impact strength polycarbonate has a stress intensity factor,  $K_{lc}$ , of 2.6 MN/m<sup>3/2</sup>, and a strain toughness,  $G_{lc}$  of 5.0 kJ/m<sup>2</sup>. The polycarbonate will be used to assemble a hockey face guard. The face guard will fit onto the helmet using several snap-fits located on the helmet. This requires



1.5 mm deep grooves on the polycarbonate face guard. What maximum stresses will you be able to subject the face guard in the region of the grooves.

- 10.3 Someone in your company designed high-density polyethylene water pipes to transport cold and hot water at pressures of 1.5 bar. The hot water will be at 50 °C, and you can assume the cold water to be at room temperature. The pipe's inner diameter is 50 mm with a wall thickness of 1 mm. Would you approve this product with a 5 year warranty for the above specifications? Why?
- 10.4 A PS-HI test specimen with a 20 mm x 1 mm cross-section and 2 mm long central crack is carrying a 100 N load. Plot the stress distribution near. but not at the crack tip.
- 10.5 A PS component with 0.5 mm long crazes is being stressed between -5 MPa and +5MPa. At what rate is the length of the crazes growing? Estimate the number of cycles to failure.
- 10.6 A creeping PS component loaded to a stress of 2 MPa is showing the formation of small crazes that measure approximately 200 µm. Estimate the time it takes for the crazes to grow to a length of 500  $\mu$ m. Use m = 7and m = 25.

#### References

- 1. Crawford, R.J., Plastics Engineering, 2nd, Ed., Pergamon Press, (1987).
- 2. Kinloch, A.J., Young, R.J., Fracture Behavior of Polymers, Applied Science Publishers, London, (1983).
- 3. Griffith, A.A., Phil. Trans. Roy. Soc., A221, 163, (1920).
- 4. Rice, J.R., J. Appl. Mech., 35, 379, (1965).
- Vincent, P.I., Plastics, 29, 79 (1964). 5.
- Beahan, P., Bevis, M., and Hull, D., Phil. Mag., 24, 1267, (1971).
- Menges, G., Werkstoffkunde der Kunststoffe, 2nd Ed., Hanser Publishers, Munich, 7. (1984).
- 8. Nicolay, Ph.D. Thesis, IKV, RWTH-Aachen, (1976).
- 9. Menges, G., and Alf, E., Kunststoffe, 62, 259, (1972).
- 10. Schultz, J.M., Polymer Materials Science, Prentice-Hall, Englewood Cliffs, N.J., (1974).
- 11. Ehrenstein, G.W., Polymeric Materials, Hanser Publishers, Munich, (2001).
- 12. Engel, L., Klingele, H., Ehrenstein, G.W., and Schaper, H., An Atlas of Polymer Damage, Hanser Publishers, Munich, (1978).
- 13. Roskothen, H.J., Ph.D. Thesis, IKV, RWTH-Aachen, (1974).
- 14. Boyer, R.F., Polymer Eng. Sci., 8, 161, (1968).

- 15. Boden, H.E., Ph.D. Thesis, IKV, RWTH-Aachen, Germany, (1983).
- 16. Menges, G., and Boden, H.-E., Failure of Plastics, Chapter 9, Eds. W. Brostow, and R.D. Corneliussen, Hanser Publishers, Munich, (1986).
- 17. Andrews, E.H., Fracture in Polymers, Oliver and Body, London, (1968). 18. Rest, H., Ph.D. Thesis, IKV-Aachen, (1984).
- 20. Plati, E. and Williams, J.G., Polym. Eng. Sci., 15, 470, (1975).
- 21. Crawford, R.J., and Benham, P.P., Polymer, 16, 908, (1975).
- 23. Gaube, E. and Kausch, H.H., Kunststoffe, 63, 391, (1973).

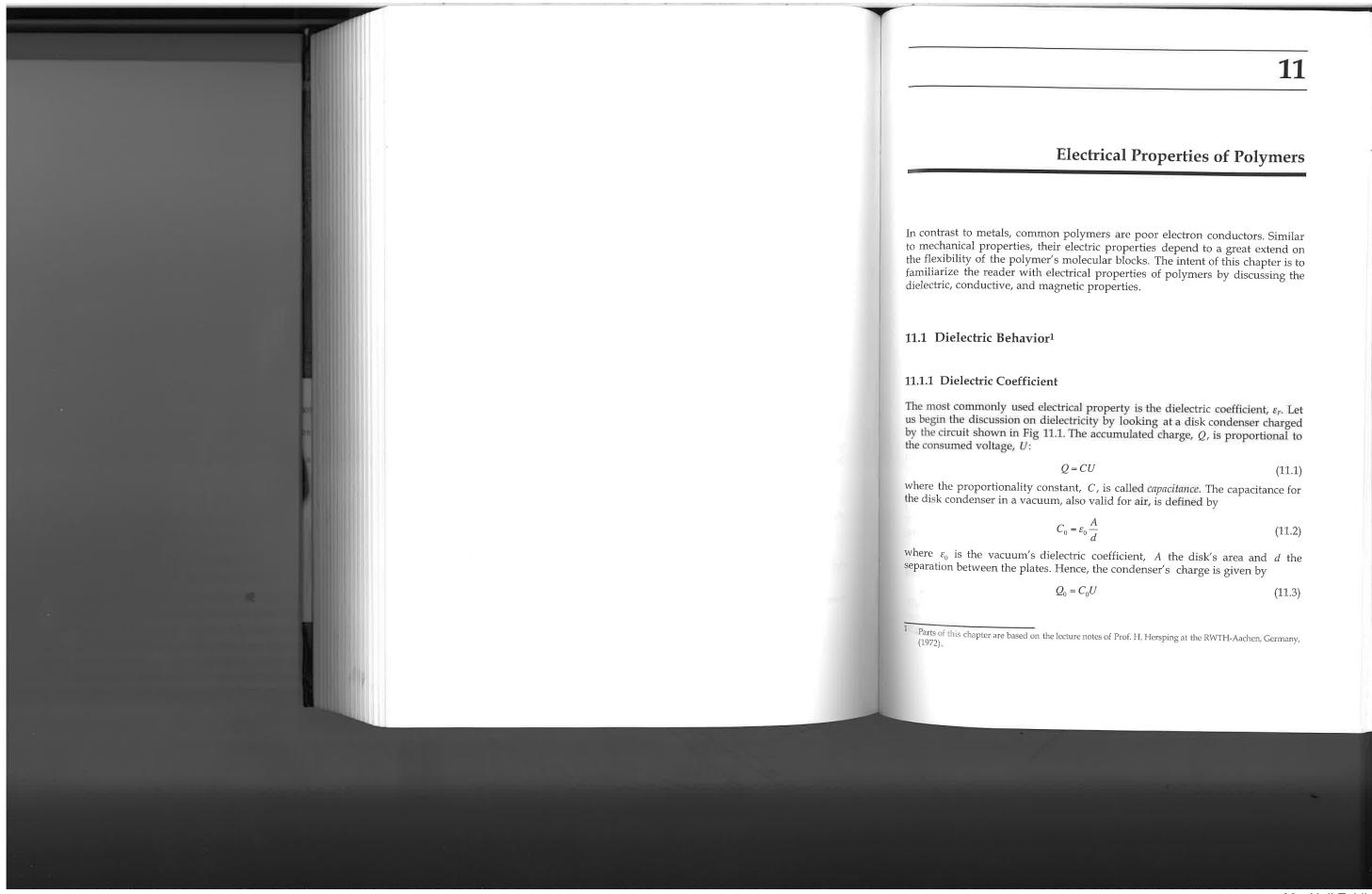
  - 24. Bannantine, J.A., Comer, J.J., and Handrock, J.L., Fundamentals of Metal Fatigue Analysis, Prentice Hall, Englewood Cliffs, (1990). 25. Riddell, M.N., Plast. Eng., 40, 4, 71, (1974).

  - (1972).
  - 28. Owen, M.J., Smith, T.R., and Dukes, R., Plast. Polym., 37, 227, (1969). 29. Hertzberg, R.W., and Manson, J.A., Fatigue of Engineering Plastics, Academic
  - Press, New York, (1980).
  - Fiberglas Corp., (1979).
- 31. Hertzberg, R.W., Manson, J.A., and Skibo, M.D., Polym. Eng. Sci., 15, 252, (1975). 32. Domininghaus, H., Plastics for Engineers, Hanser Publishers, Munich, (1993). 33. Dolfen, E., Ph.D. Thesis, IKV, RWTH-Aachen, (1978). 34. Menges, G., Wekstoffkunde Kunststoffe, Hanser Publishers, Munich, (1990). 35. Engel, L., Klingele, H., Ehrenstein, G.W., and Schaper, H., An Atlas of Polymer
- Damage, Hanser Publishers, Munich, (1978).
- London, (1983).
- 37. Ruhnke, G.M. and Biritz, L.F., Kunststoffe, 62, 250, (1972). 38. Bernier, G.A., and Kambour, R.P., Macromolecules,1,393, (1968).

10 Failure and Damage of Polymers 519

- 19. ASTM, Vol .08.01, Plastics (I): C 177-D 1600, ASTM-D 256, 58-74, (1991).
- 22. Richard, K., Gaube, E., and Diedrich, G., Kunststoffe, 49, 516, (1959).
- 26. Kleinemeier, B., Ph.D. Thesis, IKW-Aachen, Germany, (1979).
- 27. Bucknall, C.B., Gotham, K.V., and Vincent, P.I., Polymer Science. A Materials Handbook, Ed. A.D. Jenkins, Vol. 1, Chapter 10, American Elsevier, New York,
- 30. Denton, D.L., The Mechanical Properties of an SMC-R50 Composite, Owens-Corning
- 36. Davis, A. and Sims, D., Weathering of Polymers, Applied Science Publishers,





$$Q = CU \tag{11.1}$$

$$C_0 = \varepsilon_0 \frac{A}{d} \tag{11.2}$$

$$Q_0 = C_0 U \tag{11.3}$$

If we replace the vacuum or air between the disks of the condenser by a real dielectric, the charge increases, for the same voltage U, by the factor  $\varepsilon_{\epsilon}$ represented by

$$Q = \varepsilon_r Q_0 \tag{11.4}$$

and the capacity changes to

 $C = \varepsilon_r C_0 = \varepsilon_r \varepsilon_0 \frac{A}{d}$ (11.5)

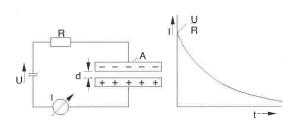


Figure 11.1 Condenser circuit used to measure capacitance properties.

The constant  $\varepsilon_r$  is often called the *relative dielectric coefficient*. It is dimensionless, and it is dependent on the material, temperature, and frequency. However, the charge changes when a dielectric material is inserted between the plates. This change in charge is due to the influence of the electric field developing polarization charges in the dielectric. This is more clearly represented in Fig. 11.2. The new charges that develop between the condenser's metal disks are called  $Q_p$ . Hence, the total charge becomes

$$Q = Q_0 + Q_\mu \tag{11.6}$$

In general terms, the charge is expressed per unit area as

A

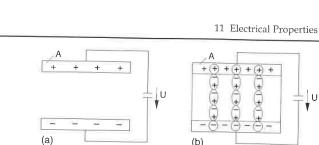
$$=\frac{Q_0}{A} + \frac{Q_p}{A} = D \tag{11.7}$$

where *D* is the total charge per unit area. Introducing the *electric field intensity*, *E*, Eq. 11.2 can be rewritten as

$$E = \frac{U}{d} = \frac{1}{\varepsilon_0} \frac{Q_0}{A} = \frac{1}{\varepsilon_0 \varepsilon_r} \frac{Q}{A}$$
(11.8)

which results in

$$\frac{Q_0}{A} = \varepsilon_0 E \tag{11.9}$$



If the charged condenser is separated from the voltage source beforehand, the voltage of the condenser will decrease with insertion of a dielectric. Thus, the inserted dielectric also increases the capacity of the condenser. Let us define the charge density of the polarization surface as

This causes the total charge per unit area to become

which can be rewritten as

No field can develop within metallic condenser plates because of the high electric conductivity. Therefore, using the dielectric charge density per unit area, Eqs. 11.7 and 11.8 can be combined to give

Substituting this result into Eq. 11.12, we get

or

 $P = \varepsilon_0$ 

The factor  $\chi$  is generally referred to as *dielectric susceptibility*. It is a measurement of the ability of a material to be a polarizer.

Table 11.1 lists the relative dielectric coefficients of important polymers. The measurements were conducted using the standard test DIN 53 483 in condensers of different geometries which, in turn depended on the sample type. The ASTM standard test is described by ASTM D150. Figures 11.3 [1] and 11.4 [1]

11 Electrical Properties of Polymers 523

**Figure 11.2** Polarization charges a) without a dielectric, b) with a dielectric.

$$P = \frac{Q_p}{A} \tag{11.10}$$

$$D = \varepsilon_0 E + P \tag{11.11}$$

$$P = D - \varepsilon_0 E \tag{11.12}$$

$$D = \varepsilon_0 \varepsilon_r E \tag{11.13}$$

$$=\varepsilon_0\varepsilon_r E - \varepsilon_0 E \tag{11.14}$$

$$\int \left[\varepsilon_{r_{0}} - 1\right] E = \varepsilon_{0} \chi E \tag{11.15}$$



MacNeil Exhibit 2117 Yita v. MacNeil IP, IPR2020-01139 Page 272

present the dielectric coefficient for selected polymers as a function of temperature and frequency, respectively.

# Table 11.1 Relative Dielectric Coefficient, ε<sub>r</sub>, of Various Polymers [Hersping]

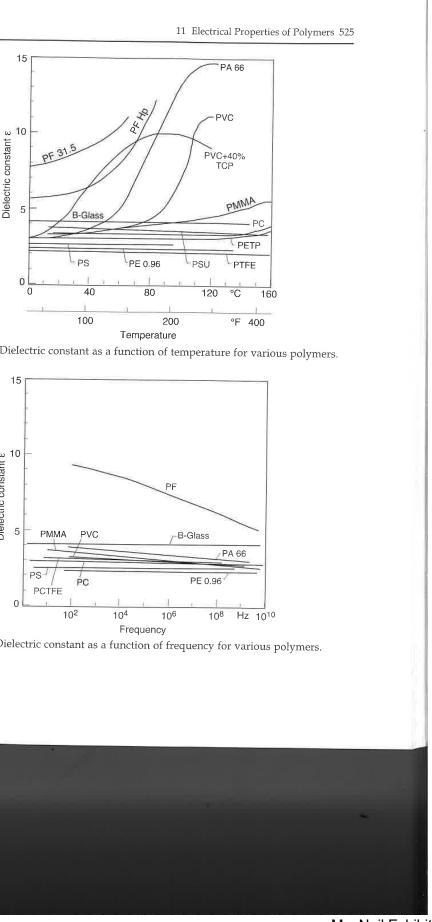
Polymer	Relative dielectric coefficient, $\varepsilon_r$	
	800 Hz	10 <sup>6</sup> Hz
Expanded polystyrene	1.05	1.05
Polytetrafluoroethylene	2.05	2.05
Polyethylene (density dependent)	2.3-2.4	2.3-2.4
Polystyrene	2.5	2.5
Polypropylene	2.3	2.3
Polyphenyleneether	2.7	2.7
Polycarbonate	3.0	3.0
Polyethyleneterephthalate	3.0-4.0	3.0-4.0
ABS	4.6	3.4
Celluloseacetate, type 433	5.3	4.6
Polyamide 6	3.7-7.0	
(moisture content dependent)		
Polyamide 66	3.6-5.0	
(moisture content dependent)		
Epoxy resin (unfilled)		2.5-5.4
Phenolic type 31.5	6.0-9.0	6.0
Phenol type 74	6.0-10.0	4.0-7.0
Urea type 131.5	6.0-7.0	6.0-8.0
Melamine type 154	5.0	10.0

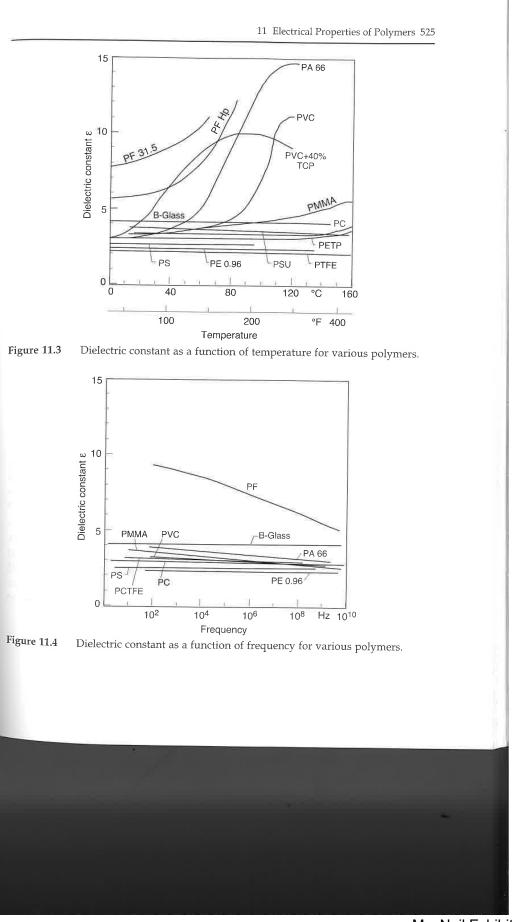
# 11.1.2 Mechanisms of Dielectrical Polarization

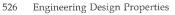
The two most important molecular types for the polarization of a dielectric in an electric field are displacement polarization and orientation polarization.

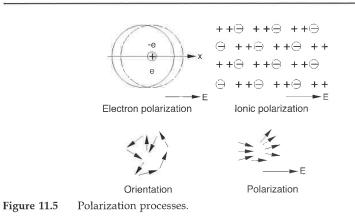
Under the influence of an electric field, the charges deform in field direction by aligning with the atomic nucleus (electron polarization) or with the ions (ionic polarization). This is usually called *displacement polarization* and is clearly demonstrated in Fig. 11.5.

Because of their structure, some molecules possess a dipole moment in the spaces that are free of an electric field. Hence, when these molecules enter an electric field, they will orient according to the strength of the field. This is generally referred to as orientation polarization and is schematically shown in Fig. 11.5.









It takes some time to displace or deform the molecular dipoles in the field direction and even longer time for the orientation polarization. The more viscous the surrounding medium is, the longer it takes. In alternating fields of high frequency, the dipole movement can lag behind at certain frequencies. This is called dielectric relaxation, which leads to dielectric losses that appear as dielectric heating of the polar molecules.

In contrast to this, the changes in the displacement polarization happen so quickly that it can even follow a lightwave. Hence, the refractive index, n, of light is determined by the displacement contribution,  $\varepsilon_v$ , of the dielectric constant<sup>2</sup>. The relation between n and  $\varepsilon_v$  is given by

$$n = \sqrt{\varepsilon_v} \tag{11.16}$$

Hence, we have a way of measuring polarization properties since the polarization of electrons determines the refractive index of polymers. It should be noted that ion or molecular segments of polymers are mainly stimulated in the middle of the infrared spectrum.

A number of polymers have permanent dipoles. The best known polar polymer is polyvinyl chloride, and C=O groups also represent a permanent dipole. Therefore, polymers with that kind of building block suffer dielectric losses in alternating fields of certain frequencies. For example, Fig. 11.6 shows the frequency dependence of susceptibility.

<sup>2</sup> For a more in-depth coverage of optical properties the reader is referred to Chapter 11 of this book.

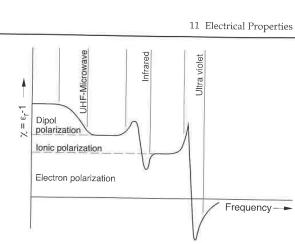


Figure 11.6 Frequency dependence of different polarization cases.

In addition, the influence of fillers on the relative dielectric coefficient is of considerable practical interest. The rule of mixtures can be used to calculate the effective dielectric coefficient of a matrix with assumingly spherically shaped fillers as

```
\mathcal{E}_{\rm eff} = \mathcal{E}_{\rm matrix}
```

Materials with air entrapments such as foams, have a filler dielectric coefficient of  $\varepsilon_{air} = 1$ ; thus, the effective dielectric coefficient of the material reduces to

$$\varepsilon_{\text{foam}} = \varepsilon_{\text{matrix}} \left( 1 - 3\phi \frac{\varepsilon_{\text{matrix}} - 1}{2\varepsilon_{\text{matrix}} + 1} \right)$$
(11.18)

#### $\mathcal{E}_{\rm eff}$

Whether a molecule is stimulated to its resonant frequency in alternating fields or not depends on its relaxation time. The relaxation time, in turn, depends on viscosity,  $\eta$ , temperature, T, and radius, r, of the molecule. The following relationship can be used:

11 Electrical Properties of Polymers 527

$$\left(1 - 3\phi \frac{\varepsilon_{\text{matrix}} - \varepsilon_{\text{filler}}}{2\varepsilon_{\text{matrix}} + \varepsilon_{\text{filler}}}\right)$$
(11.17)

and, for metal fillers where  $\varepsilon_{mend} = \infty$ , it can be written as

$$=\varepsilon_{\text{matrix}}\left(1+3\phi\right) \tag{11.19}$$

$$\lambda_{m} \sim \frac{\eta r^{3}}{T} \tag{11.20}$$



The parameter  $\lambda_m$  is the time a molecule needs to move back to its original shape after a small deformation. Hence, the resonance frequency,  $f_m$ , can be computed using

$$f_m = \frac{\omega_m}{2\pi} = \frac{1}{2\pi\lambda_m}$$
(11.21)

### 11.1.3 Dielectric Dissipation Factor

The movement of molecules, for example, during dipole polarization or ion polarization in an alternating electric field, leads to internal friction and, therefore, to the heating of the dielectric. The equivalent circuit shown in Fig. 11.7 is used here to explain this phenomenon. Assume an alternating current is passing through this circuit, with the effective value of U volts and an angular frequency  $\omega$  defined by

$$\omega = 2\pi f \tag{11.22}$$

where f is the frequency in Hz. Through such a system, a complex current  $I^*$  will flow, composed of a resistive or loss component,  $I_{r}$ , and of a capacitive component,  $I_e$ . The vector diagram in Fig. 11.8 shows that with

$$I_{e} = U/R \tag{11.23}$$

and

$$= \omega C U \tag{11.24}$$

we can write

$$= U/R + i\omega CU \tag{11.25}$$

Here, *i* represents an imaginary component oriented in the imaginary axis of the vector diagram in Fig. 11.8. An alternating current applied to a condenser free of any current loss components would result in

I

$$\frac{I_r}{I_c} = \tan \delta \to 0 \tag{11.26}$$

In such a case, the condenser current is purely capacitive, which leads to no losses at all. This results in a voltage that is lagging the current by 90°, as demonstrated in Fig. 11.9. Accordingly, capacitance also consists of a real component and an imaginary component.

**Period = 360°** ure 11.9 Current and voltag a) Without dielect displaced by the p

If the condenser has losses, when  $\tan \delta > 0$ , a resistive current  $I_{i}$  is formed which leads to a heating energy rate in the dielectric of

 $E_h$ 

where  $I_{eff}$  represents the total current or the magnitude of the vector in Fig. 11.8. Using Eq. 11.25 for capacitance leads to

11 Electrical Properties of Polymers 529

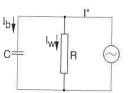


Figure 11.7 Equivalent circuit diagram for the losses in a dielectric.

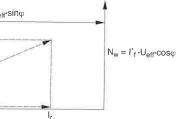
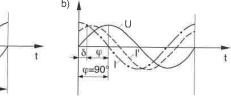


diagram or power-indicator diagram of electric alter-



**Figure 11.9** Current and voltage in a condenser.  $I \equiv$  current,  $U \equiv$  voltage,  $t \equiv$  time a) Without dielectric losses (ideal condition), current and voltage are displaced by the phase angle  $\varphi = 90^{\circ}$  or  $\pi/2$ ; b) With dielectric loss, the current curve I' is delayed by the loss angle  $\delta$ .

$$=\frac{1}{2}UI_{\rm eff}\tan\delta\tag{11.27}$$



$$C^{*} = C' - \frac{1}{R\omega} = C' - iC''$$
(11.28)

where  $C^*$  is the complex capacitance, with C' as the real component defined by

$$C' = \varepsilon_0 \varepsilon'_r \frac{A}{d} \tag{11.29}$$

and C'' as the imaginary component described by

$$C'' = \frac{1}{R\omega} = \varepsilon_0 \varepsilon_r'' \frac{A}{d}.$$
 (11.30)

Using the relationship in Eq. 11.5 we can write

$$C^* = C_0(\varepsilon_r' - i\varepsilon_r'') = C_0\varepsilon_r^*$$
(11.31)

where  $\varepsilon_r^*$  is called the *complex dielectric coefficient*. According to Eqs. 11.25 and 11.31, the phase angle difference or *dielectric dissipation factor* can be defined by

$$\tan \delta = \frac{I_r}{I_c} = \frac{\varepsilon_r''}{\varepsilon_r'} \tag{11.32}$$

If we furthermore consider that electric conductivity is determined by

$$\sigma = \frac{1}{R} \frac{d}{A} \tag{11.33}$$

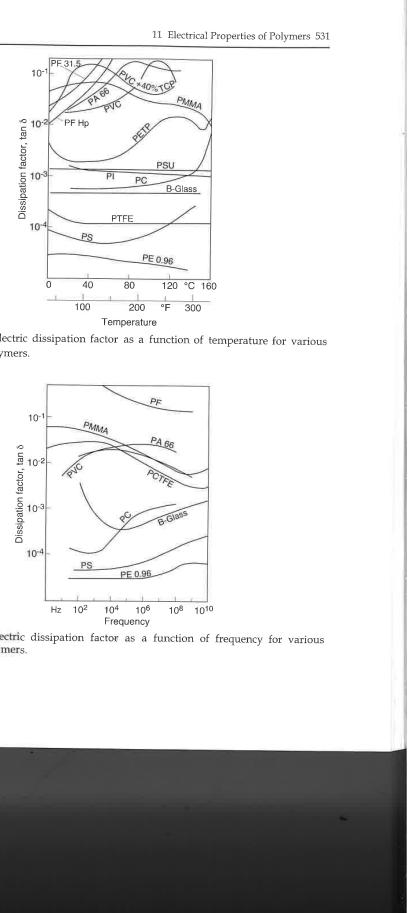
then the imaginary component of the complex dielectric coefficient can be rewritten as

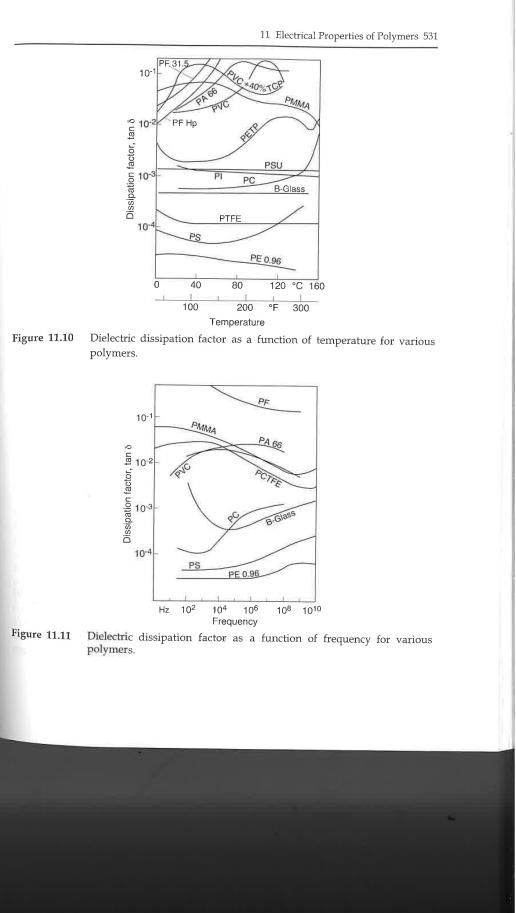
$$t' = \frac{\sigma}{\omega\varepsilon_0} = \varepsilon'_r \tan\delta \tag{11.34}$$

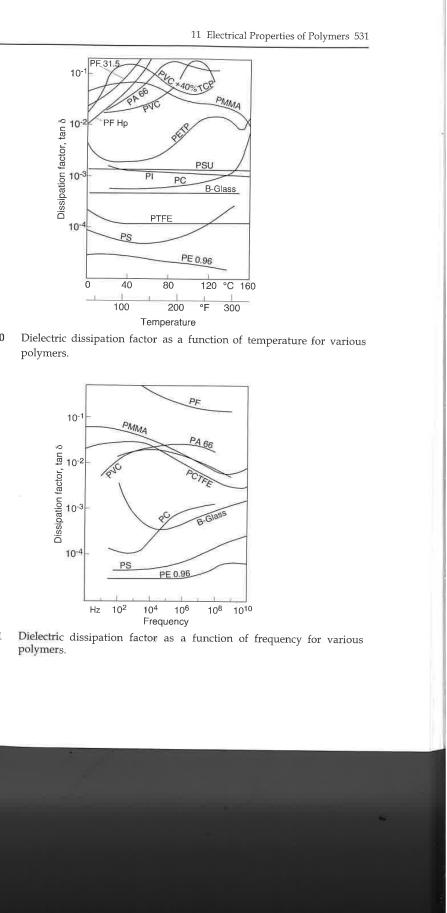
Typical ranges for the dielectric dissipation factor of various polymer groups are shown in Table 11.2. Figures 11.10 [1] and 11.11 [1] present the dissipation factor tan  $\delta$  as a function of temperature and frequency, respectively.

