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WIRELESS COMMUNICATIONS  
DESIGN HANDBOOK  
*Aspects of Noise, Interference,  
and Environmental Concerns*

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VOLUME 1: SPACE INTERFERENCE

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## Chapter 6 | Noise Representations in Transponders and Multiple Access

### 6.0 Introduction

At the heart of a satellite communications system is the transponder. The transponder consists of input and output filters, up and down converters, phase-locked loops, and traveling wave tube amplifiers (TWTAs.) More modern transponder systems are using solid state power amplifiers (SSPAs). We now consider the nonlinear behavior of the transponder. A block diagram representation of a typical transponder was shown in Figure 5.36.

Let the input of the transponder be represented by

$$S_i(t) = A \cos(\omega_c t + f(\theta)), \quad (6.1)$$

where  $\omega_c = 2\pi f_c$  is the angular carrier frequency and phase of the input signal. The transponder output can be represented as

$$S_{out} = g(A)\cos(\omega_c t + f(\theta) + f(A)). \quad (6.2)$$

If  $g(A)$  and  $f(A)$  are independent of  $\omega_c$ , let  $A_k(t)$ ,  $\omega_c + \omega_k$ , and  $f_k(\theta(t))$  denote the envelope, the angular carrier frequency, and the phase of the  $k$ th carrier.  $\omega_c$  is the midband frequency or center frequency, which can take any value within a transponder bandwidth. For  $m$  number of modulated carriers, access to a transponder input can be represented by

$$\begin{aligned} S_i(t) &= \sum_{k=1}^m A_k(t) \cos\{(\omega_c + \omega_k)t + f_k(\theta(t))\} = \left[ \sum_{k=1}^m A_k(t) \cos(\omega_k t + f_k(\theta(t))) \right] \cos \omega_c t \\ &\quad - \left[ \sum_{k=1}^m A_k(t) \sin(\omega_k t + f_k(\theta(t))) \right] \sin \omega_c t \\ &= X(t) \cos \omega_c t - Y(t) \sin \omega_c t = \sqrt{X^2 + Y^2} \cos \left[ \omega_c t + \tan^{-1} \frac{Y}{X} \right] \\ &= \text{Re} \left\{ \sqrt{X^2 + Y^2} \exp \left[ j\omega_c t + j \tan^{-1} \left( \frac{Y}{X} \right) \right] \right\}. \end{aligned} \quad (6.3)$$

The corresponding transponder output is

$$\begin{aligned} S_{\text{out}}(t) &= \text{Re} \left\{ g(\sqrt{X^2 + Y^2}) \cdot \exp \left[ j\omega_c t + \tan^{-1} \left( \frac{Y}{X} \right) + jf(\sqrt{X^2 + Y^2}) \right] \right\} \\ &= \text{Re} \left\{ g(\sqrt{X^2 + Y^2}) \cdot \exp \left[ jf(\sqrt{X^2 + Y^2}) \right] \frac{(X + jY)}{\sqrt{X^2 + Y^2}} \exp(j\omega_c t) \right\}. \end{aligned} \quad (6.4)$$

Define the double Fourier transform

$$\begin{aligned} L(u, v) &= \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \frac{g(\sqrt{X^2 + Y^2})}{\sqrt{X^2 + Y^2}} \exp \left[ jf(\sqrt{X^2 + Y^2}) \right] \\ &\quad (X + jY) \exp[-juX - jvY] dx dy, \end{aligned}$$

which means

$$\begin{aligned} g(\sqrt{X^2 + Y^2}) \exp \left[ jf(\sqrt{X^2 + Y^2}) \right] \frac{(X + jY)}{\sqrt{X^2 + Y^2}} \\ = \frac{1}{2\pi} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} L(u, v) \exp[juX + jvY] du dv. \end{aligned}$$

Therefore,

$$S_{\text{out}}(t) = \frac{1}{(2\pi)^2} \text{Re} \left[ \exp(j\omega_c t) \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} L(u, v) \exp[juX + jvY] du dv \right].$$

