



**Proceedings** 

# THIRTY-SEVENTH ANNUAL ALLERTON CONFERENCE ON COMMUNICATION, CONTROL AND COMPUTING

September 22 - 24, 1999

Allerton House, Monticello, Illinois

Sponsored by the

Coordinated Science Laboratory and the

Department of Electrical and Computer Engineering of the

University of Illinois at Urbana-Champaign

Apple v. Caltech

IPR2017-00210

Replacement - Apple 1002

HUGHES00883604

#### **PROCEEDINGS**

# THIRTY-SEVENTH ANNUAL ALLERTON CONFERENCE ON COMMUNICATION, CONTROL, AND COMPUTING

3 1924 077 849 721

Bruce Hajek R.S. Sreenivas Conference Co-Chairs



Conference held September 22, September 23, and September 24, 1999 Allerton House Monticello, Illinois

Sponsored by
The Coordinated Science Laboratory
and
The Department of Electrical and Computer Engineering
of the
UNIVERSITY OF ILLINOIS
at
Urbana-Champaign

#### TABLE OF CONTENTS

FORWORD		****
,	WORKS I S.P. Meyn and R. Srikant (University of Illinois at Urbana-Champaign) S.P. Meyn (University of Illinois at Urbana-Champaign)	
REPRESENTATION AND F. Baccelli, S. Gau	EXPANSION OF (MAX, PLUS) LYAPUNOV EXPONENTSbert, and D. Hong	1
MARTINGALE PROBLEM T.G. Kurtz and R.F	1S AND LINEAR PROGRAMS FOR SINGULAR CONTROL I. Stockbridge	11
STATIONARY REFLECTE T. Konstantopoulos	ED LÉVY PROCESSES IN STOCHASTIC NETWORKSs and G. Last	21
Y. Joo, V. Ribeiro,	NABILITY ON THE BUFFER DYNAMICS IN IP NETWORKS	
QUEUEING NETWORKS M. Armony and N.	WITH INTERACTING SERVICE RESOURCESBambos	42
Organizers:	: DECODING AND CHANNELS  R. Koetter and R.E. Blahut (University of Illinois at Urbana-Champaign) A. Vardy (University of California, San Diego)	
A. Ashikhmin, A. E		
I. Dumer	OF REED-MULLER CODES	
LOSSLESS COMPRESSION J.L. Fan, B. Marcus	N IN CONSTRAINED CODINGs, and R. Roth	70
I-C: HYBRID/DISCRETE Chair:	-EVENT-DYNAMIC SYSTEMS R.S. Sreenivas (University of Illinois at Urbana-Champaign)	
R.S. Minhas and W		
S. Abdelwahed and		
STABILITY ANALYSIS FO	OR INTERCONNECTED HYBRID SYSTEMSS I. Ushio	13

DECENTRALIZED SUPERVISORY CONTROL OF CONCURRENT DISCRETE EVENT SYSTEMS WITH PARTIAL OBSERVATIONS	., 103
A NEW PROBABILISTIC APPROACH TO CONGESTION CONTROL IN COMMUNICATION NETWORKS H. Mortazavian and J. Mirkovic	113
A BIGRAPH MATCHING THEOREMS. Ayyorgun and R.L. Cruz	124
I-D: ACTIVE NETWORKS  Organizer/Chair: Y. Shavitt  (Bell Labs, Lucent Technologies)	
CHUNKS IN PLAN: LANGUAGE SUPPORT FOR PROGRAMS AS PACKETS	127
ON THE INTERFACE OF PROGRAMMABLE NETWORK ELEMENTS	137
BOWMAN AND CANES: IMPLEMENTATION OF AN ACTIVE NETWORK  S. Merugu, S. Bhattacharjce, Y. Chae, M. Sanders, K. Calvert, and E. Zegura	147
DESIGN OF A FLEXIBLE OPEN PLATFORM FOR HIGH PERFORMANCE ACTIVE NETWORKS S. Choi, D. Decasper, J. Dehart, R. Keller, J. Lockwood, J. Turner, and T. Wolf	157
IMPLEMENTING A CONCAST SERVICE	166
ACTIVE DISTRIBUTED MANAGEMENT FOR IP NETWORKS	176
I-F: SPACE-TIME METHODS FOR COMMUNICATION Chair: D. Sarwate	
(University of Illinois at Urbana-Champaign)  NEW APPROACH FOR SPACE-TIME TRANSMITTER/RECEIVER DESIGN	186
H. El Gamal and A.R. Hammons, Jr.	
INTERFERENCE SUPPRESSION FOR CDMA VIA A SPACE-TIME POWER MINIMIZATION BASED PREPROCESSOR WITH APPLICATIONS TO GPS W.L. Myrick, M.D. Zoltowski, and J.S. Goldstein	
SOFT-WEIGHTED TRANSMIT DIVERSITY FOR WCDMA	20
MULTIUSER DETECTION TECHNIQUES FOR COMBINED ARRAY PROCESSING AND SPACE-TIME BLOCK CODING B. Lu and X. Wang	21
A TRANSMIT ADAPTIVE ANTENNA SCHEME WITH FEEDBACK FOR WIRELESS COMMUNICATIONS	21

