

Ralph E Jacobson • Sidney F Ray  
Geoffrey G Attridge • Norman R Axford

# THE MANUAL OF Photography

Photographic and Digital Imaging



NINTH EDITION



Focal Press

# **The Manual of Photography**

Ninth Edition



---

# **The Manual of Photography**

## Photographic and digital imaging

---

Ninth Edition

**Ralph E. Jacobson**

MSc, PhD, CChem, FRSC, ASIS Hon., FRPS,  
FBIPP

**Sidney F. Ray**

BSc, MSc, ASIS, FBIPP, FMIPA, FRPS

**Geoffrey G. Attridge**

BSc, PhD, ASIS, FRPS

**Norman R. Axford**


BSc



**Focal Press**

OXFORD AUCKLAND BOSTON JOHANNESBURG MELBOURNE NEW DELHI

Focal Press  
An imprint of Butterworth-Heinemann  
Linacre House, Jordan Hill, Oxford OX2 8DP  
225 Wildwood Avenue, Woburn, MA 01801-2041  
A division of Reed Educational and Professional Publishing Ltd

 A member of the Reed Elsevier plc group

*The Ilford Manual of Photography*

First published 1890  
Fifth edition 1958  
Reprinted eight times

*The Manual of Photography*

Sixth edition 1970  
Reprinted 1971, 1972, 1973, 1975  
Seventh edition 1978  
Reprinted 1978, 1981, 1983, 1987  
Eighth edition 1988  
Reprinted 1990, 1991, 1993, 1995 (twice), 1997, 1998  
Ninth edition, 2000

© Reed Educational and Professional Publishing Ltd 2000

All rights reserved. No part of this publication may be reproduced in any material form (including photocopying or storing in any medium by electronic means and whether or not transiently or incidentally to some other use of this publication) without the written permission of the copyright holder except in accordance with the provisions of the Copyright, Designs and Patents Act 1988 or under the terms of a licence issued by the Copyright Licensing Agency Ltd, 90 Tottenham Court Road, London, England W1P 0LP. Applications for the copyright holder's written permission to reproduce any part of this publication should be addressed to the publishers

Under the terms of the Copyright, Designs and Patents Act 1988, Sidney Ray asserts his moral rights to be identified as an author of this multi-authored work

**British Library Cataloguing in Publication Data**

The manual of photography: photographic and digital imaging – 9th ed.

1. Photography – Handbooks, manuals, etc.  
I. Jacobson, Ralph E. (Ralph Eric), 1941–  
771

ISBN 0 240 51574 9

**Library of Congress Cataloguing in Publication Data**

The manual of photography: photographic and digital imaging. – 9th ed./Ralph E. Jacobson ... [et al.].

p.cm.

Originally published in 1890 under the title: The Ilford manual of photography.

Includes bibliographical references and index

ISBN 0 240 51574 9 (alk. paper)

1. Photography. I. Jacobson, R. E.

TR145 .M315 2000

771–dc21

00-042984

Composition by Genesis Typesetting, Rochester  
Printed and bound in Great Britain



FOR EVERY TITLE THAT WE PUBLISH, BUTTERWORTH-HEINEMANN  
WILL PAY FOR BTCV TO PLANT AND CARE FOR A TREE.



# Contents

<b>Preface to the first edition of <i>The Ilford Manual of Photography</i> (1890)</b>	<b>ix</b>	The lens conjugate equation	45
<b>Preface to the ninth edition</b>	<b>xi</b>	Field angle of view	48
<b>1 Imaging systems</b>	<b>1</b>	Covering power of a lens	49
Ralph E. Jacobson		Geometric distortion	49
The production of images	1	Depth of field	50
Photographic and digital imaging	2	Depth of field equations	53
General characteristics of reproduction systems	5	Depth of focus	56
Imaging chains	6	Perspective	57
The reproduction of tone and colour	6		
Image quality expectations	7		
<b>2 Fundamentals of light and vision</b>	<b>9</b>	<b>5 The photometry of image formation</b>	<b>61</b>
Ralph E. Jacobson		Sidney F. Ray	
Light waves and particles	9	Stops and pupils	61
Optics	10	Aperture	62
The electromagnetic spectrum	10	Mechanical vignetting	62
The eye and vision	11	Image illumination	63
		Image illuminance with wide-angle lenses	66
<b>3 Photographic light sources</b>	<b>16</b>	Exposure compensation for close-up photography	67
Sidney F. Ray		Light losses and lens transmission	68
Characteristics of light sources	16	Flare and its effects	68
Light output	21	T-numbers	69
Daylight	25	Anti-reflection coatings	69
Tungsten-filament lamps	25		
Tungsten-halogen lamps	26	<b>6 Optical aberrations and lens performance</b>	<b>72</b>
Fluorescent lamps	27	Sidney F. Ray	
Metal-halide lamps	27	Introduction	72
Pulsed xenon lamps	27	Axial chromatic aberration	72
Expendable flashbulbs	28	Lateral chromatic aberration	74
Electronic flash	29	Spherical aberration	75
Other sources	38	Coma	76
		Curvature of field	77
		Astigmatism	77
		Curvilinear distortion	78
		Diffraction	79
		Resolution and resolving power	80
		Modulation transfer function	81
<b>4 The geometry of image formation</b>	<b>39</b>		
Sidney F. Ray		<b>7 Camera lenses</b>	<b>83</b>
Interaction of light with matter	39	Sidney F. Ray	
Image formation	41	Simple lenses	83
The simple lens	42	Compound lenses	83
Image formation by a compound lens	43		
Graphical construction of images	45		

Development of the photographic lens	85	<b>12 Sensitive materials and image sensors</b>	<b>191</b>
Modern camera lenses	88	Ralph E. Jacobson	
Wide-angle lenses	91	Latent image formation in silver halides	191
Long-focus lenses	93	Image formation by charge-coupled devices	193
Zoom and varifocal lenses	95	Production of light-sensitive materials and sensors	195
Macro lenses	98	Sizes and formats of photographic and electronic sensors and media	200
Teleconverters	99		
Optical attachments	100	<b>13 Spectral sensitivity of photographic materials</b>	<b>205</b>
Special effects	102	Geoffrey G. Attridge	
<b>8 Types of camera</b>	<b>104</b>	Response of photographic materials to short-wave radiation	205
Sidney F. Ray		Response of photographic materials to visible radiation	206
Survey of development	104	Spectral sensitization	207
Camera types	107	Orthochromatic materials	208
Special purpose cameras	113	Panchromatic materials	208
Automatic cameras	115	Extended sensitivity materials	208
Digital cameras	120	Infrared materials	209
Architecture of the digital camera	125	Other uses of dye sensitization	209
<b>9 Camera features</b>	<b>131</b>	Determination of the colour sensitivity of an unknown material	210
Sidney F. Ray		Wedge spectrograms	210
Shutter systems	131	Spectral sensitivity of digital cameras	211
The iris diaphragm	136		
Viewfinder systems	138	<b>14 Principles of colour photography</b>	<b>213</b>
Flash synchronization	143	Geoffrey G. Attridge	
Focusing systems	144	Colour matching	213
Autofocus systems	151	The first colour photograph	214
Exposure metering systems	154	Additive colour photography	214
Battery power	160	Subtractive colour photography	214
Data imprinting	161	Additive processes	215
		Subtractive processes	217
<b>10 Camera movements</b>	<b>163</b>	Integral tripacks	217
Sidney F. Ray			
Introduction	163	<b>15 Sensitometry</b>	<b>218</b>
Translational movements	165	Geoffrey G. Attridge	
Rotational movements	165	The subject	218
Lens covering power	166	Exposure	218
Control of image sharpness	168	Density	219
Limits to lens tilt	170	Effect of light scatter in a negative	220
Control of image shape	171	Callier coefficient	220
Perspective control lenses	173	Density in practice	221
Shift cameras	174	The characteristic (H and D) curve	222
		Main regions of the negative characteristic curve	223
<b>11 Optical filters</b>	<b>176</b>	Variation of the characteristic curve with the material	225
Sidney F. Ray		Variation of the characteristic curve with development	225
Optical filters	176		
Filter sizes	178		
Filters and focusing	178		
Colour filters for black-and-white photography	179		
Colour filters for colour photography	182		
Special filters	183		
Polarizing filters	186		
Filters for darkroom use	189		



91	Gamma-time curve	226	<b>17 Photographic processing</b>	<b>273</b>
	Variation of gamma with wavelength	227	Ralph E. Jacobson	
	Placing of the subject on the characteristic curve	227	Developers and development	273
	Average gradient and $\bar{G}$	228	Developing agents	273
191	Contrast index	228	Preservatives	276
	Effect of variation in development on the negative	228	Alkalis	276
193	Effect of variation in exposure on the negative	229	Restrainers (anti-foggants)	277
195	Exposure latitude	230	Miscellaneous additions to developers	277
200	The response curve of a photographic paper	231	Superadditivity (synergism)	278
	Maximum black	231	Monochrome developer formulae in general use	279
05	Exposure range of a paper	232	Changes in a developer with use	282
	Variation of the print curve with the type of emulsion	232	Replenishment	283
	Variation of the print curve with development	233	Preparing developers	284
05	Requirements in a print	234	Techniques of development	285
06	Paper contrast	234	Obtaining the required degree of development	289
07	The problem of the subject of high contrast	235	Quality control	292
08	Tone reproduction	236	Processing following development	293
08	Reciprocity law failure	238	Rinse and stop baths	293
08	Sensitometric practice	239	Fixers	294
09	Sensitometers	240	Silver recovery	296
09	Densitometers	241	Bleaching of silver images	298
10	Elementary sensitometry	244	Washing	299
10	Sensitometry of a digital camera	245	Tests for permanence	300
11			Drying	301
			<b>18 Speed of materials, sensors and systems</b>	<b>302</b>
13	<b>16 The reproduction of colour</b>	<b>247</b>	Ralph E. Jacobson	
	Geoffrey G. Attridge		Speed of photographic media	302
13	Colours of the rainbow	247	Methods of expressing speed	302
14	Colours of natural objects	247	Speed systems and standards	305
14	Effect of the light source on the appearance of colours	248	ISO speed ratings for colour materials	306
14	Response of the eye to colours	248	Speed of digital systems	307
15	Primary and complementary colours	249	Speed ratings in practice	308
17	Complementary pairs of colours	250		
17	Low light levels	250	<b>19 Camera exposure determination</b>	<b>310</b>
	Black-and-white processes	250	Sidney F. Ray	
18	Colour processes	251	Camera exposure	310
18	Formation of subtractive image dyes	254	Optimum exposure criteria	311
18	Colour sensitometry	254	Exposure latitude	311
19	Imperfections of colour processes	258	Subject luminance ratio	312
19	Correction of deficiencies of the subtractive system	259	Development variations	313
20	Masking of colour materials	260	Exposure determination	313
20	Problems of duplication	261	Practical exposure tests	315
21	The chemistry of colour image formation	263	Light measurement	315
22	Chromogenic processes	263	Exposure meter calibration	316
23	Silver-dye-bleach process	268	Exposure values	318
25	Instant colour processes	269	Incident light measurements	318
25	Alternative method for instant photography	271	Exposure meters in practice	320
			Photometry units	323
			Spot meters	324
			In-camera metering systems	324
			Electronic flash exposure metering	329
			Automatic electronic flash	333



<b>20</b>	<b>Hard copy output media</b>	<b>336</b>	<b>23</b>	<b>Colour matters</b>	<b>383</b>
	Ralph E. Jacobson			Geoffrey G. Attridge	
	Hard copy output	336		Specification by sample	383
	Photographic papers	336		The physical specification of colour	384
	Type of silver halide emulsion	336		Specification of colour by synthesis	384
	Paper contrast	337		Colour gamuts	389
	Paper surface	338		Summing up	392
	Paper base	339			
	Colour photographic papers	339	<b>24</b>	<b>Theory of image formation</b>	<b>393</b>
	Processing photographic paper	340		Norman R. Axford	
	Picrography and Picrostat	344		Sinusoidal waves	394
	Dry Silver materials	345		Images and sine waves	395
	Cylithographic materials/Cycolor	346		Imaging sinusoidal patterns	397
	Thermal imaging materials	346		Fourier theory of image formation	398
	Materials for ink-jet printing	347		Measuring modulation transfer functions (MTF)	406
<b>21</b>	<b>Production of hard copy</b>	<b>348</b>		Discrete transforms and sampling	408
	Ralph E. Jacobson			The MTF for a CCD imaging array	411
	Photographic printing and enlarging	349		Image quality and MTF	411
	Types of enlargers	349	<b>25</b>	<b>Images and information</b>	<b>413</b>
	Light sources for enlarging and printing	353		Norman R. Axford	
	Lenses for enlargers	354		Image noise	413
	Ancillary equipment	355		Photographic noise	413
	Exposure determination	355		Quantifying image noise	417
	Conventional image manipulation	358		Practical considerations for the autocorrelation function and the noise power spectrum	419
	Colour printing	359		Signal-to-noise ratio	420
	Colour enlarger design	362		Detective quantum efficiency (DQE)	422
	Types of colour enlarger	363		Information theory	426
	Methods of evaluating colour negatives for printing	365	<b>26</b>	<b>Digital image processing and manipulation</b>	<b>428</b>
	Digital output	367		Norman R. Axford	
	Evaluating the results	370		Linear spatial filtering (convolution)	428
<b>22</b>	<b>Life expectancy of imaging media</b>	<b>372</b>		Frequency domain filtering	429
	Ralph E. Jacobson			Non-linear filtering	433
	Life expectancy of photographic media	372		Statistical operations (point, grey-level operations)	434
	Processing conditions	373		Image restoration	438
	Storage conditions	375		Edge detection and segmentation	442
	Atmospheric gases	376		Image data compression	443
	Toning	377			
	Light fading	378		<b>Index</b>	<b>447</b>
	Life expectancy of digital media	379			

## 4 The geometry of image formation

### Interaction of light with matter

Imaging generally records the interaction of light or radiation with the subject, except for self-luminous or emissive subjects and uses lenses or optical systems to form an image at the photoplane of a camera. There are four principal effects of the interaction of light with an object, namely *absorption*, *reflection*, *transmission*, and *chemical change*. The first two of these always occur to some extent: transmission occurs in the case of translucent or transparent matter; and chemical change occurs under appropriate circumstances. The absorbed light energy is not destroyed, but converted to another such as heat, or sometimes electrical or chemical energy. This chapter details the behaviour of reflected or transmitted light, and the formation of an optical image.

