# BEFORE THE PATENT TRIAL AND APPEAL BOARD 

# MICROSOFT CORPORATION <br> Petitioner 

v.

## BRADIUM TECHNOLOGIES LLC

Patent Owner

CASE: To Be Assigned
Patent No. 7,908,343 B2

DECLARATION OF PROF. WILLIAM R. MICHALSON IN SUPPORT OF PETITION FOR INTER PARTES REVIEW OF U.S. PATENT NO. 7,908,343 B2

I hereby declare that all the statements made in this Declaration are of my own knowledge and true; that all statements made on information and belief are believed to be true; and further that these statements were made with the knowledge that willful false statements and the like so made are punishable by fine or imprisonment, or both, under 18 U.S.C. 1001 and that such willful false statements may jeopardize the validity of the application or any patent issued thereon.

I declare under the penalty of perjury that all statements made in this Declaration are true and correct.

Executed _June 2nd $\qquad$ 2015 in _Douglas $\qquad$ , _MA $\qquad$ .


William R. Michalson

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Appendix X George H. Forman and John Zahorjan, "The challenges of mobile computing," Computer vol. 27, no. 4, pp. 38, 47 (April 1994)

Appendix Y K. Brown and S. Singh, A Network Architecture for Mobile Computing, INFOCOM '96, Fifteenth Annual Joint Conference of the IEEE Computer Societies, Networking the Next Generation, Proceedings IEEE vol. 3, pp. 1388-139

Appendix Z Kreller, B. et al "UMTS: a middleware architecture and mobile API approach," Personal Communications, IEEE, vol. 5, no. 2, pp. 32-38 (April 1998)

Appendix AA Hansen, J. et al, "Real-time synthetic vision cockpit display for general aviation," AeroSense '99, International Society for Optics and Photonics, 1999.

Appendix BB U.S. Patent No. 5,760,783 to Migdal et al ("Migdal")
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Appendix FF Theresa-Marie Rhyne, A Commentary on GeoVRML: A Tool for 3D Representation of GeoReferenced Data on the Web, International Journal of Geographic Information Sciences, issue 4 of volume 13, 1999

## I. INTRODUCTION

1. My name is William R. Michalson. I am a faculty member at Worcester Polytechnic Institute. I have been engaged by Microsoft Corporation ("Microsoft") to investigate and opine on certain issues relating to U.S. Patent No. 7,908,343 B2 ("the 343 Patent") entitled "System and methods for network image delivery with dynamic viewing frustum optimized for limited bandwidth communication channels" in Microsoft's Petition for Inter Partes Review of the 343 Patent ("Microsoft IPR Petition") which requests the Patent Trial and Appeal Board ("PTAB") to review and cancel all claims of the 343 Patent -claims 1-20 ("Challenged Claims"). I have also been engaged by Microsoft to investigate and opine on certain issues relating to two other patents that are related to the 343 Patent- U.S. Patent Nos. 7,139,794 B2 and 8,924,506 B2 in additional petitions for inter partes review by Microsoft. I understand that Bradium Technologies LLC ("Bradium") is asserting all three patents against Microsoft in an on-going patent infringement lawsuit, No. 1:15-cv-00031-RGA, filed in the U.S. District Court for the District of Delaware on January 9, 2015.
2. I understand that the 343 Patent was assigned from the inventors Isaac Levanon and Yoni Lavi to 3DVU Ltd (2000) Israel on September 11, 2008, then assigned from 3DVU, Inc. to Inovo Limited on June 5, 2009, and assigned from

Inovo Limited to Bradium on June 17, 2013. Bradium is therefore referred to as the "Patent Owner" in this declaration.
3. In this declaration, I will first discuss the technology background related to the 343 Patent and then provide my analyses and opinions on claims 120 of the 343 Patent. The discussion of the technology background includes an overview of that technology as it was known before October 1999, which I understand as being the earliest invention date of the 343 Patent claimed by the inventors in their inventor declarations submitted to the USPTO during the original prosecution of the 343 Patent's parent patent, U.S. Patent No. 7,644,131. This overview provides some of the bases for my opinions with respect to the 343

## Patent.

4. This declaration is based on the information currently available to me.

To the extent that additional information becomes available, I reserve the right to continue my investigation and study, which may include a review of documents and information that may be produced, as well as testimony from depositions that may not yet have been taken.
5. In forming my opinions, I have relied on information and evidence identified in this declaration, including the 343 Patent, the prosecution history of
the 343 Patent, and prior art references listed as Exhibits to the Microsoft IPR Petition and listed as appendices of this declaration.

## II. SUMMARY OF OPINIONS

6. Claims 1-20 of the 343 Patent relate to a system and a method for dynamic visualization of image data transferred through a communications channel. For the reasons explained below, none of the features described in Claims 1-20 of the 343 Patent were novel as of October 1999, nor does the 343 Patent teach a novel and non-obvious way of combining these known features.
7. Claims 1-20 of the 343 Patent relate to well-known technologies in the computer industry such as multi-resolution hierarchical maps, image compression, packetized data transmission, and three-dimensional (3D) graphics rendering. No element of Claims 1-20 is novel, and Claims 1-20 do not bring these elements together in a way that brings any benefit beyond what a person of ordinary skill in art would expect from the known functions of the individual components. Claims 1-20 describe techniques that were well-known in the field, and combine them in ways that would have been readily apparent to a person of ordinary skill in the art with predictable results.
8. It is my opinion that each of Claims 1-20 is invalid under the patentability standard of 35 U.S.C. $\S 103$ as I understand it and as explained to me
by Microsoft's counsel. Within this declaration I discuss specific grounds of invalidity of Claims 1-20; however, my opinion that Claims 1-20 are invalid under 35 U.S.C. § 103 is not limited to these specific grounds, and indeed, it is my opinion that Claims 1-20 would have been invalid in light of the general knowledge of a person of ordinary skill in the art at the time of the alleged invention.
9. For purposes of my analyses in this declaration only, I provide my proposed construction of certain terms in Claims 1-20 in detail in a later part of this declaration.
10. The subsequent sections of this declaration will first provide my qualifications and experience and then describe details of my analyses and observations.

## III. QUALIFICATIONS AND EXPERIENCE

## A. Education and Work Experience

11. I received a Ph.D. degree in Electrical Engineering in 1989 and a Master of Science degree in Electrical Engineering in 1985 from the Worcester Polytechnic Institute. I received a Bachelor of Science degree in Electrical Engineering from Syracuse University in 1981.
12. I have more than twenty years of experience in the fields of electrical engineering, computer systems, navigation systems, and communications systems. My experience includes the design, implementation and use of geographic information systems ("GIS"), as well as the design, implementation and use of navigation systems relying on GPS and other positioning system technologies. I also have extensive experience in computer communication and data processing systems as well as systems for the efficient transmission of digital images and other data. Additionally, I have experience in the design and implementation of hardware and software systems used to render image data for display.
13. I have published 16 papers in technical journals and 97 papers in technical conferences. I hold eight U.S. patents in the fields of handheld GPS (Global Positioning System), portable geolocation devices, and communication networks. I have also authored one book chapter relating to optical interconnect networks for massively parallel computers. I became a Senior Member of the Institute of Electrical and Electronics Engineers (IEEE) in 2003.
14. My experience spans from product designs and R\&D in industry, teaching, research and development in an educational and research institution to technology consulting to industry. I was an engineer at Raytheon Company for ten years from 1981 to 1991. During this period, I worked on projects related to
computer display hardware for various applications, including air traffic control applications.
15. After leaving Raytheon Company, I joined the Worcester Polytechnic Institute and became a full-time faculty member there in 1991. My research at WPI focuses on navigation systems and related technologies. I am the director of WPI's Center for Advanced Integrated Radio Navigation.
16. My research projects at WPI cover various technologies and include (1) a system using tracking and communications technologies to track shipping containers, (2) an automotive based system that combined GPS and map data in an automotive environment, (3) a remote hazard detection system using GPS and radio communications, and (4) a differential GPS system that combined GPS and radio technologies to determine the precise path of vehicles operating off-road during forest operations.
17. I have worked as a consultant in the navigation and communication systems fields, e.g., in the context of space shuttle docking operations, transfer of traffic information to GPS devices, combinations of GPS and cellular communications for tracking purposes, and map-based handheld tracking devices.
18. I am familiar with numerous GIS and mapping products that existed in the market since the late 1980s, including systems and software developed by

Etak, Microsoft, DeLorme, and others. In the conduct of my research and other work, I have routinely used commercially available GIS and mapping products and have developed mapping and visualization software for specialized applications. Additionally, I have used and incorporated database systems such as Microsoft Access, Borland Paradox, Oracle, SQL and others in my research and have incorporated database systems into other hardware and software systems for use in storing and retrieving GIS-related data.
19. I have done extensive research work in communications and networking system design, and have worked with all of the digital, analog and software components needed to build communications and navigation systems. My work with communications and networking protocols began in the mid-1980s with TCP/IP over packet radio. I have used these and other communications and networking protocols extensively in conducting my research. In addition, my work on GPS and navigation systems involved implementing low-latency communications to support differential techniques that allow a GPS receiver to provide more accurate positioning information.
20. I have extensive experience with the development and maintenance of server computers, including the installation and maintenance of web servers and file servers, as well as the design, development, test, and maintenance of web
based applications. These applications typically employ C/C++, Java, JavaScript, PHP, HTML, MySQL, and etc. I am also experienced with server-client systems where the client computer exchanges navigation and/or geographical information with server computer through a wired and/or wireless network.
21. My curriculum vitae, which provides a detailed summary of my education, work experience, publication, teaching history, and etc. is attached to this declaration as Appendix A.

## B. Compensation

22. I am being compensated for the services I am providing in this and other Microsoft IPR petitions. The compensation is not contingent upon my performance, the outcome of this inter partes review or any other proceedings, or any issues involved in or related to this inter partes review or any other proceedings.

## C. Documents and Other Materials Relied Upon

23. The documents on which I rely for the opinions expressed in this declaration are documents and materials identified in this declaration, including the 343 Patent, patents related to the 343 Patent, the prosecution history for the 343 Patent and other patents related to the 343 Patent, the prior art references and information discussed in this declaration, including the references attached as
exhibits of the IPR Petition for the 343 Patent: Maps Alive: Viewing Geospatial Information on the WWW, Michael Potmesil, Computer Networks and ISDN Systems Vol. 29, issues 8-13, pp. 1327-1342 ("Potmesil") (Ex. 1002), WO 99/41675 to Cecil V. Hornbacker, III ("Hornbacker") (Ex. 1003), An Integrated Global GIS and Visual Simulation System by P. Lindstrom et al., Tech. Rep. GIT-GVU-97-07, March 1997 (Ex. 1004), U.S. Pat. No. 5,682,441 to Adrianus

Ligtenberg et al ("Ligtenberg") (Ex. 1005), U.S. Pat. No. 6,650,998 to Charles Wayne Rutledge et al ("Rutledge") (Ex. 1006), U.S. Pat. No. 6,118,456 to David G. Cooper ("Cooper") (Ex. 1007), WO 98/15920 to David Kelly Austreng ("Austreng") (Ex 1008), U.S. Pat. No. 5,940,117 to Amer Hassan et al ("Hassan") (Ex. 1012) and any other references specifically identified in this declaration, in their entirety, even if only portions of these documents are discussed here in an exemplary fashion.

## IV. STATEMENT OF LEGAL PRINCIPLES

## A. Claim Construction

24. Microsoft's counsel has advised that, when construing claim terms of an unexpired patent, a claim subject to inter partes review receives the "broadest reasonable interpretation (BRI) in light of the specification of the patent in which it appears."

## B. Anticipation

25. Microsoft's counsel has advised that in order for a patent claim to be valid, the claimed invention must be novel. Microsoft's counsel has further advised that if each and every element of a claim is disclosed in a single prior art reference, then the claimed invention is anticipated, and the invention is not patentable according to pre-AIA 35 U.S.C. § 102 effective before March 16, 2013. In order for an invention in a claim to be anticipated, all of the elements and limitations of the claim must be shown in a single prior reference, arranged as in the claim. A claim is anticipated only if each and every element as set forth in the claim is found, either expressly or inherently described, in a single prior art reference. In order for a reference to inherently disclose a claim limitation, that claim limitation must necessarily be present in the reference.

## C. Obviousness

26. Microsoft's counsel has also advised me that obviousness under preAIA 35 U.S.C. § 103 effective before March 16, 2013 is a basis for invalidity. I understand that where a prior art reference does not disclose all of the limitations of a given patent claim, that patent claim is invalid if the differences between the claimed subject matter and the prior art reference are such that the claimed subject matter as a whole would have been obvious at the time the invention was made to a
person having ordinary skill in the relevant art. Obviousness can be based on a single prior art reference or a combination of references that either expressly or inherently disclose all limitations of the claimed invention. In an obviousness analysis, it is not necessary to find precise teachings in the prior art directed to the specific subject matter claimed because inferences and creative steps that a person of ordinary skill in the art would employ can be taken into account.

## V. LEVEL OF ORDINARY SKILL IN THE ART

27. I understand from Microsoft's counsel that the claims and specification of a patent must be read and construed through the eyes of a person of ordinary skill in the art at the time of the priority date of the claims. I have also been advised that to determine the appropriate level of a person having ordinary skill in the art, the following factors may be considered: (a) the types of problems encountered by those working in the field and prior art solutions thereto; (b) the sophistication of the technology in question, and the rapidity with which innovations occur in the field; (c) the educational level of active workers in the field; and (d) the educational level of the inventor.
28. The "Background of the Invention" section of the 343 Patent describes a "well recognized problem" of how to reduce the latency for transmitting full resolution images over the Internet on an "as needed" basis,
particularly for "complex images" such as "geographic, topographic, and other highly detailed maps." Ex. 1001 at 1:34-43.
29. To solve this problem and to address some perceived issues in the existing art, the 343 Patent discloses a system capable of "optimally presenting image data on client systems with potentially limited processing performance, resources, and communications bandwidth." Id. at 3:40-43. The 343 Patent states that the disclosed technology can achieve faster image transfer by (1) dividing the source image into parcels/tiles, (2) processing the parcels/tiles into a series of progressively lower resolution parcels/tiles, and (3) requesting and transmitting the parcels/tiles needed for a particular viewpoint in a priority order, generally lowerresolution tiles first.
30. In light of the disclosed technology of the 343 Patent, a person of ordinary skill in the art for the 343 Patent would need education or work experience in computer network communications. Because a "common application" of the 343 Patent is to transmit "geographic, topographic, and other highly detailed maps," (id. at 1:37-39), a person of ordinary skill in the art would require some knowledge and experience with geographic information systems ("GIS").
31. Based on the above considerations and factors, it is my opinion that a person having ordinary skill in the art should have a Master of Science or equivalent degree in electrical engineering or computer science, or alternatively a Bachelor of Science or equivalent degree in electrical engineering or computer science, with at least 5 years of experience in a technical field related to geographic information system ("GIS") or the transmission of image data over a computer network. This description is approximate and additional educational experience could make up for less work experience and vice versa.

## VI. TECHNOLOGY BACKGROUND OF THE 343 PATENT

32. It is my opinion that the 343 Patent recites an obvious and predictable combinations of technical features that were well-known in the art at the time the 343 Patent was filed and at the time of alleged invention. In this section of my declaration, I provide an overview of some general principles that were understood and documented in the art at the time of filing of the 343 Patent, and therefore would be within the knowledge of a person of ordinary skill in the art. I use certain references (including both patents and non-patent literature) to illustrate the background knowledge of a person of ordinary skill in the art, but the knowledge of a person of ordinary skill in the art at the time regarding the claimed features would not have been limited to these specific references.

## A. Data Communications Over the Internet

33. The predominant computer networking technology and set of communications protocols used for most online communications today and prior to the filing of the application for the 343 Patent is known as the Internet Protocol (IP) suite called TCP/IP, after its two main component protocols: the Transmission Control Protocol and the Internet Protocol. The 343 Patent teaches at 7:26-46 that its preferred embodiment uses TCP/IP to send data packets. In this declaration I do not provide a detailed description of all characteristics of the very well-known TCP/IP protocols, but focus on a few specific aspects of TCP/IP that are pertinent to the claims at issue in the 343 Patent. TCP/IP transmits data between computers in a network using data packets, which are formatted units of data carried by the network as suitably sized blocks. Packets are composed of a header and a payload. The "payload" is the information which the packet is actually intended to convey. The header refers to supplemental data placed at the beginning of a block, and contains information in a standard format such as the sender's and recipient's Internet Protocol addresses, a sequence number indicating where in a sequence of packets being transmitted the packet falls, an offset (how far into the data the payload begins) and the protocol governing the format of the payload. The addresses are used to route the packet to its destination, although unlike a circuit-
switched connection, different packets going between the same sender and recipient at the same time may take different routes over the network. A rough analogy for data packets is that the header is the "envelope" which contains the address used to deliver the packet, while the payload is the contents of the envelope. The destination computer uses information in the header to place the data packet in its proper place in order, from which the original data contained in multiple packets can be reassembled. When data segments arrive in the wrong order TCP/IP buffers the out-of-order data until all data can be properly re-ordered and delivered to the application.
34. Before data is transmitted using TCP/IP, the sender and the destination exchange a short series of messages confirming a connection. The connection in this case simply means that the sender and the destination exchange messages to confirm that they are able to exchange messages via the network. When the destination computer receives a packet, it sends a short confirmation message to the sender that the packet has been received. If the confirmation is not received within a certain time period, the sender re-sends the packet. This method avoids losing data in transmission if the transmission of a single packet fails.
35. A common consideration in building online systems is how large to make the data packets. Among other trade-offs, smaller packets may be more
likely to reach their destination without loss or error; however, because the header size is similar for a large packet and a small packet, the amount of bandwidth taken up by header overhead increases with the use of smaller packets. In some cases, the network protocol sets a maximum packet length.

## B. Data Communications in Wireless Mobile Systems

36. By the late 1990s, it was well-known in the art that digital data could be transmitted by TCP/IP over wireless networks. For example, Appendix X, "The challenges of mobile computing," Computer vol. 27, no. 4, pp. 38, 47 (April 1994) provides an overview of methods for implementing internet connections on mobile devices as of 1994, noting that while wireless networks typically deliver lower bandwidth than wired networks, cellular telephone products of the time could already achieve transmission rates of 9-10 kilobits per second.
37. In another example in 1996, K. Brown and S. Singh, A Network Architecture for Mobile Computing, INFOCOM '96, Fifteenth Annual Joint Conference of the IEEE Computer Societies, Networking the Next Generation, Proceedings IEEE vol. 3, pp. 1388-1397 (Appendix Y) describes technologies that integrate wireless or mobile networks with existing fixed data networks such as the Internet. This integration was described by using mobile data protocols to interact and be compatible with the TCP/IP structure of the Internet. This paper described
how the Universal Mobile Telecommunications System (UMTS) under development in Europe was expected to offer average mobile data rates of between 1-2 megabytes per second (Mbps) per mobile user. Among other features, "Mobile users will be able to access their data and other services such as... map services." App. Y at 2.
38. Appendix Z, Kreller, B. et al "UMTS: a middleware architecture and mobile API approach," Personal Communications, IEEE, vol. 5, no. 2, pp. 32-38 (April 1998) describes the development of third-generation (3G) mobile networks offering "high-bit-rate data services, guaranteed on-demand bandwidth, and low delays." Id. at 32. To illustrate the development of frameworks to connect mobile telephone networks with existing fixed networks, the authors use the example of a mapping service called "City Guide," which allows a mobile device to request and download map imagery and other data from a server via hypertext transfer protocol (HTTP) to "provide access to maps describing the current surroundings." Id. at 33. The CityGuide could use JPEG compression and decompression, and could achieve bandwidth of up to 9.6 kbps using the then-existing Global System for Mobile Communications (GSM) cellular data standard. Id. at 36, 37.

## C. Image Tiles and Image Pyramids

39. The 343 Patent describes sub-dividing a high resolution source image into a regular array of image parcels (a.k.a. image tiles), and pre-processing the image into a series of derivative images of progressively lower resolutions. Ex. 1001 at 6:1-16; Fig. 2. Preferably, the resolution decreases by a factor of four for each derivative image in the series. Id. at 6:11-14. Fig. 2 of the six provisional applications to which the 343 Patent claims priority (which is identical in all six provisional applications) best illustrates this image tiling and image pyramid scheme. Ex. 1010 at Fig. 2.


## FIG. 2

40. This image processing scheme, however, had been developed and widely used long before the 343 Patent's priority date. For example, Hanan

Samet's book The Design and Analysis of Spatial Data Structures discloses generating an image "pyramid" from a $2^{n} \times 2^{n}$ image array, where the pyramid is "a sequence of arrays $\{A(i)\}$ such that $A(i-1)$ is a version of $A(i)$ at half the scale of A(i)." App. B , Hanan Samet, The Design and Analysis of Spatial Data Structures, at 12 (1989, Reprinted with corrections in Jan. 1994). Fig. 1.7 in the Samet book is virtually the same as Fig. 2 of the provisional applications to which the 343 Patent claims priority.


## Figure 1.7 Structure of a pyramid having three levels

41. In another example, U.S. Patent No. 5,263,136 (DeAguiar et al.) filed on April 30, 1991 and issued on November 16, 1993, entitled System for Managing Tile Images using Multiple Resolutions, discloses an "image memory management system for tiled images," where "each source image is stored as a full resolution image and a set of lower-resolution subimages." App. C at Abstract; Figs. 1 and 2. Suitable applications of the DeAguiar patent's image tiling and image pyramid
scheme include "electrical schematics, topographical maps, satellite images, heating/ventilating/air conditioning (HVAC) drawings, and the like." Id. at col. 6:65-7:2.

42. U.S. Patent 4,972,319 to Delorme, filed on Sept. 25, 1987 and issued on Nov. 20, 1990, also showed that image tiling and image pyramid can be used in mapping applications. Specifically, the Delorme patent discloses a "global mapping system which organizes mapping data into a hierarchy of successive magnitudes or levels for presentation of the mapping data with variable resolution, starting from a first or highest magnitude with lowest resolution and progressing to a last or lowest magnitude with highest resolution." App. D at Abstract. A
pyramid of successively lower resolution image tiles is shown in Fig. 8 of the Delorme 319 patent. Id. at Fig. 8.

43. In yet another example, a 1996 article entitled "The MAGIC Project: From Vision to Reality" by Barbara Fuller and Ira Richer ("Fuller") also shows the image tiling and image pyramid scheme for mapping applications. App. E at Fig. 3.


Figure 3. Relationship between tile resolutions and perspective view. (Source: SRI International)

## D. Compression of Image Tiles

44. The 343 Patent discusses that the image tiles can preferably be compressed, e.g., for a fixed compression ratio of 4:1. Ex. 1001 at 6:17-22. However, long before the 343 Patent's priority date, numerous methods existed and were published that disclose compressing images for either a variable or fixed ratio.
45. One widely used method of digital image compression is JPEG compression which is based on the Discrete Cosine Transform ("DCT") and is described in the International Telegraph and Telephone Consultative Committee ("CCITT") Recommendation T. 81 published in September 1992 (App. F). JPEG compression includes the following main steps: " 1 . The image is broken into 8 x 8 blocks of pixels. 2. Working from left to right, top to bottom, the DCT is applied to each block. 3. Each block is compressed through quantization. 4. The array of
compressed blocks that constitute the image is stored in a drastically reduced amount of space. 5. When desired, the image is reconstructed through decompression, a process that uses the Inverse Discrete Cosine Transform (IDCT)." App. G at 1, Ken Cabeen \& Peter Gent, Image Compression and the Discrete Cosine Transform.
46. Another widely used method of digital image compression is based on the wavelet transform. For example, Marc Antonini et al.'s 1992 paper Image Coding Using Wavelet Transform discloses a scheme for image compression using the wavelet transform. See generally App. H. In addition, the Antonini paper shows that image compression using wavelet transform not only achieves a good image quality (id. at 217-18), but is also suitable for a progressive transmission scheme to "allow the receiver to recognize a picture as quickly as possible at minimum cost." Id. at 218-19.
47. The JPEG 2000 image compression standard, which was designed as the next version of the JPEG Standard to address its identified problems, uses discrete wavelet transform.

## E. Progressive Image Resolution Enhancement

48. The progressive image resolution enhancement technique described and claimed in the 343 Patent is one of the "conventional" solutions that have been
used to reduce the latency of transmitting complex images over a communications network, as admitted in the "Background of the Invention" section of the 343 Patent. Ex. 1001 at 1:51-61 ("Different conventional systems have been proposed to reduce the latency affect by transmitting the image in highly compressed formats that support progressive resolution build-up of the image within the current client field of view. . . Progressive image resolution transmission, typically using a differential resolution method, permits an approximate image to be quickly presented with image details being continuously added over time.") (emphasis added).
49. For example, U.S. Patent No. 5,321,520 to Inga et al., filed July 20, 1992 and issued June 14, 1994, discloses a "Progressive Image Enhancement" ("PIE") method, where a "'crude' image is presented to the subscriber" first and then the method "progressively enhance[s] the quality of the presented image" over time. App. I at col. 12:65-13:1. "The longer the user observers a selected image, the 'better' the image becomes in the sense of pixel resolution and quantity of gray levels." Id. at col. 13:1-3.
50. The U.S. Patent No. 6,182,114 to Yap et al. was filed January 9, 1998 and issued January 30, 2001. The "Background of the Invention" section of the 343 Patent mentions Yap. The Yap Patent recognizes that "progressive
transmission" is an existing approach to solve the problem of "realtime visualization of large scale images over a 'thinwire' model of computation," i.e., over a "low bandwidth line." App. J at col. 1:47-65. In addition to the traditional progressive transmission method, where the higher resolution of the entire image will be eventually transmitted, Yap discloses an improved version of progressive transmission, where "resolution is also varied over the physical extent of the image." Id. at col. 2:4-17. Specifically, Yap discloses that "high resolution data is transmitted at the user's gaze point but with lower resolution as one moves away from that point." Id. at 2:18-20. The same scheme is used in the 343 Patent.

## F. Three-Dimensional Graphics

## 1. Overview of 3D Computer Graphics principles

51. Computer graphics is the art and science of drawing pictures on a display screen using a computer. A picture generated using computer graphics is created from numerical data describing the objects to be drawn. Computer graphics is generally divided into 2D ("two-dimensional") graphics that only depict images in two dimensions and 3D ("three-dimensional") graphics that depict images in three dimensions, although by way of a representation on a screen.
52. An image that shows up on a computer display typically corresponds to a large, rectangular, two-dimensional array of values in a computer memory
called a frame buffer. An individual location in the frame buffer can hold a color value corresponding to one "dot" or picture element, or pixel for short, on the display screen. In the simple example shown below, the values in the frame buffer at each pixel are either 0 or 1 , which get displayed as black and white, respectively, on the screen.

53. In display systems, color values at each pixel are usually either represented by a single number representing shades of gray, or by 3 numbers, R, G, and B , corresponding to red, green, and blue intensity values, for each location on the screen. The computer display is generated by repeatedly "scanning out" the array of numerical pixel values from the frame buffer memory in successive rows at a rate like 60 frames/second and used to produce the actual colors seen at each location on the screen.
54. When the computer changes an image displayed on the screen, it updates the corresponding values in the frame buffer. Simply writing a new number into the frame buffer at a given location results in a new color appearing at that position on the screen starting with the next refresh cycle.
55. Creating an image of a 3D scene involves taking a mathematical description of the objects in a scene, looking at it from a given point of view, and figuring out what colors to draw at all the pixel locations in the frame buffer to create the corresponding image on the screen, as shown in the following example of a 3D house being drawn on a 2D display. All 3D points in the scene are mapped to the corresponding pixels on the screen by projecting along lines of sight, as though the scene was being photographed by a camera onto film.

56. The mathematical description of the scene is known as a 3 D model. Each 3D object in the 3D model is typically represented using a collection of geometric "primitives" such as points, lines, and polygons (usually triangles) that
make up the object surfaces. In the simple example above, the house might be modeled using 4 polygons for the walls and 4 more polygons for the roof. Each polygon is defined by its vertices or corners. Typically, each vertex is specified using 3D numerical coordinates, $\mathrm{X}, \mathrm{Y}$, and Z , for its location in 3D space and $\mathrm{R}, \mathrm{G}$, and B values for its color. A mathematical process called rendering is used to model a virtual "camera" looking at the 3D scene from a particular point of view, mathematically project all the 3D polygons into the corresponding 2D pixels in the display, and assign the appropriate colors to them in the frame buffer.
57. Various 3D computer graphics systems are built around the concept of a graphics pipeline. Acting like an assembly line, the graphics pipeline takes in the "raw materials" consisting of the data for the underlying 3D model and processes these through a series of computational steps to produce the image displayed on the 2D screen. In its simplest form, a graphics pipeline is described as having a series of three general phases, geometry, rasterization, and display, as shown in the diagram below:
```
3D model
Displayed image
```


58. In the above diagram, the 3D model represents the $\mathrm{X}, \mathrm{Y}, \mathrm{Z}$ coordinates and $\mathrm{R}, \mathrm{G}, \mathrm{B}$ color values for all the 3D polygons that make up the objects in the desired scene, along with certain other information such as the location of the camera, light sources, display boundaries, etc. Geometry refers to the calculations performed to mathematically transform the 3D coordinates of all the polygons in the 3D model into corresponding screen coordinates given the location and orientation of the imaginary camera viewing the scene. Rasterization refers to the computations that determine all of the 2 D pixel locations that will be visible within each 3D polygon and the colors those pixels should have. Display is then the process of writing the 2D pixel color values into the frame buffer and thereby causing the corresponding image to be displayed on the screen.
59. Rasterizing a polygon generally involves three main tasks:
determining which pixels fall within the polygon (scan conversion), determining which of these pixels are visible on the screen (visible-surface determination), and determining what color to assign each visible pixel (shading).
60. The process of determining which pixels within the scan converted polygons will actually be visible on the screen is known as visible-surface determination. Depending on the direction from which the scene is viewed by the virtual camera, certain polygons (or portions thereof) may be occluded by other
polygons and not visible on the screen, such as the back wall of the house in the example shown above. One common way to solve the visible surface problem is to write the RGB value for a pixel into the frame buffer only if its 3D position is closer to the camera than what may have been previously written into that same location by another polygon, much as an oil painting is painted in layers from back to front. This involves what is known in the art as depth buffering or z-buffering, that is, keeping track of the depth or "Z" value (distance from the viewer's eye) currently residing at each pixel.
61. Once the scan conversion and rasterization processes are complete, the graphics program must assign colors to each visible pixel, a process that has evolved substantially over the history of computer graphics and depends on the level of realism desired in the resulting image. In the simple example below, only the scan converted pixels that make up the edges of each polygon are drawn with black pixels.


## Example of A Wireframe Image

62. The rendering program may further assign colors either to the entire polygon or to individual pixels within the polygon. The colors assigned to whole polygons may be calculated based on the "intrinsic" or "base" color of the object itself and the orientation of that particular polygon with respect to an imaginary light source in the 3D scene. The resulting process is commonly known as flat shading, as shown in the "teapot" example below based on an imaginary light source:


## 2. Texture

63. In 1974, "texture mapping" was developed as a further improvement in adding detail to objects or images. Texture mapping involves applying a 2D image or function approximating some real-world material like wood, bricks, fabric, marble, or a checkerboard, to the interior of polygons as in the image shown below. The "pixels" of a texture map are often referred to as texture elements or
texels to distinguish them from the pixels of the resulting image. Texture mapping is like applying wallpaper or a decal to a surface. It is possible to construct a brick wall by carefully drawing many 3D bricks, which takes a lot of work, or one can simply paste a photograph of a brick wall onto an otherwise flat wall, which is easier and looks like a brick wall if you don't look too close. Texture mapping has become standard in 3D graphics systems to use texture mapping to quickly fill in realistic detail for many of the objects in a 3D scene, especially floors, walls, sky, and other background areas. Textures can be either color images, or can be monochrome images used to modulate the untextured color of the polygon.
64. Some textures may be generic- for example, a 3D graphics rendering program might re-use a "wood" texture for all objects represented as wood. In this scenario, the texture is essentially a "wallpaper" with a repeating pattern applied to certain objects or surfaces within the field of view.
65. Textures may also be unique, or specific to a particular surface or object. This is often the case when photographs are used as textures. For example, when satellite or aerial photographs are used in a 3D rendering of a landscape, the specific portions of the imagery that correspond to a particular location are mapped onto the terrain at that location. For example, U.S. Patent No. 5,179,638 to Dawson et al., assigned to Honeywell, Inc., (App. K) illustrates how an aerial photograph
can be used as "texture data" and mapped onto co-located digital elevation data, as shown in Fig. 2:

66. This technique of using aerial imagery as a texture applied to a threedimensional model of terrain is also known as a "synthetic view." Synthetic view technology can be used in aviation to provide a pilot operating at night or bad weather with a synthesized view of the terrain around them based on actual position (e.g. derived from GPS). Appendix AA, Hansen, J. et al, "Real-time synthetic vision cockpit display for general aviation," AeroSense '99, International Society for Optics and Photonics, 1999, describes such a system. In the figure
below, the bottom portion of the figure shows a wire-frame diagram illustrating the three-dimensional model of terrain, while the top image shows the synthetic view created by rendering satellite imagery on the terrain model:


Figure 5. Terrain with extreme amounts of structure can be accommodated with high fidelity. The bottom graphic is a wire frame image of the Alaskan coastline. On the top is the fully rendered scene with imagery.
67. Microsoft used a similar technique with its popular Flight Simulator series of computer games, starting with Flight Simulator 1995. Flight Simulator utilized a real-time 3D rendering of terrain features with textures generated from a 34
variety of sources, including satellite imagery. The figure below illustrates a 3D perspective view generated in Flight Simulator 2000, which was actually released in late 1999:


## G. Mip-Maps

68. The provisional applications that the 343 Patent claims priority to described the use of "mip-maps" as "surface textures when rendering a twodimensional representation of a three-dimensional scene." See, e.g., Ex. 1009 at 7-
69. This mip-mapping technology, however, has been used for rendering surface textures since 1979, more than two decades before the filing date of the provisional applications to which the 343 Patent claims priority. App. L at 2, Lance Williams, Pyramidal Parametrics, Computer Graphics, vol. 17, no. 3, July 1983.
70. The term "mip" derives from the Latin phrase "multum in parvo" meaning "many things in a small place." The term was adopted by Lance Williams in his 1983 paper, which indicated that "the mip-mapping technology has been used successfully to bandlimit texture mapping . . . since 1979." Id. Mipmapping has been adopted in several versions of the OpenGL Standard prior to the filing date of the 343 Patent including OpenGL 1.1 released in March 1997 and OpenGL 1.2.1 released in April 1999. App. M, "Mipmapping" section of the OpenGL 1.1 Standard; ${ }^{1}$ App. T at 129-131. OpenGL (GL stands for "graphics library") is a 3D graphics standard originally designed and released by Silicon Graphics, Inc. of Mountain View, CA. As defined in OpenGL, a mipmap is "an ordered set of arrays representing the same image; each array has a resolution lower than the previous one. If the texture has dimensions $\mathbf{2}^{\mathbf{2}^{\mathbf{5}}} \mathbf{2}^{\mathbf{2 n}}$, then there are $\boldsymbol{\operatorname { m a x }}\{\mathrm{n}, m\}+1$ mipmap arrays. The first array is the original texture with

[^0]70. An illustration of the mipmap pyramid is shown below. See Photospector Blog, http://photospector.com/gigapixels/.

71. By the late 1990s, mipmaps were commonly used in 3D graphics applications, among other purposes, to render object textures at varying levels of detail based on the proximity of the object to the simulated viewpoint. For example, it would ordinarily be preferable to display an object in close proximity to the viewpoint at a high level of detail where the display is capable of showing a high
level of texture detail, whereas for more distant objects a lower level of resolution is preferable because the display screen is unlikely to be capable of displaying the highest-resolution texture at a great distance, and because lower-resolution textures require far less system resources and bandwidth to retrieve, load and render. U.S. Patent No. 5,760,783 to Migdal et al ("Migdal," App. BB) is a patent from Silicon Graphics which describes how mipmaps may be used to render textures- including satellite or aerial photographs used as terrain textures for large maps, such as a flight simulator application. App. BB, 9:5-17, 10:14-19. Migdal illustrates how mipmaps at higher levels of detail may be used for points closer to the viewpoint and lower levels of detail for more distant objects. For example, Fig. 4C of Migdal illustrates a perspective view of regions of three different level of detail maps aligned with a center line from an eyesight location:


FIG.4C
72. Migdal teaches that Fig. 4C illustrates that the clip-map "contains sufficient texel data to cover larger minified areas in the background of a display where coarser texture detail is appropriate." App. BB at 10:3-5. In my opinion, this teaching of Migdal is representative of what was already well-known in the art long before the earliest priority date claimed by the ' 343 Patent: that 3D graphics applications could "mipmaps" or similar level-of-detail pyramids, to render objects closer to the viewpoint at a higher resolution and objects more distant from the viewpoint at a lower resolution.
73. Fuller (App. E) also illustrates this principle of using mipmaps to display closer objects at higher resolution and more distant objects at lower resolution. Fuller describes an online system for 2D and 3D visualization of map
data, which creates a 3D perspective representation of a landscape using a digital elevation model (DEM), then uses mipmaps of aerial images as the textures. App. E, Fig. 4:


Figure 4. Mapping an ortho-image onto its digital elevation model. (Source: SRI International)
74. Fig. 3 of Fuller shows that higher resolution images are mapped onto portions of the terrain nearest the viewer, while lower resolution images are mapped onto more distant portions of the terrain:


Figure 3. Relationship between tile resolutions and perspective view.
(Source: SRI International)

## H. Progressive Meshes

75. Although not discussed in the 343 Patent or the priority applications to which it claims priority, the concept of a "progressive mesh" was also wellknown several years before the earliest claimed priority date of the 343 Patent. Microsoft performed much of the pioneering work in this area of computer graphics and employed the technique to render terrain and other objects (e.g. aircraft) in its popular Flight Simulator series of computer games. The use of such progressive meshes is described in detail in Hughes Hoppe's 1996 paper "Progressive Meshes," (App. N), which was published in the SIGGRAPH '96: Proceedings of the 23 rd annual conference on computer graphics and interactive techniques, pp. 99-108, and is also available online at http://research.microsoft.com/en-us/um/people/hoppe/pm.pdf. A "mesh" as used in this context is a polygonal approximation of a three-dimensional object.

# DECLARATION OF DR. WILLIAM R. MICHALSON IN SUPPORT OF PETITION FOR INTER PARTES REVIEW OF U.S. PATENT NO. 7,908,343 B2 

76. Hoppe's paper teaches that in order to improve rendering performance, it is common to define several versions of a model at various levels of detail. In the context of a mesh, different levels of detail generally refer to the number of vertices stored within a given area. The resolution of a mesh may be progressively enhanced (e.g. as an object in a 3D environment moves closer to the viewpoint) by progressively adding additional vertices and "splitting" the vertices to divide the object into a larger number of polygons, providing more detail in the representation. Conversely, the level of detail may be progressively reduced (e.g. as an object gets farther away from the viewpoint) by "collapsing" polygons by removing vertices and condensing multiple polygons into a smaller number. For example, Fig. 5 of Hoppe illustrates how an 3D model of an aircraft may be represented at varying levels of detail by a greater or smaller number of vertices and connecting polygons:


## VII. OVERVIEW OF THE 343 PATENT

77. The 343 Patent describes "[d]ynamic visualization of image data provided through a network communications channel." Ex. 1001 at Abstract.
78. The "Background of the Invention" section of the 343 Patent describes a "well recognized problem" of how to reduce the latency for transmitting full resolution images over the Internet on an "as needed" basis, particularly for "complex images" such as "geographic, topographic, and other highly detailed maps." Ex. 1001 at 1:34-51. The 343 Patent states that solutions already in existence included "transmitting the image in highly compressed formats that support progressive resolution build-up of the image within the current client field of view." Id. at 1:51-61. The 343 Patent also states that such "conventional" solutions, like the ones described in U.S. Pat. Nos. 4,698,689 (Tzou) and 6,182,114 (Yap), usually "presume that client systems have an excess of computing performance, memory and storage" and are "generally unworkable for smaller, often dedicated or embedded" clients. Id. at 1:51-2:58. According to the 343 Patent, the conventional solutions do not work well under "limited network bandwidth" situations. Id. at 3:7-31.
79. To address these perceived issues in the existing art, the 343 Patent discloses a system capable of "optimally presenting image data on client systems
with potentially limited processing performance, resources, and communications bandwidth." Id. at 3:40-43.
80. Specifically, the 343 Patent describes an image distribution system having a network image server and a client system, where a client can input navigational command to adjust a 3D viewing frustum for the image displayed on the client system. Id. at 5:24-53. High-resolution source image data is preprocessed by the image server into a series $\mathrm{K}_{1-\mathrm{N}}$ of derivative images of

progressively lower image resolution. Id. at 5:54-6:6, Fig. 2. The source image is also subdivided into a regular array of 64 by 64 pixel resolution image parcels
(a.k.a. image tiles), and each image parcel may be compressed to fit into a single TCP/IP packet for faster transmission. Id. at 6:6-22; 7:26-46.
81. The client system in the 343 Patent has a "parcel request" subsystem to request image parcels from the server, a "control block" that directs the transfer

of received image parcels and overlay data to a local parcel data store. Id. at 6:42-
82. The control block also decompresses the image parcels and directs a "rendering engine" to render them. Id. at 6:63-65; Fig. 3.
83. When the viewing point is changed in response to a user navigation command, the control block "determines the ordered priority of image parcels to be requested from the server . . . to support the progressive rendering of the displayed image." Id. at 7:17-20. A number of image parcel requests are then placed in a request queue, to be issued by the parcel request subsystem according to each 45
request's assigned request priority. Id. at 7:20-22; 8:20-32. Although various factors may affect the priority assigned to a parcel request, e.g., the "resolution of the client display" (8:50-67) or whether the image parcel is "outside of the viewing frustum" (9:26-29), generally speaking, "image parcels with lower resolution levels will accumulate greater priority values," so "a complete image of at least low resolution will be available for rendering" in a fast manner (10:6-14). In addition, the control parameter for calculating the priority can be set in a way that gives "higher priority for parcels covering areas near the focal point of the viewer" to make sure that image parcels are requested "based on the relative contribution of the image parcel data to the total display quality of the image." Id. at 10:15-33.
84. In the 343 Patent, after the needed parcels are requested and received, an algorithm is used to select the image parcel for rendering and display. Id. at 8:33-39. Overlay data may also be added to the display if its image coordinates matches the current image parcel location. Id. at 8:42-47. The 343 Patent discloses that two-dimensional image parcels are displayed in a three-dimensional space using projection transform. Id. at 5:44-53; 7:8-16; 8:33-37; 10:15-21; 10:57-61. In my opinion, there is no disclosure in the specification of the 343 Patent that teaches or suggests that the images displayed are mapped onto an elevation model, as there is neither an independent description of such a method or any reference to the
existing prior art that already had this feature, as I discussed above. The 343 Patent specification suggests that an overlay may include 3D objects (Id. at 5:60-65), but this disclosure by itself does not support any teaching that the "satellite imagery" discussed is warped to fit on a three-dimensional elevation model. The specification of the 343 Patent effectively discloses a view that is "threedimensional" in the sense that it generates a viewing perspective that contains position, rotation, and height components, but operating over a flat plane of terrain imagery. Id. at 5:47-50.
85. The 343 Patent states that its disclosed technology can achieve faster image transfer by (1) dividing the source image into parcels/tiles, (id. at 6:1-16), (2) processing the parcels/tiles into a series of progressively lower resolution parcels/tiles, (id.) and (3) requesting and transmitting the parcels/tiles needed for a particular viewpoint in a priority order, generally lower-resolution tiles first. Id. 3:40-4:41.
86. As shown in this Declaration, all of the features and combinations in Claims 1-20 were known prior to the 343 Patent's earliest priority date, which should be no earlier than Dec. 27, 2000.
87. I cite and rely on references dated before October 1999.

