ACOUSTIC ECHO AND NOISE CONTROL –
A LONG LASTING CHALLENGE

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ABSTRACT

Hands–free operation of telephones, incorporating echo cancellation and noise reduction, has been discussed for over a decade. This paper presents an overview of the wide range of algorithms which are applicable to echo cancellers and noise reduction. Practical problems associated with implementation and overall system control are also discussed.

1   INTRODUCTION

When telecommunications started about a century ago users had their two hands busy [1]. They had to hold a microphone close to their mouth and a loudspeaker close to one ear. It did not take long to get one hand free: microphone and loudspeaker were assembled in a handset. However, the aim of hands–free operation has not yet been attained.

In early years of telecommunication the lack of efficient electro acoustic devices and amplifiers justified the inconvenience to the customer. At the same time two problems were solved:

- acoustic echos transmitted back to the remote user were reduced by providing sufficient attenuation,

- operation in a noisy environment was possible by an improved signal to noise ratio.

For non–experts it is still difficult to understand that it takes all the signal processing capabilities available today to achieve at least "some" solution of these easily explained problems of hands–free operation. A large number of papers on the topic under consideration have been published within the last few years including bibliographies [2, 3, 4, 5] and reports on the state of the art [6, 7]. Adaptive algorithms for acoustic echo compensation and noise control gained special attention in [8, 9].

2   BASICS

At the most general level, there are two sources that make the solution of the hands–free problem difficult: first the physical properties of loudspeaker–enclosure–microphone systems (LEMS's) and speech signals and secondly the fulfillment of the regulations of the International Telecommunications Union (ITU). Although the latter may seem arbitrary, it is essential for the equipment to be licensed by telecommunication authorities.

2.1   Physics

Audio communication systems include at least one loudspeaker and one microphone housed within the same enclosure. Consequently, the microphone picks up not only locally generated signals like speech and environmental noise but also the signal radiated by the loudspeaker as well as its echos caused by reflections at the boundaries of the enclosure. Assuming linearity, the audio characteristics of the LEMS may be modeled by an impulse response. The duration of the response depends on the reverberation time of the enclosure. In case of an office room this time is in the order of several hundred milliseconds, in case of a passenger car it is in the order of fifty to one hundred milliseconds. Furthermore, the response of the LEMS is extremely sensitive to any movements within the enclosure. Finally, the system is driven by audio signals, typically a mixture of speech and noise, where speech itself is comprised by periodic and aperiodic components with highly fluctuating magnitudes and pauses. Briefly, from a signal processing point of view the system and the signals involved are extremely unpleasant.

2.2   Regulations

The ITU–T Recommendations [10] put very stringent conditions on hands–free telephone systems. For "ordinary" telephones the echo attenuation has to be at least 45 dB in the case of single talk. In double talk situations this value can be reduced by 15 dB. Beyond that, only a negligible delay may be introduced into the signal path by the hands–free facility.

2.3 Systems for Acoustic Echo and Noise Control

A number of systems have been proposed for acoustic echo and noise control. They all use three units (or a
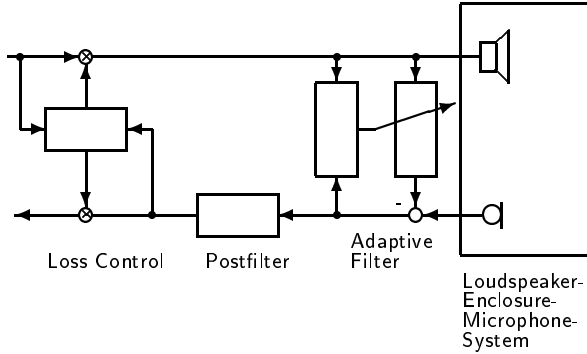

Figure 1: Basic structure for acoustic echo and noise control

subset of them) (Fig. 1): The first unit is a loss control that attenuates the incoming and/or the outgoing signal. Early hands–free communication systems used this unit only reducing conversations to half duplex. Because of the ITU regulations loss control still remains the most important function because it has to guarantee the required attenuation. The second unit consists of an adaptive filter functioning as a replica of the LEMS. If perfect adaptation could be achieved loudspeaker and microphone would be decoupled entirely without any impact on locally generated signals. The third – most modern – "ingredient" of an echo and noise control system consists of a Wiener filter within the outgoing signal path. In contrast to the loss control unit this filter provides a frequency dependent attenuation of the outgoing signal. Its aim is twofold: to suppress residual echos not covered by the adaptive filter and to enhance speech quality by suppressing noise components.

