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Higher-Order Functions for Parsing*

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Abstract

In combinator parsing, the text of parsers resembles BNF notation. We present the basic method, and a number of extensions. We address the special problems presented by white-space, and parsers with separate lexical and syntactic phases. In particular, a combining form for handling the "offside rule" is given. Other extensions to the basic method include an "into" combining form with many useful applications, and a simple means by which combinator parsers can produce more informative error messages.

1 Introduction

Broadly speaking, a parser may be defined as a program which analyses text to determine its logical structure. For example, the parsing phase in a compiler takes a program text, and produces a parse tree which expounds the structure of the program. Many programs can be improved by having their input parsed. The form of input which is acceptable is usually defined by a context-free grammar, using BNF notation. Parsers themselves may be built by hand, but are most often generated automatically using tools like Lex and Yacc from Unix (Aho86).

Although there are many methods of building parsing, one in particular has gained widespread acceptance for use in lazy functional languages. In this method, parsers are modelled directly as functions; larger parsers are built piecewise from smaller parsers using higher order functions. For example, we define higher order functions for sequencing, alternation and repetition. In this way, the text of parsers closely resembles BNF notation. Parsers in this style are quick to build, and simple to understand and modify. In the sequel, we refer to the method as *combinator parsing*, after the higher order functions used to combine parsers.

Combinator parsing is considerably more powerful than the commonly used methods, being able to handle ambiguous grammars, and providing full backtracking if it is needed. In fact, we can do more than just parsing. Semantic actions can be added to parsers, allowing their results to be manipulated in any way we please. For example, in section 2.4 we convert a parser for arithmetic expressions to an evaluator simply by changing the semantic actions. More generally, we could imagine generating some form of abstract machine code as programs are parsed.

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Although the principles are widely known (due in most part to (Wadler85)), little has been written on combinator parsing itself. In this article, we present the basic method, and a number of extensions. The techniques may be used in any lazy functional language with a higher–order/polymorphic style type system. All our programming examples are given in Miranda¹; features and standard functions are explained as they are used. A library of parsing functions taken from this paper is available by electronic mail from the author. Versions exist in both Miranda and Lazy ML.

2 Parsing Using Combinators

We begin by defining a *type* of parsers. A parser may be viewed as a function from a string of symbols to a result value. Since a parser might not consume the entire string, part of this result will be a suffix of the input string. Sometimes a parser may not be able to produce a result at all. For example, it may be expecting a letter, but find a digit. Rather than defining a special type for the success or failure of a parser, we choose to have parsers return a list of pairs as their result, with the empty list [] denoting failure, and a singleton list [(v,xs)] indicating success, with value v and unconsumed input xs. As we shall see in section 2.2, having parsers return a list of results proves very useful. Since we want to specify the type of any parser, regardless of the kind of symbols and results involved, these types are included as extra parameters. In Miranda, type variables are denoted by sequences of stars.

For example, a parser for arithmetic expressions might have type (parser char expr), indicating that it takes a string of characters, and produces an expression tree. Notice that parser is not a new type as such, but an abbreviation (or synonym); it's only purpose is to make types involving parsers easier to understand.

2.1 Primitive parsers

The primitive parsers are the building blocks of combinator parsing. The first of these corresponds to the ε symbol in BNF notation, denoting the empty string. The succeed parser always succeeds, without actually consuming any of the input string. Since the outcome of succeed does not depend upon its input, its result value must be pre-determined, so is included as an extra parameter:

```
succeed :: ** -> parser * **
```

succeed v inp = [(v,inp)]

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This definition relies on partial application to work properly. The order of the arguments means that if succeed is supplied only one argument, the result is a parser (i.e. a function) which always succeeds with this value. For example, (succeed 5)

¹ Miranda is a trademark of Research Software Limited.

is a parser which always returns the value 5. Furthermore, even though succeed plainly has two arguments, its type would suggest it has only one. There is no magic, the second argument is simply hidden inside the type of the result, as would be clear upon expansion of the type according to the parser abbreviation.

While succeed never fails, fail always does, regardless of the input string:

```
fail :: parser * **
```

fail inp = []

The next function allows us to make parsers that recognise single symbols. Rather than enumerating the acceptable symbols, we find it more convenient to provide the set implicitly, via a predicate which determines if an arbitrary symbol is a member. Successful parses return the consumed symbol as their result value.

```
satisfy :: (* -> bool) -> parser * *
satisfy p []
               = fail []
satisfy p (x:xs) = succeed x xs , p x
                = fail xs
                                , otherwise
```

Notice how succeed and fail are used in this example. Although they are not strictly necessary, their presence makes the parser easier to read. Note also that the parser (satisfy p) returns failure if supplied with an empty input string.

Using satisfy we can define a parser for single symbols:

literal :: * -> parser * * literal x = satisfy (=x)

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For example, applying the parser (literal '3') to the string "345" gives the result [('3', "45")]. In the definition of literal, (=x) is a function which tests its argument for equality with x. It is an example of operator sectioning, a useful syntactic convention which allows us to partially apply infix operators.

2.2 Combinators

Now that we have the basic building blocks, we consider how they should be put together to form useful parsers. In BNF notation, larger grammars are built piecewise from smaller ones using | to denote alternation, and juxtaposition to indicate sequencing. So that our parsers resemble BNF notation, we define higher order functions which correspond directly to these operators. Since higher order functions like these combine parsers to form other parsers, they are often referred to as combining forms or combinators. We will use these terms from now on.