### Transmission

Some transparent and translucent materials allow light to pass completely through them apart from absorption losses. Such light is said to be *transmitted* and the *transmittance* ( $T$ ) of the material is the ratio of emergent luminous flux to incident luminous flux. *Direct transmission* (sometimes miscalled 'specular transmission') refers to light transmitted without scatter, as for example by clear optical glass. If *selective absorption* takes place for particular wavelengths of incident white light, then the material is seen as coloured by transmitted light, as in the case of a camera filter. If *scattering* occurs, as in a translucent medium, the light undergoes *diffuse transmission*, which may be uniform or directional or preferential. The transmittance of such a medium may be defined as in either a general or in a specific direction.

### Reflection

Depending on the nature of the surface, particularly its smoothness, the reflection of light may be *direct* or *diffuse*. *Direct* or *specular reflection* is the type of reflection given by a highly polished surface such as a mirror, and is subject to the *laws of reflection* (Figure 4.1). Light incident on the surface is reflected at an angle equal to the angle of incidence. (The angles of incidence and reflection are both measured

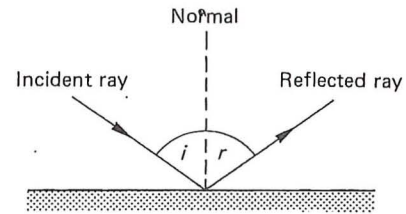


Figure 4.1 Specular reflection of an incident light ray by a plane mirror;  $i = r$

from the *normal*, i.e. the line perpendicular to the surface at the point of incidence.) The surface brightness of a directly reflecting surface is highly dependent on viewpoint. A perfectly diffuse or *Lambertian surface*, on the other hand, reflects the incident light equally in all directions; thus its *brightness* or *luminance* is seen as constant irrespective of viewpoint. Few surfaces have such extreme properties; shiny surfaces usually produce some scattered light, and matt surfaces (Figure 4.2) may show a 'sheen'. Reflection from most surfaces combines both direct and diffuse reflection and is known as *mixed reflection*. Depending on the properties of the incident light, the nature of the material and angle of incidence, the reflected light may also be partially or completely polarized. Objects are seen mainly by diffusely reflected light which permits the perception of detail and texture, qualities not found in specular surfaces such as mirrors.

*Reflectance* ( $R$ ) is defined as the ratio of the reflected luminous flux to the incident luminous flux, and (as with transmittance) this may be defined as either general or in a specific direction. Surfaces

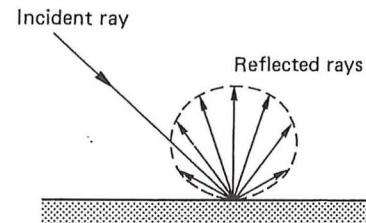


Figure 4.2 The diffuse reflection of an incident light ray by a matt surface



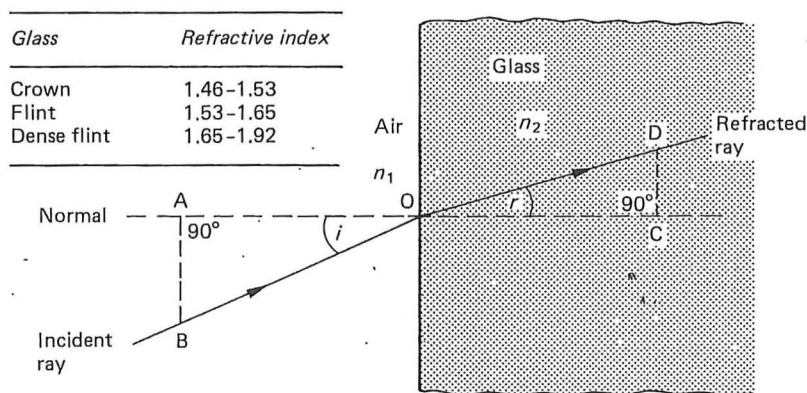


Figure 4.3 An obliquely incident light ray undergoing refraction when passing from air to glass

commonly encountered have reflectances in the range 0.02 (2 per cent) (matt black paint) to 0.9 (90 per cent).

### Refraction

When a ray of light being transmitted in one medium passes into another of different optical properties its direction is changed at the interface except in the case when it enters normally, i.e. perpendicular to the interface. This *deviation*, or *refraction* of the ray results from a change in the velocity of light in passing from one medium to the next (Figure 4.3). Lenses utilize the refraction of glass to form *images*. Light travels more slowly in a denser medium, and a decrease (increase) in velocity causes the ray to be bent towards (away from) the normal. The ratio of the velocity in empty space to that within the medium is known as the *refractive index* ( $n$ ) of the medium. For two media of refractive indices  $n_1$  and  $n_2$  where the angles of incidence and refraction are respectively  $i$  and  $r$ , then the amount of refraction is given by *Snell's Law*:

$$n_1 \sin i = n_2 \sin r \quad (1)$$

Taking  $n_1$  as being air of refractive index approximately equal to 1, then the refractive index of the medium  $n_2$  is given by

$$n_2 = \frac{\sin i}{\sin r} \quad (2)$$

The velocity of light in an optical medium depends on its wavelength, and refractive index varies in a non-linear manner with wavelength, being greater for blue light than for red light. A quoted value for

refractive index ( $n_d$ ) applies only to one particular wavelength. The one usually quoted ( $n_d$ ) refers to the refractive index at the wavelength of the *d* line in the helium spectrum (587 nm).

When light is transmitted by clear optical glass solids or prisms, refraction causes effects such as *deviation*, *dispersion* and *total internal reflection* (Figure 4.4). Deviation is the change of direction of the emergent ray with respect to the direction of the incident ray. In the case of a parallel-sided glass block, the emergent ray is not deviated with respect to the original incident ray; but it is *displaced*, the amount depending on the angle of incidence and the thickness of the block and its refractive index. A non-parallel-sided prism deviates the ray by two refractions, the deviation  $D$  depending on the refracting angle  $A$  of the prism, and on its refractive index. But when white light is deviated by a prism it is also dispersed to form a *spectrum*. The dispersive power of a prism is not directly related to its refractive index and it is possible to almost neutralize dispersion by using two different types of glass together, whilst retaining some deviation. In *achromatic lenses* this allows rays of different wavelengths to be brought to a common focus (see Chapter 6).

For a ray of light emerging from a dense medium of refractive index  $n_2$  into a less dense medium of refractive index  $n_1$ , the angle of refraction is greater than the angle of incidence, and increases as the angle of incidence increases until a *critical value* ( $i_c$ ) is reached. At this angle of incidence the ray will not emerge at all, it will undergo *total internal reflection* (TIR).

At this *critical angle* of incidence,  $i_c = \sin^{-1}(n_1/n_2)$ . For air ( $n_1 = 1$ ), also for glass with  $n_2 = 1.66$ ,  $i_c$  is 37 degrees. TIR is used in reflector prisms to give almost 100 per cent reflection as compared with 95 per cent at best for uncoated front-surface mirrors. A 45 degree prism will deviate a *collimated* (i.e. parallel) beam through 90 degrees by TIR; but for a



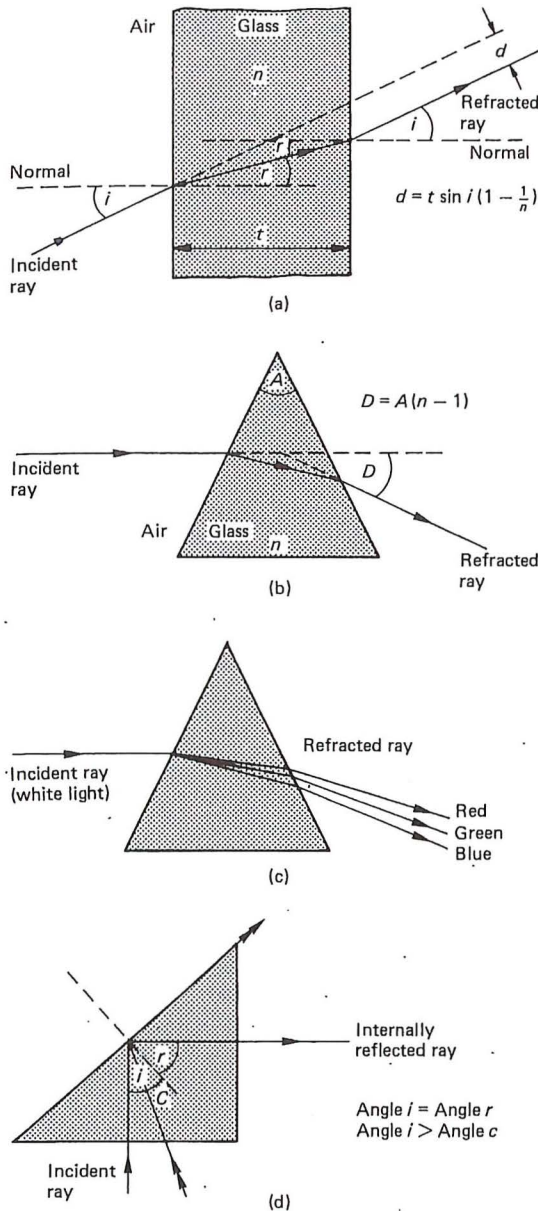


Figure 4.4 Various consequences of refraction of light by glass prisms. (a) A monochromatic light ray passing obliquely through a parallel-sided glass block, and resultant displacement  $d$ . (b) Refraction of monochromatic light caused by its passage through a prism, and resultant deviation  $D$ . (c) Dispersion of white light by a prism. (d) Total internal reflection in a right-angled prism, critical angle  $C$

widely diverging beam the angle of incidence may not exceed the critical angle for the whole beam, and it may be necessary to metallize the reflecting surface.

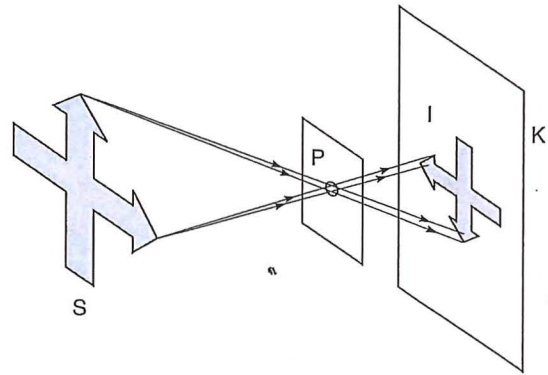


Figure 4.5 Formation of an image by a pinhole. The bundles of rays from points on the subject  $S$  pass through pinhole  $P$  and diverge to form an image  $I$  on photoplane surface  $K$ . The image is inverted, reversed, smaller and lacks sharpness

### Image formation

When light from a subject passes through an optical system, the subject may appear to the viewer as being in a different place (and probably of a different size). This is due to the formation of an *optical image*. An optical system may be as simple as a plane mirror or as complex as a highly corrected camera lens. A simple method of image formation is via a *pinhole* in an opaque material (Figure 4.5). Two properties of this image are that it is *real*, i.e. it can be formed on a screen as rays from the object pass through the pinhole, and that, as light travels in straight lines, the image is *inverted*, and *laterally reversed* left to right as viewed from behind a scattering (focusing) screen. The ground-glass focusing screen of a technical camera when used with a pinhole shows such an image.