Design considerations and results achieved by these three units will be given within the following sections.

3 ADAPTIVE ALGORITHMS

Several adaptation algorithms have been applied to acoustic echo cancellers. Each of these algorithms minimises the mean square error of signal $e(k)$ (s. Fig. 2). The algorithms discussed in this section are dealt with in order of increasing complexity.

3.1 NLMS

The least mean square (NLMS) algorithm is the most easily and frequently implemented algorithm. It is described by the following relations:

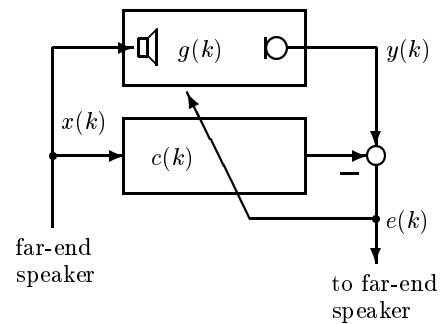$$e(k) = d(k) - \underline{c}^T(k)\,\underline{x}(k), \tag{1}$$

Figure 2: Adaptive System

$$\underline{c}(k+1) = \underline{c}(k) + \alpha\,\frac{e(k)\,\underline{x}(k)}{\|\underline{x}(k)\|^2}, \tag{2}$$

where $e(k)$ denotes the adaptation error, $d(k)$ the desired signal, $\underline{c}(k)$ the coefficient vector of the adaptive filter, $\underline{x}(k)$ the excitation vector and finally α a variable step size factor.

The computational requirements of the NLMS algorithms are low. This is important since the application considered here requires a large number of coefficients. The disadvantage is its slow speed of convergence especially in case of correlated inputs.

3.2 NLMS algorithm with pre–whitening filters

A simple approach to overcome this problem is pre–whitening of both input and reference signal. This can be achieved by a linear prediction error filter. Restricting oneself to a time invariant filter, a filter of order one to four proved to be sufficient. Pre–whitening filters of higher order have to be adaptive. They can be designed using the Levinson–Durbin–algorithm.

3.3 Step size Control

As mentioned before, the NLMS algorithm uses an adaptation factor α called step size which is responsible for both stability and speed of convergence. Controlling the step size becomes especially important in case of noisy microphone signals like those in car environments or in double talk situations [16].

It can be shown [17] that an optimal step size exists for adaptation in a noisy environment which is also suitable for non stationary excitation signals:

$$\alpha_{opt} = \frac{\mathrm{E}\{\epsilon(k)^2\}}{\mathrm{E}\{e(k)^2\}}, \tag{3}$$

where $\mathrm{E}\{...\}$ denotes expectation, $e(k)$ the current error value and $\epsilon(k)$ the residual echo signal. The application of (3), however, requires a reliable double talk detector [18].

3.4 Affine Projection Algorithm

Looking closely at the affine projection algorithm (APA), it can be considered as an extension of the NLMS algorithm, taking into account the P last excitation vectors.

$$e(k) = d(k) - \underline{c}^T(k)\underline{x}(k), \quad (4)$$

$$\underline{e}(k) = (e(k), e(k-1), \ldots, e(k-P+1))^T, \quad (5)$$

$$\underline{X}(k) = (\underline{x}(k), \underline{x}(k-1), \ldots, \underline{x}(k-P+1))^T, \quad (6)$$

$$\underline{c}(k+1) = \underline{c}(k) + \underline{X}(k) (\underline{X}^T(k) \underline{X}(k))^{-1} \underline{e}^T(k). \quad (7)$$

Usually P is small compared to the total number of filter coefficients. In contrast to the NLMS algorithm, the matrix $\underline{X}^T(k) \underline{X}(k)$ has to be inverted. This can be carried out recursively. A fast version of the APA – called FAP (fast affine projection [11]) – has been developed for an efficient implementation. This algorithm is therefore suitable for acoustic echo cancellers. However, numerical instabilities occur because of recursively calculated correlation matrices. One can overcome these problems by regularising the correlation matrix by adding a constant value to the values of the main diagonal. Furthermore, the algorithm has to be reinitialised whenever divergence is detected.

If an affine projection of second order is applied, the inverse of the matrix can be calculated directly requiring only small computational load. Compared to the NLMS algorithm, even a second order APA increases the speed of convergence remarkably.