## VIII. IDENTIFICATION OF THE PRIOR ART AND SUMMARY OF OPINIONS

87. As explained below, it is my opinion that the prior art references cited in this Declaration disclose all technical features in Claims 1-20 of the 343 Patent, thus rendering them unpatentable.
88. Based on my review of the prior art references, claims 1-9, 13 and 1719 of the 343 Patent are rendered obvious by Potmesil in view of Hornbacker and claims 10-12, 14-16 and 20 of the 343 Patent are rendered obvious by Potmesil in view of Hornbacker further in view of Lindstrom; claims 1, 2, 4-11 and 13-19 are rendered obvious over Ligtenberg in view of Rutledge and Cooper, claim 3 is rendered obvious over Ligtenberg in view of Rutledge, Cooper, and Hassan, and claims 12 and 20 are rendered obvious by Rutledge in view of Ligtenberg, Cooper, Migdal and Austreng.
89. In addition, it is my opinion that claims 1-11 and 13-19 of the 343

Patent are rendered obvious on four additional grounds: (1) The MAGIC Project:
From Vision to Reality, Barbara Fuller \& Ira Richer, IEEE Network, May/June 1996 ("Fuller") in view of Hornbacker; (2) U.S. Pat. No. 6,182,114 to Chee K. Yap et al. ("Yap") in view of Visualization of Large Terrains in Resource-Limited Computing Environments, Boris Rabinovich and Craig Gotsman ("Rabinovich") IEEE Computer Society Technical Committee on Computer Graphics' Proceedings

Visualization '97, October 19-24, 1997 ("Rabinovich," App. R.); (3) Fuller in view of Yap; and (4) Potmesil in view of Hornbacker and Cooper. In addition, it is my opinion that claims 12 and 20 of the 343 Patent are rendered obvious on three additional grounds: (1) Fuller in view of Hornbacker and further in view of U.S. Patent No. 5,818,469 to John Joseph Lawless et al. ("Lawless", App. CC), (2) Yap in view of Rabinovich; and (3) Fuller in view of Yap.

## IX. CLAIM CONSTRUCTION

90. In conducting my analyses of the asserted claims of the 343 Patent, I have applied the legal understandings I set out below regarding claim constructions consistent with the "broadest reasonable interpretation" (BRI) standard described above, and offer them only for this Inter Partes Review. The claim constructions do not necessary reflect the appropriate claim constructions to be used in litigation proceedings, such as litigation in a district court, where a different standard applies.
91. I understand that, under the BRI claim construction, claim terms are given their ordinary and customary meaning as would be understood by one of ordinary skill in the art in the context of the entire disclosure. An inventor may rebut that presumption by providing a definition of the term in the specification with reasonable clarity, deliberateness, and precision. In the absence of such a definition, limitations are not to be read from the specification into the claims.
92. The proposed BRI claim construction for terms in claims 1-20 is plain and ordinary meaning of each term in light of the 343 Patent specification.

## X. UNPATENTABILITY OF THE 343 PATENT CLAIMS

## A. GROUND 1: CLAIMS 1-9, 13 AND 17-19 ARE UNPATENTABLE UNDER 35 U.S.C. § 103(a) AS BEING OBVIOUS OVER POTMESIL IN VIEW OF HORNBACKER

93. In my opinion, claims 1-9, 13 and 17-19 are disclosed and rendered obvious by Potmesil (Ex. 1002) in view of Hornbacker (Ex. 1003). Potmesil and Hornbacker were each published more than one year before the earliest claimed filing date for the '343 Patent. Therefore, both references are prior art as the law has been explained to me. These references collectively teach all features of claims 1-9, 13 and 17-19.
94. Potmesil and Hornbacker provide related, contemporary teachings about the state of the art in 2D and 3D visualization of large image data sets such as maps that give examples of reasons why the claims of the 343 Patent cover technology that was already well-known to those of skill in the art. Potmesil teaches a client-server system utilizing plug-ins for standard web browsers to request various types of map information organized into tiles in a power-of-two pyramid, sort and cache the tiles based on factors such as level of detail and proximity to the user's viewpoint, and render the map information in two or three
dimensions on a client device. Hornbacker teaches a system for retrieving portions of very large documents over a network on a client device, utilizing power-of-two tile pyramids with a specific structure for requesting tiles based on resolution and location. Hornbacker further teaches several well-known techniques for implementing such a system on a common client device with a limited bandwidth connection, such as fixed compression ratios and progressive resolution enhancement. I discuss each of these references in more detail below.
95. In my opinion, Potmesil and Hornbacker are each directed to substantially similar problems to the 343 Patent and to each other, i.e. downloading and displaying large images on devices over limited bandwidth connections, and the teachings of these two references illustrate that claims 1-9, 13 and 17-19 of the 343 Patent do no more than articulate the use of known features in the art according to their known purposes.

## 1. Overview of Potmesil and Hornbacker

96. Potmesil is a 1997 paper published in Computer Networks and ISDN systems by Michal Potmesil of Bell Laboratories. Potmesil's paper describes an teaches an online, multi-component system for utilizing the worldwide web (WWW) to view a variety of geographic information using 2D or 3D map browsers and Hypertext Transfer Protocol (HTTP) protocol. The system described
in Potmesil includes both client-side technology (i.e., the software operating on a client computer that would enable a user to request various types of mapping information and imagery from a server) and the server-side technology that would store and retrieve that geographic information. The system of Potmesil is designed to be flexible in multiple ways. The client-side system includes browser features that are designed to operate on a wide variety of platforms, including (among other devices) NC's (which I understand to mean "notebook computers,"), ITV's (which I understand to mean either "Interactive TVs" or "Internet TVs," both of which are terms for televisions that include built-in computing capability), cellular phones, and heads-up displays on car windshields. Ex. 1002 at 1328. The browser that operates on the client uses a variety of small application programs, called mapplets, including mapplets for images (e.g. GIFs), geographical names, lines and polygons, spatial bulletin board information, weather, 3D browsing, etc. which also share certain common processes such as tile caching and rendering. Id. at 1332-40, that includes map servers and software operating on a client computer, and that allows users to view geographic information over the worldwide web (WWW) Ex. 1002 at Abstract. The server-side system described in Potmesil is also designed to be flexible because it anticipates that a digital map or a 3D geographical model may be distributed over many independent sources, which the system addresses by
designing a server that can perform image processing on tiles received from multiple sources to align them to the same tile scheme and coordinate system. Ex. 1002 at 1329-30.
97. A key feature of Potmesil on both the client and server sides is the use of image tiles containing information such as aerial images and elevation data, stored in a power-of-two pyramid. Potmesil teaches the use of power-of-two pyramids both for images and for geometrical elements such as points, lines, and polygons, for which they are referred to as "quadtrees." Id. at 1332. Potmesil refers to much of the same background work on the use of power-of-two pyramids or "mip-maps" and the OpenGL rendering standard that I discussed earlier in this declaration, and it is my opinion that a person of ordinary skill in the art would read Potmesil with that background in mind, including known features of mipmaps such as the ability to optimize the display resolution of an image texture displayed in a three-dimensional space. Ex. 1002 at 1329. The system described in Potmesil includes a "tile server" which stores images such as aerial images and elevation data in a power-of-two pyramid to allow fast access and scroll and zoom operations. Id. at Fig. 1, 1329-30. The tile server may also perform operations such as reformatting tiles to align them with other tiles stored in the server, resampling
tiles to the same coordinate system, watermarking, and tile compression. Id. at 1330.
98. One component of the browser used by Potmesil, which is shared by the various "mapplets" that work in concert, is a tile caching process, described at pp. 1332-33 of Ex. 1002. The tile caching process receives information about the current view from the "compositing process," which is responsible for the final display of a view, determines what tiles are necessary either to properly render that view or what tiles may be needed in the near future, sorts the tiles that may be needed by order of priority, requests the tiles from the server, places the received tiles in a cache, and deletes tiles less likely to be needed when the cache is full. Id. For example, in a "flight simulator" mode, the 3D browser requests and caches tiles from the flight path ahead of the user's simulated viewpoint. Ex. 1002 at 1332-33, Fig. 2. Potmesil teaches that the factors considered in cache allocation include location ( $\mathrm{x}, \mathrm{y}, \mathrm{z}$ ), level of detail, and time. Id. at 1332. In my opinion, a person of ordinary skill in the art would understand that this disclosure means that in the 2D or 3D browser modes, the cache allocation algorithm of Potmesil determines what tiles are either currently needed or may be needed for a given 2D or 3D view by taking into account the distance from the viewpoint in three dimensions as well as the optimal level of detail for displaying a particular image.

Id. Potmesil also explicitly discloses that the caching process sorts tiles that may be needed based on their distance from the user and determines how many of them can be loaded into the cache. Id. Image tiles may be compressed using a variety of formats such as JPEG or GIF. Id. at 1334-35.
99. Hornbacker teaches a method and a system for displaying portions of very large images (such as digital documents) retrieved over a network from a server. The system described in Hornbacker includes a web server networked to client workstations, which use a web browser on the workstation to request image views by means of Uniform Resource Locator (URL) code using the HTTP protocol. Ex. 1003 at 5:3-8, 5:16-25. Hornbacker provides several relevant details that further explain the implementation of the process of requesting and transmitting tiles. Potmesil teaches that the documents are divided into 128X128 pixel view tiles, which are further organized into a hierarchy of tiles at differing resolutions spaced by factors of two.
100. Hornbacker explains that tiles may be compressed at a ratio of $4: 1$ using GIF compression, which yields a data size for a view tile of approximately 512 bytes. Id. at 6:26-28. Hornbacker teaches the use of the TCP/IP protocol, which relies on packet transmission, and further explains a reason why a person of ordinary skill in the art would choose to design a system of this type such that
individual view tiles are transmitted as individual packets. Specifically, Hornbacker teaches that the view tile size is optimized to avoid the increase of "network transaction overhead... with smaller view tiles since each of the view tiles requires a network transaction." Id., 8:13-14. In my opinion, this disclosure suggests that the "network transactions" referenced are packet transmissions, and this teaching would suggest to a person of ordinary skill in the art that splitting tile information into too many packets would excessively increase the "overhead," or that amount of bandwidth taken up by the header information for packets.
101. Hornbacker further explains that individual tiles may be located using a URL code which specifically identifies the tiles based on factors including the source image, scale, location of the tile in X and Y dimensions, view rotation angle, etc. Id. at 8:30-10:2.

## 2. Motivation to Combine Potmesil and Hornbacker.

102. It is my opinion that a person of ordinary skill in the art would be motivated to combine teachings in Potmesil and teachings in Hornbacker because they both address the common technical issues in visualizing large amounts of data obtained over a data network as such the Web via HTTP protocol, using a client viewing device with much smaller memory than the database which stores the imagery data. Both Potmesil and Hornbacker address similar or the same technical
problems in rendering the images on the client device from image data received over a data network (e.g. optimizing bandwidth, prioritizing use of bandwidth, determining which portions of a larger set of image data to request, etc.). The problem addressed by both references, at a very high level, is how to view portions of a very large remote image data set using a client device and a connection with limited bandwidth, where the user only needs to see some portion of the data at a given time but the resolution at which the user may need to see the data varies. Both references reach solutions to this problem which include the transmission of large images (e.g. maps) which are divided into arrays of tiles at various resolutions within a power-of-two pyramid. Accordingly, in my opinion, a person of ordinary skill in the art in late 2000 would have viewed Potmesil and Hornbacker as analogous art. Both references teach similar solutions to bandwidth issues, including dividing large references into tiles, further processing those tiles into a "pyramid" structure containing representations of those tiles at differing resolutions, caching algorithms to optimize which tiles are requested and stored, and compression of tiles. Therefore, a person of ordinary skill in the art faced with the technical difficulties presented by transmitting large images over a narrow communication bandwidth in the late 1990s would be motivated to combine the solutions described in Potmesil and Hornbacker.
103. In addition, a person of ordinary skill in the art would be motivated to combine Potmesil and Hornbacker because both of them are applicable to mapping related applications. Potmesil specifically discloses uses of its technology in terrain visualization applications and map applications. The teachings of Hornbacker are readily applicable to online mapping references too because online maps represent a scenario in which a much larger amount of geographically organized imagery must be stored on a server than can be stored at one time on a client.
104. In fact, a related Hornbacker application specifically recognized the applicability of its teachings to mapping technology. Besides the PCT publication, Hornbacker's patent application has also been published as an European Patent Specification, EP1070290. This European counterpart of Hornbacker specifically recognizes the relevance of teachings relating to mapping to the disclosure of Hornbacker by citing and explaining several online mapping references, including Potmesil, in the description of the prior art. Ex. 1011 at [0006], [0007]
("POTMESIL M.: "Maps Alive: viewing geospatial information on the WWW", Computer Networks and ISDN Systems 29 (1997) 1327-1342 discloses a WWWbased system for viewing geospatial information. The system comprises a 2D map browser capable of continuous scroll and zoom of an arbitrarily large sheet, which downloads and caches geographical information, geometrical models and URL
anchors in small regions called tiles."). Accordingly a person of ordinary skill in the art would be motivated to consider the teachings of both references in designing a mapping application designed to view map data over a limited bandwidth communications channel. While Potmesil teaches both 2D and 3D map implementations, a person of ordinary skill in the art would recognize that the technical challenges involved in online display of 2D and 3D maps overlap in issues such as how to best request and obtain image data for display and how to optimize the use of the cache memory at the client. In my opinion, a person of ordinary skill in the art would recognize that the teachings of Hornbacker would be advantageous in addressing the technical challenges of displaying either a 2 D or a 3D image.
105. In the following sections, I will discuss other specific reasons or motivations that would cause a person of ordinary skill in the art to combine Potmesil and Hornbacker when analyzing these two references in connection with claim elements of claims 1-11 and 13-19 of the 343 Patent.

## 3. Claim $\mathbf{1}$ is Rendered Obvious by Potmesil and Hornbacker

106. Element 1.Preamble A method of retrieving large-scale images over network communications channels for display on a limited communication bandwidth computer device, said method comprising: In my opinion, the preamble
of this claim is disclosed by both Potmesil and Hornbacker. Potmesil and Hornbacker both teach computer systems that perform all elements of the claimed method. Potmesil teaches "a WWW-based system - consisting of browsers, servers and connecting protocols - which allows users to view, search and post geographically-indexed information of the Earth." Ex. 1002 at Abstract. Potmesil notes that one of its purposes is to enable users to access "very large databases of geographical information itself, such as terrain elevation, satellite and aerial images, detailed street maps and geometrical models of buildings..." (id. at 132728), and provides examples of large databases which include "the well-known Xerox PARC map server which contains data from the DMA's Digital Chart of the World and the USGS's 1:2,000,000 Digital Line Graph, (2) the U.S. Bureau of the Census TIGER street map server, and (3) the multi-resolution Mars image server at the Los Alamos National Laboratory." Id. at 1335. In my opinion, Potmesil teaches the use of a client to view portions of very large images, particularly map data, which is stored on a server. The entire purpose of retrieving such information is to view it on the device using a web browser program. Id., Abstract.
107. Hornbacker likewise teaches that the invention "relates to workstation viewing images of digital documents stored on a network server and in particular
to viewing large digital document images using a client-server architecture." Ex. 1003 at 2:11-13.
108. Both Potmesil and Hornbacker teach that the system may be used on small portable devices, such as notebook computers (NCs) and cellular phones in Potmesil and notebook computers, palm-top computers, and Web television adapters in Hornbacker. Hornbacker also notes that the system may be used to retrieve data over a communication channel such as a 28.8 kbaud modem. Ex. 1002 at 1328, Ex. 1003 at 13:28-14:11, 14:26-28. Therefore, in my opinion, while the term "limited communication bandwidth computer device" is somewhat vague, both of these references appear to have similar teachings to the corresponding disclosure in the specification of the 343 Patent, which refers to PDAs (Personal Digital Assistants, also known as palm-top devices) and webphones. Ex. 1001 at 3:14-16, 5:33, 10:31-33. Further, in my opinion, both Potmesil and Hornbacker contain extensive teachings focused on the goal of reducing the bandwidth necessary to view large images on a client device. For example, both Potmesil and Hornbacker teach the use of compression.
109. Element 1.A issuing, from a limited communication bandwidth computer device to a remote computer, a request for an update data parcel; In my opinion, this claim element is disclosed by both Potmesil and Hornbacker.
110. I previously explained in regard to the preamble why both Potmesil and Hornbacker teach or suggest "limited communication bandwidth computer devices."
111. Potmesil discusses the "tile caching" process, which requests specified tiles based on the current view and other factors such as anticipated direction of travel, at length. Ex. 1002 at Abstract, 1327, 1328, 1329-30, 1332-33, 1334-35, Fig. 2. As I previously discussed, Potmesil relies on the sale prefiltered power-of-two image or "mip-map" concept utilized in the specification and provisional application of the 343 Patent. Hornbacker teaches that tiles within a large database may be located by requests over a server which use URLs to identify the specific tile by incorporating identifying characteristics such as resolution, location, view angle, etc. See, e.g. Ex. 1003, Abstract, 3:10-27, 5:16-25, 6:13-19, 7:26-8:6, 8:30-9:28, 10:24-28, 12:24-13:10. Therefore, in my view, the "update data parcel" element is met by the image tiles requested by both Potmesil and Hornbacker.
112. Potmesil and Hornbacker identify a common problem with the display of portions of very large images over a network, which is the latency and bandwidth consumption associated with downloading an entire image, and arrive at similar solutions in the form of requests for specific tiles in a priority order based
on how soon the tiles need to be displayed. In my opinion, a person of ordinary skill in the art would consider the teachings of both references when attempting to design a system addressing these problems. Hornbacker provides further implementation details (such as fixed ratio compression and a URL syntax for identifying specific needed tiles) that complement and could be used to further refile the tile request process described by Potmesil. Therefore, in my opinion, this element would be obvious to a person of ordinary skill in the art.
113. Element 1.B wherein the update data parcel is selected based on an operator controlled image viewpoint on the computer device relative to a predetermined image; Potmesil teaches a three-dimensional terrain visualization application which renders views of terrain based on user navigational commands: Ex. 1002 at Abstract, 1328-29, 1332-33, Fig. 2, 1340-41, Fig.8. The imagery is persistently stored on the server before the user decides to access it, so in my opinion the imagery stored on the server is "a predetermined image" as required by the language of this claim element. Potmesil teaches that tiles are requested and cached based on parameters including $\mathrm{x}, \mathrm{y}, \mathrm{z}$, level-of-detail, and time. Ex. 1002 at 1332. The images are prioritized by proximity to the user viewpoint; for example, in the "flight simulator" scenario, the browser requests tiles in a "widening wedge" in front of the direction of flight; in other words, it first requests those tiles in the
current view or very likely to be needed soon as the highest priority, then requests other tiles that may be needed in the future. Id. at 1332-33. See also id. at 1327, 1334-35. In my opinion, these teachings would indicate to a person of ordinary skill in the art that the tiles (update data parcels) are selected based on the operator controlled image viewpoint relative to the predetermined image.

## 114. Element 1.C the update data parcel contains data that is used to

 generate a display on the limited communication bandwidth computer device; In my opinion, both Potmesil and Hornbacker contain straightforward teachings that the data tiles contain data used to generate a display on the client device. Potmesil teaches that retrieved data tiles, which may include data such as elevation profiles and RGB or monochrome images, are compiled and rendered by a 2 D or 3 D browser which includes a tile caching process and a tile compositing process. Ex. 1002 at Abstract, 1328, 1332, 1333-35, 1340. Hornbacker also teaches a system that uses image data tiles retrieved over the internet to form an image on the browser at the client device. Ex. 1003 at Abstract.115. Element 1.D processing, on the remote computer, source image data to obtain a series $\mathrm{K}_{1-N}$ of derivative images of progressively lower image resolution; In my opinion, both Potmesil and Hornbacker teach this element because both references teach that the server systems for providing imagery may
process source image data into a grid of tiles organized into a hierarchy of different resolution levels. In the system of Potmesil, this processing occurs on the server side and may occur either in advance or at the time tiles are needed. For example, Potmesil notes that the tile server data is "obtained by sampling on a 2D grid" and is "stored in a power-of-two pyramid." Additionally, tiles may undergo further processing in response to a request for tiles, e.g. to reformat or resample the tile to match the desired coordinate system. Ex. 1002 at Abstract, 1329-30, 1332, 1335, Fig. 1. Hornbacker also discloses that view tiles are generated at the server by an image tiling routine that divides a given image into a grid of smaller images, which are further computed for distinct resolutions. The view tiles may either be preprocessed at the server (pre-cached) or newly computed in response to a request. Ex. 1003 at 3:22-27, 5:3-8, 5:16-6:19, 6:20-7:25, 8:30-9:28, 10:3-10, 11:19-28, 12:21-13:10, 13:26-14:6. In my opinion, both references address similar technical issues with a similar technical approach of dividing large high-resolution source image data sets into a pyramid of tiles having different resolutions at each level.
116. I understand the phrase "series $\mathrm{K}_{1-\mathrm{N}}$ of derivative images of progressively lower resolution" to mean that there is a source image, followed by a series of layers of tiles in which the source image has been divided into a derivative layer of tiles at lower resolution. For example, at layer $\mathrm{K}_{\mathrm{N}+1}$, there will
be $1 / 4$ as many tiles as there are at layer $K_{N}$, each tile having half the resolution of layer $\mathrm{K}_{\mathrm{N}}$. In other words, layer $\mathrm{K}_{\mathrm{N}+1}$ is a derivative of layer $\mathrm{K}_{\mathrm{N}}$ in which every tile in layer $\mathrm{K}_{\mathrm{N}+1}$ is the result of combining an array of four adjacent $\mathrm{K}_{\mathrm{N}}$ tiles at lower resolution. This system corresponds with the teachings of Potmesil and Hornbacker, and is illustrated by Fig. 1 of Potmesil.
117. Element 1.E wherein series image $\mathrm{K}_{0}$ being subdivided into a regular array; In my opinion, Potmesil and Hornbacker both teach this element in a similar manner. Potmesil teaches a pyramid tile structure in which the highresolution base image is an array of tiles, each containing an array of pixel data, and the whole image database is subdivided into tiles related by powers-of-two. Ex. 1002, Fig. 1, 1329-30, 1332. Hornbacker teaches that view tiles are generated by an image tiling routine which divides a source image into an array of 128 X 128 pixel tiles at varying resolutions. Ex. 1003, 6:13-19, 7:11-15, 8:30-9:28, 10:7-10. Therefore, both of these references teach that source data, including $\mathrm{K}_{0}$ which is just the "base" of the pyramid from which the lower resolution tiles are divided, is divided into a regular array.
118. Element 1.F wherein each resulting image parcel of the array has a predetermined pixel resolution; In my opinion, Potmesil and Hornbacker both teach this element in a similar manner. Potmesil and Hornbacker both teach
the use of image tiles having a fixed resolution for each tile, including a multiresolution "pyramid" tile structure where each level includes tiles at a fixed resolution. Ex. 1002 at Fig. 1, 1329-30, 1332; Ex. 1003 at 6:20-7:25, 8:30-9:28, 10:3-10, 11:19-28, 12:21-13:10, 13:26-14:6.
119. Element 1.G wherein image data has a color or bit per pixel depth representing a data parcel size of a predetermined number of bytes; In my opinion, this element is obvious over Potmesil in view of Hornbacker. Potmesil teaches that the system described therein may be adapted for a range of fixed color or bit per pixel depths (e.g. 24/32 or 8 bits deep). Ex. 1002 at 1334-35. Potmesil also teaches that the tiles in the pyramid are of a fixed size (with the exception of certain tiles along the edge of the data set). Id. at 1329-30. When the tiles are the same size and have a set bit per pixel depth, a person of ordinary skill in the art would expect the resulting tile to have approximately the same size. Additionally, it was well-known in the art at the time that image formats such as JPEG, PNG, and GIF, mentioned in Potmesil and Hornbacker, typically use a fixed bit per pixel depth (e.g. 8 bits), which result in a fixed size for an image parcel of a fixed number of pixels (e.g. 128 pixels). Id., Ex. 1003 at 6:20-7:3.
120. Element 1.H resolution of the series $\mathrm{K}_{\underline{1-N}}$ of derivative images
being related to that of the source image data or predecessor image in the series by
a factor of two; In my opinion, Potmesil and Hornbacker both teach that the image tile servers store image data tiles in fixed-size power-of-two arrays. This means that the difference in resolution between each adjacent layer (i.e. between the source image and the first derivative layer of tiles, or between a layer of tiles at a higher resolution and the next lower resolution later of tiles) is a factor of two. Ex. 1002, Fig. 1, p. 1329-30, 1332. Ex. 1003 at 6:13-7:25, 8:7-15.
121. Element 1.I said array subdivision being related by a factor of two; As I explained in regard to element 1.H, Potmesil and Hornbacker both teach image data tiles storing data in fixed-size power-of-two arrays, meaning that each subsequent subdivision of the array is related by a factor of two. Ex. 1002, Fig. 1, p. 1329-30, 1332. Ex. 1003 at 6:13-7:25, 8:7-15.
122. Element 1.J such that each image parcel being of a fixed byte size; In my opinion, this element is obvious over Potmesil in view of Hornbacker. Potmesil teaches that tiles may be transmitted and received in a compressed form such as JPEG or GIF. Ex. 1002, Fig. 1, p. 1329-30, 1334-35. Hornbacker teaches that the view tiles preferably use GIF image files with a $4: 1$ compression ratio, Ex. 1003 at 6:20-7:3, that tiles may have a raw image data size of 2,048 bytes and a compressed size of 512 bytes, $i d$. at 6:26-28, and that such compression reduces the transfer time and demand on the network, id. at 14:2-16. Hornbacker further
teaches that fixed size view tiling is beneficial because it allows more effective use of the caching mechanism. Id. at 7:14-15.
123. In my opinion, the teachings of fixed compression ratios in Hornbacker, such as with GIF compression, further elaborate the benefits of the compression taught by Potmesil. Using a fixed size and fixed compression ratio could improve predictability of the system because the caching process would always need to use the same amount of space for a particular tile in the cache, which makes the caching process more straightforward. An analogy would be stacking cubic boxes of the same size in a room, compared with stacking boxes of all different sizes and shapes.
124. Potmesil and Hornbacker are both directed to related problems involving viewing portions of very large image data sets over a network, and reach similar solutions involving the use of image tiles at a hierarchy of resolutions to convey image data in discrete parcels. The need to conserve bandwidth when transmitting large amounts of data, particularly with a large online data set, was a well-known issue at the time, and image compression such as GIF or JPEG was a known solution. In my opinion, Potmesil and Hornbacker both teach this same known solution. Additionally, a person of skill in the art would recognize that the use of a standard compression format such as GIF, JPEG, or PNG would enable
the system to operate across common browsers on a wide variety of devices because these formats were and are common and frequently used in web browser applications. In my opinion, a person of ordinary skill in the art would recognize that the fixed compression ratio of Hornbacker would speed up download and reduce the bandwidth necessary in the system of Potmesil, which would be particularly useful in the mobile applications envisioned by both references.
125. Element 1.K wherein the processing further comprises compressing each data parcel; as I discussed above in regard to claim element 1.J, both Potmesil and Hornbacker teach compression of image tiles. In my opinion, a person of ordinary skill in the art would be motivated to combine these teachings for the same reasons that I discussed previously.
126. Element 1.L storing each data parcel on the remote computer in a file of defined configuration such that a data parcel can be located by specification of a $K_{D}, \mathrm{X}, \mathrm{Y}$ value that represents the data set resolution index D and corresponding image array coordinate; In my opinion, this element is disclosed and obvious over Potmesil in view of Hornbacker. Potmesil teaches that image tiles are stored on the server in a geographical array and that image tiles are may be requested and cached based on their coordinates and resolution, e.g. $x, y, z$, and level-of-detail. Ex. 1002, Abstract, Figs. 1-2, 1328, 1329-30, 1332. From this
disclosure, it is apparent that the tile caching algorithm would preferably be able to obtain tiles by identifying their location (X, Y) and the level-of-detail layer that they belong to in the pyramid. This corresponds to the $\mathrm{K}_{\mathrm{D}}$ and $\mathrm{X}, \mathrm{Y}$ value recited in the claim. Hornbacker provides further teachings that tiles stored on the server may be located and requested by providing requests in URL format specifying the zoom level and x , y coordinates of the tile. Ex. 1003 at 3:17-21, 5:16-24, 8:16-23, 8:3010:6, 10:24-28. Although a person of ordinary skill in the art would recognize that Potmesil teaches a tile caching algorithm that requests tiles based on the level of detail and image array coordinates, Hornbacker provides further amplifying details how straightforward HTML code can be used to identify a particular needed tile based on its resolution/zoom level and coordinates. The use of HTML code to request tiles is advantageous because it enables the system to operate in common web browsers over the internet. In my opinion, both Potmesil and Hornbacker teach that tiles are stored on the server "in a file of defined configuration" because they are stored in arrays having a defined format, which enables the client device to more easily locate and request tiles.

## 127. Element 1.M receiving said update data parcel from the data

 parcel stored in the remote computer over a communications channel; In my opinion, Potmesil and Hornbacker provide independent teachings that a plurality ofimage tiles are received over a network from a remote computer which stores the tiles. Ex. 1002 at Abstract, 1328, 1329-30, 1332-33, 1334-35, 1340-41. Ex. 1003 at Abstract, 3:10-27, 5:3-6:19, 8:16-23, 10:13-28, 11:29-12:9, 12:17-23, 13:19-23.

## 128. Element 1.N displaying on the limited communication

 bandwidth computer device using the update data parcel that is a part of said predetermined image, an image wherein said update data parcel uniquely forms a discrete portion of said predetermined image. In my opinion, this element is disclosed by and obvious in view of Potmesil and Hornbacker. One purpose of both Potmesil and Hornbacker is to download large images (or portions thereof) for display, and both references accordingly teach that the downloaded data tiles may be used to render the associated imagery for display. Potmesil teaches that the image tiles downloaded by the client from the tile server may include elevations, gradients, and RGB or color images, and that the tiles may be rendered as the corresponding portions of a 2D or 3D model. Ex. 1002 at Abstract, 1327-28, 132930, 1334-35, 1340-41, Fig. 1, Fig. 8. Hornbacker teaches that a large-scale image is broken up into tiles, which when displayed are rendered within the view area as the unique corresponding portions of the image at a particular resolution. 6:7-19, 7:1125, 8:7-15. In my opinion, a person of ordinary skill in the art would recognize that both references contain similar teachings, because they both relate to thedownloading of tiles that contain imagery representing a portion of a larger image (i.e. "a discrete portion of said predetermined image").

## 4. Claims 2-9 are Rendered Obvious by Potmesil and Hornbacker

129. Claim 2. The method of claim 1, wherein the update data parcel further comprises one of an image parcel textual mapping, a map parcel, a navigation cue, a text overlay and a topography. Potmesil teaches that the image tiles comprise mapping data which may further include satellite and aerial images, topographical data, and geographically linked text. Ex. 1002 at Abstract, 1329, 1330-31, 1334-35, Figs. 3-5. Therefore, in my opinion, this element is disclosed by Potmesil.
130. Claim 3. The method of claim 1, wherein the limited communication bandwidth computer device further comprises one of a mobile computer system, a cellular computer system, an embedded computer system, a handheld computer system, a personal digital assistants and an internet-capable digital phone; Potmesil teaches that the system described therein is intended for use in a variety of computing device including notebook computers (NCs), cellular phones, Internet TVs (ITVs), and automotive displays. Ex. 1002 at 1328. Hornbacker teaches that the graphical web browser is available to operate on client
devices such as palm-top computers. Ex. 1003 at 14:26-28. Therefore, in my opinion, both Potmesil and Hornbacker teach this element.
131. Claim 4. The method of claim 1, wherein the predetermined pixel resolution for each data parcel is a power of 2. As I previously discussed in regard to the teachings shown above for claim elements 1.F, 1.H, and 1.I of the 343 Patent, Potmesil and Fuller teach that tiles are stored in arrays of fixed pixel resolution where the resolution for each tile is a power of two.
132. Claim 5. The method of claim 4, wherein the predetermined pixel resolution is one of $32 \times 32,64 \times 64,128 \times 128$ and $256 \times 256$. As I discussed above in regard to claim 4, Potmesil teaches that the pixel resolution as discussed above is a power of two. In light of the teaching that the pixel resolution is a power of two, a person of ordinary skill in the art would recognize that there are a limited number of possible sizes for the tiles, including 32X32, 64X64, 128X128, and 256X256. Hornbacker further teaches specifically that the tiles may be 128X128 pixels, and that this size is chosen as a compromise between view tile granularity and view tile overhead. Ex. 1003 at 6:20, 7:4-10, 8:7-15, 14:2-6.
133. Claim 6. The method of claim 1 wherein said communications channel is a packetized communications channel and wherein said update data parcel is received from said packetized communications channel in one or more
data packets. In my opinion, this element is obvious over Potmesil, Hornbacker, and the knowledge of a person of ordinary skill in the art at the time. The TCP/IP protocol, which is a packetized data protocol, was ubiquitous by the time of the alleged invention, and common internet browsers all used TCP/IP. Since both Potmesil and Hornbacker teach systems designed to operate over the Internet or Worldwide Web, it would be obvious to a person of ordinary skill in the art that the system transmits data in packets. Hornbacker further explicitly references the TCP/IP packet transmission protocol. Ex. 1002, e.g. at Abstract, 1330, 1333-34; ex. 1003 at 4:30-5:2.
134. Claim 7. The method of claim 6 wherein the data packet contains an update image parcel as a compressed data representation of said discrete portion of said predetermined image. Potmesil teaches that image tiles may be transmitted in compressed form and are discrete representations of portions of a large image such as a map. Ex. 1002, Fig. 1, p. 1329-30, 1334-35. Hornbacker teaches that the view tiles preferably use GIF image files with a $4: 1$ compression ratio, Ex. 1003 at 6:20-7:3, that tiles may have a raw image data size of 2,048 bytes and a compressed size of 512 bytes, id. at 6:26-28, and that such compression reduces the transfer time and demand on the network, id. at 14:2-16. Hornbacker further teaches that fixed size view tiling is beneficial because it allows more effective use
of the caching mechanism. Id. at 7:14-15. For the reasons that I previously discussed above in regard to claim 1.J, a person of ordinary skill in the art would recognize that the fixed ratio compression of Hornbacker could be advantageously combined with the 2D and 3D browser of Potmesil. Hornbacker further teaches or suggests that each tile is transmitted as a single packet. For example, Hornbacker teaches that " $[t]$ he network transaction overhead increases with smaller view tiles since each of the view tiles requires a network transaction." Ex. 1003 at 8:13-14. In my opinion, since each TCP/IP packet requires a separate network transaction, a person of ordinary skill in the art would read this teaching to mean that tiles are transmitted as single packets.
135. Claim 8. The method of claim 7 wherein said data packet contains said update image parcel as a fixed compression ratio representation of said discrete portion of said predetermined image. As discussed above in regard to claim 7, Hornbacker teaches a fixed compression ratio and could be advantageously combined with the teachings of Potmesil for the same reasons. Further, because the tiles in both Potmesil and Hornbacker correspond to specific portions of the underlying image as I discussed in regard to claim element 1.N, each tile represents a "discrete portion of said predetermined image."
136. Claim 9. The method of claim 7, wherein said update image parcel contains pixel data in a fixed size array independent of the pixel resolution of said predetermined image. Potmesil teaches that the tiles stored by the tile server (and provided in response to update requests from the browser) are obtained by sampling on a 2D grid from multiple independent sources (examples of which are listed on pages 1331 and 1335 of Ex. 1002), and that the server may either reformat the tile if the requested tile is not aligned with the tiles stored in the server or resample the tile if the requested tile is not in the same coordinate system. Ex. 1002 at 1329-30. Potmesil further teaches that tiles in the data set are stored in a power-of-two pyramid and usually have the same size. Id. at 1329, Fig. 1. Therefore, it would be obvious to a person of ordinary skill in the art that the tiles in the power-of-two array are all the same size (i.e., the same number of pixels at each level of resolution) regardless of the resolution of the underlying image, and that the tile server system may resample tiles on a grid and adjust them to the appropriate scaling and coordinate independent of the resolution of the underlying image.

## 5. Claim 13 is Rendered Obvious by Potmesil and Hornbacker

137. Element 13.Preamble A display system for displaying a large-scale image retrieved over a limited bandwidth communications channel, said display
system comprising: The preamble of claim 13 is substantially similar to the preamble of claim 1 and therefore, is disclosed by the same teachings in the prior art as described in my earlier discussion. In my opinion, Potmesil and Hornbacker both discuss limited bandwidth communications devices that utilize limited communication bandwidth channels.
138. Element 13.A a display of defined screen resolution for displaying a defined image; Potmesil teaches a 2D or 3D browser for displaying a view on a client device. Ex. 1002 at 1332-33, Fig. 2, 1340-41, Fig. 8. Hornbacker teaches that the system may be preferably optimized for viewing tiles at a particular resolution, e.g. 200 pixels-per-inch (7:4-25) and that the window may have a typical view size of 896 by 512 pixels. 14:2-6, see also 11:19-28, 13:4-10. In my opinion, it would be obvious to a person of ordinary skill in the art that a digital display would necessarily have a finite resolution. It would further be obvious to a person of ordinary skill in the art that the rendering of images on that display would be limited by the resolution of the screen or the defined area of the screen, i.e., the predetermined resolution of the image display. In other words, Potmesil and Hornbacker, like the system described in the 343 Patent, generally teach software that is capable of operating on a generic client device including a display with a fixed resolution. For example, both LCD displays- which were
already widespread in various types of computing devices long before the asserted priority date of the 343 Patent- and cathode ray tube (CRT) displays would normally have an inherently limited resolution. In the case of an LCD display, the predetermined resolution is because there are a fixed number of separate liquid crystal cells that can be independently addressed, while the screen of a CRT display would be typically be divided into a fixed number of red, green, and blue phosphors. My understanding of the "display" that a person of ordinary skill in the art would expect to use in combination with the systems of Potmesil and Hornbacker is consistent with the teachings of the 343 Patent, which recites in the background that "[c]haracteristically, the client system 18, 20 displays are operated at some fixed resolution generally dependent on the underlying display hardware of the client systems 18, 20." Ex. 1001 at 5:40-43.
139. Element 13.B a memory providing for the storage of a plurality of image parcels; Potmesil teaches that retrieved tiles may be stored in a cache on the geographic browser on the client both for immediate display of tiles and so that tiles covering adjacent areas likely to be used may be retrieved quickly if they are needed. Ex. 1002 at 1328, 1332-33, 1334. Hornbacker likewise teaches that retrieved tiles may be stored in a local cache. Ex. 1003, 6:1-19, 8:1-6, 8:16-23, 10:13-28, 11:29-12:9, 12:17-23, 13:19-23. Potmesil and Hornbacker both teach
that a local cache on a client display device is advantageous to enable rapid display of pre-cached tiles and minimize delays associated with downloading. In my opinion, it is readily apparent that a memory is required for these caching functions and both references teach similar solutions to similar problems.

## 140. Element 13.C displayable over respective portions of a mesh

 corresponding to said defined image; The support in the specification for the term "mesh" is not clear as the 343 Patent does not provide support for "progressive meshes" as Microsoft and others used the term in the late 1990s. While the term "mesh" is not used in the specification, Provisional Application No. 60/258,465 ("the '465 provisional") (Ex. 1010), refers to a "grid mesh" at 10:21, indicating that the terms "mesh" and "grid" are used synonymously, consistent with the prior references to a "grid." See also Ex. 1010 at 3:21-4:1, 6:4-11, and 10:20-24. Potmesil and Hornbacker each teach that imagery is displayable over a grid corresponding to the larger predefined image (e.g. the source map of Potmesil). Ex. 1002 at Fig. 1, 1328, 1332-35; Ex. 1003 at 6:13-19. Even if this term were interpreted to require a three-dimensional mesh of vertices and polygons (e.g. a polygon mesh) despite the lack of support in the specification, Potmesil teaches this claim element because it further teaches that the 3D model utilizes "quadtrees" for "geometrical elements such as points, lines, and polygons" and that thetechniques disclosed therein are applicable to other techniques such as Triangulated Irregular Networks and VRML models. Ex. 1002 at 1332.
141. Element 13.D a communications channel interface supporting the retrieval of a defined data parcel over a limited bandwidth communications channel; Potmesil teaches a client system for dynamic visualization of image data (through a terrain rendering program) which requests image data in the form of image tiles from a network server. Ex. 1002, Abstract. Hornbacker teaches a client system for dynamic visualization of image data (through an online image viewing program) which requests image data from a network server containing image tiles. Ex. 1003 at Abstract. In my opinion, since the purpose of both systems is to receive data over an internet connection, it is readily apparent that the client devices disclosed by both devices would require a communications channel (e.g. a modem or wireless connection to the Internet) to receive tiles. I previously discussed the "limited bandwidth communications channel" in regard to the preambles of claims 1 and 13, and the same teachings and discussion apply.

## 142. Element 13.E a processor coupled between said display, memory

 and communications channel interface; Both Potmesil and Hornbacker teach systems that are designed to utilize browser software operating on a client computing device. Ex. 1002 at 1328, Ex. 1003 at 5:3-21. In order to perform theclaimed functions, the device would require a processor. Further, because the claimed functions interact with each of the display (e.g. rendering the image on the display), the memory (e.g. caching tiles on the client) and the communications channel interface (e.g. sending requests for and receiving tiles from the server), in my opinion it is obvious that the client systems taught by Potmesil and Hornbacker would require a processor coupled between the display, memory, and communications channel interface.
143. Element 13.F said processor operative to select said defined data parcel, I previously described the process of selecting a defined data parcel above in regard to claim element 1.B. In my opinion, since both Potmesil and Hornbacker teach that this function is performed by a portion of the browser software that would necessarily execute on a processor, it is my opinion that both Potmesil and Hornbacker teach that the processor that I previously discussed in regard to claim element 13.E is operative to select the defined data parcel.
144. Element 13.G retrieve said defined data parcel via said limited bandwidth communications channel interface for storage in said memory; I discussed the retrieval of a data parcel over a limited communications channel above in regard to claim element 13.D, and it is my opinion that both Potmesil and Hornbacker teach that the retrieval of data parcels is controlled by a processor on
the client device. Potmesil teaches that retrieved tiles may be stored in a cache on the geographic browser on the client both for immediate display of tiles and so that tiles covering adjacent areas likely to be used may be retrieved quickly if they are needed. Ex. 1002 at 1328, 1332-33, 1334. Hornbacker likewise teaches that retrieved tiles may be stored in a local cache. Ex. 1003, 6:1-19, 8:1-6, 8:16-23, 10:13-28, 11:29-12:9, 12:17-23, 13:19-23. Potmesil and Hornbacker both teach that a local cache on a client display device is advantageous to enable rapid display of pre-cached tiles and minimize delays associated with downloading.
145. Potmesil and Hornbacker both teach that a local cache on a client display device is advantageous to enable rapid display of pre-cached tiles and minimize delays associated with downloading. A person of ordinary skill in the art would recognize that both references teach similar solutions (caching previously received tiles) to similar problems of enhancing display speed and avoid downloading tiles that the client device already has. A person of ordinary skill in the art would also recognize that caching was well-recognized, common, and advantageous in the use of a typical internet browser, as there is no guarantee using a TCP/IP protocol that data packets will arrive in the same order that they are requested because of the asynchronous nature of the protocol, and it would be necessary at least to temporarily store data packets until they are actually needed.