A pinhole is limited in the formation of real images, as the sharpness depends on the size of the pinhole. The optimum diameter ( $K$ ) for a pinhole is given by the approximate formula:

$$K = \frac{\sqrt{v}}{25} \quad (3)$$

where  $v$  is the distance from pinhole to screen. A larger hole gives a brighter but less sharp image. A smaller hole gives a less bright image, but this is also less sharp owing to diffraction (see Chapter 6). Although a pinhole image does not suffer from curvilinear distortion, as images produced by lenses may do, its poor transmission of light and low resolution both limit its use to a few specialized applications.

rticular  
s to the  
e in the

l glass  
uch as  
refraction  
tion of  
of the  
l glass  
spect to  
ed, the  
nd the  
A non-  
refrac-  
acting  
x. But  
is also  
power  
index  
ion by  
whilst  
es this  
ight to

edium  
um of  
greater  
angle  
( $i_c$ ) is  
ill not  
ection

$\sin^{-1}$   
: 1.66,  
o give  
ith 95  
ors. A  
(i.e.  
for a

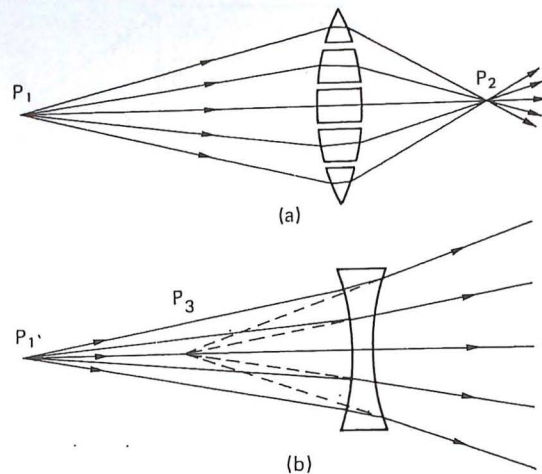


Figure 4.6 Negative and positive lenses. (a) A simple positive lens considered as a series of prisms. (b) Formation of a virtual image of a point object by a negative lens

### The simple lens

A lens is a system of one or more pieces of glass or *elements* with (usually) spherical surfaces, all of whose centres are on a common axis, the *optical* (or *principal*) axis. A *simple* or *thin* lens is a single piece of glass or *element* whose axial thickness is small compared with its diameter, whereas a *compound* or *thick* lens consists of several air spaced *components*, some of which may comprise several elements cemented together, to correct for *aberrations*. A simple lens may be regarded as a number of prisms, as shown in Figure 4.6. Light diverging from a point source  $P_1$  and incident on the front surface of the positive lens is redirected by refraction to form a real image at point  $P_2$ . These rays are said to come to a *focus*. Alternatively, by using a negative lens, the incident rays may be further diverged by the refraction of the lens, and so appear to have originated from a *virtual focus* at point  $P_3$ .

The front and rear surfaces of the lens may be convex, concave or plane; the six usual configurations of simple spherical lenses are shown in cross-section in Figure 4.7. A meniscus lens is one in which the *centres of curvature* of the surfaces are both on the same side of the lens. Simple positive meniscus lenses are used as *close-up lenses* for cameras. While the same refracting power in *dioptries* is possible with various pairs of curvatures, the *shape* of a close-up lens is important in determining its effect on the quality of the image given by the lens on the camera.

The relationships between the various parameters of a single-element lens of refractive index  $n_d$ , axial thickness  $q$  and radii of curvature of the surfaces  $R_1$

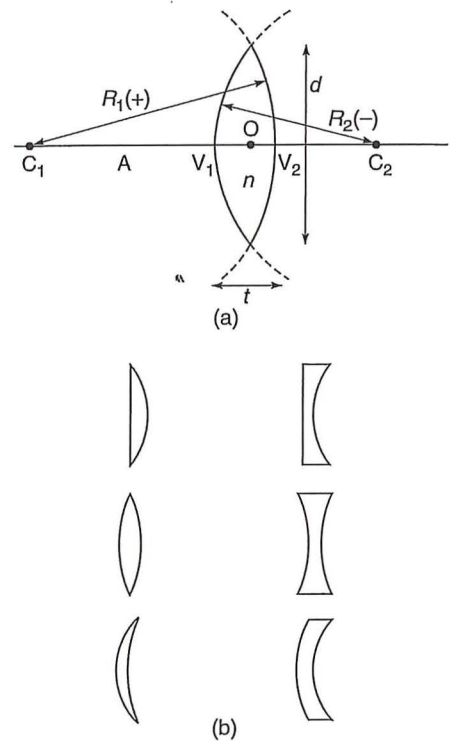


Figure 4.7 Simple lens. (a) Lens parameters; A, optical axis;  $C_1, C_2$ , centres of curvature with radii  $R_1$  and  $R_2$ ;  $V_1$  and  $V_2$ , vertices of spherical surfaces; O, optical centre;  $n$ , refractive index;  $t$ , axial thickness;  $D$ , diameter. (b) Shape configurations: plano-convex, plano-concave, equi-biconvex, equi-biconcave, positive meniscus, negative meniscus

and  $R_2$  required to give a *focal length*  $f$  or (*refractive power*  $K$ ) are given by the general 'lensmakers' formula':

$$K = \frac{1}{f} = (n_d - 1) \left( \frac{1}{R_1} - \frac{1}{R_2} \right) + \frac{(n_d - 1)q}{n_d R_1 R_2} \quad (4)$$

For  $f$  measured in millimetres, power  $K = 1000/f$  in dioptries. For a thin lens, equation (4) simplifies to

$$K = \frac{1}{f} = (n_d - 1) \left( \frac{1}{R_1} - \frac{1}{R_2} \right) \quad (5)$$

### Image formation by a simple positive lens

Irrespective of their *configuration* of elements, camera lenses are similar to simple lenses in their image-forming properties. In particular, a camera lens always forms a real image if the object is at a distance of more than one focal length. The formation of the image of a point source has been discussed, now let



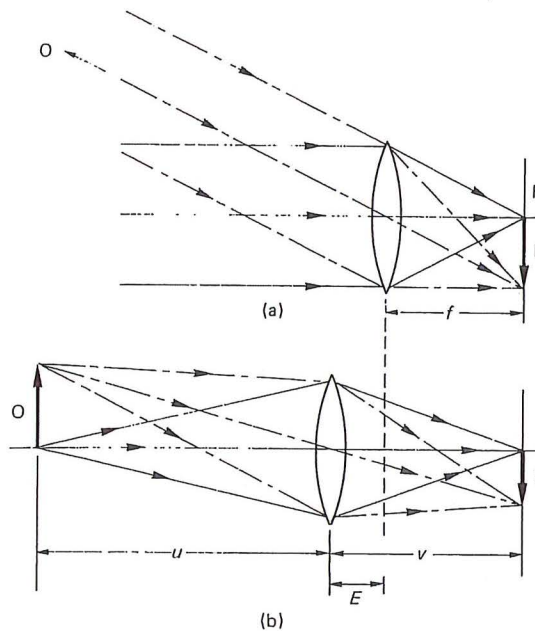


Figure 4.8 Image formation by a positive lens. (a) For a distant subject: F is the rear principal focal plane; (b) for a near subject: focusing extension  $E = (v - f)$ ; I is an inverted real image

us consider the formation of the image of an extended object.

If the object is near the lens, the position and size of the optical image can be determined from the refraction of light diverging to the lens from two points at opposite ends of the object. Figure 4.8 shows this for a simple lens. The image is inverted, laterally reversed, minified, behind the lens and real.

To a first approximation, a distant object can be considered as being located at *infinity*. The rays that reach the lens from any point on the object are effectively parallel. As before the image is formed close to the lens, inverted, laterally reversed and real. The image plane in which this image is formed is termed the *principal focal plane* (F). For a flat distant object and an 'ideal' lens, every image point lies in this plane. The point of intersection of the focal plane and the optical axis is termed the *rear principal focus* (or simply the *focus*) of the lens, and the distance from this point to the lens is termed the *focal length* ( $f$ ) of the lens. Only for an object at infinity does the *image distance* or *conjugate* ( $v$ ) from the lens correspond to the focal length. As the object approaches the lens (i.e. object distance  $u$  decreases), the value of  $v$  increases (for a positive lens). If the lens is turned round, a second focal point is obtained; the focal length remains the same. The focal lengths of thick lenses are measured from different points in the lens

configuration (see below). Finally, the distance of the rear focus from the rear surface of a lens is known as the *back focus* or *back focal distance*. This is of importance in camera design so that optical devices such as reflex mirrors or beam-splitting prisms can be located between lens and photoplane.

### Image formation by a compound lens

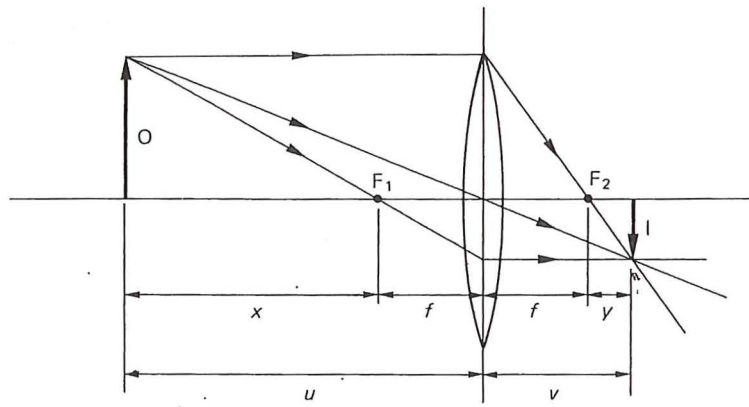
A lens is considered as 'thin' if its axial thickness is small compared to its diameter and to the object and image distances and its focal length, so that measurements can be made from the plane passing through its centre without significant error (Figure 4.9a). With a compound lens of axial thickness that is a significant fraction of its focal length, these measurements plainly cannot be made simply from the front or back surface of the lens or some point in between. However, it was proved by Gauss that a thick or compound lens could be treated as an equivalent thin one, and thin-lens formulae used to compute image properties, provided that the object and image conjugate distances were measured from two theoretical planes fixed with reference to the lens. This is referred to as *Gaussian optics*, and holds for *paraxial* conditions, i.e. for rays whose angle of incidence to the optical axis is less than some 10 degrees.

Gaussian optics uses six defined *cardinal* or *Gauss points* for any single lens or system of lenses. These are two *principal focal points*, two *principal points* and two *nodal points*. The corresponding planes through these points orthogonal to the optical axis are called the *focal planes*, *principal planes* and *nodal planes* respectively (Figure 4.9b). The focal length of a lens is then defined as the distance from a given principal point to the corresponding principal focal point. So a lens has two focal lengths, an object focal length and an image focal length; these are, however, usually equal (see below).

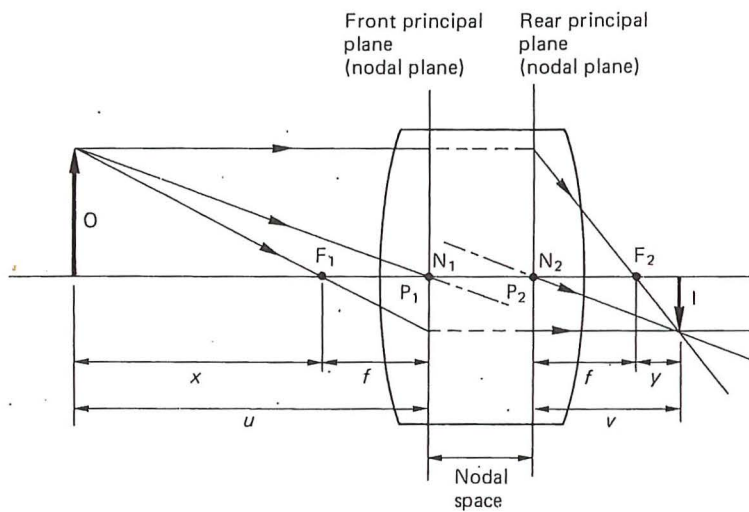
The definitions and properties of the cardinal points are as follows:

- (1) *Object principal focal point* ( $F_1$ ): The point whose image is on the axis at infinity in the image space.
- (2) *Image principal focal point* ( $F_2$ ): The point occupied by the image of an object on the axis at infinity in the object space.
- (3) *Object principal point* ( $P_1$ ): The point that is a distance from the object principal focal point equal to the object focal length  $F_1$ . All object distances are measured from this point.
- (4) *Image principal point* ( $P_2$ ): The point at a distance from the image principal focal point equal to the image focal length  $F_2$ . All image distances are measured from this point. The principal planes through these points are





(a) Simple lens



(b) Compound lens

**Figure 4.9** Image formation by simple and compound lenses. (a) For a simple lens, distances are measured from the optical centre of the lens; distance  $y$  is the focusing extension. (b) For a compound lens, distances are measured from the principal or nodal planes (the principal planes coincide with the nodal planes when the lens is wholly in air)

important, as the thick lens system can be treated as if the refraction of the light rays by the lens takes place at these planes only. An important additional property is that they are planes of unit magnification for conjugate rays.

- (5) *Object nodal point* ( $N_1$ ) and
- (6) *Image nodal point* ( $N_2$ ) These are a pair of planes such that rays entering the lens in the direction of the object nodal point leave the lens travelling parallel to their original direction as if they came from the image nodal point. Any such ray is displaced but not deviated. If a lens is

rotated a few degrees about its rear nodal point the image of a distant object will remain stationary. This property is used to locate the nodal points, and is the optical principle underlying one form of panoramic camera.

If the lens lies wholly in air, the object and image focal length of the numerous elements in the configuration (known as the *effective* or *equivalent focal length*) are equal, and the positions of the principal and nodal points coincide. This considerably simplifies imaging calculations. The value

of Gaussian optics is that if the positions of the object and cardinal points are known, the image position and magnification can be calculated with no other knowledge of the optical system. Positions of the cardinal points and planes can be used for graphical construction of image properties such as location and magnification.

Usually the nodal points lie within the lens, but in some types, either or both of the nodal points may be outside the lens, either in front of it or behind it. In a few cases the nodal points may actually be 'crossed'. The distance between the nodal points is called the *nodal space* or hiatus; in the case of crossed nodal points this value is taken as negative.

### Graphical construction of images

The refraction by a lens can be determined if the paths of some of the image-forming rays are traced by simple graphical means. For a positive lens four rules are used, based on the definitions of lens properties.

- (1) A ray passing through the centre of a thin lens is undeviated.
- (2) A ray entering a lens parallel to the optical axis, after refraction, passes through the focal point of the lens on the opposite side.
- (3) A ray passing through the focal point of a lens, after refraction, emerges from the lens parallel to the optical axis.
- (4) A meridional ray (one in a plane containing the optical axis), entering the front nodal plane at a height  $X$  above the axis, emerges from the rear nodal plane at the same height  $X$  above the axis on the same side and undeviated (see Figure 4.9b).

