providing no error protection. This unique error protection shall result in a reduction of storage requirements or a reduction in transmission bandwidth because the use of a lower level of error protection or no error protection will reduce the introduction of redundant data into the data link or storage medium while still providing error resiliency.

As known to those skilled in the art, a variety of proposed codes can be separated into a prefix and suffix fields as described above. See, for example, E. R. Fiala and D. H. Greene, "Data Compression with Finite Windows," Communications of the ACM, Vol. 32, No. 4, pp. 490-505 (1989). However, the proposed codes have not previously been separated, in order to provide error resiliency as provided by the method and apparatus of the present invention.

It will be apparent to those skilled in the art that split field coding can be applied to data sets which are not characterized by a well-behaved distribution. This application can be accomplished by initially sorting the data set to produce a re-ordered monotonic distribution. This approach will result in error resilience in the sense that a bit error in the suffix field will not result in a loss of code word synchronization. However, the resulting error in the + decoded value will not be constrained to a particular range since the sorting of the data set will destroy the contiguity of the superbins associated with specific prefix field values.

The relative positions of the significant coefficients can also be encoded in a variety of manners, such as run length coding as described above. The resulting run length values can, in turn, also be entropy encoded using an approach such as Huffman coding or the split field coding method described above. Alternatively, the positions of the significant coefficients can be encoded by other methods known to
those skilled in the art, such as tree structures or coefficient maps, without departing from the spirit and scope of the present invention.

Once the plurality of code words representative of the quantized coefficients and the encoded run lengths have been generated, the run length code words and the prefix fields of the quantized coefficient code words are preferably error protected at an appropriately high level of error protection, as shown in block 38. The run length code words are preferably afforded protection because a misdecoded run length value can potentially introduce catastrophic distortion into the reconstructed image. However, the suffix fields of the quantized coefficient code words are preferably error protected at a relatively lower level of error protection, if at all. As shown schematically in Figure 1, the data encoder 16 can therefore include unequal error protection means 29 for providing appropriate levels of error protection to the encoded data as described above.

Regardless of the error protection means, error protection adds redundancy to the encoded data and increases the storage and transmission requirements. Accordingly, by providing a reduced level of error protection or no error protection to the suffix fields of the quantized coefficient code words, the storage and transmission requirements can be reduced by the method and apparatus of the present invention while limiting the effects of bit errors incident upon the suffix fields of the quantized coefficient code words.

Following the data compression process described above, the encoded data can be efficiently stored. For example, the run length code words and the prefix fields of the quantized coefficient code words can be stored in a first data block 66 defined by a storage medium 18, such as a-magnetic disk storage
which is error protected as shown in Figure 6. In addition, the respective suffix fields of the quantized coefficient code words can be stored in a second data block 68 defined by a storage medium which includes a reduced level of error protection or no error protection. Thus, the suffix fields can be more efficiently stored within the second data block.

Likewise, the compressed and encoded data can be efficiently transmitted, such as via first and second data links. In particular the error resilient method and apparatus of the present invention can include a transmitter 20 which transmits the respective run length code words and the prefix fields of the quantized coefficient code words via a first data link 22 which is error protected, and which transmits the respective suffix fields of the quantized coefficient code words via a second data link 24 which is not error protected or is error protected to a lesser degree than the first data link. Thus, the suffix fields can be more efficiently transmitted (with reduced or no redundancy) using the second data link.

Upon reception of the compressed data, the prefix fields of the quantized coefficient code words can be decoded (as shown in Figure 7) and the lengths of the suffix fields can be determined based on the decoded prefix fields. If one or more bit errors are incident upon the suffix field of a quantized coefficient code word, the code word synchronization is not lost because the length of the suffix field is known. As a result, the resulting error in the decoded coefficient value will be constrained to the range of coefficient values for the superbin corresponding to the associated prefix field. Accordingly, the effects of the error on the reconstructed image will be limited and will not be catastrophic. Following the transmission of the encoded data and the possible detection and correction of any storage and
-36-
transmission errors by means of channel decoding known to those skilled in the art, the compressed data, including both the quantized values for the significant coefficients and the relative positions of the
-37-

2. An error resilient method of encoding data according to Claim 1 wherein said step of generating a plurality of code words comprises the step of entropy coding the data to thereby reduce the size
5 of the resulting code words.
3. An error resilient method of encoding data according to Claim 1 wherein said step of generating the second portion of each code word comprises the step of generating second portions having predetermined numbers of characters, and wherein said step of generating the first portion of each code word comprises the step of generating first portions which
include information representative of the predetermined number of characters which comprise the associated second portion.
4. An error resilient method of encoding data according to Claim 3 further comprising the step of determining the probability with which respective ones of the plurality of code words are generated, wherein said step of generating second portions having predetermined numbers of characters comprises the step of generating a plurality of second portions having the same predetermined number of characters, and wherein the plurality of second portions which have the same predetermined number of characters comprise portions of respective code words which have corresponding probabilities of generation within a predetermined range of probabilities.
5. An error resilient method of encoding data according to Claim 1 wherein said step of providing error protection comprises the steps of:
storing the at least one first portion of the plurality of code words in a first data block of a storage medium, wherein the first data block is error protected; and
storing the respective second portion associated with the at least one first portion in a second data block of the storage medium, wherein any error protection provided by the second data block is at a lower level than the error protection provided by the first data block.
6. An error resilient method of encoding data according to Claim 1 wherein said step of providing error protection comprises the steps of:
transmitting the at least one first portion of the plurality of code words via a first data link, wherein the first data link is error protected; and
transmitting the respective second portion associated with the at least one first portion via a second data link, wherein any error protection provided by the second data link is at a lower level than the error protection provided by the first data link.
7. A data encoding apparatus comprising: code word generating means for generating a plurality of code fords representative of respective portions of the dath, wherein each code word comprises a first portion and an associated second portion, and wherein said code word generating means comprises:
first generating means for generating the first portion of each code word, the first portion including information reoresentative of a predetermined characteristic of the asspciated second portion; and second generating means for generating the second portion of each fode word, the second portion including information representative of the respective portion of the dath; and
error protection meahs for providing error protection to at least one of the first portions of the plurality of code words while mafintaining any error protection provided to the respective second portion associated with the at least one first portion at a lower level than the error protection provided to the respective first portion.
8. A data encoding apparatus according to Claim 7 wherein said code word generating means comprises entropy coding means for entropy coding the data to thereby reduce the size of the resulting code words.
-40-
9. A data encoding apparatus according to Claim 7 wherein said second generating means generates second portions having predetermined numbers of characters, and wherein said first generating means generates first portions which include information representative of the predetermined number of characters which comprise the associated second portion.
10. A data encoding apparatus according to Claim 7 wherein said error protection means comprises a storage medium for storing the plurality of code words, said storage medium being partitioned into a first data block which is error protected and a second data block, wherein any error protection provided by the second data block is at a lower level than the error protection provided by the first data block, wherein the at least first portion of the plurality of code words is stored in the first data block of the storage medium, and wherein the respective second portion associated with the at least one first portion is stored in the second data block of the storage medium.
11. A data encoding apparatus according to Claim 7 wherein said error protection means comprises:
first data link transmitting means for transmitting the at least one first portion of the plurality of code words via a first data link, wherein the first data link is error protected; and
second data link transmitting means for transmitting the respective second portion associated with the at least one first portion via a second data link, wherein any error protection provided by said second data link is at a lower level than the error protection provided by said first data link.