The use of caches was widely known in several different contexts in common use on internet browsers. Typical internet browsers of the time would utilize caches in order to avoid consuming additional bandwidth in order to download the same information on a webpage that the user had already visited. Caches were (and still are) frequently used in a streaming audio or video context, in order to save data likely to be needed in the near future. Therefore, in my opinion, this element is both disclosed by and obvious over Potmesil in view of Hornbacker.
146. Element 13.H render said defined data parcel over a discrete portion of said mesh to provide for a progressive resolution enhancement of said defined image on said display; Potmesil teaches that images are stored in a power-of-two pyramid to provide fast access to scroll and zoom operations. Ex. 1002 at Abstract, Fig. 1, 1329-30, 1332-33, Fig. 2. A person of ordinary skill in the art would recognize that zooming using the power-of-two tile pyramid of Potmesil would provide progressive regional resolution enhancement of the image from lower to higher resolution as the user zooms in. Additionally, it would be obvious to a person of ordinary skill in the art that the "flight simulator" mode would provide progressive regional resolution enhancement of 3D rendered terrain as the user moves toward a point, because it was well-known in the computer graphics field (e.g. in the OpenGL standard) to utilize lower-resolution textures for more
distant objects occupying a smaller portion of the screen and transition to higherresolution textures for objects closer to the simulated user viewpoint.
147. In my opinion, it would further be obvious to a person of ordinary skill in the art that the request for tiles using the map applications would preferably request tiles nearest the user viewpoint first, before requesting more distant tiles, in order to effectively manage limited cache sizes. In my opinion, a person of ordinary skill in the art would also recognize that the disclosure of cache allocation based on $x, y, z$, level-of-detail, and time would naturally mean that all of these factors should be included in the prioritization by the algorithm. For example, if a user is flying toward a mountain or city in the "flight simulator" example, the display algorithm would naturally require a lower-resolution tile for that area first because of the need to display a large area visible in the distance but at lower resolution. As the point grows closer, the user would expect to be able to see things in more detail, and accordingly the person of ordinary skill in the art would rationally see the need for imagery and a higher resolution and program the caching algorithm accordingly. The use of these factors to create an algorithm to weight the priority given to different tiles, and to request those tiles accordingly, would have been well within the ability of a person of ordinary skill in the art
using conventional computer programming techniques, and there are many different ways that such a solution could be accomplished.
148. Hornbacker teaches that tiles within a large database may be located by requests over a server which use URLs to identify the specific tile by incorporating identifying characteristics such as resolution, location, view angle, etc. See, e.g. Ex. 1003, 3:10-27, 5:16-25, 6:13-19, 8:30-9:28. Hornbacker teaches that tiles may be requested in a priority order in order to provide progressive resolution enhancement by providing lower resolution tiles first. See, e.g., id. at Abstract, 12:24-13:10. Hornbacker also teaches that view tiles that may be required by the next view request may be "pre-computed" based on the anticipated view. Id., 7:26-8:6.
149. It is my opinion that these disclosures in Hornbacker collectively disclose or suggest rendering tiles to provide for progressive resolution enhancement of tiles within the visible display area.
150. Potmesil and Hornbacker both teach or suggest methods of requesting image tiles over a network according to a priority order to provide progressive regional resolution enhancement. Potmesil and Hornbacker both identify a common problem with the display of portions of very large images over a network, which is the latency and bandwidth consumption associated with downloading an
entire image, and arrive at similar solutions in the form of requests for specific tiles in a priority order based on how soon the tiles need to be displayed. In my opinion, a person of ordinary skill in the art would recognize that the teachings of the two references solving similar problems in closely related fields could be considered in combination when designing a display system addressing a similar problem -displaying images quickly in a visually pleasing manner.
151. Further, in my opinion, a person of ordinary skill in the art would recognize that the specific system for requesting tiles by URL, as disclosed in Hornbacker, could be advantageously utilized in the tile request process of Potmesil, which includes identifying tiles likely to be needed in the near future based on their geographic coordinates, because both Potmesil and Hornbacker concern web-based systems, and URLs are the most common way for identifying and requesting resources in such web-based systems.
152. Additionally, both Potmesil and Hornbacker teach that tiles are retrieved so that they can be rendered on the screen (i.e. viewed in the browser window), and that the tiles correspond to discrete portions of the image (e.g. map data).
153. Element 13.I a remote computer, coupled to the limited
bandwidth communications channel, that delivers the defined data parcel; Potmesil
and Hornbacker both teach that tiles are delivered by a server computer, i.e. geographical and geometrical servers in Potmesil and network servers in Hornbacker, which are coupled to the limited bandwidth communications channel. Ex. 1002 at Abstract, 1328, 1329-30, 1332; Ex. 1003 at Title, Abstract, 3:10-27, 4:26-31, Fig. 1, 5:3-6:19, 7:26-8:6, 8:16-23, 9:29-10:2, 10:13-28, 12:17-23, 13:1714:16.
154. Element 13.J wherein delivering the defined data parcel further comprises processing source image data to obtain a series $\mathrm{K}_{1-\mathrm{N}}$ of derivative images of progressively lower image resolution; this claim element is substantially similar to claim element 1.D of the 343 Patent; therefore, in my opinion, the same teachings that I previously discussed in regard to that claim element apply.
155. Element 13.K wherein series image $\mathrm{K}_{0}$ being subdivided into a regular array; this claim element is substantially similar to claim element 1.E of the 343 Patent; therefore, in my opinion, the same teachings that I previously discussed in regard to that claim element apply.
156. Element 13.L wherein each resulting image parcel of the array has a predetermined pixel resolution; this claim element is substantially similar to claim element 1.F of the 343 Patent; therefore, in my opinion, the same teachings that I previously discussed in regard to that claim element apply.
157. Element 13.M wherein image data has a color or bit per pixel depth representing a data parcel size of a predetermined number of bytes, this claim element is substantially similar to claim element 1.G of the 343 Patent; therefore, in my opinion, the same teachings that I previously discussed in regard to that claim element apply.
158. Element 13.N resolution of the series $\mathrm{K}_{1-N}$ of derivative images being related to that of the source image data or predecessor image in the series by a factor of two; this claim element is substantially similar to claim element 1.H of the 343 Patent; therefore, in my opinion, the same teachings that I previously discussed in regard to that claim element apply.
159. Element $\mathbf{1 3 . 0}$ said array subdivision being related by a factor of two; this claim element is substantially similar to claim element 1.I of the 343 Patent; therefore, in my opinion, the same teachings that I previously discussed in regard to that claim element apply.
160. Element 13.P such that each image parcel being of a fixed byte size, this claim element is substantially similar to claim element 1.J of the 343 Patent; therefore, in my opinion, the same teachings that I previously discussed in regard to that claim element apply.
161. Element 13.Q wherein the processing further comprises compressing each data parcel; this claim element is substantially similar to claim element 1.K of the 343 Patent; therefore, in my opinion, the same teachings that I previously discussed in regard to that claim element apply.
162. Element 13.R storing each data parcel on the remote computer in a file of defined configuration such that a data parcel can be located by specification of a $\mathrm{K}_{\underline{D}}, \mathrm{X}, \mathrm{Y}$ value that represents the data set resolution index D and corresponding image array coordinate. This claim element is substantially similar to claim element 1.L of the 343 Patent; therefore, in my opinion, the same teachings that I previously discussed in regard to that claim element apply.

## 6. Claims 17-19 are Rendered Obvious by Potmesil and Hornbacker

163. Claim 17. The display system of claim 13, wherein the data parcel further comprises one of an image parcel textual mapping, a map parcel, a navigation cue, a text overlay and a topography. This claim element is substantially similar to claim 2 of the 343 Patent; therefore, in my opinion, the same teachings that I previously discussed in regard to that claim element apply.
164. Claim 18. The display system of claim 13 , wherein the predetermined pixel resolution for each data parcel is a power of 2. This claim element is substantially similar to claim 4 of the 343 Patent; therefore, in my
opinion, the same teachings that I previously discussed in regard to that claim element apply.
165. Claim 19 The display system of claim 18 , wherein the predetermined pixel resolution is power of 2 and one of $32 \times 32,64 \times 64,128 \times 128$ and $256 \times 256$. This claim element is substantially similar to claim 5 of the 343 Patent; therefore, in my opinion, the same teachings that I previously discussed in regard to that claim element apply.
166. I have provided as Appendix $U$ to this declaration a claim chart showing the exemplary teachings of Potmesil and Hornbacker that are pertinent to claims 1-11 and 13-19 of the 343 Patent.
B. GROUND 2: CLAIMS 10-12, 14-16 AND 20 ARE UNPATENTABLE UNDER 35 U.S.C. § 103(a) AS BEING OBVIOUS OVER POTMESIL IN VIEW OF HORNBACKER AND FURTHER IN VIEW OF LINDSTROM
167. In my opinion, claims $10-12,14-16$ and 20 are disclosed and rendered obvious by Potmesil in view of Hornbacker, and further in view of Lindstrom. Claims 10-12 and 14-16 and 20 are dependent on claims 1 and 13. Claims 10-11 depend on claim 1 and add limitations relating to the prioritization of requests for image tiles, for which Lindstrom provides further details relating to the teaching of a priority queue. Claims 15-16 depend on claim 13 and add additional limitations relating to prioritizing image requests and optimizing tile resolution based on
screen resolution and the distance between the simulated viewpoint and the image.
Claims 12 and 20 add additional elements involving the client device performing multi-threading in connection with the display of image tiles. A "thread" in computer science, short for "thread of execution" is the smallest sequence of programmed operations that can be scheduled in an operating system. One or more threads may be executed within a process, which is an instance of a computer program that is being executed. For example, in the figure below, each of the executable (.exe) files executing on the system shown is a separate process which is separately given access to system resources:

| 포- Windows Task Manager |  |  |  | - - $\square$ ] |
| :---: | :---: | :---: | :---: | :---: |
| File Options Yiew Help |  |  |  |  |
| Applications Processes | Performance | Networking |  |  |
| Image Name | User Name | CPU | Mem Usage | CMM Size D- |
| firefox.exe | chris | 00 | $130,132 \mathrm{~K}$ | $24 \overline{2}, 424 \mathrm{~K}$ |
| iexplore.exe | chris | 00 | 2,136 K | $83,520 \mathrm{~K}$ |
| mmc.exe | chris | 01 | 10,572 K | 66,684 K |
| iexplore.exe | chris | 00 | $44,020 \mathrm{~K}$ | $62,140 \mathrm{~K}$ |
| mspaint.exe | chris | 00 | $63,108 \mathrm{~K}$ | $56,776 \mathrm{~K}$ |
| iexplore.exe | chris | 00 | $22,340 \mathrm{~K}$ | 53,176 K |
| Pandion.exe | chris | 00 | $21,156 \mathrm{~K}$ | $36,836 \mathrm{~K}$ |
| mozilla.exe | chris | 00 | 29,840 K | $33,708 \mathrm{~K}$ |
| sqlservr.exe | SYSTEM | 00 | $1,400 \mathrm{~K}$ | 33,376 K |
| thunderbird.exe | chris | 00 | 5,892 K | 32,996 K |
| svchost.exe | SYSTEM | 00 | 27,284 K | 29,148 K |
| explorer.exe | chris | 01 | 22,724K | 24,436 K |
| OUTLOOK.EXE | chris | 00 | $27,496 \mathrm{~K}$ | 21,984 K |
| putty,exe | chris | 00 | $16,712 \mathrm{~K}$ | 17,708 K |
| GIANTAntiSpywar... | chris | 01 | 21,776K | 17,188 K |
| putty, exe | chris | 00 | 1,272 K | 15,956 K |
| vmware.exe | chris | 00 | 4,724K | 15,364 K |
| vmware-vmx.exe | chris | 01 | 106,532 K | 12,476 K |
| vmware-vmx.exe | chris | 02 | 112,152 K | $11,916 \mathrm{~K} \quad$ - |
| $\square$ show processes from all users |  |  |  | End Process |
| Processes: 94 CPU Us | sage: $22 \%$ | Commit Cha | ge: $1781 \mathrm{M} / 3$ | 3943M |

168. When more than one thread is executed within a single process, the process is said to be "multi-threaded." Multi-threading is typically utilized in computer programs to enable a program to execute multiple independent tasks concurrently without needing to start a new process, which enables more efficient use of the system resources. The figure below illustrates multiple threads executing within the same process:

169. Multi-threading was a well-known technique in computer science before the earliest alleged priority or invention date of the 343 Patent. For example, Potmesil references that the server is multi-threaded, which enables it to efficiently serve multiple threads simultaneously. Ex. 1002 at 1330.
170. Lindstrom (Ex. 1004) is a 1997 technical paper from the Georgia Institute of Technology which describes an online GIS system with a visual simulation application very similar to Potmesil in a number of respects. For example, like Potmesil, Lindstrom teaches an online client/server system for viewing large-scale geographic data, including terrain elevation and imagery data, using a 3D perspective view with multiple windows. Ex. 1004 at Abstract, §§ 1, 3, 4.1, 4.2.6, Fig. 1; compare Ex. 1002 at Abstract, 1329-30, 1332-33. Lindstrom also relies on a GIS database which stores images in a hierarchical multiresoution representation so that "terrain detail can be continuously adapted based on user viewpoint and scene content." Ex. 1004 at §§ 1, 2. Lindstrom also processes requests for image tiles using a prioritized queue and an image cache. Id. at Abstract, $\S \S 2,3,4,4.1,4.2 .1,4.2 .2,4.2$.3. Therefore, it is my opinion that a person of ordinary skill in the art would consider Potmesil and Lindstrom to be related or analogous art. Additionally, in my opinion, a person of ordinary skill in the art would recognize that the teachings of Lindstrom about the function of a level of detail manager including a dynamically updated priority queue for tile requests would provide an advantageous way to implement and optimize the tile caching and tile request process taught by Lindstrom. Additionally, Lindstrom's teachings about the level-of-detail manager optimizing the display of terrain and imagery
based on display thresholds would be advantageous in a system like Potmesil, which would address similar issues in regard to avoiding wasting bandwidth or storage to download tiles that cannot be displayed.
171. Lindstrom discusses in depth a multi-threaded display process for synchronizing tasks and displaying multiple independent views. Fig. 1 of Lindstrom shows the VGIS system architecture, which includes a master "render thread" for drawing display windows, a user interface thread which acts as an overall manager of the system, and separate terrain manager threads for each view:


Figure 1: Overview of the VGIS system architecture. This figure illustrates two independent views but can be generalized to an arbitrary number. Modules are represented by rounded boxes, processes and threads by circles, data structures by rectangular boxes, and data flow and communication by arrows.
172. Among other functions, the multiple threads associated with the "terrain manager" and "object manager" for each separate view enable these threads to separately request tiles from either a local cache or from the server. Id. at $\S 4.2 .1$. This teaching of separate threads for requests for imagery data is substantially similar to the corresponding disclosure of "multi-threading" in the 343 Patent, which discloses that "concurrent threads are able to support a relatively
continuous delivery of image data parcels to the client 20 for display processing." Ex. 1001 at 7:47-8:6.
173. In my opinion, a person of ordinary skill in the art would recognize that Lindstrom teaches a substantially similar online system to Potmesil with similar goals, and that the multi-threaded system of Lindstrom would provide similar advantages to speeding up processing in the system of Potmesil, particularly in view of the related teaching in Potmesil that the tile caching and compositing processes run independently and asynchronously. Ex. 1002 at 1333. Because multi-threading, the additional element in claims 12 and 20 of the 343 Patent, was well-known in the art even in the same context of online GIS systems having similar features, these claims of the 343 Patent are not novel and nonobvious over the prior art.
[173.1] Lindstrom teaches a system for retrieving and displaying geographic information in three dimensions, including details of client software architecture for utilizing a priority queue to request image data from internal or external servers. Priorities of messages in the priority queue are changed dynamically, according to the importance of associated request as determined by a lever-ofdetail manager that uses viewing distance as one criterion to decide the importance of an object.
[173.2] Plates 1-6 of Lindstrom illustrate how the system of Lindstrom
displays a 3D perspective view of geographic information at various resolutions, including the sequence of images below zooming from a global dataset to downtown Atlanta:


1. Visualization of the global dataset ( 8 km resolution) from an altitude of $12,000 \mathrm{~km}$.

2. Four data insets of varying resolutions ( $1,10,100$, and $1,000 \mathrm{~m}$ ).

3. View approaching the state of Georgia inset data ( 100 m resolution).

4. View of downtown Atlanta data with 3D building models.
5. Claim Element 10.A The method of claim 1, wherein issuing the request for an update data parcel further comprises preparing the request by associating a prioritization value to said request, In my opinion, Potmesil in view of Hornbacker and Lindstrom teaches this claim element. Potmesil teaches software as part of the client image visualization application that identifies new
tiles to be requested from the server and cached. Ex. 1002 at Abstract, 1328, 1329$30(\$ \S 2,2.1), 1332-33(\S \S 3,3.1)$, Fig. 2. Potmesil teaches that cache allocation (i.e. priority of requests for tiles to use the limited space of the cache) is based on parameters including $x, y, z$, level-of-detail, and time. Ex. 1002 at 1332. The images are prioritized by proximity to the user viewpoint; for example, in the "flight simulator" scenario, the browser requests tiles in a "widening wedge" in front of the direction of flight; in other words, it first requests those tiles in the current view or very likely to be needed soon as the highest priority, then requests other tiles that may be needed in the future. Id. at 1332-33. A See also id. at 1327, 1334-35. In my opinion, it would be obvious to a person of ordinary skill in the art that such a caching algorithm would account for the factors specified (including $x, y, z$, level-of-detail and time) in order to prioritize which tiles to load into the cache, since the system is designed to work with both a cache of limited space and a communications channel of limited bandwidth. It would be obvious to a person of ordinary skill in the art to associate some type of prioritization value (e.g. a position in the queue) with a requested tile in order to set the order of tiles being requested. For example, it would be obvious to a person of ordinary skill in the art that the request for tiles using the map applications would preferably request tiles nearest the user viewpoint first, before requesting more distant tiles, in order to
effectively manage limited cache sizes. Additionally, if a user is flying toward a mountain or city in the "flight simulator" example, the display algorithm would naturally require a lower-resolution tile for that area first because of the need to display a large area visible in the distance but at lower resolution. As the point grows closer, the user would expect to be able to see things in more detail, and accordingly the person of ordinary skill in the art would rationally see the need for imagery and a higher resolution and program the caching algorithm accordingly. The use of these factors to create an algorithm to weight the priority given to different tiles, and to request those tiles accordingly, would have been well within the ability of a person of ordinary skill in the art using conventional computer programming techniques, and there are many different ways that such a solution could be accomplished. Lindstrom teaches examples of such solutions by illustrating how a client rendering module and level of detail manager may utilize a priority queue for making imagery requests to the server, and that the queue man change priority dynamically according to the importance determined by the level of detail manager. Ex. 1004, §§ 3, 4.2.1, Fig. 1.
6. Hornbacker teaches that tiles within a large database may be located by requests over a server which use URLs to identify the specific tile by incorporating identifying characteristics such as resolution, location, view angle,
etc. See, e.g. Ex. 1003, 3:10-27, 5:16-25, 6:13-19, 8:30-9:28. Hornbacker teaches that tiles may be requested in a priority order in order to provide progressive resolution enhancement by providing lower resolution tiles first. See, e.g., id. at Abstract, 12:24-13:10. Hornbacker also teaches that view tiles that may be required by the next view request may be "pre-computed" based on the anticipated view. Id., 7:26-8:6, 10:24-28.
7. It is my opinion that these disclosures in Hornbacker collectively disclose or suggest assigning relative prioritization values to tile requests in order to request tiles in a preferred sequence- from lower resolutions to higher resolutions for progressive resolution enhancement and tiles within the visible display area before "pre-caching" tiles outside the visible display area.
8. Potmesil, Hornbacker, and Lindstrom each teach methods of requesting image tiles over a network according to a priority order. Each reference identifies a common problem with the display of portions of very large images over a network, which is the latency and bandwidth consumption associated with downloading an entire image, and arrive at similar solutions in the form of requests for specific tiles in a priority order based on how soon the tiles need to be displayed. A person of ordinary skill in the art would recognize that the teachings of the two references solving similar problems in closely related fields could be
considered in combination when designing a display system addressing a similar problem -- displaying images quickly in a visually pleasing manner.
9. Further, a person of ordinary skill in the art would recognize that the specific system for requesting tiles by URL, as disclosed in Hornbacker, could be advantageously utilized in the tile request process of Potmesil, which includes identifying tiles likely to be needed in the near future based on their geographic coordinates, because both Potmesil and Hornbacker concern web-based systems, and URL is the most common way for identifying and requesting resources in such web-based systems.
10. It is my opinion that it would be obvious to a person of ordinary skill in the art to utilize a request queue in order to request images according to priority as discussed above in regard to both Potmesil, Hornbacker, and Lindstrom. I would expect both of the systems described by Potmesil and Hornbacker to utilize queues in light of the state of the art at the time. Typical internet functionality at the time, including requests for streaming media such as video, typically included a queue of requests for information in order to prioritize delivery of certain information, to avoid disruptions in the data stream. Additionally, because Potmesil explicitly describes a caching algorithm sorted by various criteria such as location and level of detail, I would expect that such an algorithm would be likely to employ a
request queue at some point as the output of the prioritization stage of the algorithm, and that such a queue would be used to generate the tile requests to the server.
11. Claim Element 10.B wherein said prioritization value is based on the resolution of said update data parcel relative to that of other data parcels previously received by the limited communication bandwidth computer device. Potmesil teaches that the tile cache has a finite amount of space and the tile caching process prioritizes those tiles most likely to be needed. Ex. 1002 at 1332. It would be readily apparent to a person of ordinary skill in the art that when a user either zooms in with the 2 D browser or flies toward a given point in the 3 D browser, the caching process would need to take into account the resolution of tiles expected to be needed compared to those that have already been received, in order to provide for smooth rendering of the image at greater levels of detail without wasting bandwidth downloading redundant tiles. Id. Fig. 1, 1329-30. Additionally, in my opinion, a person of ordinary skill in the art would recognize that the management of prioritization requests based on resolution could readily be implemented by a level of detail manager and priority queue such as that taught by Lindstrom. Ex. 1004, § 4.2.1.
12. Hornbacker also teaches that tiles may be requested in a priority order in order to provide progressive resolution enhancement by providing lower resolution tiles first. Ex. 1003 at Abstract, 12:24-13:10. It is my opinion that this teaching discloses a prioritization value of the update data parcel relative to that of other data parcels previously received by the limited communication bandwidth computer device, because the highest priority tiles in such a situation are naturally the tiles of higher resolution than those that have already been downloaded, and when multiple resolution layers are used in displaying an image according to Hornbacker's teachings, because the use of tiles at intermediate levels of resolution would enable the quality of the image to gradually improve as more tiles are received instead of continually displaying a very low resolution image until the highest resolution tiles are received.
13. Claim Element 10.C wherein issuing said request is responsive to said prioritization value for issuing said request in a predefined prioritization order. As I previously discussed above in regard to claim 10.A, it is disclosed and obvious over Potmesil in view of Hornbacker to issue requests for image tiles in a priority order based on which tiles are needed the soonest, and Lindstrom further illustrates how a priority queue is used to issue data requests in a prioritization order.
14. Claim 11. The method of claim 10, wherein said prioritization values is based on the relative distance of said update data parcel from said operator controlled image viewpoint. As I previously discussed, Potmesil teaches that the caching algorithm requests and caches tiles based on factors including the user's current position, velocity, and viewpoint (e.g. different views in a 3D browser). Ex. 1002 at 1332. Potmesil specifically teaches that within the caching process, tiles which intersect with the user's current view or projected path are "sorted by distance from the user" so that the caching algorithm can "determine[] how many of them can be loaded in the cache." Id. Lindstrom teaches a system that includes level of detail management based on user viewpoint, including viewpoint-to-texel distance, as well as distance-based clipping of requested tiles. Ex. 1004, § 1, 4.2.1, 4.2.6. The viewpoint may be generated based on a six degree freedom of navigation interface. Id. at 4.2.6. Additionally, a person of ordinary skill in the art would recognize in light of well-known principles of computer graphics that tiles in a power-of-two pyramid used for rendering (such as in the OpenGL standard referenced by Potmesil and Lindstrom), are preferably filtered based on the proximity of the object being rendered to the user's focal point, which in turn can be used to determine the highest resolution that can be rendered. Lindstrom further explains how such filtering may be implemented, and a person of ordinary skill in
the art would readily recognize that such teachings are applicable to the system of Potmesil.
15. Claim 12. The method of claim 1, wherein displaying the image further comprises multi-threading on the limited communication bandwidth computer device using the update data parcel to display the image. Lindstrom discloses that the display process on the client device is multi-threaded. Ex. 1004, Fig. 1, §§ 1, 3, 4, 4.2, 4.2.1, 4.2.3, 4.2.5, 4.2.6. For the reasons that I discussed above, it would be obvious to a person of ordinary skill in the art to combine this teaching with the teachings of Potmesil and Hornbacker.
16. Claim 14. The display system of claim 13 , wherein said processor is responsive to said defined screen resolution and wherein said processor is operative to limit selection of said defined data parcel to where the resolution of said defined data parcel is less than or equal to said defined screen resolution; Potmesil teaches downloading tiles including terrain and imagery data and rendering a 2D or 3D view. Ex. 1002 at Abstract, 1328, 1332, 1333-35, 1340. Potmesil further teaches that tiles are allocated to the cache by parameters, including level-of-detail, which may be used to request those tiles most likely to be needed. Id. at Fig. 1, 1328, 1329-30, 1340-41. In my opinion, a person of ordinary skill in the art would recognize in light of well-known principles of computer
graphics, including the principles used in the OpenGL standard referenced by Potmesil and Lindstrom, that an optimal resolution for displaying tiles is a resolution where the number of pixels per square inch as the tile is rendered does not exceed the number of pixels per square inch that the display can show, because otherwise download bandwidth is being wasted. This is a substantial part of the reason for using mip-maps in both 2D and 3D graphics contexts- the level-of-detail pyramid allows the rendering application to select the appropriate resolution level for any given "mip-map" at a given distance from the viewpoint. Indeed, Lindstrom teaches that the level of detail manager compares terrain geometry and imagery resolution to a resolution threshold based on screen resolution to optimize level of detail. Ex. 1011, $\S 4.2 .1$, Fig. 1.Additionally, it was well-known in the art both in graphics applications and in web browsing applications that the application would need information about the display characteristics of the underlying client in order to optimize the retrieval and display of information. Simply to render an image on a screen, the rendering system would need to know the output resolution. By way of example, conveying the overall resolution of the device could enable the server to properly format image data so that a circle does not appear on the screen as an ellipse. For example, U.S. Patent No. 5,987,256 (App. P) to Wu et al teaches a system for distributing documents to a client device which relies on
"device profiles" containing characteristics such as client device resolution and color depth to optimize the display of a document on the device.
17. Hornbacker further teaches that the resolution of tiles requested is determined based on the size of the view area and the scale at which the user is viewing the image. 7:4-25, 11:19-28, 13:4-10, 14:2-6.
18. In my opinion, it would be obvious to a person of ordinary skill in the art in light of these combined teachings that the tiles used in a system displaying a 2D or 3D perspective view as in Potmesil or Lindstromor at a given zoom level and scale as in Hornbacker would preferably request tiles at a resolution that the display was capable of displaying (i.e. less than the predetermined resolution of the display as the tiles are rendered) but that would still produce a satisfying image, and Lindstrom provides further teachings illustrating how a software function such as the LOD manager could implement such a function.
19. Claim Element 15.A The display system of claim 13, wherein said processor is operative to prioritize the retrieval of said data parcel among a plurality of selected data parcels pending retrieval; As I previously discussed above in regard to claim element 10.A, Potmesil teaches that requests for tiles are prepared in a priority order based on those tiles needed first in the caching algorithm, while Lindstrom teaches the dynamic management of a priority request
queue by a level of detail manager. In my opinion, the caching algorithm based on $x, y, z$, level-of detail, and time as taught by Potmesil would obviously assign a higher priority to those tiles needed most immediately (e.g. those closest to the viewer's viewpoint or flight path) over those pending retrieval but needed less urgently (e.g. distant tiles within the flight path). A person of ordinary skill in the art would be motivated to prioritize the retrieval of tiles because of the limited cache space and the limited bandwidth to obtain tiles; therefore, the cache space is utilized most effectively and latency is reduced by prioritizing among tile requests. Lindstrom provides additional teachings for how the prioritization of tile retrieval could be implemented by a level of detail manager and a priority queue.

Additionally, Potmesil teaches that the tile caching process is a portion of the browser, which is executed by the processor on the client workstation. Ex. 1002 at 1328, 1332.
189. Claim Element 15.B wherein the relative priority of the data parcel is based on the difference in the resolution of the image parcel and the resolution of said plurality of selected data parcels; Potmesil discloses that the caching algorithm incorporates "level of detail" as a factor considered. Ex. 1002 at 1332. In my opinion, it would further be obvious to a person of ordinary skill in the art that the request for tiles using the map applications would preferably request
tiles nearest the user viewpoint first, before requesting more distant tiles, in order to effectively manage limited cache sizes. In my opinion, a person of ordinary skill in the art would also recognize that the disclosure of cache allocation based on $x, y$, z, level-of-detail, and time would naturally mean that all of these factors should be included in the prioritization by the algorithm. For example, if a user is flying toward a mountain or city in the "flight simulator" example, the display algorithm would naturally require a lower-resolution tile for that area first because of the need to display a large area visible in the distance but at lower resolution. As the point grows closer, the user would expect to be able to see things in more detail, and accordingly the person of ordinary skill in the art would rationally see the need for imagery and a higher resolution and program the caching algorithm accordingly. The use of these factors to create an algorithm to weight the priority given to different tiles, and to request those tiles accordingly, would have been well within the ability of a person of ordinary skill in the art using conventional computer programming techniques, and there are many different ways that such a solution could be accomplished. Lindstrom provides further teachings that the priority of requests in the queue is changed dynamically according to the level of detail manager, meaning that the relative priority of a tile request may be based on the difference in resolution between that tile and the others in the queue. Ex. 1004, §
4.2.1. In my opinion, Lindstrom's teachings of a level of detail manager and a priority queue are illustrative of how a person of ordinary skill in the art would understand to implement a caching algorithm like that taught by Potmesil.

Hornbacker teaches that tiles within a large database may be located by requests over a server which use URLs to identify the specific tile by incorporating identifying characteristics such as resolution, location, view angle, etc. See, e.g. Ex. 1003, 3:10-27, 5:16-25, 6:13-19, 8:30-9:28. Hornbacker teaches that tiles may be requested in a priority order in order to provide progressive resolution enhancement by providing lower resolution tiles first. See, e.g., id. at Abstract, 12:24-13:10. Therefore, in my opinion, it would be obvious to a person of ordinary skill in the art based on the teachings of Hornbacker to assign a higher priority initially to lower resolution tiles compared to higher resolution tiles in order to provide progressive resolution enhancement. A person of ordinary skill in the art would recognize that these references provide related, complementary teachings and that the priority queue based on LOD management of Lindstrom would provide a means to sort tile requests to provide a realistic 3D browsing experience as in Potmesil or progressive resolution enhancement as in Hornbacker.
190. Claim Element 16.A The display system of claim 13, wherein said processor is response to user navigation commands to define an image
viewpoint relative to said defined image; Potmesil teaches a three-dimensional terrain visualization application which renders views of terrain based on user navigational commands, as well as a two-dimensional browser: Ex. 1002 at Abstract, 1328-29, 1332-33, Fig. 2, 1340-41, Fig.8. It is both disclosed and obvious to a person of ordinary skill in the art that the image mappings generated by the browser of Potmesil can include various combinations including elevation and imagery such as satellite imagery. Potmesil also teaches that the "mapplets" used in the browser, including the 3-D visualization application and the "image applet" that can retrieve image data such as satellite imagery may be "mixed and matched." Ex. 1002 at 1333. In my opinion, a person of ordinary skill in the art would recognize that the system of Potmesil could use its capability to download satellite images in combination with the 3D browser in order to render downloaded images on a 3D browser. In particular, as I noted previously in this declaration, the concept of rendering tiled satellite or aerial photography imagery as the texture for a three-dimensional model of the corresponding terrain was already well-known in the art. Potmesil further teaches that the 3D browser downloads image tiles based on the estimated positions of a given view, e.g. a perspective view from an airplane cockpit. Ex. 1002 at 1332. Therefore, in my opinion, this element is both disclosed by and obvious in view of Potmesil. Lindstrom teaches a similar system to

Potmesil which can visualize data through multiple 3D views and navigation controlled by a six degree of freedom interface, and provides additional details about how a 3D system of the type taught by Potmesil could be implemented. Ex. 1004, § 3, 4, 4.2.1, 4.2.3, 4.2.6.
191. Claim Element 16.B wherein said processor is operative to prioritize the retrieval of said data parcel based on the distance between said image parcel and said image viewpoint relative to said defined image. In my opinion, this element is substantially similar to claim 11, and therefore the same teachings and my analysis of those teachings apply here. Claim 16 recites that "said processor is operative to" perform the listed steps; however, all of the functions that I discussed in regard to claim 11 would ordinarily be performed by a processor on a client device.
192. Claim 20. The display system of claim 13 , wherein the processor performs multi-threading to render said defined data parcel over the discrete portion of said mesh to provide for the progressive resolution enhancement of said defined image on said display. Lindstrom teaches that the multi-threaded rendering process is used to display multiresolution images of geometrically complex terrain, using a hierarchical organization structure so that the terrain detail can be continuously adapted based on user viewpoint and scene content. Ex. 1004, Fig. 1,
$\S \S 1,3,4.2,4.2 .1$. Therefore, in my opinion it is disclosed and obvious to a person of ordinary skill in the art that the system of Lindstrom would therefore provide progressive resolution enhancement of a point on the terrain model as the viewpoint moves toward that point, and it would further be obvious to a person of ordinary skill in the art to combine this teaching with the teachings of Potmesil and Hornbacker for the reasons discussed above.
193. I have also discussed teachings of Potmesil, Hornbacker, and Lindstrom pertinent to claims 10-12, 14-16, and 20 in Appendix U.

## C. GROUND 3: CLAIMS 1, 2, 4-11 AND 13-19 ARE UNPATENTABLE UNDER 35 U.S.C. § 103(a) AS BEING OBVIOUS OVER LIGTENBERG IN VIEW OF RUTLEDGE AND COOPER

194. In additions to the grounds discussed herein, in my opinion, claims 1 , 2, 4-11, and 13-19 are also disclosed and rendered obvious by Rutledge (Ex. 1005) in view of Ligtenberg (Ex. 1004) and Cooper (Ex. 1006).
195. While the claims $1,2,4-11$, and $13-19$ do not explicitly recite that the recited method is used for browsing maps or geographical data, the specification of the 343 Patent describes map browsing as an exemplary use of the disclosed technology. In this regard, Rutledge discloses techniques for downloading map images over network from a server to a client device. Ligtenberg also provides techniques for downloading images from a server to a client device for viewing.

The images are made available as map tiles corresponding to various resolution levels and regions of the image. Cooper further discloses priority techniques used by client devices in prioritizing which image data portion to request next, based on a user's viewpoint.
196. As further discussed in my declaration, Rutledge, Ligtenberg, and Cooper collectively disclose each and every feature recited in claims $1,2,4-11$, and 13-19.

## 1. Overview of Rutledge, Ligtenberg, and Cooper

197. Rutledge is a patent document (U.S. patent number $6,650,998$ ) that was filed on July 28, 1997, claiming priority to earlier patent applications dating back to March 11, 1996. Rutledge discloses a network-based search system in which a user is able to download map data and associated additional information such as street names, people names, telephone numbers, etc. Ex. 1005 at Abstract. The map data may be in the form of images such as satellite imagery, hand digitized maps and scanned images. Id. at 4:41-47; 6:11-17; 6:38-50.
198. Rutledge teaches a system enabling a user to connect to one or more database servers using a modem connection or using the internet. Ex. 1005 at Fig. 1,$115 ; 2: 60-64$. The user is able to use a device such as a personal computer having a terminal on which the maps are displayed.
199. At the time of filing of Rutledge, a modem connection was generally considered to be a low bandwidth connection, often with long wait times when downloading image data. For example, a 56 K baud rate was considered to be a high speed connection, with real data download rates often slower than the peak connection rate.
200. Rutledge teaches that in order to allow a satisfactory user experience even when connected via such a connection, map data may be stored in the form of map tiles. Ex. 1005 at $3: 4-5 ; 5: 14-64 ; 6: 1-5 ; 6: 25-35 ; 7: 15-20$. The map tiles are stored at various resolution levels. Id. A person of ordinary skill in the art would have understood the advantage of using map tiles, because map tiles can be downloaded in smaller units of data, while providing visual information presentable on the display terminal as a self-contained unit. For example, the same geographical region may be covered by map tiles of various resolution, as depicted in Rutledge, Fig. 3, which is reproduced below:


FIG. 3, Rutledge
201. Rutledge teaches that the system allows a user to specify a zoom level at which the user wants to see the map image. Id. at 7:47-62; Fig. 4D, which is reproduced below.


Rutledge, Fig. 4D
202. In response to the user's selection of the zoom level, the map server
retrieves appropriate map tiles and transmits them to the user. If the server does not have map data at the zoom level requested by the user, the server map interpolates between two stored zoom level images to compute the corresponding image at the zoom level requested by the user. [NNi]
203. Ligtenberg also discloses a technique for storing and retrieving image files for browsing by downloading across a computer network. Ex. 1005 at


#### Abstract

. 204. Ligtenberg recognizes a problem that typical image data sizes were


 significantly large and therefore posed problem to prevalent computer systems and networks for viewing by transferring the images over a network. Id. at 1:33-42. These images could be, e.g., digitized photographs. Id. Ligtenberg also recognized that the then-prevalent image compression methods such as JPEG, did not allow for selective reconstruction of a desired portion of an image. Id. at col. 2:12-22.205. To solve these limitations, Ligtenberg discloses a file format for storing and retrieving images as tiles, which represent a smaller portion of the image. Id. at 2:25-49. An input image is decomposed into a number of images, at least some of these images are subdivided into tiles, or rectangular blocks. Id. at 2:31-49; 5:34-53. Furthermore, reduced resolution representations of the input image are generated for multiple resolution levels. Ligtenberg uses the term "layer" to refer to a reduced resolution image and additional pixel data at a given resolution. Id. at 48-50.
206. Ligtenberg discloses the use of low pass and high pass filters to decompose an input image into layers with different resolutions. The lowest
resolution image obtained after filtering is called a reduced image and the remaining data, called "complementary images" represent higher resolution components of the reduced image.
207. When images stored using the image format taught by Ligtenberg are retrieved and rendered on a client device, the expanded image is written to a display memory, Thus, a fuzzy version of the image initially appears on the screen while additional data is being retrieved from the server for improving sharpness of the image. Id. at 10:17-21.
208. Ligtenberg, in Appendix A, provides an example code listing of a file format suitable for use with the disclosed techniques. I have reviewed this code. In my opinion, this code is written in the " C " programming language and offers at least the following insights to a person of ordinary skill in the art into Ligtenberg's technique.
209. The variables fLLLayer and fLayers[i] show that data for each layer can be independently accessed, without having to access data from another layer. Id. at 12:59-66.
210. Every layer representing the original image is itself represented using multiple sub-images, with four sub-image embodiment having been discussed in the specification and the code. Id. at 13:12-18.
211. The image data in each layer is organized as tiles, with tiles arranged as an array of TileIndexEntry structures. Id. at 13:38-43. The disclosed embodiment organizes the tile data such that all entries for first row of tiles for the first image component are stored first, followed by each additional rows. Id. at 13:50-60.
212. Based on my reading of the Ligtenberg reference, it is my conclusion that some specific details of the file format are implementation choices. The design theme in Ligtenberg is to allow independent access to image tiles at a given layer. In my opinion, these feature of Ligtenberg lends itself to a bandwidth-efficient image fetching implementation because a client device need only request for, and receive, image data at a given resolution and for a given region of the image. Ligtenberg's file format can be used, e.g., to generate a user experience of "progressive resolution enhancement" in which an image initially appears fuzzy based on the display of lower resolution tiles, and then sharpens in pieces, as additional tiles are received and rendered.
213. Cooper is a U.S. Patent, No. 6,118,456, issued on September 12, 2000 from a patent application filed on April 2, 1998. Cooper discloses techniques and devices for efficiently using available network bandwidth to render visual objects and image data by prioritizing object requests by a user device. Ex. 1007 at

Abstract, 1:6-10; 2:50-55; 3:7-9; 4:48-60; 6:16-24; 6:66-7:11. Cooper discloses techniques in which a 3-D view is rendered on a display device by receiving greater detail of object display data on a frame update cycle basis. Id. at 5:58-6:4. To calculate priorities of objects, that is, data for which objects to receive in a next frame update cycle, Cooper teaches the use of an object assessment function that calculates visual importance of an object based on a user's current viewpoint. Id. at 6:11-24. Based on the determined priority of object data, a streaming function sends requests to server for the data. Id.
214. As depicted in FIG. 2 in Cooper, reproduced below, Cooper teaches client device which maintains a priority queue for visual object data that is continuously updated.