ν

II-A: CODING THEORY II: ITERATIVE DECODING AND TURBO CODES
Organizars: R. Koetter and K.E. Blanut
(University of Illinois at Urbana-Champaign)
Chair: R. Koetter (University of Illinois at Urbana-Champaign)
CONCENTRATE221 T. Richardson and R. Urbanke
EFFICIENT ENCODING OF LOW-DENSITY PARITY-CHECK CODES
T. Richardson and R. Urbanke
IRREGULAR TURBOCODES
B.J. Frey and D.J.C. Mackay
ON QUASI-CYCLIC REPEAT-ACCUMULATE CODES249
ON QUASI-CYCLIC REFERENCE AND ADDRESS OF THE PROPERTY OF THE P
THE SERIAL CONCATENATION OF RATE-1 CODES THROUGH UNIFORM RANDOM INTERLEAVERS 260 H.D. Pfister and P.H. Siegel
II-B: STOCHASTIC NETWORKS II Organizers: S.P. Meyn and R. Srikant (University of Illinois at Urbana-Champaign) Chair: R. Srikant (University of Illinois at Urbana-Champaign)
QUEUE LENGTH ASYMPTOTICS FOR MARKOVIAN SERVICE NETWORKS
EXACT ASYMPTOTICS FOR 1-LIMITED EXPONENTIAL POLLING MODELS
288
INVARIANT RATE FUNCTIONS FOR DISCRETE TIME QUEUES
LARGE DEVIATIONS AND OPTIMALITY OF THE LARGEST WEIGHTED DELAY FIRST DISCIPLINE
ON ESTIMATING BUFFER OVERFLOW PROBABILITIES UNDER MARKOV-MODULATED INPUTS
INDUCED BURSTINESS IN GENERALIZED PROCESSOR SHARING QUEUES WITH LONG-TAILED  TRAFFIC FLOWS
THE ASYMPTOTICS OF SELECTING THE SHORTEST OF TWO, IMPROVED

H-C: LEARNING ALGORITHMS IN SIGNAL PROCESSING  Organizers: A. Singer and M. Feder (University of Illinois at Urbana-Champaign and Tel Aviv University)  Chair: M. Feder (Tel Aviv University)	
UNIVERSAL FILTERING AND PREDICTION OF INDIVIDUAL SEQUENCES CORRUPTED BY NOISE3 A. Baruch and N. Merhav	
FAST RLS LAGUERRE ADAPTIVE FILTERING3 R. Merched and A.H. Sayed	
MACHINE LEARNING APPLICATIONS IN GRID COMPUTING	
REDUNDANCY OF THE LEMPEL-ZIV CODES3 S.A. Savari	
THE INFORMATION BOTTLENECK METHOD	168
THEORY MEETS PRACTICE: UNIVERSAL SOURCE CODING WITH THE BURROWS WHEELER TRANSFORM3 M. Effros	378
Organizers: M. Médard and E. Modiano (University of Illinois at Urbana-Champaign and Massachusetts Institute of Technology)  Chair: E. Modiano (Massachusetts Institute of Technology)	
OPTICAL SPACE COMMUNICATIONS AND NETWORKING3  V.W.S. Chan	388
ON THE BENEFITS OF CONFIGURABILITY IN WDM NETWORKS3  E. Modiano and A. Narula-Tam	390
NONBLOCKING WDM NETWORKS WITH FIXED-TUNED TRANSMITTERS AND TUNABLE  RECEIVERS4  T. Lin and G. Sasaki	‡0¢
ON NEW ARCHITECTURES FOR WDM NETWORKS4  A. Sen, T. Shah, and B.P. Sinha	402
ALL-OPTICAL LABEL SWAPPING WITH WAVELENGTH CONVERSION FOR WDM-IP NETWORKS WITH SUBCARRIER MULTIPLEXED ADDRESSING	414

# II-E: COMMUNICATION SYSTEMS AND SERVICES Chair: S. Lin (University of Hawaii)

ON DISCRETE SUFFICIENT STATISTICS FOR ACQUISITION IN ASYNCHRONOUS  BAND-LIMITED CDMA SYSTEMS4  A. Mantravadi and V.V. Veeravalli	124
FREQUENCY SYNCHRONIZATION ALGORITHM FOR FREQUENCY HOPPING SYSTEM BASED ON SINGULAR VALUE DECOMPOSITION4. A. Pouttu	34
A SOFTWARE-ORIENTED STREAM CIPHER FOR CELLULAR AND PERSONAL COMMUNICATIONS SERVICES	
BINARY RANK CRITERIA FOR PSK MODULATED SPACE-TIME CODES	13
TURBO CODES WITH ORTHOGONAL MODULATION IN DS-CDMA MOBILE RADIO SYSTEM WITH SHORT FRAME TRANSMISSION45 G. Li and Y.L. Guan	
AN INTERACTIVE CONCATENATED TURBO CODING SYSTEM	
BI-DIRECTIONAL SOVA DECODING FOR TURBO-CODES	I
II-F: FADING CHANNELS AND POWER CONTROL  Chair: D. Sarwate (University of Illinois at Urbana-Champaign)	
ANALYSIS OF AN UP/DOWN POWER CONTROL ALGORITHM IN CDMA REVERSE LINK UNDER FADING CONDITION	
A CLASS OF DISTRIBUTED ASYNCHRONOUS POWER CONTROL ALGORITHMS FOR CELLULAR WIRELESS SYSTEMS	
DISTRIBUTED CONNECTION ADMISSION CONTROL FOR POWER-CONTROLLED  CELLULAR WIRELESS SYSTEMS	
INTERFERENCE AVOIDANCE AND DISPERSIVE CHANNELS: A NEW LOOK AT MULTICARRIER MODULATION	
PERFORMANCE OF OPTIMAL CODES ON GAUSSIAN AND RAYLEIGH FADING CHANNELS: A GEOMETRICAL APPROACH	
IMPROVED MARKOV MODELS FOR FADING CHANNELS: ANALYSIS AND DESIGN	