The alt combinator corresponds to alternation in BNF. The parser (p1 \$alt p2) recognises anything that either p1 or p2 would. Normally we would interpret either in a sequential (or exclusive) manner, returning the result of the first parser to succeed, and failure if neither does. This approach is taken in (Fairbairn86). $Graham \ Hutton$

In combinator parsing however, we use inclusive *either* — it is acceptable for both parsers to succeed, in which case we return both results. In general then, combinator parsers may return an arbitrary number of results. This explains our decision earlier to have parsers return a list of results.

With parsers returning a list, alt is implemented simply by appending (denoted by ++ in Miranda) the result of applying both parsers to the input string. In keeping with the BNF notation, we use the Miranda notation to convert alt to an infix operator. Just as for sectioning, the infix notation is merely a syntactic convenience: (x f y) is equivalent to (f x y) in all contexts.

```
alt :: parser * ** -> parser * ** -> parser * **
```

(p1 \$alt p2) inp = p1 inp ++ p2 inp

Knowing that the empty-list [] is the identity element for ++, it is easy to verify from this definition that failure is the identity element for alternation: (fail \$alt p) = (p \$alt fail) = p. In practical terms this means that alt has the expected behaviour if only one of the argument parsers succeeds. Similarly, alt inherits associativity from ++: (p \$alt q) \$alt r = p \$alt (q \$alt r). This means we do not not need to worry about bracketing repeated alternation correctly.

Allowing parsers to produce more than one result allows us to handle ambiguous grammars, with all possible parses being produced for an ambiguous string. The feature has proved particularly useful in natural language processing (Frost88). An example ambiguous string from (Frost88) is "Who discovered a moon that orbits Mars or Jupiter ?" Most often however, we are only interested in the single longest parse of a string (i.e. that which consumes the most symbols). For this reason, it is normal in combinator parsing to arrange for the parses to be returned in descending order of length. All that is required is a little care in the ordering of the argument parsers to alt. See for example the many combinator in the next section.

The then combinator corresponds to sequencing in BNF. The parser $(p1 \ p2)$ recognises anything that p1 and p2 would if placed in succession. Since the first parser may succeed with many results, each with an input stream suffix, the second parser must be applied to each of these in turn. In this manner, two results are produced for each successful parse, one from each parser. They are combined (by pairing) to form a single result for the compound parser.

For example, applying the parser (literal 'a' \$then literal 'b') to the input "abcd" gives the result [(('a','b'),"cd")]. The then combinator is an excellent example of *list comprehension* notation, analogous to set comprehension in mathematics (e.g. $\{x^2 \mid x \in \mathbb{N} \land x < 10\}$ defines the first ten squares), except that lists replace sets, and elements are drawn in a determined order. Much of the elegance of the then combinator would be lost if this notation were not available.

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Unlike alternation, sequencing is not associative, due to the tupling of results from the component parsers. In Miranda, all infix operators made using the \$ notation are assumed to associate to the right. Thus, when we write (p \$then q \$then r) it is interpreted as (p \$then (q \$then r)).

2.3 Manipulating values

Part of the result from a parser is a value. The using combinator allows us to manipulate these results, building a parse tree being the most common application. The parser (p \$using f) has the same behaviour as the parser p, except that the function f is applied to each of its result values:

using :: parser * ** -> (** -> ***) -> parser * ***

 $(p \ susing f) \ inp = [(f v, out) | (v, out) <- p \ inp]$

Although using has no counterpart in pure BNF notation, it does have much in common with the $\{\cdots\}$ operator in Yacc (Aho86). In fact, the using combinator does not restrict us to building parse trees. Arbitrary semantic actions can be used. For example, in section 2.4 we convert a parser for arithmetic expressions to an evaluator simply by changing the actions. There is a clear connection here with *attribute grammers*. A recent and relevant article on attribute grammars is (Johnsson87). A combinator parser may be viewed as the implementation in a lazy functional language of an attribute grammar in which every node has one *inherited* attribute (the input string), and two *synthesised* attributes (the result value of the parse and the unconsumed part of the input string.) In the remainder of this section we define some useful new parsers and combinators in terms of our primitives.

In BNF notation, repetition occurs often enough to merit its own abbreviation. When zero or more repetitions of a phrase p are admissible, we simply write p^* . Formally, this notation is defined by the equation $p^* = p \ p^* \mid \varepsilon$. The many combinator corresponds directly to this operator, and is defined in much the same way:

```
many :: parser * ** -> parser * [**]
```

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many p = ((p \$then many p) \$using cons) \$alt (succeed [])

The action cons is the uncurried version of the list constructor ":", and is defined by cons (x,xs) = x:xs. Since combinator parsers return all possible parses according to a grammar, if failure occurs on the *n*th application of (many p), *n* results will be returned, one for each of the 0 to n-1 successful applications. Following convention, the results are returned in descending order of length. For example, applying the parser many (literal 'a') to the string "aaab" gives the list

[("aaa","b"),("aa","ab"),("a","aab"),("","aaab")]

Not surprisingly, the next parser corresponds to the other common iterative form in BNF, defined by $p^+ = p p^*$. The parser (some p) has the same behaviour as (many p), except that it accepts one or more repetitions of p, rather of zero or more:

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