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^M Radio Inc. - Ex. 1013, p.

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1.1 Representation of Bandpass signals

A calculated particle (i.e., the signal of Figure Constrained in the signal of Figure where the state convenient and the convenient Whencalled 1

 $\frac{a}{r}$ with the characterization of bandpass such as $r = \frac{a}{r}$ nathematical representation of bandpass stationary stochastic $\sqrt{2}$ we present a vector space representation of $\frac{1}{60}$ are vertex interface power versus interface power were power and the power were power were average power. In this capture were $\frac{1}{60}$ $\frac{1}{\omega}$ systems that are usually encountered in the usually encountered in the usually encountered in the usual

\mathbf{v} $\overline{\mathbf{B}}$ ENIATIO **D SYSTEMS**

formation-bearing signals are transmitted by some type of carrier $p \rightarrow p$ channel over which the signal is trans interval of frequencies centered about the carrier, as in doubleuch smaller than the carrier frequency are termed narrowband tratedcomponents and the state of the

bandpass signals and channels (systems). The modulation performed at the transmitting end of the communication system to generate the bandpass signal and the demodulation performed at the receiving end to recover the digital information involve frequency translations. With no loss in generality and for mathematical convenience, it is desirable to reduce all bandpass signals and erformance of the various modulation and niques presented in the subsequent chapters are independent of carrier frequencies and channel frequency bands. The representation of bandpass signals and signals andsystems in terms of equivalent lowpass waveforms and the bandpass stationary stochastic processes are the main topics of this section. involvements. With no loss in generality and for loss in generality and for loss in generality and for \mathbf{r}

to reduce all bandpass Signals and equivalent in the channels. As a consequence is a consequence, the channels. As a consequence, the consequence

A real-valued signal $g(t)$ with a frequency content concentration of frequencies in the vicinity of a frequency f can be expre

$$
s(t) = a(t)\cos\left[2\pi f_c t + \theta(t)\right]
$$
\n(3.1.1)

where $a(t)$ denotes the amplitude (envelope) of $s(t)$, and $\theta(t)$ denotes the phase convenient frequency within or near the frequency band occupied by the signal.
When the band of frequencies occupied by $s(t)$ is small relative to f_c , the signal is ategorized in a number of different ways such as random versus called a *narrowband bandpass signal* or, simply, a *bandpass signal*.

By expanding the cosine function in (3.1.1) a second representation for $s(t)$ α and α , halo and α $\mathcal{O}(\mathcal{O}_\mathcal{A})$ (3.1.1) (3.1.1) (3.1.1) (3.1.1)

$$
s(t) = a(t)\cos\theta(t)\cos 2\pi f_c t - a(t)\sin\theta(t)\sin 2\pi f_c t
$$

= $x(t)\cos 2\pi f_c t - y(t)\sin 2\pi f_c t$ (3.1.2)

 frequencywhere the signals $x(t)$ and $y(t)$, termed the *quadrature components* of $s(t)$, are defined as

$$
x(t) = a(t) \cos \theta(t)
$$

$$
y(t) = a(t) \sin \theta(t)
$$
 (3.1.3)

The frequency content of the quadrature compared at law frequencies (example $f = 0$) as components are appropriately called *lowpass signals*. Finall the signals $\lim_{t \to \infty} f(t)$ is obtained from (3.1.1) by defining the components of squadrature components of squadrat

$$
u(t) = a(t)e^{j\theta(t)} = x(t) + jy(t)
$$
 (3.1.4)

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$$
s(t) = \text{Re}\left[u(t)e^{j2\pi f_c t}\right]
$$
\n(3.1.5)

where Re | denotes the real part of the complex-val for s(t) is obtained from (3.1.1) by defining the complex envelope u(t) as \cdots

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REPRESENTATION

SYSTEMS

The Fourier transform of $s(t)$ is

$$
S(f) = \int_{-\infty}^{\infty} s(t) e^{-j2\pi ft} dt
$$

=
$$
\int_{-\infty}^{\infty} \left\{ \text{Re} \left[u(t) e^{j2\pi f_c t} \right] \right\} e^{-j2\pi ft} dt
$$
 (3.1.6)