After further mathematical manipulations,

$$\begin{aligned} S_{\text{out}}(t) &= \text{Re} \left\{ \exp(j\omega_c t) \sum_{K_1=-\infty}^{\infty} \sum_{K_2=-\infty}^{\infty} \dots \sum_{K_n=-\infty}^{\infty} \right. \\ &\quad \left. \exp \left[ jK_1(\omega_1 t + f(\theta_1)) + jK_2(\omega_2 t + f(\theta_2)) \right. \right. \\ &\quad \left. \left. + \dots + jK_n(\omega_n t + f(\theta_n)) \right] \cdot N(k) \right\}, \end{aligned}$$

where  $K_1, K_2, \dots, K_n$  can be zero or any integers either positive or negative, and

$$\begin{aligned} N(k) &= \frac{1}{(2\pi)^2} \int_{-\infty}^{\infty} \frac{g(\sqrt{X^2 + Y^2})}{\sqrt{X^2 + Y^2}} \exp[jf(\sqrt{X^2 + Y^2})] (X + jY) \prod_{\ell=1}^m J_{K_\ell}(A_\ell \sqrt{u^2 + v^2}) \\ &\quad \times \exp \left[ j \sum_{\ell=1}^m K_\ell \tan^{-1} \frac{u}{v} \right] \exp[-jux - jvy] dx dy du dv, \end{aligned} \quad (6.5)$$

where  $J_K$  is the  $K$ th-order Bessel function. Using the polar coordinate transformation

$$\begin{aligned} X &= \rho \cos \xi, & u &= \gamma \sin \eta \\ Y &= \rho \sin \xi, & v &= \gamma \cos \eta \end{aligned}$$

and performing the integration on  $\xi$  and  $\eta$  simplifies the expression to the following two cases. For  $K_1 + K_2 + \dots + K_n = 1$ ,

$$N(k) = \int_0^{\infty} \int_0^{\infty} \gamma \prod_{\ell=1}^m J_{K_\ell}(A_\ell \gamma) \rho g(\rho) \exp(jf(\rho)) \cdot J_1(\gamma \rho) d\gamma d\rho$$

and for  $K_1 + K_2 + \dots + K_n \neq 1$ ,  $N(k) = 0$ .

Finally, the output of the transponder can be expressed as

$$S_{\text{out}}(t) = \text{Re}\{N(k) \exp[j(\bar{\omega} t + f_{\bar{\ell}}^{-}(\theta))]\}, \quad (6.6)$$

where

$$\begin{aligned} f_{\bar{\ell}}^{-}(\theta) &= \sum_{\ell=1}^m K_\ell f_\ell(\theta) \\ \bar{\omega} &= \omega_c + \sum_{\ell=1}^m K_\ell \omega_\ell. \end{aligned}$$

In the case of numerical computation, the factor  $g(\rho)\exp[jf(\rho)]$  can be approximated by

$$g(\rho)\exp[jf(\rho)] = \sum_{\ell=1}^L b_\ell J_1(\alpha \ell \rho),$$

where  $L$  is the number of coefficients needed,  $J_1$  is the first-order Bessel function, and  $\alpha = 2\pi/(\text{period of the Fourier series})$ . For a given transponder, the characteristics  $g(\rho)$  and  $f(\rho)$  are known. Since  $g(\rho)$  and  $f(\rho)$  are given, the coefficients  $b_\ell$  can be obtained by an approximation, and  $N(k)$  reduces to

$$N(k) = \sum_{\ell=1}^L b_\ell \prod_{\ell=1}^m J_{K_\ell}(\alpha \ell A_\ell), \quad (6.7)$$

which outlines the amplitude for each input signal. The  $b_\ell$  are determined by best fit from the input data of  $g(\rho)$  and  $f(\rho)$  in terms of least-square error. Computer programs can calculate  $S_{\text{out}}(t)$  when  $S_i(t)$ ,  $g(\rho)$ , and  $f(\rho)$  are given.

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