**Table 11.2** Dielectric Dissipation Factor  $(\tan \delta)$  for Varoius Polymers

Material	$tan \delta$	
Non-polar polymers (PS, PE, PTFE)	< 0.0005	
Polar polymers (PVC and others)	0.001-0.02	
Thermoset resins filled with glass, paper, cellulose	0.02-0.5	









MacNeil Exhibit 2117 Yita v. MacNeil IP, IPR2020-01139 Page 276

#### 11.1.4 Implications of Electrical and Thermal Loss in a Dielectric

The electric losses through wire insulation running high frequency currents must be kept as small as possible. Insulators are encountered in transmission lines or in high-frequency fields such as the housings of radar antennas. Hence, we would select materials which have low electrical losses for these types of applications.

On the other hand, in some cases we want to generate heat at high frequencies. Heat sealing of polar polymers at high frequencies is an important technique used in the manufacturing of soft PVC sheets such as the ones encountered in automobile vinyl seat covers.

To assess whether a material is suitable for either application, one must know the loss properties of the material and calculate the actual electrical loss. To do this, we can rewrite Eq. 11.27 as

$$E_{h} = U^{2}\omega C \tan\delta \tag{11.35}$$

or as

$$E_{h} = 2\pi f U^{2} d^{2} \varepsilon_{0} \varepsilon_{r}^{\prime} \tan \delta C_{0}$$
(11.36)

The factor that is dependent on the material and indicates the loss is the loss *factor*  $\varepsilon'_r \tan \delta$ , called  $\varepsilon''_r$  in Eq. 11.34. As a rule, the following should be used:

 $\varepsilon'_{c} \tan \delta < 10^{-3}$  for high-frequency insulation applications, and

#### $\varepsilon'_r \tan \delta > 10^{-2}$ for heating applications.

In fact, polyethylene and polystyrene are perfectly suitable as insulators in high-frequency applications. To measure the necessary properties of the dielectric, the standard DIN 53 483 and ASTM D 150 tests are recommended.

### **11.2** Electric Conductivity

#### 11.2.1 Electric Resistance

The current flow resistance, R, in a plate-shaped sample in a direct voltage field is defined by Ohm's law as

$$R = \frac{U}{I} \tag{11.37}$$

the conductance, G,

or by

and the conductivity as the inverse of the specific resistance,  $\rho$ ,

The simple relationship found in Eq. 11.37-39 is seldom encountered since the voltage, U, is rarely steady and usually varies in cyclic fashion between  $10^{-1}$  to 10<sup>11</sup> Hz [2].

Current flow resistance is called volume conductivity and is measured one minute after direct voltage has been applied using the DIN 53 482 standard test. The time definition is necessary, because the resistance decreases with polarization. For some polymers we still do not know the final values of resistance. However, this has no practical impact, since we only need relative values for comparison. Figure 11.12 compares the specific resistance,  $\rho$ , of various polymers and shows its dependence on temperature. Here, we can see that similar to other polymer properties, such as the relaxation modulus, the specific resistance not only decreases with time but also with temperature.

The surface of polymer parts often shows different electric direct-current resistance values than their volume. The main cause is from surface contamination (e.g., dust and moisture). We therefore have to measure the surface resistance using a different technique. One common test is DIN 53 482, which uses a contacting sample. Another test often used to measure surface resistance is DIN 53 480. With this technique, the surface resistance is tested between electrodes placed on the surface. During the test, a saline solution is dripped on the electrodes causing the surface to become conductive, thus heating up the surface and causing the water to evaporate. This leads not only to an increased artificial contamination but also to the decomposition of the polymer surface. If during this process conductive derivatives such as carbon form, the conductivity quickly increases to eventually create a short circuit. Polymers that develop only small traces of conductive derivatives are considered resistant. Such polymers are polyethylene, fluoropolymers, and melamines.

11 Electrical Properties of Polymers 533

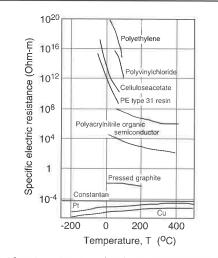
$$R = \frac{1}{\sigma} \frac{d}{A} \tag{11.38}$$

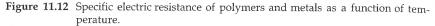
where  $\sigma$  is known as the conductivity and d and A are the sample's thickness and surface area, respectively. The resistance is often described as the inverse of

$$R = \frac{1}{G} \tag{11.39}$$

$$\sigma = \frac{1}{\rho} \tag{11.40}$$





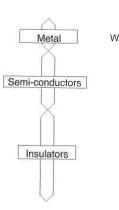


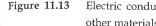
#### **11.2.2** Physical Causes of Volume Conductivity

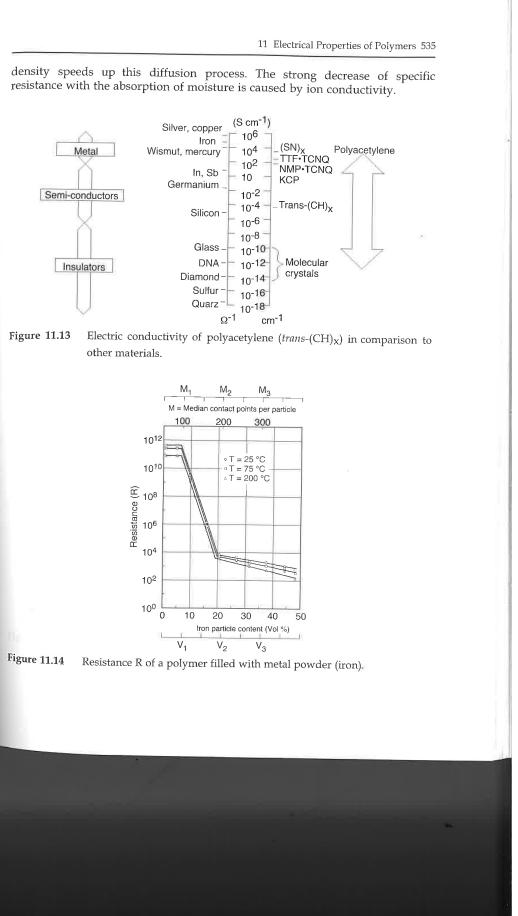
Polymers with a homopolar atomic bond, which leads to pairing of electrons. do not have free electrons and are not considered to be conductive. Conductive polymers-still in the state of development-in contrast, allow for movement of electrons along the molecular cluster, since they are polymer salts. The classification of these polymers with different materials is given in Fig. 11.13.

Potential uses of electric conductive polymers in electrical engineering include flexible electric conductors of low density, strip heaters, anti-static equipment, high-frequency shields, and housings. In semi-conductor engineering, some applications include semi-conductor devices (Schottky-Barriers) and solar cells. In electrochemistry, applications include batteries with high energy and power density, electrodes for electrochemical processes, and electrochrome instruments.

Because of their structure, polymers cannot be expected to conduct ions. Yet the extremely weak electric conductivity of polymers at room temperature and the fast decrease of conductivity with increasing temperatures is an indication that ions do move. They move because engineering polymers always contain a certain amount of added low-molecular constituents which act as moveable charge carriers. This is a diffusion process which acts in field direction and across the field. The ions "jump" from potential hole to potential hole as activated by higher temperatures (Fig. 11.12). At the same time, the lower







MacNeil Exhibit 2117 Yita v. MacNeil IP, IPR2020-01139 Page 278

Conducting polymers are useful for certain purposes. When we insulate high-energy cables, for example, as a first transition layer we use a polyethylene filled with conductive filler particles such as soot. Figure 11.14 demonstrates the relationship between filler content and resistance. When contact tracks develop, resistance drops spontaneously. The number of interparticle contacts, M, determines the resistance of a composite. At  $M_1$  or M=1there is one contact per particle. At this point, the resistance starts dropping, When two contacts per particle exist, practically all particles participate in setting up contact and the resistance levels off. The sudden drop in the resistance curve indicates why it is difficult to obtain a medium specific resistance by filling a polymer.

Figure 11.15 [3] presents the resistance in metal flakes or powder filled epoxy resins. The figure shows how the critical volume concentration for the epoxy systems filled with copper or nickel flakes is about 7% concentration of filler, and the critical volume concentration for the epoxy filled with steel powder is around 15%.

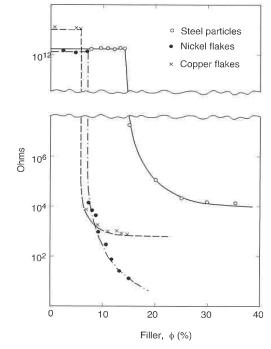
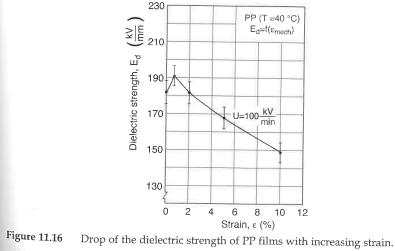


Figure 11.15 Resistance in metal flakes and powder filled epoxy resins.

# **11.3 Application Problems**

### 11.3.1 Electric Breakdown

Since the electric breakdown of insulation may lead to failure of an electric component or may endanger people handling the component, it must be prevented. Hence, we have to know the critical load of the insulating material to design the insulation for long continuous use and with a great degree of confidence. One of the standard tests used to generate this important material property data for plate or block-shaped specimens is DIN 53 481. This test neglects the effect of material structure and of processing conditions. From the properties already described, we know that the electric breakdown resistance or dielectric strength must depend on time, temperature, material condition, load application rate, and frequency. It is furthermore dependent on electrode shape and sample thickness. In practice, however, it is very important that the upper limits measured on the experimental specimens in the laboratory are never reached. The rule of thumb is to use long-term load values of only 10% of the short-term laboratory data. Experimental evidence shows that the *dielectric* strength decreases as soon as crazes form in a specimen under strain and continues to decrease with increasing strain. This is demonstrated in Fig 11.16 [4].



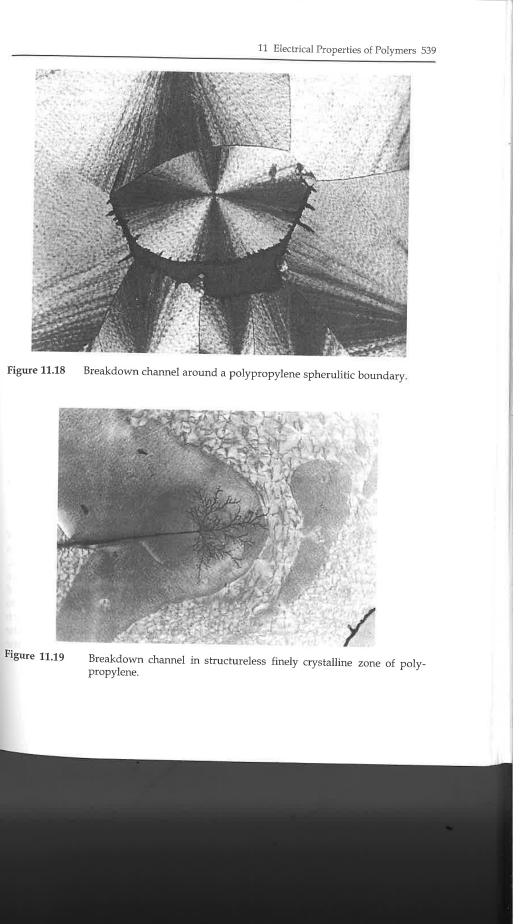
11 Electrical Properties of Polymers 537

MacNeil Exhibit 2117 Yita v. MacNeil IP, IPR2020-01139 Page 279

On the other hand, Fig. 11.17 [4] demonstrates how the dielectric dissipation factor, tan  $\delta$ , rises with strain. Hence, one can easily determine the beginning of the viscoelastic region (begin of crazing) by noting the starting point of the change in tan  $\delta$ . It is also known that amorphous polymers act more favorably to electric breakdown resistance than partly crystalline polymers. Semicrystalline polymers are more susceptible to electric breakdown as a result of breakdown along inter-spherulitic boundaries as shown in Fig. 11.18 [5]. Longterm breakdown of semi-crystalline polymers is either linked to "treeing," as shown in Fig. 11.19, or occurs as a heat breakdown, burning a hole into the insulation, such as the one in Fig. 11.18. In general, with rising temperature and frequency, the dielectric strength continuously drops.

Insulation materials- mostly LDPE- are especially pure and contain voltage stabilizers. These stabilizers are low-molecular cyclic aromatic hydrocarbons. Presumably, they diffuse into small imperfections or failures, fill the empty space and thereby protect them from breakdown.

Table 11.3 [6] gives dielectric strength and resistivity for selected polymeric materials.



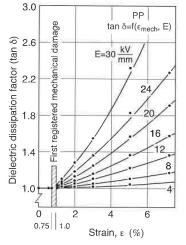
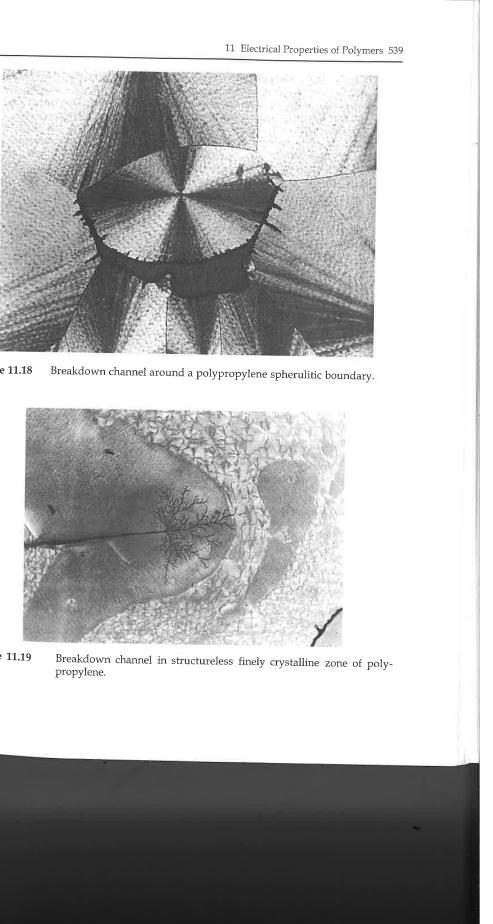


Figure 11.17 Increase of dielectric dissipation with increased strain in PP foils.



MacNeil Exhibit 2117 Yita v. MacNeil IP, IPR2020-01139 Page 280

 Table 11.3
 Dielectric Strength and Resistivity for Selected Polymers

Polymer	Dielectric strength MV/m	Resistivity Ohm-m
ABS	25	10 <sup>14</sup>
Acetal (homopolymer)	20	1013
Acetal (copolymer) acrylic	20	10 <sup>13</sup>
Acrylic	11	1013
Cellulose acetate	11	10 <sup>9</sup>
CAB	10	109
Ероху	16	1013
Modified PPO	22	1015
Nylon 66	8	1013
Nylon 66 + 30% GF	15	1012
PEEK	19	$10^{14}$
PET	17	1013
PET + 36% GF	50	$10^{14}$
Phenolic (mineral filled)	12	109
Polycarbonate	23	1015
Polypropylene	28	1015
Polystyrene	20	10 <sup>14</sup>
LDPE	27	10 <sup>14</sup>
HDPE	22	10 <sup>15</sup>
PTFE	45	10 <sup>16</sup>
uPVC	14	1012
pPVC	30	10 <sup>11</sup>
SAN	25	1014

### 11.3.2 Electrostatic Charge

An electrostatic charge is often a result of the excellent insulation properties of polymers- the very high surface resistance and current-flow resistance. Since polymers are bad conductors, the charge displacement of rubbing bodies, which develops with mechanical friction, cannot equalize. This charge displacement results from a surplus of electrons on one surface and a lack of electrons on the other. Electrons are charged positively or negatively up to hundreds of volts. They release their surface charge only when they touch another conductive body or a body which is inversely charged. Often the discharge occurs without contact, as the charge arches through the air to the close-by conductive or inversely charged body, as demonstrated in Fig. 11.20.

The currents of these breakdowns are low. For example, there is no danger when a person suffers an electric shock caused by a charge from friction of synthetic carpets or vinyls. There is danger of explosion, though, when the sparks ignite flammable liquids or gases.

	- 1-	
	- h	-(
	一日	~
	- F	S
	-11	100
	네는	-74
	- P	/
	-1-	~ 6
		-21
	-1-	-
	-14	-

~	-
	-

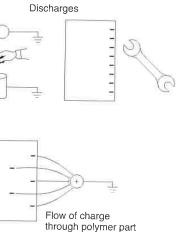
Figure 11.20 Electrostatic charges in polymers.

As the current-flow resistance of air is generally about  $10^9 \ \Omega cm$ , charges and flashovers only occur if the polymer has a current-flow resistance of  $>10^9$  to  $10^{10} \ \Omega cm$ . Another effect of electrostatic charges is that they attract dust particles on polymer surfaces.

Electrostatic charges can be reduced or prevented by the following means:

- using conductive fillers such as graphite.
- over time.
- radiation.

11 Electrical Properties of Polymers 541



- Reduce current-flow resistance to values of  ${<}10^9~\Omega{\rm cm},$  for example, by

· Make the surfaces conductive by using hygroscopic fillers that are incompatible with the polymer and surface. It can also be achieved by mixing-in hygroscopic materials such as strong soap solutions. In both cases, the water absorbed from the air acts as a conductive layer. It should be pointed out that this treatment loses its effect over time. Especially, the rubbing in of hygroscopic materials has to be repeated

• Reduce air resistance by ionization through discharge or radioactive



### 11.3.3 Electrets

An electret is a solid dielectric body that exhibits permanent dielectric polarization. One can manufacture electrets out of some polymers when they are solidified under the influence of an electric field, when bombarded by electrons, or sometimes through mechanical forming processes.

Applications include films for condensers (polyester, polycarbonate, or fluoropolymers).

### 11.3.4 Electromagnetic Interference Shielding (EMI Shielding)

Electric fields surge through polymers as shown schematically in Fig. 11.20. Since we always have to deal with the influence of interference fields, signalsensitive equipment such as computers cannot operate in polymer housings. Such housings must therefore have the function of Faradayic shields. Preferably, a multilayered structure is used - the simplest solution is to use one metallic layer. Figure 11.21 classifies several materials on a scale of resistances. We need at least  $10^2 \Omega$ cm for a material to fulfill the shielding purpose. With carbon fibers or nitrate coated carbon fibers used as a filler, one achieves the best protective properties. The shielding properties are determined using the standard ASTM ES 7-83 test.

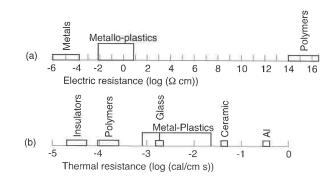


Figure 11.21

Comparison of conductive polymers with other materials: a) Electric resistance  $\rho$  of metal-plastics compared to resistance of metals and polymers b) Thermal resistance  $\lambda$  of metal-plastics compared to other materials

### **11.4 Magnetic Properties**

External magnetic fields have an impact on substances which are subordinate to them because the external field interacts with the internal fields of electrons and atomic nuclei.

## 11.4.1 Magnetizability

Pure polymers are diamagnetic; that is, the external magnetic field induces magnetic moments. However, permanent magnetic moments, which are induced on ferromagnetic or paramagnetic substances, do not exist in polymers. This magnetizability M of a substance in a magnetic field with a field intensity H is computed with the magnetic susceptibility,  $\chi$  as

The susceptibility of pure polymers as diamagnetic substances has a very small and negative value. However, in some cases, we make use of the fact that fillers can alter the magnetic character of a polymer completely. The magnetic properties of polymers are often changed using magnetic fillers. Well-known applications are injection molded or extruded magnets or magnetic profiles, and all forms of electronic storage such as recording tape, floppy or magnetic disks.

### 11.4.2 Magnetic Resonance

Magnetic resonance occurs when a substance, in a permanent magnetic field, absorbs energy from an oscillating magnetic field. This absorption develops as a result of small paramagnetic molecular particles stimulated to vibration. We use this phenomenon to a great extent to clarify structures in physical chemistry. Methods to achieve this include electron spinning resonance (ESR) and, above all, nuclear magnetic resonance (NMR) spectroscopy.

Electron spinning resonance becomes noticeable when the field intensity of a static magnetic field is altered and the microwaves in a high frequency alternating field are absorbed. Since we can only detect unpaired electrons using this method, we use it to determine radical molecule groups.

When atoms have an odd number of nuclei, protons and neutrons, the magnetic fields which are caused by self-motivated spin cannot equalize. The alignment of nuclear spins in an external magnetic field leads to a magnetization vector which can be measured macroscopically as is

11 Electrical Properties of Polymers 543

 $M = \chi H$ (11.41)



schematically demonstrated in Fig. 11.22 [7]. This method is of great importance for the polymer physicist to learn more about molecular structures.

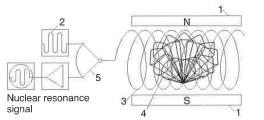


Figure 11.22 Schematic of the operating method of a nuclear spin tomograph: 1) magnet which produces a high steady magnetic field 2) radio wave generator 3) high-frequency field, produced by 2, when switch 5 is in upper position 4) processing nucleus, simulated by high frequency field 5) switch; in this position the decrease of relaxation of the nucleus' vibrations is measured.

### References

1. Domininghaus, H., Plastics for Engineers, Hanser Publishers, Munich, (1993).

2. Baer, E., Engineering Design for Plastics, Robert E. Krieger Publishing Company, (1975).

3. Reboul, J.-P., Thermoplastic Polymer Additives, Chapter 6, J.T. Lutz, Jr., Ed., Marcel Dekker, Inc., New York, (1989).

4. Berg, H., Ph .D Thesis, IKV, RWTH-Aachen, Germany, (1976).

5. Wagner, H., Internal report, AEG, Kassel, Germany, (1974).

6. Crawford, R.J., Plastics Engineering, 2nd Ed., Pergamon Press, (1987).

7. From Bild der Wissenschaft.

Since some polymers have excellent optical properties and are easy to mold and form into any shape, they are often used to replace transparent materials such as inorganic glass. Polymers have been introduced into a variety of applications such as automotive headlights, signal light covers, optical fibers, imitation jewelry, chandeliers, toys, and home appliances. Organic materials such as polymers are also an excellent choice for high-impact applications where inorganic materials such as glass would easily shatter. However, due to the difficulties encountered in maintaining dimensional stability, they are not apt for precision optical applications. Other drawbacks include lower scratch resistance, when compared to inorganic glasses, making them still impractical for applications such as automotive windshields.

In this section, we will discuss basic optical properties which include the index of refraction, birefringence, transparency, transmittance, gloss, color, and behavior of polymers in the infrared spectrum.