Use of the identity

$$
Re(\xi) = \frac{1}{2}(\xi + \xi^*)
$$
 (3.1.7)

$$
S(f) = \frac{1}{2} \int_{-\infty}^{\infty} \left[u(t) e^{j2\pi f_c t} + u^*(t) e^{-j2\pi f_c t} \right] e^{-j2\pi ft} dt
$$

= $\frac{1}{2} \left[U(f - f_c) + U^*(-f - f_c) \right]$ (3.1.8)

where $U(f)$ is the Fourier transform of $u(t)$. Since the frequency content of the bandpass signal $s(t)$ is concentrated in the vicinity of the carrier f_c , the result in (3.1.8) indicates that the frequency content of $u(t)$ is concentrated in the vicinity

(3.1.8) indicates that the frequency content of $u(t)$ is concentrated in the vicinity

The signal $a^2(t) \cos{4\pi f(t + 2\theta(t))}$ $\frac{1}{2}$ is used in $\frac{1}{2}$ is used in $\frac{1}{2}$, we obtain the following results in $\frac{1}{2}$,,,,,,,,,

The energy in the signal $s(t)$ is defined as

$$
\mathscr{E} = \int_{-\infty}^{\infty} s^2(t) dt
$$

=
$$
\int_{-\infty}^{\infty} {\Re e [u(t) e^{j2\pi f_c t}]}^2 dt
$$

$$
= \int_{-\infty}^{\infty} {\Re e [u(t) e^{j2\pi f_c t}]}^2 dt
$$
 (3.1.9)

 α (3.1.7) is used in (3.1.9), we obtain the following result:

$$
\mathcal{E} = \frac{1}{2} \int_{-\infty}^{\infty} |u(t)|^2 dt
$$

+ $\frac{1}{2} \int_{-\infty}^{\infty} |u(t)|^2 \cos [4\pi f_c t + 2\theta(t)] dt$ (3.1.10)

Consider the second integral in (3.1.10). Since the signal $s(t)$ is narrowband, the real envelope $a(t) = |u(t)|$ or, equivalently, $a^2(t)$ varies slowly relative to the rapid variations exhibited by the cosine function. A graphical illustration of the integrand in the second integral of (3.1.10) is shown in Fig. 3.1.1. The value
of the integral is just the net area under the cosine function modulated by $a^2(t)$. Using (3.1.12), we have Since the modulating waveform $a^2(t)$ varies slowly relative to the cosine function, the net area contributed by the second integral is very small relative to the value of the first integral in (3.1.10) and, hence, it can be neglected. Thus, for all practical purposes, the energy in the bandpass signal $s(t)$, expressed in terms of the equivalent lowpass signal $u(t)$, is

$$
\mathscr{E} = \frac{1}{2} \int_{-\infty}^{\infty} |u(t)|^2 dt \qquad (3.1.11)
$$

where $|u(t)|$ is just the envelope $a(t)$ of $s(t)$.

$3.1.2$ **Representation of Linear Bandpass Systems**

A linear filter or system may be described either by its impulse
by its frequency response $H(f)$, which is the Fourier transfor $h(t)$ is real,

$$
H^*(-f) = H(f)
$$

Let us define $C(f - f_c)$ as

$$
C(f - f_c) = \begin{cases} H(f) & f > 0 \\ 0 & f < 0 \end{cases}
$$

$$
C^*(-f-f_c) = \begin{cases} 0 & f > 0\\ H^*(-f) & f < 0 \end{cases}
$$

$$
H(f) = C(f - f_c) + C^*(-f - f_c) \qquad \qquad \stackrel{\geq}{\equiv} \qquad \qquad
$$

The inverse transform of $H(f)$ in (3.1.15) yields $h(t)$ in the for

$$
h(t) = c(t)e^{j2\pi f_c t} + c^*(t)e^{-j2\pi f_c t}
$$

= 2 Re [c(t) e^{j2\pi f_c t}]

where $c(t)$ is the inverse Fourier transform of $C(f)$. In gene response $c(t)$ of the equivalent lowpass system is complex-value

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 f°° s(z)e-fl"f'dt {ReRe(£) %/_00 [u(t)ej2-nfct Hum—f.) Fourier transform concentrated frequency complex-valued in the signal s(t) is defined as 2-f_°°|u(t)|2dt Find authenticated [court documents without watermarks](https://www.docketalarm.com/) at docketalarm.com.