3.5 RLS and FTF

The recursive least squares algorithm (RLS) is known as a very fast converging recursive algorithm. A straight forward notation of this algorithm is given here:

$$\underline{w}(k) = \lambda^{-1} R_{xx}^{-1}(k) \underline{x}(k), \quad (8)$$

$$R_{xx}^{-1}(k+1) = \lambda^{-1} R_{xx}^{-1}(k) - \frac{\underline{w}(k) \underline{w}^T(k)}{1 + \underline{w}^T(k) \underline{x}(k)}, \quad (9)$$

$$e(k) = d(k) - \underline{c}^T(k) \underline{x}(k), \quad (10)$$

$$\underline{c}(k+1) = \underline{c}(k) + e(k) \underline{w}(k), \quad (11)$$

where $R_{xx}(k)$ denotes an estimate of the autocorrelation matrix of the excitation signal, λ an exponential forgetting factor $(0 < \lambda < 1)$ and $\underline{w}(k)$ the gain vector. The convergence of the RLS algorithm is superior to the NLMS algorithm. However, there is the problem of locking when λ is chosen close to one. The tracking performance of the RLS algorithm is therefore not as satisfying as the initial convergence.

If the algorithm is implemented with finite–precision, it can become unstable for the numerical round–off error increases. A QR–Decomposition based inversion of the autocorrelation matrix does not show this behaviour [12].

If one has to deal with a large number of coefficients, the direct implementation of the RLS algorithm is not feasible since its computational complexity of order M^2.

Several approaches for a fast version of the RLS algorithm are known, principally based on pre–windowing techniques which reduce the computational load to order M. A fast implementation of the RLS algorithm – called Fast Transversal Filter algorithm (FTF) – is organised in four steps:

- Recursive forward linear prediction.

- Recursive backward linear prediction.

- Recursive computation of the gain vector.

- Recursive estimation of the desired response.

Unfortunately, the FTF algorithm is numerically unstable and tends to diverge. In fact, stabilising the RLS algorithms is a topic in its own right [13, 15]. One basic idea is to extend the algorithm by accumulating the round–off errors and to perform corrections when the numerical error becomes significant.

3.6 Fast Newton

Whereas the APA may be considered as an extended version of the NLMS algorithm, the Fast Newton algorithm can be seen as a simplified version of the fast RLS algorithm [14]. In fast implementations of the RLS algorithm, linear predictions of the order M are required, where M is the size of the coefficient vector. When the order of correlation of the excitation signal is small, there is actually no need to calculate the full prediction vector of order M. Reducing the size of the prediction vector to a size P appropriate to the excitation signal leads to the Fast Newton algorithm. The convergence performance is comparable to the RLS algorithm, whereas the numerical complexity is of order MP.

3.7 Fullband – Subband – Block–processing

Until now, our discussion of adaptive filters has dealt only with fullband signals, since this is the most straight forward method of implementation. However, straightforward does not necessarily mean most efficient. Both sub–band and block processing enable implementations resulting in less computational cost.

If a signal is split up into subbands, one can subsample the resulting signals leading to shorter adaptive echo cancellers. All of the adaptive algorithms mentioned above are suitable for subband implementation. The

processing power saved may be used for more complex adaptation. However, subband realisations do have one substantial disadvantage that may prohibit their application: they introduce delay into the system [10]. This delay is caused by the filter–banks for analysis (decomposition) and synthesis of the excitation and error signals. These filter–banks have to be designed with respect to the special demands of an adaptive echo canceller. The aliasing terms for example have to be minimised [19]. There is a substantial body of literature concerned with the design of polyphase filter banks used for echo cancellation (e.g. [20, 21]).

In block processing, the impulse response of the adaptive filter is split up into blocks. Using fast convolution techniques, the calculation of the output signal can be carried out very efficiently [22]. Again, there is a trade–off between efficiency of processing and delay. However, block–processing offers the advantage of optimising delay versus processing power. Small block sizes keep the delay low but increase the processing power required.