Cooper, FIG. 2

## 2. Motivation to Combine Rutledge, Ligtenberg, and Cooper

215. Rutledge teaches a technique that is versatile enough that many different formats could be used for communicating map tiles from a server to a client. Rutledge teaches storing map tiles at various zoom levels. This can be accomplished by using fLayers[] as taught by Ligtenberg for accessing tiles at each layer. Furthermore, while Ligtenberg's disclosed exemplary embodiment splits every layer into four subimages, the use of arrays would have made it easily possible to a person of ordinary skill in the art to use the same file structure for storing any number of tiles on a per-layer basis.
216. The file structure taught by Ligtenberg allows independent access to tile data by specifying point values within the file or database in which all tiles are stored. In other words, each tile can be independently accessed by its layer and resolution level, thereby allowing the system to request and download only image data that is needed for rendering. Put differently, no pre-caching at the client side would have to be done.
217. Rutledge and Ligtenberg provide solutions to efficiently use bandwidth and storage space so that a client can selectively request, receive, and render portions of visual data in the form of correct amount of map tiles at the correct resolution level based on user requests. A person of ordinary skill in the art
would have understood that this technology can be used for navigating through maps, satellite images, landscapes etc.
218. Cooper similarly discloses techniques by which a user can perform three-dimensional navigation through images, including virtual reality and flight simulations. Cooper addresses a similar issue as Rutledge and Ligtenberg in that Cooper discloses techniques by which the available network bandwidth can be efficiently used to request, receive and render only the most-needed portions of a visual image to render a scene based on user commands. Furthermore, a person of ordinary skill in the art would have understood that the visual data, called "objects" in Cooper, could easily be features displayed in a view of a terrain model.
219. A person of ordinary skill in the art would have known at the time that, whether images or computer graphics, the finer the detail rendered to a user, the greater the user satisfaction in viewing the image. A person of ordinary skill in the art would have understood that, when rendering three-dimensional objects, the number of polygons rendered will increase the perceived quality of the images. Similarly, a better resolution of images rendered near the focal point of the image will also increase the perceived quality of images because the eye can detect higher resolution near the center of the view. A person of ordinary skill in the art would have therefore understood that Cooper's prioritization technique in which objects
that improve the perceived quality images are prioritized for transmission over a network will benefit Rutledge's map browsing technique by placing the transmission of map tiles in a priority order. A person of ordinary skill in the art would have also understood that Ligtenberg's file format is especially suitable for the storage and retrieval of such image data because independent access to map tiles at specific resolution level and specific locations on the screen allow for download of specific image portions without having to download image data before or after the desired image data in scan order.
220. To a person of ordinary skill in the art, a user's viewpoint would obviously influence the zoom layer. Similarly, when a user performs panning - it would mean moving the eye point at least into two dimensions: an X or left-right direction and a Y , or up-down, direction.
221. Furthermore, as previously discussed, a user's perceived image quality typically depends on the resolution of the image data rendered.
222. A person of ordinary skill in the art would have found it obvious to use progressive resolution enhancement techniques because the progressive resolution technique efficiently uses the available bandwidth by downloading data of visual importance first, followed by finer details of the image. In addition to the
above reasons to combine the cited references, the following sections provide further reasons to combine the cited references.

## 3. Claims 1, 2, 4-11, and 13-19 Are Rendered Obvious by Rutledge in view of Ligtenberg and Cooper

## 223. Element 1.Preamble A method of retrieving large-scale images

 over network communications channels for display on a limited communication bandwidth computer device, said method comprising: In my opinion, the preamble is described and is obvious over Rutledge in view of Ligtenberg and Cooper. Both Rutledge and Cooper are addressed to similar or analogous problems relating to obtaining large sets of imagery over a network for viewing on a client device that cannot view the entire image at one time. For example, Rutledge discloses techniques to search large data sources including a map database and images of a geographic region, satellite imagery, digitized maps and scanned images. Ex. 1006, 1:21-23, 3:2-10, 3:54-57; 4:43-47; 6:11-13. Ligtenberg also discloses techniques for retrieving large images over a network. Ex. 1005, 11:1-2. Cooper also relates to downloading and rendering large amounts of imagery representing an environment in the field of 3D imaging. In my opinion, Cooper is in a related and analogous field because the system of Cooper also requires selectively accessing and displaying multi-resolution imagery corresponding to portions of a large environment. Specifically, Cooper discloses a technique for downloading andrendering image data in which complex graphical scenes, with a large number of data items, that requires substantial transmissions of data from a server to a client Ex. 1007, 2:27-30; 3:19-22.
224. Rutledge, Ligtenberg and Cooper each disclose downloading over a network communication channel - e.g., Rutledge's internet 120 (Ex. 1006, 2:62-65; 3:21-23), Ligtenberg's local area or wide area network or internet (Ex. 1005, 1:3941; 4:40-42; 5:14-17) and Cooper's "data pipe" which is a local area or a wide area network (Ex. 1007, 4:21-23). In my opinion, all of these references teach or suggest to a person of ordinary skill in the art that the imagery could be accessible via the Internet or a local network via TCP/IP.
225. Furthermore, each of these references discloses conveying image data to a limited communication bandwidth device, e.g., as discussed by Rutledge and Ligtenberg with respect to the use of a "modem" for image data download and a "limited bandwidth" channel between a server and a client as disclosed in Cooper. Ex. 1005, 4:51-54; 12:4-6; Ex. 1006, 2:62-64; Ex. 1007, 2:50-52; 4:61-5:6.
226. In my opinion, a person of ordinary skill in the art would have recognized that the file format of Ligtenberg would produce substantial benefits in the system of Rutledge to reduce CPU and I/O resource utilization, so that the utilization of these resources would be proportional only to data needed. Ex. 1005,

11:67-12:2; In my opinion, a person of ordinary skill in the art would have further recognized that Cooper's use of priorities for requesting additional visual data would provide substantial benefits in the combination of Rutledge and Ligtenberg by providing a way by which available network bandwidth can be efficiently used. The combined teachings of these references describe a system that performs the claimed method.
227. Element 1.A issuing, from a limited communication bandwidth computer device to a remote computer, a request for an update data parcel: In my opinion, both Rutledge and Cooper teach that the client system is a "limited communication bandwidth computer device" because the client system access tiles over a limited communication bandwidth channel, as discussed above in regard to the preamble. Rutledge and Cooper provide similar teachings in regard to this feature. Rutledge discloses that client devices retrieve images from a server by issuing a data request. Ex. 1006, 3:37-37; 7:5-9; 7:54-57; 10:10-19. Cooper further discloses that the client sends requests to server requesting data that it has not already received. Ex. 1007, Abstract; 3:49-53; 4:61-5:8; 6:5-10; 6:16-20. Therefore, in my opinion, this element is obvious over Rutledge in view of Cooper.
228. Element 1.B wherein the update data parcel is selected based on an operator controlled image viewpoint on the computer device relative to a
predetermined image; Cooper discloses techniques for rendering 3D graphics scenes by determining most important objects from a viewer's perspective and rendering them accordingly. Cooper teaches not only rendering of objects to provide a 3D feel to the rendered image, but also teaches that simulated user viewpoint could be moving through a three dimensional space, e.g., virtual reality, flight simulation, or moving from room to room or moving closer to certain objects.
229. Cooper also teaches that a user may turn to left or turn to right while viewing visual objects, or may move closer or farther from an object. Cooper also discloses determining a viewpoint orientation within an image displayed in a threedimensional space that includes rotational changes to the user's viewpoint. Ex. 1007 at Abstract, $1: 6-10,1: 16-21,1: 23-29,1: 34-38,3: 16-54,3: 59-65,4: 14-19$, 4:27-29, 4:39-4147, 4:48-51, 5:3426-36, 35:44-4948-57. Cooper discloses that during the viewing, the user's viewpoint orientation may change in a 3-D space. Id. Cooper also teaches that the view being seen by the observer is displayed in a 3-D space. Id.
230. Based on the above, it is my opinion that the technical feature recited in this claim is taught by Cooper.
231. Furthermore, in my opinion, a person of ordinary skill in the art would have understood the potential benefit of combining the three-dimensional navigation feature of Cooper with Rutledge and Ligtenberg to obtain the benefit of Rutledge's image download technique in combination with Ligtenberg's file structure and Cooper's priority scheme to utilize available network bandwidth efficiently.
232. Element 1.C the update data parcel contains data that is used to generate a display on the limited communication bandwidth computer device; In my opinion, Rutledge, Ligtenberg, and Cooper all teach that the data received via update data parcels (tiles or objects) is used to generate a display on a display device. The primary purpose of all three references is to describe retrieving data over a network for display on a client device. Rutledge teaches that a personal computer terminal allows a user to retrieve and display images. Ex. 1006, 6:38-40, 6:45-50, 7:48-62, 10:10-17. Ligtenberg discloses retrieval and display of images across a network. Ex. 1005, 1:16-19, 1:34-42, 4:28-34, 5:1-8, 5:13-17. Cooper also teaches displaying images on the client device. Ex. 1007, 1:13-22, 1:31-35, 4;14-18, 5:26-36, 5:58-67.
233. Element 1.D processing, on the remote computer, source image data to obtain a series $\mathrm{K}_{1-\mathrm{N}}$ of derivative images of progressively lower image
resolution; In my opinion, this claim element is taught by Rutledge, Ligtenberg, and Cooper. Rutledge teaches that map database server stores image data corresponding to various zoom layers. Each zoom layer represents a predetermined scale ,e.g., in miles covered by the zoom layer and thus represents progressively lower image resolution. Ex. 1006, 4:41-47, 5:15-24, 5:50-64; 7:48-62. Ligtenberg also teaches processing an image for storage at a server by decomposing an input image into a number of images of various resolutions, by producing lower resolution copies of the original image. Ex. 1005, FIG. 3, 2:31-38, 5:39-43, 5:5465; 6:7-12.
234. Cooper discloses that object data for displaying images is stored on a server. Ex. 1007, 1:29-33, 1:49-64, 2:9-12, 2:19-26, 2:45-50, 5;1-8, 5:65-6:4. The object data may be stored as a number of tessellated polygons that are rendered to fill in detail of the object. Id. The object data thus represents derivative images of progressively lower resolution.
235. In my opinion, a person of ordinary skill in the art would understand that Rutledge, Ligtenberg, and Cooper address similar problems- delivering image data that may be viewed at a wide variety of zoom levels or distances, and the need to optimize delivery and viewing of that imagery without wasting resources or delivering a sub-optimal image- and reach similar solutions in the form of
processing image data into a series of data objects of progressively lower resolution. Therefore, in my opinion, a person of ordinary skill in the art would consider these teachings related and analogous and would be motivated to consider these references in combination.
236. Element 1.E wherein series image $\mathrm{K}_{0}$ being subdivided into a regular array; In my opinion, this element is obvious over Rutledge, Ligtenberg, and Cooper. Rutledge teaches that image maps are divided into multiple zoom layers, with each tile in the zoom layer representing a geographical area, also called "a grid format." Ex. 1006, 4:41-47; 5:15-24, 5:50-64, FIG. 3. Rutledge discloses using zoom layers in which each tile represents a square area, e.g., 200 feet length, with each zoom layer representing a resolution that differs by a factor of 8 from the zoom layer above it. Id. In my opinion, Rutledge thus teaches using a series of images in which an image corresponding to the largest geographic region is subdivided into a regular array of tiles. Id.
237. Ligtenberg also teaches this claim element. For example, Ligtenberg teaches that large images are subdivided into tiles by way of rectangular arrays. Ex. 1005, Abstract, 2:9-22, 2:25-30, 5:21-27, 5:34-53, 7:19-21, 9:6-20, Appendix A.
237.1 Element 1.F wherein each resulting image parcel of the array has a predetermined pixel resolution; In my opinion, this element is obvious in
view of the collective teachings of Rutledge and Ligtenberg. Rutledge teaches that each map tile in a zoom layer has a fixed resolution that can be expressed as length in feet, miles or in longitude and latitude. Ex. 1006, Abstract, 5:9-13, 5:1422; 5:52-64, 8:27-30, 9:15-17. It would have been obvious to a person of ordinary skill in the art that all tiles in a particular zoom layer would thus have a same pixel resolution. Similarly, in Ligtenberg, the reduced resolution tiles are obtained by using a same decimation filter on a higher resolution image. A person of ordinary skill in the art would have understood that resulting images obtained by filtering and decimating a starting image would all have the same pixel resolution. Ex. 1005, Abstract, 2:56-62, 6:52-57, 7:19-21, 7:57-8:11, 11:62-66, Ligtenberg's (LayerImage data structure defined in Appendix A).
237.2 Element 1.G wherein image data has a color or bit per pixel depth representing a data parcel size of a predetermined number of bytes; In my opinion, in addition to the reasons I have discussed earlier with respect to element 1.E, this claim element would have been obvious because Ligtenberg further uses bit pixel depth that has a predetermined number of bytes, as listed in Ligtenberg's code in Appendix A, e.g., 8-bit or 12 bit gray scale or RGB or CMYK images. Id., 13:5-12. In my opinion, Ligtenberg's bits per pixel assignment was an obvious implementation choice for a person of ordinary skill in the art because assigning
equal number of bytes per pixel to represent color value of a pixel allows for a straightforward software or hardware implementation by assigning a same type of variable, e.g., integer, to an array that holds all pixels of the image parcel.
238. Element 1.H resolution of the series $\mathrm{K}_{\underline{1-N}}$ of derivative images being related to that of the source image data or predecessor image in the series by a factor of two; In my opinion, this element is obvious over the combined teachings of Rutledge, Ligtenberg, and Cooper. Ligtenberg teaches the use of layers of tile blocks of varying resolutions, which may be related by a reduction of a factor of two in one embodiment. Ex. 1005, 2:56-62; 5:39-43, 2:9-22, 2:25-38, 5:21-27, 5:34-53, 7:19-21, 9:6-20, Appendix A. Rutledge discloses using zoom layers, where each zoom layer can be a factor of eight greater in scale from one zoom layer below it. Ex. 1006, 2:31-38; 5:15-24, 4:41-47, 5:50-64, FIG. 3. In my opinion, a person of ordinary skill in the art would recognize that utilizing a factor of two or multiple of two as the relationship between successive derivative layers would simplify the processes of generating and rendering successive images, because each pixel in the derivative image represents an integral number of pixels in the successor image, as illustrated by Fig. 1.7 of App. B (Samet), which I discussed in § VI.C above. The choice of what factor of two to use $(2,4,8)$ would have been an obvious design choice driven by well-known considerations such as
how much storage the designer wanted to use for successive layers, how many intermediate layers were desired for transmission and progressive resolution rendering, etc.
239. Element 1.I said array subdivision being related by a factor of
two; As I discussed above in regard to Claim 1.H, the array subdivisions of Rutledge and Ligtenberg are related by a factor of two. A person of ordinary skill in the art would have been motivated to combine the references for the same reasons as described in 1.H.
240. Element 1.J such that each image parcel being of a fixed byte
size, Ligtenberg teaches the use of fixed size image parcels, e.g., $64 \times 64$ or 128x128 pixel resolution parcels for each layer of resolution. Ex. 1005, Abstract, 1:42-56, 2:31-38, Abstract, 13:30-37. Since each tile in a layer has the same size ("fTileSize"), uses the same number of bits for each pixel and uses the same compression method or no compression, in my opinion, it would be obvious that each image parcel could have the same fixed byte size. Id. Ligtenberg further teaches that the system may use a compression regime that compresses to a fixed size. Id. at 6:51-57. In my opinion, using a fixed size and fixed compression ratio could improve predictability of the system because the caching process would always need to use the same amount of space for a particular tile in the cache,
which makes the caching process more straightforward. An analogy would be stacking cubic boxes of the same size in a room, compared with stacking boxes of all different sizes and shapes. Therefore, it is my opinion that this teaching of Ligtenberg could provide similar benefits when used in the system of Rutledge or Cooper and that a person of ordinary skill in the art would recognize that benefit.
241. Element 1.K wherein the processing further comprises compressing each data parcel; Ligtenberg teaches that tiles may be compressed using the well-known JPEG standard or another regime which compresses to a fixed size. Ex. 1005, Abstract, 1:42-56, 2:31-38, 6:51-57, 13:30-37. In my opinion, each of Ligtenberg, Rutledge, and Cooper addresses a common issue relating to retrieving data over a network, and image compression was a well-known solution to the problem of optimizing bandwidth use for image transmission over a network.
242. Element 1.L storing each data parcel on the remote computer in a file of defined configuration such that a data parcel can be located by specification of a $\mathrm{K}_{\underline{D}}, \mathrm{X}, \mathrm{Y}$ value that represents the data set resolution index D and corresponding image array coordinate; Ligtenberg discloses a file format for storing image data which includes a defined file format for imagery tiles, shown as Appendix A to Ex. 1005. The designated file format includes values for identifying the offset to the lossless layer, i.e. how many layers removed from the source data
each tile is (FileOffset fLayers), as well as width and height values. Ex. 1005, 12:60:66; 13:29-38. Imagery can be retrieved based on the location and its offset level. Id. at 11:31-57. Rutledge also teaches that tiles are retrieved based on the zoom layer and geographic coordinates. Ex. 1006, Fig. 5, 7:63-8:44. In my opinion, these references contain teachings of similar solutions to similar problems, and a person of ordinary skill in the art would readily recognize that a system for displaying map imagery would need a means of identifying the coordinates and zoom level of the tiles used to display that imagery.
243. Element 1.M receiving said update data parcel from the data parcel stored in the remote computer over a communications channel: In my opinion, this element is substantially similar to the preamble of claim 1. I previously discussed in regard to the preamble how Ligtenberg, Rutledge, and Cooper teach receiving image data tiles from a remote computer over a communications channel, and in my opinion the same teachings are applicable to this element.
244. Element 1.N displaying on the limited communication bandwidth computer device using the update data parcel that is a part of said predetermined image, an image wherein said update data parcel uniquely forms a discrete portion of said predetermined image. In my opinion, this element is taught
by Ligtenberg and Rutledge. Ligtenberg teaches that image tiles are transferred in a format in which the tile location is specified by an X and Y offset in the image array. Therefore, each tile has a corresponding location within the image. Ex. 1005, Appendix A, 10:9-21. The received tiles are used for displaying images. Id. Each tile, which has a different X or Y offset than another tile, therefore uniquely forms its own or discrete portion of the image.
245. As I previously discussed in regard to claim element 1.L, Rutledge teaches that map tiles can be retrieved based on zoom layer and geographic coordinates. When the user changes the zoom level, the client requests tiles of the appropriate zoom layer, which are transferred from the map server to the user's device. Each map tile is defined by its own latitude and longitude and corresponds to an area of a given size, e.g., 200 feet wide or 3 miles wide, and thus forms a discrete, unique portion of the map image. Ex. 1006, 4:41-47, 5:14-64, 7:48-62.
246. Claim 2. The method of claim 1, wherein the update data parcel further comprises one of an image parcel textual mapping, a map parcel, a navigation cue, a text overlay and a topography. In my opinion, this claim element is disclosed by Rutledge. Rutledge teaches that the information provided in map tiles may include image data such as satellite or aerial photos as well as objects that include text strings, the image data, e.g., filled polygons, navigation cues such as
longitudinal and latitude data, orientation, etc., text overlay information such as location labels, and topography, e.g., building outlines, parks, bodies of water, etc. Ex 1006, 4:16-28, 4:41-64, 6:6-10, Table 1.
247. Claim 4. The method of claim 1, wherein the predetermined pixel resolution for each data parcel is a power of 2. In my opinion, this element is disclosed by Ligtenberg, which teaches the use of image data tiles in arrays that are powers of two, such as 64 X 64 or 128 X 128. Ex. 1005, 6:7-12; 7:8-21.
248. Claim 5. The method of claim 4, wherein the predetermined pixel resolution is one of $32 \times 32,64 \times 64,128 \times 128$ and $256 \times 256$. As I discussed above in regard to claim 4, Ligtenberg teaches the use of image data tiles measuring 64 X 64 or 128 X 128. Id.
249. Claim 6. The method of claim 1 wherein said communications channel is a packetized communications channel and wherein said update data parcel is received from said packetized communications channel in one or more data packets. As I discussed in regard to the preamble of claim 1, it is obvious that the systems taught by Rutledge, Ligtenberg, and Cooper would be implemented using packetized data channels, such as the internet or a local area network using TCP/IP. Therefore, in my opinion, it would be obvious that tiles would be received from the server in one or more TCP/IP packets in these systems.
250. Claim 7. The method of claim 6 wherein the data packet contains an update image parcel as a compressed data representation of said discrete portion of said predetermined image. In my opinion, Ligtenberg discloses this feature because Ligtenberg teaches using a compression technique such as JPEG to compress image tiles. Ex. 1005, 1:16-19; 1:34-56; 5:13-17; Appendix A.
251. Claim 8. The method of claim 7 wherein said data packet contains said update image parcel as a fixed compression ratio representation of said discrete portion of said predetermined image. As I discussed above in regard to claim element 1.J, it would be obvious that uncompressed tiles having the same resolution and bit per pixel depth would have the same resulting image file size. Additionally, Ligtenberg teaches that a compression method that compresses to a fixed file size may be used. Ex. 1005, 6:51-57. In my opinion, when the uncompressed size of each tile is always the same and the tile is always compressed to the same file size, the result is a fixed compression ratio. Therefore, Ligtenberg teaches a fixed compression ratio.
252. Claim 9. The method of claim 7, wherein said update image parcel contains pixel data in a fixed size array independent of the pixel resolution of said predetermined image. Ligtenberg teaches using a tile size of fixed size, e.g., $64 \times 64$ or $128 \times 128$, without any dependence on the pixel resolution of the image. Ex.

1005, 2:56-62; 6:52-57; 7:19-21. It would be obvious to a person of ordinary skill in the art that the tiles in the power-of-two array are all the same size (i.e., the same number of pixels at each level of resolution) regardless of the resolution of the underlying image, and that the tile server system may resample tiles on a grid and adjust them to the appropriate scaling and coordinates independent of the resolution of the underlying image. In my opinion, the use of fixed size tiles as taught by Ligtenberg provides a ready method to render a portion of a large image or progressively enhance the resolution of an image as it is downloaded, and such fixed tile sizes need not be dependent on the original resolution of the predetermined image. In particular, in a system such as Rutledge that integrates a variety of data types from a variety of sources, the underlying source data may have different resolutions but a common size for processed tiles enables the display system to integrate the display. Therefore, in my opinion, a person of ordinary skill in the art would recognize that the fixed tile resolution taught by Ligtenberg would provide this benefit in the mapping system taught by Rutledge.
253. Element 10.A The method of claim 1, wherein issuing the request for an update data parcel further comprises preparing the request by associating a prioritization value to said request: In my opinion, this element is taught by Cooper. Cooper teaches the use of an object assessment function which maintains a list of
visible objects in the priority queue. When a scene updates, e.g., when user's viewpoint changes, all objects in the queue are reprioritized according to the importance of objects with respect to the viewer's perspective. For example, objects closer to the user's focal point (e.g. the center of the screen) are given higher priority than objects near the periphery of the view. An object assessment function 22 determines a priority value for each visible object among the objects in object list 20 and orders the list of objects in priority queue 24 correspondingly. A streaming function sends requests to the server for three dimensional imagery data starting with the most important object first. Ex. 1007, 4:48-60, 6:27-32, 7:16-44, 9:65-10:2. In this way, the system of Cooper can prioritize its requests for graphics data (polygons or textures) to obtain data at the highest resolution where it contributes the most to the perceived quality of the image, because the human eye has much higher resolution near the center of the visual field than around the periphery.
254. In my opinion, Cooper is analogous art to Rutledge and Ligtenberg because all three references address problems related to the real-time display of spatially-organized imagery obtained over a network. All of these references accordingly deal with issues of optimizing the use of limited bandwidth in order to support display of images. Cooper teaches a method for optimizing the use of
limited bandwidth by prioritizing portions of the data that contribute the most to the user's immediate view. In my opinion, a person of ordinary skill in the art would recognize that the prioritization scheme taught by Cooper could be applied to a three-dimensional map system (which is basically what a virtual reality environment is, only with simulated coordinates rather than real) and to access map imagery as taught by Rutledge, which would be further enhanced by the tiling system and file format taught by Ligtenberg. It is also my opinion that a person of ordinary skill in the art would have been capable of combining the teachings of these references because Rutledge and Ligtenberg store imagery in a tiled hierarchical format, while it was well-known in the art that three-dimensional imaging systems like that in Cooper could be implemented using a tiled or "mipmap" texturing structure, like that I discussed earlier in this declaration in regard to the OpenGL standard.
255. Element 10.B wherein said prioritization value is based on the resolution of said update data parcel relative to that of other data parcels previously received by the limited communication bandwidth computer device: In my opinion, Cooper teaches or suggests this element. Cooper discloses that the priority values assigned to visual data objects in the priority queue depend on the data deficit for that object, i.e., how many polygons for the object have yet to be received. Ex.

1007, Abstract, 5:65-6:4; 6:13-21; 6:51-61; 7:12-20; 10:7-11; 10:40-45; 11:15-19. When the amount of data received for an object is sufficient to render the object with sufficient detail, that object is removed from priority order. Id. Cooper therefore discloses prioritization of further data requests based on data parcels previously requested. Ligtenberg further teaches that image tiles may be prioritized to provide progressive resolution enhancement by downloading lower-resolution tiles first, followed by higher-resolution tiles or differential data. Ex. 1006, 9:6410:21. Therefore, Ligtenberg teaches requesting image tiles by priority (lowest to highest resolution) and that additional tiles are requested based on the resolution of those tiles previously received, because the additional tiles requested are those of higher resolution than those already received. In my opinion, a person of ordinary skill in the art would understand in light of the combination of teachings in Cooper and Ligtenberg that network communications channel bandwidth usage can be optimized in a 2D or 3D graphics scenario by utilizing prioritized requests for tiles, and these teachings would be readily applicable to a mapping application such as Rutledge.
256. Element 10.C wherein issuing said request is responsive to said prioritization value for issuing said request in a predefined prioritization order.

Cooper discloses an object assessment function at a client that maintains a list of
visible objects in a priority queue in accordance with an instantaneous viewpoint of a hypothetical viewer within a 3D environment. Ex. 1007, 4:48-51. Cooper also discloses a streaming function that manages the request and receipt of object data from the server by making requests in accordance with contents of the priority queue, starting with the most important objects. Id., Abstract, 4:61-62, 5:2-6, 5:1619, 7:6-11. In my opinion, this teaching and the teachings of Ligtenberg that I discussed in regard to claim 10.B would teach a person of ordinary skill in the art that a system for requesting imagery tiles online could optimize bandwidth my utilizing prioritization values when issuing requests, and that the known benefits of this teaching would be readily applicable to an online mapping system such as Rutledge.
257. Claim 11. The method of claim 10 , wherein said prioritization values is based on the relative distance of said update data parcel from said operator controlled image viewpoint. Cooper discloses that visual data objects are prioritized based on 3-dimensional location of a user's viewpoint, including distance from a focal point of the display. Ex. 1007, 7:48-52, 8:23-32, 9:1-12. In my opinion, a person of ordinary skill in the art would have recognized that the teaching in Cooper of sorting requests for data objects based on their proximity to the user and the user's focal point (i.e. based on how much the data object
contributes to the quality of the image, based on the well-known fact that the human eye and brain process visual information at much higher resolution near the center of the visual field) could be used according to its known advantage in a realtime online mapping application such as Rutledge, where it is also advantageous to prioritize the portions of the image contributing the most to the user's perception of image quality.
258. Element 13.Preamble A display system for displaying a large-scale image retrieved over a limited bandwidth communications channel, said display system comprising: The preamble of claim 13 is very similar to the preamble of claim 1, which I previously discussed. In my opinion, Rutledge, Ligtenberg, and Cooper collectively teach systems according to the claim.
259. Element 13.A a display of defined screen resolution for displaying a defined image; Rutledge discloses that images were displayed on a computer terminal 110. Ex. 1006, 5:24-47. Ligtenberg discloses that a display terminal is used for displaying images that have a known resolution measured in dots per inches (dpi). Ex 1005, Fig. 1, 1:63-67, 5:1-8. In my opinion, it would be obvious to a person of ordinary skill in the art that a digital display would necessarily have a finite resolution. It would further be obvious to a person of ordinary skill in the art that the rendering of images on that display would be
limited by the resolution of the screen or the defined area of the screen, i.e., the predetermined resolution of the image display. In other words, Rutledge, Ligtenberg, and Cooper, like the system described in the 343 Patent, generally teach software that is capable of operating on a generic client device including a display with a fixed resolution. For example, both LCD displays- which were already widespread in various types of computing devices long before the asserted priority date of the 343 Patent- and cathode ray tube (CRT) displays would normally have an inherently limited resolution. In the case of an LCD display, the predetermined resolution is because there are a fixed number of separate liquid crystal cells that can be independently addressed, while the screen of a CRT display would be typically be divided into a fixed number of red, green, and blue phosphors. My understanding of the "display" that a person of ordinary skill in the art would expect to use in combination with the systems of Rutledge, Ligtenberg, and Cooper is consistent with the teachings of the 343 Patent, which recites in the background that "[c]haracteristically, the client system 18, 20 displays are operated at some fixed resolution generally dependent on the underlying display hardware of the client systems 18, 20." Ex. 1001 at 5:40-43.
260. Element 13.B a memory providing for the storage of a plurality of image parcels: Cooper discloses a display device that access data from an object
data table for each visual data object. The received data objects are stored in an object data table and made available to a rendering program. Ex. 1007, 6:11-10:45 and FIG. 5. The retrieval is selective because the "most important objects in the scene for the current viewpoint are most accurately rendered." Id., 6:28-38. Cooper also teaches that the user device makes a determination of which object should be rendered at what level of detail. Id., 5:59-65, 1:54-65, 5:6-8, 6:28-32. Ligtenberg discloses a display that includes a display memory for storing pixels that appear on the display device. Ex. 1005, 5:1-8. An image available for display is sent to display memory. Id., 10:2-6. In my opinion, these references teach a local memory used for storing a plurality of tiles in a similar manner.
261. Element 13.C displayable over respective portions of a mesh corresponding to said defined image; In my opinion, this element is taught by Rutledge and Ligtenberg in a similar, related manner. Rutledge discloses the use of map tiles, thus showing a mesh arrangement of images. Ex. 1006, 7:48-62.

Similarly, Ligtenberg discloses the use of image tiles in the form of rectangular arrays. Ex. 1005, 2:31-38, 4:16-17, 5:39-43, 5:54-65, 6:7-12, 7:18-21.
262. Element 13.D a communications channel interface supporting the retrieval of a defined data parcel over a limited bandwidth communications
channel: Rutledge discloses a user terminal that receives map data via a
communication network. Ex. 1006, 1:22-23. Rutledge teaches a system that downloads maps as image tiles stored in a map database. Id., 3:50-55, 4:41-47, 6:38-43. The maps can be both raster and vector data from a wide variety of sources including satellite imagery, digitized maps and scanned images. Id., 4:4447. The visualization is dynamic because a user can pan and zoom in or out and navigate through the image. Id., Fig. 4D. Corresponding to the user's viewpoint changes, map tiles are transferred from the map database to the user terminal. Id., 7:41-45. Ligtenberg also discloses a technique in which image data that is stored as tiles of multiple resolutions is sent from a server to a client for selective displaying Ex. 1005, 1:16-42. In particular, Ligtenberg discloses a file format used for storage and transmission of map tiles with different resolutions. Id., Appendix A. Cooper discloses a technique for retrieving image object data from a server and rendering on a user device or a client device. The Cooper technique prioritizes which visual data objects to retrieve based on observer's viewpoint in order to efficiently utilize available network bandwidth. Ex. 1007, 6:11-24. In my opinion, since the purpose of all three of these systems is to receive data over an internet connection, it is readily apparent that the client devices disclosed by both devices would require a communications channel (e.g. a modem or wireless connection to the Internet) to receive tiles. I previously discussed the "limited bandwidth communications
channel" in regard to the preambles of claims 1 and 13, and the same teachings and discussion apply.
263. Element 13.E a processor coupled between said display, memory and communications channel interface, Ligtenberg discloses a processor coupled to several peripheral devices, including bus, memory, input/output, display, and file storage system. Ex. 1005, 4:28-34; 11:66-12:2. The invention disclosed in Rutledge and Cooper are both implemented by computers, which necessarily contain a processor. See generally Exs. 1006, 1007. Further, because the claimed functions interact with each of the display (e.g. rendering the image on the display), the memory (e.g. caching tiles on the client) and the communications channel interface (e.g. sending requests for and receiving tiles from the server), in my opinion it is obvious that the client systems taught by Rutledge, Ligtenberg, and Cooper would require a processor coupled between the display, memory, and communications channel interface.
264. Element 13.F said processor operative to select said defined data parcel, Rutledge teaches that a user can select a desired viewpoint by zooming and panning. Ex. 1006, 7:48-62. Thus, the processor in Rutledge is operative by the user to select "defined data parcel" -- map tiles corresponding to the currently displayed viewpoint. Id. Additionally, I previously described the process of
selecting a defined data parcel above in regard to claim element 1.B. In my opinion, since Cooper teaches that this function is performed by a portion of the browser software that would necessarily execute on a processor, it is my opinion that Cooper teaches that the processor that I previously discussed in regard to claim element 13.E is operative to select the defined data parcel.

## 265. Element 13.G retrieve said defined data parcel via said limited

 bandwidth communications channel interface for storage in said memory, Ligtenberg teaches retrieving reduced-size image data over a communication network to avoid the delay in transferring a large image. Ex. 1005, 1:16-19; 1:3242. The image data retrieved from the communication network are saved in the memory and then displayed. Id., 10:1-7. Additionally, I previously discussed the teachings of Rutledge and Cooper regarding a memory to store tiles received via the network in regard to claim element 13.B.266. Element 13.H render said defined data parcel over a discrete portion of said mesh to provide for a progressive resolution enhancement of said defined image on said display; Rutledge discloses that in response to a user's zoom command, map tiles with higher resolution and more details will be retrieved from the database server and displayed on the client device. Ex. 1006, 7:48-62; 10:10-17. Similarly, Ligtenberg teaches that tiles can have progressively smaller sizes, so that
"a single tile in one layer will correspond to a single (smaller) tile in the next reduced layer." Ex. 1005, 7:7-21.
267. Cooper discloses progressive object resolution improvement where visual data objects are requested in a priority order, starting from most important objects and progressing to least important objects. Ex. 1007, Abstract, 4:34-38, 4:48-58, 4:61-5:6, 6:16-24, 6:27-32, 7:12-16, 9:65-10:5. Cooper thus teaches prioritizing requests for data so as to more completely render those objects that contribute more to a scene. Id., 7:4-11.
268. Element 13.I a remote computer, coupled to the limited bandwidth communications channel, that delivers the defined data parcel; As I previously discussed for claim elements 1.Preamble and 1.A, Rutledge, Ligtenberg, and Cooper disclose a remote computer, i.e., a server, that delivers image data over a limited bandwidth communications channel. Ex. 1005, 1:16-19; 4:51-54; 12:4-6; Ex. 1006, 2:62-64; 3:37; 7:5-9;7:48-62; 10:10-19; Ex. 1007, Abstract; 2:23-29; 2:50-52; 3:49-53; 4:9-12; 4:19-27; 4:61-5:8; 6:5-10; 6:16-20; Fig. 1.
269. Element 13.J wherein delivering the defined data parcel further comprises processing source image data to obtain a series $\mathrm{K}_{1-\mathrm{N}}$ of derivative images of progressively lower image resolution: this claim element is substantially similar
to claim element 1.D of the 343 Patent; therefore, in my opinion, the same teachings that I previously discussed in regard to that claim element apply.
270. Element 13.K wherein series image $\mathrm{K}_{0}$ being subdivided into a regular array: this claim element is substantially similar to claim element $1 . E$ of the 343 Patent; therefore, in my opinion, the same teachings that I previously discussed in regard to that claim element apply.
271. Element 13.L wherein each resulting image parcel of the array has a predetermined pixel resolution: this claim element is substantially similar to claim element 1.F of the 343 Patent; therefore, in my opinion, the same teachings that I previously discussed in regard to that claim element apply.
272. Element 13.M wherein image data has a color or bit per pixel depth representing a data parcel size of a predetermined number of bytes: this claim element is substantially similar to claim element 1.G of the 343 Patent; therefore, in my opinion, the same teachings that I previously discussed in regard to that claim element apply.
273. Element 13.N resolution of the series $\mathrm{K}_{1-\mathrm{N}}$ of derivative images being related to that of the source image data or predecessor image in the series by a factor of two: this claim element is substantially similar to claim element 1.H of
the 343 Patent; therefore, in my opinion, the same teachings that I previously discussed in regard to that claim element apply.
274. Element $\mathbf{1 3 . 0}$ said array subdivision being related by a factor of two: this claim element is substantially similar to claim element 1.I of the 343 Patent; therefore, in my opinion, the same teachings that I previously discussed in regard to that claim element apply.
275. Element 13.P such that each image parcel being of a fixed byte size: this claim element is substantially similar to claim element 1.J of the 343 Patent; therefore, in my opinion, the same teachings that I previously discussed in regard to that claim element apply.
276. Element 13.Q wherein the processing further comprises compressing each data parcel: this claim element is substantially similar to claim element 1.K of the 343 Patent; therefore, in my opinion, the same teachings that I previously discussed in regard to that claim element apply.
277. Element 13.R storing each data parcel on the remote computer in a file of defined configuration such that a data parcel can be located by specification of a $K_{\underline{D}}, X, Y$ value that represents the data set resolution index D and corresponding image array coordinate: This claim element is substantially similar
to claim element 1.L of the 343 Patent; therefore, in my opinion, the same teachings that I previously discussed in regard to that claim element apply.
278. Claim 14. The display system of claim 13 , wherein said processor is responsive to said defined screen resolution and wherein said processor is operative to limit selection of said defined data parcel to where the resolution of said defined data parcel is less than or equal to said defined screen resolution.

Ligtenberg discloses that only a limited amount of tile data is needed for generating an image. Ex. 1005, 8:37-42, 8:60-65, 9:2-3. Rutledge discloses that only image data having the desired resolution need to be retrieved and displayed. Ex. 1006, 2:25-30; 3:17-20; 5:13-17; 7:38-47; 8:37-42; 10:1-7. It would have been obvious to a person of ordinary skill in the art that because displays have a finite resolution and because a display cannot display an image having a resolution greater than that of the display, the image parcel rendering would advantageously be limited to a resolution of no greater than screen resolution to save computational resources and memory usage.
279. Element 15.A The display system of claim 13, wherein said processor is operative to prioritize the retrieval of said data parcel among a plurality of selected data parcels pending retrieval, Cooper discloses prioritizing the retrieval of image data based on the visual importance of objects. Ex. 1007,

3:44-49; 4:47-60; 6:51-59. Rutledge and Ligtenberg also disclose prioritize the image data retrieval, based on, e.g., the areas visible to user's current viewpoint. Ex. 1006, 7:10-16; Ex. 1005, 8:36-43. In my opinion, these patents contain similar teachings of solutions to related problems, and therefore a person of ordinary skill in the art would have been motivated to consider the teachings of these references in combination.
280. Element 15.B wherein the relative priority of the data parcel is based on the difference in the resolution of the image parcel and the resolution of said plurality of selected data parcels. In my opinion, Cooper teaches or suggests this element. Cooper discloses that the priority values assigned to visual data objects in the priority queue depend on the data deficit for that object, i.e., how many polygons for the object have yet to be received. Ex. 1007, Abstract, 5:65-6:4; 6:13-21; 6:51-61; 7:12-20; 10:7-11; 10:40-45; 11:15-19. When the amount of data received for an object is sufficient to render the object with sufficient detail, that object is removed from priority order. Id. Cooper therefore discloses prioritization of data requests compared to other data parcels. Ligtenberg further teaches that image tiles may be prioritized to provide progressive resolution enhancement by downloading lower-resolution tiles first, followed by higher-resolution tiles or differential data. Ex. 1006, 9:64-10:21. Therefore, Ligtenberg teaches requesting
image tiles by priority (lowest to highest resolution). In my opinion, a person of ordinary skill in the art would understand in light of the combination of teachings in Cooper and Ligtenberg that network communications channel bandwidth usage can be optimized in a 2 D or 3D graphics scenario by utilizing prioritized requests for tiles, and these teachings would be readily applicable to a mapping application such as Rutledge.
281. Element 16.A The display system of claim 13, wherein said processor is response to user navigation commands to define an image viewpoint relative to said defined image; In my opinion, Rutledge and Cooper contain similar teachings in regard to this element. Rutledge discloses that a user can select a desired viewpoint by navigation commands such as panning and zooming. Ex. 1006, 3:5-10, 5:14-23, 4:41-47, 7:48-8:6, 9:11-17. A user in Cooper can determine a viewpoint relative to an image displayed in a three-dimensional space. Ex. 1007, Abstract, 1:6-10, 1:16-21, 1:23-29, 1:34-38, 3:16-54, 3:59-65, 4:14-19, 4:27-29, 4:39-47, 4:48-51, 5:26-36, 5:48-57. In my opinion, a person of ordinary skill in the art would recognize that the teachings of a viewpoint in three dimensions as taught in Cooper could be readily applied to a mapping application such as Rutledge, and as I discussed previously in Section VI this declaration, in fact such three-dimensional online mapping applications were well-known in the
art at the time. Additionally, a person of ordinary skill in the art would recognize that such a three-dimensional image viewpoint on a client device would naturally be determined by the processor in response to user commands.
282. Element 16.B wherein said processor is operative to prioritize the retrieval of said data parcel based on the distance between said image parcel and said image viewpoint relative to said defined image. In my opinion, this claim element is substantially similar to the additional element of claim 11, and in my opinion the same teachings apply here. Additionally, it is my opinion that because Rutledge, Ligtenberg, and Cooper discuss software executed on a client system, it would be obvious to a person of ordinary skill in the art that the prioritization of retrieval of image data is executed by a processor.
283. Claim 17. The display system of claim 13, wherein the data parcel further comprises one of an image parcel textual mapping, a map parcel, a navigation cue, a text overlay and a topography. This claim element is substantially similar to claim 2 of the 343 Patent; therefore, in my opinion, the same teachings that I previously discussed in regard to that claim element apply.
284. Claim 18. The display system of claim 13 , wherein the predetermined pixel resolution for each data parcel is a power of 2. This claim element is substantially similar to claim 4 of the 343 Patent; therefore, in my
opinion, the same teachings that I previously discussed in regard to that claim element apply.
285. Claim 19 The display system of claim 18 , wherein the predetermined pixel resolution is power of 2 and one of $32 \times 32,64 \times 64,128 \times 128$ and $256 \times 256$; This claim element is substantially similar to claim 5 of the 343 Patent; therefore, in my opinion, the same teachings that I previously discussed in regard to that claim element apply.
286. I have provided as Appendix V to this declaration a claim chart showing the exemplary teachings of Rutledge, Ligtenberg, and Cooper that are pertinent to claims 1, 2, 4-11 and 13-19 of the 343 Patent.

## D. GROUND 4: CLAIM 3 IS UNPATENTABLE UNDER 35 U.S.C. § 103(a) AS BEING OBVIOUS OVER RUTLEDGE IN VIEW OF LIGTENBERG, COOPER AND HASSAN

287. Claim 3. The method of claim 1, wherein the limited communication bandwidth computer device further comprises one of a mobile computer system, a cellular computer system, an embedded computer system, a handheld computer system, a personal digital assistants and an internet-capable digital phone. Ligtenberg teaches that the client computer system may be either a desktop or a portable system. Hassan, titled "Method for Transmitting Multiresolution Image Data in a Radio Frequency Communication System,"
describes a system in which a wireless client computer device such as a cell phone may request and receive images broken down into discrete levels of resolution over a wireless network from a server. Ex. 1012, Abstract, 1:20-25, 1:44-48, 1:55-57, 2:26-32, Fig. 5.
288. In my opinion, Hassan contains related teachings to Rutledge, Ligtenberg, and Cooper in regard to downloading images at varying levels of resolution. All of these references are directed to related issues in regard to downloading large-scale images on a system with constrained download and display resources, and therefore a person of ordinary skill in the art would consider these references to be analogous art. While Ligtenberg contains a suggestion that the client device may be a portable device, Hassan contains further details explaining how a portable client system such as a cell phone could optimize delivery of high-resolution images over a narrow-bandwidth channel. Therefore, in my opinion, it would have been obvious for a person of ordinary skill in the art to utilize Hassan's teaching of improvements for downloading multi-resolution images onto a mobile cellular device in combination with the mapping system of Rutledge and the multi-resolution progressive-resolution downloading and file format of Ligtenberg, in combination with the prioritization features of Cooper.
289. I have provided as Appendix V to this declaration a claim chart showing the exemplary teachings of Rutledge, Ligtenberg, Cooper, and Hassan that are pertinent to claim 3 of the 343 Patent.

