

# DIGITAL COMMUNICATIONS

**John G. Proakis**

**THIRD EDITION**

McGraw-Hill Series in Electrical and Computer Engineering

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Third Edition

**John G. Proakis, Ph.D., P.E.**

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#### DIGITAL COMMUNICATIONS

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