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An error resilient method of compressing data comprising the steps of:
tran forming the data based upon a predetermined t fansformation function;
quantizing the transformed data such that the quantized data has fewer unique coefficients than the transformed data; and
encoding the quantized data, said encoding step comprising the steps of:
generkting a plurality of code words, representative of respective portions of the data, which have respective first and second portions, wherein the first portipn includes information representative of a predetermined characteristic of the associated second portion, and wherein the second portion includes information representative of a respective portion of the data; and
providing ertor protection to at least one of the first portions of the plurality of code words while maintaining any efror protection provided to the respective second portipn associated with the at least one first portion at a lower level than the error protection provided to the respective first portion.
13. An error resilient method of compressing data according to Claim 12 wherein said step of encoding the quantized data comprises the step of entropy coding the quantized data to thereby reduce the size of the resulting code words.
14. An error resilient method of compressing data according to Claim 12 wherein said step of generating a plurality of code words comprises the steps of:
generating second portions having predetermined numbers of characters; and
generating first portions which include information representative of the predetermined number of characters which comprise the associated second portion.
15. An error resilient method of compressing data according to Claim 14 further comprising the step of determining the probability of occurrence of respective ones of the quantized data values, wherein said step of generating second portions having predetermined numbers of characters comprises the step of generating a plurality of second portions having the same predetermined number of characters, and wherein the plurality of second portions which have the same predetermined number of characters comprise portions of respective code words which represent quantized data values having corresponding probabilities of generation within a predetermined range of probabilities.
16. An error resilient method of compressing data according to Claim 12 wherein said step of providing error protection comprises the steps of:
storing the at least one first portion of the plurality of code words in a first data block of a storage medium, wherein the first data block is error protected; and
storing the respective second portion associated with the at least one first portion in a second data block of the storage medium, wherein any error protection provided by the second data block is at a lower level than the error protection provided by the first data block.
17. An error resilient method of compressing data according to Claim 12 wherein said step of providing error protection comprises the steps of: number of transformed coefficients which are not detected is at least as great as a predetermined clipping ratio.
22. An error resilient data compression apparatus comprising: of the plurality of code words via a first data link, wherein the first data link is error protected; and
transmitting the respective second portion associated with the at least one first portion via a second data link, wherein any error protection provided by the second data link is at a lower level than the error protection provided by the first data link.
18. An error resilient method of compressing data according to Claim 12 wherein said transforming step comprises the step of transforming the data based upon a wavelet transform.
19. An error resilient method of compressing data according to Claim 18 wherein said transforming step comprises the step of transforming the data based upon a biorthogonal wavelet transform.
20. An error resilient method of compressing data according to Claim 12 wherein the transformed data includes a plurality of transformed coefficients, and wherein said quantizing step comprises the step of detecting transformed coefficients below a predetermined clipping threshold.
21. An error resilient method of compressing data according to Claim 20 further comprising the step of establishing a clipping threshold such that the ratio of the number of detected coefficients to the
transmitting the at least one first portion
23. An error resilient data compression apparatus according to Claim 22 wherein said data encoder comprises entropy coding means for entropy coding the quantized data to thereby reduce the size of the resulting code words.
24. An error resilient data compression apparatus according to Claim 22 wherein said code word generating means comprises:
second generating means for generating second portions having predetermined numbers of characters; and
first generating means for generating first portions which include information representative of

the predetermined number of characters which comprise the associated second portion.
25. An error resilient data compression apparatus according to Claim 22 wherein said error protection means comprises a storage medium for storing the plurality of code words, said storage medium being partitioned into a first error protected data block and a second data block, wherein any error protection provided by said second data block is at a lower level than the error protection provided by said first data block, wherein the at least first portion of the plurality of code words is stored in the first data block of the storage medium, and wherein the respective second portion associated with the at least one first portion is stored in the second data block of the storage medium.
26. An error resilient data compression apparatus according to Claim 22 wherein said error protection means comprises:
first data link transmitting means for transmitting the at least one first portion of the plurality of code words via a first data link, wherein the first data link is error protected; and
second data link transmitting means for transmitting the respective second portion associated with the at least one first portion via a second data link, wherein any error protection provided by the second data link is at a lower level than the error protection provided by the first data link.
27. An error resilient data compression apparatus according to Claim 22 wherein said data transformer comprises a wavelet transformer for transforming the data based upon the wavelet transformer.

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28. A computer readable memory for storing error resilient encoded data, the computer readable memory comprising:
a storage medium for storing the error resilient encoded data, said storage medium being partitioned into a first error protected data block and a second data blo\&k, wherein any error protection provided by said second data block is at a lower level than the error protection provided by said first data. block; and
a plurality of code words, representative of respective portions of the original data, which have respective first and second portions, wherein the first portion includes information representative of a predetermined characteristic of the associated second portion, and wherein the second portion includes information representative of a respective portion of the original data,
wherein at least one of the first portions of the plurality of code words is stored in the first data block of said storage medium such that the at least one first portion is error protected, and wherein the respective second portion associated with the at least one first portion is stored in the second data block of said storage medium such that any error protection provided to the respective second portion associated with the at least one first portion is at a lower level than the error protection provided to the respective first portion.
29. A computer readable memory for storing error resilient encoded data according to Claim 21 wherein the second portion of each code word has a predetermined number of characters, and wherein the first portion of each code word includes information representative of the predetermined number of

## -47-

characters which comprise the associated second portion.
30. A computer readable memory for storing error resilient encoded data according to Claim 29 wherein each of the plurality of code words occurs according to a predetermined probability, wherein a plurality of second portions of code words have the same predetermined number of characters, and wherein. the plurality of second portions which have the same predetermined number of characters comprise portions of respective code words which have corresponding probabilities of occurrence within a predetermined range of probabilities.


ABSTRACT OF THE DISCLOSURE
The error resilient method and apparatus for encoding data includes an encoder including a code word generator for generating a plurality of code words representative of respective portions of the data. The code word generator encodes data pursuant to split field coding in which each code word includes a prefix field and an associated suffix field. The prefix field includes information representative of a predetermined characteristic of the associated suffix field, such as the predetermined number of characters which form the associated suffix field. In addition, the suffix fields include information representative of at least some of the original data. Consequently, if the prefix field of a code word is decoded correctly, i.e, without the occurrence of bit error, the error resilient method and apparatus can correctly determine the length of the associated suffix field and the range of coefficient values to be represented by the associated suffix field such that the associated suffix field is resilient to errors. In order to increase the probability that the prefix field will be correctly decoded, the method and apparatus protects the prefix and suffix fields of the encoded data to greater and lesser degrees, respectively, such that the data can be more efficiently compressed.



FIG. 3.


1 FIG. 4.




FIG. 7.

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FIG. 3.


FIG. 4.


Page 88 of 437

## File History Content Report

The following content is missing from the original file history record obtained from the United States Patent and Trademark Office. No additional information is available.

Document Date - 1996-04-17
Document Title - Drawings

Page(s) - FIG 6


FIG. 7.

## 08/633896

APR
RATENT
1996
Christopher J. Martens
Serial No. To Be Assigned
Filed: Concurrently Herewith
FOr: ERROR RESILIENT METHOD AND
APPARATUS FOR ENTHROPY CODING

April 17, 1996

Assistant Commissioner of Patents and Trademarks Washington, DC 20231

## APPLICATION FILED UNDER 37 CFR 1.41 (c)

Sir:
The above-identified application is being filed on behalf of the inventors, residents of Des Peres, St. Louis County, Missouri; and Creve Coeur, St. Louis County, Missouri, respectively, under the provisions of 37 CFR 1.41 (c). A Declaration and Power of Attorney from the inventors will follow, 37 CFR 1.63.


```
Bell, Seltzer, Park & Gibson
Post Office Drawer 34009
Charlotte, North Carolina 28234
Telephone: (704) 331-6000
Our File No. 8190-43
204780
"Express Mail" mailing label number
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Date of Deposit

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I hereby certify that this paper or fee is being deposited with the United States Postal Service "Express Mail Post office to Addressee" service under 37 CFR 1.10 on the date indicated above and is addressed to the Commissioner of Patents and Trademarks, Washington, DC 20231.

```



An Application Number and Filing Date have been assigned to this application. However, the items indicated below are missing. The required items and fees identified below must be timely submitted ALONG WITH THEF PAYMENT OF: A SURCHARGE for items 1 and \(3-6\) only of \$ \(\mathbf{3} 0\) - for large entities or \(\$\) 6. 5 ~ for small entities who have filed a verified statement claiming such status. The surcharge is set forth in 37 CFR \(1.16(0)\).

If all required items on this form are filed within the perigd set below, the total amount owed by applicant as a Glarge entity, \(\square\) small entity (verified statement filed), is \(\$ .48\).

Applicant is given ONE MONTH FROM THE DATE OF THIS LETTER, OR TWO MONTHS FROM THE FILING DATE of this application; WHICHEVER IS LATER, within which to file all required items and pay any fees required above to avoid abandonment. Extensions of time may be obtained by filing a petition accompanied by the extension fee under the provisions of 37 CFR 1:136(a).
1. The statutory basic filing fee is: \(\square\) missing. \(\square\) insufficient. Applicant as a \(\square\) large entity \(\square\) mall entity, must submit \$ \(\qquad\) to complete the basic filing fee.
2. Additional claim fees of \(\$\) \(\qquad\) as a \(\square\) large entity, \(\square\) small entity, including any required multiple dependent claim fee, are required. Applicant must submit the additional claim feos or cancel the additional claims for which fees are due.
3. Thg oath or declaration:
is missing.
\(\square\) does not cover items omitted at time of execution.
An oath or declaration in compliance with 37 CFR 1.63, identifying the application by the above Application Number and Filing Date is required.
4. The oath or declaration does not identify the application to which it applies. An oath or declaration in compliance with 37 CFR 1.68 , identifying the application by the above Application Number and Filing Date, is required.
5. The signature(s) to the oath or declaration is/are: \(\square\) missing; \(\square\) by a person other than the inveptor or a person qualified under 37 CFR 1.42, 1.43, or 1.47. A properly signed oath or declaration in compliance with 37 CFR 1.63, identifying the application by the above Application Number and Filing Date, is required.
6.

The signature of the following joint inventor(s) is missing from the oath or declaration
An oath or declaration listing the names of all inventors and signed by the omitted inventor(s), identifying this application by the above Application Number and Filing Date, is required.
7. The application was filed in a language other than English. Applicant must file a verified English translation of the application and a:fee of \$ \(\qquad\) under 37 CFR 1.17(k), unless this fee has already been paid.

