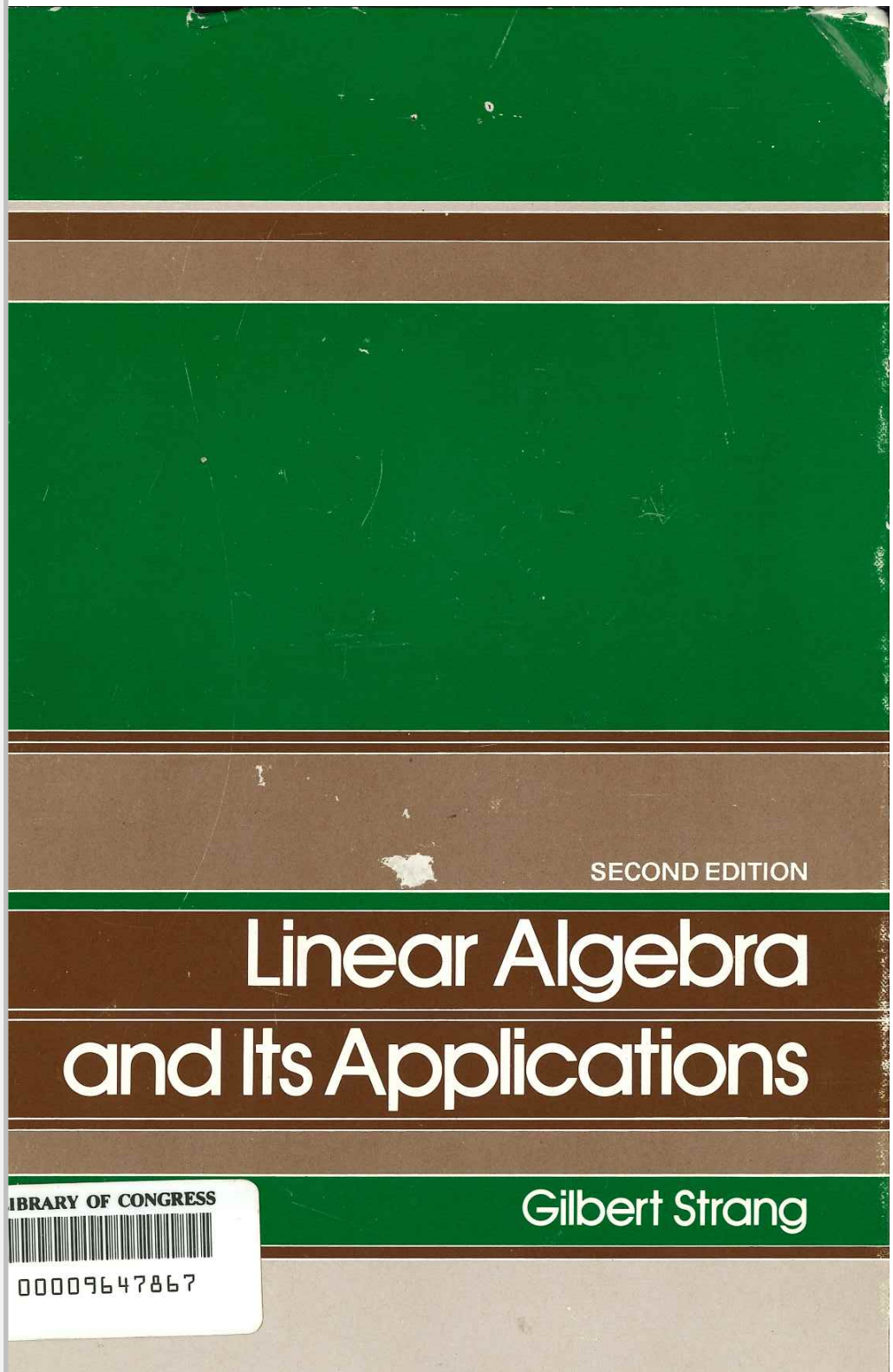

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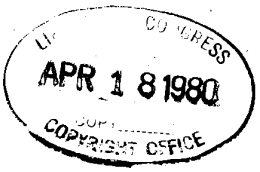

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ACADEMIC PRESS, INC.
111 Fifth Avenue, New York, New York 10003

United Kingdom Edition published by
ACADEMIC PRESS, INC. (LONDON) LTD.
24/28 Oval Road, London NW1 7DX

ISBN: 0-12-673660-X
Library of Congress Catalog Card Number: 79-53993

PRINTED IN THE UNITED STATES OF AMERICA

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CONTENTS

Preface ix

1 GAUSSIAN ELIMINATION

1.1 Introduction 1
1.2 An Example of Gaussian Elimination 2
1.3 Matrix Notation and Matrix Multiplication 6
1.4 Gaussian Elimination = Triangular Factorization 19
1.5 Row Exchanges, Inverses, and Transposes 26
1.6 Band Matrices, Applications, and Roundoff 37
Review Exercises 45

2 THE THEORY OF SIMULTANEOUS LINEAR EQUATIONS

2.1 Vector Spaces and Subspaces 48
2.2 The Solution of m Equations in n Unknowns 55
2.3 Linear Independence, Basis, and Dimension 62
2.4 The Four Fundamental Subspaces 71
2.5 Orthogonality of Vectors and Subspaces 80
2.6 Pairs of Subspaces and Products of Matrices 92
Review Exercises 100

3 ORTHOGONAL PROJECTIONS AND LEAST SQUARES

3.1 Inner Products and Projections onto Lines 103
3.2 Projections onto Subspaces and Least Squares Approximations 111
3.3 Orthogonal Bases, Orthogonal Matrices, and Gram–Schmidt Orthogonalization 121

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3.4	The Pseudoinverse and the Singular Value Decomposition	137
3.5	Weighted Least Squares	145
	Review Exercises	150

4 DETERMINANTS

4.1	Introduction	153
4.2	The Properties of the Determinant	155
4.3	Formulas for the Determinant	161
4.4	Applications of Determinants	169
	Review Exercises	177

5 EIGENVALUES AND EIGENVECTORS

5.1	Introduction	179
5.2	The Diagonal Form of a Matrix	190
5.3	Difference Equations and the Powers A^k	195
5.4	Differential Equations and the Exponential e^{At}	205
5.5	The Complex Case: Hermitian and Unitary Matrices	217
5.6	Similarity Transformations and Triangular Forms	231
	Review Exercises	240

6 POSITIVE DEFINITE MATRICES

6.1	Minima, Maxima, and Saddle Points	243
6.2	Tests for Positive Definiteness	249
6.3	Semidefinite and Indefinite Matrices; $Ax = \lambda Bx$	256
6.4	Minimum Principles and Rayleigh's Quotient	264
6.5	The Rayleigh–Ritz Principle and Finite Elements	273

7 COMPUTATIONS WITH MATRICES

7.1	Introduction	279
7.2	The Norm and Condition Number of a Matrix	280
7.3	The Computation of Eigenvalues	287
7.4	Iterative Methods for $Ax = b$	297

8 LINEAR PROGRAMMING AND GAME THEORY

8.1	Linear Inequalities	305
8.2	The Simplex Method	311
8.3	The Theory of Duality	323
8.4	Network Models	334
8.5	Game Theory and the Minimax Theorem	339

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