Organizers:	III: ALGEBRAIC AND COMBINATORIAL CODING THEORY R. Koetter and R.E. Blahut (University of Illinois at Urbana-Champaign) N. Boston	
	(University of Illinois at Urbana-Champaign)	
ON THE CLASSIFICATIO P. Gaborit, W.C. H	N OF EXTREMAL ADDITIVE CODES OVER GF(4)uffman, JL. Kim, and V. Pless	535
TWO FAST ALGORITHM GL. Feng	S IN THE SUDAN DECODING PROCEDURE	545
FROM WEIGHT ENUMER I. Duursma	ATORS TO ZETA FUNCTIONS	555
ALTERNATIVE APPROAC CODES	CHES TO THE COMPUTATION OF ERROR VALUES FOR HERMITIAN	557
HI-B: STOCHASTIC NET Organizers:	S.P. Mevn and R. Srikant	
	(University of Illinois at Urbana-Champaign) S.P. Meyn (University of Illinois at Urbana-Champaign)	
LONG-TAILED INPUTS	YMPTOTICS IN HOL SERVICE SYSTEMS WITH HETEROGENEOUS Likhanov and R.R. Mazumdar	567
	TROL OF MANUFACTURING SYSTEMS — A FLUID APPROACH	577
MULTICLASS NETWORK POLICIES C. Maglaras	S IN HEAVY TRAFFIC: ASYMPTOTIC OPTIMALITY OF TRACKING	587
•	EUEING NETWORKS WITH SUFFICIENTLY FLEXIBLE RESOURCES	597
OPTIMALLY STABILIZIN P. Dupuis and R. A	NG CONTROLS FOR A DETERMINISTIC NETWORK MODEL	607
	OL AND DECISION MAKING  C. Beck (University of Illinois at Urbana-Champaign)	
PROBLEM IN THE PRESE	NT CONTROLLERS ON A BENCHMARK STRUCTURE PROTECTION ENCE OF CLASSIC EARTHQUAKES	617
DISK SENSITIVE DECISE	ON-THEORETIC TROUBLESHOOTING	627

H <sub>*</sub> CONTROL FOR MIXED DISTURBANCE REJECTION	
SOLVING POLYNOMIAL SYSTEMS IN ROBUST STABILITY ANALYSIS	
ROBUST, NEAR TIME-OPTIMAL CONTROL OF THIRD-ORDER UNCERTAIN SYSTEMS	51
A NEW CONVEX RELAXATION FOR ROBUST H <sub>2</sub> PERFORMANCE ANALYSIS OF UNCERTAIN LINEAR SYSTEMS	55
A NEW RESULT ON THE BELLMAN EQUATION FOR EXIT TIME CONTROL PROBLEMS WITH CRITICAL GROWTH DYNAMICS	7
III-D: OPTICAL NETWORKS II Organizers: M. Médard and E. Modiano (University of Illinois at Urbana-Champaign and Massachusetts Institute of Technology) Chair: M. Médard (University of Illinois at Urbana-Champaign)	
FAULT PROTECTION IN WDM MESH NETWORKS659 G. Ellinas	
A COMPARISON OF ALLOCATION POLICIES IN WAVELENGTH ROUTING NETWORKS	
OPTICAL BUFFERS FOR MULTI-TERABIT IP ROUTERS679 D.K. Hunter, I. Andonovic, and M.C. Chia	
THE λ-SCHEDULER: A MULTIWAVELENGTH SCHEDULING SWITCH	
ON DIFFERENT ROUTING STRATEGIES IN TRANSPARENT ALL-OPTICAL NETWORKS	
III-E: COMMUNICATION NETWORKS  Chair: R. Cruz  (University of California, San Diego)	
FRANSMISSION POLICIES FOR TIME VARYING CHANNELS WITH AVERAGE DELAY  CONSTRAINTS  B.E. Collins and R.L. Cruz	
FAIR ALLOCATION OF UTILITIES IN MULTIRATE MULTICAST NETWORKS	
ON THE USE OF MULTIPLE WORKING POINTS IN MULTICHANNEL ALOHA WITH DEADLINES	

SPECIFICATION AND ANALYSIS OF A RELIABLE BROADCASTING PROTOCOL  IN MAUDE	738
G. Denker, J.J. Garcia-Luna-Aceves, J. Meseguer, P.C. Ölveczky, J. Raju, B. Smith, and C.L. Talcott	
MODELING AND ANALYSIS OF ACTIVE MESSAGES IN VOLATILE NETWORKS	748
IMPLEMENTATION OF AN ACTIVE CONGESTION CONTROL SCHEME IN NARROWBAND ATM NETWORKS	758
CPU SCHEDULING FOR ACTIVE PROCESSING USING FEEDBACK DEFICIT ROUND ROBINT. Wolf and D. Decasper	768
HI-F: WIRELESS COMMUNICATION I: DETECTION AND ESTIMATION  Organizers: V.V. Veeravalli and U. Madhow  (Cornell University and University of Illinois at Urbana-Champaign)  Chair: V.V. Veeravalli  (Cornell University)	
PRECODING FOR SCATTERING FUNCTION ESTIMATION OF MOBILE CHANNELS USING OUTPUT CORRELATIONS ONLY	770
TWO-STAGE HYBRID ACQUISITION OF MULTICARRIER DIRECT-SEQUENCE SPREAD-SPECTRUM SIGNALSF.J. Block and C.W. Baum	780
TRAINING SEQUENCE-BASED MULTIUSER CHANNEL ESTIMATION FOR BLOCK-SYNCHRONOUS CDMA	790
SUPPRESSION OF HIGH-DENSITY, DYNAMIC NARROWBAND INTERFERENCE IN DS/CDMA SPREAD-SPECTRUM SYSTEM	
LARGE SYSTEM PERFORMANCE OF REDUCED-RANK LINEAR FILTERS	810
NONLINEAR MULTIUSER RECEIVERS WITH DISTRIBUTED POWER CONTROL IN CELLULAR RADIO NETWORKS	820