8, \(\square\) A (37 CFR 1.21(m))Your fling receipt was mailed in error because your check was returned without payment.
10. The application does not comply with the Sequence Rules. See attached Notice to Comply with Sequence Rules 37 CFR 1.821-1.825.


Direct the response and any questions about this notice to, Attention: Application Processing Division, Special Processing and Correspondence Branch (703) 308-1202.

A copy of this notice MUST be returned with the response.


Meany and Martens
Serial No. 08/633,896
Filed: April 17, 1996
For: ERROR RESILIENT METHOD
AND APPARATUS FOR
ENTHROPY CODING
July 3, 1996
Assistant Commissioner
of Patents and Trademarks
Washington, DC 20231

\section*{SUBMITTAL OF DECLARATION \\ UNDER 37 CFR 1.63}
sir:
Enclosed is a Declaration and Power of Attorney for the above-identified application which has been executed by the named inventors.

A check in the amount of \(\$ 130\) is also enclosed to cover the surcharge under \(36 \mathrm{CFR} 1.16(\mathrm{e})\). Any additional fee or credit may be charged to our deposit account No. 16-0605.


Registration No. 34,610
```

Bell, Seltzer, Park \& Gibson
Post Office Drawer 34009
Charlotte, North Carolina }2823
Telephone: (704) 331-6000
Our File No. 8190-43
Order No. 14879

```

232684
I hereby certify that this correspondence is being deposited with the United States Postal Service by first class mail in an envelope addressed to: Assistant Commissioner of Patents and Trademarks, Washington, D.C. 20231, on

July 3, 1996 by: fuuss fícoplenoffere signed: July 3, 1996

\section*{DECLARATION AND POWER OF 'ATTORNEY FOR PATENT APPLICATION}

\section*{Attorney Docket No: 8190-43}

As a below named inventor, I hereby declare that:
My residence, post office address and citizenship are as stated below next to my name,

I believe I am the original, first and sole inventor (if only one name is listed below) or an original, first and joint inventor (if plural names are listed below) of the subject matter which is claimed and for which a patent is sought on the invention entitled ERROR RESILIENT METHOD AND APPARATUS FOR ENTROPY CODING, the specification of which
[ ] is attached hereto.
[ ] was filed on April 17, 1996 as Application Serial No. 08/633,896
and was amended on \(\qquad\)
(if applicable)
I hereby state that I have reviewed and understand the contents of the above-identified specification, including the claims, as amended by any amendment referred to above.

I acknowledge the duty to disclose information which is material to the examination of this application in accordance with Title 37, Code of Federal Regulations, Section 1.56 (a).

I hereby claim foreign priority benefits under Title 35, United States Code, Section 119 of any foreign application(s) for patent or inventor's certificate listed below and have also identified below any foreign application for patent or inventor's certificate having a filing date before that of the application on which priority is claimed:

Prior Foreign Application(s)
Priority Claimed
\(\frac{\text { (None) }}{\text { (Number) }} \overline{\text { (Country) }} \overline{\text { (Day/Month/Year Filed) }}\)
\(\overline{\text { (Number) }} \overline{\text { (Country) }} \overline{\text { (Day/Month/Year Filed) }}\)
\(\overline{\text { (Number) }} \overline{\text { Country) }} \overline{\text { (Day/Month/Year Filed) }}\)
\(\left.\begin{array}{ll}\text { [ }] & {[ }\end{array}\right]\)
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Declaration

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Page 2

I hereby claim the benefit under Title 35, United States Code, § \(119(\mathrm{e})\) of any United States provisional application(s) listed below.
\begin{tabular}{lc}
\(\frac{\text { (None) }}{\text { (Application Number) }}\) & \\
\hline (Application Number) &
\end{tabular}

I hereby claim the benefit under Title 35, United States Code, Section 120 of any United States application(s) listed below and, insofar as the subject matter of each of the claims of this application is not disclosed in the prior United States application in the manner provided by the first paragraph of Title 35, United States Code, Section 112, I acknowledge the duty to disclose material information as defined in Title 37, Code of Federal Regulations, Section \(1.56(a)\) which occurred between the filing date of the prior application and the national or PCT international filing date of this application:
(None)
\(\frac{\text { (Appln. Serial No.) }}{} \frac{\text { (Filing Date) }}{\text { (patented/pending/aban.) }}\)
\(\frac{\text { (Appln. Serial No.) }}{\text { (Filing Date) }} \frac{\text { (Status) }}{\text { (patented/pending/aban.) }}\)

I hereby declare that all statements made herein of my own knowledge are true and that all statements made on information and belief are believed to be true; and further that these statements were made with the knowledge that willful false statements and the like so made are punishable by fine or imprisonment, or both, under Section 1001 of Title 18 of the United States Code and that such willful false statements may jeopardize the validity of the application or any patent issued thereon.

POWER OF ATTORNEY: As a named inventor, I hereby appoint the following attorneys to prosecute this application and transact all business in the Patent and Trademark Office connected therewith.

Timothy H. Courson Registration No. 33,300



An Application Number and Filing Date have been assigned to this application. However, the items indicated below are missing. The required items and fees identified below must be timely submitted ALONG WITH THE PAYMIENT OF A SURCEARGE for items 1 and \(3-6\) only of \$ 3 for large entities or \(\$ 10\) for small entities who have filed a verified statement claiming such status. The surcharge is set forth in 37 CFR 1.16(e).

If all required items on this form are filed within the period set below, the total amount owed by applicant as a large entity, D'small entity (verified statement filed), is \$ \(2 \mathrm{C}_{\mathrm{L}}\).

Applicant is given ONE MONTH FRQM THE DATE OF THIS LETTER, OR TWO MONTHS FROM THE FILING DATE of this application, WHICHEVER IS LATER, within which to file all required items and pay any fees required above to avoid abandonment. Extensions of time may be obtained by filing a petition accompanied by the extension fee under the provisions of 37 CFR 1.136 (a).
1. The statutory basic filing fee is: \(\square\) missing \(\square\) insufficient. Applicant as a \(\square\) large entity \(\square\) mall entity; must submit \$ \(\qquad\) to complete the basic filing fee.
2. Additional claim fees of \$ \(\qquad\) as a \(\square\) large entity, \(\square\) small entity, including any required multiple dependent claim fee, are required. Applicant must submit the additional claim feors or cancel the additional claims for which fees are due.
3. The oath or declaration:

Is missing.
\(\square\) does not cover items omitted at time of execution.
An oath or declaration in compliance with 37 CFR 1.63, identifying the application by the above Application Number and Filing Date is required.
4. The oath or declaration does not identify the application to whioh it applies. An oath or declaration in compliance with 37 CFR 1.63, identifying the application by the above Application Number and Filing Date, is required.
5. \(\square\) The signature(s) to the oath or declaration is/are: \(\square\) missing; \(\square\) by a person other than the inventor or a person qualified under 37 CFR 1.42, 1.43, or 1.47. A properly signed oath or declaration in compliance with 87 CFR 1.63, identifying the application by the above Application Number and Filing Date, is required.
6. The signature of the following joint inventor(8) is missing from the oath or declaration:

An oath or declaration listing the names of all inventors and signed by the omitted inventor(s), identifying this application by the above Application Number and Filing Date, is required.
7. \(\square\) The application was filed in a language other than English. Applicant must file a verified English translation of the application and a fee of \$ \(\qquad\) under 37 CFR 1:17(k), unless this fee has already been paid.
8. A\$
(37 CFR 1.21(m)).
9. Your filing receipt was mailed in error because your check was returned without payment.
10. The application does not comply with the Sequence Rules. See attached Notice to Comply with Sequence Rules 37 CFR 1.821-1.825.

340 UT 07/18/96 08633896
1105 130.00 CK
11, \(\square\) Other.

- .

Direct the response and any questions about this notice to, Attention: Application Processing Division; Special Processing and Correspondence Branch (703) 308-1202.


\section*{INFORMATION DISCLOSURE} STATEMENT UNDER 37 CFR 1.97

Sir:
Attached is a form PTO-1449 listing several documents which may be considered material to the examination of the above-identified application. A copy of each document is also enclosed. It is requested that these documents be considered by the Examiner and officially made of record in accordance with the provisions of 37 CFR 1.97 and Section 609 of the MPEP.