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signal u(t), is

°°

$$
\begin{aligned}\n\text{from of } s(t) \text{ is} \\
f) &= \int_{-\infty}^{\infty} s(t) e^{-j2\pi ft} \, dt \\
&= \int_{-\infty}^{\infty} \left\{ \text{Re} \left[u(t) e^{j2\pi f_c t} \right] \right\} e^{-j2\pi ft} \, dt \tag{3.1.6} \\
\text{Re} \left(\xi \right) &= \frac{1}{2} \left(\xi + \xi^* \right) \tag{3.1.7}\n\end{aligned}
$$

$$
[U(f - f_c) + U^*(-f - f_c)] \qquad (3.1.8)
$$

concentrated in the vicinity of the c the complex-valued waveform $u(t)$ is basically a low-pass
ence, is called the *equivalent lowpass signal*.
signal $s(t)$ is defined as

$$
\mathscr{E} = \int_{-\infty}^{\infty} s^2(t) dt
$$

=
$$
\int_{-\infty}^{\infty} {\{\text{Re}[u(t) e^{j2\pi f_c t}]\}}^2 dt
$$
 (3.1.9)

 (1.7) is used in $(3.1.9)$, we obtain the

$$
\frac{1}{2}\int_{-\infty}^{\infty} |u(t)|^2 dt
$$
\n
$$
+\frac{1}{2}\int_{-\infty}^{\infty} |u(t)|^2 \cos [4\pi f_c t + 2\theta(t)] dt
$$
\n(3.1.10)

egral in (3.1.10). Since the signal $s(t)$ is narrowband, the in (3.1.7) is used in (3.1.9), we obtain the following result: Let $\frac{1}{2}$ avelon $u(t)$ varies slowly felally 1 in (3.1.10) and, hence, it can be neglected. Thus, for all energy in the bandpass signal $s(t)$, expressed in terms of ignal $u(t)$, is

$$
\mathscr{E} = \frac{1}{2} \int_{-\infty}^{\infty} |u(t)|^2 dt
$$
 (3.1.11)

avelope $a(t)$ of $s(t)$. by the second integral is very small relative to the

(3.1.10) and, hence, it can be neglected. The neglected \sim in the bandpass signal s(t), expresse^d in terms of

3.1.2 Representation of Linear Bandpass Systems

by its frequency response $H(f)$, which is the Fourier transform of $h(t)$. Since

$$
H^*(-f) = H(f) \tag{3.1.12}
$$

$$
C(f - f_c) = \begin{cases} H(f) & f > 0 \\ 0 & f < 0 \end{cases}
$$
 (3.1.13)

its frequency response \mathcal{L}_{max}

FIGURE 1999

is
Lista de la provincia de la
Lista de la provincia de la pr real,

3.1.1

signal a2(t)cos $\frac{4}{3}$

linear filter or system

define

inverse transform

$$
C^*(-f - f_c) = \begin{cases} 0 & f > 0\\ H^*(-f) & f < 0 \end{cases}
$$
 (3.1.14)

$$
H(f) = C(f - f_c) + C^*(-f - f_c)
$$
 (3.1.15)

$$
h(t) = c(t)e^{j2\pi f_c t} + c^*(t)e^{-j2\pi f_c t}
$$

= 2 Re [c(t)e^{j2\pi f_c t}] (3.1.16)

 \mathcal{S} , we have have have \mathcal{S} sponse $c(t)$ of the equivalent lowpass system is complex-

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