These rules (except the last) are illustrated in Figure 4.10, together with their modification to deal with image formation by negative lenses and concave and convex spherical mirrors. Image formation is shown for a range of types of lenses and mirrors. Note that in practice other surface shapes are used such as ellipsoidal and paraboloidal as well as aspheric, principally in the optics of illumination systems for projection and enlarging. Increasingly, aspheric surfaces are used in camera lenses to reduce the number of spherical surfaces otherwise required for adequate aberration correction.

### The lens conjugate equation

A relationship can be derived between the conjugate distances and the focal length of a lens. With

reference to Figure 4.11, a positive lens of focal length  $f$  with an object distance  $u$  forms an image at distance  $v$ .

From similar triangles ABC and XYZ,

$$\frac{AB}{XY} = \frac{BC}{YC} = \frac{u}{v} \tag{6}$$

From the figure,

$$BF_1 = u - f \tag{7}$$

Also from similar triangles ABF and QCF

$$\frac{BF_1}{CF_1} = \frac{AB}{QC} = \frac{AB}{XY} \tag{8}$$

By substituting equations (6) and (7) in (8) we obtain

$$\frac{u - f}{f} = \frac{u}{v}$$

Rearranging and dividing by  $uf$  we obtain the *lens conjugate equation*

$$\frac{1}{u} + \frac{1}{v} = \frac{1}{f} \tag{9}$$

This equation may be applied to thick lenses if  $u$  and  $v$  are measured from the appropriate cardinal points.

The equation is not very suitable for practical photographic use as it does not make use of object size AB or image size XY, one or both of which are usually known. Defining *magnification* ( $m$ ) or *ratio of reproduction* or *image scale* as  $XY/AB = v/u$ , and substituting into the lens equation and solving for  $u$  and  $v$  we obtain

$$u = f \left( 1 + \frac{1}{m} \right) \tag{10}$$

and

$$v = f(1 + m) \tag{11}$$

Because of the conjugate relationship between  $u$  and  $v$  as given by the lens equation above, these distances are often called the *object conjugate distance* and *image conjugate distance* respectively. These terms are usually abbreviated to 'conjugates'.

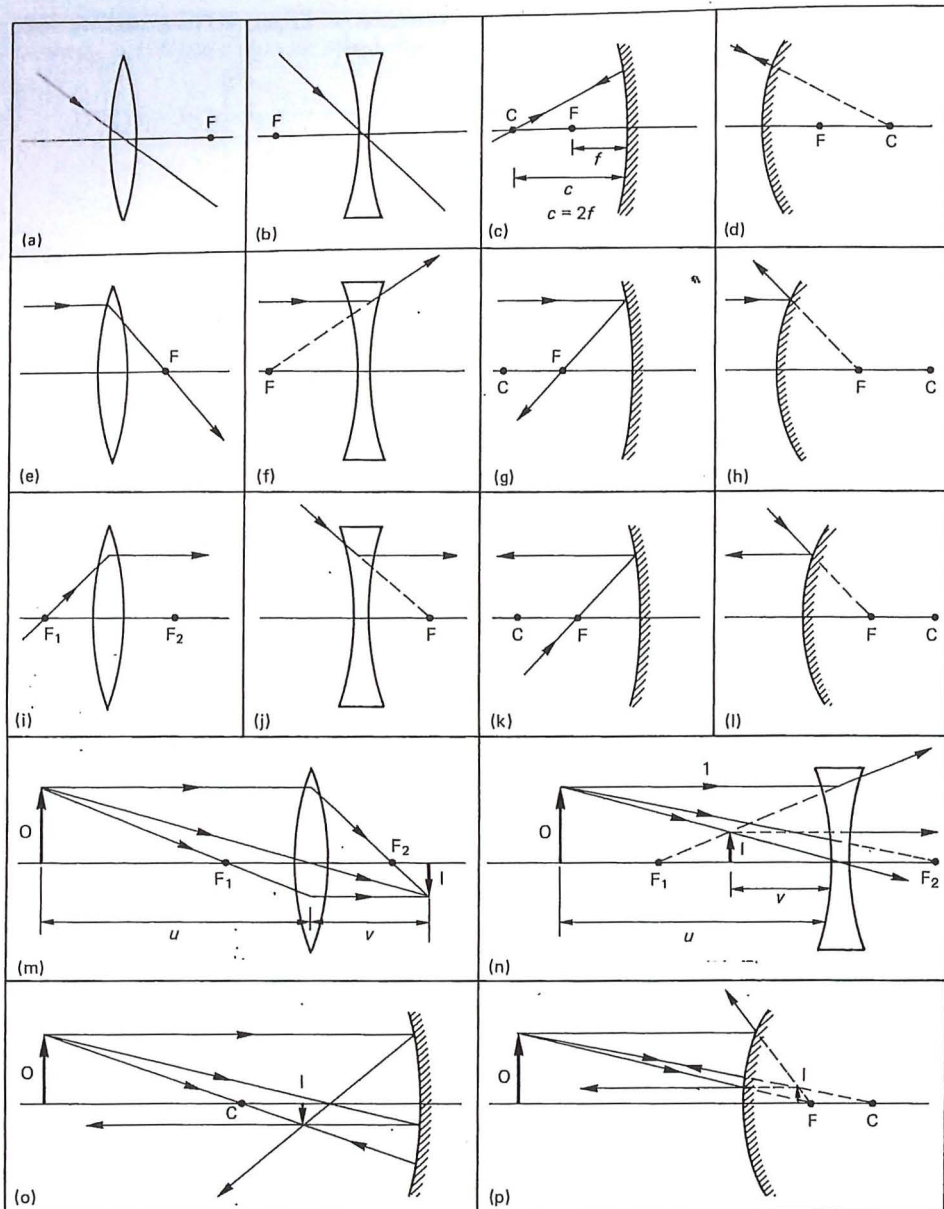
A summary of useful lens formulae is given in Figure 4.12, including formulae for calculating the combined focal length of two thin lenses in contact or separated by a small distance. A suitable sign convention must be used. For most elementary photographic purposes the 'real is positive' convention is usually adopted. By this convention, all

ical  
il or

l point  
emain  
ite the  
under-

image  
n the  
valent  
of the  
con-  
value





**Figure 4.10** The graphical construction of images formed by simple lenses and spherical mirrors. (a) A ray passing through the centre of a positive (i.e. convex) lens is undeviated. (b) A ray passing through the centre of a negative (i.e. concave) lens is undeviated. (c) A ray passing through the centre of curvature of a concave mirror is directed back upon itself. (d) A ray directed towards the centre of curvature of a convex mirror is directed back upon itself. (e) A ray travelling parallel to the optical axis of a positive lens, after refraction passes through the far focal point of the lens. (f) A ray travelling parallel to the optical axis of a negative lens, after refraction appears as if it had originated at the near focal point of the lens. (g) A ray travelling parallel to the optical axis of a concave mirror, after reflection passes through the focus of the mirror. (h) A ray travelling parallel to the optical axis of a convex mirror, after reflection appears as if it had originated from the focus of the mirror. (i) A ray passing through the near focal point of a positive lens, after refraction emerges from the lens parallel to the optical axis. (j) A ray travelling towards the far focal point of a negative lens, after refraction emerges from the lens parallel to the optical axis. (k) A ray passing through the focus of a concave mirror, after reflection travels parallel to the optical axis. (l) A ray directed towards the focus of a convex mirror, after reflection travels parallel to the optical axis. (m) An example of image construction for a positive lens using the three rules illustrated above. (n) An example of image construction for a negative lens. (o) An example of image construction for a concave mirror. (p) An example of image construction for a convex mirror



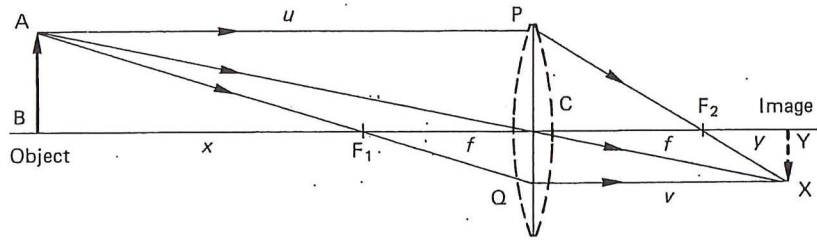
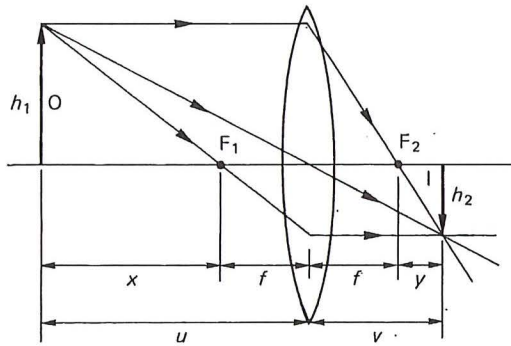
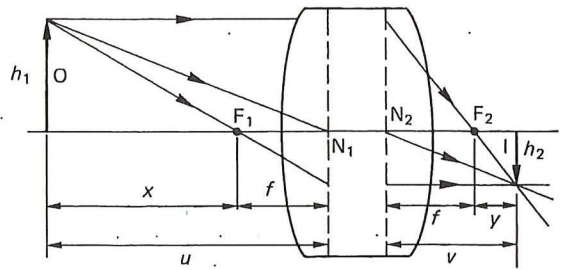


Figure 4.11 Derivation of the lens equation

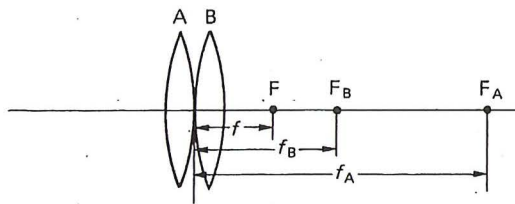


(a) Simple lens



(b) Compound lens

1.  $\frac{1}{u} + \frac{1}{v} = \frac{1}{f}$
2.  $\frac{h_2}{h_1} = \frac{I}{O} = \frac{v}{u} = m$
3. For  $u = \infty$ , or for  $u \gg v$ ,  $v = f$  so that  $m = \frac{f}{u}$
4.  $xy = f^2$

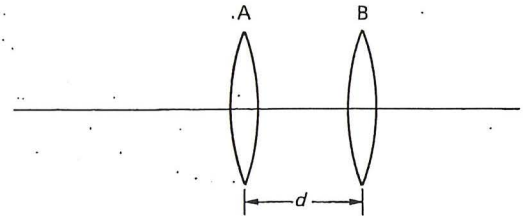


(c) Thin lenses in contact

$$\frac{1}{f} = \frac{1}{f_A} + \frac{1}{f_B} \text{ or,}$$

$$\frac{1}{f} = P = P_A + P_B$$

$P$  is the 'power' (expressed in dioptres)



(d) Thin lenses separated by a small distance

$$\frac{1}{f} = \frac{1}{f_A} + \frac{1}{f_B} - \frac{d}{f_A f_B}$$

Figure 4.12 Some useful lens formulae for lens calculations

gh the  
s  
rected  
axis of  
of a  
to the  
optical  
gh the  
wards  
rough  
convex  
he  
ion

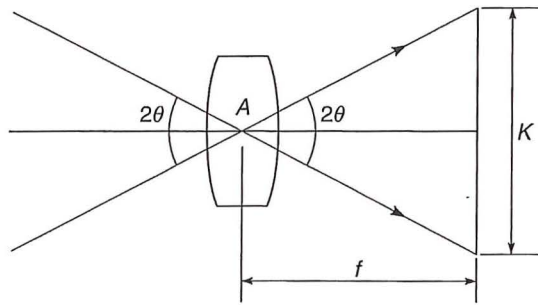


Figure 4.13 Field (angle) of view (FOV) of a lens related to format dimension

distances to real objects and real images are considered to be positive. All distances to virtual images are considered as negative. The magnification of a virtual image is also negative. An alternative Cartesian convention takes the lens or refracting surface at the origin so distances measured to the right are positive, and distances to the left are negative.

It is useful to note that when the object conjugate  $u$  is very large, as for a distant subject, the corresponding value of the image conjugate  $v$  may be taken as  $f$ , the focal length. Consequently, the magnification is given by  $m = f/u$ . Thus, image magnification or scale depends directly on the focal length of the camera lens for a subject at a fixed distance. From a fixed viewpoint, to maintain a constant image size as subject distance varies a lens with variable focal length is required, i.e. a zoom lens (see Chapter 7).

### Field angle of view

The focal length of a lens also determines the angle of the *field of view* (FOV) relative to a given film or sensor format. The FOV is defined as the angle subtended at the (distortion-free) lens by the diagonal ( $K$ ) of the format when the lens is focused on infinity (Figure 4.13).

Given that the FOV angle  $A$  is twice the semi-angle of view  $\theta$ , then:

$$A = 2\theta = 2 \tan^{-1} \left( \frac{K}{2f} \right) \quad (12)$$

The field of view for a particular combination of focal length and film format may be obtained from Table 4.1. To use this table, the diagonal of the negative should be divided by the focal length of the lens; the FOV can then be read off against the quotient obtained.