4 STEREOPHONIC ECHO CANCELLATION

Recently stereophonic acoustic echo cancellation became more and more important for applications such as teleconferencing or video games [23].
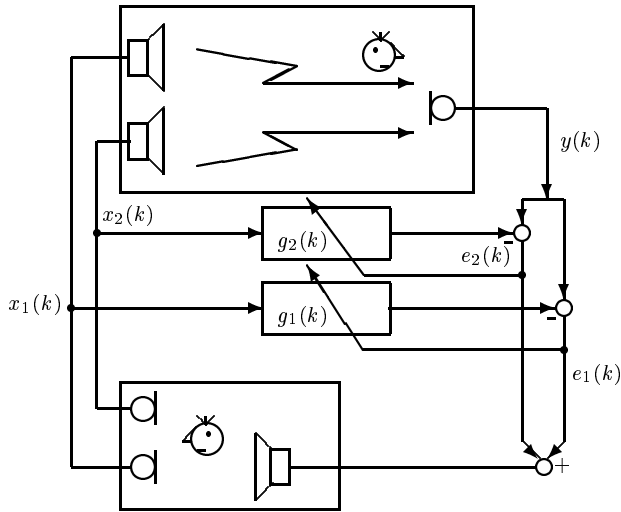

Figure 3: Stereophonic echo cancellation

As the excitation signals of the two channels are correlated (Fig. 3), there is no unique solution for identifying the two impulse responses. Furthermore, an extended correlation matrix of the two input signals has to be inverted. In case of high correlation, this causes numerical instabilities due to ill–conditioning which, in turn, leads to divergence. However, there are a number of approaches to overcome the correlation of the two excitation signals. One technique applies a nonlinear func-

tion to one of the excitation signals [23]. In a second approach the correlation matrix is regularised by introducing leakage into the update of the coefficient vector [24].

5 NOISE REDUCTION

With the increasing number of mobile telephones, more and more people use them in cars. This generates a demand for hands–free telephone sets for cars that not only increase the comfort to the user but also allow the driver to keep his hands on the steering wheel.

To enhance the speech signal outgoing to the far–end user, noise reduction methods are desirable.

We describe one channel methods for two reasons: first the cost for installing a second channel may be prohibitive, and secondly single channel procedures can also be extended to multi–channel methods.

5.1 Basic architecture

Most noise reduction procedures are based on the Wiener solution [25]:

$$
G_{opt}(kB, n) = \begin{cases} 1 - \left(\kappa \frac{N_{PSD}(kB,n)}{X_{PSD}(kB,n)} \right)^p : G_{opt} > \beta_f \\ \beta_f \qquad\qquad : \text{otherwise}, \end{cases} \quad (12)
$$

where $N_{PSD}(kB, n)$ and $X_{PSD}(kB, n)$ denote the PSD of the noise and the distorted input signal respectively and B is equal to the block size. The frequency index is given by n. Compared to the well–known Wiener filter an overestimation factor κ, a variable power p, and a spectral floor β_f are introduced.

Unfortunately, there is a conflict between the ratio of the noise reduction and the quality of the resulting speech signal. The parameters suggested above have to be chosen such that a subjective obtimum is achieved.

To preserve natural sounding speech the spectral floor is introduced which in turn limits the SNR–improvement to $-20 \log(\beta_f)$dB. The imprecision associated with estimation of the time–varying PSDs causes an unpleasant tonal noise. The so–called musical–tones can be attenuated by tailoring the transfer function adequately with the additional parameters.

Modifications of the filter (12) are given by the MMSE–STSA estimator (Minimum Mean Square Error Short–Time Spectral Amplitude) and its derivation the MMSE–LSA estimator (Minimum Mean Square Error Logarithmic Spectral Amplitude) [26, 27]. To derive the algorithms the time–varying property of the distorted input signal has been taken into account. For these algorithms an 'a priori' and an 'a posteriori' signal to noise ratio (SNR) are estimated:

$$
SNR_{post}(kB, n) = \frac{|X(kB, n)|^2}{|N_{PSD}(kB, n)|^2} - 1, \quad (13)
$$

$$
SNR_{prio}(kB, n) = (1 - \gamma) \max(SNR_{post}(kB, n), 0)
$$

$$+ \gamma \frac{|G_{opt}((k-1)B, n) \, X(kB, n)|^2}{|N_{PSD}(kB, n)|^2}. \tag{14}$$

$X(kB, n)$ describes the STFT of the input signal $x(k)$ at block and kB. The weighting rules for the algorithms are given by:

1) MMSE–STSA:

$$G_{opt}(kB, n) \quad = \tag{15}$$

$$\frac{\sqrt{\pi}}{2} \sqrt{\frac{1}{1 + SNR_{post}(kB, n)} \frac{SNR_{prio}(kB, n)}{1 + SNR_{prio}(kB, n)}}$$

$$* M_1 \left[(1 + SNR_{post}(kB, n)) \frac{SNR_{prio}(kB, n)}{1 + SNR_{prio}(kB, n)} \right]$$

with: $\quad M_1[u] = \exp(-\frac{u}{2}) \left[(1 + u)I_0(\frac{u}{2}) + I_1(\frac{u}{2}) \right]$