### 12.1 Index of Refraction

As rays of light pass through one material into another, the rays are bent due to the change in the speed of light from one media to the other. The fundamental material property that controls the bending of the light rays is the index of refraction, N. The index of refraction for a specific material is defined as the ratio between the speed of light in a vacuum to the speed of light through the material under consideration

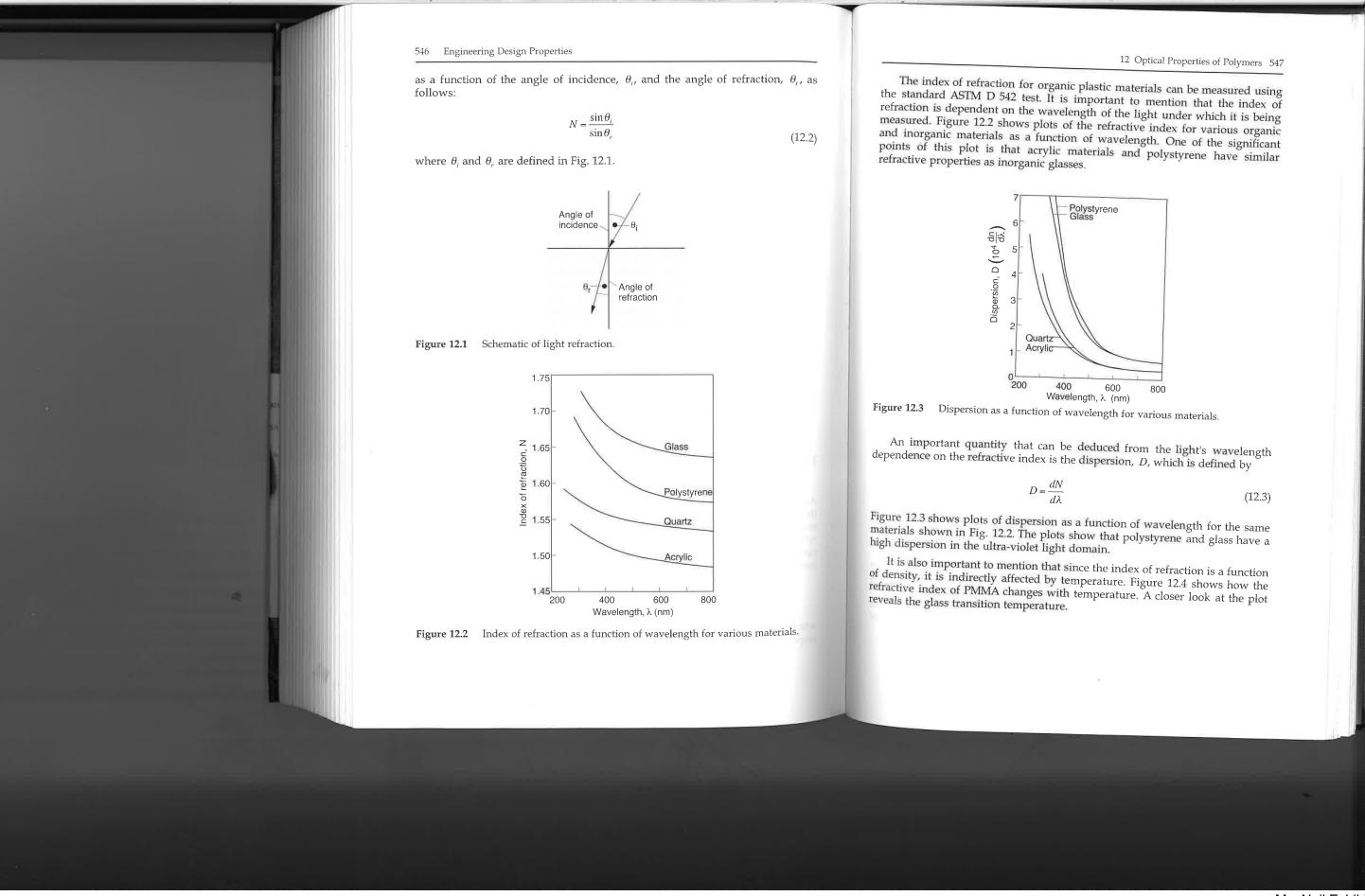
where c and v are the speeds of light through a vacuum and transparent media, respectively. In more practical terms, the refractive index can also be computed

# 12

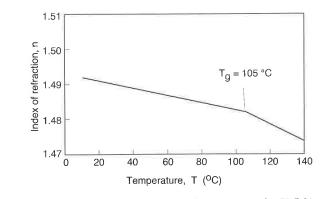
# **Optical Properties of Polymers**

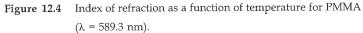
$$N = \frac{c}{v}$$
(12.1)





$$=\frac{dN}{d\lambda}$$
(12.3)





### 12.2 Photoelasticity and Birefringence

Photoelasticity and flow birefringence are applications of the optical anisotropy of transparent media. When a transparent material is subjected to a strain field or a molecular orientation, the index of refraction becomes directional; the principal strains  $\varepsilon_1$  and  $\varepsilon_2$  are associated with principal indices of refraction  $N_1$  and  $N_2$  in a two-dimensional system. The difference between the two principal indices of refraction (birefringence) can be related to the difference of the principal strains using the *strain-optical coefficient*, *k*, as

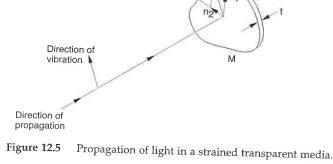
$$N_1 - N_2 = k(\varepsilon_1 - \varepsilon_2) \tag{12.4}$$

or, in terms of principal stress, and

$$N_1 - N_2 = C(\sigma_1 - \sigma_2)$$
(12.5)

### where C is the stress-optical coefficient.

Double refractance in a material is caused when a beam of light travels through a transparent media in a direction perpendicular to the plane that contains the principal directions of strain or refraction index, as shown schematically in Fig. 12.5 [1]. The incoming light waves split into two waves that oscillate along the two principal directions. These two waves are out of phase by a distance  $\delta$ , defined by



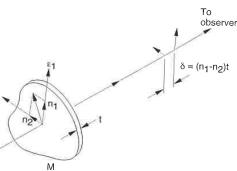
where d is the thickness of the transparent body. The out-of-phase distance,  $\delta$ , between the oscillating light waves is usually referred to as the retardation.

In photoelastic analysis, one measures the direction of the principal stresses or strains and the retardation to determine the magnitude of the stresses. The technique and apparatus used to performed such measurements is described in the ASTM D 4093 test. Figure 12.6 shows a schematic of such a set-up, composed of a narrow wavelength band light source, two polarizers, two quaterwave plates, a compensator, and a monochromatic filter. The polarizers and quaterwave plates must be perpendicular to each other (90°). The compensator is used for measuring retardation, and the monochromatic filter is needed when white light is not sufficient to perform the photoelastic measurement. The set-up presented in Fig. 12.6 is generally called a polariscope.

The parameter used to quantify the strain field in a specimen observed through a polariscope is the color. The retardation in a strained specimen is associated to a specific color. The sequence of colors and their respective retardation values and fringe order are shown in Table 12.1 [1]. The retardation and color can also be associated to a fringe order using

fringe or

12 Optical Properties of Polymers 549



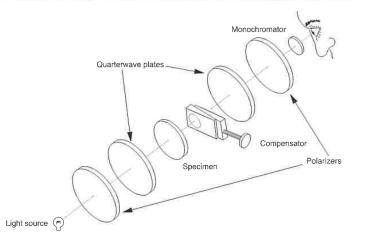
 $\delta = (N_1 - N_2)d$ 

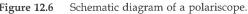
(12.6)

order = 
$$\frac{\delta}{\lambda}$$

(12.7)



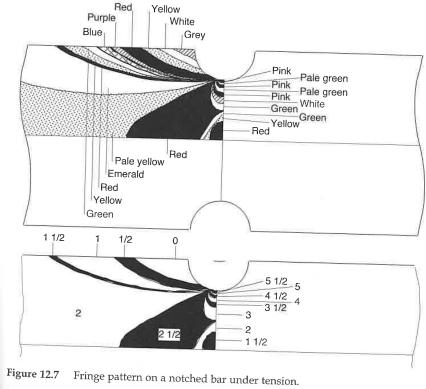




and Fringe Order Produced in a Polariscope

Color	Retardation (nm)	Fringe order
Black	0	0
Gray	160	0.28
White	260	0.45
Yellow	350	0.60
Orange	460	0.79
Red	520	0.90
Tint of passage	577	1.00
Blue	620	1.06
Blue-green	700	1.20
Green-yellow	800	1.38
Orange	940	1.62
Red	1050	1.81
Tint of passage	1150	2.00
Green	1350	2.33
Green-yellow	1450	2.50
Pink	1550	2.67
Tint of passage	1730	3.00
Green	1800	3.10
Pink	2100	3.60
Tint of passage	2300	4.00
Green	2400	4.13

A black body (fringe order zero) represents a strain free body, and closely spaced color bands represent a component with high strain gradients. The color bands are generally called the *isochromatics*. Figure 12.7 shows the isochromatic fringe pattern in a stressed notched bar. The fringe pattern can also be a result of molecular orientation and residual stresses in a molded transparent polymer component. Figure 12.8 shows the orientation induced fringe pattern in a molded part. The residual stress-induced birefringence is usually smaller than the orientation-induced pattern, making them more difficult to measure the orientation-induced pattern, making them more difficult to measure.



rre 12.6 Schema Table 12.1 Color Black Gray White	
Color Black Gray	
 Black Gray	Retar
Gray	
Yellow Orange Red Tint of passa Blue-green Green-yellov Orange Red Tint of passa Green Green-yellov Pink Tint of passa Green Pink Tint of passa Green	N ge N ge
	Green-yellow Orange Red Tint of passa Green Green-yellow Pink Tint of passa Green Pink Tint of passa



## 12 Optical Properties of Polymers 551

Flow induced birefringence is an area explored by several researchers [2-4]. Likewise, the flow induced principal stresses can be related to the principal refraction indices. For example, in a simple shear flow this relation can be written as [5]

$$[N_1 - N_2] = \frac{2C}{\sin 2x} \tau_{12} = \frac{2C}{\sin 2x} \eta \dot{\gamma}$$
(12.8)

where *x* is the orientation of the principal axes in a simple shear flow.

Figure 12.9 [6] shows the birefringence pattern for the flow of linear lowdensity polyethylene in a rectangular die.

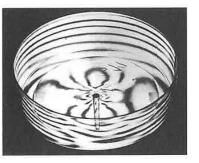


Figure 12.8 Transparent injection molded part viewed through a polariscope.

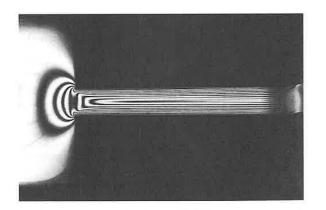


Figure 12.9 Birefringence pattern for flow of LLDPE in a rectangular die.

# 12.3 Transparency, Reflection, Absorption, and Transmittance

As rays of light pass through one media into another of a different refractive index, light will be scattered if the interface between the two materials shows discontinuities larger than the wavelength of visible light<sup>1</sup>. Hence, the transparency in semi-crystalline polymers is directly related to the crystallinity of the polymer. Since the characteristic size of the crystalline domains are larger than the wavelengths of visible light, and since the refractive index of the denser crystalline domains is higher compared to the amorphous regions, semi-crystalline polymers are not transparent; they are opaque or translucent. Similarly, high impact polystyrene- which is actually formed by two amorphous components, polybutadiene rubber particles<sup>2</sup> and polystyrene appears white and translucent due to the different indices of refraction of the two materials. However, filled polymers can be made transparent if the filler size is smaller than the wavelength of visible light. Figure 12.10 shows various types of high impact polystyrene. The two types of HIPS shown in the lower part of the figure have polybutadiene particles that are smaller than the wavelength of visible light, making them transparent.

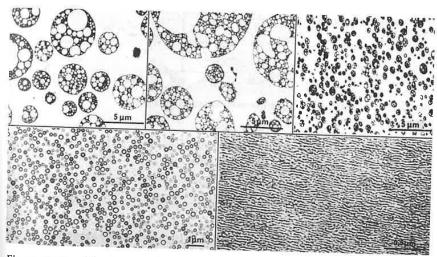


Figure 12.10

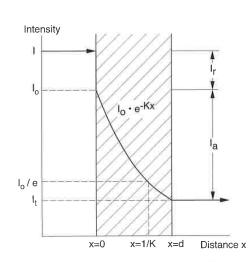
1  $\,$  The wavelength of visible light runs between 400 and 700 nm (0.4 and 0.7  $\mu m).$ 2 The characteristic size of a rubber particle in high impact polystyrene is 1-10µm.

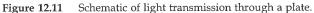
12 Optical Properties of Polymers 553

Morphology of polybutadiene particles in a polystyrene matrix for different types of high impact polystyrene.

The concept of absorption and transmittance can be illustrated using the schematic and notation shown in Fig. 12.11. The figure plots the intensity of a light ray as it strikes and travels through an infinite plate of thickness d. For simplicity, the angle of incidence,  $\theta_i$ , is 0°. The initial intensity of the incoming light beam, I, drops to  $I_0$  as a fraction  $\rho_0$  of the incident beam is reflected out. The reflected light beam can be computed using

$$I_r = \rho_0 I \tag{12.9}$$





The fraction of the incident beam which is reflected can be computed using Beer's law:

$$\rho_0 = \frac{(N-1)^2 + \chi^2}{(N+1)^2 + \chi^2}$$
(12.10)

Here,  $\chi$  is the *absorption index* described by

$$\chi = \frac{K\lambda}{4\pi} \tag{12.11}$$

where  $\lambda$  is the wavelength of the incident light beam and K the coefficient of absorption.

The fraction of the beam that does penetrate into the material continues to drop due to absorption as it travels through the plate. The intensity fraction of the incident beam as it is transmitted through the material can be computed using Bourger's law,

### T(

where K is the *coefficient of absorption*. The intensity fraction of the incident beam transmitted to the rear surface of the plate can now be computed using

However, as illustrated in Fig. 12.12, part of the beam is reflected back by the rear surface of the plate and is subsequently reflected and absorbed several times as it travels

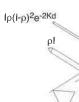


Figure 12.12 Schematic of light reflectance, absorption and transmission through a plate.

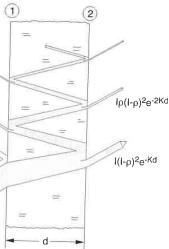
between the front and back surfaces of the plate. The infinite sum of transmitted rays can be approximated by

and the total reflected rays can be approximated with

12 Optical Properties of Polymers 555

$$f(x) = I_0 e^{-\kappa x}$$
 (12.12)

 $\tau = (1 - \rho_0) e^{-\kappa d}$ (12.13)



$$\frac{\rho_0^2}{\rho_0^2 e^{-Kd}}$$

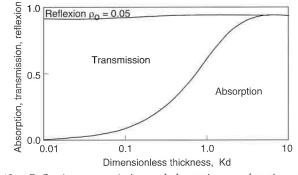
(12.14)

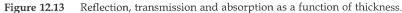
$$\rho = \rho_0 \left( 1 + \tau e^{-\kappa d} \right) \tag{12.15}$$

The fraction of incident beam absorbed by the material and transformed into heat inside the material is calculated using

$$\alpha = 1 - \tau - \rho \tag{12.16}$$

Figure 12.3 shows this relationship as a function of dimensionless thickness *Kd*.





The above analysis is complicated further for the case where the incident angle is no longer 0°. For such a case, and for materials with low coefficient of absorption, the amount of visible light reflected can be computed using Fresnel's equation [7],

$$I_r = \frac{1}{2} \left( \frac{\sin^2(\theta_i - \theta_r)}{\sin^2(\theta_i + \theta_r)} + \frac{\tan^2(\theta_i - \theta_r)}{\tan^2(\theta_i + \theta_r)} \right) I_0$$
(12.17)

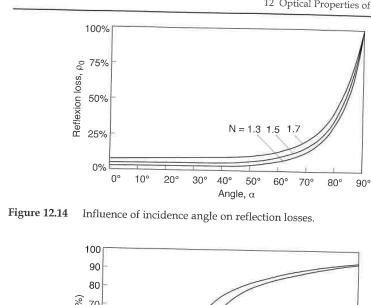
which can be written as

$$=\rho I_0 \tag{12.18}$$

Plots of  $\rho$  as a function of incidence angle are shown in Fig. 12.14 for various refraction indices.

For the case with  $\theta_i = 0^\circ$  the equation can be rewritten in terms of transmittance, T, as

$$T = \left(1 - \frac{\left(N - 1\right)^2}{N^2 + 1}\right) \tag{12.19}$$



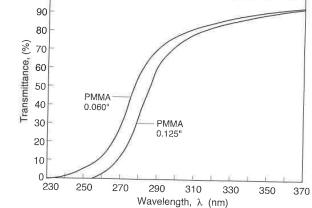


Figure 12.15 Ultraviolet light transmission through PMMA.

which is the fraction of the incident light that is transmitted through the material. For example, a PMMA with a refractive index of 1.49 would at best have a transmittance of 0.92 or 92%. The transmittance becomes less as the wavelength of the incident light decreases, as shown for PMMA in Fig. 12.15. The figure also demonstrates the higher absorption of the thicker sheet.

The transmissivity of polymers can be improved by altering their chemical composition. For example, the transmissivity of PMMA can be improved by substituting hydrogen atoms by fluorine atoms. The improvement is clearly

12 Optical Properties of Polymers 557



demonstrated in Fig. 12.16<sup>3</sup>. Such modifications bring polymers a step closer to materials appropriate for usage in fiber optic applications<sup>4</sup>. Nucleating agents can also be used to improve the transmissivity of semi-crystalline polymers. A large number of nuclei will reduce the average spherulite size to values below the wavelength of visible light.

The haziness or luminous transmittance of a transparent polymer is measured using the standard ASTM D 1003 test, and the transparency of a thin polymer film is measured using the ASTM D 1746 test. The haze measurement (ASTM D 1003) is the most popular measurement for film and sheet quality control and specification purposes.

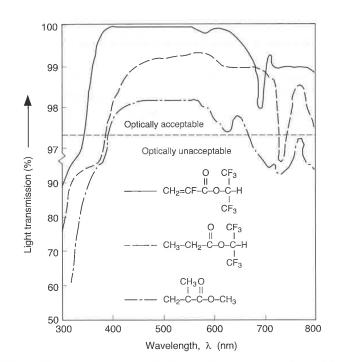


Figure 12.16 Effect of fluorine modification on the transmissivity of light through PMMA.

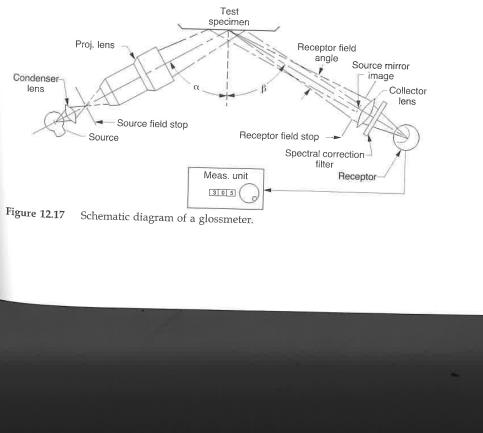
3 Courtesy of Hoechst, Germany.

4 Their ability to withstand shock and vibration and cost savings during manufacturing make some amorphous polymers important materials for fiber optics applications. However, in unmodified polymer fibers, the initial light intensity drops to 50% after only 100 m, whereas when using glass fibers the intensity drops to 50% after 3000 m.

### 12.4 Gloss

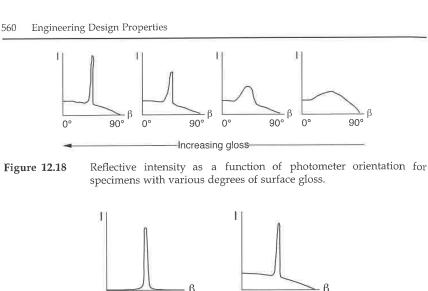
Strictly speaking, all of the above theory is valid only if the surface of the material is perfectly smooth. However, the reflectivity of a polymer component is greatly influenced by the quality of the surface of the mold or die used to make the part.

Specular gloss can be measured using the ASTM D 2457 standard technique which describes a part by the quality of its surface. A glossmeter or lustremeter is usually composed of a light source and a photometer as shown in schematic diagram in Fig. 12.17 [8]. These types of glossmeters are called goniophotometers. As shown in the figure, the specimen is illuminated with a light source from an angle  $\alpha$ , and the photometer reads the light intensity from the specimen from a variable angle  $\beta$ . The angle  $\alpha$  should be chosen according to the glossiness of the surface. For example, for transparent films values for  $\alpha$  range from 20° for high gloss, 45° for intermediate and 60° low gloss. For opaque specimens ASTM test E 97 should be used. Figure 12.18 presents plots of reflective intensity as a function of photometer orientation for several surfaces with various degrees of gloss illuminated by a light source oriented at a 45° angle from the surface. The figure shows how the intensity distribution is narrow and sharp at 45° for a glossy surface, and the distribution becomes wider as the surface becomes matte. The color of the surface also plays a significant role on the intensity distribution read by the photometer as it sweeps through various angular positions. Figure 12.19 shows plots for a black and a white surface with the same degree of glossiness. The specular gloss is used as a measurement of the glossy appearance of films. However, gloss values of opaque and transparent films should not be compared with each other.



12 Optical Properties of Polymers 559





Black specimen

Figure 12.19

Reflective intensity as a function of photometer orientation for black and white specimens with equal surface gloss.

White specimen

## 12.5 Color

The surface quality of a part is not only determined by how smooth or glossy it is but also by its color. Color is often one of the most important specifications for a part. In the following discussion it will be assumed that the color is homogeneous throughout the surface. This assumption is linked to processing, where efficient mixing must take place to disperse and distribute the pigments that will give the part color.

Color can always be described by combinations of basic red, green, and blue<sup>5</sup>. Hence, to quantitatively evaluate or measure a color, one must filter the intensity of the three basic colors. A schematic diagram of a color measurement device is shown in Fig. 12.20. Here, a specimen is lit in a diffuse manner using a photometric sphere, and the light reflected from the specimen is passed through red, green, and blue filters. The intensity coming from the three filters are allocated the variables X, Y, and Z for red, green, and blue, respectively. The variables X, Y, and Z are usually referred to as tristimulus values.

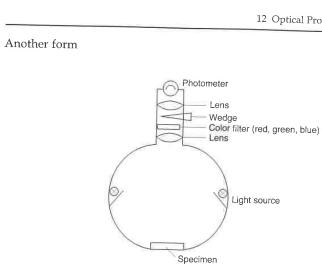


Figure 12.20 Schematic diagram of a colorimeter.

of measuring color is to have an observer compare two surfaces. One surface is the sample under consideration illuminated with a white light. The other surface is a white screen illuminated by light coming from three basic red, green, and blue sources. By varying the intensity of the three light sources, the color of the two surfaces are matched. This is shown schematically in Fig. 12.21 [9]. Here too, the intensities of red, green, and blue are represented with X, Y, and Z, respectively.

The resulting data is better analyzed by normalizing the individual intensities as

X =

y =

Z =

The parameters X, Y, and Z, usually termed trichromatic coefficients, are plotted on a three-dimensional graph that contains the whole spectrum of

12 Optical Properties of Polymers 561

$$\frac{X}{X+Y+Z} \tag{12.20}$$

$$\frac{Y}{X+Y+Z} \tag{12.21}$$

$$\frac{Z}{X+Y+Z} \tag{12.22}$$



MacNeil Exhibit 2117 Yita v. MacNeil IP, IPR2020-01139 Page 291

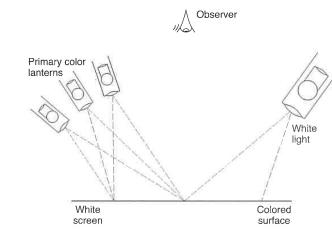
<sup>5</sup> Most color measurement techniques are based on the CIE system. CIE is the *Commission International de l'Eclairage*, or International Commission on Illumination.

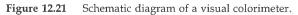


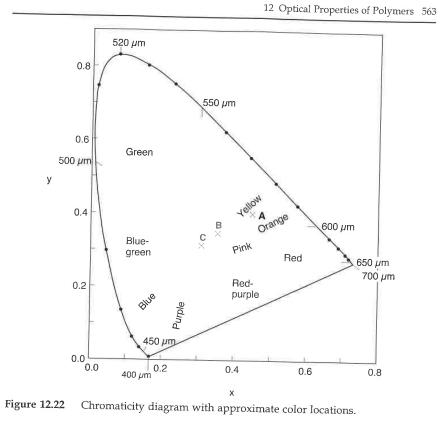
visible light, as shown in Fig. 12.22. This graph is usually referred to as a chromaticity diagram. The standard techniques that make use of the chromaticity diagram are ASTM E 308-90 and DIN 5033. Three points in the diagram have been standardized:

- Radiation from a black body at 2848 K corresponding to a tungsten filament light and denoted by A in the diagram;
- Sunlight, denoted by B; and
- North sky light, denoted by C.

It is important to note that colors plotted on the chromaticity diagram are only described by their hue and saturation. The luminance factor is plotted in the z direction of the diagram. Hence, all neutral colors such as black, gray, and white lie on point C of the diagram.







# 12.6 Infrared Spectroscopy

Infrared spectroscopy has developed into one of the most important techniques used to identify polymeric materials. It is based on the interaction between matter and electromagnetic radiation of wavelengths between 1 and 50  $\mu$ m. The atoms in a molecule vibrate in a characteristic mode, which is usually called a fundamental frequency. Thus, each molecule has a set group of characteristic frequencies which can be used as a diagnostics tool to detect the presence of distinct groups. Table 12.2 [10] presents the absorption wavelength for several chemical groups. The range for most commercially available infrared spectroscopes is between 2 and 25  $\mu$ m. Hence, the spectrum taken between 2 and 25  $\mu$ m serves as a fingerprint for that specific polymer, such as shown in Fig. 12.23 for polycarbonate.



An *infrared spectrometer* to measure the absorption spectrum of a material is schematically represented in Fig.12.24. It consists of an infrared light source that can sweep through a certain wavelength range, and that is split in two beams: one that serves as a reference and the other that is passed through the test specimen. The comparison of the two gives the absorption spectrum, such as shown in Fig. 12.23.

Using infrared spectroscopy, also helps in quantitatively evaluating the effects of weathering (e.g., by measuring the increase of the absorption band of the COOH group, or by monitoring the water intake over time). One can also use the technique to follow reaction kinetics during polymerization.

Table 12.2 Absorption Wavelengths for Various Groups

Group	Wavelength region (µm)
О-Н N-Н C-Н C-О C-С	2.74 3.00 3.36 9.67 11.49
C=O C=N C=C C=S	5.80 5.94 6.07 6.57

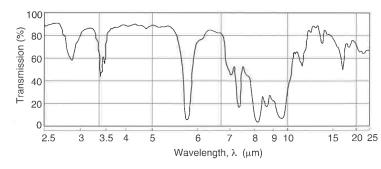
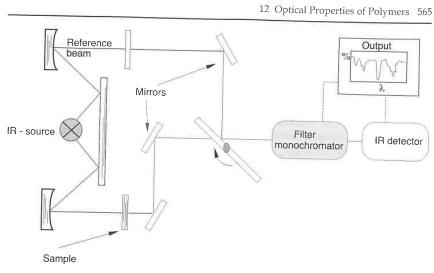


Figure 12.23 Infrared spectrum of a polycarbonate film.