Table 4.1 Table for deriving field of view of an orthoscopic lens

Diagonal/focal length ( $K/f$ )	Field of view* ( $2\theta$ ) degrees
0.35	20
0.44	25
0.54	30
0.63	35
0.73	40
0.83	45
0.93	50
1.04	55
1.15	60
1.27	65
1.40	70
1.53	75
1.68	80
1.83	85
2.00	90
2.38	100
2.86	110
3.46	120

\*These values are for a lens which produces geometrically correct perspective.

As the lens to subject distance decreases, the lens to film distance increases, and the FOV decreases from its infinity-focus value. At unit magnification the FOV has approximately half its value at infinity focus.

Photographic lenses can be classified according by FOV for the particular film format for which they are designed. There are sound reasons for taking as 'standard' a lens that has a field of view approximately equal to the diagonal of the film format. For most formats this angle will be around 52 degrees. Wide-angle lenses can have FOVs up to 120 degrees or more, and long focus lenses down to 1 degree or less. Table 4.2 gives a classification of lenses for various formats based on FOV.

Occasionally confusion may arise as to the value of the FOV of a lens as quoted, because a convention exists in many textbooks on optics to quote the semi-angle  $\theta$ , in which cases value given must be doubled for photographic purposes. It should also be noted that the FOV for the *sides* of a rectangular film format is always less than the value quoted for the diagonal. The horizontal FOV is perhaps the most useful value to quote.

The term 'field of view' becomes ambiguous when describing lenses that produce distortion, such as fish-eye and anamorphic objectives. In such cases it may be preferable to describe the angle subtended by the diagonal of the format at the lens as the 'angle of the field' and the corresponding angle in the object space as the 'angle of view'.



Table 4.2 Lens type related to focal length and format coverage

Focal length (mm)	Nominal format (mm)	Angle of view (degrees on diagonal)	Lens type
15	24 × 36	110	EWA
20	24 × 36	94	EWA
20	APS	75	WA
24	24 × 36	84	WA
24	APS	67	WA
35	24 × 36	63	SWA
35	APS	50	S
40	24 × 36	57	S
40	60 × 60	94	EWA
40	APS	47	S
50	24 × 36	47	S
50	60 × 60	81	WA
50	60 × 70	85	WA
65	24 × 36	37	MLF
65	60 × 60	66	SWA
65	4 × 5 in	103	EWA
80	60 × 60	56	S
90	24 × 36	27	MLF
90	APS	22	MLF
90	4 × 5 in	84	WA
135	24 × 36	18	LF
135	60 × 60	35	MLF
135	4 × 5 in	62	S
150	60 × 60	32	LF
150	4 × 5 in	57	S
200	24 × 36	12	LF
200	8 × 10 in	78	WA
250	60 × 60	19	LF
300	24 × 36	8	VLF
300	8 × 10 in	57	S
500	24 × 36	5	VLF
500	60 × 60	10	LF
500	4 × 5 in	19	LF
1000	24 × 36	2.5	ELF
1000	60 × 60	5	VLF
1000	4 × 5 in	9	LF
1000	8 × 10 in	19	LF

EWA extreme wide-angle; WA wide-angle; SWA semi wide-angle; S standard; MLF medium long-focus; LF long-focus; VLF very long-focus; ELF extreme long-focus.

### Covering power of a lens

Every lens projects a fuzzy edged disc of light as the base of a right circular cone whose apex is at the centre of the exit pupil of the lens. The illumination of this disc falls off towards the edges; at first gradually and then very rapidly. The limit to this *circle of illumination* is due to *natural vignetting* as distinct from any concomitant mechanical vignetting. Also, owing to the presence of residual lens aberrations, the definition of the image within this disc deteriorates

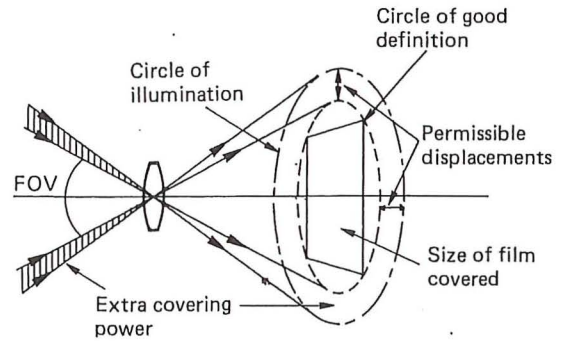


Figure 4.14 The covering power of a lens and image format

from the centre of the field outwards, at first gradually and then more rapidly. By defining an acceptable standard of image quality, it is possible to locate a boundary defining a *circle of good or acceptable definition* within this circle of illumination. The sensor format should be located within this region (Figure 4.14).

The extent of the circle of acceptable definition also determines the practical performance of the lens as regards the covering power relative to a given format. The *covering power* is usually expressed as an angle of view which may be the same as or greater than that given by the format in use. A greater FOV than set by the format is called *extra covering power* and is essential for a lens fitted to a technical camera or a *perspective-control* (PC) or 'shift' lens when lens displacement movements are to be used. The extra covering power permits displacement of the format within the large circle of good definition until vignetting occurs, indicated by a marked decrease in luminance at the periphery of the format.

Covering power is increased by closing down the iris diaphragm of a camera lens, because mechanical vignetting is reduced, and off-axis lens aberrations are decreased by this action. The covering power of lenses for technical cameras is quoted for use at  $f/22$  and with the lens focused on infinity. Covering power increases as the lens is focused closer; for close-up work a lens intended for a smaller format may cover a larger format, with the advantage of a shorter bellows extension for a given magnification.

### Geometric distortion

A wide-angle lens, i.e. a lens whose FOV exceeds some 75 degrees, is invaluable in many situations, such as under cramped conditions, and where use of the 'steep' perspective associated with the use of such lenses at close viewpoints is required. The large angle of view combined with a flat film plane (rather than

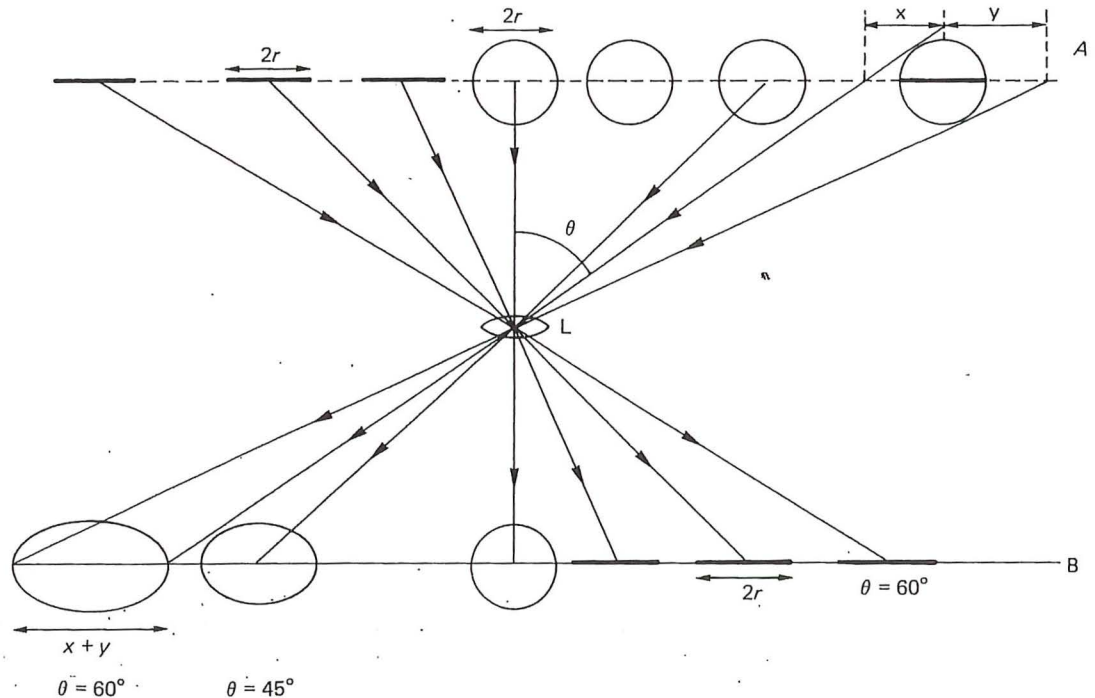


Figure 4.15 Geometric distortion by a lens. An array of spheres of radius  $r$  and lines of length  $2r$  in the subject plane A are imaged by lens L in image plane B at unit magnification. The lines retain their length independent of field angle  $\theta$  but the spheres are progressively distorted into ellipses with increase in  $\theta$

the saucer-shaped surface that would intuitively be thought preferable), makes shape distortion of three-dimensional objects near the edge of the field of view very noticeable. The geometry of image formation by a lens over a large field is shown in Figure 4.15, producing *geometrical distortion* which must not be confused with the *curvilinear distortion* caused by lens aberrations. Flat objects are of course not distorted in this way so a wide-angle lens can be used for the copying of flat originals. As an example of the distortion occurring with a subject such as a sphere of diameter  $2r$ , the image is an ellipse of minor diameter  $2r$  and major diameter  $W$ , where  $W = 2r \sec\theta$ , given unit magnification and that  $r$  is small relative to the object distance. The term  $\sec\theta$  is the *elongation factor* of the image.

## Depth of field

### Image sharpness

Any subject can be considered as made up of a large number of points. An ideal lens would image each of these as a point image (strictly, an Airy diffraction pattern) by refracting and converging the cone of light from the subject point to a focus. The purpose of

focusing the camera is to adjust the image conjugate to satisfy the lens equation. The image plane is strictly correct for all object points in a conjugate plane, provided all points of the object *do* lie in a plane. Unfortunately, objects in practice do not usually lie in a plane, and so the image also does not lie in a single plane. Consider just two of the planes through the object (Figure 4.16). For an axial point in both planes, each point can be focused in turn but both cannot be rendered sharp simultaneously. When the image of one is in focus the other is represented by an image patch, called more formally a *blur circle*. These discs or *circles of confusion* are cross-sections of the cone of light coming to a focus behind or in front of the surface of the film.

This purely geometrical approach suggests that when photographing an object with depth, only one plane can be in sharp focus and all other planes are out of focus. Yet in practice pictures of objects are obtained with considerable depth that appear sharp all over. The reason is that the eye is satisfied with something less than pin-point sharpness. In the absence of other image-degrading factors such as lens aberrations or camera shake, a subjective measure of image quality is its perceived *sharpness*, which may be defined as the adequate provision of resolved detail in the image. Inspection of a photograph



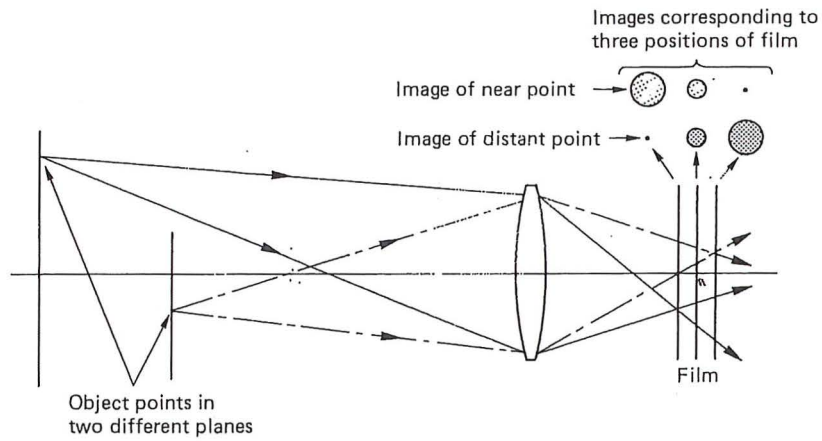


Figure 4.16 Object points at different distances and their images at different photoplanes

containing subject matter covering a considerable depth shows that the sharpness of the image does vary with depth. Detail both in front of and behind the point of optimum focus may, however, be rendered adequately sharp, giving a zone of acceptably sharp focus; this zone is termed the *depth of field*. (The term

applies only to the object space and should not be confused with the related *depth of focus*, which applies to the conjugate region through the focal plane in the image space.) Depth of field is of great importance in most types of photography, the manipulation of its positioning and extent being an

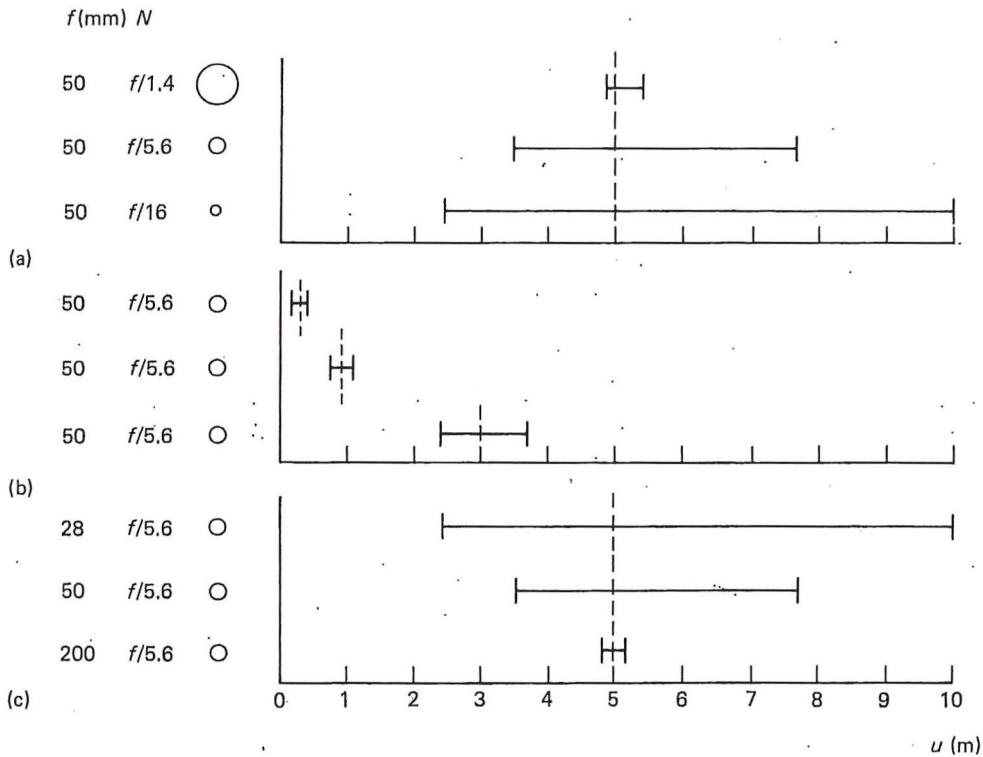


Figure 4.17 Depth of field. Three variables in general influence depth of field  $T$  at a constant value for the circle of confusion. (a) Lens aperture  $N$ , varying from  $f/1.4$  to  $f/16$  with a 50-mm lens focused at 5 m. (b) Focused distance  $u$ , varying from 0.5 to 3 m with a 50 mm lens at  $f/5.6$  (c) Focal length  $f$ , varying from 28 to 200 mm at  $f/5.6$  focused on 5 m