## E. GROUND 5: CLAIMS 12 AND 20 ARE UNPATENTABLE UNDER 35 U.S.C. § 103(a) AS OBVIOUS OVER RUTLEDGE IN VIEW OF LIGTENBERG, COOPER AND AUSTRENG

290. In my opinion, claims 12 and 20 are disclosed and rendered obvious by Rutledge in view of Ligtenberg and Cooper and further in view of Austreng. The additional element of these claims is primarily that the client device executes multi-threading as part of the process of using the update data parcel to display the image. I previously explained the background concept of multi-threading and the general knowledge in the art of multi-threading above in regard to Ground 2. Austreng provides further teachings that teach this element. Specifically, Austreng teaches that a client computer can operate in a multi-threaded manner where one thread of execution displays the image, while another thread keeps downloading image data. Ex. 1008, 4:11-16, 6:13-22.
291. Like Rutledge, Ligtenberg, and Cooper, Austreng discloses a method of transferring digital image data from a server to a client for displaying at the client device. See, e.g., Id., Abstract; Figs. 1, 2, 5. A user can manipulate the displayed object by, e.g., rotating it using a mouse. Id., Abstract; Fig. 4. To shorten
the transmission time, the image data can be compressed using various method prior to being downloaded from the server. Id., Abstract. Therefore, in my opinion, Austreng is analogous art to Rutledge, Ligtenberg, and Cooper, and a person of ordinary skill in the art would recognize that the multi-threading mechanism of Austreng would provide similar benefits in the system collectively disclosed in Rutledge, Ligtenberg, and Cooper.
292. Claim 12. The method of claim 1, wherein displaying the image further comprises multi-threading on the limited communication bandwidth computer device using the update data parcel to display the image. In my opinion, for the reasons discussed above, Austreng teaches this claim element and a person of ordinary skill in the art would have viewed the combination of these teachings of Austreng with the teachings of Rutledge, Ligtenberg, and Cooper that I previously discussed in regard to claim 1 as obvious.
293. Claim 20. The display system of claim 13, wherein the processor performs multi-threading to render said defined data parcel over the discrete portion of said mesh to provide for the progressive resolution enhancement of said defined image on said display. In my opinion, the teachings of Austreng and reasons to combine that I previously discussed in regard to this ground also apply to this claim. I previously discussed progressive resolution enhancement in regard
to claim element 13.H. In my opinion, the progressive enhancement resolution methods that I previously discussed in regard to claim element 13. H could be executed by a dedicated rendering thread as taught by Austreng, and the multithreading arrangement of Austreng would provide similar known benefits in such a situation.
294. I have provided as Appendix V to this declaration a claim chart showing the exemplary teachings of Rutledge, Ligtenberg, Cooper, and Austreng that are pertinent to claims 12 and 20 of the 343 Patent.

## XI. OTHER PERTINENT GROUNDS OF PRIOR ART

295. The grounds of invalidity discussed above are contained in the

Microsoft IPR Petition on the 343 Patent. In my opinion, a large body of printed publications was made by others prior to the earliest purported invention date of the 343 Patent that describe the technical features and claimed subject matter of claims 1 to 20 of the 343 Patent. Referring back to Section VI entitled
"TECHNOLOGY BACKGROUND OF THE 343 PATENT" above, I cite various prior art references not in the Microsoft IPR Petition on the 343 Patent to show that technical features disclosed or claimed in the 343 Patent were described before the earliest priority date of the 343 Patent.
296. In the sections below, I provide additional invalidity grounds beyond the specific invalidity grounds in the Microsoft IPR Petition on the 343 Patent as examples of additional reasons why claims 1 to 20 contain obvious combinations of known technical features. Specifically, claims 1-11 and 13-19 are obvious over (1) Fuller in view of Hornbacker, (2) Yap in view of Rabinovich, (3) Fuller in view of Yap, and (4) Potmesil in view of Hornbacker and Cooper, and claims 12 and 20 are obvious over (1) Fuller in view of Hornbacker and Lawless, (2) Yap in view of Rabinovich, and (2) Fuller in view of Yap, as discussed below.
A. CLAIMS 1-20 ARE UNPATENTABLE UNDER 35 U.S.C. § 103(a) AS BEING OBVIOUS OVER FULLER IN VIEW OF HORNBACKER AND/OR LAWLESS
297. The MAGIC Project: From Vision to Reality authored by Barbara Fuller and Ira Richer ("Fuller") was published in the May/June 1996 issue of IEEE Network. App. E. Fuller was published more than one year before the earliest priority date of the 343 Patent and isprior art to the 343 Patent.
298. Fuller describes a networked system ("MAGIC") for visualizing image data rendered on a terrain model in three dimensions (p. 17). The system includes an image server system that stores and processes Digital Elevation Model ("DEM") terrain and aerial imagery data, then transmits that data upon request to remote client workstations equipped with a three-dimensional terrain visualization
application. Fig. 1, p. 16 ("Overview of the MAGIC testbed"). The DEM and aerial imagery data is organized into small, fixed-size tiles. Fig. 3, p. 17. The terrain visualization application identifies tiles that are needed to render a particular view or path and requests those tiles according to an assigned priority. Fig. 5, p. 19. Exemplary reasons to assign priority in tile requests is to obtain lower-resolution tiles first to display a coarse image while higher-resolution tiles are still being downloaded, to obtain near tiles first if the viewpoint of the visualization application is moving across a landscape, and to pre-cache tiles that may be used in the near future. Id. The three-dimensional image rendering mode generates a three-dimensional model of the terrain from the DEM and superimposes the aerial imagery from the imagery tiles on the terrain. P. 17-18, fig. 4. The visualization application may display high-resolution tiles for terrain near the viewpoint and low-resolution tiles for distant terrain. P. 17.
299. As can be seen from the summary above, the teachings in Fuller are similar to the teachings in Potmesil. Therefore, most of the reasons for a person of ordinary skill in the art to combine Potmesil and Hornbacker are equally applicable for combining Fuller and Hornbacker.
300. Specifically, a person of ordinary skill in the art would be motivated to combine Fuller and Hornbacker because they both address common technical
issues relating to visualizing large amounts of data obtained over a data network, using a client viewing device with much smaller memory than the database which stores the imagery data. In this regard, both Fuller and Hornbacker address similar or the same technical problems in rendering the images on the client device from image data received over a data network (e.g. optimizing bandwidth, prioritizing use of bandwidth, determining which portions of a larger set of image data to request, etc.).
301. Fuller specifically discloses uses of its technology in terrain visualization applications and map applications. The teachings of Hornbacker are readily applicable to online mapping references because online maps represent a scenario in which a much larger amount of geographically organized imagery must be stored on a server than can be stored at one time on a client. The European counterpart of Hornbacker, EP1070290, specifically recognizes the relevance of teachings relating to mapping to the disclosure of Hornbacker by citing and explaining several online mapping references in the description of the prior art. Ex. 1011 at [0006], [0007]. Accordingly a person of ordinary skill in the art would be motivated to consider the teachings of the references in designing a mapping application designed to view map data over a limited bandwidth communications channel.

## 1. Claims 1-11 and 13-19 are Rendered Obvious by Fuller and

 Hornbacker302. Element 1.Preamble A method of retrieving large-scale images over network communications channels for display on a limited communication bandwidth computer device, said method comprising: Fuller teaches a client system for retrieving large-scale images over network communications channels, and then display the retrieved image. Fuller at Abstract; Fig. 1.
303. Fuller also teaches that avoiding excessive bandwidth use and preventing delays associated with data retrieval is an intended feature of the system. See, e.g. Fuller at 15 (network delays), 18-19 (design considerations), 21
("performance"). Fuller also suggests that it is desirable to adapt the technology described therein to systems that can deliver processed data to "end users with a range of communications speeds, link qualities, computational powers, and display capabilities." Fuller at 25. For example, applications may include "military operations, intelligence imagery analysis, and natural disaster response," all situations in which remote access to imagery data as described throughout Fuller using devices having limited communication bandwidth is advantageous. Id. Fuller specifically suggests "mobile access to backbone services." Id.
304. Fuller suggests the use of its system to provide map data to devices having a range of communications speeds and link qualities, including mobile devices connected over wireless networks. Fuller at 25.
305. Relevant teachings of Hornbacker for this claim element have been discussed in Ground 1.
306. A person of ordinary skill in the art would recognize that the compression techniques taught by Hornbacker could advantageously be used to implement the connection over a mobile network suggested by Fuller.

Additionally, a person of ordinary skill in the art would recognize that the system of Fuller could readily be adapted to provide 2D or 3D image data to a device with a low bandwidth connection, such as a remote computer device used in a disaster response, by making readily known trade-offs such as decreasing the frame rate of the visualization.
307. Element 1.A issuing, from a limited communication bandwidth computer device to a remote computer, a request for an update data parcel Fuller teaches a client system that issues requests for update data parcels in the form of image tiles from a network server. Fuller at Abstract, Fig. 1. As a specific example, the disclosed technology in Fuller is used for an innovative terrain visualization application that requires massive amounts of remotely stored data and was tested in
a 3-year project from 1992 to 1995 known as MAGIC ( "Multidimensional Applications and Gigabit Internetwork Consortium"). Fuller at 15. TerraVision for terrain visualization application in MAGIC allows a user to view and navigate through (i.e., "fly over") a representation of a landscape created from aerial or satellite imagery. The data used by TerraVision are derived from raw imagery and elevation information which have been preprocessed by a companion application known as TerraForm. TerraVision requires very large amounts of data in real time, transferred at both very bursty and high steady rates. Fuller at 17.
308. In order to render an image, TerraVision requires a digital description of the shape and appearance of the subject terrain. The shape of the terrain is represented by a two-dimensional grid of elevation values known as a digital elevation model ("DEM"). The appearance of the terrain is represented by a set of aerial images, known as orthographic projection images (ortho-images), that have been specially processed (i.e., ortho-rectified) to eliminate the effects of perspective distortion, and are in precise alignment with the DEM. Low-resolution tiles are required for terrain that is distant from the viewpoint, whereas highresolution tiles are required for close-in terrain. In addition, multiple resolutions are required to achieve perspective. These requirements are addressed by preparing a hierarchy of increasingly lower-resolution representations of the DEM and ortho-
image tiles in which each level is at half the resolution of the previous level. The tiled, multiresolution hierarchy and the use of multiple resolutions to achieve perspective are shown in Fig. 3. Fuller at 17. Registration of the user's viewpoint to a map enables the user to specify the area he wishes to explore by pointing to it, and it aids the user in orienting himself. Fuller at 18. See also Fuller at 25 on "Future Work" for MAGIC II.
309. Relevant teachings in Hornbacker for this claim element have been discussed previously in Ground 1.
310. As I discussed above, a person of ordinary skill in the art would recognize the applicability of the teachings of Hornbacker to a map application, as shown by the description of several map display-related references in the corresponding EU patent for Hornbacker. Therefore, a person of ordinary skill in the art would be motivated to combine the teachings of Hornbacker and Fuller when, for example, designing online mapping applications.
311. Element 1.B wherein the update data parcel is selected based on an operator controlled image viewpoint on the computer device relative to a predetermined image: Fuller teaches a terrain visualization application, known as "TerraVision," which generates a perspective view of rendered terrain based on user navigation commands. Fuller at 17-19, Figs. 3-5.


Figure 3. Relationship between tile resolutions and perspective view. (Source: SRI International)


Aerial terrain image is mapped onto elevation model


Elevation data rendered with orthographic image of terrain
Figure 4. Mapping an ortho-image onto its digital elevation model. (Source: SRI International)


Figure 5. Schematic representation of the operation of the ISS. (Source: Lawrence Berkeley National Laboratory)
312. Hornbacker also discloses that the required image file is selected based on an image viewpoint selected by a user. Hornbacker at 5:16-25; 7:11-25; 13:11-14:16; Fig. 2.
313. Element 1.C the update data parcel contains data that is used to generate a display on the limited communication bandwidth computer device; Both Fuller (p.18) and Hornbacker (Abstract; 8:7-15) discloses rendering the image tiles to generate a display on the client device.
314. Element 1.D processing, on the remote computer, source image data to obtain a series $\mathrm{K}_{1-N}$ of derivative images of progressively lower image resolution: Fuller teaches that source image data is pre-processed to tiles containing a hierarchy of increasingly lower-resolution images of the DEM and aerial imagery in which each level is at half the resolution of the previous level. Fuller at p. 17; Fig. 3. Fuller also motivates a person of skill in the art to modify the system to perform processing of the tiles on the same server that distributes the tiles. Specifically, Fuller teaches that it is desirable to use the technology of the reference to provide access to data from a variety of sources in "real-time" shortly after data is generated, e.g. in a scenario involving military operations, intelligence imagery analysis, and natural disaster response. Id. at 25 .
315. Relevant teachings of Hornbacker for this claim element have been discussed in Ground 1.
316. It is my opinion that it would be obvious to a person of ordinary skill in the art to combine these two references, because Fuller provides a suggestion that real-time processing of images on the server is desirable in order to support applications that would demand rapid production of image tiles from different underlying image data sources, while Hornbacker teaches methods for processing source data in real-time on the server from a variety of potential image sources. A
person of ordinary skill in the art would recognize that the real-time server-side processing features of Hornbacker would readily meet the need for real-time generation and transmission of image tiles discussed in Fuller.
317. Element 1.E wherein series image $\mathrm{K}_{0}$ being subdivided into a regular array: In my opinion, Fuller and Hornbacker both teach this element in substantially identical ways, in which a large-scale image is divided into a regular array of individual map tiles. Fuller at p. 17; Fig. 3; Hornbacker at 6:13-19; 7:1115; 8:30-9:28; 10:7-10.
318. Element 1.F wherein each resulting image parcel of the array has a predetermined pixel resolution: In my opinion, Fuller and Hornbacker both teach this element because the references teach the use of image tiles having a fixed resolution for each tile, including a multi-resolution "pyramid" tile structure where each level includes tiles at a fixed resolution. Fuller at 17, 21, Fig. 3; Hornbacker at 6:20-7:25, 8:30-9:28, 10:3-10, 11:19-28, 12:21-13:10, 13:26-14:6.
319. Element 1.G wherein image data has a color or bit per pixel depth representing a data parcel size of a predetermined number of bytes: It is my opinion that Fuller and Hornbacker both teach solutions that involve image parcels (tiles) that contain a predetermined number of bytes (e.g. 128 X 128 pixels with 24
bits of color information). Fuller at p. 21; Hornbacker, 6:13-7:25, 8:7-15, 10:11-23; 12:2-16.
320. Element 1.H resolution of the series $\mathrm{K}_{1-N}$ of derivative images being related to that of the source image data or predecessor image in the series by a factor of two: Fuller and Hornbacker both teach that image data tiles' resolutions in adjacent levels are related by a factor of two. Fuller at Fig. 3; Hornbacker at 6:13-7:25, 8:7-15.
321. Element 1.I said array subdivision being related by a factor of two: Fuller and Hornbacker both teach that the subdivision of image data tiles in adjacent levels are related by a factor of two. Fuller at Fig. 3; Hornbacker at 6:137:25, 8:7-15.
322. Element 1.J such that each image parcel being of a fixed byte size, Relevant teachings of Hornbacker for this claim element have been discussed in Ground 1.
323. A person of ordinary skill in the art would recognize that Fuller and Hornbacker address similar problems regarding optimizing the use of bandwidth to download large images over resource-constrained tiles and reach similar solutions by using tiles sorted by priority and image compression. A person of ordinary skill in the art would recognize that Hornbacker's teaching of using fixed byte size tiles
to improve the caching mechanism would provide the same benefit in the system of Fuller.

## 324. Element 1.K wherein the processing further comprises

 compressing each data parcel: Relevant teachings of Hornbacker for this claim element have been discussed in Ground 1.325. Fuller suggests the use of its system to provide map data to devices having a range of communications speeds and link qualities, including mobile devices connected over wireless networks, which requires reducing the amount of data transmitted over a network. Hornbacker teaches that the use of compression for image tiles may be used to reduce the necessary bandwidth to transmit such data, e.g. over a conventional 28.8 kbaud modem. Therefore, a person of ordinary skill in the art would recognize that the compression techniques taught by Hornbacker could advantageously be used to implement the connection over a mobile network suggested by Fuller.
326. Element 1.L storing each data parcel on the remote computer in a file of defined configuration such that a data parcel can be located by specification of a $K_{\underline{D}}, X, Y$ value that represents the data set resolution index D and corresponding image array coordinate; Fuller teaches that tiles are stored on server disks and each tile has its own tile identifier. Fuller at pp. 17, 19; Figs. 3, 5.

Relevant teachings of Hornbacker for this claim element have been discussed in Ground 1.
327. Fuller and Hornbacker contain overlapping, related teachings showing that individual image tiles are stored in such a way that an individual tile may readily be identified by its location and resolution. Hornbacker teaches that requests for individual tiles may take the form of a URL that specifies zoom and location. It would be readily apparent to a person of ordinary skill in the art that the URL request form specified by Hornbacker could be readily applied to the tile request process of Fuller to identify specific needed tiles as described by Fuller.
328. Element 1.M receiving said update data parcel from the data parcel stored in the remote computer over a communications channel: Fuller and Hornbacker provide independent teachings that a plurality of image tiles are stored at a remote server and received over a computer network. Fuller at Fig. 1, pp. 15, 17, 19-21; Hornbacker at Abstract, 3:10-27, 5:3-6:19.

## 329. Element 1.N displaying on the limited communication

 bandwidth computer device using the update data parcel that is a part of said predetermined image, an image wherein said update data parcel uniquely forms a discrete portion of said predetermined image. Fuller teaches that image tiles representing sections of aerial images are uniquely used for the correspondingportions of a map, which are either rendered as corresponding portions of a 2D model or aligned with the elevation model for a 3D image and rendered as textures on the elevation model. Fuller Figs. 3, 4, pp. 17, 18.
330. Relevant teachings in Hornbacker for this claim element have been discussed previously in Ground 1.
331. Claim 2. The method of claim 1, wherein the update data parcel further comprises one of an image parcel textual mapping, a map parcel, a navigation cue, a text overlay and a topography. The update data parcel in Fuller can be a map parcel, a navigation cue, or a topography. Fuller at pp. 17-19, Figs. 4 and 5.
332. Claim 3. The method of claim 1, wherein the limited communication bandwidth computer device further comprises one of a mobile computer system, a cellular computer system, an embedded computer system, a handheld computer system, a personal digital assistants and an internet-capable digital phone. Fuller suggests that the system described therein may be modified to enable mobile access to services. Fuller at p. 25.
333. Claim 4. The method of claim 1, wherein the predetermined pixel resolution for each data parcel is a power of 2. Both Fuller and Hornbacker
disclose a tile having a pixel resolution that is a power of 2, e.g., 128 X 128 pixels. Fuller at p. 21; Hornbacker at 6:20-7:25; 8:30-9:16; 14:2-6.
334. Claim 5. The method of claim 4, wherein the predetermined pixel resolution is one of $32 \times 32,64 \times 64,128 \times 128$ and $256 \times 256$. As discussed for claim 4 above, both Fuller and Hornbacker disclose a pixel resolution of 128 X 128. Fuller at p. 21; Hornbacker at 6:20-7:25; 8:30-9:16; 14:2-6. Hornbacker also discloses the pixel resolution of $256 \times 256$. Hornbacker at 7:11-25.
335. Claim 6. The method of claim 1 wherein said communications channel is a packetized communications channel and wherein said update data parcel is received from said packetized communications channel in one or more data packets. Fuller and Hornbacker both teach that the systems disclosed therein transmit tiles under the TCP/IP protocol, which is a packetized transmission format. Fuller at pp. 16-17; Hornbacker at Abstract; 4:24-5:25; 6:20-7:25; 8:7-15; 13:26-14:6.
336. Claim 7. The method of claim 6 wherein the data packet contains an update image parcel as a compressed data representation of said discrete portion of said predetermined image. See discussions for claim element 1.K in this Ground and discussions for claim 7 in Ground 1.
337. Claim 8. The method of claim 7 wherein said data packet contains said update image parcel as a fixed compression ratio representation of said discrete portion of said predetermined image. Relevant teachings in Hornbacker for this claim have been discussed previously in Ground 1.
338. For the reasons described above in regard to claim element 1.K, a person of ordinary skill in the art would recognize that the compression techniques described in Hornbacker would improve the system described in Fuller by enabling less bandwidth to be used. A person of ordinary skill in the art would further recognize that a fixed compression ratio would further improve efficiency by making each packet containing a tile having the same size.
339. Claim 9. The method of claim 7, wherein said update image parcel contains pixel data in a fixed size array independent of the pixel resolution of said predetermined image. See discussions for claim element 1.L in this Ground and discussions for claim 9 in Ground 1.
340. Claim Element 10.A The method of claim 1, wherein issuing the request for an update data parcel further comprises preparing the request by associating a prioritization value to said request: Fuller discloses assigning one of three levels of priority to each map tile requested: priority-1 for tiles that are needed as soon as possible, priority-2 for the tiles that are needed, but should be
transmitted only if there are no priority-1 tiles awaiting transfer, and priority- 3 for tiles that are less likely to be needed. Fuller at p. 19.
341. Relevant teachings in Hornbacker for this claim have been discussed previously in Ground 1.
342. Claim Element 10.B wherein said prioritization value is based on
the resolution of said update data parcel relative to that of other data parcels previously received by the limited communication bandwidth computer device:

Fuller teaches prioritization based on relative tile resolution because Fuller's rendering algorithm needs the coarse tiles before it needs the next-higherresolution tiles. Fuller at p. 19.
343. Relevant teachings in Hornbacker for this claim have been discussed previously in Ground 1.
344. It is my opinion that Fuller and Hornbacker teach three related, complementary reasons why prioritization values in a request queue for image tiles may be based on the relative resolution of a requested tile relative to those that have already been downloaded. First, the references teach that progressive resolution display may be used to download lower resolution images before higher resolution images in order to display part of an image even when the high resolution tiles are not yet available due to network constraints. Second, Fuller also
teaches that as the user viewpoint moves toward a location, tiles previously represented by lower resolution tiles when the location was distant may be replaced by higher resolution tiles. Finally, both Fuller and Hornbacker teach, and it would be obvious to a person of ordinary skill in the art, not to retrieve tiles that have already been retrieved and stored in order to avoid wasting bandwidth. It would be readily apparent to a person of ordinary skill in the art that these overlapping, complementary teachings could be employed in the same system using packets corresponding to image tiles.
345. Claim Element 10.C wherein issuing said request is responsive to said prioritization value for issuing said request in a predefined prioritization order. Responsive to the prioritization value, Fuller's TerraVision image visualization application issues a prioritized list of new tiles to be requested from the server. See, e.g. Fuller at Abstract, Fig. 5, pp. 17-19.
346. Relevant teachings in Hornbacker for this claim element have been discussed previously in Ground 1.
347. Claim 11. The method of claim 10 , wherein said prioritization values is based on the relative distance of said update data parcel from said operator controlled image viewpoint. Fig. 5 of Fuller shows that the list of tiles to
be retrieved first requests tiles nearest the initial viewpoint along the path of travel controlled by the user. See also Fuller at Fig. 3, pp. 17-19.
348. A person of ordinary skill in the art would recognize in light of wellknown principles of computer graphics that tiles in a power-of-two pyramid used for rendering (such as in the OpenGL standard), are preferably filtered based on the proximity of the object being rendered to the user's view point, which in turn can be used to determine the highest resolution that can be rendered.

## Claim 13:

349. Element 13.Preamble A display system for displaying a large-scale image retrieved over a limited bandwidth communications channel, said display system comprising: See discussions for claim element 1.Preamble.
350. Element 13.A a display of defined screen resolution for displaying a defined image; Fuller teaches that the system is coupled to a workstation having a display with a full-screen resolution taking up about 100 tiles. Fuller, p. 18, 21.
351. Relevant teachings in Hornbacker for this claim element have been discussed previously in Ground 1.
352. It would be obvious to a person of ordinary skill in the art that any digital display would necessarily have a defined resolution.
353. Element 13.B a memory providing for the storage of a plurality of image parcels: Fuller teaches that retrieved tiles may be stored in a cache memory on the visualization system both for immediate display of tiles and so that tiles covering adjacent areas likely to be used may be retrieved quickly if they are needed. Fuller at 18 .
354. Relevant teachings in Hornbacker for this claim element have been discussed previously in Ground 1.
355. Thus, Fuller and Hornbacker both teach that a local cache memory on a client display device is advantageous to enable rapid display of pre-cached tiles and minimize delays associated with downloading. A person of ordinary skill in the art would recognize that the references teach similar solutions (caching previously received tiles) to similar problems of enhancing display speed and avoiding downloading tiles that the client device already has.
356. Element 13.C displayable over respective portions of a mesh corresponding to said defined image; See discussions for claim element 1.E.
357. Element 13.D a communications channel interface supporting the retrieval of a defined data parcel over a limited bandwidth communications channel; Fuller discloses that map tiles can be retrieved over the MAGIC Internetwork. Fuller at p. 16; Figs 1 and 2.
358. Relevant teachings in Hornbacker for this claim element have been discussed previously in Ground 1.
359. Element 13.E a processor coupled between said display, memory and communications channel interface, Both Fuller and Hornbacker teach systems that are designed to operate in connection with a computing device. See generally Fuller and Hornbacker. It would be obvious to a person of ordinary skill in the art that in order to perform the functions claimed, the computer device would require a processor coupled between the display, memory, and communications channel interface.
360. Element 13.F said processor operative to select said defined data parcel, See discussions for claim element 1.B.
361. Element 13.G retrieve said defined data parcel via said limited bandwidth communications channel interface for storage in said memory: See discussions for claim element 13.B.
362. Element 13.H render said defined data parcel over a discrete portion of said mesh to provide for a progressive resolution enhancement of said defined image on said display: Fuller and Hornbacker both teach progressive resolution enhancement: tiles representing a coarser resolution may be displayed
first while higher resolution images are downloading. Fuller at 19, Figs. 3, 5;
Hornbacker at 12:24-13:10.
363. Element 13.I a remote computer, coupled to the limited bandwidth communications channel, that delivers the defined data parcel: See discussions for claim element 1.M.
364. Element 13.J wherein delivering the defined data parcel further comprises processing source image data to obtain a series $K_{1-N}$ of derivative images of progressively lower image resolution: See discussions for claim element 1.D.
365. Element 13.K wherein series image $\mathrm{K}_{0}$ being subdivided into a regular array: See discussions for claim element 1.E.
366. Element 13.L wherein each resulting image parcel of the array has a predetermined pixel resolution: See discussions for claim element 1.F.
367. Element 13.M wherein image data has a color or bit per pixel depth representing a data parcel size of a predetermined number of bytes: See discussions for claim element 1.G.
368. Element 13.N resolution of the series $\mathrm{K}_{1-N}$ of derivative images being related to that of the source image data or predecessor image in the series by a factor of two: See discussions for claim element 1.H.
369. Element 13.0 said array subdivision being related by a factor of two: See discussions for claim element 1.I.
370. Element 13.P such that each image parcel being of a fixed byte size: See discussions for claim element 1.J.
371. Element 13.Q wherein the processing further comprises compressing each data parcel: See discussions for claim element 1.K.
372. Element 13.R storing each data parcel on the remote computer in a file of defined configuration such that a data parcel can be located by specification of a $K_{D}, \mathrm{X}, \mathrm{Y}$ value that represents the data set resolution index D and corresponding image array coordinate. See discussions for claim element 1.L.
373. Claim 14. The display system of claim 13, wherein said processor is responsive to said defined screen resolution and wherein said processor is operative to limit selection of said defined data parcel to where the resolution of said defined data parcel is less than or equal to said defined screen resolution. Fuller teaches that higher resolution images are optimal for points near the viewpoint in a perspective view while lower resolution images are optimal for points distant from the viewpoint. Fuller, Figs. 3, 5, pp. 17-19; Hornbacker teaches that the resolution of tiles requested is determined based on the size of the view
area and the scale at which the user is viewing the image. 7:4-25, 11:19-28, 13:410, 14:2-6.
374. In my opinion, it would be obvious to a person of ordinary skill in the art in light of these combined teachings that the tiles used in a system displaying a perspective view with higher resolution closer to the focal point as in Fuller or at a given zoom level and scale as in Hornbacker would preferably request tiles at a resolution that the display was capable of displaying (i.e. less than or equal to the defined resolution of the display as the tiles are rendered) but that would still produce a satisfying image. Attempt to render a tile having higher resolution than the display device's own resolution will simply result in a waste of bandwidth and system resources.
375. Claim Element 15.A The display system of claim 13, wherein said processor is operative to prioritize the retrieval of said data parcel among a plurality of selected data parcels pending retrieval: See discussions for claim element 10.A.
376. Claim Element 15.B wherein the relative priority of the data parcel is based on the difference in the resolution of the image parcel and the resolution of said plurality of selected data parcels. See discussions for claim element 10.B.
377. Claim Element 16.A The display system of claim 13, wherein said processor is response to user navigation commands to define an image viewpoint relative to said defined image: See discussions for claim 11.
378. Claim Element 16.B wherein said processor is operative to prioritize the retrieval of said data parcel based on the distance between said image parcel and said image viewpoint relative to said defined image. See discussions for claim 11.
379. Claim 17. The display system of claim 13, wherein the data parcel further comprises one of an image parcel textual mapping, a map parcel, a navigation cue, a text overlay and a topography. See discussions for claim 2.
380. Claim 18. The display system of claim 13 , wherein the predetermined pixel resolution for each data parcel is a power of 2. See discussions for claim 4.
381. Claim 19 The display system of claim 18 , wherein the predetermined pixel resolution is power of 2 and one of $32 \times 32,64 \times 64,128 \times 128$ and $256 \times 256$. See discussions for claim 5 .

## 2. Claims 12 and $\mathbf{2 0}$ are Rendered Obvious by Fuller in View of Hornbacker and Lawless

382. U.S. Patent No. 5,818,469 to John Joseph Lawless et al. ("Lawless"), entitled Graphics Interface Processing Methodology in Symmetric Multiprocessing
or Distributed Network Environments, was filed on April 10, 1997 and issued on October 6, 1998. App. CC. Because Lawless was issued more than one year before the earliest priority date of the 343 Patent, December 27, 2000, I understand that Lawless is prior art under at least $\S 102(b)$.
383. Lawless generally discloses "an improved graphics processing method and apparatus for multiprocessor or distributed network computer graphics systems supporting an OpenGL or similar graphics programming interface." Lawless at 1:8-12.
384. Claim 12. The method of claim 1 , wherein displaying the image further comprises multi-threading on the limited communication bandwidth computer device using the update data parcel to display the image. Lawless teaches that multi-threading on a rendering system was well-known in the art of computeraided rendering. For example, the master thread 105 in Lawless can create a plurality of threads 107 and 109 to be sued for rendering graphics to be displayed. Lawless at Abstract; 2:8-35; 3:6-24; Fig. 1.
385. Lawless teaches that multi-threading may be used advantageously in a graphics rendering application, in order to enable the processor or processors to perform multiple functions within the same process (e.g. steps of the rendering process) simultaneously. Fuller teaches a terrain visualization application which
requires several steps including predicting a path of travel, requesting image times, caching tiles, transforming the DEM into a three-dimensional model, mapping digital image data onto the three-dimensional model, and rasterizing the final image for display.
386. Therefore, it is my opinion that a person of ordinary skill in the art would recognize that the multi-threading features taught by Lawless would advantageously improve processing of the rendering application taught by Fuller.
387. Claim 20. The display system of claim 13, wherein the processor performs multi-threading to render said defined data parcel over the discrete portion of said mesh to provide for the progressive resolution enhancement of said defined image on said display. See discussions for claim 12.
388. I have provided as Appendix DD to this declaration a claim chart showing the exemplary teachings of Fuller, Hornbacker, and Lawless that are pertinent to claims 1-20 of the 343 Patent.

## B. CLAIMS 1-20 ARE UNPATENTABLE UNDER 35 U.S.C. § 103(a) AS BEING OBVIOUS OVER YAP IN VIEW OF RABINOVICH

389. U.S. Patent No. 6,182,114 to Chee K. Yap et al. ("Yap") was filed on January 9, 1998 and issued on January 30, 2001. Because Yap's filing date is earlier than the 343 Patent's earliest priority date, I understand that Yap is prior art for the 343 Patent under at least § 102(e). Yap discloses a method and apparatus
for serving large images over a "thinwire," e.g., over the Internet or any other network or application having bandwidth limitations. App. J at 1: 8-11.
390. Visualization of Large Terrains in Resource-Limited Computing Environments authored by Boris Rabinovich and Craig Gotsman ("Rabinovich") was published in IEEE Computer Society Technical Committee on Computer Graphics' Proceedings Visualization '97, October 19-24, 1997. App. R. Because Rabinovich was published more than one year before the 343 Patent's earliest priority date, I understand that Rabinovich qualifies as prior art of the 343 Patent under at least § 102(b). Rabinovich discloses a "system supporting interactive visualization of large terrains in a resource-limited environment, i.e., a low-end client computer accessing a large terrain database server through a low-bandwidth network." App. R at 1, Abstract.
391. A person of ordinary skill in the art would be motivated to combine Yap and Rabinovich because they both address the common technical issues present in interactively visualizing large size images over a narrow bandwidth network, using a thin client viewing device with small memory comparing to the image size. Yap and Rabinovich uses similar approaches in addressing these technical issues too, including dividing large images into tiles, compressing the image tiles using wavelet transform or other methods, transmitting only the
relevant tiles to the client device based on the viewpoint, and rendering the received tiles to achieve progressive resolution enhancement. As shown in the detailed discussions for each claim element, Yap and Rabinovich have overlapping disclosures for most of the claim elements of the 343 Patent. Therefore, it is obvious for a person of ordinary skill in the art to combine the teachings of Yap and Rabinovich.

## 1. The 343 Patent Fails To Distinguish Over Yap

392. As an initial matter, after reviewing the discussion of Yap in the background of the 343 Patent, it is my opinion that the 343 Patent mischaracterizes the alleged shortcomings of Yap and the ways that the 343 Patent supposedly overcomes those shortcomings.
393. The 343 Patent, in its "BACKGROUND" section, acknowledged that an "image visualization system proposed by Yap . . . overcomes some of the foregoing problems [of inherently increasing latency in resolving finder levels of detail]." Ex. 1001 at 2:11-13. The 343 Patent states that: "[ $t]$ he Yap et al. system also employs a progressive encoding transform to compress the image transfer stream. The transform also operates on a subdivided image, but the division is indexed to the encoding level of the transform. The encoded transform coefficient data sets are, therefore, of constant size, which supports a modest improvement in
the algorithmic performance of the inverse transform operation required on the client." Id. at 2:13-20.
394. The 343 Patent recognized certain advantages achieved by Yap: "Yap et al. adds utilization of client image panning or other image pointing input information to support a foveation-based operator to influence the retrieval order of the subdivided image blocks. This two-dimensional navigation information is used to identify a foveal region that is presumed to be the gaze point of a client system user. The foveation operator defines the corresponding image block as the center point of an ordered retrieval of coefficient sets representing a variable resolution image. The gaze point image block represents the area of highest image resolution, with resolution reduction as a function of distance from the gaze point determined by the foveation operator. This technique thus progressively builds image resolution at the gaze point and succeedingly outward based on a relatively compute intensive function. Shifts in the gaze point can be responded to with relative speed by preferentially retrieving coefficient sets at and near the new foveal region." Id. at 2:21-37.
395. Nonetheless, the 343 Patent maintained that "[s]ignificant problems remain in permitting the convenient and effective use of complex images by many different types of client systems, even with the improvements provided by various
conventional systems," including the system described in Yap. Id. at 2:38-41. Specifically, the 343 Patent alleged that conventional approaches such as described in Yap cannot work properly on "[s]mall clients," which "typically have restricted performance processors with no dedicated floating-point support, little general purpose memory, and extremely limited persistent storage capabilities, particularly relative to common image sizes." Id. at 2:45-51. These small clients "are not readily capable, if at all, of performing complex, compute-intensive Fourier or wavelet transforms, particularly within a highly restricted memory address space." Id. at 2:55-58.
396. In addition, the 343 Patent criticizes Yap as "simply rel[ying] on the data packet transfer protocols to provide for an efficient transfer of the compressed image data." Id. at 3:24-26. The 343 Patent found this problematic because "[r]eliable transport protocols, however, merely mask packet losses and the resultant, sometimes extended, recovery latencies. When such covered errors occur, however, the aggregate bandwidth of the connection is reduced and the client system can stall waiting for further image data to process." Id. at 3:27-31.
397. None of these perceived shortcomings of Yap is true. First, the invention disclosed in Yap can be implemented on a small client device like a PDA, a "characteristic small client" mentioned in the 343 Patent. Id. at 2:51-53. Yap's
client device include "a storage device 3 , memory device 7 , display 5 , user input device 6 and processing device 4 ," all of them are readily found in a PDA. In addition, the wavelet transform described in Yap does not require complex floating-point calculation as alleged in the 343 Patent. To the contrary, the "Haar wavelet transform" used in Yap is done by simple addition, subtraction, and division by two, the most basic types of calculation. See Fig. 2A and 2B of Yap:

398. Second, contrary to the 343 Patent's characterization, Yap is not "simply rel[ying] on the data packet transfer protocols to provide for an efficient transfer of the compressed image data." Id. at 3:24-26. Quite on the opposite, the Yap invention is not relying on any particular data transfer protocol and various protocols can be used, e.g., TCP/IP or UDP. App. J at 5:25-30. It is well known in the art that the User Datagram Protocol ("UDP") uses a simple connectionless transmission model and "it does not guarantee data packet delivery and no notification is sent if a packet is not delivered." App. S, User Datagram Protocol (UDP) (Windows CE 5.0), available at https://msdn.microsoft.com/enus/library/ms885773.aspx. Therefore, the perceived problem of bandwidth being occupied by error recovery (re-send of lost packets) and the problem of stalled systems waiting for the error recovery, are not present in Yap.
399. Therefore, it is my opinion that the 343 Patent fails to distinguish over Yap. All of the deficiencies allegedly exist in Yap and solved by the 343 Patent are, as discussed above, simply not present in Yap.

## 2. Claims $\mathbf{1}$ to $\mathbf{2 0}$ are Rendered Obvious by Yap and

## Rabinovich

400. Element 1.Preamble A method of retrieving large-scale images over network communications channels for display on a limited communication bandwidth computer device, said method comprising: Yap discloses "realtime
visualization" of images, "even very large images, over a 'thinwire' (e.g., over the Internet or any other network or application having bandwidth limitations)." Yap at Abstract; 1:8-11. Similarly, Rabinovich describes a "system supporting interactive visualization of large terrains in a resource-limited environment, i.e., a low-end client computer accessing a large terrain database server through a lowbandwidth network." Rabinovich at 1. Therefore, it is my opinion that both references disclose the Preamble of claim 1.
401. Element 1.A issuing, from a limited communication bandwidth computer device to a remote computer, a request for an update data parcel Yap discloses a Display Thread 20 which can place user input requests in a "request queue," which will be converted by the Manager Thread 18 into a "manager request queue," which is a queue of "request[s] for coefficients." Yap at 9:1-11. Rabinovich also teaches that a client devices can send requests for geometry and texture data to the server. Rabinovich at p.2, System Overview. Therefore, it is my opinion that both references disclose this claim element.
402. Element 1.B wherein the update data parcel is selected based on an operator controlled image viewpoint on the computer device relative to a predetermined image: Yap discloses determining the viewpoint location in response to user navigational commands, e.g., the user's movement of a mouse
pointer. Yap at 8:55-9:5. As shown in Fig. 3, Rabinovich also discloses a viewpoint relative to an image.


Figure 3: Determining the DTM points of the rendered Delaunay triangulation for a given view at different geometric resolutions. The narrow cone represents a low-resolution view, and the wide one a high resolution. The "elevations" of the DTM points are their precalculated grades. All points within the footprint with grade above the relevant cone are included in the triangulation. This range-reporting operation is performed efficiently using an octree structure on the points in each tile. Note that more points are admitted in the view foreground than in its background.
403. Element 1.C the update data parcel contains data that is used to generate a display on the limited communication bandwidth computer device; In

Yap, the image data received from the server and stored in the client's storage device can be used by the Display Thread to generate display on the client device. Yap at 10:45-48. In Rabinovich, the DTM points and texture tiles received from the server are used to generate display on the client device. Rabinovich at pp.3-4.
404. Element 1.D processing, on the remote computer, source image data to obtain a series $\mathrm{K}_{1-\mathrm{N}}$ of derivative images of progressively lower image resolution: Yap teaches using wavelet transform (e.g., Haar wavelet transform), to
convert the original image into "a series of approximation and difference matrices at various level (or resolutions)." Yap at 7:6-8:7. Thus, "the approximation matrix 8 at varying levels of the wavelet transform can be used as a representation of the relevant color component of the image at varying levels of resolution." Id. at 7:6063. In addition to wavelet transform, "multi resolution pyramid schemes" can also be used for the invention disclosed in Yap. Id. at 4:21-24.
405. Similar to Yap, Rabinovich also teaches compressing the texture tiles using a progressive wavelet scheme. Rabinovich at p. 2, System Overview; p. 3, Texture Processing. Rabinovich also teaches a texture pyramid that contains "texels representing the same terrain area, at decreasing resolutions." Id. at p. 3, Texture Processing; Fig. 4. Therefore, it is my opinion that the combined teachings in Rabinovich and Yap disclose this claim element.


Figure 4: The contribution of individual tiles in the texture buffer to the rendered image corresponding to the marked footprint. Those tiles not contributing need not reside in the texture buffer at all, and are not streamed and decoded from the server.
406. Element 1.E wherein series image $\mathrm{K}_{0}$ being subdivided into a regular array: In Yap, the original image is subdivided into a regular array of $2 \times 2$ blocks. Yap at 7:10-15. Similarly, the "large terrain scene" on the server disk in Rabinovich is also subdivided into a regular array of tiles. Rabinovich at p. 2, § 2, System Overview; Fig. 4.