## 12.7 Infrared Pyrometry

Today it is possible to measure the temperature at the surface of a polymer melt or component using an infrared probe. Infrared pyrometry is based on Planck's law, which describes the spectral distribution of blackbody radiation by

> $I_2 = -$ πλ

$$\frac{c_1}{\lambda^5 \left[ \exp\left(\frac{c_2}{\lambda T_\lambda}\right) - 1 \right]}$$
(12.23)

where  $\lambda$  is the mean effective wavelength utilized by an IR pyrometer,  $I_{\lambda}$  is the amount of spectral radiance emitted by a blackbody with a spectral radiance temperature of  $T_{\lambda}$  (K), and  $c_1 (= 3.742 \times 10^8 \text{ W} \mu \text{m}^4/\text{m}^2)$  and  $c_2 (= 1.439 \times 10^4 \mu \text{m}^0 \text{ K})$ are Planck's first and second radiation constants, respectively. Within the range of typical polymer processing temperatures, Planck's law can be further simplified as Wien's law, i.e.,  $\exp(c_2/\lambda T) >> 1$  which is given by

(12.24)

Equations 12.23 or 12.24 can be used to convert the measured radiance from an IR pyrometer,  $I_{i}$ , into a temperature,  $T_{i}$ , for a blackbody with an emissivity of 1.0. However, when measuring the temperature of a non-blackbody whose emissivity is  $\varepsilon_l \ (\neq 1.0)$ , the true surface temperature of the non-blackbody,  $T_s$ , and the spectral radiance temperature,  $T_{\lambda}$ , can be related to each other using Eq. 12.24 by the following equation

$$I_{\lambda} = \frac{c_1}{\pi \lambda^5 \exp\left(\frac{c_2}{\lambda T_{\lambda}}\right)} = \frac{\varepsilon_{\lambda} c_1}{\pi \lambda^5 \exp\left(\frac{c_2}{\lambda T_{\lambda}}\right)}$$
(12.25)

The true surface temperature of a polymer melt or component can then be calculated from rearranging Eq. 12.25 to,

$$\frac{1}{s} = \frac{1}{T_{\lambda}} + \frac{\lambda}{c_2} \ln(\varepsilon_{\lambda})$$
(12.26)

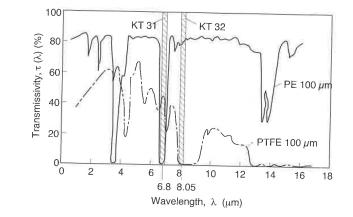
The spectral surface emissivity of a material can be obtained by either direct measurement [11] or by calculation using both Kirchhoff's law and the radiation energy balance equation (i.e., Eq. 12.16). Kirchhoff's law basically states that the emissivity and the absorptivity of the material are equal (i.e.,  $\varepsilon_{1} = \alpha_{1}$ ). Therefore, if the reflectivity and transmissivity of a semi-transparent polymer are known, then the emissivity of a polymer can be computed from Eq. 12.16 as

$$\varepsilon_{\lambda} = 1 - \tau_{\lambda} - \rho_{\lambda} \tag{12.27}$$

However, if the polymer specimen is thick enough, we can eliminate transmissivity from Eq. 12.27, taking the measurements at a wavelength at which polymers absorb strongly; that is, at a wavelength which has a strong dip in its spectrum. To do this we select proper narrow-band filters to control the bandwidth and mean effective wavelength of the pyrometer. This concept is clearly demonstrated in Fig. 12.25 [12], which shows the transmissivity spectrum of polyethylene and polytetrafluoroethylene. It is easy to spot the bands of low transmissivity such as the one around 6.8  $\mu$ m (CH<sub>3</sub> band) in the PE spectrum. For most polymer films one can assume a reflectivity value,  $\rho$ , of 0.05 [13].

As indicated from the preceding description, if the mean effective wavelength of an IR pyrometer is controlled at a bandwidth where the target polymer has a low transmissivity, then the IR pyrometer can measure the surface temperature of the target polymer. More recently, attempts have been made to measure the subsurface temperature in a polymer melt stream in a non-invasive manner using IR probes [14, 15]. For such measurements, the mean effective wavelength of an IR pyrometer is controlled at a bandwidth

where the transmissivity of the polymer is relatively high (i.e., the polymer has a low radiation absorbing behavior), then the IR pyrometer is able to capture subsurface radiation and provide bulk temperature information of the polymer. Since the captured bulk temperatures contain detailed thermal information about the volume of the polymer, it is possible to retrieve the detailed temperature profile from the captured bulk temperatures using an inverse radiation technique [16]. The inverse radiation technique basically deciphers a set of bulk radiation measured at several different mean effective wavelengths utilized by an IR pyrometer, to retrieve the temperature distribution within the polymer. The theoretical background of the inverse radiation technique provides the foundation of a new generation IR pyrometer which will be very useful for process monitoring during polymer processing.



## 12.8 Heating with Infrared Radiation

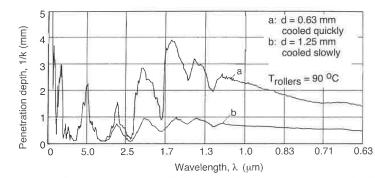
Although the heating of polymer sheets for thermoforming or other membrane stretching processes belongs to the field of radiative heat transfer, it is largely an optical problem. In such processes, an infrared heater is used to radiate infrared rays onto the surface of the sheet under consideration. Much of the process that takes place can be analyzed using the theory of absorption and transmittance discussed in Section 12.3. For example, the absorption properties largely depend on pigments or spherulite size. Figure 12.26 [17] shows a plot of

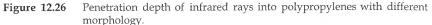
### 12 Optical Properties of Polymers 567

Figure 12.25 Transmissivity of a polyethylene and a polytetrafluoroethylene.



the inverse of the absorption coefficient (penetration depth) of polypropylene with two different spherulite sizes as a function of the wavelength. Figure 12.27 [15] presents a similar graph for polystyrene without pigmentation, translucent polystyrene with a blue pigment, and opaque polystyrene with a white pigment. The absorption of polymers also varies according to the temperature of the radiative heater. Figure 12.28 [15] shows this dependence for various polymer sheets of 1 mm thickness and variable pigment. It is interesting to note that all polymers observe a similar absorption at a heater temperature of 1200 K.





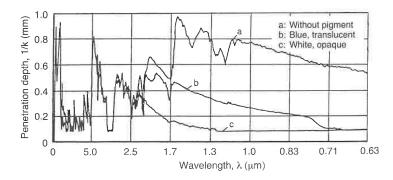
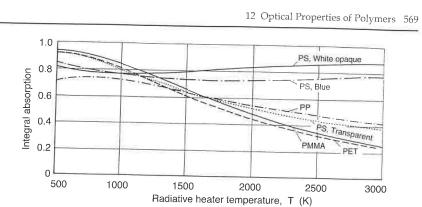


Figure 12.27 Penetration depth of infrared rays into polystyrenes with different pigmentation.



# polymers.

### References

- 1. ASTM Vol 08.02, Plastics (II): ASTM-D4093, (1994).
- Amsterdam, (1984). Isayev, A.I., Polym. Eng. Sci., 23, 271, (1983). 3.
- Wimberger-Friedl, R., Polym. Eng. Sci., 30, 813, (1990). 4.
- Lodge, A.S., Trans. Faraday Soc., 52, 120, (1956). 5.
- Sornberger, G., Quantin, J.C., Fajolle, R., Vergnes, B., and Agassant, J.F., J. Non-6.
- Newt. Fluid Mech., 23, 123, (1987). 7. Publishing Co., (1975).
- 8. ASTM Vol 08.02, Plastics (II): ASTM-D2457, (1994).
- 10. Chapman, D., The Science of Surface Coatings, Chapter 19, Ed. H.W. Chatfield, D. van Nostrand Co., Inc. Princeton, (1962).
- 11. Dewitt, D.P., and Richmond, J. C., "Thermal Radiative Properties of Materials," Chapter 2 in *Theory and Practice of Radiation Thermometry*, D.P. Dewitt and G.D. Nutter, Eds., Wiley, New York, (1988).

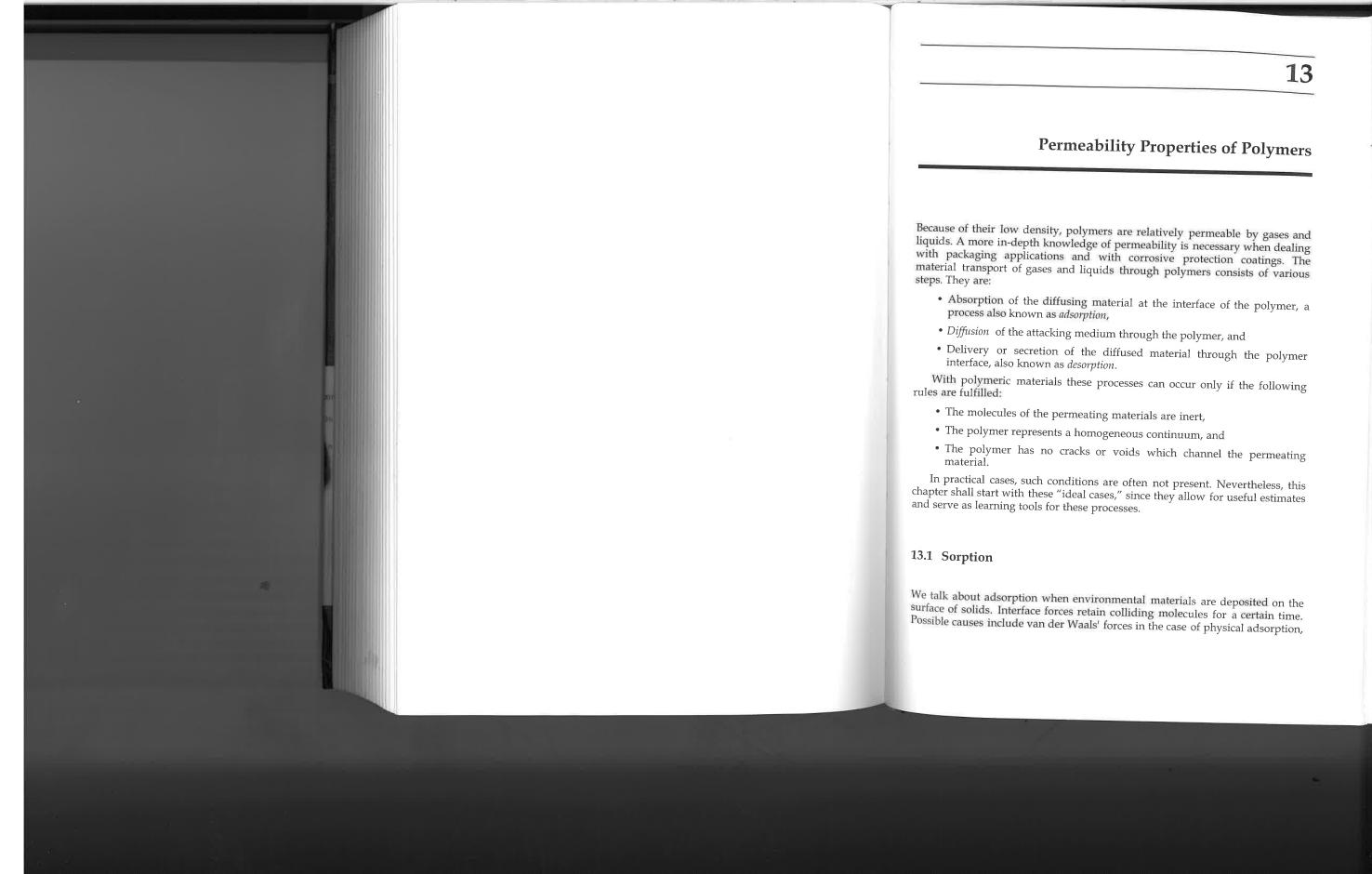
- 14. Rietveld, J.X., and Lai, G.-Y., SPE ANTEC, 38, 2192, (1992).
- 15. Lai, G.-Y., Ph.D. Thesis, University of Wisconsin-Madison, Madison, WI, (1993). 16. Rietveld, J.X., and Lai, G.-Y., SPE ANTEC, 40, 836, (1994).

Figure 12.28 Integral absorption as a function of heater temperature for various

- 2. Janeschitz-Kriegl, H., Polymer Melt Rheology and Flow Birefringence, Elsevier,

  - Bartoe, W.F., Engineering Design for Plastics, E. Baer, Ed., Chapter 8, R.E. Krieger
- 9. Adams, J.M., The Science of Surface Coatings, Chapter 12, Ed. H.W. Chatfield, D. van Nostrand Co., Inc. Princeton, (1962).
- 12. Heimann, W., Communication, Firma W. Heimann, Wiesbaden, Germany.
- 13. Haberstroh, E., Ph.D. Thesis, IKV, RWTH-Aachen, Germany, (1981).
- 17. Weinand, D., Ph.D. Thesis, IKV, RWTH-Aachen, Germany, (1987).





chemical affinity (chemical sorption), or electrostatic forces. With polymers, we have to take into account all of these possibilities.

A gradient in concentration of the permeating substance inside the material results in a transport of that substance which we call molecular diffusion. The cause of molecular diffusion is the thermal motion of molecules that permit the foreign molecule to move along the concentration gradient using the intermolecular and intramolecular spaces. However, the possibility to migrate essentially depends on the size of the migrating molecule.

The rate of permeation for the case shown schematically in Fig. 13.1 is defined as the mass of penetrating gas or liquid that passes through a polymer membrane per unit time. The rate of permeation,  $\dot{m}$ , can be defined using Fick's first law of diffusion as

$$\dot{m} = -DA\rho \frac{dc}{dx} \tag{13.1}$$

where *D* is defined as the *diffusion coefficient*, *A* is the area and  $\rho$  the density. If the diffusion coefficient is constant Eq. 13.1 can be easily integrated to give

$$\dot{n} = -DA\rho(c_1 - c_2)/L \tag{13.2}$$

The equilibrium concentrations  $c_1$  and  $c_2$  can be calculated using the pressure,  $p_1$ , and the sorption equilibrium parameter, S:

*C* =

$$Sp$$
 (13.3)

which is often referred to as *Henry's law*.

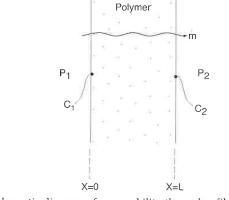
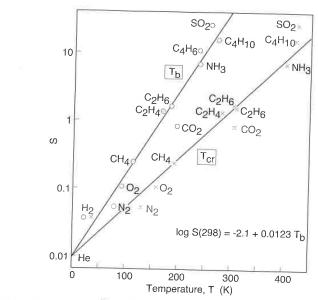
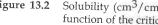


Figure 13.1 Schematic diagram of permeability through a film.

The sorption equilibrium constant, also referred to as solubility constant, is almost the same for all polymer materials. However, it does depend largely on the type of gas and on the boiling,  $T_b$ , or critical temperatures,  $T_{cr}$ , of the gas, such as shown in Fig. 13.2.





## 13.2 Diffusion and Permeation

Diffusion, however, is only one part of permeation. First, the permeating substance has to infiltrate the surface of the membrane; it has to be absorbed by the membrane. Similarly, the permeating substance has to be desorbed on the opposite side of the membrane. Combining Eq. 13.2 and 13.3 we can calculate the sorption equilibrium using

 $\dot{m} = -DS\rho A (p_1 - p_2)/L$ 

where the product of the sorption equilibrium parameter and the diffusion coefficient is defined as the *permeability* of a material

13 Permeability Properties of Polymers 573

Figure 13.2 Solubility  $(cm^3/cm^3)$  of gas in natural rubber at 25 °C and 1 bar as a function of the critical and the boiling temperatures.

(13.4)



$$P = DS = \frac{\dot{m}L}{A\Delta p\rho} \tag{13.5}$$

Equation 13.5 does not take into account the influence of pressure on the permeability of the material and is only valid for dilute solutions. The Henry-Langmuir model takes into account the influence of pressure and works very well for amorphous thermoplastics. It is written as

$$P = DS\left(1 + \frac{KR'}{1 + b\Delta p}\right) \tag{13.6}$$

where  $K = c'_H b / S$ , with  $c'_H$  being a saturation capacity constant and b an affinity coefficient. The constant R<sup>i</sup> represents the degree of mobility, R'=0 for complete immobility and R'=1 for total mobility. Table 13.1 [1] presents permeability of various gases at room temperature through several polymer films. In the case of multi-layered films commonly used as packaging material, we can calculate the permeation coefficient P<sub>C</sub> for the composite membrane using

$$\frac{1}{P_{C}} = \frac{1}{L_{C}} \sum_{i=1}^{l \leq n} \frac{L_{i}}{P_{i}}$$
(13.7)

**Table 13.1** Permeability of Various Gases Through Several Polymer Films

Permeability (cm <sup>3</sup> mil/100 in <sup>2</sup> /24 h/atm)				
Polymer	CO <sub>2</sub>	O <sub>2</sub>	H <sub>2</sub> O	
PET	12-20	5-10	2-4	
OPET	6	3	1	
PVC	4.75-40	8-15	2-3	
HDPE	300	100	0.5	
LDPE		425	1-1.5	
PP	450	150	0.5	
EVOH	0.05-0.4	0.05-0.2	1-5	
PVDC	1	0.15	0.1	

Sorption, diffusion, and permeation are processes activated by heat and as expected follow an Arrhenius type behavior. Thus, we can write

$$S = S_0 e^{-\Delta H_S/RT} \tag{13.8}$$

$$D = D_0 e^{-E_D / RT} \quad \text{and} \tag{13.9}$$

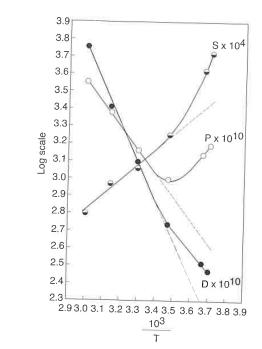


Figure 13.3 Sorption, diffusion, and permeability coefficients, as a function of temperature for polyethylene and methyl bromine at 600 mm of Hg.

13 Permeability Properties of Polymers 575

 $P = P_0 e^{-E_P / RT}$ 

where  $\Delta H_S$  is the enthalpy of sorption,  $E_p$  and  $E_p$  are diffusion and permeation activation energies, R is the ideal gas constant, and T is the absolute temperature. The Arrhenius behavior of sorption, diffusion and permeability coefficients, as a function of temperature for polyethylene and methyl bromine at 600 mm of Hg are shown in Fig. 13.3 [2]. Figure 13.4 [3] presents the permeability of water vapor through several polymers as a function of temperature. It should be noted that permeability properties drastically change once the temperature goes above the glass transition temperature. This is demonstrated in Table 13.2 [4], which presents Arrhenius constants for diffusion of selected polymers and CH<sub>3</sub>OH.



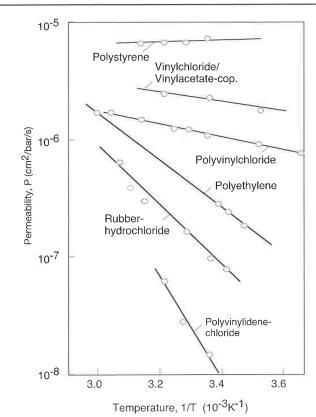
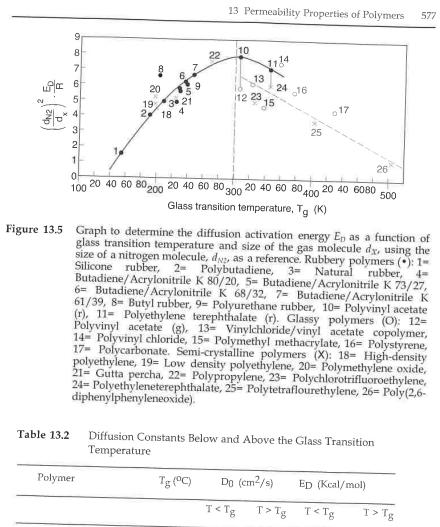


Figure 13.4 Permeability of water vapor as a function of temperature through various polymer films.

The diffusion activation energy  $E_{D}$  depends on the temperature, the size of the gas molecule  $d_x$ , and the glass transition temperature of the polymer. This relationship is well represented in Fig. 13.5 [1] with the size of nitrogen molecules,  $d_{N2}$  as a reference. Table 13.2 contains values of the effective cross section size of important gas molecules. Using Fig. 13.5 with the values from Table 13.1 and using the equations presented in Table 13.3 the diffusion coefficient, *D*, for several polymers and gases can be calculated.

Table 13.4 also demonstrates that permeability properties are dependent on the degree of crystallinity. Figure 13.6 presents the permeability of polyethylene films of different densities as a function of temperature. Again, the Arrhenius relation becomes evident.



Polymethylmethacrylate	
Polystyrene	
Polyvinyl acetate	

g ( <sup>o</sup> C)	$D_0 (cm^2/s)$		E <sub>D</sub> (Kcal/1	mol)
	T < Tg	$T > T_g$	T < Tg	T > Tg
90 88 30	0.37 0.33 0.02	110 37 300	12.4 9.7 7.6	21.6 17.5 20.5

### Table 13.3 Important Properties of Gases

Gas	d (nm)	V <sub>cr</sub> (cm <sup>3</sup> )	т <sub>ь</sub> (К)	T <sub>cr</sub> (K)	$dN_2/dz$
He H2O	0.255 0.370	58 56	4.3 373	5.3 647	0.67 0.97
H <sub>2</sub>	0.282	65	20	33	0.74
– Ne NH3	0.282 0.290	42 72.5	27 240	44.5 406	0.74 0.76
02	0.347	74	90	55	0.91
Ar CH3OH	0.354 0.363	75 118	87.5 338	151 513	0.93 0.96
Kr CO CH4	0.366 0.369 0.376	92 93 99.5	121 82 112	209 133 191	0.96 0.97 0.99
N <sub>2</sub>	0.380	90	77	126	1.00
CO <sub>2</sub>	0.380	94	195	304	1.00
Xe SO2	0.405 0.411	119 122	164 263	290 431	1.06 1.08
C <sub>2</sub> H <sub>4</sub>	0.416	124	175	283	1.09
CH3Cl	0.418	143	249	416	1.10
C <sub>2</sub> H <sub>6</sub>	0.444	148	185	305	1.17
CH <sub>2</sub> Cl <sub>2</sub>	0.490	193	313	510	1.28
C3H8	0.512	200	231	370	1.34
C <sub>6</sub> H <sub>6</sub>	0.535	260	353	562	1.41

 Table 13.4
 Equations to Compute D Using Data from Table 13.1 and Table 13.2<sup>a</sup>

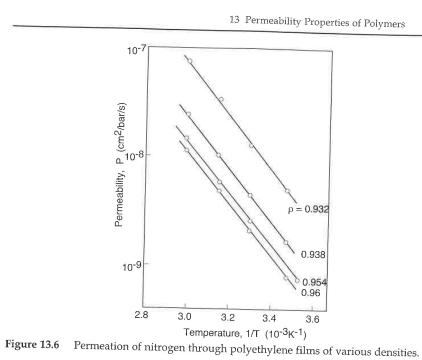
Elastomers  

$$\log D = \frac{E_D}{2.3R} \left( \frac{1}{T} - \frac{1}{T_R} \right) - 4$$
Amorphous thermoplastics  

$$\log D = \frac{E_D}{2.3R} \left( \frac{1}{T} - \frac{1}{T_R} \right) - 5$$
Semi-crystalline thermoplastics  

$$\log D = \left( \frac{E_D}{2.3R} \left( \frac{1}{T} - \frac{1}{T_R} \right) - 5 \right) (1 - x)$$

<sup>a</sup>  $T_R$  = 435K and X is the degree of crystallinity.



## 13.3 Measuring S, D, and P

The *permeability* P of a gas through a polymer can be measured directly by determining the transport of mass through a membrane per unit time.

The sorption constant S can be measured by placing a saturated sample into an environment which allows the sample to desorb and measure the loss of weight. As shown in Fig. 13.7, it is common to plot the ratio of concentration of absorbed substance c(t) to saturation coefficient  $c_{\infty}$  with respect to the root of time.

The diffusion coefficient D is determined using sorption curves as the one shown in Fig. 13.7. Using the slope of the curve, a, we can compute the diffusion coefficient as

where L is the thickness of the membrane.

13 Permeability Properties of Polymers 579

 $D = \frac{\pi}{16}L^2a^2$ 



Another method uses the lag time,  $t_0$ , from the beginning of the permeation process until the equilibrium permeation has occurred, as shown in Fig. 13.8. Here, the diffusion coefficient is calculated using

$$D = \frac{L^2}{6t_0}$$
(13.12)

The most important techniques used to determine gas permeability of polymers are the ISO 2556, DIN 53 380 and ASTM D 1434 standard tests.

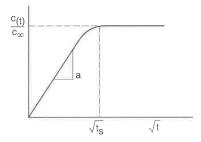


Figure 13.7 Schematic diagram of sorption as a function time.

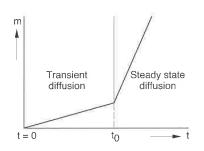


Figure 13.8 Schematic diagram of diffusion as a function of time.

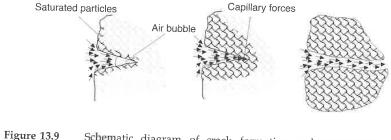
### 13.4 Corrosion of Polymers and Cracking [5]

In contrast to metallic corrosion, where electrochemical corrosion mechanisms are dominant, several mechanisms play a role in the degradation of polymers. Attacks may occur by physical or chemical means or by combinations of both.

Even without a chemical reaction, the purely physical effect of a surrounding medium can adversely affect the properties of a polymer. Due to the low density of polymers, every surrounding medium that has moveable molecules will infiltrate or permeate the polymer. Experiments have shown that polymer samples under high hydrostatic pressures have even been permeated by silicon oils, which are completely inert at low pressures. The infiltration of silicone oil caused stress cracks and embrittlement in amorphous thermoplastics in the regions of low density, such as particle boundaries, filler material interfaces, and general surface imperfections. If we consider imperfections or particles of characteristic size L, we can perform an energy balance and conclude that the critical strain,  $\varepsilon_{cin}$ , at which a crack will occur is given by [6]

3

where *E* represents Young's modulus and  $\gamma$  the adhesion tension between the individual particles. Crack formation and propagation is shown schematically in Fig. 13.9 [7]. Figure 13.101 shows an electron micrograph of permeating media through the inter-spherulitic boundaries of polypropylene.



diffusion.

Desorption, schematically shown in Fig. 13.11, is also undesirable for polymeric components. Similar to soil, which cracks as it dries out too quickly, the stresses that arise as the medium desorbs from the polymer give rise to cracks which may lead to failure of the component. As the absorbed media desorbs, the polymer component shrinks according to the loss of volume. However, inner layers which remain saturated do not shrink, leading to residual stress build-up similar to that which occurs with a cooling component with high temperature gradients. The schematic of the residual stress build-up

1 Courtesy IKV Aachen.

13 Permeability Properties of Polymers 581

$$c_{\rm crit} \sim \sqrt{\frac{\gamma}{EL}}$$
 (13.13)





and concentration of the absorbed media is shown in Fig. 13.12 [8]. The stress history at the edge and center of a desorbing film is shown in Fig. 13.13. The stresses that arise during desorption are easily three times larger than during absorption. The maximum stress, which occurs at the outer edge of the part can be calculated using

$$\sigma_{\max} = \varepsilon_{\text{saturation}} \frac{E}{1 - \nu}$$
(13.14)

The volume change in the immediate surface of the component is caused by the desorption process. The desorpting materials can be auxiliary agents for processing such as coloring agents, softeners, stabilizers, and lubricants, as well as low molecular components of the polymer.

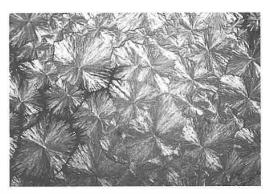
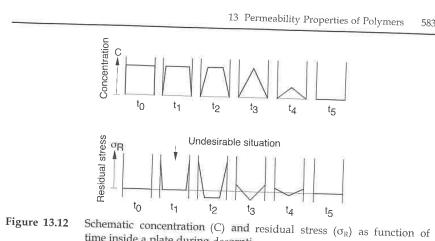
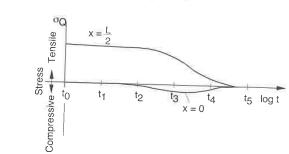


Figure 13.10 Electron micrograph of permeating media through the interspherulitic boundaries of polypropylene.



Figure 13.11 Schematic diagram of desorption from a plate.





The ability to infiltrate the surface of a host material decreases with molecular size. Molecules of  $M > 5 \times 10^3$  can hardly diffuse through a porous-free membrane. Self-diffusion is when a molecule moves, say in the melt, during crystallization. Also, when bonding rubber, the so-called tack is explained by the self-diffusion of the molecules. The diffusion coefficient for self-diffusion is of the order of

where *T* is the temperature and  $\eta$  the viscosity of the melt.