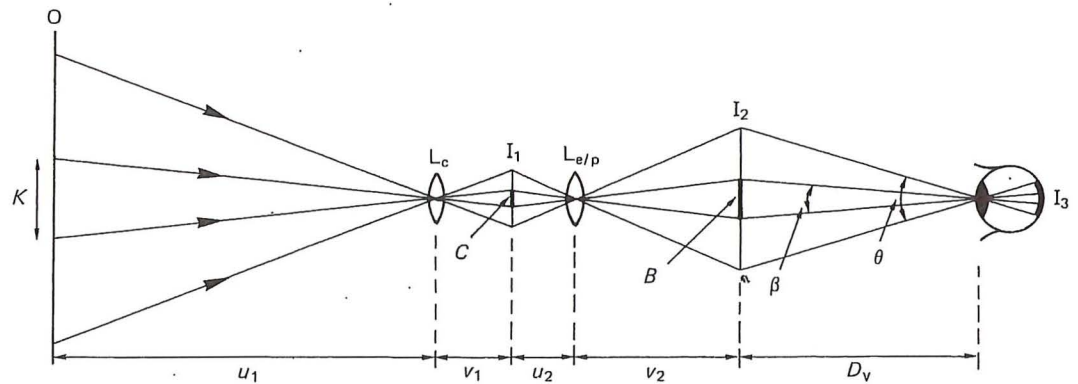


Figure 4.18 Geometry of the blur circle. Subject plane O with detail K is imaged by camera lens  $L_C$  at  $I_1$ , then re-imaged by enlarger or projector lens  $L_{e/p}$  at  $I_2$  and finally imaged on the retina at  $I_3$ . The circle of confusion  $C$  is seen as blur circle  $B$  in the cone of vision angle  $\theta$ . Visual acuity is  $1/\beta$ . Relationships are:  $m = v_1/u_1$ ,  $M = v_2/u_2$ ,  $K = C/m$ ,  $B = CM$ ,  $\beta = B/D_v$

important creative control. Knowledge of the means of extending, restricting or simply achieving depth of field is a vital skill in practical photography.

Manipulation of a camera and lens will demonstrate the control of depth of field possible by a choice of the focal length and aperture of the lens together with the focused subject distance (Figure 4.17) for a chosen circle of confusion. The various movements of a technical camera can also be used, and described in Chapter 10.

Depth of field can be quantified and calculated in terms of four variables, but first it is necessary to define 'an acceptable standard of sharpness' for a photographic record such as a print viewed in the hand. The depth of field boundaries are not as a rule sharply defined; usually there is a blending of acceptably sharp into less sharp detail. Much depends on the viewing conditions and also on aperture shape to some extent.

### Visual acuity

Perception of detail, judgement of its sharpness, and depth of field in a photograph depend largely upon viewing distance and visual acuity, though other factors such as image contrast and ambient illumination are also significant. Normal vision requires muscular action to alter the refractive state of the eye in order to focus. This internal focusing is called *accommodation*, and physiological limitations set a comfortable *near distance of distinct vision* ( $D_v$ ) of some 250 mm. The resolving power of the eye, or *visual acuity*, is the ability to discriminate fine details of objects in the visual field of view, and it decreases radially. It may be specified as the width of an object at a specific distance or as the angle subtended by this object or even as the width of its retinal image that is

just resolved by the eye. For example, in ideal conditions a high-contrast line of width 0.075 mm can be perceived at  $D_v$  subtending an angle of approximately 1 minute of arc, and representing an image on the retina of the eye of some 5 micrometres in width. The performance is limited by the structure of the retina, which consists of light receptors of finite size. The limiting performance is seldom achieved, and a lower value of 0.1 mm line width at  $D_v$  is commonly adopted. Converted into resolving power, an acuity of 0.1 mm corresponds to a spatial cycle of 0.2 mm, being the width of the line plus an adjacent identical space such as is used on a bar-type resolution test target, giving a value of 5 cycles per mm for the average eye. The accuracy of focusing aids such as split-image rangefinders depends upon visual acuity in 'aligning two parts of a subject detail with a horizontal separation or 'split'.

### Circle of confusion

For a photograph viewed at  $D_v$ , any subject detail resolved and recorded optically that is smaller than 0.2 mm in general dimensions may not be perceptible to the unaided eye. Thus any detail finer than this size is not required. This leads to a practical definition of resolution. A limit is set to the diameter of an image blur circle that is not distinguishable from a true point (by the unaided eye), and this is called the (minimum permissible) *circle of confusion* ( $C$ ). This is arrived at by empirical means. A photograph is viewed in a *cone of vision* where acceptable visual acuity is given over a FOV of some 50 to 60 degrees. The *comfortable viewing area* has a diameter of some 290 mm at  $D_v$ . The acceptable circle of confusion is derived from what is accepted as satisfactory definition within this area.



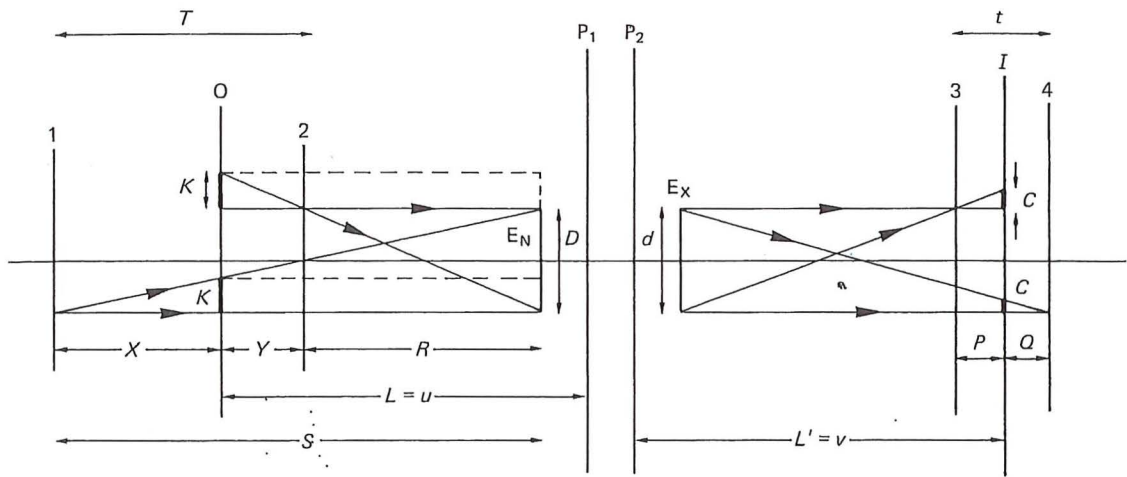


Figure 4.19 Geometry of image formation for depth of field

The obsolete 'whole-plate' size of 6.5 × 8.5 inches (165 × 216 mm, with a diagonal of some 270 mm), fitted neatly into the cone of vision at a distance of about 10 inches, and indeed for early photography was the usual size for contact prints for hand viewing. The standard lens for this format had a focal length of 10 inches (250 mm), and a contact print viewed at  $D_v$  gave correct perspective. A value of approximately 0.2 mm could be used for  $C$  to determine the required lens performance and depth of field.

Smaller formats, especially 24 × 36 mm, require enlargement to give a print for viewing at  $D_v$  with correct perspective (Figure 4.18). According to the 'rules' of perspective, a satisfactory visual rendering is given of an image corresponding spatially to the original scene when viewed at a distance equal to the focal length of the taking lens. Strictly a 24 × 36 mm image taken with a 50 mm lens should be viewed as a contact print at 50 mm, which is less than  $D_v$ . In practice an enlargement is viewed at 250 mm, but correct perspective is retained providing the proportional increase in viewing distance corresponds numerically to the degree of enlargement or print magnification  $M$ .

Obviously the value of  $C$  in the camera image must be related to subsequent enlargement and correspondingly reduced as enlargement increases. A linear enlargement of ×8 from a 24 × 36 mm negative is common practice: it gives a resultant print of 192 × 288 mm, suited to 8 × 10 inch (203 × 254 mm) print material, a size readily viewable within the cone of vision. This implies a minimum resolving power of 40 cycles/mm or  $\text{lp mm}^{-1}$  for the camera lens, the product of ×8 enlargement and visual performance of 5  $\text{lp mm}^{-1}$ . The latter value also relates usefully to the

resolving power of photographic printing paper which is approximately 6  $\text{lp mm}^{-1}$ .

To summarize, the permissible diameter of the circle of confusion must be reduced if subsequent enlargement is to take place. In practice values of  $C$  from 0.025 to 0.033 mm are used for the 24 × 36 mm format to allow ×8 enlargement. Values of 0.06 mm and 0.1 mm are used for medium and large formats respectively.

It is worth noting that in the early days of small-format photography a criterion of 1/1000 of the focal length of the lens was used for  $C$ , giving 0.05 mm for the 50 mm lens, which was for a long time the standard lens used for the 24 × 36 mm format, and correspondingly different values for different focal lengths. This criterion was in use for many years and is still quoted by some sources. It gives values for depth of field which imply different degrees of enlargement for different focal lengths. Some confusion has arisen on depth of field matters, especially in the provision of tables and scales, as well as comparisons between equivalent lenses from different sources. The idea of  $C=f/1000$  is now deprecated, and instead the value of  $C$  is taken as constant for a given format, for the whole range of lenses.

## Depth of field equations

### Derivations

Useful equations for the calculation of depth of field (and depth of focus) are derived from the geometry of image formation, as shown in Figure 4.19. A lens of focal length  $f$  is focused on subject plane  $O$ , distant  $L$  from the front principal plane  $P_1$ , with conjugate

image plane I distant  $L'$  from  $P_2$ . Image magnification is  $m$ . The entrance and exit pupils  $E_N$  and  $E_X$  have diameters  $D$  and  $d$  respectively. Plane O is also distant  $u$  from  $E_N$ . There are two other planes, 1 and 2, at distances  $R$  and  $S$  from  $E_N$ , rays from which to  $E_N$  intersect plane O in small circles of diameter  $K$  to be imaged in plane I as circles of confusion, diameter  $C$ , where  $C = mK$ .

In the object space, from similar triangles,

$$S = \frac{uD}{D - K} \quad (13)$$

$$R = \frac{uD}{D + K} \quad (14)$$

Now  $m = L'/L = v/u$ , and the effective aperture  $N' = v/D$ , so that  $D = um/N'$ . Taking  $D = uL'/N'L$  and also  $K = CL/L'$ , then, substituting for  $D$  and  $K$  in equations (13) and (14),

$$S = \frac{u \left( \frac{uL'}{N'L} \right)}{\left( \frac{uL'}{N'L} \right) - \left( \frac{CL}{L'} \right)} \quad \text{and} \quad R = \frac{u \left( \frac{uL'}{N'L} \right)}{\left( \frac{uL'}{N'L} \right) + \left( \frac{CL}{L'} \right)}$$

So that

$$S = \frac{u^2(L')^2}{u(L')^2 - N'CL} \quad \text{and} \quad R = \frac{u^2(L')^2}{u(L')^2 + N'CL}$$

Considering the general photographic case, for distant subjects where  $m$  is less than unity, the object plane is near infinity, so we may put  $L'$  approximately equal to  $f$ . Likewise,  $N'$ , the effective aperture, may be replaced by  $N$ , the relative aperture. For simple and symmetrical lenses, the pupils are located in the principal planes, so we may take  $L = u$ . Hence

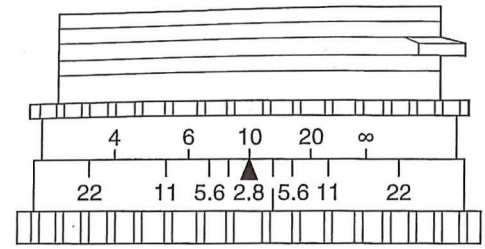
$$S = \frac{uf^2}{f^2 - NCu} \quad (15)$$

$$R = \frac{uf^2}{f^2 + NCu} \quad (16)$$

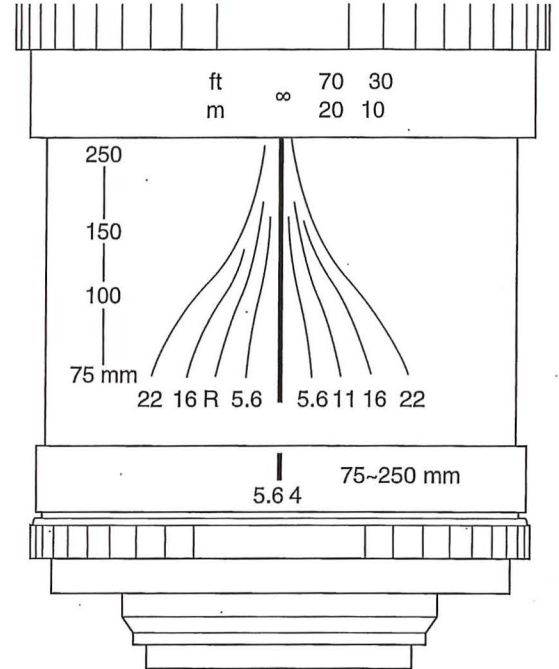
The values of  $S$  and  $R$  define the far and near limits respectively of the depth of field, when the lens is focused on distance  $u$ . The values may be tabulated in various ways, displayed in graphical form or provided as depth of field scales on the focusing mounts of lenses (Figure 4.20).

