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Brown University Department of Computer Science Technical Report No. 92–18 Revised version, April 1992 (Formerly Technical Report No. CS-91-45)

Appears in *Image and Text Compression*, James A. Storer, ed., Kluwer Academic Publishers, Norwell, MA, 1992, pages 85–112.

A shortened version appears in the proceedings of the International Conference on Advances in Communication and Control (COMCON 3), Victoria, British Columbia, Canada, October 16–18, 1991.

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PRACTICAL IMPLEMENTATIONS OF ARITHMETIC CODING¹

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Abstract

We provide a tutorial on arithmetic coding, showing how it provides nearly optimal data compression and how it can be matched with almost any probabilistic model. We indicate the main disadvantage of arithmetic coding, its slowness, and give the basis of a fast, space-efficient, approximate arithmetic coder with only minimal loss of compression efficiency. Our coder is based on the replacement of arithmetic by table lookups coupled with a new deterministic probability estimation scheme.

Index terms: Data compression, arithmetic coding, adaptive modeling, analysis of algorithms, data structures, low precision arithmetic.

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²Support was provided in part by NASA Graduate Student Researchers Program grant NGT– 50420 and by a National Science Foundation Presidential Young Investigators Award grant with matching funds from IBM. Additional support was provided by a Universities Space Research Association/CESDIS associate membership.

³Support was provided in part by National Science Foundation Presidential Young Investigator Award CCR-9047466 with matching funds from IBM, by NSF research grant CCR-9007851, by Army Research Office grant DAAL03-91-G-0035, and by the Office of Naval Research and the Defense Advanced Research Projects Agency under contract N00014-91-J-4052 ARPA Order No. 8225. Additional support was provided by a Universities Space Research Association/CESDIS associate membership.

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1 Data Compression and Arithmetic Coding

Data can be compressed whenever some data symbols are more likely than others. Shannon [54] showed that for the best possible compression code (in the sense of minimum average code length), the output length contains a contribution of $-\lg p$ bits from the encoding of each symbol whose probability of occurrence is p. If we can provide an accurate model for the probability of occurrence of each possible symbol at every point in a file, we can use arithmetic coding to encode the symbols that actually occur; the number of bits used by arithmetic coding to encode a symbol with probability p is very nearly $-\lg p$, so the encoding is very nearly optimal for the given probability estimates.

In this paper we show by theorems and examples how arithmetic coding achieves its performance. We also point out some of the drawbacks of arithmetic coding in practice, and propose a unified compression system for overcoming them. We begin by attempting to clear up some of the false impressions commonly held about arithmetic coding; it offers some genuine benefits, but it is not the solution to all data compression problems.

The most important advantage of arithmetic coding is its flexibility: it can be used in conjunction with any model that can provide a sequence of event probabilities. This advantage is significant because large compression gains can be obtained only through the use of sophisticated models of the input data. Models used for arithmetic coding may be adaptive, and in fact a number of independent models may be used in succession in coding a single file. This great flexibility results from the sharp separation of the coder from the modeling process [47]. There is a cost associated with this flexibility: the interface between the model and the coder, while simple, places considerable time and space demands on the model's data structures, especially in the case of a multi-symbol input alphabet.

The other important advantage of arithmetic coding is its optimality. Arithmetic coding is optimal in theory and very nearly optimal in practice, in the sense of encoding using minimal average code length. This optimality is often less important than it might seem, since Huffman coding [25] is also very nearly optimal in most cases [8,9, 18,39]. When the probability of some single symbol is close to 1, however, arithmetic coding does give considerably better compression than other methods. The case of highly unbalanced probabilities occurs naturally in bilevel (black and white) image coding, and it can also arise in the decomposition of a multi-symbol alphabet into a sequence of binary choices.

The main disadvantage of arithmetic coding is that it tends to be slow. We shall see that the full precision form of arithmetic coding requires at least one multiplication per event and in some implementations up to two multiplications and two divisions per event. In addition, the model lookup and update operations are slow because of the input requirements of the coder. Both Huffman coding and Ziv-Lempel [59, 60] coding are faster because the model is represented directly in the data structures

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