13 Permeability Properties of Polymers 583

time inside a plate during desorption.

Figure 13.13 Residual stresses inside a plate during desorption.

# 13.5 Diffusion of Polymer Molecules and Self-diffusion

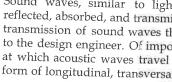
$$D \sim \frac{T}{\eta} \tag{13.15}$$





### References

- 1. Rosato, D., and Rosato, D.V., Blow Molding Handbook, Hanser Publishers, Munich, (1989).
- Rogers, C.E., Engineering Design for Plastics, Ed. E. Baer, Chapter 9, Robert E. Krieger Publishing Company, Huntington, (1975).
- 3. Knappe, W., VDI-Berichte, 68, 29, (1963).
- 4. van Krevelen, D.W., and Hoftyzer, P.J., Properties of Polymers, 2nd Ed., Elsevier, Amsterdam, (1976).
- 5. Menges, G., and Löwer, K., Metallic Corrosion: Proceedings, 8th ICMC, 2202, Mainz (1981).
- 6. Menges, G., Kunststoffe, 63, 95, (1973).
- 7. Menges, G. and Suchanek, H., Kunststoffe, Fortschrittsberichte, Vol. 3, Hanser Publishers, Munich, (1976).
- 8. Pütz, D., Ph.D. Thesis, IKV, RWTH-Aachen, Germany, (1977).



## 14.1 Speed of Sound

The speed at which sound is transmitted through a solid barrier is proportional to Young's modulus of the material, E, but inversely proportional to its density,  $\rho$ . For sound waves transmitted through a rod, in the longitudinal direction, the speed of sound can be computed as

## $C_L^{rot}$

Similarly, the transmission speed of sound waves through a plate along its surface direction can be computed as

### $C_I^{\text{plate}} =$

where v is Poisson's ratio. The transmission speed of sound waves through an infinite three-dimensional body can be computed using

# 14

# **Acoustic Properties of Polymers**

Sound waves, similar to light waves and electromagnetic waves, can be reflected, absorbed, and transmitted when they strike the surface of a body. The transmission of sound waves through polymeric parts is of particular interest to the design engineer. Of importance is the absorption of sound and the speed at which acoustic waves travel through a body, for example in a pipe, in the form of longitudinal, transversal, and bending modes of deformation.

$$e^{d} = \sqrt{\frac{E}{\rho}}$$
(14.1)

$$\sqrt{\frac{E}{\rho(1-\nu^2)}} \tag{14.2}$$

$$\frac{E(1-\nu)}{(1+\nu)(1-2\nu)}$$
(14.3)



The transmission of sound waves transversely though a plate (in shear) can be computed using

$$C_T^{\text{plate}} = \sqrt{\frac{G}{\rho}} \tag{14.4}$$

where G is the modulus of rigidity of the material. The transmission speed of sound waves with a frequency f which cause a bending excitation in plates can be computed using

$$C_{B}^{\text{plate}} = \sqrt{\frac{2\pi f h}{2\sqrt{3}} \frac{E}{\rho(1-v^{2})}}$$
(14.5)

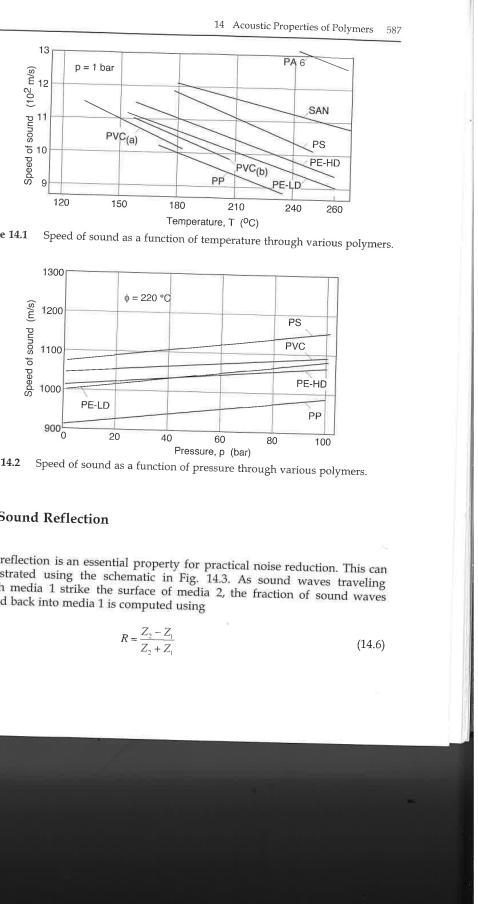
### where h is the thickness of the plate.

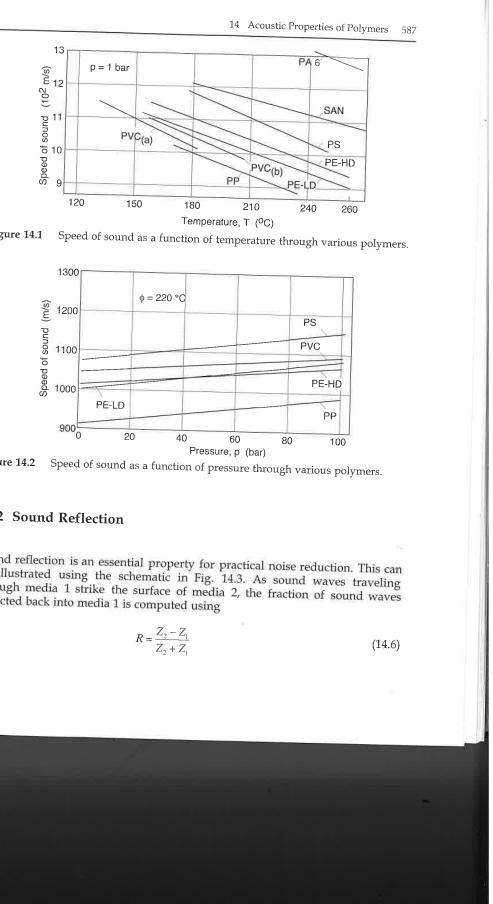
The speed of sound through a material is dependent on its state. For example, sound waves travel much slower through a polymer melt than through a polymer in the glassy state. Table 14.1 presents orders of magnitude of the speed of sound through polymers in the glassy and rubbery states for various modes of transmission. One can see that the speed of sound through a polymer in the rubbery state is 100 times slower than that through a polymer in a glassy state.

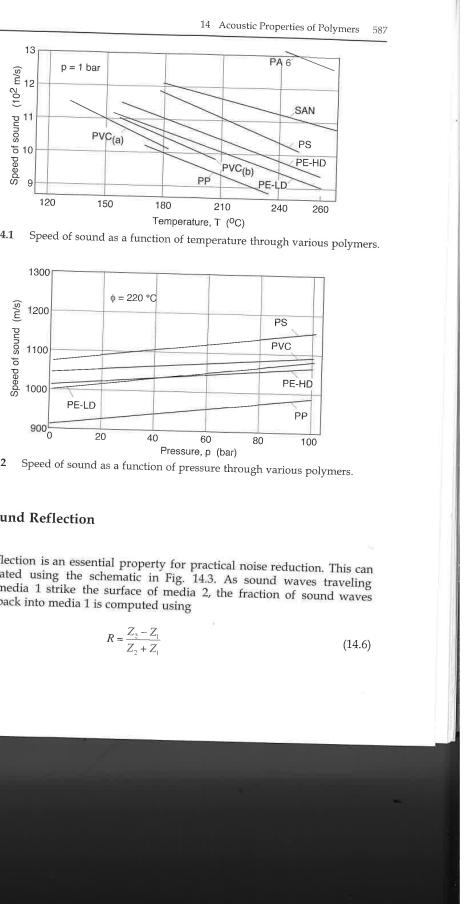
In the melt state, the speed of sound drops with increasing temperature due to density increase. Figure 14.1 [1] presents plots of speed of sound through several polymer melts as a function of temperature. On the other hand, speed of sound increases with pressure as clearly demonstrated in Fig. 14.2 [1].

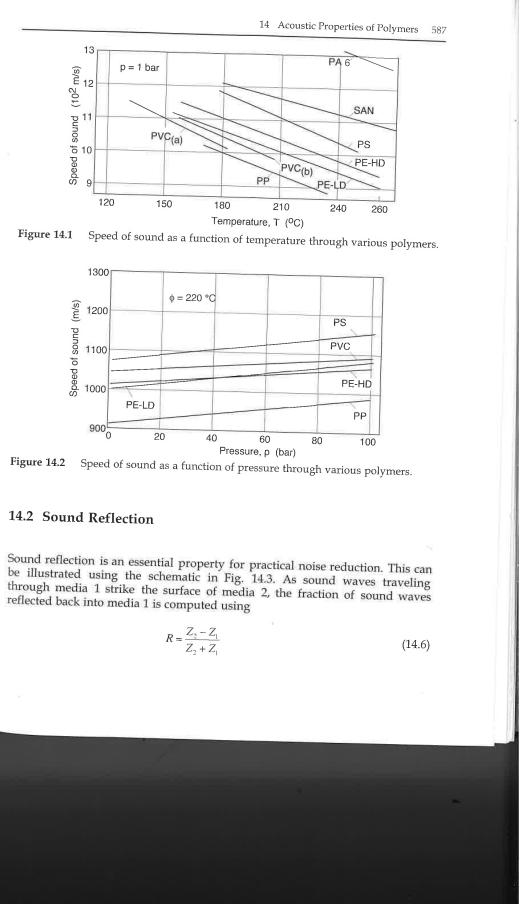
 
 Table 14.1
 Order of Magnitude of Properties Related to Sound
 Transmission

Speed of sound (m/s)
Glassy ( $v = 0.3$ )
C <sub>L</sub> ∪ 2000 C <sub>T</sub> ∪ 1000 C <sub>3D</sub> ∪ 2000
Rubbery ( $\nu = 0.5$ )
C <sub>L</sub> U 10 to 400 C <sub>T</sub> U 6 to 200 C <sub>3D</sub> U 2000











588 Engineering Design Properties

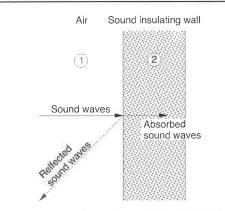


Figure 14.3 Schematic diagram of sound transmission through a plate.

where *Z* is the impedance or wave resistance, and is defined by

$$Z = \rho C_w \tag{14.7}$$

### where $C_{ii}$ is the sound wave speed.

In order to obtain high sound reflection, the mass of the media 2 must be high compared to the mass of media 1 such that  $Z_2 >> Z_1$ . The mass of insulating sound walls can be increased with the use of fillers such as plasticized PVC with barium sulfate or by spraying similar anti noise compounds on the insulating walls. Using the mass of the insulating wall, another equation used to compute sound reflectance is

$$R = 20\log\left(\frac{\pi f M}{Z_0}\right) \tag{14.8}$$

where f is frequency of the sound wave, M the mass of the insulating wall and,  $Z_0$  is the impedance of air. However, doubling the thickness of a wall (media 2) results in only 6 dB of additional sound reduction. It is common practice to use composite plates as insulating walls. This is only effective if walls whose flexural resonance frequencies do not coincide with the frequency of the sound waves are avoided.

## 14.3 Sound Absorption

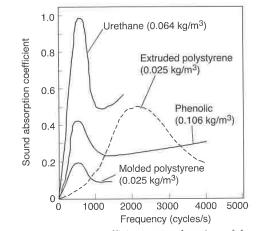
Similar to sound reflection, sound absorption is an essential property for practical noise insulation. Materials which have the same characteristic impedance as air  $(Z_1 \cup Z_2)$  are the best sound-absorbent materials. The sound waves that are not reflected back out into media 1, penetrate media 2 or the sound insulating wall. Sound waves that penetrate a polymer medium are damped out similar to that of mechanical vibrations. Hence, sound absorption also depends on the magnitude of the loss tangent  $\tan \delta$ , or logarithmic decrement  $\Delta$ , described in Chapter 9. Table 14.2 presents orders of magnitude for the logarithmic decrement for several types of materials. As expected, elastomers and amorphous polymers have the highest sound absorption properties, whereas metals have the lowest.

Table 14.2 Damping Properties for Various Materials

Material	Temperature range	Logarithmic decrement $\Delta$
Amorphous polymers	T <tg< td=""><td>0.01 to 0.1</td></tg<>	0.01 to 0.1
Amorphous polymers	T>Tg	0.1 to 1
Elastomers		0.1 to 1
Semi-crystalline polymers	Tg <t<tm< td=""><td>≈ 0.1</td></t<tm<>	≈ 0.1
Fiber reinforced polymers	Tg <t<tm< td=""><td>&lt; 0.01</td></t<tm<>	< 0.01
Wood	T <tg< td=""><td>0.01 to 0.02</td></tg<>	0.01 to 0.02
Ceramic and glass	T <tg< td=""><td>0.001 to 0.01</td></tg<>	0.001 to 0.01
Metals	T <t<sub>m</t<sub>	< 0.0001

In a material, sound absorption takes place by transforming acoustic waves into heat. Since foamed polymers have an impedance of the same order as air, they are poor reflectors of acoustic waves. This makes them ideal to eliminate multiple reflections of sound waves in *acoustic* or *sound proof rooms*. Figure 14.4 [2] presents the sound absorption coefficient for several foamed polymers as a function of the sound wave frequency. It should be noted that the speed at which sound travels in foamed materials is similar to that of the solid polymers, since foaming affects the stiffness and the density in the same proportion.

14 Acoustic Properties of Polymers 589



Sound absorption coefficients as a function of frequency for various Figure 14.4 foams.

When compared to wood, even semi-crystalline polymers are considered "sound-proof" materials. Materials with the glass transition temperature lower than room temperature are particularly suitable as damping materials. Commonly used for this purpose are thermoplastics and weakly cross-linked elastomers. Elastomer mats are often adhered on one or both sides of sheet metal, preventing resonance flexural vibrations of the sheet metal such as in automotive applications.

### References

- Offergeld, H., Ph.D Thesis, IKV, RWTH-Aachen, (1990).
   Griffin, J.D., and Skochdopole, R. E., *Engineering Design for Plastics*, E. Baer, (Ed.), Chapter 15, Robert E. Krieger Publishing Company, Huntington, (1975).

# Appendix



Polymer	Abbre-	Density		Mechanica	l properties
	viation	g/cm <sup>3</sup>	lb/in <sup>3</sup>	Tensile stre	ength
				N/mm²	psi
Low density polyethylene High density polyethylene EVA Polypropylene Polybutene-1 Polyisobutylene Poly-4-methylpent-1-ene konomers	PE-LD PE-HD EVA PP PB PIB PMP	0.914/0.928 0.94/0.96 0.92/0.95 0.90/0.907 0.905/0.920 0.91/0.93 0.83 0.94	0.0329-0.0330 0.0338-0.0345 0.0331-0.0341 0.0324-0.0327 0.0325-0.0331 0.0327-0.0334 0.0298 0.0338	8/23 18/35 10/20 21/37 30/38 2/6 25/28 21/35	1140/3270 2560/4980 1420/2840 2990/5260 4270/5400 284/853 3560/3980 2990/4980
Rigid PVC	PVC-U	1.38/1.55	0.0496-0.0557	50/75	7110/10670
Plasticized PVC	PVC-P	1.16/1.35	0.0417-0.0486	10/25	1420/3560
Polystyrene	PS	1.05	0.0378	45/65	6400/9240
Styrene/acrylonitrile copolymër	SAN	1.08	0.0392	75	10670
Styrene/polybutaliene graft polymer	SB	1.05	0.0378	26/38	3700/5400
Acrylonitrile/polybut,/styrene graft polymer	ABS	1.04/1.06	0.0374–0.0381	32/45	4550/6400
AN/AN elastomers/styrene graft polymer	ASA	1.04	0.0374	32	4550
Polymethylmethacrylate	PMMA	1.17/1.20	0.0421-0.0431	50/77	7110/10950
Polyvinylcarbazole	PVK	1.19	0.0428	20/30	2840/4270
Polyacetal	POM	1.41/1.42	0.0507-0.0511	62/70	8820/9960
Polytetrafluoroethylene	PTFE	2.15/2.20	0.0774-0.0791	25/36	3560/5120
Tetrafluoroethylene/hexafluoropropylene copolymer	FEP	2.12/2.17	0.0763-0.0781	22/28	3130/3980
Polytrifluorochlorethylene	PCTFE	2.10/2.12	0.0755-0.0762	32/40	4550/5690
Ethylene/tetrafluoroethylene	E/TFE	1.7	0.0611	35/54	4980/7680
Polyamide 6	PA 6	1.13	0.0406	70/85	9960/12090
Polyamide 66	PA 66	1.14	0.0410	77/84	10950/11950
Polyamide 11	PA 11	1.04	0.0374	56	7960
Polyamide 12	PA 12	1.02	0.0367	56/65	7960/9240
Polyamide 6-3-T	PA-6-3-T	1.12	0.0403	70/84	9960/11950
Polycarbonate	PC	1.2	0.0432	56/67	7960/9530
Polyethyleneterephthalate	PET	1.37	0.0492	47	6680
Polybutyleneterephthalate	PBT	1.31	0.0471	40	5690
Polyphenyleneether modified	PPE	1.06	0.0381	55/68	7820/9670
Polysulfone	PSU	1.24	0.0446	50/100	7110/14200
Polyphenylenesulfide	PPS	1.34	0.0483	75	10670
Polyarylsulfone	PAS	1.36	0.0490	90	12800
Polyethersulfone	PES	1.37	0.0492	85	12090
Polyarylether	PAE	1.14	0.0411	53	7540
Phenol/formaldehyde, grade 31 Urea/formaldehyde, grade 131 Melamine/formaldehyde, grade 152 Unsaturated polyester resin, grade 802 Polydiallylphthalate (GF) molding compound Silicone resin molding compound Polyimide molding	PF UF MF UP PDAP SI PI	1.4 1.5 1.5 2.0 1.51/1.78 1.8/1.9 1.43	0.0504 0.0540 0.0540 0.0720 0.0543-0.0640 0.0648-0.0684 0.0515	25 30 30 40/75 28/46 75/100	3560 4270 4270 4270 5690/10670 3980/6540 10570/14200
Epoxy resin, grade 891	EP	1.9	0.0683	30/40	4270/5690
Polyurethane casting resin	PU	1.05	0.0378	70/80	9960/11380
Thermoplastic PU-elastomers	PU	1.20	0.0432	30/40	4270/5690
Linear polyurethane (U50)	PU	1.21	0.0435	30 (σ <sub>s</sub> )	4270 (σ <sub>s</sub> )
Vulcanized fiber	VF	1.1/1.45	0.0396-0.0522	85/100	12090/14200
Celluloseacetate, grade 432	CA	1.30	0.0468	38/(σ <sub>s</sub> )	5400 (σ <sub>y</sub> )
Cellulosepropionate	CP	1.19/1.23	0.0429-0.0452	14/55	7990/7820
Celluloseacetobutyrate, grade 413	CAB	1.18	0.0425	26 (σ <sub>s</sub> )	3600 (σ <sub>y</sub> )

# Ta

Elongation	Tensile mod	ulus of elasticity	Ball indent	ation hardness	Impact	Notched in	pact strength
at break %	N/mm²	kpsi	10-s-value	10-s-value psi	strength kJ/m <sup>2</sup>	kJ/m²	ft lb/ in of notch
300/1000 100/1000 600/900 20/800 250/280 >1000 13/22 250/500	200/500 700/1400 7/120 11000/1300 250/350 - 1100/1500 180/210	28.4/71.1 99.6/199 0.99/17.1 156/185 35.6/49.8 - 156/213 25.6/29.9	13/20 40/65 - 36/70 30/38 - -	1850/2840 5690/9240  5120/9960 4270/5400  	no break no break no break no break no break no break	no break no break 3/17 4/no break no break	
10/50 170/400	1000/3500	142/498	75/155	10670/22000	no break/>20 no break	2/50 no break	0.4/20
3/4 5 25/60 15/30 40	3200/3250 3600 1800/2500 1900/2700 1800	455/462 512 256/356 270/384 256	120/130 130/140 80/130 80/120 75	17 100/18 500 18 500/19 900 11 380/18 500 11 380/17 100 10 670	5/20 8/20 10/80 70/no break no break	2/2,5 2/3 5/13 7/20 18	0.25/0.6 0.35/0.5 no break 2.5/12 6/8
2/10 - 25/70	2700/3200 3500 2800/3200	384/455 498 398/455	180/200 200 150/170	25 600/28 400 28 400 21 300/24 200	18 5 100	2 2 8	0.3/0.5 - 1/2.3
350/550 250/330 20/175 400/500	410 350 1050/2100 1100	58.3 49.8 149/299 156	27/35 30/32 65/70 65	3840/4980 4270/4550 9240/9960 9240	no break  no break	13/15 8/10	3.0 no break 2.5/2.8 no break
200/300 50/300 00 00 0/150	1400 2000 1000 1600 2000	199 284 142 228 284	75 100 75 75 160	10 670 14 200 10 670 10 670 22 800	no break no break no break no break no break	no break 15/20 30/40 10/20 13	3.0 2.1 1.8 2/5.5
00/130 0/300 5 0/60	2100/2400 3100 2000 2500	299/341 441 284 356	110 200 180	15600 28400 25600	no break no break no break no break	20/30 4 4 -	12/18 0.8/1.0 0.8/1.0 4
5/30 3 0/80 5/90	2600/2750 3400 2600 2450 2250	370/391 484 370 348 320			2 2 2 2	н н н н н н н н	1.3 0.3 1/2 1.6 8.0
4/0.8 5/1.0 6/0.9 6/1.2	5600/12000 7000/10 500 4900/9100 14000/20000 9800/15 500 6000/12000 23000/28000	796/1710 996/1490 697/1294 1990/2840 1394/2200 853/1710 3270/3980	250/320 260/350 260/410 240	35 600/45 500 39 000/49 800 37 000/58 300 34 100  -	> 6 > 6.5 > 7.0 > 4.5 = -	>1.5 >2.5 >1.5 >3.0	0.2/0.6 0.5/0.4 0.2/0.3 0.5/16 0.4/15 0.3/0.8 0.5/1.0
6 00/450 5 (r <sub>s</sub> )	21 500 4000 700 1000	99.6	-		>8 no break no break	> 3 no break 3	2/30 0.4 no break
(c <sub>s</sub> ) )/100 (c <sub>s</sub> )	2200 420/1500 1600	313 59,7/213	80/140 50 47/79 35/43	11 380/19 900 7110 6680/11 240 4980/6120	20/120 65 no break no break	15 6/20 30/35	- 2.5 1.5 4/5

(continued on next page)

MacNeil Exhibit 2117 Yita v. MacNeil IP, IPR2020-01139 Page 307



Table I (cont.) Guide Values of the Physical Properties of Plastics

Polymer	Abbre- viation	Density	
	Viation	g/cm <sup>3</sup>	lb/in <sup>3</sup>
Low density polyethylene High density polyethylene EVA Polypropylene Polybutene-1 Polyisobutylene Poly-4-methylpent-1-ene Ionomers	PE-LD PE-HD EVA PP PB PIB PMP	0.914/0.928 0.94/0.96 0.92/0.95 0.90/0.907 0.905/0.920 0.91/0.93 0.83 0.94	0.0329-0.0330 0.0338-0.0345 0.0331-0.0341 0.0324-0.0327 0.0325-0.0331 0.0327-0.0334 0.0298 0.0338
Rigid PVC	PVC-U	1.38/1.55	0.0496-0.0557
Plasticized PVC	PVC-P	1.16/1.35	0.0417-0.0486
Polystyrene	PS	1.05	0.0378
Styrene/acrylonitrile copolymer	SAN	1.08	0.0392
Styrene/polybutadiene graft polymer	SB	1.05	0.0378
Acrylonitrile/polybut./styrene graft polymer	ABS	1.04/1.06	0.0374-0.0381
AN/AN elastomers/styrene graft polymer	ASA	1.04	0.0374
Polymethylmethacrylate	PMMA	1.17/1.20	0.0421-0.0431
Polyvinylcarbazole	PVK	1.19	0.0428
Polyacetal	POM	1.41/1.42	0.0507-0.0511
Polytetrafluoroethylene	PTFE	2.15/2.20	0.0774-0.0791
Tetrafluoroethylene/hexafluoropropylene copolymer	FEP	2.12/2.17	0.0763-0.0781
Polytrifluorochlorethylene	PCTFE	2.10/2.12	0.0755-0.0762
Ethylene/tetrafluoroethylene	E/TFE	1.7	0.0611
Polyamide 6	PA 6	1.13	0.0406
Polyamide 66	PA 66	1.14	0.0410
Polyamide 11	PA 11	1.04	0.0374
Polyamide 12	PA 12	1.02	0.0367
Polyamide 6-3-T	PA-6-3-T	1.12	0.0403
Polycarbonate	PC	1.2	0.0432
Polycthyleneterephthalate	PET	1.37	0.0492
Polybutyleneterephthalate	PBT	1.31	0.0471
Polyphenyleneether modified	PPE	1.06	0.0381
Polysulfone	PSU	1.24	0.0446
Polyphenylenesulfide	PPS	1.34	0.0483
Polyarylsulfone	PAS	1.36	0.0490
Polyethersulfone	PES	1.37	0.0492
Polyarylether	PAE	1.14	0.0411
Phenol/formaldehyde, grade 31	PF	1.4	0.0504
Urea/formaldehyde, grade 131	UF	1.5	0.0540
Melamine/formaldehyde, grade 152	MF	1.5	0.0540
Unsaturated polyester resin, grade 802	UP	2.0	0.0720
Polydiallylphthalate (GF) molding compound	PDAP	1.51/1.78	0.0543-0.0640
Silicone resin molding compound	SI	1.8/1.9	0.0648-0.0684
Polyimide molding	PI	1.43	0.0515
Epoxy resin, grade 891	EP	1.9	0.0683
Polyurethane casting resin	PU	1.05	0.0378
Thermoplastic PU-elastomers	PU	1.20	0.0432
Linear polyurethane (U <sub>50</sub> )	PU	1.21	0.0435
Vulcanized fiber	VF	1.1/1.45	0.0396-0.0522
Celluloseacetate, grade 432	CA	1.30	0.0468
Cellulosepropionate	CP	1.19/1.23	0.0429-0.0452
Celluloseacetobutyrate, grade 413	CAB	1.18	0.0425