If depth of field ( $T$ ) is defined as  $T = S - R$  then

$$T = \frac{2f^2u^2NC}{f^4 - N^2C^2u^2} \quad (17)$$



(a)



(b)

Figure 4.20 Visual indication of depth of field. (a) Depth of field indicator scale. (b) Converging scales on a 75-250 mm  $f/4$  zoom lens, including an infrared focus correction mark R

For practical purposes the  $N^2C^2u^2$  term in the denominator may be disregarded, so to a first approximation

$$T = \frac{2u^2NC}{f^2} \quad (18)$$

This equation finds many useful applications.

Depth of field is directly proportional to the diameter of the circle of confusion, the  $f$ -number and the square of the focused distance, and inversely



proportional to the square of the focal length of the lens. Subject distance and focal length have the greatest influence; doubling the value of  $u$  increases  $T$  fourfold, while doubling focal length reduces  $T$  (at a fixed distance) by a factor of four.

It is of interest to note that equation (16) shows that a short-focus lens yields more depth of field than one of longer focus, provided that both are used to give the same magnification of a particular subject, in which case the two values of  $u$  differ. For example, using  $C = 0.025$  mm, a lens of focal length 100 mm focused at 5 m and with an aperture of  $f/4$  gives a magnification of 0.0204 and depth of field 501 mm. If a lens of focal length 25 mm is used, with  $u$  reduced to 1.25 m to give the same magnification, the depth of field at  $f/4$  is now 521 mm, a little greater. However, subjective effects regarding the changed viewpoint for the subject and different performances from the two lenses can give a further subjective impression of a greater depth of field, as there is no fixed boundary that separates 'sharp' from 'unsharp'.

When the subject is closer, say 2 m for the 100 mm lens and a corresponding 0.5 m for the 25 mm lens, the depth of field at  $f/4$  is 80 mm for both lenses, so that, in theory, there should be no difference.

The differences in practice are due to the approximations and assumptions made in deriving the formulae. Use of the simplified equation (17) gives identical results in both examples. In the alternative case of a fixed viewpoint and constant  $u$ , with the value of  $f$  altered by use of zoom lens (or interchangeable lens) followed by different degrees of enlargement to give the same final print magnification, then when viewed at  $D_v$ , the depth of field will be seen to remain essentially constant when the actual diameter of the aperture of the lens remains unaltered. Thus combinations of 100 mm at  $f/11$ , 50 mm at  $f/5.6$  and 25 mm at  $f/2.8$ , all have the same depth of field for a fixed viewpoint.

Note that the use of the criterion of  $C = f/1000$  gives different values for both lenses in the example above and would indicate that depth of field is greater for the longer focal length in such circumstances, which is incorrect.

### Departures from theory

The theory developed above assumes a truly circular circle of confusion; but this is not always so and marked departures from circular are found in anamorphic lenses, lenses with uncorrected aberrations and catadioptric (mirror) lenses. The 'circle of confusion' for the last of these is an annulus (caused by the central opaque disc inside the lens), and its effect can clearly be seen in out-of-focus detail. In the special case of a soft-focus lens, where uncorrected spherical aberration is used to give the desired soft effect with a core of sharpness, the

diameter of the blur circle cannot be defined and calculations are meaningless. The so-called *deep-field lens* is often incorrectly taken to mean a lens possessing enhanced depth of field, but the effect is due to anti-reflection coatings which provide increased light transmittance, so that a reduced aperture may be used for a given exposure level compared with a lens of lower transmittance. It is the smaller aperture that gives the increased depth of field, not any special correction of aberrations. In practice, for an ordinary aberration-limited lens, progressive stopping down brings the depth of field closer to predicted values until diffraction effects occur.

### Hyperfocal distance

Maximum depth of field in any situation is obtained by use of the hyperfocal distance. The value of  $S$ , the far limit of  $T$ , is given by equation (15). The *hyperfocal distance* ( $h$ ) is defined as the value of a particular focus setting  $u$  of the lens, which makes  $S$  equal to infinity. The necessary condition is  $f^2 = NCu$ ; then, as  $u = h$ ,

$$h = \frac{f^2}{NC} \tag{19}$$

The concept of  $h$  allows simplification of equations (15) and (16) to

$$S = \frac{hu}{h - u} \tag{20}$$

$$R = \frac{hu}{h + u} \tag{21}$$

And likewise

$$T = \frac{2hu^2}{(h^2 - u^2)} \tag{22}$$

From equation (21), if  $u$  equals  $h$ , then  $R$  is  $h/2$ ; when  $u$  is infinity, then  $R$  equals  $h$ . So if the lens is focused at a distance  $u$  so that  $u$  equals  $h$ , then the near limit of the depth of field is  $h/2$ . This gives the maximum depth of field, from infinity to  $h/2$ , for a given aperture  $N$ .

Cameras with fixed-focus lenses have the focus set on the hyperfocal distance (for the maximum aperture if this is variable) so as to give maximum depth of field.

### Close-up depth of field

Close-up photography is defined as photography where the distance from the subject to the lens is such



pth of  
'mm  
rk R

the  
first

(18)

the  
and  
rsely

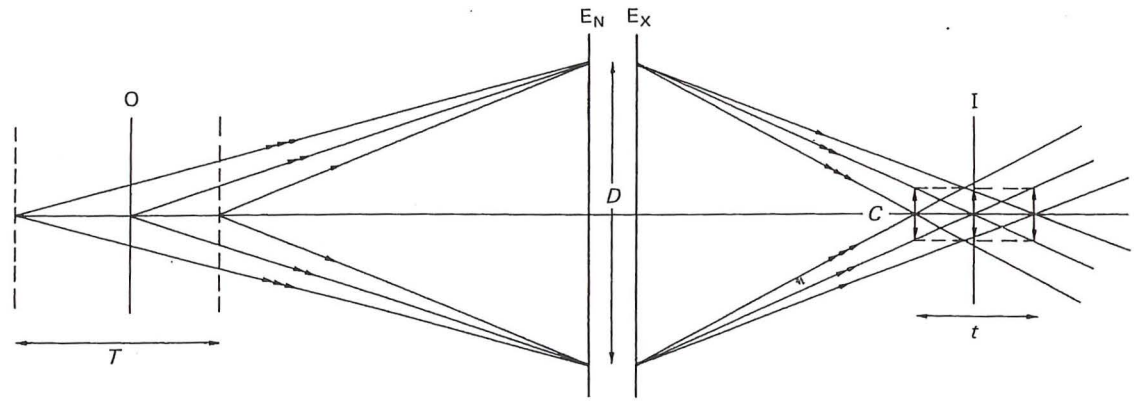


Figure 4.21 Conjugate relationship between depth of field  $T$  and depth of focus  $t$ , where  $T = mt$

that magnification  $m$  is in the range 0.1 to 1.0. Referring again to Figure 4.19, the close-up depth of field  $T$  may be taken as the sum of distances  $X$  and  $Y$ , the respective distances of planes 1 and 2 from the plane of focus  $O$ , where

$$X = \frac{uK}{D - K}$$

$$Y = \frac{uK}{D + K}$$

As these planes are close to the entrance pupil, the value of  $K$  is much smaller than  $D$  and so can be neglected in the denominators, giving

$$X = Y = \frac{uK}{D}$$

Now  $u/D$  can be replaced by  $N'/m$ , and also  $C = mK$ , therefore

$$X = Y = \frac{CN'}{m^2}$$

The effective aperture  $N'$  may be replaced by  $N(1 + m)$ , where  $N$  is the marked  $f$ -number. As  $T = X + Y$ , we have

$$T = \frac{2CN(1 + m)}{m^2} \quad (23)$$

Equation (23) does not involve focal length directly, so for a given magnification a long focal length is preferable to a short focal length, as it gives a longer working distance and better perspective by virtue of its more distant viewpoint, without any change in depth of field for a given  $f$ -number. Unlike general photography, the final magnification  $Z$  in the

print of the subject is usually stated. So for a print enlargement of  $M$ ,  $Z = mM$ .

### Depth of focus

The term *depth of focus* applies only to the image space (Figure 4.21) and is the tolerance in the position of the film plane  $I$ , which depends on the acceptable diameter  $C$  of the circle of confusion (Figure 4.19). Alternatively, it may be regarded as the distance between the conjugate planes 3 and 4 either side of image plane  $I$ , corresponding to planes 1 and 2 respectively, which define depth of field. Planes 3 and 4 are distant  $P$  and  $Q$  respectively from plane  $I$ , and the cones of light from the exit pupil  $E_X$  of diameter  $d$  coming to focus on planes 3 and 4 form blur circles of diameter  $C$  on plane  $I$ , which is distant  $v$  from  $P_2$ , the rear principal plane. From similar triangles,

$$P = \frac{vC}{d + C}$$

$$Q = \frac{vC}{d - C}$$

But  $C$  is small compared with  $d$  and may be removed from the denominators, so

$$P = Q = \frac{vC}{d}$$

Remembering  $N' = v/d$  and also  $N' = N(1 + m)$ , the depth of focus ( $t$ ) is the sum of  $P$  and  $Q$ , so

$$t = 2CN(1 + m) \quad (24)$$

$$t = \frac{2CNv}{f} \quad (25)$$



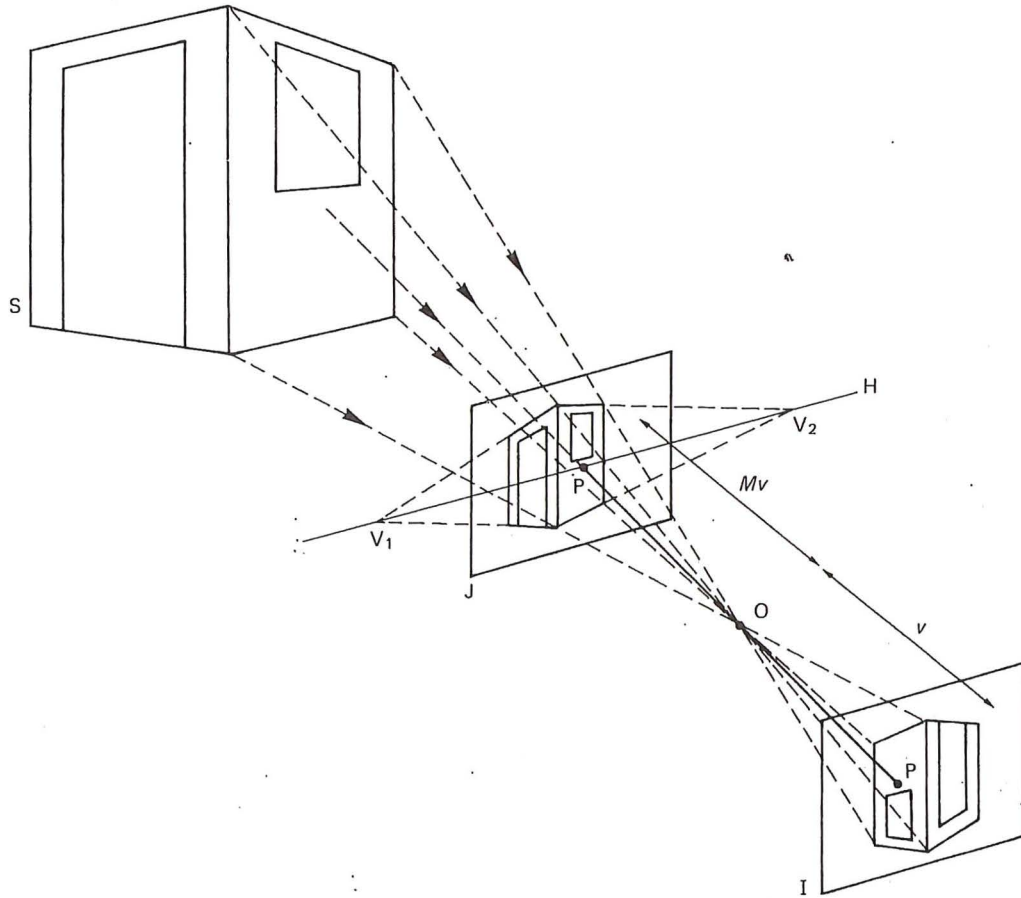
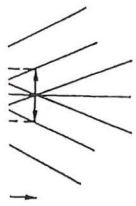


Figure 4.22 Elements of central perspective. In the diagram S represents the subject, I the optical image, O the centre of perspective, P the principal point, OP the principal distance, J the perspective of the subjected or picture plane,  $V_1$  and  $V_2$  the vanishing points, H the horizon line

For general photography where  $m$  is small, equations (24) and (25) reduce to

$$t = 2CN \tag{26}$$

For a large-aperture lens the depth of focus is small and the film gate or photoplane must be accurately perpendicular to the optical axis. The necessary tolerances can be relaxed for large formats where  $C$  is greater and small apertures are used; but even so, a 75 mm  $f/4.5$  wide-angle lens used on a 4 × 5 inch format has only 0.9 mm depth of focus at full aperture (assuming  $C$  is 0.1 mm), so the position of the film surface in a dark-slide or roll film back must correspond very accurately to the plane of the focusing screen.