## 407. Element 1.F wherein each resulting image parcel of the array

 has a predetermined pixel resolution: See discussions for element 1.D above.408. Element 1.G wherein image data has a color or bit per pixel depth representing a data parcel size of a predetermined number of bytes:

Rabinovich discloses rendering a fixed size image of $300 \times 400$ pixels on a client device, R5000 SGI $\mathrm{O}_{2}$, and each output image pixel has a size of 0.5 texture bytes. Rabinovich at p. 4, Experimental Results; Fig. 5.
409. Yap teaches that a pixel can have three color components: Red, Green, and Blue. Yap at 7:6-10. Yap also discloses that a large image can be divided into blocks for transformation and storage purposes. Yap at 8:4-7. For a person skilled in the art, it is an obvious design choice to use fixed size image blocks for easier computation and transmission. Therefore, it is my opinion that the combined teachings in Rabinovich and Yap disclose this claim element.
410. Element 1.H resolution of the series $\mathrm{K}_{1-N}$ of derivative images being related to that of the source image data or predecessor image in the series by a factor of two: Figure 4 of Rabinovich shows that the resolution of two adjacent levels of derivative images are related by a factor of two. Similarly, Yap discloses creating an "approximation matrix" of the original matrix using the "average" of each $2 \times 2$ group of 4 pixels. Yap at 7:36-40; Fig. 2A. Thus, the resolution of the approximation matrix relates to the original matrix by a factor of two.
411. Element 1.I said array subdivision being related by a factor of two: Figure 4 of Rabinovich shows that the array subdivision in two adjacent levels is being related by a factor of two. In Yap, the array subdivision in the approximation matrix and the original matrix is also related by a factor of two. Yap at 7:36-40; Fig. 2A.
412. Element 1.J such that each image parcel being of a fixed byte size, Rabinovich discloses that the large terrain scene on the server disk is partitioned into texture tiles of fixed size. Rabinovich at 2, § 2, System Overview. Yap also discloses that a large image can be divided into blocks for transformation and storage purposes. Yap at 8:4-7. For a person skilled in the art, it is an obvious design choice to use fixed byte size image blocks for easier computation and
transmission. Therefore, it is my opinion that the combined teachings in Rabinovich and Yap disclose this claim element.
413. Element 1.K wherein the processing further comprises compressing each data parcel: The texture tiles in Rabinovich are compressed using the progressive wavelet scheme to approximately $30 \%$ of their raw sizes. Rabinovich at 2, § 2, System Overview. The coefficient matrix in Yap is also compressed. Yap at 8:3-4.
414. Element 1.L storing each data parcel on the remote computer in a file of defined configuration such that a data parcel can be located by specification of a $K_{\underline{D}}, \mathrm{X}, \mathrm{Y}$ value that represents the data set resolution index D and corresponding image array coordinate; Figure 4 of Rabinovich shows that the texture tiles are identified by their resolution index, e.g., levels $1,2,3$, or 4 . The texture tiles are also arranged in a regular array in Figure 4. Therefore, it is obvious for a person of ordinary skill in the art that a particular tile can be located by its resolution index and it $\mathrm{X}, \mathrm{Y}$ coordinate value.
415. Element 1.M receiving said update data parcel from the data parcel stored in the remote computer over a communications channel: The client apparatus of Yap includes a Network Thread 19 which receives image data from the server, performs inverse wavelet transform, and then stores the resultant image
data (in the form of approximation matrix at various levels of resolution) in the storage device of the client. Yap at 10:25-44; see also Yap at Abstract.
416. Rabinovich's client device also receives image data parcels from the server and then stores the data in the cache memory. Rabinovich at p.3, Caching. In a prototype system implementing the invention disclosed in Rabinovich, the client's geometry cache is a 2MB RAM. Id. at p.4, Experimental Results. Therefore, it is my opinion that both references disclose this claim element.
417. Element 1.N displaying on the limited communication bandwidth computer device using the update data parcel that is a part of said predetermined image, an image wherein said update data parcel uniquely forms a discrete portion of said predetermined image. In Yap, the image data received from the server and stored in the client's storage device can be used by the Display Thread to generate display on the client device. Yap at 10:45-48. In Rabinovich, each texture tiles are rendered for displaying at its corresponding portion of the image. Rabinovich at pp. 3-4, Texture Processing.
418. Claim 2. The method of claim 1, wherein the update data parcel further comprises one of an image parcel textual mapping, a map parcel, a navigation cue, a text overlay and a topography. The update data parcel in both Yap and Rabinovich is a map parcel because Yap and Rabinovich both relate to
mapping applications. See, e.g., Yap at 1:19-23; Rabinovich at p.1, § 1, Introduction.
419. Claim 3. The method of claim 1, wherein the limited communication bandwidth computer device further comprises one of a mobile computer system, a cellular computer system, an embedded computer system, a handheld computer system, a personal digital assistant and an internet-capable digital phone. As discussed in claim element 1.Preamble, both Yap and Rabinovich's client devices are designed to work in a low bandwidth environment. Therefore, it is obvious for a person of ordinary skill in the art to use a mobile computer system, a cellular computer system, an embedded computer system, a handheld computer system, a personal digital assistants, or an internet-capable digital phone as the client device in Yap and Rabinovich.
420. Claim 4. The method of claim 1, wherein the predetermined pixel resolution for each data parcel is a power of 2. Yap discloses a pixel matrix having the size of 128x128 (9:31-36; Fig. 5), or 256x256 (8:11-37). Rabinovich teaches a texture buffer with a capacity of $1024 \times 1024$ pixels. All of these pixel resolutions are a power of two.
421. Claim 5. The method of claim 4 , wherein the predetermined pixel resolution is one of $32 \times 32,64 \times 64,128 \times 128$ and $256 \times 256$. See discussions for claim 4 above.
422. Claim 6. The method of claim 1 wherein said communications channel is a packetized communications channel and wherein said update data parcel is received from said packetized communications channel in one or more data packets. Yap teaches transmitting tiles using the TCP/IP protocol, which is a packet based transmission protocol. Yap at 5:29-46. Rabinovich discloses transmitting data using the Internet, which also commonly transmits data parcels in packetized communications channels. Rabinovich at p.1, § 1, Introduction.
423. Claim 7. The method of claim 6 wherein the data packet contains an update image parcel as a compressed data representation of said discrete portion of said predetermined image. See discussions for claim element 1.K.
424. Claim 8. The method of claim 7 wherein said data packet contains said update image parcel as a fixed compression ratio representation of said discrete portion of said predetermined image. Rabinovich discloses compressing the texture tiles to a fixed compression ratio of approximately $30 \%$. Rabinovich at p.2, § 2, System Overview; p.3, § 4, Texture Processing.
425. Claim 9. The method of claim 7, wherein said update image parcel contains pixel data in a fixed size array independent of the pixel resolution of said predetermined image. See discussions for claim element 1.L.
426. Claim Element 10.A The method of claim 1, wherein issuing the request for an update data parcel further comprises preparing the request by associating a prioritization value to said request: Yap discloses a Display Thread 20 which can place user input requests in a "request queue," which will be converted by the Manager Thread 18 into a "manager request queue," with is a queue of "request[s] for coefficients." Yap at 9:1-11. Requests put in the queue are in a priority order because queues are "data structures with first-in-first-out characteristics that are generally known in the art." Id. at 9:4-5.
427. Rabinovich also teaches that a client devices can send requests for geometry and texture data to the server. Rabinovich at p.2, System Overview. These requests can be sent "using a priority queue mechanism" to achieve incremental image surface approximation. Id. at p.2, Data Reduction. Therefore, it is my opinion that both references disclose this claim element.
428. Claim Element 10.B wherein said prioritization value is based on the resolution of said update data parcel relative to that of other data parcels previously received by the limited communication bandwidth computer device:

Rabinovich teaches loading only the texture tiles at the appropriate resolution, "if they are not yet loaded." Rabinovich at 3, § 4, Texture Processing.
429. Claim Element 10.C wherein issuing said request is responsive to said prioritization value for issuing said request in a predefined prioritization order.

Yap discloses that in response to a user's input at the input device, the Display Thread places user input requests in a request queue, which is then converted by the Manager Thread into a manager request queue for image data in the form of coefficients. Yap at 9:1-11. The quests in the manager request queue are ordered based on a number of "foveal parameters," e.g., "shape of the foveal region, a maximum resolution, a rate of decay of the resolution, etc.," and these parameters can be either set by the user manually or determined by the Manager Thread automatically to "ensure a trade-off between (1) achieving a reasonable response time over the estimated current network bandwidth, and (2) achieving a maximum throughput in the transmission of data. Id. at 9:12-10:9; Fig. 5.
430. In Rabinovich, the Digital Terrain Map ("DTM") points are also requested from the server "using a priority queue mechanism." Rabinovich at p.2, Data Reduction. The priority, or "grades" assigned to the DTM points reflect "their importance in approximating the terrain surface." Id. at p.2, System Overview. When determining which DTM points to request, "the client considers a virtual
cone centered at the viewpoint, and calculates which DTM points in the geometry cache have a grade positioning them inside the cone," as shown in Fig. 3. Id. at p.3, Continuous Resolution. In view of these teachings in Yap and Rabinovich, it is my opinion that both references disclose this claim element.


Figure 3: Determining the DTM points of the rendered Delaunay triangulation for a given view at different geometric resolutions. The narrow cone represents a low-resolution view, and the wide one a high resolution. The "elevations" of the DTM points are their precalculated grades. All points within the footprint with grade above the relevant cone are included in the triangulation. This range-reporting operation is performed efficiently using an octree structure on the points in each tile. Note that more points are admitted in the view foreground than in its background.
431. Claim 11. The method of claim 10 , wherein said prioritization values is based on the relative distance of said update data parcel from said operator controlled image viewpoint. Yap teaches the use of "foveation techniques," where "high resolution data is transmitted at the user's gaze point but with lower resolution as one moves away from that point." Yap at 2:18-20; 3:20-22. The location of the foveal region is determined from the user input device, e.g., a mouse. Id. at 8:55-9:5. The location of the foveal region, as well as the "shape of
the foveal region," the "maximum resolution," and the "rate of decay of the resolution, etc." determines the transmission priority of the image data. Id. at 9:5759.
432. Rabinovich also discloses that a DTM point's "grade," i.e., its importance in approximating the terrain surface, is "proportional to the distance of the point from the viewpoint." Rabinovich at p. 2, System Overview. In turn, a DTM point's grade and the point's "distance from the viewpoint," is the basis to determine whether the point must be requested from the server for terrain approximation on the client device. Id. at p. 2, Data Reduction. Therefore, it is my opinion that both references disclose this claim element.
433. Claim 12. The method of claim 1 , wherein displaying the image further comprises multi-threading on the limited communication bandwidth computer device using the update data parcel to display the image. The program running on the client device in Yap can be multi-threaded. Yap at 4:34-42; 8:41-54; 11:6-12.

## Claim 13:

434. Element 13.Preamble A display system for displaying a large-scale image retrieved over a limited bandwidth communications channel, said display system comprising: See discussions for claim element 1.Preamble.
435. Element 13.A a display of defined screen resolution for displaying a defined image; Yap's client device has a display 5, which can be implemented as any analog or digital monitor. Yap at 5:58-67. Rabinovich also discloses a client running on a R5000 SGI O2 based on the OpenGL API and an X/Motif GUI. Rabinovich at 4, Experimental Results. A person of ordinary skill in the art would understands that the image display devices disclosed in the references must have their respective defined resolutions. Therefore, it is my opinion that both references disclose this claim element.
436. Element 13.B a memory providing for the storage of a plurality of image parcels: The client apparatus of Yap includes a Network Thread 19 which performs inverse wavelet transform of the image data (in the form of coefficients) received from the server, and then stores the resultant image data (in the form of approximation matrix at various levels of resolution) in the storage device of the client, using sparse matrices and their associated algorithms. Yap at 10:25-44; see also Yap at Abstract.
437. In Rabinovich, image data parcels received from the server are "stored in the client cache." Rabinovich at p.3, Caching. In a prototype system implementing the invention disclosed in Rabinovich, the client's geometry cache is
a 2MB RAM. Id. at p.4, Experimental Results. Therefore, it is my opinion that both references disclose this claim element.
438. Element 13.C displayable over respective portions of a mesh corresponding to said defined image; See discussions for claim element 1.E.
439. Element 13.D a communications channel interface supporting the retrieval of a defined data parcel over a limited bandwidth communications channel; Figure 1 of Yap shows the communications channel interface connecting the client devices to the servers.
440. Element 13.E a processor coupled between said display, memory and communications channel interface, The client device in Yap has a microprocessor chip, such as an Intel Pentium chip. Yap at 6:5-10. Rabinovich's client device likewise has a CPU. Rabinovich at p. 1, § 1, Introduction. It would be obvious to a person of ordinary skill in the art that in order to perform the functions claimed, the client device would require a processor coupled between the display, memory, and communications channel interface.
441. Element 13.F said processor operative to select said defined data parcel, See discussions for claim element 1.B.
442. Element 13.G retrieve said defined data parcel via said limited bandwidth communications channel interface for storage in said memory: See discussions for claim element 13.B.
443. Element 13.H render said defined data parcel over a discrete portion of said mesh to provide for a progressive resolution enhancement of said defined image on said display: It is my opinion that the "progressive regional resolution enhancement," a technique that has been widely used long before the 343 Patent's earliest priority date, was disclosed in Yap. For example, the invention in Yap "takes advantage of progressive transmission, which gives the image perceptual continuity." Yap at 10:65-67. The multifoveated images in Yap "can be dynamically (incrementally) updated" (3:31-34), "based on the pyramid representation stored in the storage device 3. ." (10:45-48).
444. Element 13.I a remote computer, coupled to the limited bandwidth communications channel, that delivers the defined data parcel: See discussions for claim element 1.M.
445. Element 13.J wherein delivering the defined data parcel further comprises processing source image data to obtain a series $\mathrm{K}_{1-\mathrm{N}}$ of derivative images of progressively lower image resolution: See discussions for claim element 1.D.
446. Element 13.K wherein series image $\mathrm{K}_{0}$ being subdivided into a regular array: See discussions for claim element 1.E.
447. Element 13.L wherein each resulting image parcel of the array has a predetermined pixel resolution: See discussions for claim element 1.F.
448. Element 13.M wherein image data has a color or bit per pixel depth representing a data parcel size of a predetermined number of bytes: See discussions for claim element 1.G.
449. Element 13.N resolution of the series $\mathrm{K}_{1-N}$ of derivative images being related to that of the source image data or predecessor image in the series by a factor of two: See discussions for claim element 1.H.
450. Element 13.0 said array subdivision being related by a factor of
two: See discussions for claim element 1.I.
451. Element 13.P such that each image parcel being of a fixed byte size: See discussions for claim element 1.J.
452. Element 13.Q wherein the processing further comprises compressing each data parcel: See discussions for claim element 1.K.
453. Element 13.R storing each data parcel on the remote computer in a file of defined configuration such that a data parcel can be located by
specification of a $\mathrm{K}_{\underline{D}}, \mathrm{X}, \mathrm{Y}$ value that represents the data set resolution index D and corresponding image array coordinate. See discussions for claim element 1.L.
454. Claim 14. The display system of claim 13 , wherein said processor is responsive to said defined screen resolution and wherein said processor is operative to limit selection of said defined data parcel to where the resolution of said defined data parcel is less than or equal to said defined screen resolution. Yap recognizes that the "whole map, at highest (full) level of resolution will likely require a pixel representation beyond the size of the viewer screen in highest resolution mode," and "in some instances, the lower resolution version [of an image] may be sufficient or may in any event exhaust the display capabilities of the viewer display device (e.g., monitor)." Yap at 1:21-23; 1:62-65. Thus, Yap provides the option to display the image up to a user specified resolution level, rather than "fill[ing] the pixels to the highest resolution that is currently available locally." Id. at 11:19-22. The most common design choice for a person skilled in the art is to set the specified upper limit of the resolution at the predetermined resolution of the display device. Similarly, it is obvious for a person skilled in the art to cap the texture tile resolution at the display device resolution in Rabinovich, because "the lower the required resolution, the less bits required," and thus the
lower the bandwidth needed to transmit the image tiles from the server. Rabinovich at pp. 3-4, Texture Processing.
455. Claim Element 15.A The display system of claim 13, wherein said processor is operative to prioritize the retrieval of said data parcel among a plurality of selected data parcels pending retrieval: See discussions for claim element 10.A.
456. Claim Element 15.B wherein the relative priority of the data parcel is based on the difference in the resolution of the image parcel and the resolution of said plurality of selected data parcels. See discussions for claim element 10.B.
457. Claim Element 16.A The display system of claim 13, wherein said processor is response to user navigation commands to define an image viewpoint relative to said defined image: See discussions for claim 11.
458. Claim Element 16.B wherein said processor is operative to prioritize the retrieval of said data parcel based on the distance between said image parcel and said image viewpoint relative to said defined image. See discussions for claim 11.
459. Claim 17. The display system of claim 13, wherein the data parcel further comprises one of an image parcel textual mapping, a map parcel, a navigation cue, a text overlay and a topography. See discussions for claim 2.
460. Claim 18. The display system of claim 13 , wherein the predetermined pixel resolution for each data parcel is a power of 2 . See discussions for claim 4.
461. Claim 19 The display system of claim 18 , wherein the predetermined pixel resolution is power of 2 and one of $32 \times 32,64 \times 64,128 \times 128$ and $256 \times 256$. See discussions for claim 5 .
462. Claim 20. The display system of claim 13, wherein the processor performs multi-threading to render said defined data parcel over the discrete portion of said mesh to provide for the progressive resolution enhancement of said defined image on said display. See discussions for claim 12.
463. I have provided as Appendix EE to this declaration a claim chart showing the exemplary teachings of Yap and Rabinovich that are pertinent to claims 1-20 of the 343 Patent.
C. CLAIMS 1-20 ARE UNPATENTABLE UNDER 35 U.S.C. § 103(a) AS BEING OBVIOUS OVER FULLER IN VIEW OF YAP
464. In addition to the two invalidity grounds in subsections XI.A and B discussed above, it is my opinion that claims 1 to 20 of the 343 Patent are also
unpatentable under 35 U.S.C. § 103(a) as being obvious over Fuller in view of Yap. The relevant teachings in Fuller and Yap for each claim element are discuss above in subsections XI.A and B.
465. A person of ordinary skill in the art would be motivated to combine the teachings of Fuller and Yap because they both address common technical issues relating to visualizing large amounts of data obtained over a data network, using a client viewing device with much smaller memory than the database which stores the imagery data. Fuller and Yap use similar approaches in addressing these technical issues too, including dividing large images into tiles, transmitting only the relevant tiles to the client device in a priority order, and rendering the received tiles to achieve progressive resolution enhancement.

## D. CLAIMS 1-11 AND 13-19 ARE UNPATENTABLE UNDER 35

 U.S.C. § 103(a) AS BEING OBVIOUS OVER POTMESIL IN VIEW OF HORNBACKER AND COOPER466. In my opinion, the challenged claims are also unpatentable as obvious over Potmesil in view of Hornbacker, further in view of Cooper. In the previous sections, I have provided an overview and summarized the pertinent teachings of Potmesil, Hornbacker with respect to Grounds 1 and 2; I have also provided an overview and summarized the pertinent teachings of Cooper above in regard to Grounds 3 to 5 . In my opinion, in addition to the grounds that I discussed
previously, claims 1-11 and 13-19 are unpatentable as obvious in view of the combined teachings of Potmesil, Hornbacker and Cooper.
467. As I have discussed previously in paragraphs 96-98, Potmesil teaches a server-client system in which image tiles stored in a pyramid are used to communicate a digital map or a 3D geographical model from the server to a client device. Further, as discussed in paragraphs 99 to 101, Hornbacker teaches techniques using multi-resolution hierarchies of tiles to provide image data. Potmesil further teaches that VRML (which I understand to mean Virtual Reality Modeling Language, which was previously known as Virtual Reality Markup Language) was known in the art for use with geographic search applications. Specifically, Potmesil teaches that development was underway on an online geographically-indexed VRML project called "Bigbook3D" which would "let users view 3D VRML models of cities and find business locations." Ex. 1002 at 1329.
468. VRML is a common markup language designed with the worldwide web in mind that is designed to provide a common format for 3D objects and textures. The use of VRML for geographic uses was well-known in the art prior to the priority date of the 343 patent. For example, the 1999 article "A Commentary on GeoVRML: A Tool for 3D Representation of GeoReferenced Data on the

Web," Int. J. Geographical Information Science, 1999, Vol. 13, No. 4, 439-443 (available online at http://www.siggraph.org/~rhyne/carto/3D/3D-geovrml.html) (App. FF) describes how in the late 1990s, a GeoVRML working group had updated the VRML standard to include methods to use VRML to display geographical information. For example, a figure from App. FF below illustrates how a TIFF image of a U.S. Geographical Survey (USGS) map could be mapped onto a 3D terrain representation as a texture to create a 3D rendering of the map:

469. Cooper teaches a system for viewing a three-dimensional representation of a scene from a simulated user perspective. Cooper notes in the description of the related art that the types of 3D virtual environment to which the system described therein may be applicable include flight simulation and virtual reality. Ex. 1007, 1:12-15. In my opinion, due to the related teachings of similar applications (flight simulators and virtual reality), a person of ordinary skill in the
art would consider Potmesil and Cooper to be analogous art and consider the teachings of the references when designing a system for viewing map data.
470. Cooper teaches a system for optimizing the use of limited bandwidth between a client and a server for prioritizing data requests sent by a client device when retrieving image data from a server. I have previously discussed these teachings of Cooper in paragraphs 213 and 214. A person of ordinary skill in the art would have readily recognized similarities between the teachings of Potmesil, Hornbacker and Cooper because these references provide solutions to improve performance of a client-server system in which graphical and/or image data is transferred from a server to a client device. Potmesil further teaches that the techniques disclosed therein are applicable to both 3D geometric data and images stored in hierarchical terrain representation. A person of ordinary skill in the art would have further recognized that the use of a priority queue as taught by Cooper could provide further benefits in an image browsing application like that taught by Potmesil by prioritizing data retrieval based on user's viewpoint.
471. It is therefore my opinion that one of ordinary skill in the art would have been motivated to and could have combined the teachings of Potmesil with Hornbacker and Cooper to arrive at the subject matter recited in claims 1-11 and 13-19 of the 343 patent.
472. This is the END of my declaration.

# Curriculum Vitae for <br> William R. Michalson 

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## 1. Personal:

### 1.1 Education

Ph.D. in Electrical Engineering, 1989, Worcester Polytechnic Institute, Worcester, Massachusetts.

Dissertation: A Parallel Computer Architecture for Real-Time Decision Making. The dissertation develops a hierarchical, multiple processor, computer architecture for executing artificial intelligence programs in real-time. Dissertation Directors: Dr. Peter E. Green and Dr. R. James Duckworth.

Minor Areas: Minor sequences completed in Mathematics and Physics.
Specialties: Area examinations passed in the fields of Computer Architecture, Probabilistic Systems Analysis, and State Space Analysis.
M.S. in Electrical Engineering, 1985, Worcester Polytechnic Institute, Worcester, Massachusetts.

Specialties: The courses taken stressed Computer Architecture, Communications Systems, and Solid-State Physics.
B.S. in Electrical Engineering, 1981, Syracuse University, Syracuse, New York.

### 1.2 Work experiences - Academic.

## 1991-Present Worcester Polytechnic Institute

Professor of Electrical and Computer Engineering; Professor of Computer Science.
Effective July 1, 2005 Promoted to the rank of Full Professor (Professor of Electrical and Professor of Computer Science)
November 17, 2004 Appointed dual professorship, adding the title of Associate Professor of Computer Science.
July 1, $1998 \quad$ Granted tenure and promoted to the rank of Associate Professor.
August 1, 1992 Assistant Professor of Electrical Engineering (tenuretrack).
August 1, $1991 \quad$ Visiting Assistant Professor of Electrical Engineering.
January 1, 1990

### 1.3 Work experiences other than teaching (chronological).

## 2012-2014 Grid Roots, LLC

Grid Roots, LLC is a company which was formed in 2012 for the purpose of commercializing a navigation and tracking device for use by children and the elderly to allow caregivers to nonintrusively monitor their activities. The system under development integrates GPS, inertial and beacon-based navigation technologies to develop a system for users to track deployed devices. My responsibilities within Grid Roots, LLC relate to hardware and software engineering, as well as the development of IP related to tracking individuals.

## 1995-Present Research Associates, LLC

Research Associates, LLC is a company I formed in which I perform engineering and consulting in the areas of computer systems, communications and navigation. All of my litigation-related and other consulting activities are performed through Research Associates, LLC.

## 1988-1991 Raytheon Company

Subsequent to receiving my Ph. D., I returned to the Equipment Division of the Raytheon Company. Shortly after I returned, I was promoted to a title of Engineer, Design and Development which was the highest title I could hold based on my level of education and years of experience. Within a year, I was selected to sit on the engineering staff of a newly formed System Engineering Department of the Division's Computer and Displays Laboratory. In this department I acted primarily as a consultant to other departments within the laboratory. My responsibilities ranged from leading the hardware/software development of supercomputer-class computer systems to performing applied research into the exploitation of new technology. My role was similar to that of a Principle Investigator in an academic setting as I was responsible for securing funding and personnel, leading research efforts, interacting with the research sponsor, and reporting results. At the time of my departure I was involved with the following projects:

## Fault-Tolerant Multiprocessor

The development of a highly fault tolerant, highly reliable, real-time computer system intended for long-duration spaceborne applications. This system is designed to produce in excess of one gigaoperation per second of raw processing power.

## Optimal Task Allocation

A program of applied research into the use of Genetic Algorithms for deriving optimal mappings of software tasks to the hardware processing elements in distributed systems.

## Performance Modeling and Scaling

This project focused on the development of simulation models for characterizing the performance of a large scale multiple processor system. These models formed a basis for predicting system performance for several different hardware configurations to ensure compliance with system specifications.

## High Clutter Signal Detection

A program of applied research into the use of Neural Networks to detect the presence of targets in extremely high clutter environments.

## Power Efficient Computing

A program of applied research into an Integrated Optical computer structure that is designed to maximize the number of computations that can be performed per unit of power.

## 1985-1988 Raytheon Company (Leave of Absence)

In 1985 I became one of two people in the Equipment Division to receive Aldo Miccioli Fellowships. This Fellowship was awarded to allow me to pursue full-time study towards the Ph.D. degree. I returned to Raytheon during the summer of 1986, but otherwise remained on leave of absence to dedicate my time to my studies.

## 1982-1985 Raytheon Company

Engineer in the VLSI Design Department of the Computer and Displays Laboratory within Raytheon's Equipment Division. I was lead engineer for the design of several semi-custom VLSI circuits for both signal and data processing applications.

## 1981-1982 Raytheon Company

Engineer in the Cursive Displays Department of the Computer and Displays Laboratory. I designed and debugged circuit assemblies which were used in vector displays for air traffic control applications.

### 1.4 Consulting experiences.

### 1.4.1 Law-Related

## Locata LBS LLC v. YellowPages.com LLC,

Retained by Baker Botts on behalf of defendant YellowPages.com. Case before the Central District of California (2:13-cv-07664). See also IPR2015-00151. Retained 9/14 to present.

## M/A-COM Technology Solutions Holdings, Inc. v. Laird Technologies, Inc.

Retained by Erise IP on behalf of Laird Technologies, Inc., for invalidity consulting regarding U.S. Patent No. 6,272,349. Retained 6/14 to present.

Certusview Technologies, LLC v. S\&N Locating Services, LLC and S\&N Communications, Inc.,
Retained by Baker \&McKenzie on behalf of defendant S\&N. Patents-in-suit are U.S. Patents $8,265,344,8,290,204,8,340,359,8,407,001$, and $8,532,341$. Case before the Eastern District of Virginia, (2:13-cv-346). Deposed 11/8/14; Retained 6/14 to present.
adidas AG and adidas America, Inc. v. Under Armour, Inc. and MapMyFitness, Inc. Retained by Kilpatrick Townsend on behalf of plaintiff adidas. Case before the District of Delaware, (1:14-cv-00130). Retained 5/14 to present.

GeoTag, Inc., v. AT\&T Mobility LLC and AT\&T Services, Inc., Retained by Baker Botts as an expert on behalf of defendant AT\&T. Patent-in-suit is U.S. Patent 5,930,474. Case before the Northern District of Texas, Dallas Division, (3:13-cv-00169). Deposed 5/29/14; Retained 1/14 to 9/14. Matter settled.

## Nokia Corp v. HTC Corp.

Retained by Quinn Emanuel as an expert on behalf of defendant HTC. Case being litigated in Germany. Patent number EP0766811B1. Retained 12/13 to 2/14. Matter settled.

## Porto Technology, Co., Ltd. et al. v. Cellco Partnership d/b/a Verizon Wireless

Retained by Wiley-Rein as an expert on behalf of defendant Verizon. Case before the United States District Court for the Eastern District of Virginia (Case No. 3:13-cv-00265). Retained 10/13 to 2/14. Matter dismissed.

## Nokia Corp v. HTC Corp.

Retained by McDermott Will and Emery and White \& Case as an expert on behalf of defendant HTC. Case before the United States District Court for the District of Delaware (Case No. Case No. 1:12-cv-00550-UNA and Case No. 1:12-cv-551-UNA. Retained 6/13 to 2/14. Matter settled.

NXP B.V. v. Research In Motion, Ltd., et al.
Retained by Fish and Richardson as an expert on behalf of defendant Research In Motion. Patent-in-suit is U.S. Patent 6,501,420. Case before the United States District Court for the

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Middle District of Florida (Case No. 6:12-cv-00498). Deposed 9/18/13; Testified in Court: $4 / 1 / 14$ and $4 / 2 / 14$; Retained $5 / 13$ to $4 / 14$.

## Vehicle IP LLC v. Wal-Mart Stores Inc., et al.

Retained by Polsinelli-Shugart, as an expert on behalf of defendant Werner Enterprises. Patent-in-suit is U.S. Patent 5,694,322. Case before the United States District Court for the District of Delaware (Case No. 1:10-cv-00503). Deposed 7/15/13 and 9/20/13; Testified in Court: 9/27/13 and 9/30/13; Retained 4/13 to 9/13.

## TracBeam, LLC v. Google Inc.

Retained by Quinn-Emanuel as an expert on behalf of defendant Google. Patents-in-suit are U.S. Patents 7,764,231 and 7,525,484. Case before the United States District Court for the Eastern District of Texas (6:11-cv-00093). Deposed 2/5/14; Retained 3/13 to 6/14.

## Microsoft Corporation and Google Inc., v. GeoTag, Inc.

Retained by Perkins-Coie as an expert on behalf of plaintiff Microsoft Corporation. Patent-insuit is U.S. Patents $5,930,474$. Case before the United States District Court for the District of Delaware (1:11-cv-00175). Retained $1 / 13$ to present.

## GeoTag, Inc., v. Frontier Communications Corp., et al.,

Retained by multiple firms as an expert on behalf of defendants. Patent-in-suit is U.S. Patents $5,930,474$. Case before the Eastern District of Texas, Marshall Division, (2:10-cv-00265; other defendants are listed in case numbers 2:10-cv-00265, 2:10-cv-00272, 2:10-cv-00437, 2:10-cv00569, 2:10-cv-00570, 2:10-cv-00571, 2:10-cv-00572, 2:10-cv-00573, 2:10-cv-00574, 2:10-cv00575, 2:10-cv-00587, 2:11-cv-00175, 2:11-cv-00404, 2:11-cv-00421, 2:11-cv-00424, 2:11-cv00425, 2:11-cv-00570, 2:12-cv-00043, 2:12-cv-00051, 2:12-cv-00436, 2:12-cv-00438, 2:12-cv00439, 2:12-cv-00441, 2:12-cv-00442, 2:12-cv-00444, 2:12-cv-00445, 2:12-cv-00446, 2:12-cv00447, 2:12-cv-00448, 2:12-cv-00449, 2:12-cv-00450, 2:12-cv-00452, 2:12-cv-00454, 2:12-cv00456, 2:12-cv-00459, 2:12-cv-00460, 2:12-cv-00462, 2:12-cv-00464, 2:12-cv-00466, 2:12-cv00468, 2:12-cv-00469, 2:12-cv-00470, 2:12-cv-00471, 2:12-cv-00473, 2:12-cv-00474, 2:12-cv00475, 2:12-cv-00476, 2:12-cv-00476, 2:12-cv-00477, 2:12-cv-00480, 2:12-cv-00481, 2:12-cv00482, 2:12-cv-00482, 2:12-cv-00483, 2:12-cv-00486, 2:12-cv-00487, 2:12-cv-00520, 2:12-cv00521, 2:12-cv-00523, 2:12-cv-00524, 2:12-cv-00525, 2:12-cv-00527, 2:12-cv-00528, 2:12-cv00530, 2:12-cv-00532, 2:12-cv-00534, 2:12-cv-00535, 2:12-cv-00536, 2:12-cv-00537, 2:12-cv00542, 2:12-cv-00543, 2:12-cv-00545, 2:12-cv-00547, 2:12-cv-00548, 2:12-cv-00549, 2:12-cv00550, 2:12-cv-00551, 2:12-cv-00552, 2:12-cv-00555, 2:12-cv-00556, 2:12-cv-00570, 2:12-cv00572, 2:12-cv-00573, 2:12-cv-00575, 2:12-cv-00587, 3:13-cv-00217). Deposed 5/29/14; Retained 1/13 to 9/14.

## MOSAID Technologies Inc., v. Realtek Semiconductor Corporation

Retained by Sidley Austin, LLP as an expert on behalf of defendant Realtek Semiconductor Corporation. Patents-in-suit are U.S. Patents 5,131,006; 5,151,920; 5,422,887; 5,706,428;
6,563,786; and 6,992,972. Case before the United States District Court for the Eastern District of Texas (Tyler Division) (Case No. 2:11-cv-00179). Retained 12/12 to 12/12. Matter settled.

## Hoyt A. Flemming v. Cobra Electronics Corporation

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Retained by Sidley Austin, LLP as an expert on behalf of defendant Cobra Electronics Corporation. Patents-in-suit are U.S. Patents RE39038, RE40653 and RE41905. Case before the United States District Court for the District of Idaho (Case No. 1:12-cv-00392). Retained 11/12 to 06/13. Matter settled.

## LBS Innovations LLC v. Aaron Bros., Inc., et al.

Retained as an expert on behalf of defendants Whole Foods Marketplace, Comerica, Hotels.com, Academy, Ltd., and Homestyle Dining. Patent-in-suit is U.S. Patent 6,091,956. Case before the Eastern District of Texas, Marshall Division, (Case No. 2:11-cv-00142-MHS-CMC. Deposed 10/5/12; Retained 7/12 to 12/12. Plaintiff moved to dismiss.

## Advanced Media Networks, L.L.C. v. Gogo LLC et al.

Retained by Sidley Austin, LLP as an expert on behalf of defendant Gogo. Patent-in-suit is U.S. Patent $5,960,074$. Case before the United States District Court for the Central District of California (Case No. 11-cv-10474). Deposed 2/6/13. Retained 7/12 to 8/13.

## Walker Digital, LLC v. Google Inc.

Retained by O’Melveny \& Meyers, LLP as an expert on behalf of defendant Google Inc. Patents-in-suit are U.S. Patents 6,199,014. Case before the United States District Court for the District of Delaware (Case No. 1:11-cv-00309-SLR). Deposed 2/27/13-2/28/13. Retained 6/12 to present (case stayed as of $8 / 13$ ).

Silver State Intellectual Technologies, Inc. v. Garmin International, Inc., et al. Retained by Erise IP, P.A. as an expert on behalf of defendants Garmin International, Inc. and Garmin USA, Inc. Patents-in-suit are U.S. Patents 6,525,768; 6,529,824; 6,542,812; 7,343,165; 7,522,992; 7,593,812; 7,650,234; 7,702,455 and 7,739,039. Case before the United States District Court for the District of Nevada (Case No. 2:11-cv-1578). Deposed 2/19/14; Retained 4/12 to present.

## Beacon Navigation GmbH v. Toyota Motor Corporation, et al.

Retained by Kirkland \& Ellis, LLP on behalf of defendants Toyota Motor Corporation; Toyota Motor North America, Inc.; Toyota Motor Sales, U.S.A. Inc.; Toyota Motor Engineering \& Manufacturing North America, Inc.; Toyota Motor Manufacturing, Indiana, Inc.; Toyota Motor Manufacturing, Kentucky, Inc.; Toyota Motor Manufacturing Mississippi, Inc.; Mazda Motor Corporation; Mazda Motor of America, Inc.; Fuji Heavy Industries, Ltd.; Fuji Heavy Industries U.S.A. Inc.; Subaru of America, Inc.; Jaguar Land Rover North America, LLC; Jaguar Cars Limited; Land Rover; Volvo Car Corporation; and Volvo Cars of North America, LLC; Adduci Mastriani \& Schaumberg, LLP on behalf of defendants Suzuki and Garmin; Crowell-Moring on behalf of General Motors; Dickstein Shapiro on behalf og Chrysler Group, LLC; Finnegan, Henderson, Farabow, Garrett \& Dunner on behalf of Bayerische Motoren Werke AG, BMW of North America, LLC, and BMW Manufacturing Co. LLC; Fish \& Richardson on behalf of Honda Motor Co., Ltd., Honda North America, Inc., American Honda Motor Co., Inc., Honda Manufacturing of Alabama, LLC, Honda Manufacturing of Indiana, LLC, and Honda of America, Mfg., Inc.; Frommer Lawrence and Haug, LLP on behalf of Dr. Ing. h.c.F. Porsche AG and Porsche Cars North America, Inc.; Hogan Lovells on behalf of Daimler AG, Mercedes-Benz USA, LLC, or Mercedes-Benz U.S. International, Inc.; Quinn-Emanuel on behalf of Nissan and

Ford. Case before the US International Trade Commission, Washington D.C., in the matter of: "Certain Automotive Navigation Systems, Components Thereof, and Products Containing Same, Inv. No. 337-TA-814. Case withdrawn by Plaintiff. Retained 1/12-4/12.

## Beacon Navigation GmbH v. Toyota Motor Corporation, et al.

Retained by Kirkland \& Ellis, LLP on behalf of defendants Toyota Motor Corporation; Toyota Motor North America, Inc.; Toyota Motor Sales, U.S.A. Inc.; Toyota Motor Engineering \& Manufacturing North America, Inc.; Toyota Motor Manufacturing, Indiana, Inc.; Toyota Motor Manufacturing, Kentucky, Inc.; Toyota Motor Manufacturing Mississippi, Inc.; Mazda Motor Corporation; Mazda Motor of America, Inc.; Fuji Heavy Industries, Ltd.; Fuji Heavy Industries U.S.A. Inc.; Subaru of America, Inc.; Jaguar Land Rover North America, LLC; Jaguar Cars Limited; Land Rover; Volvo Car Corporation; and Volvo Cars of North America, LLC. Multiple cases before the United States District Court for the District of Delaware. Case numbers 1:11-cv-00942-UNA, 1:11-cv-00941-UNA, 1:11-cv-00951-UNA, 1:11-cv-00952-UNA, 1:11-cv-00936-UNA, 1:11-cv-00937-UNA, 1:11-cv-00955-UNA, 1:11-cv-00959-UNA, and 1:11-cv-00960-UNA. Currently stayed. Retained $1 / 12$ to Present.

## Beacon Wireless Solutions, Inc., et al., v. Garmin International, Inc., et al.

Retained by Shook, Hardy and Bacon, LLP as an expert on behalf of defendant Garmin. Matter involves alleged trade secret misappropriation. Case before the United States District Court for the Western District of Virginia, Harrisonburg Division (Case No. 5:11-cv-00025). Testified in Court: 5/25/12. Retained $12 / 11$ to 5/25/12.

## Tramontane IP, LLC v. Garmin Int'l, Inc., et al.

Retained by Shook, Hardy and Bacon, LLP as an expert on behalf of defendant Garmin. Patents-in-suit are U.S. Patents 6,526,268 and 7,133,775. Case before the United States District Court for the Eastern District of Virginia (Case No. 1:2011-cv-00918). Case Settled. Retained 11/11 to $12 / 11$.

## Sourceprose, Inc. v. AT\&T, Inc., MetroPCS Communications, Inc., et al.

Retained by Kilpatrick Townsend as an expert on behalf of defendant AT\&T. Patents-in-suit are US Patent Nos. 7,142,217 and 7,161,604. Case before the United States District Court for the Western District of Texas, Austin Division. Case number 1:11-cv-00117. Retained 11/11 to present.

## Furuno Electric Co., Ltd. and Furuno U.S.A., Inc. v. Honeywell International, Inc.

 Retained by Quinn-Emanuel as an expert on behalf of complainant Furuno. Case before the US International Trade Commission, Washington D.C., in the matter of: "Certain GPS Navigation Products, Components Thereof, and Related Software," Investigation number 337-TA-810. Patents-in-suit are U.S. Patent Nos. 6,084,565; 7,095,367; 7,089,094; and 7,161,561. Case settled. Retained 8/11-12/11.Honeywell International, Inc. v. Furuno Electric Co., Ltd. and Furuno U.S.A., Inc. Retained by Quinn-Emanuel as an expert on behalf of respondent Furuno. Case before the US International Trade Commission, Washington D.C., in the matter of: "Certain GPS Navigation

Products, Components Thereof, and Related Software," Investigation number 337-TA-783. Patents-in-suit are U.S. Patent Nos. 7,209,070; 6,865,452; 5,461,388; and 6,088,653. Case Settled. Retained 8/11-12/11.

## Triangle Software, Inc. v. Garmin International, Inc.

Retained by Weil, Gotshal \& Manges, LLP., as an expert on behalf of defendant Garmin. Patents-in-suit are US Patents 7,557,730, 7,221,287, 7,375,649, 7,508,321 and 7,702,452. Case before the United States District Court, Eastern District of Virginia, Case No. 1:10-cv-1457 CMH/TCB. Deposed 7/28/11; Testified in Court: 11/3/11 (jury trial). Retained 4/11 to 11/11.

Garmin International, Inc. v. Pioneer Corporation and Pioneer Electronics (USA), Inc. Retained by Shook, Hardy and Bacon, LLP as an expert on behalf of plaintiff Garmin. Patents-in-suit are U.S. Patents 5,365,448; 5,424,951; and 6,122,592. Case before the United States District Court for the District of Kansas. Case No. 10-CV-2080 JWL/GLR. Declarative Judgment action stayed. Retained 3/11 to 11/11.

## Visteon Global Technologies, Inc. And Visteon Technologies, LLC v. Garmin International, Inc.

Retained by Shook, Hardy and Bacon as an expert on behalf of defendant Garmin. Patents-insuit are US Patents 5,544,060, 5,654,892, 5,832,408, 5,987,375 and 6,097,316. Case before the United States District Court, Eastern District of Michigan, Case No. 2:10-cv-10578--PDB-
MAR. Deposed 10/9/12; Retained 12/10 to present.

## Thomson Licensing SAS and Thomson Licensing, LLC. v. Realtek Semiconductor Corporation

Retained by Sidley-Austin as an expert on behalf of respondent Realtek Semiconductor. Case before the US International Trade Commission, Washington D.C., in the matter of: "Certain Liquid Crystal Display Devices, Including Monitors, Televisions, Modules, And Components Thereof," Investigation number 337-TA-741. Patent-in-suit is US Patent 6,121,941. Deposed 6/29/11; Testified in Court: 9/15/11 and 9/16/11. Retained 11/10-9/11.

## Ambato Media, LLC. v. Clarion Co., LTD., et al.

Retained by Traurig-Greenberg as an expert on behalf of defendant Garmin. Patent-in-suit is US Patent $5,432,542$. Case before the United States District Court for the Eastern District Of Texas, Marshall Division. Case number 2:09-CV-242. Deposed 4/26/12 and 5/10/12; Testified in Court: 7/11/12. Retained 10/10 to present.

## Gabriel Technologies Corporation and Trace Technologies, LLC, v. Qualcomm Incorporated, Snaptrack, Inc. and Norman Krasner

Retained by Cooley-Godward as an expert on behalf of defendants Qualcomm, Snaptrack, and Krasner. Trade secret misappropriation case related to US Patents 6,377,209, 6,583,757, 6,661,372, 6,799,050, 6,861,980, 6,895,249, 7,254,402, 7,289,786, 7,319,876, 7,421,277, $7,446,655,7,570,958,7,574,195$, and $7,660,588$. Case before the Southern District of California San Diego Division, Case No. 08-cv-1992 MMA POR. Retained 6/10 to 7/12.