IV-A: WIRELESS COMMUNICATIONS II: SYSTEM CONSIDERATIONS IN PHYSICAL LAYER DESIGN Organizers: V.V. Veeravalli and U. Madhow (Cornell University and University of Illinois at Urbana-Champaign) Chair: U. Madhow (University of Illinois at Urbana-Champaign)
THE CODING-SPREADING TRADEOFF IN CDMA SYSTEMS
SPECTRAL EFFICIENCY OF RANDOMLY SPREAD DS-CDMA IN A MULTI-CELL MODEL
CDMA DESIGN THROUGH ASYMPTOTIC ANALYSIS: FADING CHANNELS
PACKING SPHERES IN THE GRASSMANN MANIFOLD: A GEOMETRIC APPROACH TO THE NON-COHERENT MULTI-ANTENNA CHANNEL
BLIND ADAPTIVE MULTIUSER DETECTION FOR DS/SSMA COMMUNICATIONS WITH GENERALIZED RANDOM SPREADING IN A FREQUENCY-SELECTIVE FADING CHANNEL
TRAFFIC AIDED MULTIUSER DETECTION FOR PACKET SWITCHING RANDOM ACCESS/CDMA NETWORKS
IV-B: CODING THEORY IV Chair: R.E. Blahut (University of Illinois at Urbana-Champaign)
OPTICAL CHANNELS WITH DEAD TIME
AWGN CODING THEOREMS FOR SERIAL TURBO CODES
LINEAR CODES OVER Z/(2 <sup>k</sup> ) OF CONSTANT EUCLIDEAN WEIGHT
SPACE-TIME TURBO CODES
TURBO DECODING OF CONCATENATED SPACE-TIME CODES
SOFT OUTPUT AND ITERATIVE STACK DECODING
ALGEBRAIC GEOMETRIC CODES AND AN IMPROVEMENTS ON THE GILBERT-VARSHAMOV BOUND

IV-C: STOCHASTIC SYSTEMS AND CONTROL Chair: G. Dullerud (University of Illinois at Urbana-Champaign)	
SINGLE-SAMPLE-PATH-BASED OPTIMIZATION OF MARKOV DECISION PROCESSZ. Ren and B.H. Krogh	905
TRACKING CAPABILITY ANALYSIS OF THE LMS ALGORITHM FOR FIR SYSTEMS WITH AR COEFFICIENTSY. Wei, S.B. Gelfand, and J.V. Krogmeier	915
ADAPTIVE OPTIMAL PREDICTION FOR MIMO STOCHASTIC SYSTEMS USING CANONICAL FORMS B. Shahrrava and J.D. Aplevich	925
SDRE ESTIMATOR PERFORMANCE IN A HARMONIC DISTORTION PROBLEM E.E. Yaz, Y. Gao, and K.J. Olejniczak	935
STOCHASTIC DIFFERENCE EQUATIONS WITH TIME DELAYS	937
CONTROL UNDER COMMUNICATION CONSTRAINTS	940
IV-D: SPACE-TIME PROCESSING I  Organizer/Chair: A. Nehorai  (University of Illinois at Chicago)	
SPACE-TIME FADING CHANNEL ESTIMATION IN UNKNOWN SPATIALLY CORRELATED NOISE A. Dogandžić and A. Nehorai	948
BLAST TRAINING: ESTIMATING CHANNEL CHARACTERISTICS FOR HIGH CAPACITY SPACE-TIME WIRELESS	958
ANALYSIS OF THE PARALLEL INTERFERENCE CANCELER FOR DS/CDMA SIGNALS	967
BEARING ESTIMATION IN A RICEAN CHANNEL	977
OPTIMAL DOWNLINK BEAMFORMING USING SEMIDEFINITE OPTIMIZATION	987
AN OVERVIEW OF A SIMULATION ENVIRONMENT TO STUDY THE IMPACT OF NON-IDEAL HARDWARE ON ARRAY PROCESSING	997
SIGNAL REPRESENTATIONS FOR TRANSMIT-RECEIVE ANTENNA ARRAYS	1006
BLOCK SPACE-TIME ANTENNA PRECODING/DECODING FOR GENERALIZED MULTICARRIER COMMUNICATIONS IN UNKNOWN MULTIPATHZ. Liu, A. Scaglione, S. Barbarossa, and G.B. Giannakis	1016