Optical properties		Water absorpt	ion
Refractive index $n_D^{20}$	Transparency	mg (4d)	% (24 h)
1.51 1.53 1.49 1.46 1.51	transparent opaque transparent/opaque transparent/opaque opaque opaque opaque transparent	<0.01 <0.01 <0.01 <0.01 <0.01	<0.01 <0.01 0.05/0.13 0.01/0.03 <0.02 <0.01 0.1/1.4
1.52/1.55	transparent/opaque transparent/opaque	3/18 6/30	0.04/0.4 0.15/0.75
1.59 1.57 	transparent transparent opaque opaque translucent/opaque	9 8 8 9 1 1 1 1 1 1 1	0.03/0.1 0.2/0.3 0.05/0.6 0.2/0.45
1.49 1.48	transparent opaque opaque	35/45 0.5 20/30	0.1/0.4 0.1/0.2 0.22/0.25
1.35 1.34 1.43 1.40	opaque transparent/translucent translucent/opaque transparent/opaque	तः तः सः	0 <0.1 0 0.03
1.53 1.53 1.52 1.53	translucent/opaque translucent/opaque translucent/opaque translucent/opaque transparent	で ま ま ま ま	1.3/1.9 1.5 0.3 0.25 0.4
1.58	transparent transparent/opaque opaque opaque	10 18/20 	0.16 0.30 0.08 0.06
.63 67 65	transparent/opaque opaque opaque transparent translucent/opaque		0.02 0.02 1.8 0.43 0.25
	opaque opaque opaque opaque opaque opaque opaque	<150 <300 <250 <45 - -	0.3/1.2 0.4/0.8 0.1/0.6 0.03/0.5 0.12/0.35 0.2 0.32
	opaque transparent translucent/opaque translucent/opaque	<30 - - 130	0.05/0.2 0.1/0.2 0.7/0.9 
50 .47 .47	opaque transparent transparent transparent	- 130 40/60 40/60	7/9 6 1.2/2.8 0.9/3.2

(continued on next page)



Polymer	Abbre-	Density		Thermal	properties			
	viation	g/cm <sup>3</sup>	lb/in³	Service te	emperatur	9		
				max/short time n		max /con	max./continuous	
				°C	°F	°C	°F	
Low density polyethylene High density polyethylene EVA = Polypropylene Polybutene-1 Polyisobutylene Poly-4-methylpent-1-ene Ionomers	PE-LD PE-HD EVA PP PB PIB PMP	0.914/0.928 0.94/0.96 0.92/0.95 0.90/0.907 0.905/0.920 0.91/0.93 - 0.83 0.94	0.0329-0.0330 0.0338-0.0345 0.0331-0.0341 0.0324-0.0327 0.0325-0.0331 0.0327-0.0334 0.0298 0.0338	80/90 90/120 65 140 130 80 180 120	176/194 194/248 149 284 266 176 356 248	60/75 70/80 55 100 90 65 120 100	140/167 158/176 131 212 194 149 248 212	
Rigid PVC Plasticized PVC	PVC-U PVC-P	1.38/1.55 1.16/1.35	0.0496-0.0557 0.0417-0.0486	75/100 55/65	167/212 131/149	65/85 50/55	149/185 122/131	
Polystyrene Styrene/acrylonitrile copolymer Styrene/polybutadiene graft Acrylonitrile/polybut./ styrene graft polymer AN/AN elastomers/ styrene graft polymer	PS SAN SB ABS ASA	1.05 1.08 1.05 1.04/1.06 1.04	0.0378 0.0392 0.0378 0.0374–0.0381 0.0374	60/80 95 60/80 85/100 85/90	140/176 203 140/176 188/212 188/194	50/70 85 50/70 75/85 70/75	122/158 185 122/158 167/185 158/167	
Polymethylmethacrylate Polyvinylcarbazole Polyacetal	PMMA PVK POM	1.17/1.20 1.19 1.41/1.42	0.0421-0.0431 0.0428 0.0507-0.0511	85/100 170 110/140	188/212 338 230	65/90 160 90/110	149/194 320 194/230	
Polytetrafluoroethylene Tetrafluoroethylene hexafluoropropylene copolymer Polytrifluorochlorethylene Ethylene tetrafluoroethylene	PTFE FEP PCTFE E/TFE	2.15/2.20 2.12/2.17 2.10/2.12 1.7	0.0774-0.0791 0.0763-0.0781 0.0755-0.0762 0.0611	300 250 180 220	572 482 356 428	250 205 150 150	482 401 302 302	
Polyamide 6 Polyamide 66 Polyamide 11 Polyamide 12 Polyamide 6-3-T	PA 6 PA 66 PA 11 PA 12 PA-6-3-T	1.13 1.14 1.04 1.02 1.12	0.0406 0.0410 0.0374 0.0367 0.0403	140/180 170/200 140/150 140/150 130/140	284/356 338/392 284/302 284/302 266/284	80/100 80/120 70/80 70/80 80/100	176/212 176/248 158/176 158/176 176/212	
Polycarbonate Polyethyleneterephthalate Polybutyleneterephthalate Polyphenyleneether modified	PC PET PBT PPE	1.2 1.37 1.31 1.06	0.0432 0.0492 0.0471 0.0381	160 200 165 150	320 392 329 302	135 100 100 80	275 212 212 176	
Polysulfone Polyphenylensulfide Polyarylsulfone Polyethersulfone Polyarylether	PSU PPS PAS PES PAE	1.24 1.34 1.36 1.37 1.14	0.0446 0.0483 0.0490 0.0492 0.0411	200 300 300 260 160	392 572 572 500 320	150 200 260 200 120	302 392 500 392 248	
Phenol/formaldehyde, grade 31 Urea/formaldehyde, grade 131 Melamine/formaldehyde, grade 152 Unsaturated polyester resin, grade 802 Polydiallylphthalate (GF) molding compound Silicone resin molding compound Delvimide molding	PF UF MF UP PDAP SI B	1.4 1.5 1.5 2.0 1.51/1.78 1.8/1.9	0.0504 0.0540 0.0540 0.0720 0.0543-0.0640 0.0648-0.0684	140 100 120 200 190/250 250	284 212 248 392 374/482 482 752	110 70 80 150 150/180 170/180	230 158 176 302 302/356 338/356 500	
Polyimide molding Epoxy resin, grade 891 Polyurethane casting resin Thermoplastic PU-elastomers Linear polyurethane (U <sub>50</sub> )	PI EP PU PU PU PU	1.43 1.9 1.05 1.20 1.21	0.0515 0.0683 0.0378 0.0432 0.0435	400 180 100 110 80	752 356 212 230 176	260 130 80 80 60	266 176 176 140	
Vulcanized fiber Celluloseacetate, grade 432 Cellulosepropionate Celluloseacetobutyrate, grade 413	VF CA CP CAB	1.1/1.45 1.30 1.19/1.23 1.18	0.0396-0.0522 0.0468 0.0429-0.0452 0.0425	180 80 80/120 80/120	356 176 176/248 176/248	105 70 60/115 60/115	221 158 140/239 140/239	

		Heat de	flection ter	mperature °F		Coefficien		Thermal	vitv	Specific heat	
			-	-						nout	
min./com	ntinuous	VSP (Vicat 5 kg)	1.86/ 0.45 N/ mm <sup>2</sup>	VSP (Vicat Ib)	264/ 66 psi	K <sup>-1</sup> ·10 <sup>6</sup>	in/in/°F • 10 <sup>-6</sup>	W/mK	BTU in/ ft²h°F	kJ/ kgK	BTU/ lb°F
°C	°F										
-50 -50 -60 0/-30 0 -50 0 -50	58 58 76 32/22 32 58 32 58	 60/70  85/100 70  	35 50 34/62 45/120 60/110 - - 38/45		93/144	250 200 160/200 150 150 120 117 120	140 110 90/110 83 83 67 65 67	0.32/0.40 0.38/0.51 0.35 0.17/0.22 0.20 0.12/0.20 0.17 0.24	2.2/2.8 2.6/3.5 2.4 1.2/1.5 1.4 0.8/1.4 1.2 1.7	2.1/2.5 2.1/2.7 2.3 2.0 1.8 2.18 2.20	8.8/10.5 8.8/11.5 9.5 8.3 7.5 - 9.1 9.2
-5 0/-20	21 32/-4	75/110 40	60/82 -	167/230 104	140/180	70/80 150/210	39/45 83/110	0.14/0.17 0.15	1.0/1.2 1.05	0.85/0.9 0.9/1.8	3.55/3.7: 3.75/7.5
-10 -20 -20 -40	14 4 40 40	78/99 - 77/95 95/110 92	110/80 104/90 104/82 80/120 100/110	172/210 - 171/203 203/230 198	230/176 219/194 219/180 176/248 212/230	70 80 70 60/110 80/110	39 45 39 33/61 44/61	0.18 0.18 0.18 0.18 0.18	1.25 1.25 1.25 1.25 1.25	1.3 1.3 1.3 1.3	5.4 5.4 5.4 5.4 5.4
40	-40	70/100	60/100	158/212	140/212	70	39	0.18	1.25	1.3	6.15
-100 - 60	-148 -76	180 160/173	- 110/170	356 320/344	- 230/338	- 90/110	 50/61	0.29 0.25/0.30	2.0 1.7/2.1	- 1.46	- 6.1
-200 -100	- 328 - 148	91 34 24	-/121 -/70	1	-/250 -/158	100 80	56 45	0.25 0.25	1.7 1.7	1.0 1.12	4.20 4.65
40 190	-40 -310	-	-/126 71/104	-	-/259 160/219	60 40	33 22	0.22 0.23	1.5 1.6	0.9 0.9	3.75 3.75
-30 -30 -70 -70 -70	-22 -22 -94 -94 -94	180 200 175 165 145	80/190 105/200 150/130 140/150 140/80	356 392 347 329 293	176/374 221/392 302/266 284/302 284/176	80 80 130 150 80	44 44 72 83 45	0.29 0.23 0.23 0.23 0.23 0.23	2.0 1.6 1.6 1.6 1.6 1.6	1.7 1.7 1.26 1.26 1.6	7.1 7.1 5.25 5.25 6.70
-100 -20 -30 -30	148 4 22 22	138 188 178 148	130/145 - 50/190 100/140	280 280 352 298	266/293  122/374 212/284	60/70 70 60 60	33/39 39 33 33 33	0.21 0.24 0.21 0.23	1.45 1.65 1.45 1.60	1.17 1.05 1.30 1.40	4.90 4.40 5.40 5.85
100 	148   		175/180 137/- - 150/160	1.1.1.1	347/356 277/- - 302/320	54 55 47 55 65	30 31 26 31 36	0.28 0.25 0.16 0.18 0.26	1.95 1.70 1.10 1.25 1.80	1.30  1.10 1.46	5.40  4.6 6.1
- - - - 50	- - - - - - 58	10 10 10 10 10 10 10 10 10 10 10	150/190 130/- 180/- 230/- 220/-	1 1 1 1	302/374 266/ 356/- 446/- 428/-	30/50 50/60 50/60 20/40 10/35	17/28 28/33 28/33 11/22 55/19	0.35 0.40 0.50 0.70 0.60	2.40 2.75 3.45 4.85 4.15	1.30 1.20 1.20 1.20	5.40 5.0 5.0 5.0 5.0 5.0
50 200	58 239	-	480/- 240/-	-	896/- 464/-	20/50 50/63	11/28 28/35	0.3/0.4 0.6/0.65	2.05/2.75 4.15/4.50	0.8/0.9	3.35/3.75
-  40 15		- - 100	200/- 90/ 	- 212	392/- 194/- -	11/35 10/20 150 210	6.1/19 5.5/11 83 12	0.88 0.58 1.7 1.8	6.1 4.0 1.15 1.25	0.8 1.76 0.5 0.4	3.35 7.30 2.10 1.65
30 40 40 40	-22 -40 -40 -40	50/63 100 60/75	 90/ 73/98 62/71	- 122/144 212 140/167		- 120 110/130 120	67 61/72 67	0.22 0.21 0.21	- 1.50 1.45 1.45	1.6 1.7 1.6	6.7 7.1 6.7

### Ta

(continued on next page)

	1400
	N
	- All
	Se site
	a.

Polymer	DIN 7728	Density		Electrical pro	operties
	Bl. 1	g/cm³	lb/in <sup>3</sup>	Volume resistivity $\Omega$ cm	Surface resistance Ω
Low density polyethylene High density polyethylene EVA Polypropylene Polybutene-1 Polyisobutylene Poly-4-methylpent-1-ene Jonomers	PE-LD PE-HD EVA PP PB PIB PMP	0.914/0.928 0.94/0.96 0.92/0.95 0.90/0.907 0.905/0.920 0.91/0.93 0.83 0.94	0.0329-0.0330 0.0338-0.0345 0.0331-0.0341 0.0324-0.0327 0.0325-0.0331 0.0327-0.0334 0.0298 0.0338	$> 10^{17} > 10^{17} < 10^{15} > 10^{17} > 10^{17} > 10^{15} > 10^{16} > 10^{16}$	$\begin{array}{c} 10^{14} \\ 10^{14} \\ 10^{13} \\ 10^{13} \\ 10^{13} \\ 10^{13} \\ 10^{13} \\ 10^{13} \\ 10^{13} \\ 10^{13} \end{array}$
Rigid PVC	PVC-U	1.38/1.55	0.0496-0.0557	$> 10^{15}$	10 <sup>13</sup>
Plasticized PVC	PVC-P	1.16/1.35	0.0417-0.0486	> 10^{11}	10 <sup>11</sup>
Polystyrene	PS	1.05	0.0378	$> 10^{16}$	$> 10^{13} > 10^{13} > 10^{13} > 10^{13} > 10^{13} > 10^{13} $
Styrene/acrylonitrile copolymer	SAN	1.08	0.0392	$> 10^{16}$	
Styrene/polybutadiene graft polymer	SB	1.05	0.0378	$> 10^{16}$	
Acrylonitrile/polybut./styrene graft polymer	ABS	1.04/1.06	0.0374–0.0381	$> 10^{15}$	
AN/AN elastomers/styrene graft polymer	ASA	1.04	0.0374	$> 10^{15}$	
Polymethylmethacrylate	PMMA	1.17/1.20	0.0421-0.0431	$> 10^{15}$	10 <sup>15</sup>
Polyvinylcarbazole	PVK	1.19	0.0428	> 10^{16}	10 <sup>14</sup>
Polyacetal	POM	1.41/1.42	0.0507-0.0511	> 10^{15}	10 <sup>13</sup>
Polytetrafluoroethylene	PTFE	2.15/2.20	0.0774-0.0791	$> 10^{18}$	$ \begin{array}{c} 10^{17} \\ 10^{16} \\ 10^{16} \\ 10^{13} \end{array} $
Tetrafluoroethylenc/hexafluoropropylene copolymer	FEP	2.12/2.17	0.0763-0.0781	> 10^{18}	
Polytrifluorochloroethylene	PCTFE	2.10/2.12	0.0755-0.0762	> 10^{18}	
Ethylene/tetrafluoroethylene	E/TFE	1.7	0.0611	> 10^{16}	
Polyamide 6 Polyamide 66 Polyamide 11 Polyamide 12 Polyamide 6-3-T	PA 6 PA 66 PA 11 PA 12 PA-6-3-T	1.13 1.14 1.04 1.02 1.12	0.0406 0.0410 0.0374 0.0367 0.0403	$ \begin{array}{c} 10^{12} \\ 10^{12} \\ 10^{13} \\ 10^{13} \\ 10^{11} \end{array} $	$ \begin{array}{c} 10^{10} \\ 10^{10} \\ 10^{11} \\ 10^{11} \\ 10^{10} \end{array} $
Polycarbonate	PC	1.2	0.0432	$> 10^{17}$	$> 10^{15}$
Polyethyleneterephthalate	PET	1.37	0.0492	$10^{16}$	$10^{16}$
Polybutyleneterephthalate	PBT	1.31	0.0471	$10^{16}$	$10^{13}$
Polyphenyleneether modified	PPE	1.06	0.0381	$10^{16}$	$10^{14}$
Polysulfone	PSU	1.24	0.0446	$> 10^{16}$	2
Polyphenylenesulfide	PPS	1.34	0.0483	> 10^{16}	2
Polyarylsulfone	PAS	1.36	0.0490	> 10^{16}	2
Polyethersulfone	PES	1.37	0.0492	10^{17}	2
Polyarylether	PAE	1.14	0.0411	> 10^{10}	3
Phenol/formaldehyde, grade 31 Urea/formaldehyde, grade 131 Melamine/formaldehyde, grade 152 Unsaturated polyester resin, grade 802 Polydiallylphthalate (GF) molding compound Silicone resin molding compound Polyimide molding	PF UF MF UP PDAP SI PI	1.4 1.5 1.5 2.0 1.51/1.78 1.8/1.9 1.43	0.0504 0.0540 0.0540 0.0720 0.0543-0.0640 0.0648-0.0684 0.0515	$\begin{array}{c} 10^{11} \\ 10^{11} \\ 11^{11} \\ > 10^{12} \\ 10^{13}/10^{16} \\ 10^{14} \\ > 10^{16} \end{array}$	$>10^{8} > 10^{10} > 10^{10} > 10^{8} > 10^{10} = 10^{13} = 10^{13} = 10^{12} > 10^{15} = 10^{15}$
Epoxy resin, grade $891$	EP	1.9	0.0683	$> 10^{14}$	$> 10^{12} \\ 10^{14} \\ 10^{11} \\ 10^{12}$
Polyurethane casting resin	PU	1.05	0.0378	$10^{16}$	
Thermoplastic PU-elastomers	PU	1.20	0.0432	$10^{12}$	
Linear polyurethane (U <sub>50</sub> )	PU	1.21	0.0435	$10^{13}$	
Vulcanized fiber Celluloseacetate, gradé 432 Cellulosepropionaté Celluloseacetobutyrate, grade 413	VF CA CP CAB	1.1/1.45 1.30 1.19/1.23 1.18	0.0396-0.0522 0.0468 0.0429-0.0452 0.0425	$ \begin{array}{c} 10^{10} \\ 10^{13} \\ 10^{16} \\ 10^{16} \end{array} $	$ \begin{array}{c} 10^8 \\ 10^{12} \\ 10^{14} \\ 10^{14} \end{array} $

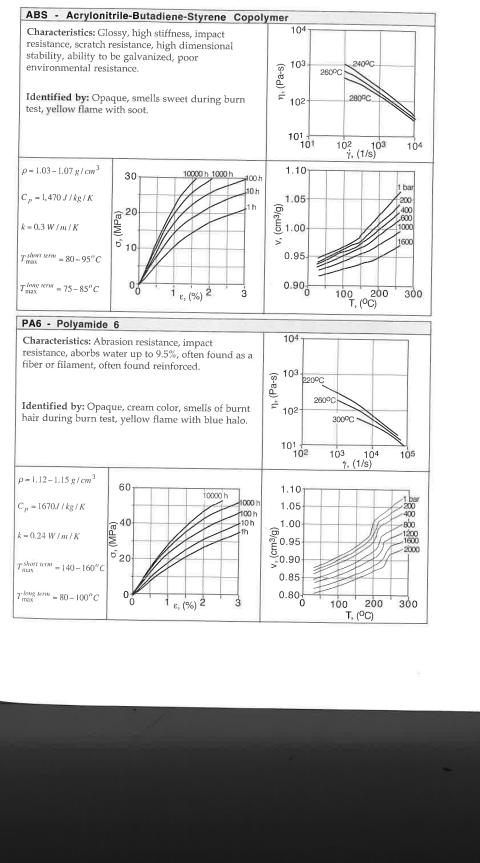
Dielectri	ic constant	Dissipation tan δ	(power) factor	Dielectric stre	ength	Tracki	ing resistance	
50 Hz	10 <sup>6</sup> Hz	50 Hz	10 <sup>6</sup> Hz	– kV/25 μm	kV/cm	KA	KB	KC
2.29 2.35 2.5/3.2 2.27 2.5 2.3 2.12	2.28 2.34 2.6/3.2 2.25 2.2 - 2.12	$ \begin{array}{c} 1.5 \cdot 10^{4} \\ 2.4 \cdot 10^{-4} \\ 0.003/0.02 \\ < 4 \cdot 10^{-4} \\ 7 \cdot 10^{-4} \\ 0.0004 \\ 7 \cdot 10^{-5} \end{array} $	$\begin{array}{c} 0.8 \cdot 10^{-4} \\ 2.0 \cdot 10^{-4} \\ 0.03/0.05 \\ < 5 \cdot 10^{-4} \\ 6 \cdot 10^{-4} \\ \hline \\ 3 \cdot 10^{-5} \end{array}$	> 700 > 700 = 800 700 230 280	 620/780 500/650  700	3b 3c - 3c 3c 3c 3c	> 600 > 600 - 600 > 600 > 600 > 600 > 600	> 600 > 600  > 600 > 600 > 600 > 600
3.5 4/8	3.0 4/4.5	0.011 0.08	0.015 0.12	200/400 150/300	350/500 300/400	2/3b -	600	600
2.5 2.6/3.4 2.4/4.7 2.4/5 3/4	2.5 2.6/3.1 2.4/3.8 2.4/3.8 3/3.5	$\frac{1/4 \cdot 10^{-4}}{6/8 \cdot 10^{-3}}$ $\frac{4/20 \cdot 10^{-4}}{3/8 \cdot 10^{-3}}$ 0.02/0.05	$\begin{array}{c} 0.5/4\cdot 10^{-4} \\ 7/10\cdot 10^{-3} \\ 4/20\cdot 10^{-4} \\ 2/15\cdot 10^{-3} \\ 0.02/0.03 \end{array}$	500 500 500 400 350	300/700 400/500 300/600 350/500 360/400	1/2 1/2 2 3a 3a	140 160 > 600 > 600 > 600	$ \begin{array}{r} 150/250 \\ 150/260 \\ > 600 \\ > 600 \\ > 600 \\ > 600 \end{array} $
3.3/3.9 3.7	2.2/3.2 3 3.7	0.04/0.06 6/10 · 10 <sup>-4</sup> 0.005	0.004/0.04 6/10 · 10 <sup>-4</sup> 0.005	300 500 700	400/500 	3c 3b 3b	>600 >600 >600	>600 >600 >600
<2.1 2.1 2.3/2.8 2.6	<2.1 2.1 2.3/2.5 2.6	$ \begin{array}{c} <2\cdot 10^{-4} \\ <2\cdot 10^{-4} \\ 1\cdot 10^{-3} \\ 8\cdot 10^{-4} \end{array} $	$ \begin{array}{c} <2 \cdot 10^{-4} \\ <7 \cdot 10^{-4} \\ 2 \cdot 10^{-2} \\ 5 \cdot 10^{-3} \end{array} $	500 500 500 380	480 550 550 400	3c 3c 3c 3c	> 600 > 600 > 600 > 600	> 600 > 600 > 600 > 600 > 600
3.8 8.0 3.7 4.2 4.0	3.4 4.0 3.5 3.1 3.0	0.01 0.14 0.06 0.04 0.03	0.03 0.08 0.04 0.03 0.04	350 400 300 300 250	400 600 425 450 350	3b 3b 3b 3b 3b 3b	> 600 > 600 > 600 > 600 > 600 > 600	> 600 > 600 > 600 > 600 > 600 > 600
3.0 4.0 3.0 2.6	2.9 4.0 3.0 2.6	$7 \cdot 10^{-4}  2 \cdot 10^{-3}  2 \cdot 10^{-3}  4 \cdot 10^{-4}$	$ \begin{array}{r} 1 \cdot 10^{-2} \\ 2 \cdot 10^{-2} \\ 2 \cdot 10^{-2} \\ 9 \cdot 10^{-4} \end{array} $	350 500 500 500	380 420 420 450	1 2 3b 1	120/160 - 420 300	260/300 - 380 300
3.1 3.1 3.9 3.5 3.14	3.0 3.2 3.7 3.5 3.10	$ \begin{array}{r} 8 & 10^{-4} \\ 4 & 10^{-4} \\ 3 & 10^{-3} \\ 1 & 10^{-3} \\ 6 & 10^{-3} \end{array} $	$\begin{array}{c} 3 \cdot 10^{-3} \\ 7 \cdot 10^{-4} \\ 13 \cdot 10^{-3} \\ 6 \cdot 10^{-3} \\ 7 \cdot 10^{-3} \end{array}$		425 595 350 400 430	1 - -	175 	175 
5 3 5 5 2 4 3 5 5	4.5 7 8 5 4 3.5 3.4	$\begin{array}{c} 0.1 \\ 0.04 \\ 0.06 \\ 0.04 \\ 0.04 \\ 0.03 \\ 2 \cdot 10^{-3} \end{array}$	$\begin{array}{c} 0.03 \\ 0.3 \\ 0.03 \\ 0.02 \\ 0.03 \\ 0.02 \\ 5 \cdot 10^{-3} \end{array}$	50/100 80/150 80/150 120	300/400 300/400 290/300 250/530 400 200/400 560	1 3a 3b 3c 3c 3c 1	140/180 > 400 > 500 > 600 > 600 > 600 > 300	125/175 >600 >600 >600 >600 >600 >600 >380
3.5/5 3.6 5.5 8.8	3.5/5 3.4 5.6 4.0	0.001 0.05 0.03 0.12	0.01 0.05 0.06 0.07	- - 330	300/400 240 300/600	3c 3c 3a -	> 300 	200/600 
5.8 4.2 3.7	- 4.6 3.7 3.5	0.08 0.02 0.01 0.006		70/180 320 350 380	- 400 400 400	 3a 3a 3a	> 600 > 600 > 600	

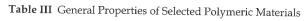
### Tal



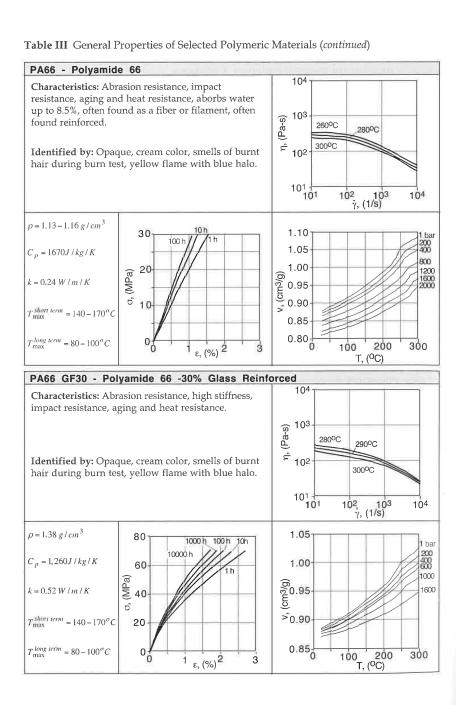
Polymer	Temper- ature	Film thickness	Water vapor	N <sub>2</sub>	Air	O <sub>2</sub>	CO <sub>2</sub>	H <sub>2</sub>	Ar	He
	°C	μm <sup>1</sup> )	g/cm² day	cm <sup>3</sup> /m <sup>2</sup> d	ay bar					
PE-LD	23	100	1	700	1100	2000	10000	8 0 0 0	. <del></del>	-
PE-HD ( $\rho = 0.95 \text{ g/cm}^3$ , unstretched)	25 30 40 50	40 40 40 40	0.9 1.7 3.5 8.1	525 720 1220 2140	754 960 1660 2650	1890 2270 3560 5650	7 1 50 8 600 13 100 19 500	6 000 7 600 11 400 16 800	5 E E E	
PE-HD ( $\rho = 0.95 \text{ g/cm}^3$ , stretched)	25 30 40 50	40 40 40 40	1.0 1.6 4.3 10.5	430 560 1050 1870	680 830 1490 2670	1210 1530 2650 4650	5900 7200 11200 18100	5000 6000 9400 14800	1.1.1	*
E/VA copolymer, VAC 20%	23	100	455	1400		4000	17000	1	-	
Polypropylene (unstretched)	25 30 40 50	40 40 40 40	2.1 3.2 7.4 19.0	430 600 1280 2800	700 960 1820 3600	1900 2500 5100 9200	6 100 8 400 14 800 27 300	17 700 18 200 28 100 46 600	1480 2100 4100 8000	1920 2170 2980 4350
Polypropylene (stretched)	25 30 40 50	40 40 40 40	0.81 1.2 3.3 8.4	200 260 560 1200	350 480 940 1850	1000 1200 2300 4150	3 300 3 900 7 050 13 200	6700 8200 12300 19800		730 850 1210 1780
PVC-U (unstretched PVC-U (stretched) PVC-P Polyvinylidenechloride	20 20 20 25	40 40 40 25	7.6 4.4 20 0.1/0.2	12 13 350 1.8/2.3	28 13 550 5/10	87 43 1500 1.7/11	200 110 8500 60/700	- 630/ 1400		18 H H
Polystyrene (stretched) Polyacetal	25 20	50 40	14.0 2.5	27 10	80 16	235 50	800 96	1260 420	-	- 5
PFEP copolymers CTFE	40 40	25 25	2.0 0.38/0.85	375 39	1.1	3000 110/230	6500 250/620	2000 3400/ 5200	-	
E/TFE copolymers E/CTFE copolymers PVF	23 23 23	25 25 25	0.6 9.0 50.0	470 150 3.8		1560 39.0 4.7	3800 1700 170	900	의 의 위 위	1.00
Polyamide 6 Polyamide 66 Polyamide 11 Polyamide 12	25 25 25 25	25 25 25 25	80/110 15/30 1.5/4.0 0.35	14 11 50 200/280		40 80 540 800/ 1400	200 140 2400 2600/ 5300	1500  5000 	र स स स	(明 (明 (明 (明
Polycarbonate	23	25	4	680	=	4000	14 500	22000	<b>3</b> 5	÷
Polyethyleneterephthalate (stretched)	23	25	0.6	9/15	=	80/110	200/340	1500	70	1
Polysulfone	23	25	6	630	-	3600	15000	28000	<b>9</b> 3	. ee
PU elastomers	23	25	13/25	550/ 1600		1000/ 4500	6000/ 22 000	-	4	4
Polyimide	23	25	25	94	-	390	700	3800	-	-
Celluloseacetate	25	25	150/600	470/630	-	1800/ 2300	13000/ 15000	14000	-	-
Celluloseacetobutyrate	25	25	460/600	3800	=	15000	94000	-	-	+