Guy f. Gosnell
Registration No. 34,610

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Post Office Drawer 34009
Charlotte, North Carolina 28234
Telephone: (704) 331-6000
Our File No. 8190-43
232678
I hereby certify that this correspondence is being deposited with the United States Postal Service by first class mail in an envelope addressed to:
Commissioner of Patents and Trademarks, Washington, D.C. 20231, on
July 3, 1996 by: Quex Ftucbleoffer signed: July 3, 1996

*EXAMINER Initial if reference considered, whether or not citation is in conformance with MPEP 609; Draw line through citation if not in conformance and not considered. Include copy of this form with next communication to applicant:



insertion time for a filc of siza m . Since later encodings will use much larger values for \(d\) than 16. it is important to eliminate d from the runnjitg time.
To insort the strings in \(O\) (11) timo. McCrcight added additional suffix polnters to the treco. Each intornal nod \(\dot{C}\), representing the string \(a X\) on the path from the root to the internal node, has a pointer to the node representing \(X\), the string obtained by stripping a single letter from the beginning of \(i \mathrm{X}\). If fastring starting at \(i\) has just been insertod at lovel d wo do npt need to return to the root 10 insort the string at i +1 ; instead, a nearby suffix pointor will load us to the relevant branch of the tree.
Figura 3 shows how suffix links are created and used, On the provious iteration, we have malched the string \(a X Y\), where \(a\) is a single choractor, \(X\) and \(Y\) are strings, and \(b\) is the first urimatchod character after'Y. Figure 3 shows a complicated caso where a now intarnal nodo. \(\alpha\), has been added to the treo, and the suffix link of \(\alpha\) must be computed. We Insert the next string XYb by going up the tree to nodo \(\beta\). representing the string \(a X\), and crossing its suffix link to \(\gamma\), representing \(X\). Once we have crossod the suffix link, we descend again in the tree, first by "rescanning" the string \(Y\), and then by "scanning" from \(\delta\) until the new string is inserted. The first part is called "rescanning" because it covers a portion of the string that was covered by the provious insert, and so it doos not roquire checking the intornal strings on the arcs. (In fact, avolding these checks is essential to tho lincar time functioning of the algo: rithm.) The rescan cither ends at an existing node 8 , or \(\delta\) is created to insort the new string XYb; either way we have the destination for the suffix.link of \(a\). We have restored the invariant that ovory internal node, excopt possibly the one just created; has a suffix link.
For the A1 compressor, with a 4096 -byte fixad window, we need a way to delete and roclaim the storage lor portions of theisuffix tree representing strings further back than 4096 in the filo. Soveral things must be added to the suffix tree data structure. The leaves of the tree are placed in a circular buffer, so that the oldest loaf can bo dontifiod and, reclalmed, and the intornal nodos ari given"son count" fields. When an

figure 2. A Parmicia Tree with a Sulfix Pointor


FIGURE 3. Building a Suffix Tree
internal "son count" falls 70 one, the nodo is deleled and two consecutive arcs are combinod. In Section 3, it is shown that this approach will never leave a "dangling" suffix link pointing to deleled nodes. Unfortu nately, this is not the only problem in mainlatring a valid suffix tree. The modifications that avoided a roturn to the root for each now insortion create havoc for delotions. Since we have not always roturned to the root, we may have consistently enlered a branch of the tree sideways. The pointers flo strings in the 4006 -byte window) in the higher levels of such a branch can become out-of-date. However, traversing the branch and updating the pointors would destroy any advantage gained by using the suffix links.
We can keep valid pointers and avoid oxtensive updating by partially updating according to a potcolating update. Each in:ernal nodo has a single "update" bit. If the update bit is true when twe are updating a node. then we set tho bilt folso and propagato the update recursively to the node's parent. Otherviso. we set the bit true and stop the propagation. In the worst case, a long string of true updates can cause the update to propagate to the rool. However, when amorlized over all new loavos, the cost of updaling is constant, and the offect of updating is to kegp all internal pointors on positions within tho lost 4096 positions of the file. Theso facis will bo shown in Section 3.
Wo can now summarize the operation of the inner oop, using Figure 3 agoin. If we havo jusl created noted r, then wo uso a's parent's suffix link in find \(\gamma\). From \(\gamma\) wo move down in the Ireo, first rescatining, and then scanning. At the ond of tho sean, wo percolate an up. dato from tha leaf, moving toward the root, sulting the position fiadds of uni to the currant pusition, and satting tho updato bits falso. until wo find a muda wilh an updato bit that is alruady falso, wherenpuin wa sot that noda's upelate bit true und stop the percalntiom. Finally: wo ko to the circeular huffer of themves and replaca the oldest leuf with thu nety houlf. If the uldest leaf's purem Thns only ono remuining sim, then it must also he do.

namic programming since the one-pass heuristic is a lot fostor, and we estimstod for soveral typical files that the heuristically comprossed output was only about 1 percent larger than the optimum. Furthormare, we will show in tho romnaindor of this soction that the sizo of tho compressed file is nevor worse than \(5 / 4\) the size of the optimal solution for the spocific A1 encoding. This will require developing some analytic lools, so the non-mathematical rador should feel free to skip to Section 4.
The following dofinltions are useful:
Definition. \(F(i)\) is the longest fensible copy at position i in the file.
Samplo \(F(i)\) 's were given above in oquation 1 . They are dependent on the encoding used. For now. Wh are assuming that they are limited in magnifudo 1010 -and must correspond to copy sources ivithin the last 4096 characters.

Definition. \(B(i)\) is the size of the best tway to compress the remainder of. He fifle, starting at position i.
\(B(\vec{i})\) 's would be computed in the revorse pass of the optimal algorithm outlinod above.
The following Thooroms aro given without proof;
Tиеогем. \(F(i+1)\) 玉 \(F(i)-1\).
Theorem. There cxisis ain optimal solution where copies are longest possible (iic., only copies correspanding to \(F(i)\) 's are used).
Tıeorem. \(B(i)\) is môntome decreasing:
Tiugorem. Any solutiovi can be modified, withour affecting lensth, so that (literal \(x_{1}\) ) followed inmuediately by (literal \(x_{2}\) ) implics that \(x_{1}\) is maximum (int this case 16).
We could continuin to ranson in this voin, but thero is an absitract way of looking at the problem that is both clearer and more genoral. Suppose We have a nondeterministic: finite automaton whore each transition is given a cost. A simpla examplo is shown in Figuro 4. The miachine ncecuiss \((n+b)^{\circ}\), with cosis as shown in parenthases.
The total coss of accerpting i sitring is tha sum of tho


FIGURE 4. A Nondolorministle Automaian with Transition Cosis

Iransition cosls for each character. (While it is not important to our problem, the optimal solution can be computed by forming a tronsition matrix for each let. tor, using the costs sliown in parentheses, and then multiplying the matricos for a givon string. Ireating the coefficients as olements of the closed semiring with op: erations of addilion and minimization.) We con obtain a solution that appraximatos the minimum by deleting transitions in the original machine until it becomes a determinisfic machin.o. This corrésponds to choosing a policy in our original data compression problem. 1 policy for the machino in Figure 4 is shown in Figure 5.
Wo now wish to compare, in the worst case, the difforence between oplimally accepting a siring with the non-deterministic machino, and detorministically accepling the same string with the "policy", machine. This is done by taking a cross product of the two machines. as shown in Figurọ 6.
In Figure 6 there are now Iwo weights on each Iransition; the first is the cost in the non-deterministic graph, and the second is the cost in the policy graph. Asymp. totically, the relationship of the optimal solution to tho policy solution is dominated by the smallest ratio on a cycle in this graph. In the cose of Figure G, there is a cyclo from 1, 1' to 1, 2' and back that has cost In the non-dotorministic graph of \(2+1=3\), and cost In tho policy graph of \(3+3=6\), giving a ratio of \(1 / 2\). That is,


FIGURE 5. A. Deterministic "Policy" Automaton for Figure 4
the policy solvition can lo Iwice as batd as the optimum on the string uluahatubath....
In goneral, wo dan find the cyele with the smallest ratlo mochanically, usimg wall known loc:hniques [8, 27). Thu idha is lo conjecture a rate \(r\) and then rethen tho pairs of weights \((x, y)\) on the arex to singla weights \(x-r y\). Under this reduclion, a syde wilh zare! weight has ratio oxacily \(r\). If a cegte has negative weight, then \(r\) Is too largo. The ration on tho negntive seyda is used us a now conjacluro, und thin promess is iterubal. (Nogativa syctos ara dotuctorl hy rubiving a shorlest path algorthom and chauk fing for tanvargente.) ()nas wo have found tho minimune ralio sevelo, we con eronte a worst




copting the siring non-deterministically and deterministically will converge to the ratio of the cycle. (The path taken in the cross product graph wilt not necessarily bring us to the same cycle, due to the initial path fragment; we will, novortheless, do at least as well.) Conversoly, if wo have a sufficiontly long string with non-deterministic ta dotorministic patio \(r_{r}\), then the string will eventually loop in the cross product graph. If we remnvo loops with ratio groatot than \(r\) wo only improve the ratlo of the string, so wa must oventually find a loop with ralio at loast as small as \(r\).
The above discussion gives us an algorithmic way of analyzing our original data comprossion problem. The possible values of \(F(i)\) are encodod in a 17 charactor Alphabet \(p_{9} \ldots, p_{1}\), ropresenting the lenglh of copy available at each posilion. The comprossion algorithm is described by a non-delorministic machino that accepls sitrings of \(p_{1}\); this machino has cosis oqual to tho langths of tha codewords used by tho algorithm. There aro two paramatorizod statip in this machine: \(l_{z}\) means that there is a literal coslaword undar construction with \(x\) spaces stilt availablo; cy monns that a copy is in progress with y charactors rumaining to copy. Tho idlo stato is \(l_{0}=c_{\mathrm{n}}\). In tha tion-dotorministic, machine, tha possiblo Irausitions afe:
\begin{tabular}{|c|c|}
\hline \(I_{10} \xrightarrow{P(2)} l_{15}\) & slarl a litural \\
\hline \(I_{1} \xrightarrow{\sim \rightarrow 10} I_{1-1}\) & comtinuei a litaral ( \(x \geq 1\) ) \\
\hline \(1, \xrightarrow{n+1} c_{1-1}\) & starl 14 capy \\
\hline \(\rightarrow c_{v}\). & confioun a copy \\
\hline
\end{tabular}
(An usturisk is uset as a wild caral to denola any stute.) Hasul on tha thourums nlmiva wo hove alruatly allmimatul sonn Iransilious fusimullify whul follows, For "xample.