FOR BROADBAND WIR	I-USER FREQUENCY-DOMAIN CHANNEL ESTIMATION ELESS COMMUNICATION SYSTEMS102	26
T.A. Thomas, F.W.	7. Vook, and K.L. Baum	
IV-E: MANUFACTURIN Organizer/Chair:	S. Reveliotis	
<del></del>	(Georgia Institute of Technology)	
SYSTEMS	ROCESS MODELING FOR CONTROL SWITCHING OF DISCRETE EVENT	6
H. Darabi and M.A		_
SUPERVISORY CONTRO X. Guan and L.E. I	L OF CONTRADICTIONS IN HIERARCHICAL TASK CONTROLLERS 104 Holloway	2
IV-F: STOCHASTIC NET	TWORKS IV	
Organizers:	S.P. Meyn and R. Srikani (University of Illinois at Urbana-Champaign)	
Chair:	R. Srikant (University of Illinois at Urbana-Champaign)	
MULTIUSER RECEIVERS D.N.C. Tse	, RANDOM MATRICES AND FREE PROBABILITY1055	5
R. Vijayakumar and		
P. Marbach	SES IN A DIFFERENTIATED SERVICES NETWORK	
COMPARING TANDEM Q E. Altman, G. Kool	UEUEING SYSTEMS AND THEIR FLUID LIMITS	
WAITING TIME ASYMPT	OTICS FOR TIME VARYING MULTISERVER QUEUES ND RETRIALS	
WITH ABANDONMENT A A. Mandelbaum, W	A. Massey, M.I. Reiman, and A.L. Stolyar	
M. Mandjes and J.H.		
OVERFLOW AND LOSSES B. Tsybakov and N.	IN A NETWORK QUEUE WITH SELF-SIMILAR INPUT1113  D. Georganas	
V-A: STOCHASTIC NETV	VORKS V	
Organizers:	S.P. Meyn and K. Sirkant (University of Illinois at Urbana-Champaign)	
Chair:	S.P. Meyn (University of Illinois at Urbana-Champaign)	
CHOKE A STATELESS ME	CHANISM FOR PROVIDING QUALITY OF SERVICE	
IN THE INTERNET		

	M PARALLEL QUEUES WITH NO BUFFERSai, B. Gaujal, and A. Hordijk	1132
THE EFFECT OF SCALE ( M. Siler and J. Wal	ON INTERNET QUALITYrand	1142
	NE INPUT-BUFFERED SWITCHES WITH MARKOV-MODULATED  J. Walrand	1152
Organizers:	UNICATIONS III: NETWORKING ISSUES  V.V. Veeravalli and U. Madhow (Cornell University and University of Illinois at Urbana-Champaign)  V.V. Veeravalli (University of Illinois at Urbana-Champaign)	
CHANNELS	ON FOR SPREAD-SPECTRUM COMMUNICATIONS OVER MULTIPATH	1162
M.B. Pursley and C	C.S. Wilkins	
ADAPTIVE REDUNDANC T. Ji and W.E. Star	Y RETRANSMISSION PROTOCOLS FOR WIRELESS NETWORKSk	1171
RESOURCE POOLING AN S.V. Hanly and D.J	ND EFFECTIVE BANDWIDTHS FOR CDMA ANTENNA ARRAYS N.C. Tse	1181
ROUTING FOR MAXIMU JH. Chang and L.	M SYSTEM LIFETIME IN WIRELESS AD-HOC NETWORKS Tassiulas	1191
A SELF ORGANIZING W K. Sohrabi, J. Gao	RELESS SENSOR NETWORK	1201
V-C: MULTIUSER DETE Chair:	CCTION  M.K. Varanasi  (University of Colorado at Boulder)	
BLIND ADAPTIVE NONC D. Das and M.K. V	COHERENT MULTIUSER DETECTION FOR NONLINEAR MODULATION /aranasi	1211
FOR OVERSATURATED	N-COHERENT NEAR-OPTIMAL MULTIUSER DETECTION MA COMMUNICATION	1221
CELLULAR DS-CDMA	DECISION FEEDBACK FOR ASYNCHRONOUS  oodward, and M.L. Honig	1236
MULTIUSER EQUALIZA WITH AND WITHOUT D R.R. Müller	TION FOR RANDOM SPREADING: LIMITS OF DECORRELATION ECISION-FEEDBACK	1246

V-D: SPACE-TIME PROCESSING II Organizer/Chair: A. Nehorai (University of Illinois at Chicago)
SCHEDULING OF SWITCHED MULTIBEAM ANTENNAS IN A MULTIPLE ACCESS ENVIRONMENT 1256 A. Logothetis and H.V. Poor
MULTIPLE ANTENNA DIFFERENTIAL MODULATION
SPACE-TIME ZERO FORCING EQUALIZATION FOR 3G CDMA FORWARD LINK TO RESTORE ORTHOGONALITY OF CHANNEL CODES
A NOVEL SPACE-TIME SPREADING SCHEME FOR WIRELESS CDMA SYSTEMS
V-E: CODING FOR MAGNETIC CHANNELS Organizer/Chairs: E. Kurtas (Quantrum Corporation)
2D EQUALIZATION FOR PAGE-ORIENTED DATA STORAGE SYSTEMS
TOWARDS SOFT OUTPUT APP DECODING FOR NONSYSTEMATIC NONLINEAR BLOCK CODES 1304 K.D. Anim-Appiah and S.W. McLaughlin
LOW DENSITY PARITY CHECK CODES FOR MAGNETIC RECORDING
DESIGN CONSIDERATIONS FOR CONCATENATING CONVOLUTIONAL CODES WITH PARTIAL RESPONSE CHANNELS
TURBO CODES FOR TWO-TRACK MAGNETIC RECORDING SYSTEMS
LIST OF AUTHORS

### Irregular Turbocodes

Brendan J. Frey

Computer Science, University of Waterloo Electrical and Computer Engineering, University of Illinois at Urbana http://www.cs.uwaterloo.ca/~frey

David J. C. MacKay
Department of Physics, Cavendish Laboratories
Cambridge University
http://wol.ra.phy.cam.ac.uk/mackay

#### Abstract

Recently, several groups have increased the coding gain of iteratively decoded Gallager codes (low density parity check codes) by varying the number of parity check equations in which each codeword bit participates. In regular turbocodes, each "systematic bit" participates in exactly 2 trellis sections. We construct irregular turbocodes with systematic bits that participate in varying numbers of trellis sections. These codes can be decoded by the iterative application of the sum-product algorithm (a low-complexity, more general form of the turbodecoding algorithm). By making the original rate 1/2 turbocode of Berrou et al. slightly irregular, we obtain a coding gain of 0.15 dB at a block length of N=131,072, bringing the irregular turbocode within 0.3 dB of capacity. Just like regular turbocodes, irregular turbocodes are linear-time encodable.