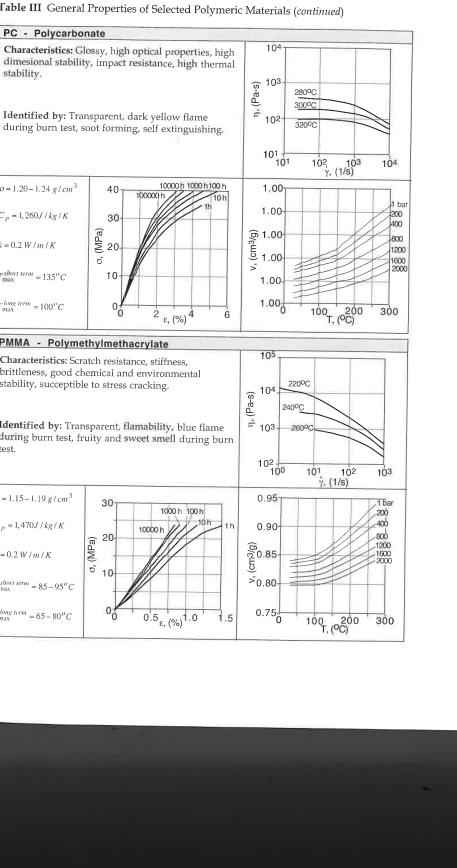
ABS	- Acryl	onitril	e-Bu	tadie
resist stabil	acteristics ance, scra lity, ability onmental	tch resi v to be	istanc galva	e, hig
Ident test, y	t <b>ified by:</b> vellow flar	Opaqu ne witł	e, sme 1 soot	ells s'
ρ = 1.03	8–1.07 g/cn	1 <sup>3</sup>	30	
	470 J / kg / K N / m / K	(MPa)	20	
T short to	<sup>rm</sup> = 80 - 95'	'с	10	V



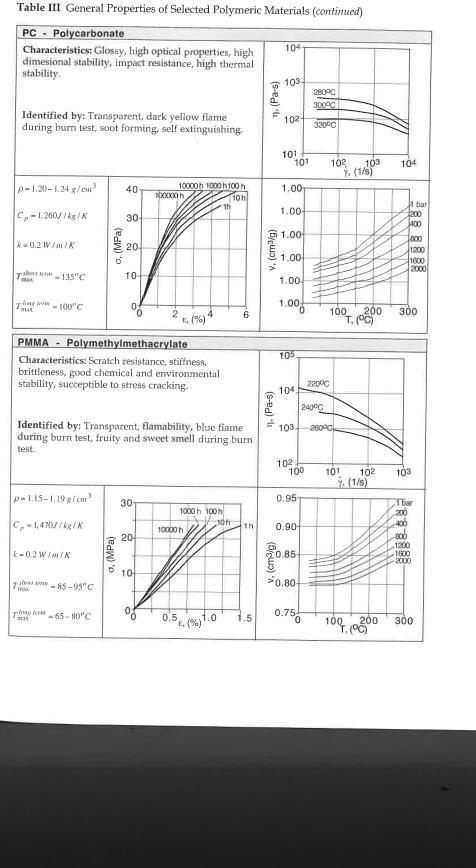




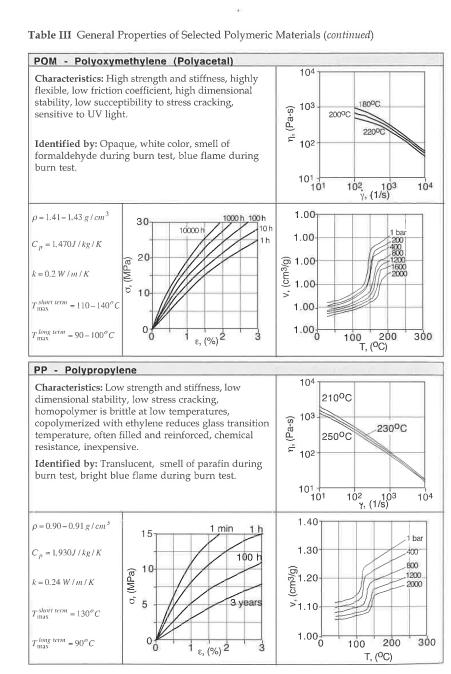


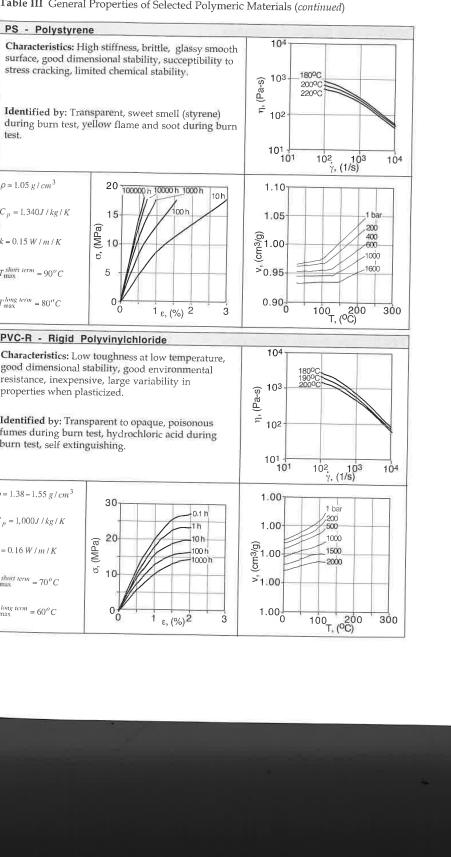


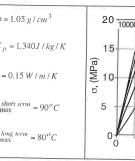
test.

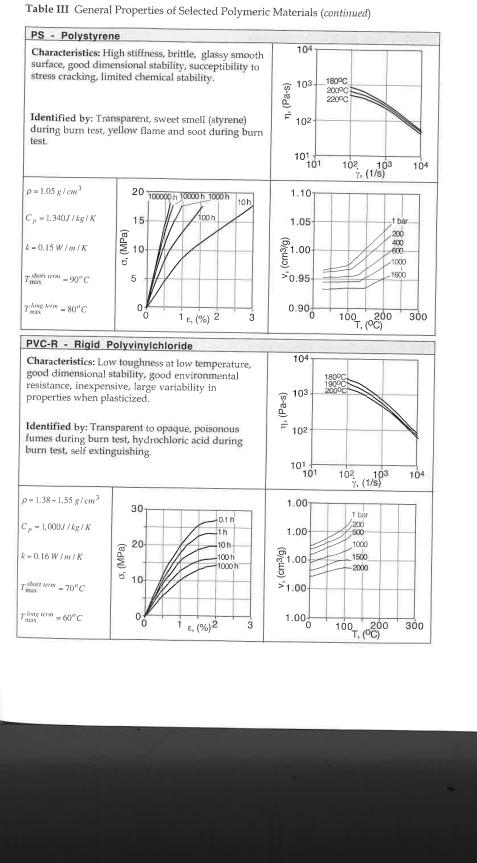














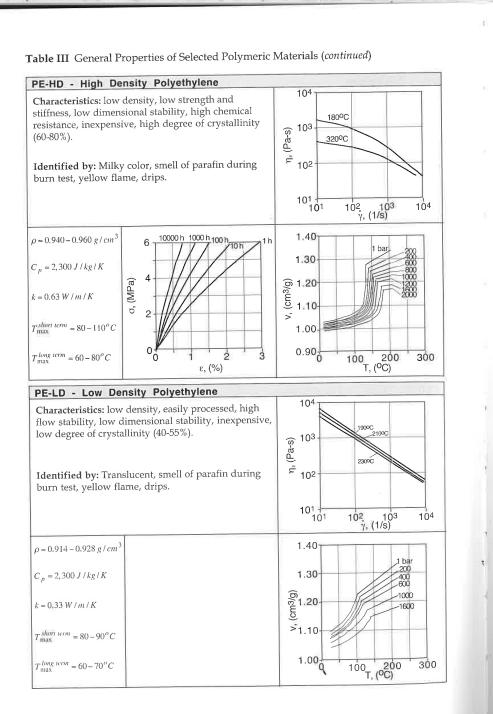


Table IV Energy Equation **Tensor** notation  $\rho C_{\nu} \frac{DT}{Dt} = \left( \nabla \cdot k \nabla T \right) + \frac{1}{2} \mu \left( \underline{\dot{\gamma}} : \underline{\dot{\gamma}} \right) + \dot{Q}$ Expanded equation in rectangular coordinates (x,y,z):  $\rho C_{\psi} \left( \frac{\partial T}{\partial t} + v_{x} \frac{\partial T}{\partial x} + v_{y} \frac{\partial T}{\partial y} + v_{z} \frac{\partial T}{\partial z} \right)$  $+2\mu\left(\left(\frac{\partial v_x}{\partial x}\right)^2 + \left(\frac{\partial v_y}{\partial y}\right)^2 + \left(\frac{\partial v_z}{\partial z}\right)^2\right) + \mu$ Expanded equation in cylindrical coordinates  $(r, \theta, z)$ :  $\rho C_{\nu} \left( \frac{\partial T}{\partial t} + v_{\ell} \frac{\partial T}{\partial r} + \frac{v_{\theta}}{r} \frac{\partial T}{\partial \theta} + v_{z} \frac{\partial T}{\partial z} \right)$  $+2\mu \left( \left( \frac{\partial v_r}{\partial r} \right)^2 + \left( \frac{1}{r} \left( \frac{\partial v_{\theta}}{\partial \theta} + v_r \right) \right)^2 + \left( \frac{\partial v_{\theta}}{\partial \theta} + v_r \right) \right)^2 + \left( \frac{\partial v_{\theta}}{\partial \theta} + v_r \right)^2 + \left( \frac{\partial v_r }{\partial \theta} + v_r \right)^2 + \left( \frac{\partial v_r }{\partial \theta} + v_r \right)^2 + \left( \frac{\partial v_r }{\partial \theta} + v_r \right)^2 + \left( \frac{\partial v_r }{\partial \theta} + v_r \right)^2 + \left( \frac{\partial v_r }{\partial \theta} + v_r \right)^2 + \left( \frac{\partial v_r }{\partial \theta} + v_r \right)^2 + \left( \frac{\partial v_r }{\partial \theta} + v_r \right)^2 + \left( \frac{\partial v_r }{\partial \theta} + v_r \right)^2 + \left( \frac{\partial v_r }{\partial \theta} + v_r \right)^2 + \left( \frac{\partial v_r }{\partial \theta} + v_r \right)^2 + \left( \frac{\partial v_r }{\partial \theta} + v_r \right)^2 + \left( \frac{\partial v_r }{\partial \theta} + v_r$ Table V Continuity Equation in Compressible fluids. Tenson notation  $\nabla \cdot \underline{\mathbf{v}} = \mathbf{0}$ Expanded equation in rectangular coordinates  $\frac{\partial v_x}{\partial x} + \frac{\partial v_y}{\partial y} + \frac{\partial v_z}{\partial z} = 0$ Expanded equation in cylindrical coordinates  $(r, \theta, z)$  $\frac{1}{r}\frac{\partial}{\partial r}(rv_r) + \frac{1}{r}\frac{\partial v_\theta}{\partial \theta} + \frac{\partial v_z}{\partial z} = 0$ 

$$= K \left( \frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2} + \frac{\partial^2 T}{\partial z^2} \right)$$
  
$$\left( \left( \frac{\partial v_x}{\partial y} + \frac{\partial v_y}{\partial x} \right)^2 + \left( \frac{\partial v_x}{\partial z} + \frac{\partial v_z}{\partial x} \right)^2 + \left( \frac{\partial v_y}{\partial z} + \frac{\partial v_z}{\partial y} \right)^2 \right) + \dot{Q}$$

$$= K \left( \frac{1}{r} \frac{\partial}{\partial r} \left( r \frac{\partial T}{\partial r} \right) + \frac{1}{r^2} \frac{\partial^2 T}{\partial \theta^2} + \frac{\partial^2 T}{\partial z^2} \right)$$

$$\frac{v_z}{\partial z} \right)^2 + \mu \left( \left( \frac{\partial v_0}{\partial z} + \frac{1}{r} \frac{\partial v_z}{\partial \theta} \right)^2 + \left( \frac{\partial v_z}{\partial r} + \frac{\partial v_r}{\partial z} \right)^2 + \left( \frac{1}{r} \frac{\partial v_r}{\partial \theta} + r \frac{\partial}{\partial r} \left( \frac{v_0}{r} \right) \right)^2 \right) + \dot{Q}$$



# **Table VI**Equation of Motion in Terms of $\underline{\underline{\tau}}$

## Tensor notation

 $\rho \frac{D\mathbf{v}}{Dt} = -\nabla p + [\nabla \cdot t] + \rho \mathbf{g}$ 

Expanded equation in rectangular coordinates (x,y,z)

 $\rho \left( \frac{\partial v_x}{\partial t} + v_x \frac{\partial v_x}{\partial x} + v_y \frac{\partial v_x}{\partial y} + v_z \frac{\partial v_x}{\partial z} \right) = -\frac{\partial \rho}{\partial x} \left( \frac{\partial \tau_{xx}}{\partial x} + \frac{\partial \tau_{yx}}{\partial y} + \frac{\partial \tau_{zx}}{\partial z} \right) + \rho g_x$   $\rho \left( \frac{\partial v_y}{\partial t} + v_x \frac{\partial v_y}{\partial x} + v_y \frac{\partial v_y}{\partial y} + v_z \frac{\partial v_y}{\partial z} \right) = -\frac{\partial \rho}{\partial y} + \left( \frac{\partial \tau_{xy}}{\partial x} + \frac{\partial \tau_{yy}}{\partial y} + \frac{\partial \tau_{zy}}{\partial z} \right) + \rho g_y$   $\rho \left( \frac{\partial v_z}{\partial t} + v_x \frac{\partial v_z}{\partial x} + v_y \frac{\partial v_z}{\partial y} + v_z \frac{\partial v_z}{\partial z} \right) = -\frac{\partial \rho}{\partial z} + \left( \frac{\partial \tau_{xx}}{\partial x} + \frac{\partial \tau_{yy}}{\partial y} + \frac{\partial \tau_{zy}}{\partial z} \right) + \rho g_z$ 

Expanded equation in cylindrical coordinates  $(r, \theta, z)$ 

$\rho\left(\frac{\partial v_r}{\partial t} + v_r\frac{\partial v_r}{\partial r} + \frac{v_\theta}{r}\frac{\partial v_r}{\partial \theta} - \frac{v_\theta^2}{r} + v_z\frac{\partial v_r}{\partial z}\right) = -\frac{\partial p}{\partial r} + \left(\frac{1}{r}\frac{\partial}{\partial x}(r\tau_{rr}) + \frac{1}{r}\frac{\partial \tau_{r\theta}}{\partial \theta} - \frac{\tau_{\theta\theta}}{r} + \frac{\partial \tau_{rz}}{\partial z}\right) + \frac{\partial v_r}{\partial z}$	ρg <sub>r</sub>
$\rho\left(\frac{\partial v_{\theta}}{\partial t} + v_{r}\frac{\partial v_{\theta}}{\partial r} + \frac{v_{\theta}}{r}\frac{\partial v_{\theta}}{\partial \theta} + \frac{v_{r}v_{\theta}}{r} + v_{z}\frac{\partial v_{\theta}}{\partial z}\right) = -\frac{1}{r}\frac{\partial p}{\partial \theta} + \left(\frac{1}{r^{2}}\frac{\partial}{\partial r}(r^{2}\tau_{r\theta}) + \frac{1}{r}\frac{\partial \tau_{\theta\theta}}{\partial \theta} + \frac{\partial \tau_{\thetaz}}{\partial z}\right)$	+ $\rho g_{\theta}$
$\rho\left(\frac{\partial v_z}{\partial t} + v_r \frac{\partial v_z}{\partial r} + \frac{v_\theta}{r} \frac{\partial v_z}{\partial \theta} + v_z \frac{\partial v_z}{\partial z}\right) = -\frac{\partial p}{\partial z} + \left(\frac{1}{r} \frac{\partial}{\partial r} (r\tau_{rz}) + \frac{1}{r} \frac{\partial \tau_{\theta z}}{\partial \theta} + \frac{\partial \tau_{zz}}{\partial z}\right) + \rho g_z$	

Table VII	Equation of Moti	
Tensor notation $\rho \frac{D\mathbf{v}}{Dt} = -\nabla p + \mathbf{v}$		
Expanded eq	uation in rectangula	
$ \rho \left( \frac{\partial v_x}{\partial t} + v_x \frac{\partial v_x}{\partial x} \right) $	$+ v_y \frac{\partial v_x}{\partial y} + v_z \frac{\partial v_x}{\partial z} \bigg) =$	
$ \rho \left( \frac{\partial v_y}{\partial t} + v_y \frac{\partial v_y}{\partial x} \right) $	$+ v_y \frac{\partial v_y}{\partial y} + v_z \frac{\partial v_y}{\partial z} =$	
$ \rho \left( \frac{\partial v_z}{\partial t} + v_x \frac{\partial v_z}{\partial x} \right) $	$+ v_y \frac{\partial v_z}{\partial y} + v_z \frac{\partial v_z}{\partial z} = -$	
Expanded equation in cylindrical		
$\rho \left( \frac{\partial v_r}{\partial t} + v_r \frac{\partial v_r}{\partial r} \right)$	$+\frac{v_{\theta}}{r}\frac{\partial v_{r}}{\partial \theta}-\frac{v_{\theta}^{2}}{r}+v_{z}\frac{\partial v_{\theta}}{\partial z}$	
$ \rho \left( \frac{\partial v_{\theta}}{\partial t} + v_r \frac{\partial v_{\theta}}{\partial r} \right) $	$+\frac{v_0}{r}\frac{\partial v_0}{\partial \theta} + \frac{v_r v_0}{r} + v_z$	

 $\left| \rho \left( \frac{\partial v_z}{\partial t} + v_r \frac{\partial v_z}{\partial r} + \frac{v_\theta}{r} \frac{\partial v_z}{\partial \theta} + v_z \frac{\partial v_z}{\partial z} \right) = - \right|$ 

tion in terms of **y** (Navier-Stokes Equations),

$$= -\frac{\partial \rho}{\partial x} + \mu \left( \frac{\partial^2 v_x}{\partial x^2} + \frac{\partial^2 v_x}{\partial y^2} + \frac{\partial^2 v_x}{\partial z^2} \right) + \rho g_x$$
$$= -\frac{\partial \rho}{\partial y} + \mu \left( \frac{\partial^2 v_y}{\partial x^2} + \frac{\partial^2 v_y}{\partial y^2} + \frac{\partial^2 v_y}{\partial z^2} \right) + \rho g_y$$
$$- \frac{\partial \rho}{\partial z} + \mu \left( \frac{\partial^2 v_z}{\partial x^2} + \frac{\partial^2 v_z}{\partial y^2} + \frac{\partial^2 v_z}{\partial z^2} \right) + \rho g_z$$

l coordinates (r,θ,z)

$$\begin{split} \frac{v_r}{\partial z} &= -\frac{\partial p}{\partial r} + \mu \left( \frac{\partial}{\partial r} \left( \frac{1}{r} \frac{\partial}{\partial r} (rv_r) \right) + \frac{1}{r^2} \frac{\partial^2 v_r}{\partial \theta^2} - \frac{2}{r^2} \frac{\partial v_\theta}{\partial \theta} + \frac{\partial^2 v_r}{\partial z^2} \right) + \rho g_r \\ \frac{\partial v_\theta}{\partial z} &= -\frac{1}{r} \frac{\partial p}{\partial \theta} + \mu \left( \frac{\partial}{\partial r} \left( \frac{1}{r} \frac{\partial}{\partial r} (rv_\theta) \right) + \frac{1}{r^2} \frac{\partial^2 v_\theta}{\partial \theta^2} - \frac{2}{r^2} \frac{\partial v_r}{\partial \theta} + \frac{\partial^2 v_\theta}{\partial z^2} \right) + \rho g_\theta \\ - \frac{\partial p}{\partial z} + \mu \left( \frac{1}{r} \frac{\partial}{\partial r} \left( r \frac{\partial v_z}{\partial r} \right) + \frac{1}{r^2} \frac{\partial^2 v_z}{\partial \theta^2} + \frac{\partial^2 v_z}{\partial z^2} \right) + \rho g_z \end{split}$$



### Α

Abbreviations 6 abs 99,102,105,450,464,476,494,497,509,510 absorption 468,469,535,543,553,555,556,563, 564 absorption index 554 acoustic properties 585 acrylic materials 547 acrylonitrile-butadiene-styrene (abs) 69 additives 71 alternating copolymers 68 amorphous thermoplastics 56,58,84,85,88,382,386,393,409,410,413,414 anisotropic strain-stress relation 422 anisotropy induced curvature change 357 Anisotropy 283,285,294,345,537,418 aramid fiber 416 arrangement of polymer molecules 55 atactic 51,53 Avrami equation 327 azodicarbonamide 262

### B

Baekeland 25,26,27 Bagley Equation 162 bakelite 22,25,26,27 Banbury Mixer 214,216 Beer's law 554 Bingham Fluid 140 biot number 347,348,351,352 bipolymer 68 birefringence 284,285,287,545,548,551,552 blackbody radiation 565 blends 203,204 block copolymers 68 blow molding 129,140,156,169,245,249 blowing agents 262 Boltzmann Superposition Principle 76,80,83, 398 Bourger's law 555 brittle failure 456,469,475,484,492-495 brittle fracture 455,456,464,484

С

calendering 185,222,224,255 caoutschouc 15,17

capacitance 521,522,528,530 capillary viscometer 149,159 Carothers 20,31-35 Castro-Macosko curing model 340

Charpy test 473,478,482 chemical degradation 511 chewing gum 76 China 39 chromaticity diagram 561,562,563 cis-1,4- polybutadiene 53 clamping unit 233,239,240 closed cell 262 co-rotating twin screw extruder 187,221-224 cokneader 220 cold feed rubber extruder 218 Colombia 39 Color 560 common polymer blends 204 compatibilizers 203 compatible polymers 204 complex current 528 complex dielectric coefficient 530 complex capacitance 530 complex modulus 401 composite laminate properties 426 compression molding 140,244,260,261,292,293, 295,297,303,308,310 condenser 521-523,528,529,542 conformation and configuration of polymer molecules 51 consistency index 138 continuity equation 608 continuum mechanics 129 convected derivative 151 corrosion of polymers 580 Couette flow 204,205 Couette Rheometer 166 Coulomb's law of friction 499 counter-rotating twin screw extruder 221,223, 259 crack growth 448,450,451,487,498 crack pinning 465 cracking 496,506,513

cavity transfer mixing section 219

cellulose acetate 285,286

crazes 457,458,464,469,470,513 crazing 457,458,459,465,486,513



creep compliance 389,390 creep modulus 389,391,400,402 creep response 389,390,392,400,402,404 creep rupture 447,456,483,485,487,489 creep rupture test 484,511 creep test 388,389,392,400,404,484 critical capillary number 211,212,213 critical energy release rate 452 critical stress intensity factor 448,516 critical surface tension 171 cross-linked elastomers 67 cross-linked polymers 418 cross-linking 67 crystalline growth rate 328,329 crystallinity 53,54,58,59,61 crystallinity for high density polyethylene 59 crystallinity for low density polyethylene 59 crystallization 322,323,326,332 cure Kinetics 336,339 curing reaction 321,334,336,337,353 curtain coating 257,259

### D

damage of polymers 447 debonding 466,496 deborah number 134 deformation dependent tensor 154 degree of crystallization 322 degree of cure 142-145,336,337 density 54,55,58,59,78,97,100,101,109,111,122 density measurements 122 desorption 571,581,582,583 deviatoric stress 131,133,140,151,176 diamagnetic substances 543 dielectric behavior 521 dielectric coefficient 521,523,524,527,530 dielectric dissipation factor 528,531,538 dielectric strength 537,538,540 dielectric susceptibility 524 dielectrical polarization 524 differencial scanning calorimer (DSC) 118, 328,336 differential thermal analysis (DTA) 117 differential viscoelastic models 151 diffusion 571,574575,576,577,583 diffusion coefficient 572,576,579,580,583 dioctylphthalate 227 dip coating 257 dispersed melting 220

dispersion index 225,226

dispersive mixing 203,208,246,266 displacement gradient tensors 155 displacement polarization 524,526 distributive mixing 203,204,211,214,219 double refractance 548 double refraction 284 drop break-up 211 ductile failure 459,484 ductile fracture 455 dynamic fatigue 488 dynamic mechanical test 393