## SiRF/CSR v. Global Locate/Broadcom Corporation

## APPENDIX A

Retained by Wilmer-Hale as an expert on behalf of defendant Global Locate / Broadcom. Patents-in-suit are US Patents 5,663,735, 6,480,150, 6,519,466, 6,650,879, 6,882,827, 6,934,322, $7,412,157,7,236,883$, and $7,573,422$. Case before the Central District of California, Case No. 8:06-cv-01216 and Case No. 8:10-cv-01281. Retained 9/10 to 1/11.

## Pioneer Electronics v. Garmin Corporation

Retained by Shook, Hardy and Bacon, LLP as an expert on behalf of respondent Garmin In the matter of Certain Multimedia Display and Navigation Devices and Systems, Components Thereof, and Products Containing Same; Inv. No. 337-TA-694. Patents-in-suit are U.S. Patents $5,365,448 ; 5,424,951$; and $6,122,592$. Case before the U.S. International Trade Commission. Deposed on 7/29/10; Testified at technology tutorial (8/27/20) and in the evidentiary hearing (9/20/10). Retained 4/10 to 9/10.

## EMSAT Advanced Geo-Location Technology, LLC and Location Based Services LLC, v. AT\&T Mobility, LLC

Retained by Baker-Botts as an expert on behalf of defendant AT\&T Mobility, LLC. Patents-insuit are U.S. Patents $7,289,763$; $5,946,611 ; 6,324,404$; and $6,847,822$. Case before the U.S. District Court for the Northern District of Ohio, Eastern Division, Civil Action No. 4:08 CV 822. Deposed 5/4/10; Testified in Court: 5/10/10 (Markman hearing). Retained 12/09 to 3/11.

## Tendler Cellular of Texas, LLC v. AT\&T Mobility, LLC, et al.

Retained by Baker-Botts as an expert on behalf of defendants AT\&T Mobility, LLC, et al. Patents-in-suit are U.S. Patents 7,447,508; 7,305,243; 7,050,818; and 6,519,463. Case before the U.S. District Court for the Eastern District of Texas (Tyler), Civil Action No. 6:09-CV-00115. Retained 8/09 to 7/10.

## Ambit Corporation v. Delta Air Lines, Inc., and Aircell LLC.

Retained by Sidley Austin, LLP., as an expert on behalf of defendants Delta Airlines, Inc., and Aircell, LLC. Patent-in-suit is US patent 7,400,858. Case before the US District Court, District of Massachusetts, Boston, Civil Action No. 1:09-CV-10217-WGY. Deposed 12/4/09; Testified in Court: 12/7/09 (evidentiary hearing), 7/10 (jury trial). Retained 8/09 to 7/10.

GPS Industries, Inc. and Optimal I.P. Holdings, L.P. v. Altex Corporation, et. al. Retained by Hitchcock-Evert as an expert on behalf of defendants Altex Corporation, Deca International Corporation, Golflogix, Inc. and L1 Technologies. Patent-in-suit is US patent 5,364,093. Case before the US District Court, Northern District of Texas, Dallas Division, Civil Action No. 3-07-CV0831-K. Deposed 6/30/09. Retained 5/08 through 7/09.

## Satellite Tracking of People, LLC v. Omnilink Systems, Inc.

Retained by DLA Piper as an expert on behalf of defendant Omnilink Systems, Inc.. Patent-insuit is US patent RE39,909. Case before the US District Court, Eastern District of Texas, Marshall Division, Civil Action No. 2-08CV-116. 12/08-1/11.

SiRF Technology, Inc. v. Global Locate, Inc.
Retained by DLA Piper/WilmerHale as an expert on behalf of Global Locate. Patents-in-suit include US patents 6,304,216; 6,417,801; 6,606,346; 6,651,000; 6,704,651; 6,937,187;

7,043,363; 7,091,904; 7,132,980 and 7,158,080. Case before the US International Trade Commission, Washington D.C., in the matters of: "Certain GPS Devices and Products Containing Same," Investigation number 337-TA-602 (Global Locate, plaintiff) and "Certain GPS Chips, Associated Software and Systems, and Products Containing Same," Investigation number 337-TA-596 (SiRF Technologies, plaintiff). My work focused on the 7,043,363 and 7,091,904 patents in defense of Global Locate/Broadcom from June 2007 through March 2008. Deposed 1/18-1/19/08; testified at trial 3/18-3/19/08.

## Intellectual Science and Technology

Retained Dykema Gossett, PLCC as a technical expert on patent infringement issues related to "suspend-to-RAM" technologies in personal computers. Pre-litigation work.

## Intellectual Science and Technology, Inc., v. Sony, JVC and Panasonic

Retained Dykema Gossett, PLCC as a technical expert on patent infringement issues related to US Patent 5,748,575, US Patent 6,222,799, US Patent 6,785,198, US Patent 6,662,239 and US Patent 6,717,890. Sony Electronics Inc., case number 2:06-CV-10406, JVC Americas Corp., case number 2:06-CV-10409 and Panasonic Corporation of North America case number 2:06-CV-10412. Cases heard in United States District Court, Eastern District of Michigan, Southern Division. Expert for Intellectual Science and Technology, Inc. Dec 2006 - 2008..

## Kirsch Technologies v. Xerox, Canon

Retained Dykema Gossett, PLCC as an Expert Witness on patent infringement issues related to US Patent $4,816,911$, Canon case number CA 00-72775, Xerox case number CA 00-72778, cases heard in United States District Court, Eastern District of Michigan, Southern Division. Expert for Kirsch Technologies. Nov 2006 - 2008.

## American Video Graphics v. ATI Technologies

Retained by Sidley, Austin, Brown \& Wood, Dallas, TX as a technical expert on patent infringement issues related to US Patents 5,132,670, 5,109,520, 5,084,830, 4,761,642, 4,742,474, 4,734,690, 4,730,185 and 4,694,286. Hewlett-Packard Co., et al., defendants, case number CA 6:04-CV-379-LED and Sony Corporation of America et al., defendants, case number CA 6:04-CV-399-LED. Cases heard in United States District Court, Eastern District of Texas, Tyler Division. Expert for ATI Technologies, intervener. Jan 2005 - Sep 2005.

## Microsoft v. EMC

Dewey Ballantine, LLP, Washington, D.C., as a technical expert on patent infringement issues related to US Patents 5,588,147; 5,689,700; 6,393,466; 6,424,151; 6,490,594; and 6,632,248. Wrote a declaration on behalf of Microsoft. Oct 2004 - Jan 2005.

## Optimum Return v. Meier Brothers

Retained by Sidley, Austin, Brown \& Wood, Dallas, TX as a technical expert on Copyright infringement allegations related to software owned by Optimum Return, LLC. Cyberkatz Consulting, Inc., Handsquare, LLC, Meier Brothers, et al., defendants, case number CA 3-03CV1064-D. Case heard in United States District Court, Northern District of Texas, Dallas Division. Expert for Meier Brothers. July 2004.

## Parental Guide of Texas, Inc. v. Funai Corp., et. al.

Technical expert for defendants JVC and Panasonic in their dispute over non-infringement of US Patent number 4,605,964.

## Elonex I.P. Holdings, LTD. and Elonex PLC, Phase II

Expert witness for defendants Chuntex, Acer, Tatung, Lite-On, Daewoo and Envision in their dispute with Elonex non-infringement and validity for US Patent numbers 5,389,952; 5,648,799; and $5,880,719$.

## Storage Computer Corporation vs. Veritas Software

Technical expert for the plaintiff in matters involving Patents US 5,257,367; US 5,893,919; and US 6,098,128.

## Storage Computer Corporation vs. Seagate Technology LLC

Technical expert for the defendant in matters involving US Patent RE 34,100.
Elonex I.P. Holdings, LTD. and Elonex PLC, vs. Packard Bell et. al., CA 98-689-GMS Expert witness for defendants ViewSonic Corp., Dell Computer Corporation, MAG Technology USA, Princeton Graphic Systems, Inc., Micron Electronics, Sony Electronics and Capetronic Computer USA in their dispute with Elonex non-infringement and validity for US Patent numbers 5,389,952; 5,648,799; and 5,880,719.

### 1.4.2 Engineering Consulting

## Offspring Media Inc.

Technical consultant for the development of real-time auralization algorithms for integration into a consumer electronics product. Sep 2004.

Raytheon Company, Sudbury, MA
Development of techniques and requirements for implementing a fault tolerant computer system using software implemented fault tolerance (SIFT) techniques on commercial off-the-shelf processing hardware. The resultant system is to be used for highly reliable radar data and signal processing.

## TVM Techno Venture Management

Provided consulting services to assist in assessing the technical claims of a company pursuing venture capital investment for a hardware implemented RAID 5 system .

Keyhold Engineering Inc., Northboro, MA.
Development of a prototype system for automatically calibrating multiple channel audio systems.

## American Navigation Systems Inc., Milbury, MA.

Consulting on the development of the hand-held personal navigation and mapping system.

## Lincoln Laboratory, Bedford, MA.

Simulated, tested and evaluated a GPS integrity monitoring algorithm developed at Lincoln Laboratories.

### 1.5 Licenses and Certifications

### 1.5.1 Commercial

General Radiotelephone Operator License
Ship RADAR endorsement

### 1.5.2 Amateur

Amateur Extra class radio operator license.

## 2. Courses Taught at WPI

### 2.1 Course Descriptions

Short descriptions of the courses taught are as follows:

## EE572N Advanced System Architecture

This course focuses on the architectural techniques used to achieve high-performance in SISD and SIMD computer systems. In this course the interaction between the software application and hardware architecture and the effect of this interaction on achievable performance is stressed. The course begins by covering the basic architectural tricks used to enhance system performance and ends with a series of case studies that analyze specific architectures such as the CRAY and CDC vector supercomputers, the MasPar, the Connection Machine, the ICL DAP, and others.

## ECE505 Computer Architecture

This course is an introductory graduate course in computer architecture. Most aspects of CPU architecture are covered using a combined hardware/software approach. Specific topics include datapath design, memory systems, microprogramming, memory management, operating systems, and instruction set design.

## ECE579M Real-Time System Design

This course focuses on the design of computer systems for which the timeliness of producing results is a critical factor for establishing the correctness of the system design. Topics covered include hardware specification, real-time operating systems and programming, scheduling, communications, and validation/verification. Issues and choices arising for single processor and distributed systems are also covered. Both hard and soft real-time system issues and the interactions between real applications and real systems is stressed.

## ECE2010 Introduction to Electrical and Computer Engineering.

The objective of this course is to introduce students to the broad field of electrical and computer engineering within the context of real world applications. This course is designed for first-year students who are considering ECE as a possible major or for non-ECE students fulfilling an out-of-major degree requirement. The course will introduce basic electrical circuit theory as well as analog and digital signal processing methods currently used to solve a variety of engineering design problems in areas such as entertainment and networking media, robotics, renewable energy and biomedical applications. Laboratory experiments based on these applications are used to reinforce basic concepts and develop laboratory skills, as well as to provide system-level understanding. Circuit and system simulation analysis tools are also introduced and emphasized.

## ECE2022 Introduction to Digital Circuits and Computer Engineering.

The objective of this course is to expose students (including first year students) to basic electrical and mathematical concepts that underlie computer engineering while continuing an introduction to basic concepts of circuits and systems in a hands-on environment. Experiments representing practical devices introduce basic electrical engineering concepts and skills which typify the study and practice of electrical and computer engineering. In the laboratory, the students construct, troubleshoot, and test analog and digital circuits that they have designed. They will also be introduced to the nature of the interface between hardware and software in a typical microprocessor based computer.

## ECE2801 Foundations of Embedded Systems

This course teaches the principles of programming microprocessors and microcontrollers for real-time applications. Students are introduced to software engineering principles and are taught how to translate product specifications into engineering solutions.

## ECE2799 ECE Design

This is a new course added to the curriculum that teaches sophomore Electrical Engineering students the basic principles of design. Topics are covered which range from project planning and management through manufacturing and implementation. Students are exposed to external factors influencing design such as safety, liability, cost, and other constraints.

## ECE3801 Logic Circuits

This is an introductory course in logic circuit design. Topics covered include Boolean Logic, Algebraic minimization of logic equations, Karnaugh Maps, sequential machine design and timing analysis.

## ECE3803 Introduction to Microprocessor Systems

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This is an undergraduate-level first-course in microprocessor design. Topics covered include timing analysis, address decoding, memory system design, assembly language programming, programmed I/O, and digital/analog interfacing. Experiments are run using ISA-bus interfaces to standard PCs.

## ECE3810 Advanced Digital System Design

This course addresses the design of advanced digital logic systems using VHDL to design, synthesize and model digital circuits, and to implement these circuits using Xilinx FPGA devices. The course emphasizes understanding functional design, designing for speed and power objectives, and testing. The course ends with students designing moderately complicated "system on a chip" (SOC) based systems

## ECE4815 Computer Architecture (crosslisted as CS4515)

A first course in computer architecture. Essential aspects of CPU architecture are covered using a combined hardware/software approach. Students learn how a CPU interprets and processes instructions. Issues associated with interfacing hardware with software are covered in detail as are the hardware/software tradeoffs associated with performance optimization.

## ECE4801 Microprocessor System Design

Microprocessor System Design is the second course in the microprocessor sequence. In this course, students learn the advanced concepts used in modern microprocessor systems. Topics such as system organization, dynamic and cache memory systems, communications, mixed language programming, and device driver design are covered.

## ECE430X Fundamentals of Navigation Systems

This course introduces students to the fundamentals of navigation using electronic systems. The course covers types of navigation systems, how to interpret sensor data and sources of navigation system error. Topics include: types of navigation systems (dead reckoning, inertial, radio based systems), sensors and error sources, coordinate frames and transformations, system dynamics and measurement processing. Case studies explore the use of accelerometers, gyroscopes, GPS (including, differential and assisted GPS) as well as other types of navigation systems.

## RBE 3001 Unified Robotics III

Third of a four-course sequence introducing foundational theory and practice of robotics engineering from the fields of computer science, electrical engineering and mechanical engineering. The focus of this course is actuator design, embedded computing and complex response processes. Concepts of dynamic response as relates to vibration and motion planning will be presented. The principles of operation and interface methods various actuators will be discussed, including pneumatic, magnetic, piezoelectric, linear, stepper, etc. Complex feedback

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mechanisms will be implemented using software executing in an embedded system. The necessary concepts for real-time processor programming, re-entrant code and interrupt signaling will be introduced. Laboratory sessions will culminate in the construction of a multi-module robotic system that exemplifies methods introduced during this course.

## RBE 3002 Unified Robotics IV

Fourth of a four-course sequence introducing foundational theory and practice of robotics engineering from the fields of computer science, electrical engineering and mechanical engineering. The focus of this course is navigation, position estimation and communications. Concepts of dead reckoning, landmark updates, inertial sensors, vision and radio location will be explored. Control systems as applied to navigation will be presented. Communication, remote control and remote sensing for mobile robots and tele-robotic systems will be introduced. Wireless communications including wireless networks and typical local and wide area networking protocols will be discussed. Considerations will be discussed regarding operation in difficult environments such as underwater, aerospace, hazardous, etc. Laboratory sessions will be directed towards the solution of an open-ended problem over the course of the entire term.

## RBE 400x Robot System Engineering and Design

The designers of robotic systems start with a system requirement to define the mechanical, electrical and software systems which must work together to achieve the system goals. Typically, parallel teams of engineers will work concurrently to create the requirements document as well as model various aspects of the system to verify operational capabilities and the ability to meet time and budget constraints. For complex systems, the development of such teams can itself be a complex problem since the project has to be organized in such a way that parallel teams can work independently, yet have excellent communication channels and information passing to insure project success.

This course explores the tools and techniques used to develop complex systems. The topics covered include: requirements development; system architecture and partitioning; requirements flowdown; functional and interface specifications; trade studies; system modeling and simulation; system integration; as well as design verification and validation.

## RBE500 Foundations of Robotics

Foundations and principles of processing sensor information in robotic systems. Topics include an introduction to probabilistic concepts related to sensors, sensor signal processing, multi-sensor control systems and optimal estimation. The material presented will focus on the types of control problems encountered when a robot must operate in an environment where sensor noise and/or tracking errors are significant. Techniques for assessing the stability, controllability and expected accuracy of multi-sensor control and tracking systems will be presented. Lab projects will involve processing live and synthetic data, robot simulation and projects involving the control of robot platforms.

## 3. List of Publications:

### 3.1 Journal Papers

[1] T. Padir, W.R. Michalson, et. al., "Implementation of an Undergraduate Robotics Engineering Curriculum," Computers in Education Journal, vol. I, no. 3, pp. 92-101, 2010.
[2] W. R. Michalson, A. Navalekar and H. Parikh, "Error mechanisms in indoor positioning systems without support from GNSS," The Journal of Navigation, Cambridge University Press, vol. 62, no. 2, pp. 239-49, 2009.
[3] H.K. Parikh and W. R. Michalson, "Impulse Radio - UWB or Multicarrier UWB for Non-GPS based Indoor Precise Positioning Systems," NAVIGATION J. Inst. Nav., Vol. 55, no. 1, 2008.
[4] I. F. Progri, W. R. Michalson, J. Wang and M.C. Bromberg, "Indoor Geolocation Using FCDMA Pseudolites: Signal Structure and Performance Analysis", NAVIGATION J. Inst. Nav., Vol. 54, No. 3, Fall 2007.
[5] I. F. Progri, M. C. Bromberg and W. R. Michalson, "Maximum-Likelihood GPS Parameter Estimation", NAVIGATION J. Inst. Nav., vol. 52, no. 4, pp. 229-238, Winter, 2005-2006.
[6] I.F. Progri, W.R. Michalson, and D. Cyganski, "An OFDM/FDMA Indoor Geolocation System," NAVIGATION J. Inst. Nav., vol. 51, no. 2, pp. 133-142, Summer, 2004.
[7] I.F. Progri, G. Bogdanov, V.C. Ramanna, and W.R. Michalson, "An Investigation Of A GPS Adaptive Temporal Selective Attenuator," NAVIGATION J. Inst. Nav., Vol. 49 No. 3, pp. 137-147, 2002.
[8] G. Bogdanov, W. R. Michalson, and R. Ludwig, "A new apparatus for non-destructive evaluation of green-state powder metal compacts using the electrical resistivity method," Measurement Science and Technology, IOP Publishing, vol. 11, pp. 157-166, January 2000.
[9] B. Findlen, E. Reuter, R. Campbell, and W. R. Michalson, "Effects of time domain response on the sonic characteristics of microphones," Journal of the Acoustical Society of America, vol. 104, no. 3, pt. 2 pp. 1764, September 1998.
[10] J. Sedgwick, W. R. Michalson, and R. Ludwig, "Design of a Digital Gauss Meter for Precision Magnetic Field Measurements," IEEE Transactions on Instrumentation and Measurement, vol. 47, no. 4, pp. 972-977, August 1998.
[11] J. Stander, J Plunkett, W. Michalson, J. McNeill, and R. Ludwig, "A Novel Multi-Probe Resistivity Approach to Inspect Green-State Powdered Metallurgy Compacts," Journal of Non-Destructive Evaluation, vol. 16, no. 4, pp. 205-214, 1997.
[12] Woltereck, R. Ludwig, and W. Michalson, "A Quantitative Analysis of the Separation of Aluminum Cans Out of a Waste Stream Based on Eddy Current Induced Levitation," IEEE Transactions on Magnetics, vol. 33, no. 1, pp. 772-781, January 1997.
[13] W. R. Michalson, "Auralization on a Laptop PC," abstract appears in The Journal of the Acoustical Society of America , vol. 100 No. 4, Pt 2, pp. 2608, October 1996.

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[14] R. H. Campbell, S. K. Martin, I. Schneider, and W. R. Michalson, "Analysis of Mosquito Wingbeat Sound," The Journal of the Acoustical Society of America vol. 100 No. 4, Pt 2, pp. 2710, October 1996.
[15] W. R. Michalson, "Ensuring GPS Navigation Integrity using Receiver Autonomous Integrity Monitoring," IEEE Aerospace and Electronic Systems Magazine. vol. 10, no. 10, pp. 31-34, October 1995.
[16] S. Clayton, R. J. Duckworth, W. Michalson, A. Wilson, "Determining Update Latency Bounds in Galactica Net," Concurrency: Practice, and Experience, vol. 7, no. 7, pp. 595611, October 1994.

### 3.2 Conference Papers

[1] K.C. Seals, W.R. Michalson, R.J. Hartnett and P.F. Swaszek, "Using Both GPS L1 C/A and L1C: Strategies to Improve Acquisition Sensitivity," Proc. $26^{\text {th }}$ International Technical Meeting of the Satellite Division of the Institute of Navigation (ION GNSS 2013), Sep. 16-20, 2013.
[2] K.C. Seals, W.R. Michalson, R.J. Hartnett and P.F. Swaszek, "Semi-Coherent and Differentially Coherent Integration for L1C Acquisition," Proc. 2013 International Technical Meeting of the Institute of Navigation (ION ITM 2013), Honolulu, HI, Apr. 22-25, 2013.
[3] J.M. Barrett, M.G. Gennert, W. R. Michalson, et. al., "Development of a Low-Cost, SelfContained, Combined Vision and Inertial Navigation System," 2013 International Conference on Technologies for Practical Robotic Applications, Boston, MA Apr. 22-23, 2012.
[4] K.C. Seals, W.R. Michalson, R.J. Hartnett and P.F. Swaszek, "Analysis of L1C Acquisition by Combining Pilot and Data Components Over Multiple Code Periods," Proc. 2013 International Technical Meeting of the Institute of Navigation (ION ITM 2013), San Diego, CA, Jan. 28-30, 2013.
[5] K.C. Seals, W.R. Michalson, R.J. Hartnett and P.F. Swaszek, "Analysis of Coherent Combining for L1C Acquisition," Proc. $25^{\text {th }}$ International Technical Meeting of the Satellite Division of the Institute of Navigation (ION GNSS 2012), pp.384-393, Nashville, TN, Sep. 17-21, 2012.
[6] J.M. Barrett, M.G. Gennert, W. R. Michalson and J.L. Center, "Analyzing and Modeling an IMU for Use in a Low-Cost Combined Vision and Inertial Navigation System," 2012 International Conference on Technologies for Practical Robotic Applications, Boston, MA Apr. 23-24, 2012.
[7] G. Fischer, W. R. Michalson, T. Padir and G. Pollice,"Development of a Laboratory Kit for Robotics Engineering Education" AAAI 2010 Spring Symposium on Educational Robotics and Beyond: Design and Evaluation, Mar. 22-24, Palo Alto, CA, 2010.
[8] W.R. Michalson, and F. J. Looft, "Designing Robotic Systems: Preparation for an Interdisciplinary Capstone Experience," American Society of Engineering Educators 2010 Annual Conference, Louisville, KY, Jun 20-23, 2010.
[9] W.R. Michalson, S.J. Bitar and R.C.Labonte, "The Technical, Process, and Business Considerations For Engineering Design - A 10 Year Retrospective," American Society of Engineering Educators 2010 Annual Conference, Louisville, KY, Jun 20-23, 2010.
[10] M. Gennert, M. Demietrio and W. R. Michalson, "A Robotics Engineering M.S. Degree," American Society of Engineering Educators 2010 Annual Conference, Louisville, KY, Jun 20-23, 2010.
[11] R. Beach, W. R. Michalson, et. al., "Robotics Innovations Competition and Conference (RICC): Building Community Between Academia and Industry Through a UniversityLevel Student Competition," American Society of Engineering Educators 2010 Annual Conference, Louisville, KY, Jun 20-23, 2010.
[12] G. Tryggvason, W.R. Michalson, et. al., Teaching Multidisciplinary Design to Engineering Students: Robotics Capstone," American Society of Engineering Educators 2010 Annual Conference, Louisville, KY, Jun 20-23, 2010.
[13] A.C.Navalekar, W.R. Michalson, "Asymmetric throughput problem due to Push-to-talk (PTT) delays in CSMA/CA based heterogeneous Land Mobile Radio (LMR) networks", accepted for publication, Milcom 2009.
[14] A. Navalekar and W.R. Michalson, "Effects of Unintentional Denial of Service (DOS) due to PTT delays on performance of CSMA/CA based Adhoc Land Mobile Radio (LMR) networks", accepted for publication, ICST Adhocnet 2009.
[15] W. R. Michalson, et. al., "Unified Robotics: Balancing Breadth and Depth in Engineering Education", American Society of Engineering Educators 2009 Annual Conference, AC 2009-1681, Austin, TX, Jun 14-17, 2009.
[16] G. Tryggvason, W.R. Michalson, et. al., "Robotics Engineering: A New Discipline for a New Century", American Society of Engineering Educators 2009 Annual Conference, AC 2009-997, Austin, TX, Jun 14-17, 2009.
[17] M. DiBlasi, W. R. Michalson, et. al., "Social Networking in the FIRST Robotics Competition Community," ASEE Northeast Section Conference, University of Bridgeport, Apr 3-4, Bridgeport, CT, 2009.
[18] A. Navalekar, H.K Parikh and William R. Michalson,"Error Mechanisms in Indoor Positioning Systems without Support from GNSS", RIN NAV 08.
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### 3.3 Book Chapters

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### 3.4 Patents

## Precision location methods and systems

United States Patent 8,928,459, Issued January 6, 2015

The invention describes systems and methods for determining the location of a transmitter by jointly and collectively processing the full sampled signal data from a plurality of receivers to form a single solution.

## Apparatus and methods for addressable communication using voice-grade radios

United States Patent 8,284,711, Issued 9 October 2012
The invention relates to methods and apparatus for conducting directed communication using voice-grade radios. The methods and apparatus can be used to form a packet-switched wireless network using legacy analog transceivers, providing, e.g., both data and voice-over-Internet Protocol communication.

## Multi-channel electrophysiologic signal data acquisition system on an integrated circuit.

 United States Patent 7896807, issued 3 March 2011.A physiologic data acquisition system includes an analog input, a sigma-delta front end signal conditioning circuit adapted to subtract out DC and low frequency interfering signals from and amplify the analog input before analog to digital conversion. The system can be programmed to acquire a selected physiologic signal, e.g., a physiologic signal characteristic of or originating from a particular biological tissue. The physiologic data acquisition system may include a network interface modulating a plurality of subcarriers with respective portions of an acquired physiologic signal. A receiver coupled to the network interface can receive physiologic data from, and send control signals and provide power to the physiologic data acquisition system over a single pair of wires. The network interface can modulate an RF carrier with the plurality of modulated subcarriers and transmit the resulting signal to the receiver across a wireless network. An integrated circuit may include the physiologic data acquisition system. Also included are methods for acquiring physiologic data comprising the step of selectively controlling an acquisition circuit to acquire the physiologic signal.

Methods and apparatus for high resolution positioning. United States Patent 7292189. The invention relates to a method of signal analysis that determines the location of a transmitter and to devices that implement the method. The method includes receiving by at least three receivers, from a transmitter, a first continuous-time signal having a first channel. The first channel includes a first plurality of signal carriers having known relative initial phases and having known frequencies which are periodically spaced and which are orthogonal to one another within a first frequency range. The signal analysis method also includes determining the phase shifts of the carriers of the first channel resulting from the distance the carriers traveled in reaching the first receiver. Analysis of the phase shifts yields time difference of arrival information amongst the receivers, which is further processed to determine the location of the transmitter. 6 Nov 2007.

A Reconfigurable Indoor Geolocation System, US Patent Number 7,079,025. A portable reconfigurable geolocation system is provided. The system includes a portable user node and one or more portable pseudolite nodes in communication one another and with the user node. Each of the user nodes and pseudolite nodes includes a transmitter that generates a signal on one or more carrier frequencies. Each signal is modulated with digital signals necessary to establish distances between the nodes and to convey data between the nodes. Each node also includes a receiver for receiving and demodulating the signals transmitted between the nodes, and a processor for receiving the demodulated signals, extracting data values and derived values from the
demodulated signals and determining a three-dimensional position of each node in the system. Issued 18 Jul 2006.

Auto-Calibrating Surround System, United States Patent 7158643. A multi-channel surround sound system and method is described that allows automatic and independent calibration and adjustment of the frequency, amplitude and time response of each channel of the surround sound system. The disclosed auto-calibrating surround sound (ACSS) system includes a processor that generates a test signal represented by a temporal maximum length sequence (MLS) and supplies the test signal as part of an electric input signal to a loudspeaker. A microphone coupled to the processor receives the signal in a listening environment. The processor correlates the received sound signal with the test signal in the time domain and determines from the correlated signals a whitened response of the audio channel in the listening environment. Issued 2 Jan 2007.

Hand-held GPS-mapping device, US. Patent Number 5,987,380. A hand-held navigation, mapping and positioning device contains a GPS receiver, a database capable of storing vector or bit mapped graphics, a viewing port, an embedded processor, a simplified user interface, a data compression algorithm, and other supporting electronics, The viewport is configured such that the data presented in the viewport if clearly visible in any ambient light condition. The database stores compressed image data which might include topographical map data, user annotations, building plans, or any other image. The system includes an interface to a personal computer which may be used to annotate or edit graphic information externally to the device for later upload. In addition, the device contains a simple menu-driven user interface which allows panning and zooming the image data, marking locations of interest, and other such functions. The device may be operated from an internal rechargeable battery, or powered externally. , Issued 16 Nov 1999.

Hand-held GPS-mapping device, US. Patent Number 5,902,347. A hand-held navigation, mapping and positioning device contains a GPS receiver, a database capable of storing vector or bit mapped graphics, a viewing port, an embedded processor, a simplified user interface, a data compression algorithm, and other supporting electronics. The viewpoint is configured such that the data presented in the viewport is clearly visible in any ambient light condition. The database stores compressed image data which might include topographical map data, user annotations, building plans, or any other image. The system includes an interface to a personal computer which may be used to annotate or edit graphic information externally to the device for later upload. In addition, the device contains a simple menu-driven user interface which allows panning and zooming the image data, marking locations of interest, and other such functions. The device may be operated from an internal rechargeable battery, or powered externally. Issued 11 May 19/99.

### 3.5 Professional Presentations

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Agilent Wireless Technology Summit: Dynamic Node Location in an Ad Hoc Indoor
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Security \& Technology Online (SATO) Security Leadership Council. Panel discussion on Smart Surveillance, Command and Control, Oct 28-29, 2004.
"Worcester Polytechnic Institute Barcelona Summit: The Future of Information Technology," delivered presentation entitled "Personal Navigation in the Information Age," Apr 2001.

## 4. Projects advised (undergraduate).

### 4.1 Major Qualifying Projects (current)

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### 4.2 Major Qualifying Projects (completed)

[2] Aeacus, N. Anderson, D. Praetorius and C. Roddy, co-advised with S. Nestinger, 2011.
[3] Realization of Performance Advancements for WPI's UGV-Prometheus, M. Akmanalp, R. Doherty, J. Gorges, P. Kalauskas, E. Peterson and F. Polido, co-advised with T. Padir, S. Nestinger, M. Ciraldi, K. Stafford, 2011.
[4] Autonomous Underwater Vehicle, J. Baker, C. Frumento, J. Grzyb and T. North, coadvised w/I. Hussein, 2011.
[1] Tactical Vest, V. Brisian, J. Fernando, A. Khandaker and J. Zorrilla DeLos Santos, 2011.
[2] Marsupial AUV, N. Smith, B. Berard and C. Pietre, Lincoln Laboratory Project Center, co-advised with G. Heiniman, 2010.
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[5] Accurate Real-Time Audio Circuit Simulation, B. Gleason, WZM-MB09, 2010.
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[29] WZM-MQP-1C01: PC Controlled Laser Light Show Device, Joel Smith, 2001.
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[31] WZM-MQP-2A00: Automotive PC Development Platform Travis Pouliot and David Philips, 2001.
[32] The RoadCom Automotive Computing System, Benjamin Kennedy and John Pong, 2000.
[33] WZM-MQP-1A99: Compressed Sample Wavetable Synthesizer, Justin Brzozoski, 2000.
[34] WZM-MQP-3499, Automatically Equalizing Monitor, Fernando Braghin, Tenzin Lama, Rahul Bhan and Dion Soetadi, 2000.
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[39] Digital Image Enhancement, Julie Bolduc, Wei Fu and Joseph Perry, 2000.
[40] WZM-MQP-4A98, Railroad Communications System, Matthew Lug, 1999.
[41] 99D078M: Modular Effects Processor II, Erik Neyland, 1999.
[42] 99D176M: Portable Digital Audio Recorder Eric Toledo and Duc Truong, 1999.
[43] EE-WZM-1A97, C Sound Synthesizer, Ross E. Borgeson, Michael W. Hamel and Matthew S. Walsh, 1998.
[44] EE-WZM-4A97, Firewire Audio Device, Daniel R. Stutzbach, 1998.
[45] EE-WZM-2A97, Modular Effects Processor, Michael J. Dellisanti, 1998.
[46] EE-WZM-3A97, GPS Personal Navigation, Jeffery A. Alderson and Helder Machado, 1998.
[47] HU-FB-CS01, C Sound Synthesizer, Peter W. DeBonte (co-advised).
[48] EE-WZM-1E97, PM Measurement System, Yevgeniy Bogdanov.
[49] EE-REL-C008, Design and Development of a Microprocessor-Based Gaussmeter, David M. Burnham.
[50] EE-WZM-RC01, Acoustic Guitar Amplifier, Christopher Thomas.
[51] EE-WZM-GSD1, Guitar Sustaining Device, Paul D’Ambra.
[52] EE-RXV-5260, Audio Feedback Elimination System, Ross D. Pease and John R. Pelliccio.
[53] EE-RJD-M963, Embedded Systems Design, Christopher A. Briggs and Anthony J. Viapiano.
[54] EE-WHE-9601, GPS Hazard Detector, Michael Roberts, William Cidela, and Chris Mangiarelli.
[55] EE-WZM-2C96, Flexible Synthesis, Noah T. Vawter and Luke Demoracski.
[56] EE-WZM-1A96, Tap Dancer MIDI Interface, Thomas Trela and William Dowell.
[57] EE-WZM-2A96, GPS Hazard Detector II, Will Brothers, Jon Day, and John Zaghi.
[58] EE-WZM-3A96, Loudspeaker Data Acquisition System, Adam Gross.
[59] EE-WZM-4A96, Audio Morphing Processor, William Butterfield and Ted Phipps.
Page 29 of 35
[60] EE-WZM-5A96, Acoustic Modeling, Peter DeBonte.
[61] EE-WZM-1B96, Distributed Audio Controller, Stephen S. Richardson.
[62] EE-WZM-1A95, Acoustic Hazard Meter, Ronald D. Slack.
[63] EE-WZM-2A95, Forest Service DGPS, Joshua J. Single and Michael T. Spadazzi.
[64] EE-WZM-1C95, Audio to MIDI Converter, Jennifer R. Principe.
[65] EE-WZM-1D95, Low Cost Auralizer, Jason R. Hills and Mark R. Paulson.
[66] EE-WZM-3A95, Passive Radiator Design, Kevin R. Weldon.
[67] EE-WZM-1C94, Char Model Generation, Colin J. Florendo.
[68] EE-WZM-1D94, Wide Area DGPS Simulator, Daniel Cohen and Robert Schroter.
[69] EE-WZM-2D94, Digital Soundcard, Timothy Alsberg (Russian Project Center).
[70] EE-WZM-3D94, Digital Univibe, Andrew Willis and Daniel Toohey.
[71] EE-WZM-1A94, DSP Based Real-Time Audio Feedback Eliminator, Kevin M. Eddy.
[72] EE-WZM-2A94, Digital LCD Oscilloscope, William F. Brown and John F. Ebersole.
[73] 93D236M, MIDI Mapper, Jonathan Kemble and Brian Candiloro.
[74] EE-WZM-1C93, Fault-Tolerant Computer, Frederick N. Parmenter.
[75] EE-WZM-1A93, Wireless MIDI Controller, Sanjay Raja, Charles Cimalore, Ty Panagoplos.
[76] EE-WZM-2A93, Multiple Pitch Detector, Jeanne A. Sawtelle.
[77] EE-WZM-3A93, Multiprocessor Cache Coherence, Lauren C. Lind and Norman E. Rhodes.
[78] EE-WZM-1C92, A Simulation of the DLX Architecture, Lisa Harlow.
[79] EE-WZM-2C92, A New Microprocessor Development System, Gregory B. Burlingame, David J. Fortin, Kevin S. Pearson.
[80] EE-WZM-1A92, Digital Audio Sampler, Roger D. Gagnon and James M. Lach.
[81] EE-WZM-2A92, Intelligent Harmonizer, Prabhjot S. Anand and Aftab M. Yusuf.
[82] EE-WZM-3A92, Computerized Audio Mixer, Richard J. Wood.
[83] EE-WZM-1B92, Real-Time Harmonizer, Mohiuddin M. Kahn.
[84] EE-WZM-1A91, Residue Number System Processor, Ravdeep S. Anand and Christine A. Easton.
[85] EE-WZM-2A91, SCSI Bus Analyzer, Brian Costello, George Delouriero, Matthew Maguire, and Keith Nevins.

### 4.3 Graduate Theses Advised and Co-Advised

### 4.3.1 MS Theses (current)

[1] No Current MS Students

### 4.3.2 MS Theses (completed)

[1] Morin, Russell, "A Novel Localization System For Experimental Autonomous Underwater Vehicles," MS Thesis, co-advisor, Worcester Polytechnic Institute, 2010.
[2] Navalekar, Abhijit, "Design of an OFDM-Based VHF Modem," MS Thesis, primary advisor, Worcester Polytechnic Institute.
[3] Ahlehagh, Hasti, "Techniques for Communications and Geolocation Using Wireless Ad Hoc Networks," MS Thesis, primary advisor, Worcester Polytechnic Institute, 2004.
[4] Sebastian, Dalys, "Development of a Field-Deployable Ultrasound Scanner System," MS Thesis, co-advisor, Worcester Polytechnic Institute, 2004.
[5] Tobgay, Sonam, "Novel Concepts for RF Surface Coils with Integrated Receivers," MS Thesis, co-advisor, Worcester Polytechnic Institute, 2004.
[6] Breen, Daniel, "Characterization of Multi-Carrier Locator Performance," MS Thesis, coadvisor, 2004.
[7] Aghogho, Obi, "A Novel Radio Frequency Coil Design for Breast Cancer Screening in a Magnetic Resonance Imaging System," MS Thesis, co-advisor, Worcester Polytechnic Institute, 2003.
[8] Fei, Ming, "Electromagnetic Detection, Infrared Visualization and Image Processing Techniques for Non-Metallic Inclusions in Molten Aluminum," MS Thesis, co-advisor, 2002.
[9] Lavoie, Bruce, "Design and Implementation of an N-Channel Self Calibrating Audio System," MS Thesis, primary advisor, Worcester Polytechnic Institute, 2000.
[10] Bogdonov, Gene, "Theoretical and Practical Implementation of Electrical Impedance Material Inspection of Powder Metallurgy Compacts," MS Thesis, co-advisor, Worcester Polytechnic Institute, 1999.
[11] Messier, Andrew, "Modeling the Effects of Terrain Masking on GPS Accuracy and Integrity," MS Thesis, primary advisor, Worcester Polytechnic Institute, 1998.
[12] Antonescu, Bogdan, "Elliptic Curve Cryptosystems on Embedded Microprocessors," Bogdan Antonescu, MS Thesis, co-advisor, Worcester Polytechnic Institute, 1998.
[13] Lai, Qiang, "Ground-Penetrating Radar Data Processing System," MS Thesis, co-advisor, Worcester Polytechnic Institute, 1998.
[14] Soria-Rodríguez, Pedro, "Multicast-Based Interactive-Group Object-Replication For Fault Tolerance," MS Thesis, co-advisor, Worcester Polytechnic Institute, 1998.
[15] Hoy, William, "Audio Signal Denoising Using Wavelets," MS Thesis, primary advisor, Worcester Polytechnic Institute, 1997.
[16] Progri, Ilir, "Harmonic Flow Monitoring by means of Global Positioning System," MS Thesis, primary advisor, Worcester Polytechnic Institute, 1997.
[17] Bretchko, Pavel, "Pulsed Hysteresis Graph System," MS Thesis, co-advisor, Worcester Polytechnic Institute, 1997.
[18] Repkin, Dmitry V., "A Hierarchical Neural Network Based Data Processing System for Ground Penetrating Radar," MS Thesis, co-advisor, Worcester Polytechnic Institute, 1997.
[19] Metsis, Sophocles, "Design of a Real-Time Capable, Fault-Tolerant, Distributed System," MS Thesis, primary advisor, Worcester Polytechnic Institute, 1996.
[20] Hill, Jonathan, "Efficient Implementation of Mesh Generation and FDTD Simulation of Electromagnetic Fields," MS Thesis, primary advisor, Worcester Polytechnic Institute, 1996.
[21] Dunkelberg, John, "FEM Mesh Mapping to a SIMD Machine Using Genetic Algorithms," MS Thesis, co-advisor, Worcester Polytechnic Institute, 1996.
[22] Leuenberger, Georg, "Design and Development of a Microprocessor Based Gauss Meter," MS Thesis, co-advisor, Worcester Polytechnic Institute, 1995.
[23] Valentino, Ralph, "DISC: A Dynamic Instruction Set Coprocessor," MS Thesis, primary advisor, Worcester Polytechnic Institute, 1995.
[24] Muley, Aalok, "A Fault Tolerant Network for a Real-Time Environment," MS Thesis, primary advisor, Worcester Polytechnic Institute, 1994.
[25] Mohan, Surrender, "Automatic Surface Mesh Generation for 3D Solid Models Using Delaunay Algorithm," MS Thesis, co-advisor, Worcester Polytechnic Institute, 1994.
[26] Petrangelo, John, "Experimental Preconditioners for Large Dense Systems," MS Thesis, co-advisor, Worcester Polytechnic Institute, 1994.
[27] Schneider, Eric, "Design, Simulation, and Analysis of a 3D Integrated Optical Computer," MS Thesis, primary advisor, Worcester Polytechnic Institute, 1993.
[28] Palmer, Bradley, "A Comparison of Three Protocols Supporting Time-Dependent and Time-Independent Communications," MS Thesis, primary advisor, Worcester Polytechnic Institute, 1992.
[29] Clayton, Shawn, "An Analysis of the Real-Time Behavior of Galactica Net," MS Thesis, primary advisor, Worcester Polytechnic Institute, 1992.
[30] Levergood, Thomas, "An Experimental Evaluation of Split User/Supervisor Cache Memories," MS Thesis, primary advisor, Worcester Polytechnic Institute, 1992.
[31] Lavalee, James, "The Design and Development of Real-Time Systems Using Ada and the Activation Framework," MS Thesis, co-advisor, Worcester Polytechnic Institute, 1992.
[32] Velazques, Javier, "The Development of a Real-Time Environment Using the Activation Framework," MS Thesis, co-advisor, Worcester Polytechnic Institute, 1992.

### 4.3.3 Ph. D. Dissertations (current)

[1] Jitesh, "Ad-Hoc Networking for Bandwith Limited LMR Systems," primary advisor.