#### 1 Introduction

Recent work on irregular Gallager codes (low density parity check codes) has shown that by making the codeword bits participate in varying numbers of parity check equations, significant coding gains can be achieved [1–3]. Although Gallager codes have been shown to perform better than turbocodes at BERs below  $10^{-5}$  [4]<sup>1</sup>, until recently Gallager codes performed over 0.5 dB worse than turbocodes for BERs greater than  $10^{-5}$ . However, in [3], Richardson *et al.* found irregular Gallager codes that perform 0.16 dB *better* than the original turbocode at BERs greater than  $10^{-5}$  [5] for a block length of  $N \approx 131,072$ .

<sup>&</sup>lt;sup>1</sup>Gallager codes to not exhibit decoding errors, only decoding failures, at long block lengths with N > 5,000.

In this paper, we show that by tweaking a turbocode so that it is irregular, we obtain a coding gain of 0.15 dB for a block length of N = 131,072. For example, an N = 131,072 irregular turbocode achieves  $E_b/N_0 = 0.48$  dB at BER =  $10^{-4}$ , a performance similar to the best irregular Gallager code published to date [3]. By further optimizing the degree profile, the permuter and the trellis polynomials, we expect to find even better irregular turbocodes. Like their regular cousins, irregular turbocodes exhibit a BER flattening due to low-weight codewords.

#### 2 Irregular turbocodes

In Fig. 1, we show how to view a turbocode so that it can be made irregular. The first picture shows the set of systematic bits (middle row of discs) being fed directly into one convolutional code (the chain at the top) and being permuted before being fed into another convolutional code (the chain at the bottom). For a rate 1/2 turbocode, each constituent convolutional code should be rate 2/3 (which may, for example, be obtained by puncturing a lower-rate convolutional code).

Since the order of the systematic bits is irrelevant, we may also introduce a permuter before the upper convolutional code, as shown in the second picture. In the third picture, we have simply drawn the two permuters and convolutional codes side by side.

For long turbocodes, the values of the initial state and the final state of the convolutional chains do not significantly influence performance (e.g., see [6]). So, as shown in the fourth picture, we can view a turbocode as a code that copies the systematic bits, permutes both sets of these bits, and then feeds them into a convolutional code. We refer to this turbocode as "regular", since each systematic bit is copied exactly once.

The final picture illustrates one way the above turbocode can be made irregular. Some of the systematic bits are "tied" together, in effect causing some systematic bits to be replicated more than once. Notice that too keep the rate of the overall code fixed at 1/2, some extra parity bits must be punctured.

More generally, an irregular turbocode has the form shown in Fig. 2, which is a type of "trellis-constrained code" as described in [7]. We specify a degree profile,  $f_d \in [0,1], d \in \{1,2,\ldots,D\}$ .  $f_d$  is the fraction of codeword bits that have degree d and d is the maximum degree. Each codeword bit with degree d is repeated d times before being fed into the permuter. Several classes of permuter lead to linear-time encodable codes. In particular, if the bits in the convolutional code are partitioned into "systematic bits" and "parity bits", then by connecting each parity bit to a degree 1 codeword bit, we can encode in linear time.

The average codeword bit degree is

$$\bar{d} = \sum_{d=1}^{D} d \cdot f_d \tag{1}$$

The overall rate R of an irregular turbocode is related to the rate R' of the convolutional code and the average degree  $\bar{d}$  by

$$\bar{d}(1-R') = 1-R.$$
 (2)

So, if the average degree is increased, the rate of the convolutional code must also be increased to keep the overall rate constant. This can be done by puncturing the convolutional code or by designing a new, higher rate convolutional code.

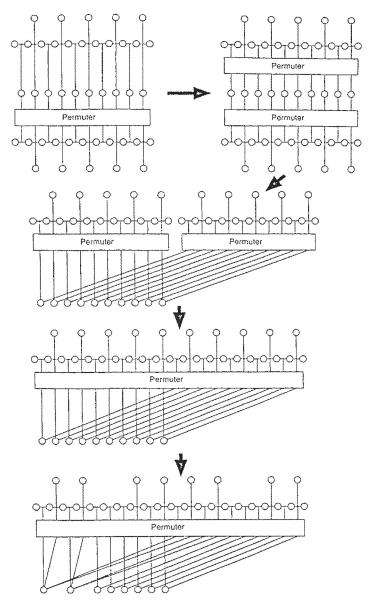


Figure 1: The first 4 pictures show that a turbocode can be viewed as a code that copies the systematic bits, permutes both sets of these bits and then feeds them into a convolutional code. The 5th picture shows how a turbocode can be made irregular by "tying" some of the systematic bits together, i.e., by having some systematic bits replicated more than once. Too keep the rate fixed, some extra parity bits must be punctured. Too keep the block length fixed, we must start with a longer turbocode.

## 3 Decoding irregular turbocodes

Fig. 2 can be interpreted as the graphical model [6,8-10] for the irregular turbocode. Decoding consists of the iterative application of the sum-product algorithm (a low-complexity, more general form of turbodecoding) in this graph.

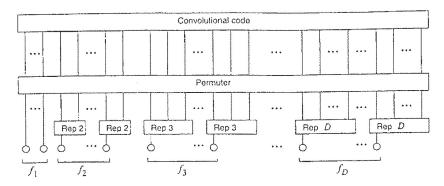


Figure 2: A general irregular turbocode. For d = 1, ..., D, fraction  $f_d$  of the codeword bits are repeated d times, permuted and connected to a convolutional code.