### E

effect of orientation 205 efficiency 207,214,225 Einstein's model 146 elastic energy release rate 452 electrets 542 electric breakdown 537 electric breakdown resistance 537 electric conductivity 523,531,532,534,535 electric field intensity 522 electric resistance 532,534,542 electrical loss in a dielectric 532 electrical properties 521 electromagnetic interference shielding (EMI Shielding) 542 electron spinning resonance (ESR) 543 electrostatic charge 540 elongational viscosity 140 emulsions 140 endurance stress 486 energy balance 97 energy consumption 224 energy equation 608 engineering elastic constant 427 enthalpy 322 environmental effects 500,505 Epoxy 5,450,465,466,490 Erwin's ideal mixer 207 ethylene 43,44,55,68 ethylene propylene rubber 5 ethylene-propylene 68,70 ethylene-propylene copolymer 70 extensional rheometry 167 extrudate swell 135 extruder dimensions 188 extrusion 185,249 extrusion dies 199

### F

failure of composites 464 failure of polymers 447 falling dart test 477, fatigue 483,488 fatigue failure 496,498 fatigue test method 488 fiber attrition 312 fiber damage 312,314 fiber density continuity equation 299 fiber orientation 429 fiber reinforced polymer (FRP) 421 fiber spinning 129,140,141,245,246 fibers 4,8,10,246,260 filled polymers 378,422 fillers 225 film 243,245 film blowing 247 film casting 246,247 finger strain tensors 154 finite strain tensors 155 first contravariant convected time der 151 first normal stress differences 134,156 first-order particle interactions 146 flexural strength 49.50 flow induced birefringence 552 foaming 140,262 Folgar-Tucker Model 303,304,308,310 fountain flow effect 289-291,306 Fourier's Law 97 fracture mechanics 447,498 fracture prediction (energy balance) fracture toughness 448,477,478,479 friction 490,499 fringe order 549,550,551 frozen-in flow 346

### G

Geisbüsch model 146 general properties 3 generalized Maxwell model 83 generalized Newtonian fluid 131 geometrical crack factor 479 Gibbs free energy equation 229 Giesekus model 152 glass fiber 102-106,108,109,111,112 glass filled polyester mat 496 glass transition 45,57,59,60,63-66,86 glass transition temperature Subject Index 613

9	45,47,57,59,60,76,79,86,88 gloss 559 glossmeter 559 goniophotometer 559 graft copolymers 68 Griffith's hypothesis 452 grooved feed extruder 187,192,193,194,198 gummi elasticum 15,17 gummi plasticum 18 Guth equation 378 Guth's model 146 gutta-percha 18,23	
	н	
rivative 6 0	Halpin-Tsai model 424 haze measurement 558 heat activated cure 334 heat of crystallization 322,332 heat of fusion 107,119,123,322,332 heat transfer during cure 340 heat transfer during solidification 329 heat-distortion temperature 429 Hele-Shaw model 306 Henry's law 572 Henry-Langmuir model 574 high density polyethylene 5,135,156,374,383,384,477,484,485,501,506 high impact polystyrene 69,73,395,459,464,469,470,481,553 hookean model 399	
448	hue 562	
	immiscible fluid 208 impact failure 478 impact strength 447,464,467,506 impact test method 473 incompatible polymers 204 index of refraction 545 infrared pyrometry 565 infrared radiation 567 infrared spectrometer 564,565, infrared spectroscopy 565,563 infrared spectrom 545,564 injection molding 233,306,312,313,316 injection molding cycle 234 injection molding machine 202,238,239,240, 241,273 injection unit 238 integral viscoelastic model 154	



inter-molecular attraction 45 intrinsic viscosity 48 introduction to processing 185 isochromatic 284,285,286,551 isochronous creep plots 391 isometric creep plots 391 isotactic 52,53,63,64 izod impact test 473,474,479,481 izod-type impact machine 473

### J

J-integrals 447,453 Jeffrey Model 401

### K

Kelvin model 399 Kenics static mixer 215 kinetic theory of rubber elasticity 375 Kirchhoff's law 566 Knappe's model 106 knife coating 257,258 knitlines 293,295

### L

lamellar crystal 58 linear coefficient of thermal expansion 110, 113 linear elastic fracture mechanics (LEFM) 447, 478 linear viscoelastic fracture 448, 453 linear viscoelasticity 76,80,81 liquid crystalline polymers 416 logarithmic decrement 394,395,410 long fiber composites 421 long-term tests 388 loss modulus 87,394,398,401,407 loss tangent 395 low density polyethylene 5,54,58,102,132,134 lubricating squeezing flow 167 luminance 562 lustremeter 559

### Μ

Maddock mixing section 220 magnetic properties 543 magnetic resonance 543 magnetic susceptibility 543 magnetizability 543

Mark-Houwink relation 48 Martens temperature test 429 material derivative 130 Maxwell model 81-86 Maxwell-Wiechert Model 405 mechanical behavior 371 melamine 5 melt flow indexer 159 melt fracture 135,136 melting temperature 102,109,113,114,116 melting zone 195 memory function 154,155,156 metering zone 197 methane 51,52 methyl bromine 575 microcracks 456,457,460,466,486 513 Mixing 202 mixing activated cure 334,336,340 mixing devices 202,210,214 mixing in single screw extruder 218 mixing processes 185,202,225 mixing quality 202,214,223,225 mixing section 192,218,219,220 molding diagram 236,237 molecular bonds 45 molecular diffusion 572 molecular weight 45,56,57,61 Mooney plot 377 Mooney-Rivlin equation 376 morphological structure 325,414 morphology development 203,222 morphology development of polymer blends 203 motion equation 609

### Ν

multi-layered films 574

natural rubber 5,374,376,377,378,379,577, 581

necking 460,462,463 Neumann solution can 330 non-linear viscoelasticity 76 normal stresses 133 notched Charpy test 473 nuclear magnetic resonance (NMR) 543 nucleating agents 262 number average 46-48,50 nylon 66 497

### 0

open cell 262 optical properties 545 optimal orientation 206 orientation 206,207,208,215,219,243 251, 261,283,295,297,298 orientation (planar) 298 orientation (predicting) 297,306 orientation distribution function 298 orientation polarization 524,526 oriented thermoplastic 412

### P

p-v-T diagram 109,110-114,324 particle motion 300 particulate agglomerates 208 penetration depth 568,569 permeability 575,578,579,580 permeability properties 571,575 permeation 572,573,575 Phan-Thien Tanner models 152 phenol-formaldehyde 67 phenolic 5,67,72 photoelasticity 548 pin barrel extruder 218,219 pin mixing 219 pineapple mixing section 219 Planck's law 565 plane strain 372,373 plane stress 372 plasticating extruder 188,189 plasticating unit 202,233,238,239,244 plasticization 227 plasticized polyvinyl chloride 5 plasticized PVC 382,384,385,386,390, plasticizers 228,229,233 PMMA 380,390,391,413,431,547,557 Poincaré sections 227 Poisson's ratio 391,433 polariscope 549,550,552 polyamide 5 polyamide 6 102,104,107,227-229,23 polyamide 66 107,109,111,126,228,2 277,329,450,322 polybutadiene rubber particles 553 polybuthadiene 5 polybutylene terephthalate 420,421 polycarbonate 5,102,104,108,109,110 374,408,450,477,494,563,564 polydispersed polymer 48

Subject Index 615

	polydispersity index 48
	polyethylene
	43,44,49,54,55,58,61,132,156,168,575
	polyisobutylene 8,  76,406,407 polymethyl methacrylate 5,101,114
3,245,246,	polyoxymethylene 506
	polypropylene 5,43,53,63,72,101,107,136,139,
	140,173,322,326,327,329,332,334,388,392,395,39
8,300,310	6,408,412,419,450, 459,460,462,467,470,471,477, 577,581,582
	polypropylene copolymer 388,450
	polystyrene
	5,37,40,43,45,50,69,75,83,84,85,86,108,
	131,132,139,140,148,152,152,173,204,231,234,24
	9,262,322,329,352,395,408, 410,411,450,569
	polytetrafluoroethylene 5
	polyurethane 5
	polyvinyl chloride 43,57,58,72,73,75,477
	power law index 138,139,149,164,166
	power law model 137
	predicting orientation 297,306
	processing thermoplastic polymers 283
	processing thermoset polymers 292 pumping systems 186
	PVC fabric 121
	PVC pipes 507
	0
	$\sim$
	QSM-extruder 218
	quality 223,225,239
4,255,262	R
409	random copolymers 70
107	ratcheting 495 rate of deformation 131,141,176
569,573	Rayleigh disturbances 246
	reactive end-groups 55,56
	reduced stress 377
	Reduced viscosity 133
1	Reduced viscosity 133 Reflection 553,556
	Reduced viscosity 133 Reflection 553,556 refractive index 545,547,557
	Reduced viscosity 133 Reflection 553,556 refractive index 545,547,557 reinforced polymer 420
	Reduced viscosity 133 Reflection 553,556 refractive index 545,547,557 reinforced polymer 420 relative dielectric coefficient 522,524,527
	Reduced viscosity 133 Reflection 553,556 refractive index 545,547,557 reinforced polymer 420 relative dielectric coefficient 522,524,527 relaxation test 381,386
1 29,231,	Reduced viscosity 133 Reflection 553,556 refractive index 545,547,557 reinforced polymer 420 relative dielectric coefficient 522,524,527 relaxation test 381,386 relaxation time 77,83-87,90,91
29,231,	Reduced viscosity 133 Reflection 553,556 refractive index 545,547,557 reinforced polymer 420 relative dielectric coefficient 522,524,527 relaxation test 381,386
	Reduced viscosity 133 Reflection 553,556 refractive index 545,547,557 reinforced polymer 420 relative dielectric coefficient 522,524,527 relaxation test 381,386 relaxation time 77,83-87,90,91 representative viscosity method 163



retardation 549,550 rheology 129 rheometry 159 roll coating 257,258 rotational molding 264 rubber 3,16 rubber elasticity 373

### S

S-N curves 488,493,494 saturation 562 Schottky-Barriers 534 screw characteristic curves 190,192,194,197,198 secant modulus 381 second normal stress differences 133,134 second-order orientation 304 self-cleaning 220 self-diffusion 583 Semi-Crystalline Thermoplastics 58,381,382, 385,393,408,410,414 shark skin 135 shear modulus 57,59,61 shear thinning effect 131 sheet inflation 170 sheet molding compound (SMC) 260 sheeting dies 199 shish-kebab 326,328 short fiber composites 421 short-term tensile strength 455 short-term tensile test 371,373 silicone rubber 5 single crystals 326 single screw extruder 187,188,190,192,218, 220,239 sink marks 343,358 sinusoidal disturbance 213 sinusoidal oscillatory test 397 slurries 140 solidification 321,329 solidification of thermoplastics 322 solidification of thermosets 334 solids conveying zone 188,191 solubility constant 573 solubility parameters 230,512 solutions 574 sorption 574,575,579 sorption constant 579 sorption equilibrium constant 573 sound absorption 589 sound proof rooms 589

sound reflection 587,589 specific heat 97,98,107,119 specific resistance 535,536 spectral radiance 565,566 specular gloss 559 speed of sound 585 spherulites 58,325,326 spring-forward effect 357 spurt flow 135 squeezing flow 167,168 stabilizers 255 standard linear solid model 403 static fatigue 483 static mixers 215 Staudinger 29,32,34,35 stefan condition 332 stick-slip effect 135 storage modulus 87,398,401,407 strain 371,373,422 strain-optical coefficient 548 strength stability under heat 429 stress 371,373,400,403,405 stress cracking 344 stress intensity factor 487,498,516 stress relaxation 380,381,388,389,400,405,406 stress relaxation test 76,392,391 stress whitening 460,461 stress-optical coefficient 548 striation thickness 204 structural units 63-66 Structure of Polymers 43 styrene-butadiene-rubber (SBR) 5,374 substantial derivative 130 surface tension 170 suspension rheology 146 swelling 229,230 syndiotactic 52,53

### Т

tacticity 51,53 tangent modulus 381 tensile test 379 tensor representation of fiber orientation 304 terpolymer 68,69 thermal conductivity 100 thermal conductivity of ABS 105 thermal conductivity of LDPE 103 thermal conductivity of polyamide 6 104 thermal conductivity of polyamotate 104 thermal degradation 119,227,237,513

thermal diffusivity 98,112 Thermal Expansion 113 thermal fatigue 491,495,496 Thermal Penetration 115 thermodynamics during cooling thermoforming 130,140,169,245, thermogravimetry (TGA) 121,514 thermomechanical analysis (TMA thermoplastic polymers 51,55,58, thermosets 55,67 tie molecules 414 time-temperature superposition torsion pendulum 393 total stress 131,141 toughness 448,450,452,453,464,47 trans-1,4- polybutadiene 53 translucent 58 transmissivity 557,558,566 transmittance 553,556,567 transparency 545,553 transparent 56,58 treeing 539 trichromatic coefficients 561 tristimulus values 561 Trouton viscosity 141 tubular dies 201 twin screw extruders 187,188,202,

### U

ultra high molecular weight polye fibers 416 ultra-drawn, ultra-high molecular density polyethylene 8 ultra-violet radiation 505 Union Carbide mixing section 220 United States 19,20,22,26,29,30,40 unplasticized PVC (uPVC) 5,382,3 unsaturated polyester 334,335,342 unsaturated polyester 5 unsaturated polyester 151

### V

Van-der-Waals forces 45 Vicat temperature test 429 vinyl ester 142-144,336,337 viscoelastic flow models 151 Viscosity average 46,48 viscosity curves 132,142 Subject Index 617

	viscosity ratios 215 viscous flow models 137
	volume conductivity 535,536
	volume-specific energy absorption 469
; 322	volume-specific energy to fracture 496
,253	vulcanization 18
14	
A) 120	W
8,379	Wana an (num disting) 254
	warpage (predicting) 354
77	warpage 323,325,330,344,354,359
76	wavelength disturbance amplitude 213 wear 499
	weathering 505
79	weight average 46
	Weissenberg-Rabinowitsch Equations 162
	White-Metzner model 151
	Wien's law 565
	Williams-Landel-Ferrey (WLF) equation
	78,79,80,85-87,90,91
	wire coating 257
	X
	X groups 43,51,53
	A groups 43,31,33
	Υ
2,214,221,222	
	yield point 462
	yield strength 462
vethylene	yield stresses 140
	Young's modulus 585
r weight high	Z
	L
0	zero shear rate viscosity 139
.0 )	
,383,386	
2,361	
2,001	
ass fiber	
	2



# **Author Index**

### Α

Adams, J.M. 569 Advani, S.G. 319 Agassant, J.F. 180,569 Aklonis, J.J. 94 Alam, M. 180 Alf, E. 518 Andersen, O. 367 Andrews, E.H. 519 Anturkar, N.R. 281 Araujo, F.F.T. 128 Armstrong, R.C. 180, 181 Avenas, P. 180 Avrami, M. 367

### В

Baaijens, F.P.T. 367 Baaijens, J.P.W. 181 Baer, E. 13,544 Bagley, E.B. 182 Bailey, R. 319 Bannantine, J.A. 518 Barone, M.R. 319,367 Bartoe, W.F. 569 Batchelor, G.K. 181 Bay, R.S. 318 Beahan, P. 518 Becker, H. 319,445 Bellehumeur, C.T. 281 Benham, P.P. 519 Bentley, B.J. 280 Berezhnaya, G.V. 180 Berg, H. 544 Bernier, G.A. 519 Bernstein, B. 181 Berry, G.C. 94 Bird, R.B. 180,280,281 Biritz, L.F. 519 Biswas, A. 280 Boden, H.E. 519 Bogetti, T.A. 367 Boonstra, B.B. 280 Borisenkova, E.K. 180 Boyer, R.F. 519 Brandrup, J. 367 Brintrup, H. 445

Bucknall, C.B. 519 Burgers, J.M. 319 Bushko, W.C. 367

### С

Carreau, P.J. 95,180,181 Castiff, E. 95 Castro, J.M. 180 Catič, I. 128 Caulk, D.A. 319,367 Chapman, D. 569 Chatrei, Sh. 182 Chen, C.Y. 319 Cheng, J.I. 280 Chhabra, R.P. 95, 180 Chiang, H.H. 367 Cintra, J. S. 319 Co, A. 281 Cohen, R.E. 181 Comer, J.J. 519 Cox, R.G. 280 Crawford, R.J. 128,281,445,518,519,544 Crochet, M.J. 181,319,367 Crouthamel, D.L. 367 Crowder, M.L. 94

### D

Dalke, B.D. 94 Davies, A.R., 181 Davis, A. 519 de la Condamine, C.M. 41 De Kee, D.C.R. 95, 180 de Waale, A. 181 Dealy, J.M. 180, 181 Debbaut, B. 181 Denn, M.M. 181 Denton, D.L 281,519 Dewitt, D.P. 569 DiBenedetto, A.T. 367 Diedrich,G. 519 Dietsche, L. 181 Dietz, W. 128 Dillon, R.D. 180 Domininghaus, H. 94,445,519,544 Dooley, J. 181

DuBois, J.H. 41 Dukes, R. 519 Dupret, F. 319 Dusek, K. 367

### Е

E. Gaube 519 Eder, G. 128,367 Ehrenstein, G.W. 13,367,445,5519 Einstein, A. 181 Elemans, P.H.M. 280 Engel, L. 519 Enns, J.B. 368 Erwin, L. 280

### F

Fajolle, R. 569 Faupel, J. H. 367 Ferry, J.D. 95 Fillers, R.W. 95 Fischer, F.E. 128,367 Folgar, F.P. 319 Fox, T.G. 94 Frisch, K.C. 95 Fujimoto, T. 95

### G

Gaube, E. 519 Geisbüsch, P. 181, 318 Gillespie, J.W. 367 Gillham, J.K. 367 Godovsky, Y.K. 128 Gogos, C.G. 41,128, 280,367 Gordon, G.V. 180 Gotham, K.V. 519 Grace, H.P. 280 Gramann, P.J. 280,319 Green, J. 94 Greener, J. 280 Griffin, J.D. 590 Griffith, A.A. 518 Gumbrell, S.M. 445 Gupta, R.K. 181,319 Guth, E. 181,445

### Η

Haberstroh, E. 569 Hadley, D.W. 445 Author Index 619

Hagen, G.H.L. 181 Halpin, J.C. 445 Han, C.D. 181 Handrock, J.L. 519 Harms, E. 280 Hassager, O. 180 Hatzikiriakos, S.G. 180,181 Havlicek, I 368 Heimann, W. 569 Hele-Shaw H.S. 319 Henning, F. 445 Herrmann, H. 42 Hertzberg, R.W. 519 Hieber, C.A. 368 Hildebrand, J. 182,281 Hiltner, A. 13 Himasekhar, K. 368 Hoftyzer, P.J. 94,128,182,281,367 Hosemann, R. 445 Hrymak, A.N. 319 Huer, W. 94 Hughes, K. 181

### Ι

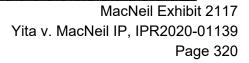
Ihm, D.W. 13 Immergut, E.H. 368 Isayev, A.I. 180,368,569

### J

Jackson, W.C. 319 Janeschitz-Kriegl, H. 128,368,569 Janssen, J.M.H. 281 Jeffery, G.B. 319

### Κ

Kabanemi, K.K. 368 Kamal, M.R. 368 Kambour, R.P. 519 Kanamoto, T. 445 Karbhari, V.M. 366 Kaufman, M. 41 Kausch, H.H. 519 Kaye, A. 181 Kearsley, E. 181 Keunings, R. 181 Kinloch, A.J. 518 Kiriakidis, D.G. 181 Kleinemeier, B. 519 Klemin, A. 41





### 620 Author Index

Klempner, D. 95 Klingele, H. 519 Knappe, W. 128,584 Knausenberber, R. 445 Kraft, H. 319 Krämer, S. 445 Krieger, S. W. 368 Krishnamachari, S.I. 445 Krobath, G. 368

### L

Lai, G.-Y. 569 Landel, R.F. 95,445 Laun, H.M. 180 Lauterbach, M. 280 Leal, L.G. 280 Lee, C.-C. 319,368 Leibfried, D. 319 Lem, K.W. 181 Levi, P. 41 Liebigs Ann. 42 Liedauer, S. 368 Lightfoot, E.N. 280 Lim, S 280 Lodge, A.S. 181,569 Löwer, K. 590 Luo, X.-L. 181

### Μ

MacKnight, W.J. 94 Macosko, C.W. 180,181,280,368 Malkin, A.Y., 180 Manas-Zloczower, I. 280 Manson, J.A. 519 Marchal, J.M. 181 Mascia, L. 281 Mathot, V.B.F.128 Mavrides, H. 319 Maxwell, J.C. 128 McPherson, A.T. 41 Medalia, A.I. 280 Meissner, J. 182 Menges, G. 181,280,281,318,367,444,445,519, 590 Meredith, R.E. 128 Michaeli, W. 181,280 Milliken, W.J. 181 Mitsoulis, E. 181 Mittal, R.K. 319 Mooney, M. 445

Moore, E.R. 94 Mullins, L. 445 Münstedt, H. 95,181

### Ν

Nagasawa, M. 95 Ng, K.Y. 280 Nicolay 519 Nielsen, L.E. 445 Nir, A. 280 Noriega M. del P. 42

### 0

O'Neill, J.M. 368 O'Toole, J.L. 445 Offergeld, H. 590 Ogale, A.M. 94 Orbey, N. 181 Osswald, T.A. 280,281,319,367,368 Ostwald, W. 181 Ott, S. 319 Owen, M.J. 519 Owens, D.K 182 Ozaki, M. 95

### Р

Pagano, N.J. 445 Palmese, G.R. 368 Papanastasiou, A.C. 181 Paulik, Ch. 128 Pazek, D.J. 95 Perry, S.J. 181 Plati, E. 519 Poiseuille, L.J. 181 Powell, P.C. 445 Powell, R.L. 181 Progelhof, R.C. 42 Pütz, D. 590

### Q

Quantin, J.C. 569

### R

Rabinowitch, E. 368 Rabinowitsch, B. 182 Randell, D.R. 368 Rauwendaal, C. 280 Reboul, J.-P. 545

### Regnault, H.V. 42 Rest, H. 519 Retting, W. 445 Rice, J.R. 518 Richard, K. 519 Richmond, J. C. 569 Riddell, M.N. 519 Rietveld, J.X. 569 Rivlin, R.S. 445 Rogers, C.E. 590 Rogers, T.G. 367 Rosato, D.V. 281,590 Rosen, S.L. 94,281 Rosenberg, H.M. 128 Roskothen, H.J. 519 Ruhnke, G.M. 519

### $\mathbf{S}$

Santhanam, N. 368 Saunders, D.W. 445 Schacht, T. 319 Schaper, H. 519 Schmachtenberg, E. 445 Schultz, J.M. 519 Schümmer, P. 182 Scott, R.L. 182,280,281 Scriven, L.E. 181 Sharma, P.K. 319 Sharples, A. 368 Shaw, M.T. 180 Shutov, F.A. 281 Simha, R. 181,445 Sims, D. 519 Skibo, M.D. 519 Skochdopole, R.E. 590 Smallwood, H.M. 445 Smith P. 13 Smith, T.R. 519 Sonntag, R. 41 Sornberger, G. 569 Spencer, A.J.M. 368 Spencer, R.S. 180 Staudinger, H. 94 Stefan, J. 368 Stern, H.J. 41 Stevenson, J.F. 280 Steward, W.E. 280 Stokes, V.K. 368 Stone, H.A. 280 Stradins, L. 280

Author Index 621

Suchanek, H. 590 Suetsugu 280 Sun, E.M. 319 Sundararaj, U. 280

### Т

Tadmor, Z. 41,128,280,281,367 Termonia, Y. 13 Thieltges, H.-P. 319 Thimm, Th. 445 Throne, J.L. 42 Timoshenko, S. P. 368 Tobias, C.W. 128 Tobin, N.R. 445 Tobolsky, A.V.J. 95 Treloar, L.R.G. 445 Trouton, F.T. 181 Tsai, S.W. 445 Tschoegl, N.W. 95 Tseng, S.C. 367,368 Tucker III, C.L. 180,319 Turng, L.S. 280

### U

Ulrich, H. 42 Utracki, L.A. 42,280

### $\mathbf{V}$

van Krevelen, D. W. 94,128,182,281,367,590 Vergnes, B. 569 Verleye, V. 319 Vincent, P.I. 518 Vinogradov, G.V. 180 Vlachopoulos, J. 180,281,319

### W

Wagner, H. 367,544 Wagner, M.H. 181 Walters, K. 181 Wang, K.K. 368 Ward, I.M. 445 Weinand, D. 569 Wende, A. 445 Wendt, R.C. 182 Weng, M. 445 White, J.L. 280 Wiest, J.M. 180 Williams, M.L. 95



### 622 Author Index

Williams, J.G. 519
Wimberger-Friedl, R. 318,368,569
Winkel, E. 367
Winter, H.H. 182
Wippel, H. 128
Wissbrun, K.F. 180
Woebken, W. 318
Wortberg, F. 181
Worthoff, R.H. 182
Wu, S. 182
Wu, S. 182
Wübken, G. 95,319,368
Wübken, W. 318

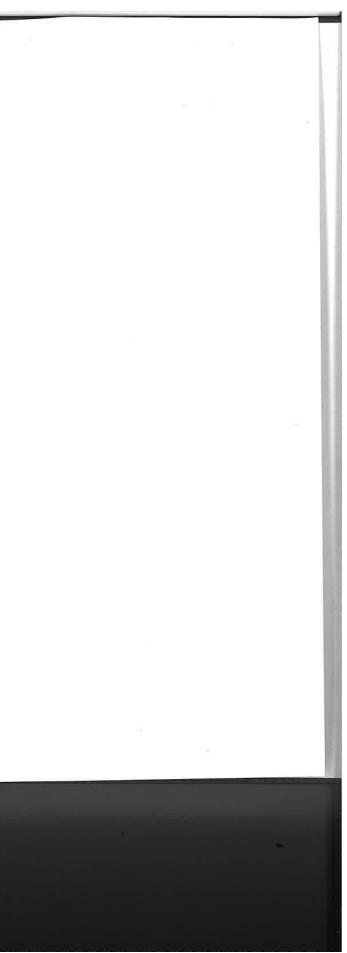
## Y

Yanovskii, Y.G. 180 Yarlykov, B.V. 180 Yasuda, K. 181 Young, R.J. 518

### Z

3

Zachariades, A.E. 445 Zapas, L. 181 Zisman, W.A. 182





in three major sections:

- properties of polymers
- processes.
- permeability of polymers.

A new chapter introducing polymers from a historical perspective not only makes the topic less dry, but also sheds light on the role polymers played, for better and for worse, in shaping today's industrial world.

The first edition was praised for the vast number of graphs and data that can be used as a reference. A new table in the appendix containing material property graphs for several polymers further strengthens this attribute.

The most important change made to this edition is the introduction of real-world examples and a variety of problems at the end of each chapter.

ISBN 1-56990-348-4 Hanser Gardner Publications http://www.hansergardner.com

ISBN 3-446-22464-5 Carl Hanser Verlag http://www.hanser.de

This unified approach to polymer materials science is divided

 Basic Principles – covering historical background, basic material properties, molecular structure, and thermal

• Influence of Processing on Properties – tying processing and design by discussing rheology of polymer melts, mixing and processing, the development of anisotropy, and solidification

• Engineering Design Properties – covering the different properties that need to be considered when designing a polymer component – from mechanical properties to failure mechanisms, electrical properties, acoustic properties, and