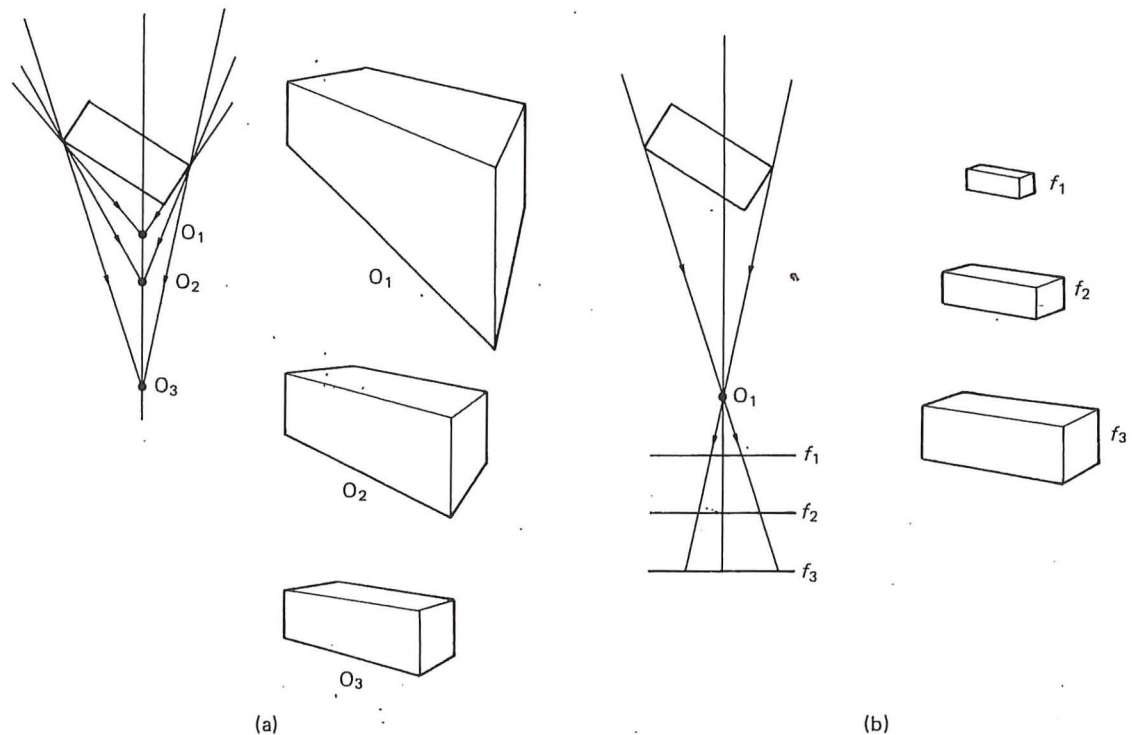
When a lens is focused close up, so that  $m$  has a significant value, the depth of focus is increased. The use of small apertures also increases depth of focus.

## Perspective

### Viewpoint

The term 'perspective' literally means 'to look through'; and an accurate record of the spatial relationships of objects in a scene can be obtained by placing a glass plate, 'the picture plane', in the observer's FOV, and tracing the necessary outlines on it. The reduced-size facsimile records the intersection of the projection of each subject point, converging to the *centre of perspective* or *viewpoint* (Figure 4.22), then diverging to the image plane.

The *viewpoint* is the centre of the pupil of the eye of the observer. Conventionally the picture plane is vertical, so that vertical lines in the subject remain vertical and parallel. Horizontal lines in planes parallel to the picture plane also remain horizontal and parallel, but in inclined subject planes they will



**Figure 4.23** Perspective in an image related to camera viewpoint and focal length. (a) Subject appearance due to reducing the viewpoint distance and increasing the field of view of the lens. (b) From a fixed viewpoint, an increase in principal distance or focal length leaves the perspective unchanged but size altered

converge to one or more *vanishing points*, positioned on the *horizon line* of the facsimile where the visual axis intersects it at the *principal point*. The orthogonal distance between the picture plane and viewpoint is the *principal distance* of the perspective record.

By the geometry of the situation, alteration of the principal distance alters only the size of the picture and not the perspective of the spatial relationships. However, alteration of the viewpoint in terms of distance from the subject will alter the convergence and hence alter perspective.

The perspective of the scene is correctly reconstructed only by viewing from the principal distance, which is then termed the *viewing distance* ( $D$ ).

### Camera viewpoint

A camera records a three-dimensional scene as a two-dimensional planar image in the photoplane and in the print. By placing the camera lens at the visual viewpoint, familiar photographic parameters replace the terminology of perspective as defined above.

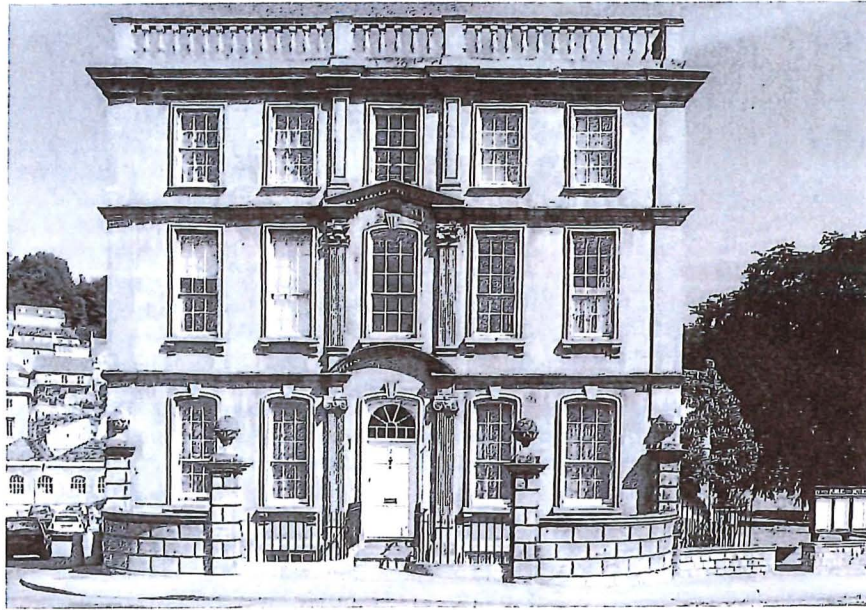
The convergent rays form a *central perspective* by passing through the lens, and continue diverging

beyond the viewpoint to an image plane conjugate to the subject plane. The principal distance is now the image conjugate  $v$ , commonly taken as the focal length  $f$  for distant scenes. The facsimile or photographic record is now inverted and laterally reversed but can be contact printed and 'flopped' to position in the picture plane for viewing at correct distance  $D = v$ .

Various points need clarification. By altering the lens to one of longer focal length,  $v$  is increased and the image enlarged; but it retains identical perspective. So a change of focal length for a given viewpoint does not alter perspective but only image size. By altering viewpoint by changing the object conjugate  $u$ , the perspective *does* change, the more obviously since a lens of large FOV may be used to include the same area of the subject from a closer viewpoint (Figure 4.23). Such 'steep' perspective can be used to dramatic effect. Figure 4.24 illustrates the alteration of perspective given by a change of viewpoint with a building chosen as the subject to show also two possible pictorial 'treatments' of the subject. A distant central viewpoint with a medium long focus lens gives an accurate view of the front elevation. A closer off-centre viewpoint with a wide-



$f_2$



ing the  
ce or

gate to  
ow the  
focal  
photo-  
versed  
tion in  
e  $D =$

ng the  
ed and  
l per-  
given  
image  
object  
; more  
used to  
closer  
ve can  
tes the  
ge of  
ject to  
of the  
edium  
e front  
wide-

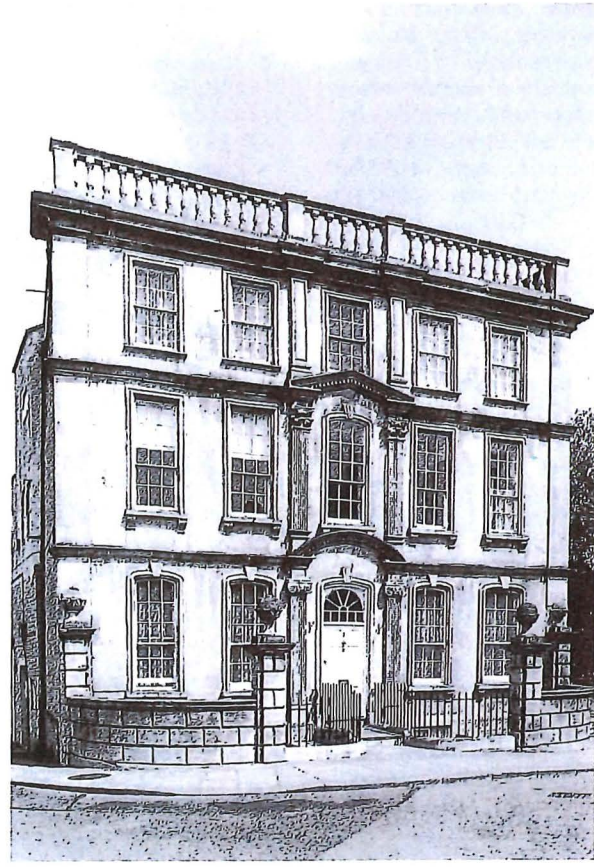


Figure 4.24 Perspective and viewpoint. (a) Distant central viewpoint. (b) Closer oblique viewpoint

angle lens plus some rising front movement changes the shape to retain verticals, while giving more depth to the subject.

### Perspective distortion

The centre of perspective or viewpoint of a camera lens is the centre of the entrance pupil for object space. The centre of the exit pupil is the centre of projection for image space. The correct viewing distance is then given by

$$D = v = f(1 + m) \quad (27)$$

This theoretical value of  $D$  cannot usually be used, especially if it is less than  $D_v$ . Small images need to be enlarged by magnification  $M$  for comfortable viewing and the viewing distance is then given by

$$D = Mv \quad (28)$$

For distant scenes,  $v$  is replaced by  $f$  as usual.

The correct-viewing-distance criterion is seldom observed for photographic images, prints being viewed at a convenient distance, irrespective of the values of  $f$  and  $M$  used (usually these are not known to the observer). Incorrect viewing gives rise to

perspective distortions. In pictorial terms, a near viewpoint gives a 'steep perspective' with large changes of scale in a subject, while a distant viewpoint gives a 'flattened perspective' with only small changes of scale even in a subject of considerable depth. The perspective of a print viewed from too great a distance tends to appear steep, while that of a print viewed from too short a distance tends to appear flat. This is the reverse of the perspective effects achieved on taking the picture.

### Bibliography

- Blaker, A. (1985) *Applied Depth of Field*. Focal Press, Stoneham, MA.
- Freeman, M. (1990) *Optics*, 10th edn. Butterworths, London.
- Hecht, E. (1998) *Optics*, 3rd edn. Addison-Wesley, Reading, MA.
- Jenkins, F. and White, H. (1981) *Fundamentals of Optics*, 4th edn. McGraw-Hill, London.
- Kingslake, R. (1992) *Optics in Photography*. SPIE, Bellingham, WA.
- Ray, S. (1984) *Applied Photographic Optics*, 2nd edn. Focal Press, Oxford.



Ralph E Jacobson • Sidney F Ray  
Geoffrey G Attridge • Norman R Axford

# THE MANUAL OF Photography

Photographic and Digital Imaging

NINTH EDITION

**The Manual of Photography** is the standard work for anyone who is serious about photography - professional photographers and lab technicians or managers, as well as students and enthusiastic amateurs who want to become more technically competent. The authors provide comprehensive and accessible coverage of the techniques and technologies of photography.

The Manual has aided many thousands of photographers in their careers. The ninth edition now brings this text into a third century, as the first edition dates from 1890.

**MAJOR NEW UPDATES FOR THE NINTH EDITION INCLUDE:**

- coverage of digital techniques - more emphasis on electronic and hybrid media
- greater coverage of colour measurement, specification and reproduction - illustrated with a new colour plate section

Dealing with the fundamental principles as well as the practices of photography and imaging, the Manual topics range from optics to camera types and features, to colour photography and digital image processing and manipulation.

The authors write in a reader-friendly style, using many explanatory illustrations and dividing topics into clear sections.

**REVIEWS OF PREVIOUS EDITIONS INCLUDE:**

'I can offer no better recommendation.' **BRITISH JOURNAL OF PHOTOGRAPHY**

'A respected pedigree... a most comprehensive explanation of the essential principles behind the practical applications of silver-based photography.' **THE PHOTOGRAPHIC JOURNAL**

The authors all lecture in Photographic and Digital Imaging at the University of Westminster, UK.



**Focal Press**

An imprint of Butterworth-Heinemann

<http://www.focalpress.com>