2) MMSE − LSA:

$$G_{opt}(kB, n) \quad = \quad \frac{SNR_{prio}(kB, n)}{1 + SNR_{prio}(kB, n)} \tag{16}$$

$$* M_2 \left[(1 + SNR_{post}(kB, n)) \frac{SNR_{prio}(kB, n)}{1 + SNR_{prio}(kB, n)} \right]$$

with: $\quad M_2[u] = \exp \left\{ \frac{1}{2} \int_u^\infty \frac{e^{-t}}{t} dt \right\}$ and I_0, I_1 the modified Bessel functions of first and second order.

5.2 Frequency Decomposition

As shown above the noise reduction filter is defined in the frequency domain. Therefore a frequency analysis of the non–stationary input signal is required. One method achieving this is to use the STFT (Short Time Fourier Transform) which needs the multiplication of the input signal by a time–window $\gamma(m)$:

$$X(kB, n) = \sum_{m=0}^{N-1} x(m)\gamma(m - kB)e^{-j\frac{2\pi}{N}nm} \tag{17}$$

Subband decomposition provides a second class of methods. The sample values of the subband signals can produce a set of spectral coefficients for the noise reduction algorithm (Fig. 4).

After noise reduction the subband signals are upsampled, passed through anti–aliasing filters, and synthesised to obtain the enhanced output signal. The filterbanks shown in Fig. 4 split the input signal into uniformly spaced frequency bands [20] comparable to the STFT. Modifications include non–uniformly spaced frequency resolutions [28] offering the possibility of modeling the human perception system (ear and brain)
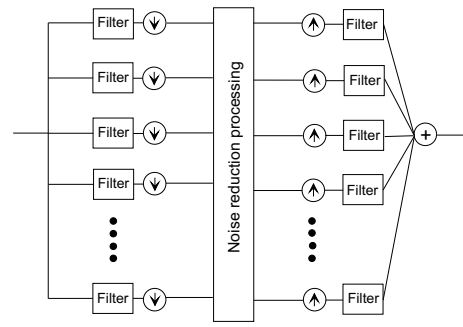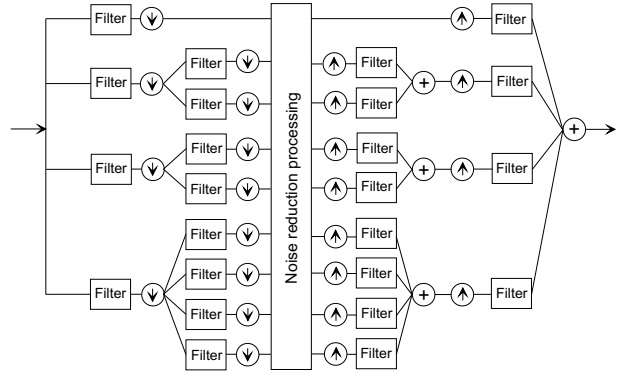

Figure 4: Filterbank

Figure 5: Cascaded filterbank

(s. 5.4). Alternatively non–uniformly distributed resolution can be obtained by cascaded filter banks (Fig. 5) including the special case of the discrete wavelet transform (Fig. 6) [29, 30].

With these cascaded structures also different time–resolutions are obtained as subsampling is performed after each filter stage. Fast varying high frequency components can be treated with a higher resolution in time whereas low frequency components show a more detailed frequency resolution.

5.3 Estimation of the Power Spectral Densities

The time–frequency analysed input signal can be used to estimate $X_{PSD}(kB, n)$ and $N_{PSD}(kB, n)$.

To determine $X_{PSD}(kB, n)$ a recursively smoothed periodogramm is sufficient. However, only slight smoothing is tolerable to avoid echo–reverberation effects in the enhanced signal.

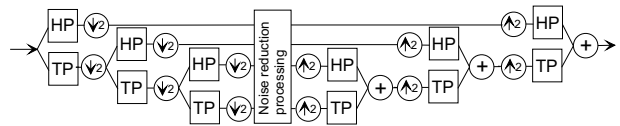The estimation of $N_{PSD}(kB, n)$ has to be based on $X(kB, n)$ also. To distinguish between noise compo-

Figure 6: Wavelet filterbank

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