below, eliminates many moro transitions:
\(\mathrm{I}_{0} \xrightarrow{\Gamma_{1}(2)} I_{15}\), start a literal if \(i \leq 1\)
\(\left.i_{x} \xrightarrow{n, 111}\right|_{x-1}\) continuo a literal if \(x \geq 1\) and \(i \leq 2\)
\(i_{x} \xrightarrow{p_{1}(2)} c_{i-1}\) start a copy if \(i \geq 3\) or \(x=0\) and \(i \neq 2\) \(c_{c} \xrightarrow{p(p)} c_{y-1}\) continue a copy

Finally, ws add one moro machino to guarantoo that the strings of \(p_{1}\) are realistic. In this machine, state's means itat the previous charactor twas \(p_{i}\), so. the index of the next charactor'must be at loast \(p_{t-1}\) :
\[
\begin{equation*}
s_{i} \xrightarrow{h_{i}} s_{i} \quad(j \geq i-1) \tag{Pos}
\end{equation*}
\]

The cross product of these three machinos has ap-: proximatoly 17 K statos and was analyzed mechanically to prove a-minimum ratio cycle of \(\mathrm{t} / \mathrm{s}\). Thus the nolicy wo have chosen is nevor off by more than 25 percent. and the worst case is realized on a string that repents a pi poltern ás follows:
\[
\begin{array}{lllllll}
1 & 2 & 3 & 4 & 5 & 6 & 7
\end{array}
\]
\[
\begin{array}{lllllll}
p_{10} & p_{10} & p_{0} & p_{3} & p_{7} & p_{0} & p_{3}
\end{array}
\]
\[
\begin{array}{llllllll}
8 & 9 & 10 & 11 & 12 & 13 & 14 & 15
\end{array}
\]
(6)
(There is nothing spocial about 10: if was chosen to illustrate a long copy and to match the examplo in Appendix A.) The detorministic algorithm takes a copy of length 10 in the first position, and then switchos to nlitoral for positions 11 and 12. Five bytes aro used in each repotition of the patlorn. Tho optimal solution is one position out of phasa. It takes a copy of longth 10 in the socond position, and then finds a copy of length 2 at position 12, for a lotal of four bytes on nach itoration. We have abstractod the problom so that the possiblo copy oparations aro doscribod by a string of \(p i\), and wo havo shown a pathological puttern of \(p\), that rosults in \(8 / 4\) of the optimal ancoding. Thore might still be some doubt that such a stririg oxists, since the condition that our thitd maching (5) guarantees, \(F(i+1) \geq F(i)-1\), is a necessary but not sufficiont condition. Novertheless, tho dolails of an actual pathological string can be found in Appendix \(A\).

\section*{4. \(\Lambda\) SIMPLER DATA STRUCTURE:}

Although the quantliy of cotlo associatod with A1 is not onormous, It is complicatad, and tho data structures arm fairly largo. In this socition, wo prosent simplar metherls for finding the suffix and for propagationg tho wintow position.
- Tho aliornailivo to a parcolation upelato is to upelato tha posilions in all nodus buek to tha roet whanavar a now loaf is lusorlocl, Than no uphlitus are unuded when nodes aro dolotod. Tho upilatr hags tann bu ollinitutul.

Tha altormativo to suffix polnturs is more complecatod. The cose of movemmet in a Irou is not tuiform; moving doopuir ruquitus a hash tublu locohup, which is moro expunsivo than following a peront pulatar. So wo can dotirming tho suffix by starting nt the suffle lomf and followling parant polnturs lanek tuward ther row un-
til the suffix noda is roached. The suffix leaf is known bocatise the string al i matehod the siting at some earlier window position \(j\) : the suffex loaf \(j+1\) is the next. contry in the lenf array. With this change, the suffix pointers can be oftininated.
(Frorn a theorelical perspoctive, thase modifications, which have \(O\) (nd) worst case performance for a filo of size \(n\) and cut-off depth, \(n\), are inforior to the \(O(n)\) porfarmance of the sulfix troe. For \(A 1\), with a cufoff of 10 , these modificalions improve nvoringa porformance, but the \(\Lambda 2\) methad diseussed in the noxt soction has such a teep cut-off that suffix pointers and percolated updates are proferable.

\section*{5. 1 MORE POWERFUL ENCODING} The 4.096 -byte window of \(\Lambda 1\) is roughly optimarf for fixed siza copy and litaral codewords. Longer copios would, on average; bo found in a; larger window, but a fargor disppaceniont fiold would bo requirod to encode tham. To oxploit a latgor window, we must use a variabla-width encorling statistically sensitive to tho fiet that recont window, positions are more likely to bo used by copy codowords than thoso posilions further back. Similarly, it is advantagoous to uso variablo. width encodings for copy ared litoral longths.
Thare are several appronchos wo might use for vari-ablo-longth encoding. Wo could uso fixed or adaptive Huffman coding a arithmotic oncoding, a variablo-longth encoding of the integors, or a managnable set of handdasignoded codowords. We oliminated from considoration adaptiva Huffman and arilimetic coding bocause thoy ate slow. Moropvor, wa fell thoy would provido (at best) a sexondary ndaptive advantago since the "front ond" textual sulstitution is itsolf adapting to the input. Wo exparimentad will a fixod Huffman encoding, a hand. dessignod family of codlowg̣rds, athed a variable-longth encorling of the intogers, so wo will compare thoso options briofly:

Hand-Designed Codegwards, This is a diroct genoralizatiun of \(\Lambda 1\); with sliorl copios that use fowor bits but caninel addras tha full window, and longor coplos that cam ntidress liugur hilocks furthor back in tha window. Wifh in fliw conderworsls, this is fast nnel rolativoly onsy to imploment. Howover, sbme caro must bo taken in tho chanico of coclowords io maximlzo comprosslon.

Variahla-langith Intagurn. Thin simplast mothad wo Itiod usos a unary canlo to spucify fiold width, followod by the fiehd itsolf. Copy longith and displacomont flelds
 ralatons ara Igniorosl. Thare aro mora olaboralo codinge af than lotegure (xitelh an [0|, f(0)|, or [13|), that hava boon usent by [15], und \(|30|\) In thatr Implamantatlons of L.ampal-'/iv tanuproaskian. Thase ancodings havo nico asymplatic propurilus for vary Inrgo Intogors, hut tho unury cada is hest fie our purpowas aliteo, as wo will seo


lago of a simplo hardware implementation. We will return to the unary codo in more delail shortly.

Fixed Huffman. Ideally, a fixed Huffman encorder should be applind to source consisting of the copy length and displacement concatenated togothor (to capture the corrolation of these two fields). However, since wo wish to expand window size to 16384 and maximum copy longth to 2000, the roalitios of gathering slatistics and consltucting an implementation dictate that wo restrict the input of tho fixed Huffman comprossor to a size much smallor than \(2000 \times 16.384\) by grouping logether codos with nearly equal copy lengths and displacoments. To improve speed wo use tables to encodo and decode a byte at a time. Novertheless, the fixed Huffman approach is the most complex and slowest of the three options compared hero.
To docido how much comprossion could bo increased with a Fixed Huffman approach, we oxporimentod with sovoral groupings of noarly equal copy longiths and displacomonts, using a fincer granularity for small values. so that the inpul to the Fixed Huffman compressor had only about 30,000 stalos, and we computed the entropy to give a theoretical bound on the compression. The smallest ontropy wo obtained was only 4 percont more compact than the actual compression nchieved with the unary oncoding doscribed below; and any roal implemenlation would do worse than an entropy bound. Consequently, becnusa tho Fixod Huffman approach did not achiove significantly higher compression, we favor the simpler unary corlo, though this is not an overwholmingly clear choice.
Dofine a (starl, stop, slop) unary codo of tho integors as follows: The \(n\)th codoword has \(n\) ones folloiwed hy a zora followad by a fiold of sizo slart \(+n\), slap. If tho fiold sizo is oqual to stop then tho precoding woro can be omittod. The integers aro laid out soquentially through thoso codowords. For oxample. (3, 2, 9) wouldlook likn:
\begin{tabular}{|c|c|}
\hline Codeword & Range \\
\hline \({ }_{0} \mathbf{1} \times x \times\) & 0-7 \\
\hline \(10 . x \times x \times x\) & 8-39 \\
\hline 110xxxxxxx & 40-187 \\
\hline  & 1 18-67 \\
\hline
\end{tabular}