After receiving the channel output, the decoder computes the channel output  $\log$ -likelihood ratios for the N codeword bits,

$$L_1^0, L_2^0, \dots, L_N^0,$$
 (3)

and then repeats each log-likelihood ratio appropriately. If codeword bit i has degree d, we set

$$L_{i,1} \leftarrow L_i^0, \ L_{i,2} \leftarrow L_i^0, \ \dots, \ L_{i,d} \leftarrow L_i^0.$$
 (4)

Next, the log-likelihood ratios are permuted and fed into the BCJR algorithm [11] for the convolutional code. The BCJR algorithm assumes the inputs are a priori log-probability ratios and uses the forward-backward algorithm [12] to compute a set of a posteriori log-probability ratios. If codeword bit i has degree d, the algorithm produces d a posteriori log-probability ratios,

$$L'_{i,1}, L'_{i,2}, \dots, L'_{i,d}.$$
 (5)

For a regular turbocode, there are just two *a posteriori* log-probability ratios,  $L'_{i,1}$  and  $L'_{i,2}$ , for each degree 2 bit and they correspond to the "extrinsic information" produced by each constituent convolutional code.

The current estimate of the log-probability ratio for bit i given the channel output is

$$\hat{L}_i \leftarrow L_i^0 + \sum_{k=1}^d (L'_{i,k} - L_{i,k}). \tag{6}$$

To compute the inputs to the BCJR algorithm needed for the next iteration, we subtract off the corresponding outputs from the BCJR algorithm produced by the previous iteration:

$$L_{i,k} \leftarrow \hat{L}_i - L'_{i,k}. \tag{7}$$

So, each iteration consists of computing the inputs to the BCJR algorithm, permuting the inputs, applying the BCJR algorithm, permuting the outputs of the BCJR algorithm, and taking the repetitions into account to combine the outputs to form estimates of the log-probability ratios of the codeword bits given the channel output.

In our simulations, after each iteration, we check to see if the current decision gives a codeword. If it does, the iterations terminate and otherwise, the decoder iterates further until some maximum number of iterations is reached and a decoding failure is declared.

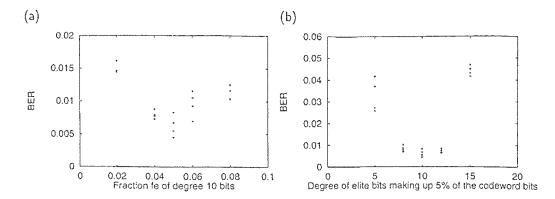


Figure 3: (a) shows the effect of changing the fraction of elite bits on the BER, while keeping the degree of the elite bits fixed at 10. (b) shows the effect of changing the degree of the elite bits on the BER, while keeping the fraction of elite bits fixed at 0.05. For each fraction and degree, the performance of 4 randomly drawn permuters is shown.

### 4 Selecting the profile

Finding a good profile is not trivial, since the best profile will depend on the parameters of the convolutional code, the permuter and the distortion measure (bit error rate, block error rate, decoding failure rate, high-weight decoding failure rate, etc.)

The results we report in this paper were obtained by making small changes to a block length N=10,000 version of the original rate R=1/2 turbocode proposed by Berrou *et al.*. In this turbocode,  $f_1=f_2=1/2$  (see Fig. 2) and the convolutional code polynomials are 37 and 21 (octal). The taps associated with polynomial 37 are connected to the degree 2 codeword bits, 1/2 of the taps associated with polynomial 21 are connected to the degree 1 bits, and the remaining 1/2 of the taps associated with polynomial 21 are punctured, giving the required convolutional code rate of R'=2/3.

To simplify our search, we considered profiles where besides degrees 1 and 2, only one other degree, e for "elite", had a nonzero fraction. So, for a code with overall rate R and fraction  $f_e$  of degree e elite bits, we have

$$f_1 = 1 - R = 1/2,$$
  
 $f_2 = 1 - f_1 - f_e = 1/2 - f_e.$  (8)

In this restricted class of codes, irregularity is governed by two parameters, e and  $f_e$ .

From (2) it is clear that when the average degree is increased, the rate of the convolutional code must also be increased to keep the overall rate at 1/2. We increased the rate of the punctured convolutional code by further puncturing the taps associated with polynomial 21 to obtain a convolutional code with rate

$$R' = 1 - \frac{1 - R}{\bar{d}} = 1 - \frac{1/2}{1/2 + 2(1/2 - f_e) + ef_e}.$$
 (9)

So, in the codes we explored, the level of puncturing was quite high and some extra low-weight codewords were introduced.

To begin with, we made an irregular turbocode with e = 10 (chosen using intuition) and varied  $f_e$  from 0.02 to 0.08 while measuring the BER at  $E_b/N_0 = 0.6$  dB. In each

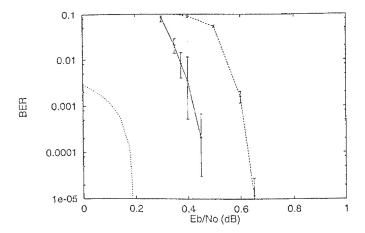


Figure 4: Performance of the original block length N=131,072 turbocode (dashed line) and one of its irregular cousins (solid line). These results are for irregular turbocodes obtained by tweaking the original turbocode – we are currently searching for optimal degree profiles, permuters and trellis polynomials.

experiment, we simulated enough blocks to obtain a relatively small confidence interval. The results are shown in Fig. 3a, which indicates that for degree 10 elite bits, the best fraction is roughly 0.05. Next, we kept the fraction of elite bits fixed at  $f_e = 0.05$  and we varied the degree of the elite bits. The results are shown in Fig. 3b, which indicates that for a fraction of 0.05, the best degree is roughly 10.