Appondix B contains a simple proce..dura that goneralas unary codlos.
Tho A2 Ioxiual substjluition mothod oncodes copy longth with a \((2,1,10)\) covdo, londing to it maximum copy longth of 20.44. A conpy longil of zoro signals a litornl, for which litoral longth is thon oncoudod with a \((0,1,5)\) codo, landing lo a maximum litornl lougth of 63 bytos, If copy langth ix non-zare, thon capy displatenmont is ancostad with a \((10,2,1 \cdot 4)\) condu, Thio axast minx mum copy and tloral longihs afo chosen lo asoid Whalod status In tho unary progrossions; a maximum copy Inngils of \(2(1) 44\) is sufficione for tha kinds of dath situdlad In Suedon II. Thu NI pulley for chavishan ha. - Livoun topy and litaral sondowortes is aseut.

this section we will explore the other direction: improving the compression ratio with a slight cost to the running time of the algorithm.
When a string occurs frequently in a filo, all the methods we have"considered so far waste space in their oncoding when they aro oncoding the ropoaling string. they are capable of spocilying the copy displacement to: multiple provious occurrences of the string, yet only one string needs to be copied. By contrast, the data structures we have-used do not waste space. The repeating strings share a common path near the root. If we base the copy codewords directly on the data struclure of the dictionary; we can improve the compression ratio significantly. This brings us closet to the second : style of Ziv and Lempel's textual substitution work [19, 29, 43), whore a dictionary is mafntained by both the compresser and expander. However, since we stlll use a window and an explicit copy length coding, it is natural \(t 0\) viest this as a modification of our carlier compres. sors; in the stylo of Ziv and Lempol's first toxlual substitution work.)
- The C2 method uses the same Patricia tree data structuros as B2 to storo ifts dictionary. Thus it takes two prieces of information to specify a word in the dictionary: a nodo, and a location along the are botween the node and its pareni (sineo Pitricia troe arcs may corrospond to-strings with more than one characler). We will distinguish iwo cases for a copy: if the arc is at a leaf of the trep, then we will use a LeafCopy codeword, while If the arc is intornal to the troe we will use a NodeCupy codoword. Essontlally, those strings appearing two or more times in the window are coded with NoileCopics, avoiding the redundancy of A2 or B2 in theso casos.

The C2 oncoding bogins with a single prefix bit that is 0 for a NodeCopy, 1 for a LeafCppy or Literal.
Por NadeCopy codowords, the profix is followed by a node number in [ \(0:\) i, maxNordeNo], where maxNodeNo is tho largost nodo numbor used since initialization; for most files tested, maxNodeNo is about 50 percent the number of leaves, Following the nodo number, a displacement along the arc from the node to its parent is encoded; for most NodeCopy codowords the Incoming are is of length 1,so no length fiold is roquirad. If a length fiold is roquirod, 0 donotos a match oxacily at the noilo, 1 a displacomont 1 down the arc from tho paront nodo, olc. Raroly is the langth fiold longor than one or two bits bocause tho are longths aro usually shori, so all possiblo displacomonts coñ bo onumoratod with only a fow bits, For both tho nodo numbor and tho Incoming are dlsplacamont, tho trick doscribed in Soction 5 is usod to oliminato wastod statos in tho fiold; that is, If \(u\) values must lon oncodod, than tho smallor valuns uro pacodad with tlogze 1 bits and largor valuos wilh fog \(\mathrm{g}_{2} \mathrm{v}\) ] blts.
I.ea/Copies aro codod with unary progrosslons llko thosn of \(\Lambda 2\) or \(132 . \Lambda(1,1,11)\) prograssion is usod 10 spacify the distanco of inu longosit match down tho leif ure: from lis partiol nide, with 0 donoting a litatal; this
progression loads to a maximum copy length of 4094 bytes. Since another literal never occurs immediatoly after a literal of less than maximum literal length, the LeafCopy are dislance progression is shiftod down by 1 when the proceding codoword was a literal (i.e.. arc displacoment 1 is coded as 0.2 as 1 , elc.). On a cross soction of filos from the data sets discussed later, distance down the loaf are was highly skoived, with about half the are displacements occurring one character down the leaf arc. Because of this probability spike at 1 and thorapid drop off at lorger distances, the average length field is small. Following the length fiold. the window position is coded by gradually phasing in a \((10,2,14)\) unary progrossion exactly like \(B 2\) 's.
Literals aro coded by first coding a LeafCopy arc displacoment of 0 and then using a \((0,1,5)\) unary progrossion for the literal length exactly like B2.

Unlike A2 and B2, the expander for C2 must mainLain a dictionary tree oxactly like the compressor's tree to permit decoding. Notice that this is not as onerous as it might seem. During compression, the algorithm must search the tree downward (root toward leavos) to find the longest match, and this requires a hash table access at each node. By contrast. the expander is told which node was matched, and can recover the longth and window position of the match from the node. No hash tablo is roquired, but the encoding is restricted: a copy codoword must always represent the longest match found in the troo, in particular, the superior heuristic used by B2 to choose between Literal and Copy codewords must be discarded; instead, when the longest match is of length 2 or more, a copy codeword must always be produced. With this restriction, the expander I can roconstruct the tree during decoding simply by hanging each new leal from the node or are indicated by the NodeCopy or LeafCopy codeword, or in the case of literals, by hanging the loaf from the permaneni dopth 1 nodo for each literal character.

\section*{B. EMPIRICAL STUDIES}

In this section, we compare the five compression-methods wo have dovolopod with other one-pass, adaptivg methods. For most other mothods, wo do not have welltuned implomontations and report only compression rosults. For implomentations wo have tuned for efficioncy, spood is also ostimatod (for our 3 MIP . 16 -bit word sizo, 8 megabyto workstations). The oxecution limos usod to dotarmina speed finclude the time to openi road, and writo files on tha local disk (which has a rolntivoly slow, maximum transfer rale of 5 megahits por socond); tho spead is computad by dividing the uncomprossod file sizo by tho uxacution time for a large filo.

Wo tostod fila typos important in our working onvironment. Ench numbor in Tablo I is the sum of the comprassad filo sizos for inl files in tho group tivided by tha stim of tha original fila sizas. Clurrs 1 -i show tho dopondensy of camprassion on files siza fur all of tho


Chart 1. Compression vs. File Size, Daita Sot SC
comprossion methods tested or the sourco code (SC) data set.

Data Sets
SC Source Codo. All 8-bit Ascil source filos from which the boot file for our programming environment is built. Filos includo some English comments, and a donsoly-coded colloction of formalting information at the end of oach file roducos comprossibility. The files thomsolves aro written in the Codar languago. (1185 filos, avorago siza 11 Kbylos, total siza 13.4 Myblos)
TM Tochnical Momoranda. All filas from a diractory whore computer scionce lechnical momoranda and roporis a ro filod, excluding those conifaining tmagos. Theso filos aro 8 -bit Ascll loxt with donsoly-codad formatting information at tho and (liko the source codo). ( 1.34 filos, avarago sizo 22 Kbytos, total alzo 2.9 Mbytos)
NS Nows Servico. Ona filo for onch work day of a week from n major wiro sorvico; thoso filos ara 8-blt Ascil with no furmatilng Information Using loxtual. substitution-methods, thoso do not compross as woll as tho tuehnical momoranda of tho provious study group, avon lhough thay aro much largor and should bo loss Impaciond by slurlup tranalunt; Inspoction suggosis that tha largor vocabulary and oxtonslvo uso of propor numes inght bo rosjonaiblo for this. (s flles, avorago slzu 459 Khytus, total nizo 2,3 Mbyins)

CC Compiled Code. The compiled-code files produced from the SC data set. Each file contains several different fegions: symbol names, pointers to the symbols, statement boundaries and source positions for the debugger, and executable. code. Because each region is small and the regions have different characteristics, these files severely test an adaptivo compressor. (1220 files, average size 13 Kbytes , total size 16.5 Mbytes)

BF Boot File. The boot file for our programming environment, basically a core image and memory map. (I file, size 525 Kbytes)

SF Spline Fonts.. Spline-described character fonts used to generate the bitmaps for character sets at a variety of resolutions, ( 94 files, average size 39 Kbytes , total size 3.6 Mbytes)

RCF Run-coded Fonts. High-resolution characler fonts, where the original bitmaps have been replaced by a run-coded representation. (68 files, average size 47 Kbytes, total size 3.2 Mbytes)
SNI Synthetic Images. All 8 bit /pixel synthetic image files from the directory of an imaging researcher. The 44 files are the red, green, and blue color separations for 12 color images, 2 of which also have an extra file to


Chart 2. Compression ya. File Slie, Data Sel SC


Chart 3. Compression vs, File Size, Data Set SC
encodo background transparency: in addition, there are 6 uther grey scale imagos. ( 44 files, average size 328 Kbytes, total size 14.4 Mbytos)
SCI Scanned Images. The red separations for all 8 bit/pixel scanned-in color imagos from the diroctory of an inaging resoarcher. The low-order one or two bits of each pixel are probably noiso, reducing compressibility. (12 files, avorage size 683 Kbyles, total size 8.2 Mbytos)
BI Binary Images. CCITT standard images used to \(\Phi\) ©ialuato binary facsimilo comprossion mothods. Each fle consisis of a 148 -byto heador followod by a binary scan of 1 page ( 1728 pixols/scan line \(\times 2376\) scan linos/ page). Some imagos havo blocks of zeros moro than 30,000 byios long. Becauso thoso filos aro composed of 1-bit rathor than B -bit itams, the goneral-purpose comprossors do worso than thay othorwiso might. (8 filas, averago sizo 513 Klyylos, (otal sizo 4:1 Mbytos)
Tho spocial-purposo CCITT 1D and 2D comprossion methods roportod in [18] nchlova, rospoctively. 0.112 and 0.064 comprossion ralios on tli2so siandard Imagos whan the oxtranoous ond-of-lino codos requirad by the facsimilo sinndard aro romovod and whon tho oxtra- noous 148 -byto hondor is romovod. Tho spocial-purposo CCITT 21) rosult is algnificanily moro compact than any gonural purposo moihod wo loslod, and only CW and C2 surpassad (ha 11) rosull.

Measurements and Compression Methods
H 0 and H 1 . These are entropy calculations madio on a por file basis according 10 :
\[
\begin{align*}
H_{0}= & -\sum_{i=0}^{n-1} P\left(x=c_{i}\right) \log _{2} P\left(x=c_{i}\right)  \tag{7}\\
H_{1}= & -\sum_{i, i=0}^{n-1} P\left(x=c_{i}\right) P\left(y=c_{i} \mid x=c_{i}\right)  \tag{8}\\
& \cdot \log _{2} P\left(y=c_{i} \mid x=c_{i}\right)
\end{align*}
\]
where \(x\) is a random symbol of the source, \(x y\) is a randomly chosen pait of adjacent source characters; and \(c_{i}\) ranges over all possible symbols. Because of tho small file size, the curves in Charts 1 to 3 drop off to the left. In theory, this small sampling problem can be corrected according to [2], but we have found it difficult to estimate the total character set size in order to apply these corrections. Nevertheless, Chart 1 shows that HO is a good estimator for how ivell a memoryluss (zero-order) compressor can do when file size is a large multiple of 256 bytes, and H 1 bounds the compression for a first-order Markov method. (None of our files were large enough for H 1 to be an accurate estimaṭor.)

KG and V. These adaptive methods maintain a Huffman tree based on the frequency of characters seen so far in a file. The compressor and expander have roughily equal performance. The theory behind the KG approach appears in [11] and [23]. The similar V method, discussed in [37] should get better compression during the startup transient at the expense of being about 18 percent slower. 11 is also possible to bound the performance of Vitter's scheme closely to that of a fixed non-adaptive compressor. Except on the highly compressible C.CITT Images, these methods achieve compression slightly worse than HO , as expected. But because of bit quantization, the compression of the CCITT images is poor-arithmetic coding would compress close to H 0 even on these highly compressible sources.
CW. Based on [6]. this method gathers higher-order statistlcs than KG or \(V\) above (which we ran only on zeroth-order statistics). The mothod that Cloary and Witton describo keeps statistics to some order o and encodos each now character based on the contoxt of the o preceding charactors. (We'vo usod \(o=3\), because any highor ordor exhausts storago on most of our data sols.) If tho now charactor has never bofore appeared in the same contoxt, then an escape mechanism is used to back down to smallor contoxts to oncodo the charticter using thoso stalistics. (Wo'vo used thair escenpe mochanism A with oxclusion of counts from highor-order contexis.) Bocauso of high ovent probabilitios in some
- highor-ordorod contoxis and tho possibility of muiliplo oscapos bofore a charactor is encodod, thu fruetional bit loss of Huffman oncoding is a concorn, so [0] usus aritlimotic oncoding. Wo havo usod the arithmetic mesuler \(\therefore \ln\) [40].

specialized for text, though we were able to run it on some other kinds of data as well. The core of the compressor is a move-to-front heuristic. Within each class, the most recently seen words are kopt on a list (we have used list size 256). If the next input word is already in the word list, then the compressor simply encodes the position of the word in the list and then moves the word to the front of the list. The move-tofront heuristic means that frequently used words will be near the front of the list, so they can be encoded with fewer bits. If the next word in the input stream is not on the sord list, then the new word is added to the front of the list, while another word is removed from the end of the list, and the new word must be compressed character-by-character,

Since the empirical results in [5] do not actually give an encoding for the positions of words in the list or for the characters in new words that are oulput, we have taken the liberty of using the V compressor as a subrou. tine to generate these encodings adaptively. (There are actually four copies of Vitter's algorithm running, one \(t 0\) oncode positions and one to encode characters in each of two partitions.) Using an adaptive Huffman is slow; a fixed encoding would run faster, but we expect that a fixed encoding would slightly reduce compression on larger files while slightly improving compression on small files. We could not run BSTW for all of the dala sets. since the parsing mechanism assumes human-readable text and long "words" appear in the other data sets. When the unreadable input parsed well, as in the case of run-coded fonts, the compression was very good:
A1. This is our basic method described earlier, It has a fast and simple expander ( \(560,000 \mathrm{bits} / \mathrm{sec}\) ) with a small storage requirement ( 10,000 bytes). However, the compressor is much slower and larger ( \(73,000 \mathrm{bits} / \mathrm{sec}\), 145,000 byles using scan-from-leaf and update-to-root). The encoding has a maximum compression to \(1 / \mathrm{n}=12.5\) percent of the original file size because the best it can do is copy 16 characters with a 16 -bit codeword.
Caveat: As we menlloned above, the running times reported include the file system overhead for a relalivaly slow disk. To provide a baseline, we timed a file copy without compression and obtained a rato of 760,000 bits per second. Thus, some of the faster expansion rales we report are severely limited by the disk. For oxample, wo estimato that without disk ovorhead the A1 oxpander would be about Iwice as fast. On the other hand, romoving disk overhoad would hardly affect the comprossion spoed of A1.
A2. This mothod, discussod in Soction 5, onlarges tho window to 16,384 charactors and uses variable-width unary-codod copy and litoral codowords to significantly increaso comprossion. The running timo and storago roquiromonis aro \(410,000 \mathrm{blts} / \mathrm{sec}\) and 21,000 bylos for oxpansion and \(00,000 \mathrm{blis} / \mathrm{soc}\) and 630,000 bytos for comprossion (using suffix pointors and porcolalod updoto).

B1. This method, discussed in Section 6, uses the A1 encoding but triples compression speed by updating the tree only at codeword boundaries and literal characters. The running time and storage requirements are \(470,000 \mathrm{bits} / \mathrm{sec}\) and 45,000 bytes for expansion and \(230,000 \mathrm{bits} / \mathrm{sec}\) and 187,000 bytes for compression.
B2. This method, discussed in Section 6. uses the same encoding as A2 but triples compression speed by updating the tree only at codeword boundaries and literal characters. The compressor and expander run at 170,000 and 380.000 bits \(/ \mathrm{sec}\), respectively, and havo storage requirements of 792,000 and 262,000 bytes.
C2. This method, discussed in Section 7, uses the same data structures as B2 but a more powerful encodIng based directly upon the structure of the dictionary tree. Compression is about the same and expansion about 25 percent slower than B2; the comprassor uses about the same storaga as B2, but the expander uses. more (about 529,000 bytes).

Table I highlights some differerices between textual substitution methods like C2 and statistical methods like CW. (TIme and space performance differences have been discussed earlier.) There are several data sets where these methods differ dramatically. On NS, CW is significanlly better than C2. We believe that this is because NS shows great diversity in vocabulary: a property that is troublesome for textual substitution, since it cannot copy new words easily from elsewhere in the document, but is benign for CW, since new words are likely to follow the existing English statistics. On CC. for example, C2 is significantly better than CW. We belleve that this is because CC contains several radically different parts, e,g. symbol tables, and compiled code. C2 is able to adjust to dramatic shifts within a
file, due to literal codewords and copy addressing that favors nearby context, while CW has no easy way to rapidly diminish the effect of older statistics.
For all of our methods, A2, B2, and C2, window size is a significant consideration because it determines storage requirements and affects compression ratios. Chart 4 shows compression as a function of window size for the NS data set (concatenated into a single file to avoid start-up effects), and for the BF boot file. These two data sets were lypical of the bimodal bohavior we observed in our other data sets: large human-readable files benefit greatly from increasing window size, whilo other test groups show little improvement beyond a window size of 4 K .