These results show that for e = 10,  $f_e = 0.05$  is a good fraction and that for  $f_e = 0.05$ , e = 10 is a good degree. However, values of e and  $f_e$  that give good profiles are probably correlated, so we are currently extending our search.

#### 5 Results

Fig. 4 shows the simulated BER- $E_b/N_0$  curves for the original block length N=131,072 regular turbocode (dashed line) and its irregular cousin (solid line), using profile e=10,  $f_e=0.05$ .

The irregular turbocode clearly performs better than the regular turbocode for BER  $> 10^{-4}$ . At BER =  $10^{-4}$ , the N = 131,072 irregular turbocode is 0.3 dB from capacity, a 0.15 dB improvement over the regular turbocode.

For high  $E_b/N_0$ , most of the errors for the irregular turbocode were due to low-weight codewords. According to preliminary results, the distribution of error weights appears to indicate that the flattening effect for the particular N=131,072 irregular turbocode we constructed occurs at a higher BER than it does for the regular turbocode. However, the flattening effect is highly sensitive to the technique used to construct the permuter (we drew it at random) and the design of the convolutional code (we just further punctured the convolutional code used in the original turbocode). We are currently experimenting with techniques for lowering the level of the flattening effect (e.g., see [13]).

#### 6 Conclusions

We have shown that by making the original, regular turbocode irregular, a coding gain of 0.15 dB is obtained, bringing the irregular turbocode within 0.3 dB of capacity at a BER of 10<sup>-4</sup>. This irregular turbocode performs in the same regime as the best known irregular Gallager code.

We emphasize that we obtained these results by tweaking the regular turbocode originally introduced by Berrou et al. We believe we will be able to improve these performance curves significantly, both by exploring the polynomials used in the convolutional code and by adjusting the degree profile and the permuter structure. (One way to speed up the search is to extend the method of "density evolution" [3] to models with state.) In particular, we are investigating ways to select the permuter and the polynomials to eliminate low-weight codewords, thus reducing the flattening effect [13-15]. We are also studying ways of constraining the degree 1 "parity" bits (i.e., increasing their degree) to eliminate low-weight codewords.

#### References

- [1] M. G. Luby, M. Mitzenmacher, M. A. Shokrollahi, and D. A. Spielman, "Improved low-density parity-check codes using irregular graphs and belief propagation," in *Proceedings of IEEE International Symposium on Information Theory*, 1998.
- [2] D. J. C. MacKay, S. T. Wilson, and M. C. Davey, "Comparison of constructions of irregular Gallager codes," *IEEE Transactions on Communications*, vol. 47, October 1999.
- [3] T. Richardson, A. Shokrollahi, and R. Urbanke, "Design of provably good low density parity check codes." Submitted to *IEEE Transactions on Information Theory*, July 1999.
- [4] D. J. C. MacKay, "Good error-correcting codes based on very sparse matrices," IEEE Transactions on Information Theory, vol. 45, pp. 399-431, March 1999.
- [5] C. Berrou and A. Glavieux, "Near optimum error correcting coding and decoding: Turbo-codes," *IEEE Transactions on Communications*, vol. 44, pp. 1261-1271, October 1996.
- [6] B. J. Frey, Graphical Models for Machine Learning and Digital Communication. Cambridge MA.: MIT Press, 1998. See http://www.cs.utoronto.ca/~frey.
- [7] B. J. Frey and D. J. C. MacKay, "Trellis-constrained codes," in Proceedings of the 35<sup>th</sup> Allerton Conference on Communication, Control and Computing 1997, 1998. Available at http://www.cs.utoronto.ca/~frey.
- [8] N. Wiberg, H.-A. Loeliger, and R. Kötter, "Codes and iterative decoding on general graphs," *European Transactions on Telecommunications*, vol. 6, pp. 513-525, September/October 1995.
- [9] F. R. Kschischang and B. J. Frey, "Iterative decoding of compound codes by probability propagation in graphical models," *IEEE Journal on Selected Areas in Communications*, vol. 16, pp. 219–230, February 1998.

- [10] R. J. McEliece, D. J. C. MacKay, and J. F. Cheng, "Turbo-decoding as an instance of Pearl's 'belief propagation' algorithm," *IEEE Journal on Selected Areas in Com*munications, vol. 16, February 1998.
- [11] L. R. Bahl, J. Cocke, F. Jelinek, and J. Raviv, "Optimal decoding of linear codes for minimizing symbol error rate," *IEEE Transactions on Information Theory*, vol. 20, pp. 284–287, March 1974.
- [12] L. E. Baum and T. Petrie, "Statistical inference for probabilistic functions of finite state markov chains," *Annals of Mathematical Statistics*, vol. 37, pp. 1559–1563, 1966.
- [13] M. Öberg and P. H. Siegel, "Application of distance spectrum analysis to turbocode performance improvement," in Proceedings of the 35<sup>th</sup> Allerton Conference on Communication, Control and Computing 1997, 1998.
- [14] D. Divsalar and F. Pollara, "Turbo-codes for PCS applications," in *Proceedings of the International Conference on Communications*, pp. 54-59, 1995.
- [15] D. Divsalar and R. J. McEliece, "Effective free distance of turbocodes," *Electronics Letters*, vol. 32, pp. 445–446, February 1996.