\section*{9. CONCLUSIONS}

Wo have doscribed soveral practical mothods for lossless data comprossion and dovoloped data structures to support thom. Thoso mothods aro sirongly atlaplive in tho sonso that thoy adapt not only during startup but also to contoxt changos occurring later. Thoy aro suitabla for most high spood applications becnuso they mako only ond pass over source dala hese only'in con-


Chart 4. Compression vs. Window Size, Data Set NS (bottom) Data Set BF (top)
stant amount of storage, and have constant amortized execution time per character.

Our ompirical studies point to soveral broad generalizations. First, based on the H 0 and H 1 theoretical limits, textual substilution via A2, B2, or C2 surpasses memoryless or first-order Markov methods applied on a character-by-character basis on half the data sets. On the other half, even the CW third-order method can't achieve tha H1 bound. This suggests that, to surpass. textual substitution for general purpose compression, any Markov mothod must be af loast socond-order, and 10 date, all such methods havo poor spaco and time performanco.
Secondly, the methods wa'va devoloped adapt rapidly during startup and at transitions in the middle of files. One reason for rapid adaptation is the use of smaller roprosentations for displacaments to rocent positions in the window. Another reason is tho inclusion of mulif-charactor literal codowords; Togethor the litor als and short displacemonts allow our mothods to porform wall on short files, filos with major intornal shifts of vocabulary or slatistical propertios, and files with bursts of poorly comprossing malorial-all proporlios of a significant number of filos in our onvironmont.
Thirilly, It appoars that tho displacomont-and-longth approath to textual substitition is ospocially offocilvo
on small files. On 11,000-byte program source files, for example, A2 and B2 were over 20 percent more compact than textual substitution methods which did not use a length field (UW, MW1, and MW2). This is not surprising because the particular advantage of the length field in copy codewords is rapid adaptation on small files. However, even on the largest files tested. A2 and B2 usually achieved significantly higher compression. Only on images did other methods compete with them; our most powerful method, C2, achieved higher compression than any other textual substitution method we tested on all data sets. The effect of a length field is to greatly expand dictionary size with little or no increase in storage or processing time; our results sugsest that textual substitution methods that use a lensth field will work better than those which do not.
Fourthly, studies of A2, B2, and C2 using different window sizes showed that, for human-readable input (e.g., English, source code), each doubling of window size Improves the compression ratio by roughly 6 percent (for detalls see Chart 4). Furthermore, the data structures supporting these methods scale well: running time is independent of window size, and memory usage grows linearly with window size. Thus increasing window size is an easy way to improve the compression ratio for large files of human-readable input. For other types of input the window size can be reduced to 4096 without significantly impacting compression
- Going beyond these empirical results, an importan practical consideration is the tradeoff among speed storage, and degree of compression; speed and storage have to be considered for both compression and expansion. Of our own methods, A2 has very fast expansion with a minimal storage requirement: its weakness is slow compression; even though the suffix tree deta structure with amortized update has constant amortized time per character, compression is still seven times slower than expansion. However, in applications which can afford relatively slow compression, A2 is excellent; for example, A2 would be good for mass.distribution of software on floppy disks or for overnight compression of files on a file server. Furthermore, if the parallel matching in the compression side of A2 were supporled with VLSI, the result would be a fast; powerful method requiring minimal storago both compressing and expanding.
- B2 provides naarly three times faster compression than A2 but has somewhat slowor expansion and adap. tation. Thus B2 is well sulted for communication and archlving applications.
A1 and B1 do not compross as well as A2 and B2. respectively, but because of thoir two-codeword, bylealligned encodings they aro belter choices fur applications where simplicity or speod is critical. (For example, ). Gasbarro has dosignod and implomented its oxpansion mothod liko \(\Lambda 1\) to improve the bar *.viduth of a VLSI circult tostor [12].)
C2 achlovos algnificantly highor comprossion than B2, but lis oxpandor is somowhat slower and has i

Rescarch Comtributions
larger storage requiroment. In the comprossion study reported in Soction.8, C2 achioved the highest compres. sion of all mothods tasted on 6 of tho 10 data sets. IVe believe that our implementations and empirical
results demonstrate the value of window-based textual substitution. Together the A, B and C methods offer good options that can be chosen according to resource requirements.

APPENDIX A
A Pathological Example

We now shoiv a string that has the \(F\) pattern of equation (0) of Section 3:
\(\begin{array}{ccccccccccc}1 & 2 & 3 & 4 & 5 & 6 & 7 & & & \\ p_{10} & p_{10} & p_{3} & p_{8} & p_{7} & p_{6} & p_{5} & & & & \\ & & 8 & 0 & 10 & 11 & 12 & 13 & 14 & 15 & \\ & & p_{4} & p_{3} & p_{2} & p_{1} & p_{2} & p_{10} & p_{10} & p_{0} & \ldots\end{array}\)
Heroaftor wo will stop abstracting the string by its copy lengths; capital lettors are sirings, small letters are single characlers, and \(i, j, r, p, b\) are integers. The pathological string follows the pattern:
\[
\begin{equation*}
M_{0} M_{1} \ldots M_{r-1} M_{0} M_{1} \ldots M_{r-1} M_{0} M_{1} \ldots \tag{9}
\end{equation*}
\]
whero the parameter \(r\) is choson large enough so. that one iteration excceds the finito window (this prevonis diroct copying from the boginning of ono \(M_{n}\) to a subsequent \(M_{0}\) ). Within each \(M_{i}\) wa. have groups,
\[
\begin{equation*}
M_{i}=G_{n 1} G_{i 1} G_{i 2} \ldots G_{i n / n-1)} . \tag{10}
\end{equation*}
\]
and each group is:

\(B_{2} s_{1+i+1 p+2} c_{1} s_{i p+3} \ldots B_{p-1} s_{(i+1 p e+r-1} C_{1}\)
\(\square\) respectively even and odd numbered \(s_{1}\), and match
in pairs with their following sis. For oxample. the e \(e_{0}\)
in \(G_{0}=s_{1} B_{1} s_{1} c_{0} s_{2} B_{2} s_{2} \ldots\) will match with \(s_{2}\). The \(G_{o n}=s_{1} B_{1} s_{1} c_{0} s_{2} B_{2} s_{2} \ldots\) will match with \(s_{2}\). The \(\mathrm{e}_{0} \mathrm{~s}_{2}\) match is hidden in a minor block segregated from the odd numbered \(s_{i}\) :


Aremains io create the match of longth 2 at position 12 in equation (6). For this purpose, each of the \(c_{i}\) above are either \(e_{i}\) or \(o_{i}\). They will always' precede \(c_{i}\) respectively even and odd numbered \(s\), and match
\[
\begin{equation*}
r=2, \quad b=8, \quad p=100, n=200 \tag{13}
\end{equation*}
\]

We need to take some care that the heuristic doos not find the optimal solution. It turns out that if we just slart as in equation (9). then the first \(M_{0}\) will not compress well, but the houristic will start the behav. ior we are seoking in \(M_{1}\). Asymptotically wo achiove a worst case ratio of \(1 / \mathrm{s}\) betweon tho optimal algorithm and the policy heuristic.

Wo have iniriduced two moro parameters: \(p\) is the number of minor blocks \(B_{i}\), and \(n\) is the number of \(s\) characlers. All of the s subscripts in the above formula aro computed mod \(n\). Tha groups skow so that, for examplo, the beginning of \(\mathrm{C}_{10}=s_{1} B_{1} s_{n+1} \ldots\) will not match ontirely with tha boginning of \(G_{i x 1}=s_{1} B_{1} s_{1}, \ldots\) It will. howaver, match in two parts: tho profix \(s_{1} B_{1}\) appears in both strings, and tho suffix \(G_{10}=\ldots B_{1} s_{n+1} \ldots\) will match with the suffix of \(C_{w 1}=\ldots, B_{1} s_{n+1}\). If. for example, \(B_{1}\) has 9 charac:oiss, this givos two consocutivo locations whore a copy of size 10 is possiblo. In the pattorn of equation 0 .

\section*{APPENDIX B}

Compuling a Unary-Based Variable Length Entoding of the Integers

In Soction 5 wo dofinad a (statt, stop, stop) unary codo of tha intogars ns a string of \(n\) ones followod by a zoro followad by a fiold of \(j\) bits, whora / Is in tho artitmatic progrossion defined by (start; slop, stop). This can be duffined procisoly by tho following oncotar: .

Encodo Var:
proc (out: cardinal., start, stop, list: cardinal.) ~ UNTIL oul < Powar2[sinarl] DO PutBits[1,1];
out - out - Powor2|stari):
starl - starl + slop;

ENDLOOP
If start < last then Putbits\{out, start +1 ] -0 follawed by ficld of size "start"
eLse IF start > last then error
else PutBits[out, start]; :-save a bit
-

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PutBits: proc[out: card, bits: integer] -
Output the binary encoding of "out" in a field of size "bits."

Notice that the encoder is able to save one bit in the last field size of the arithmetic progression.
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