### 4.3.4 Ph. D. Dissertations (completed)

[1] Iyer, Vishwanath, "Broadband Impedance Matching of Antenna Radiators," Ph.D. Dissertation, co-advisor, Worcester Polytechnic Institute, 2010.
[2] Navalekar, Abhijit, "Distributed Digital Radios For Land Mobile Radio Applications," Ph.D. Dissertation, primary advisor, Worcester Polytechnic Institute, 2009.
[3] Parikh, Hemish, "Design of an OFDM Transmitter and Receiver for Precision Personnel Location," primary advisor.
[4] Progri, Ilir, "An Assessment of Indoor Geolocation Systems," Ph.D. Dissertation, primary advisor, Worcester Polytechnic Institute, 2003.
[5] Li, Xinrong, "Super-Resolution TOA Estimation with Diversity Techniques for Indoor Applications," Ph.D. Dissertation, co-advisor, Worcester Polytechnic Institute, 2003.
[6] Leuenberger, Gerog H. W., "Electrostatic Density Measurements in Green-State PM Parts," Ph.D. Dissertation, co-advisor, Worcester Polytechnic Institute, 2003.
[7] Bogdanov, Gene, "Radio-Frequency Coil Design for High Field Magnetic Resonance Imaging," Ph.D. Dissertation, co-advisor, Worcester Polytechnic Institute, 2002.
[8] Elbirt, Adam J., "Reconfigurable Computing for Symmetric-Key Algorithms," Ph.D. Dissertation, co-advisor, Worcester Polytechnic Institute, 2002.
[9] Bretchko, Pavel, "Design and Development of Ultra-wideband DC-Coupled Amplifier," Ph.D. Dissertation, co-advisor, Worcester Polytechnic Institute, 2001.
[10] Hill, Jonathan, "Development of an Experimental Global Positioning System (GPS) Receiver Platform for Navigation Algorithm Evaluation," Ph.D. Dissertation, primary advisor, 2001.
[11] Spasojević, Mirko, "Creation of Sparse Boundary Element Matricies for 2-D and Axisymmetric Electrostatic Problems Using a Bi-orthogonal Wavelet," Ph.D. Dissertation, co-advisor, Worcester Polytechnic Institute, 1997.
[12] Shi, Funan, "Optimal Designs of Gradient and RF Coils for Magnetic Resonance Imaging (MRI) Instrument," Ph.D. Dissertation, co-advisor, Worcester Polytechnic Institute, 1996.

## 5. Proposals and Funding (past 5 years):

### 5.1 In Review

\$ 199,996 A National Model Robotics Curriculum, NSF (PI: Dr. M. Gennert, Co-PIs: Drs. T. Padir, W.R. Michalson, G. Fischer and C. Demetry), May 2009.
\$ 199,052 A National Model Robotics Capstone, NSF (PI: Dr. W.R. Michalson, Co-PIs: Drs.T. Padir, C. Demetry, G. Tryggvason and F. Looft), May 2009.
\$ 399,791 Modular System for Teaching Robotics Engineering (MySTRE), NSF (PI: Dr. G. Fischer, Co-PIs: Drs. W.R. Michalson and T. Padir), March 2009.

### 5.2 Funding Received

\$ 50,524 PCGO Broadband Modem, Powerwave Technologies, Inc., (PI: Dr. W.R. Michalson), May 2009.
\$ 1,245,000 Real-Time Troop Status Monitoring System, US Army Telemedicine and Advanced Technology Research Center. (PI: Dr. Peder Pedersen, Co-PIs: Drs. William R. Michalson and Yitzhak Mendelson). Third year of funding. Projected funding period: Oct 1, 2004 to Sep 30, 2005.
\$ 148,422 Precision Personnel Locator System, National Institute of Justice (PI: Dr. John Orr, Co-PIs: Drs. David Cyganski and William R. Michalson). Second year of funding. Projected funding period: Sep 1, 2004 to Oct 31, 2005. Grant code 219240.
\$74,048 High-Speed VHF Modem, US Army Telemedicine and Advanced Technology Research Center (PI: Dr. William R. Michalson). Funding period: Mar 1, 2004 to Dec 31, 2004. Grant code 214370.
\$ 81,499 WPI Nanosat Program, Air Force Office of Scientific Research (PI: Dr. Fred Looft, Co-PIs: Drs. William R. Michalson and Diran Apelian). Funding period: Apr 1, 2003 to Mar 31, 2005. Grant code 214400.
\$ 996,000 Precision Personnel Locator System, National Institute of Justice (PI: Dr. David Cyganski, Co-PIs: Drs. William R. Michalson and John Orr). Second year of funding. Projected funding period: Sep 1, 2004 to Aug 31, 2005. Grant code 219240.
\$ 813,141 Real-Time Troop Status Monitoring System, US Army Telemedicine and Advanced Technology Research Center, (PI: Dr. William R. Michalson, Co-PIs: Drs. Peder Pedersen and Yitzhak Mendelson). Second year of funding. Funding period Oct 1, 2003 to Sep 30, 2004. Grant code 214370.

## 6. Honors, Awards, and Recognitions:

Elected Senior Member of the IEEE.

Joseph Samuel Satin Distinguished Fellowship awarded for the 1994-1995 academic year.
Aldo Miccioli Fellowship recipient from Raytheon Equipment Division.
ION Best Paper Award - GPS-96 for W. R. Michalson, W. Cidela, et. al., "A GPS-Based Hazard Detection and Warning System," in review, " ION GPS-96, 9th International Meeting of the Satellite Division of the Institute of Navigation, pp. 167-175, Kansas City, MO, Sep 17-20, 1996
$2^{\text {nd }}$ Place -2004 ECE Department MQP Award / Provost's MQP Award for GPS-Based Orbit and Attitude Determination System for PANSAT, Joshua Holwell, Andrew Coonradt and Himanshu Agrawal.
$1^{\text {st }}$ Place - 2003 ECE Department MQP Award / Provost’s MQP Award for Personal Inertial Navigation System, Jason DeChiaro and Chris Struus.
$1^{\text {st }}$ Place - 2002 ECE Department MQP Award / Provost’s MQP Award for Handspring Digital Voltmeter, Andrew Young and Pavel Loven.
$3^{\text {rd }}$ Place - 1998 ECE Department MQP Award / Provost’s MQP Award for Design of a Personal Handheld GPS Receiver, Jeffery Alderson and Helder Machado.
$2^{\text {nd }}$ Place - 1997 ECE Department MQP Award / Provost’s MQP Award for Distributed Audio Controller, EE-WZM-1B96, Stephen S. Richardson.
$3^{\text {rd }}$ Place - 1997 ECE Department MQP Award / Provost’s MQP Award for GPS Hazard Detector II, EE-WZM-2A96, Will Brothers, Jon Day, and John Zaghi.
$1^{\text {st }}$ Place - 1996 ECE Department MQP Award / Provost’s MQP Award for GPS Hazard Detector, EE-WHE-9601, Michael Roberts, William Cidela, and Chris Mangiarelli.

### 6.1 Memberships and offices held in professional society

Institute of Electrical and Electronic Engineers, Senior Member
Institute of Navigation
Royal Institute of Navigation
American Society of Engineering Educators

### 6.2 Professional Service

Massachusetts Board of Bar Overseers Hearing Committee Member, 2010-Present.
Steering Committee - 2009 First Annual Robotics Innovations Competition and Conference (RICC ’09), Nov 7-8, Worcester, MA, 2009.

Conference Technical Co-Chair - 2009 IEEE International Conference on Technologies of Practical Robot Applications (TePRA 2009), Nov. 9-11, Woburn, MA, 2009.

Reviewer - Proposal number CRDPJ 379622-08, Natural Sciences and Engineering Research Council of Canada (NSERC), Mar. 2009

Co-Chair - Urban and Indoor Geolocation, Institute of Navigation International Technical Meeting (ITM2009), Anaheim CA, Jan. 2009.
Reviewer - Proposal number CRDPJ 379622-08, Natural Sciences and Engineering Research Council of Canada (NSERC), Mar. 2009

# The Design and Analysis of Spatial Data Structures 

# The Design and Analysis of Spatial Data Structures 

Hanan Samet<br>UNIVERSITY OF MARYLAND

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Figures 2.26 and 2.27 are from D. T. Lee and C. K. Wong, Worst-case analysis for region and partial region searches in multidimensional binary search trees and quad trees, Acta Informatica 9, 1 (1977), 23-29. Reprinted by permission of Springer Verlag. Continued on p. 493

## APPENDIX B

To my parents, Julius and Lotte

## APPENDIX B

## PREFACE

Spatial data consist of points, lines, rectangles, regions, surfaces, and volumes. The representation of such data is becoming increasingly important in applications in computer graphics, computer vision, database management systems, computer-aided design, solid modeling, robotics, geographic information systems (GIS), image processing, computational geometry, pattern recognition, and other areas. Once an application has been specified, it is common for the spatial data types to be more precise. For example, consider a geographic information system (GIS). In such a case, line data are differentiated on the basis of whether the lines are isolated (e.g., earthquake faults), elements of tree-like structures (e.g., rivers and their tributaries), or elements of networks (e.g., rail and highway systems). Similarly region data are often in the form of polygons that are isolated (e.g., lakes), adjacent (e.g., nations), or nested (e.g., contours). Clearly the variations are large.

Many of the data structures currently used to represent spatial data are hierarchical. They are based on the principle of recursive decomposition (similar to divide and conquer methods [Aho74]). One such data structure is the quadtree (octree in three dimensions). As we shall see, the term quadtree has taken on a generic meaning. In this book, it is my goal to show how a number of hierarchical data structures used in different domains are related to each other and to quadtrees. My presentation concentrates on these different representations and illustrates how a number of basic operations that use them are performed.

Hierarchical data structures are useful because of their ability to focus on the interesting subsets of the data. This focusing results in an efficient representation and in improved execution times. Thus they are particularly convenient for performing set operations. Many of the operations described can often be performed as efficiently, or more so, with other data structures. Nevertheless hierarchical data structures are attractive because of their conceptual clarity and ease of implementation. In addition, the use of some of them provides a spatial index. This is very useful in applications involving spatial databases.

As an example of the type of problems to which the techniques described in this book are applicable, consider a cartographic database consisting of a number of maps and some typical queries. The database contains a contour map, say at 50 -foot elevation intervals, and a land use map classifying areas according to crop growth. Our goal is to determine all regions between 400 - and 600 -foot elevation levels where wheat is grown. This will require an intersection operation on the two maps. Such an analysis could be rather costly, depending on the way the maps are represented. For example, since areas where corn is grown are of no interest, we wish to spend a minimal amount of effort searching such regions. Yet traditional region representations such as the boundary code [Free74] are very local in application, making it difficult to avoid examining a corn-growing area that meets the desired elevation criterion. In contrast, hierarchical representations such as the region quadtree are more global in nature and enable the elimination of larger areas from consideration.

Another query might be to determine whether two roads intersect within a given area. We could check them point by point; however, a more efficient method of analysis would be to represent them by a hierarchical sequence of enclosing rectangles and to discover whether in fact the rectangles do overlap. If they do not, the search is terminated. If an intersection is possible, more work may have to be done, depending on which method of representation is used.

A similar query can be constructed for point data - for example, to determine all cities within 50 miles of St. Louis that have a population in excess of 20,000 . Again we could check each city individually. However, using a representation that decomposes the United States into square areas having sides of length 100 miles would mean that at most four squares need to be examined. Thus California and its adjacent states can be safely ignored.

Finally, suppose we wish to integrate our queries over a database containing many different types of data (e.g., points, lines, areas). A typical query might be, "Find all cities with a population in excess of 5,000 people in wheat-growing regions within 20 miles of the Mississippi River." In this book we will present a number of different ways of representing data so that such queries and other operations can be efficiently processed.

This book is organized as follows. There is one chapter for each spatial data type, in which I present a number of different data structures. The aim is to gain the ability to evaluate them and to determine their applicability. Two problems are treated in great detail: the rectangle intersection problem, discussed in the context of the representation of collections of small rectangles (Chapter 3), and the point location problem, discussed in the context of the representation of curvilinear data (Chapter 4). A comprehensive treatment of the use of quadtrees and octrees in other applications in computer graphics, image processing, and geographic information systems (GIS) can be found in [Same90b].

Chapter 1 gives a general introduction to the principle of recursive decomposition with a concentration on two-dimensional regions. Key properties, as well as a historical overview, are presented.

Chapter 2 discusses hierarchical representations of multidimensional point data. These data structures are particularly useful in applications in database management systems because they are designed to facilitate responses to search queries.

Chapter 3 examines the hierarchical representation of collections of small rectangles. Such data arise in applications in computational geometry, very large-scale integrations (VLSI), cartography, and database management. Examples from these fields (e.g., the rectangle intersection problem) are used to illustrate their differences. Many of the representations are closely related to those used for point data. This chapter is an expansion of [Same88a].

Chapter 4 treats the hierarchical representation of curvilinear data. The primary focus is on the representation of polygonal maps. The goal is to be able to solve the point location problem. Quadtree-like solutions are compared with those from computational geometry such as the K-structure [Kirk83] and the layered dag [Edel86a].

Chapter 5 looks at the representation of three-dimensional region data. In this case, a number of octree variants are examined, as well as constructive solid geometry (CSG) and the boundary model (BRep). Algorithms are discussed for converting between some of these representations. The representation of surfaces (i.e., 2.5dimensional data) is also briefly discussed in this chapter.

There are a number of topics for which justice requires a considerably more detailed treatment. However, due to space limitations, I have omitted a detailed discussion of them and instead refer interested readers to the appropriate literature. For example, surface representations are discussed briefly with three-dimensional data in Chapter 5 (also see Chapter 7 of [Same90b]). The notion of a pyramid is presented only at a cursory level in Chapter 1 so that it can be contrasted with the quadtree. In particular, the pyramid is a multiresolution representation, whereas the quadtree is a variable resolution representation. Readers are referred to Tanimoto and Klinger [Tani80] and the collection of papers edited by Rosenfeld [Rose83a] for a more comprehensive exposition on pyramids.

Results from computational geometry, although related to many of the topics covered in this book, are discussed only in the context of representations for collections of small rectangles (Chapter 3) and curvilinear data (Chapter 4). For more details on early work involving some of these and related topics, interested readers should consult the surveys by Bentley and Friedman [Bent79b], Overmars [Over88a], Edelsbrunner [Edel84], Nagy and Wagle [Nagy79], Peuquet [Peuq84], Requicha [Requ80], Srihari [Srih81], Samet and Rosenfeld [Same80d], Samet [Same84b, Same88a], Samet and Webber [Same88c, Same88d], and Toussaint [Tous80].

There are also a number of excellent texts containing material related to the topics that I cover. Rosenfeld and Kak [Rose82a] should be consulted for an encyclopedic treatment of image processing. Mäntylä [Mänt87] has written a comprehensive introduction to solid modeling. Burrough [Burr86] provides a survey of geographic information systems (GIS). Overmars [Over83] has produced a particularly good treatment of multidimensional point data. In a similar vein, see Mehlhorn's [Mehl84] unified treatment of multidimensional searching and computational geometry. For thorough introductions to computational geometry, see Preparata and

## APPENDIX B

PREFACE II

K-structure and the layered dag in Section 4.3 are relevant to computational geometry. Bucket methods such as linear hashing, spiral hashing, grid file, and EXCELL, in Section 2.8, and R-trees in Section 3.5.3 are important in the study of database management systems. Methods for multidimensional searching that are discussed include $\mathrm{k}-\mathrm{d}$ trees in Section 2.4, range trees and priority search trees in Section 2.5, and pointbased rectangle representations in Section 3.4. The discussions of the representation of two-dimensional regions in Chapter 1, polygonal representations in Chapter 4, and use of point methods for focussing the Hough Transform are relevant to image processing. Finally the rectangle-representation methods and plane-sweep methods of Chapter 3 are important in the field of VLSI design.

The natural home for courses that use this book is in a computer science department, but the book could also be used in a curriculum in geographic information systems (GIS). Such a course is offered in geography departments. The emphasis for a course in this area would be on the use of quadtree-like methods for representing spatial data.

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## x \| PREFACE

Shamos [Prep85] and Edelsbrunner [Edel87] (also see [Prep83, ORou88]). A broader view of the literature can be found in related bibliographies such as the ongoing collective effort coordinated by Edelsbrunner [Edel83c, Edel88], and Rosenfeld's annual collection of references in the journal Computer Vision, Graphics, and Image Processing (e.g., [Rose88]).

Nevertheless, given the broad and rapidly expanding nature of the field, I am bound to have omitted significant concepts and references. In addition at times I devote a disproportionate amount of attention to some concepts at the expense of others. This is principally for expository purposes; I feel that it is better to understand some structures well rather than to give readers a quick runthrough of buzzwords. For these indiscretions, I beg your pardon and hope you nevertheless bear with me.

My approach is an algorithmic one. Whenever possible, I have tried to motivate critical steps in the algorithms by a liberal use of examples. I feel that it is of paramount importance for readers to see the ease with which the representations can be implemented and used. In each chapter, except for the introduction (Chapter 1), I give at least one detailed algorithm using pseudo-code so that readers can see how the ideas can be applied. The pseudo-code is a variant of the ALGOL [Naur60] programming language that has a data structuring facility incorporating pointers and record structures. Recursion is used heavily. This language has similarities to C [Kern78], PaSCal [Jens74], Sail [Reis76], and algol w [Baue68]. Its basic features are described in the Appendix. However, the actual code is not crucial to understanding the techniques, and it may be skipped on a first reading. The index indicates the page numbers where the code for each algorithm is found.

In many cases I also give an analysis of the space and time requirements of different data structures and algorithms. The analysis is usually of an asymptotic nature and is in terms of big $O$ and $\Omega$ notation [Knut76]. The big $O$ notation denotes an upper bound. For example, if an algorithm takes $O\left(\log _{2} N\right)$ time, then its worst-case behavior is never any worse than $\log _{2} N$. The $\Omega$ notation denotes a lower bound. As an example of its use, consider the problem of sorting $N$ numbers. When we say that sorting is $\Omega\left(N \cdot \log _{2} N\right)$ we mean that given any algorithm for sorting, there is some set of $N$ input values for which the algorithm will require at least this much time.

At times I also describe implementations of some of the data structures for the purpose of comparison. In such cases counts, such as the number of fields in a record, are often given. These numbers are meant only to amplify the discussion. They are not to be taken literally, as improvements are always possible once a specific application is analyzed more carefully.

Each chapter contains a substantial number of exercises. Many of the exercises develop further the material in the text as a means of testing the reader's understanding, as well as suggesting future directions. When the exercise or its solution is not my own, I have preceded it with the name of its originator. The exercises have not been graded by difficulty. They rarely require any mathematical skills beyond the undergraduate level for their solution. However, while some of the exercises are quite straightforward, others require some ingenuity. Solutions, or references to papers that
contain the solution, are provided for a substantial number of the exercises that do not require programming. Readers are cautioned to try to solve the exercises before turning to the solutions. It is my belief that much can be learned this way (for the student and, even more so, for the author). The motivation for undertaking this task was my wonderful experience on my first encounter with the rich work on data structures by Knuth [Knut73a, Knut73b].

An extensive bibliography is provided. It contains entries for both this book and the companion text [Same90b]. Not all of the references that appear in the bibliography are cited in the two texts. They are retained for the purpose of giving readers the ability to access the entire body of literature relevant to the topics discussed in them. Each reference is annotated with a key word(s) and a list of the numbers of the sections in which it is cited in either of the texts (including exercises and solutions). In addition, a name and credit index is provided that indicates the page numbers in this book on which each author's work is cited or a credit is made.

## ACKNOWLEDGMENTS

Over the years I have received help from many people, and I am extremely grateful to them. In particular Robert E. Webber, Markku Tamminen, and Michael B. Dillencourt have generously given me much of their time and have gone over critical parts of the book. I have drawn heavily on their knowledge of some of the topics covered here. I have also been extremely fortunate to work with Azriel Rosenfeld over the past ten years. His dedication and scholarship have been a true inspiration to me. I deeply cherish our association.

I was introduced to the field of spatial data structures by Gary D. Knott who asked "how to delete in point quadtrees." Azriel Rosenfeld and Charles R. Dyer provided much interaction in the initial phase of my research. Those discussions led to the discovery of the neighbor-finding principle. It is during that time that many of the basic conversion algorithms between quadtrees and other image representations were developed as well. I learned much about image processing and computer vision from them. Robert E. Webber taught me computer graphics, Markku Tamminen taught me solid modeling and representations for multiattribute data, and Michael B. Dillencour' taught me about computational geometry.

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## A GUIDE TO THE INSTRUCTOR

This book can be used in a second data structures course, one with emphasis on the representation of spatial data. The focus is on the use of the principle of divide-and-conquer for which hierarchical data structures provide a good demonstration. Throughout the book both worst-case optimal methods and methods that work well in practice are emphasized in conformance with my view that the well-rounded computer scientist should be conversant with both types of algorithms. This material is more than can be covered in one semester; but the instructor can reduce it as necessary. For example, the detailed examples can be skipped or used as a basis of a term project or programming assignments.

The book can also be used to organize a course to be prerequisite to courses in computer graphics and solid modeling, computational geometry, database management systems, multidimensional searching, image processing, and VLSI design. The discussions of the representations of two-dimensional regions in Chapter 1, polygonal representations in Chapter 4, and most of Chapter 5 are relevant to computer graphics and solid modeling. The discussions of plane-sweep methods and their associated data structures such as segment trees, interval trees, and priority search trees in Seccions 3.2 and 3.3 and point location and associated data structures such as the

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## APPENDIX B

## INTRODUCTION

## 1

There are numerous hierarchical data structuring techniques in use for representing spatial data. One commonly used technique is the quadtree, which has evolved from work in different fields. Thus it is natural that a number of adaptations of it exist for each spatial data type. Its development has been motivated to a large extent by a desire to save storage by aggregating data having identical or similar values. We will see, however, that this is not always the case. In fact, the savings in execution time that arise from this aggregation are often of equal or greater importance.

In this chapter we start with a historical overview of quadtrees, including definitions. Since the primary focus in this book is on the representation of regions, what follows is a discussion of region representation in the context of different space decomposition methods. This is done by examining polygonal and nonpolygonal tilings of the plane. The emphasis is on justifying the use of a decomposition into squares. We conclude with a detailed analysis of the space requirements of the quadtree representation.

Most of the presentation in this chapter is in the context of two-dimensional regions. The extension of the topics in this chapter, and remaining chapters, to threedimensional region data, and higher, is straightforward and, aside from definitions, is often left to the exercises. Nevertheless, the concept of an octree, a quadtree-like representation of three-dimensional regions, is defined and a brief explanation is given of how some of the results described here are applicable to higher-dimensional data.

### 1.1 BASIC DEFINITIONS

First, we define a few terms with respect to two-dimensional data. Assume the existence of an array of picture elements (termed pixels) in two dimensions. We use the term image to refer to the original array of pixels. If its elements are black or

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white, then it is said to be binary. If shades of gray are possible (i.e., gray levels), the image is said to be a gray-scale image. In the discussion, we are primarily concerned with binary images. Assume that the image is on an infinite background of white pixels. The border of the image is the outer boundary of the square corresponding to the array.

Two pixels are said to be 4-adjacent if they are adjacent to each other in the horizontal or vertical direction. If the concept of adjacency also includes adjacency at a corner (i.e., diagonal adjacencies), then the pixels are said to be 8-adjacent. A set $S$ is said to be four-connected (eight-connected) if for any pixels $p, q$ in $S$ there exists a sequence of pixels $p=p_{0}, p_{1}, \cdots, p_{n}=q$ in $S$, such that $p_{i+1}$ is 4-adjacent (8adjacent) to $p_{i}, 0 \leq i<n$.

A black region, or black four-connected component, is a maximal fourconnected set of black pixels. The process of assigning the same label to all 4adjacent black pixels is called connected component labeling (see Chapter 5 of [Same90b]). A white region is a maximal eight-connected set of white pixels defined analogously. The complement of a black region consists of a union of eightconnected white regions. Exactly one of these white regions contains the infinite background of white pixels. All the other white regions, if any, are called holes in the black region. The black region, say $R$, is surrounded by the infinite white region and $R$ surrounds the other white regions, if any.

A pixel is said to have four edges, each of which is of unit length. The boundary of a black region consists of the set of edges of its constituent pixels that also serve as edges of white pixels. Similar definitions can be formulated in terms of rectangular blocks, all of whose pixels are identically colored. For example, two disjoint blocks, $P$ and $Q$, are said to be 4-adjacent if there exists a pixel $p$ in $P$ and a pixel $q$ in $Q$ such that $p$ and $q$ are 4 -adjacent. Eight-adjacency for blocks (as well as connected component labeling) is defined analogously.

### 1.2 OVERVIEW OF QUADTREES AND OCTREES

The term quadtree is used to describe a class of hierarchical data structures whose common property is that they are based on the principle of recursive decomposition of space. They can be differentiated on the following bases:

1. The type of data they are used to represent
2. The principle guiding the decomposition process
3. The resolution (variable or not)

Currently they are used for point data, areas, curves, surfaces, and volumes. The decomposition may be into equal parts on each level (i.e., regular polygons and termed a regular decomposition), or it may be governed by the input. In computer graphics this distinction is often phrased in terms of image-space hierarchies versus object-space hierarchies, respectively [Suth74]. The resolution of the decomposition


Figure 1.1 An example of (a) a region, (b) its binary array, (c) its maximal blocks (blocks in the region are shaded), and (d) the corresponding quadtree
(i.e., the number of times that the decomposition process is applied) may be fixed beforehand, or it may be governed by properties of the input data. For some applications we can also differentiate the data structures on the basis of whether they specify the boundaries of regions (e.g., curves and surfaces) or organize their interiors (e.g., areas and volumes).

The first example of a quadtree representation of data is concerned with the representation of two-dimensional binary region data. The most studied quadtree approach to region representation, called a region quadtree (but often termed a quadtree in the rest of this chapter), is based on the successive subdivision of a bounded image array into four equal-sized quadrants. If the array does not consist entirely of 1 s or entirely of 0 s (i.e., the region does not cover the entire array), then it is subdivided into quadrants, subquadrants, and so on, until blocks are obtained that consist entirely of 1 s or entirely of 0 s ; that is, each block is entirely contained in the region or entirely disjoint from it. The region quadtree can be characterized as a variable resolution data structure.

As an example of the region quadtree, consider the region shown in Figure 1.1a represented by the $2^{3} \times 2^{3}$ binary array in Figure 1.1b. Observe that the 1 s correspond to picture elements (i.e., pixels) in the region, and the 0 s correspond to picture elements outside the region. The resulting blocks for the array of Figure 1.1 b are shown in Figure 1.1c. This process is represented by a tree of degree 4 (i.e., each nonleaf node has four sons).

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In the tree representation, the root node corresponds to the entire array. Each son of a node represents a quadrant (labeled in order NW, NE, SW, SE) of the region represented by that node. The leaf nodes of the tree correspond to those blocks for which no further subdivision is necessary. A leaf node is said to be black or white depending on whether its corresponding block is entirely inside (it contains only 1s) or entirely outside the represented region (it contains no ls). All nonleaf nodes are said to be gray (i.e., its block contains 0 s and 1 s ). Given a $2^{n} \times 2^{n}$ image, the root node is said to be at level $n$ while a node at level 0 corresponds to a single pixel in the image. ${ }^{1}$ The region quadtree representation for Figure 1.1c is shown in Figure 1.1d. The leaf nodes are labeled with numbers, while the nonleaf nodes are labeled with letters. The levels of the tree are also marked.

Our definition of the region quadtree implies that it is constructed by a top-down process. In practice, the process is bottom-up, and one usually uses one of two approaches. The first approach [Same80b] is applicable when the image array is not too large. In such a case, the elements of the array are inspected in the order given by the labels on the array in Figure 1.2 (which corresponds to the image of Figure 1.1a). This order is also known as a Morton order [Mort66] (discussed in Section 1.3). By using such a method, a leaf node is never created until it is known to be maximal. An equivalent statement is that the situation does not arise in which four leaf nodes of the same color necessitate the changing of the color of their parent from gray to black or white as is appropriate. (For more details, see Section 4.1 of [Same90b].)

The second approach [Same81a] is applicable to large images. In this case, the elements of the image are processed one row at a time-for example, in the order given by the labels on the array in Figure 1.3 (which corresponds to the image of Figure 1.1a). This order is also known as a row or raster-scan order (discussed in Section 1.3). A quadtree is built by adding pixel-sized nodes one by one in the order in which they appear in the file. (For more details, see Section 4.2.1 of [Same90b].) This process can be time-consuming due to the many merging and node insertion operations that need to take place.

The above method has been improved by using a predictive method [Shaf86a, Shaf87a], which only makes a single insertion for each node in the final quadtree and performs no merge operations. It is based on processing the image in row order (top to bottom, left to right), always inserting the largest node (i.e., block) for which the current pixel is the first (upper leftmost) pixel. Such a policy avoids the necessity of merging since the upper leftmost pixel of any block is inserted before any other pixel of that block. Therefore it is impossible for four sibling nodes to be of the same color. This method makes use of an auxiliary array of size $O\left(2^{n}\right)$ for a $2^{n} \times 2^{n}$ image. (For more details, see Section 4.2 .3 of [Same90b].)

The region quadtree is easily extended to represent three-dimensional binary region data and the resulting data structure is called a region octree (termed an octree

[^1]| 1 | 2 | 5 | 6 | 17 | 18 | 21 | 22 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 3 | 4 | 7 | 8 | 19 | 20 | 23 | 24 |
| 9 | 10 | 13 | 14 | 25 | 26 | 29 | 30 |
| 11 | 12 | 15 | 16 | 27 | 28 | 31 | 32 |
| 33 | 34 | 37 | 38 | 49 | 50 | 53 | 54 |
| 35 | 36 | 39 | 40 | 51 | 52 | 55 | 56 |
| 41 | 42 | 45 | 46 | 5 | 58 | 61 | 62 |
| 43 | 44 | 4 | 7 | 48 | 59 | 60 | 63 |

Figure 1.2 Morton order for the pixels of Figure 1.1
in the rest of this chapter). We start with a $2^{n} \times 2^{n} \times 2^{n}$ object array of unit cubes (termed voxels or obels). The octree is based on the successive subdivision of an object array into octants. If the array does not consist entirely of 1 s or entirely of 0 s , it is subdivided into octants, suboctants, and so on until cubes (possibly single voxels) are obtained that consist of 1 s or of 0 s ; that is, they are entirely contained in the region or entirely disjoint from it.

This subdivision process is represented by a tree of degree 8 in which the root node represents the entire object and the leaf nodes correspond to those cubes of the array for which no further subdivision is necessary. Leaf nodes are said to be black or white (alternatively, full or void) depending on whether their corresponding cubes are entirely within or outside the object, respectively. All nonleaf nodes are said to be gray. Figure 1.4 a is an example of a simple three-dimensional object, in the form of a staircase, whose octree block decomposition is given in Figure 1.4b and whose tree representation is given in Figure 1.4c.

The region quadtree is a member of a class of representations characterized as being a collection of maximal (according to an appropriate definition) blocks, each of which is contained in a given region and whose union is the entire region. The simplest such representation is the runlength code, where the blocks are restricted to $1 \times m$ rectangles [Ruto68]. A more general representation treats the region as a union of maximal square blocks (or blocks of any other desired shape) that may possibly overlap. Usually the blocks are specified by their centers and radii. This representation is called the medial axis transformation (Mat) [Blum67, Rose66]. Of course, other approaches are also possible (e.g., rectangular coding [Kim83, Kim86], TID [Scot85, Scot86]).

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 |
| 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 |
| 25 | 26 | 27 | 28 | 29 | 30 | 31 | 32 |
| 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 |
| 49 | 50 | 51 | 52 | 53 | 54 | 55 | 56 |
| 57 | 58 | 59 | 60 | 61 | 62 | 63 | 64 |

Figure 1.3 Raster-scan order for the pixels of Figure 1.1

## 6 || 1 INTRODUCTION



Figure 1.4 (a) Example three-dimensional object; (b) its octree block decomposition; (c) its tree representation

The region quadtree is a variant on the maximal block representation. It requires the blocks to be disjoint and to have standard sizes (i.e., sides of lengths that are powers of two) and standard locations. The motivation for its development is a desire to obtain a systematic way to represent homogeneous parts of an image. Thus to transform the data into a region quadtree, a criterion must be chosen for deciding that an image is homogeneous (i.e., uniform).

One such criterion is that the standard deviation of its gray levels is below a given threshold $t$. Using this criterion, the image array is successively subdivided into quadrants, subquadrants, and so on until homogeneous blocks are obtained. This process leads to a regular decomposition. If one associates with each leaf node the mean gray level of its block, the resulting region quadtree will then completely specify a piecewise approximation to the image where each homogeneous block is represented by its mean. The case where $t=0$ (i.e., a block is not homogeneous unless its gray level is constant) is of particular interest since it permits an exact reconstruction of the image from its quadtree.

Note that the blocks of the region quadtree do not necessarily correspond to maximal homogeneous regions in the image. Most likely there exist unions of the blocks that are still homogeneous. To obtain a segmentation of the image into maximal homogeneous regions, we must allow merging of adjacent blocks (or unions of blocks) as long as the resulting region remains homogeneous. This is achieved by a 'split-and-merge' algorithm [Horo76]. However, the resulting partition will no longer be represented by a quadtree; instead the final representation is in the form of an adjacency graph. Thus the region quadtree is used as an initial step in the segmentation process.

For example, Figure 1.5b-d demonstrates the results of the application, in sequence, of merging, splitting, and grouping to the initial image decomposition of Figure 1.5 a . In this case, the image is initially decomposed into 16 equal-sized square blocks. Next the 'merge' step attempts to form larger blocks by recursively merging groups of four homogeneous 'brothers' (the four blocks in the NW and SE quadrants of Figure 1.5b). The 'split' step recursively decomposes blocks that are not homogeneous (the NE and SW quadrants of Figure 1.5c) until a particular homogeneity criterion is satisfied or a given level is encountered. Finally the 'grouping` step aggregates all homogeneous 4 -adjacent black blocks into one region apiece;


Figure 1.5 Example illustrating the 'split-and-merge' segmentation procedure: (a) start, (b) merge, (c) split, (d) grouping
the 8 -adjacent white blocks are similarly aggregated into white regions (Figure 1.5 d ).
An alternative to the region quadtree representation is to use a decomposition method that is not regular (i.e., rectangles of arbitrary size rather than squares). This alternative has the potential of requiring less space. Its drawback is that the determination of optimal partition points may be computationally expensive (see Exercise 1.10). A closely related problem, decomposing a region into a minimum number of rectangles, is known to be NP-complete ${ }^{2}$ [Gare79] if the region is permitted to contain holes [Ling82].

The homogeneity criterion ultimately chosen to guide the subdivision process depends on the type of region data represented. In the remainder of this chapter we shall assume that the domain is a $2^{n} \times 2^{n}$ binary image with 1 , or black, corresponding to foreground and 0 , or white, corresponding to background (e.g., Figure 1.1).

[^2]Nevertheless the quadtree and octree can be used to represent multicolored data (e.g., a landuse class map associating colors with crops [Same87a]).

It is interesting to note that Kawaguchi, Endo, and Matsunaga [Kawa83] use a sequence of $m$ binary-valued quadtrees to encode image data of $2^{m}$ gray levels, where the various gray levels are encoded by use of Gray codes (see, e.g., [McCl65]). This should lead to compaction (i.e., larger-sized blocks) since the Gray code guarantees that the binary representation of the codes of adjacent gray level values differ by only one binary digit. ${ }^{3}$ Note, though, that if the primary interest is in image compression, there exist even better methods (see, e.g., [Prat78]); however, they are beyond the scope of this book (but see Chapter 8 of [Same90b]). In another context, Kawaguchi, Endo, and Yokota [Kawa80b] point out that a sequence of related images (e.g., in an animation application) can be stored compactly as a sequence of quadtrees such that the $i^{\text {th }}$ element is the result of exclusive oring the first $i$ images (see Exercise 1.7).

Unfortunately the term quadtree has taken on more than one meaning. The region quadtree, as described earlier, is a partition of space into a set of squares whose sides are all a power of two long. This formulation is due to Klinger [Klin71] and Klinger and Dyer, who used the term Q-tree [Klin76], whereas Hunter [Hunt78] was the first to use the term quadtree in such a context. Actually a more precise term would be quadtrie, as it is really a trie structure [Fred60] in two dimensions. ${ }^{4}$ A similar partition of space into rectangular quadrants, also termed a quadtree, was used by Finkel and Bentley [Fink74]. It is an adaptation of the binary search tree [Knut73b] to two dimensions (which can be easily extended to an arbitrary number of dimensions). It is primarily used to represent multidimensional point data, and we shall refer to it as a point quadtree where confusion with a region quadtree is possible.

As an example of a point quadtree, consider Figure 1.6, which is built for the sequence Chicago, Mobile, Toronto, Buffalo, Denver, Omaha, Atlanta, and Miami ${ }^{5}$

[^3]

Figure 1.6 A point quadtree and the records it represents
in the order in which they are listed here. ${ }^{6}$ Its shape is highly dependent on the order in which the points are added to it. Of course, trie-based point representations also exist (see Sections 2.6.1 and 2.6.2).

## Exercises

1.1. The region quadtree is an alternative to an image representation that is based on the use of an array or even a list. Each of these image representations may be biased in favor of the computation of a particular adjacency relation. Discuss these biases for the array, list, and quadtree representations.
1.2. Given the array representation of a binary image, write an algorithm to construct the corresponding region quadtree.

[^4]1.3. Given an image represented by a region quadtree with $B$ black and $w$ white nodes, how many additional nodes are necessary for the nonleaf nodes?
1.4. Given an image represented by a region octree with $B$ black and $w$ white nodes, how many additional nodes are necessary for the nonleaf nodes?
1.5. Suppose that an octree is used to represent a collection of disjoint spheres. What would you use as a leaf criterion?
1.6. The quadtree can be generalized to represent data in arbitrary dimensions. As we saw, the octree is its three-dimensional analog. The renowned artist Escher [Coxe86] is noted for etchings of unusual interpretations of geometric objects such as staircases. How would you represent one of Escher's staircases?
1.7. Let $\oplus$ denote an exclusive or operation. Given a sequence of related images, $\left\langle P_{n}, P_{n-1}, \cdots, P_{0}\right\rangle$, define another sequence $\left\langle Q_{n}, Q_{n-1}, \cdots, Q_{0}\right\rangle$ such that $Q_{0}=P_{0}$ and $Q_{i}=P_{i} \oplus Q_{i-1}$ for $i>0$. Show that when the sequences $P$ and $Q$ are represented as quadtrees, replacing sequence $P$ by sequence $Q$ results in fewer nodes.
1.8. Prove that in Exercise 1.7 the sequence $P$ can be reconstructed from the sequence $Q$. In particular, given $Q_{i}$ and $Q_{i-1}$, determine $P_{i}$.
1.9. Write an algorithm to construct the Gray codes of the integers 0 to $2^{n \prime}-1$.
1.10. Find a polynomial-time algorithm to decompose a region optimally so that its quadtree representation uses a minimum amount of space (i.e., a minimum number of nodes). In this case, you can assume that the decomposition lines can be placed in arbitrary positions so that the space requirement is reduced. In other words, the decomposition lines need not split the space into four squares of equal size. Thus the decomposition is similar to that induced by a point quadtree.

### 1.3 HISTORY OF THE USE OF QUADTREES AND OCTREES

The origin of the principle of recursive decomposition, upon which all quadtrees are based, is difficult to ascertain. Below, to give some indication of the uses of the region quadtree, some of its applications to geometric data are traced briefly. Most likely it was first seen as a way of aggregating blocks of zeros in sparse matrices. Indeed Hoare [Hoar72] attributes a one-level decomposition of a matrix into square blocks to Dijkstra. Morton [Mort66] used it as a means of indexing into a geographic database (i.e., it acts as a spatial index).

Warnock, in a pair of reports that serve as landmarks in computer graphics [Warn68, Warn69b], described the implementation of hidden-line and hidden-surface elimination algorithms using a recursive decomposition of the picture area. The picture area is repeatedly subdivided into rectangles that are successively smaller while searching for areas that are sufficiently simple to be displayed. Klinger [Klin71] and Klinger and Dyer [Klin76] applied these ideas to pattern recognition and image processing, while Hunter [Hunt78] used them for an animation application.

The SRI robot project [Nils69] used a three-level decomposition of space to represent a map of the robot's world. Eastman [East70] observes that recursive decomposition might be used for space planning in an architectural context and presents a simplified version of the SRI robot representation. A quadtree-like representation in the form of production rules called DF-expressions (denoting 'depth-first') is discussed by Kawaguchi and Endo [Kawa80a] and Kawaguchi, Endo, and Yokota
[Kawa80b] (see also Section 1.5). Tucker [Tuck84a] uses quadtree refinement as a control strategy for an expert vision system.

The three-dimensional variant of the region quadtree-the octree-was developed independently by a number of researchers. Hunter [Hunt78] mentioned it as a natural extension of the quadtree. Reddy and Rubin [Redd78] proposed the octree as one of three representations for solid objects. The second is a threedimensional generalization of the point quadtree of Finkel and Bentley [Fink74]-that is, a decomposition into rectangular parallelepipeds (as opposed to cubes) with planes perpendicular to the $x, y$, and $z$ axes. The third breaks the object into rectangular parallelepipeds that are not necessarily aligned with an axis. The parallelepipeds are of arbitrary sizes and orientations. Each parallelepiped is recursively subdivided into parallelepipeds in the coordinate space of the enclosing parallelepiped. Reddy and Rubin prefer the third approach for its ease of display.

Situated somewhere between the second and third approaches of Reddy and Rubin is the method of Brooks and Lozano-Perez [Broo83] (see also [Loza81]), who use a recursive decomposition of space into an arbitrary number of rectangular parallelepipeds, with planes perpendicular to the $x, y$, and $z$ axes, to model space in solving the findpath or piano movers problem [Schw88] in robotics. This problem arises when planning the motion of a robot in an environment containing known obstacles and the desired solution is a collision-free path obtained by use of a search. Faverjon [Fave84] discusses an approach to this problem that uses an octree, as do Samet and Tamminen [Same85g] and Fujimura and Samet [Fuji89].

Jackins and Tanimoto [Jack80] adapted Hunter and Steiglitz's quadtree translation algorithm [Hunt78, Hunt79b] to objects represented by octrees. Meagher [Meag82a] developed numerous algorithms for performing solid modeling operations in an environment where the octree is the underlying representation. Yau and Srihari [Yau83] extended the octree to arbitrary dimensions in the process of developing algorithms to handle medical images.

Both quadtrees and octrees are frequently used in the construction of meshes for finite element analysis. The use of recursive decomposition for meshes was initially suggested by Rheinboldt and Mesztenyi [Rhei80]. Yerry and Shephard [Yerr83] adapted the quadtree and octree to generate meshes automatically for threedimensional solids represented by a superquadric surface-based modeler. This has been extended by Kela, Voelcker, and Goldak [Kela84b] (see also [Kela86]) to mesh boundary regions directly, rather than through discrete approximations, and to facilitate incremental adaptive analysis by exploiting the spatial index nature of the quadtree and octree.

Parallel to the development of the quadtree and octree data structures, there has been related work by researchers in the field of image understanding. Kelly [Kell71] introduced the concept of a plan, which is a small picture whose pixels represent gray-scale averages over $8 \times 8$ blocks of a larger picture. Needless effort in edge detection is avoided by first determining edges in the plan and then using these edges to search selectively for edges in the larger picture. Generalizations of this idea motivated the development of multiresolution image representations-for example,


Figure 1.7 Structure of a pyramid having three levels
the recognition cone of Uhr [Uhr72], the preprocessing cone of Riseman and Arbib [Rise77], and the pyramid of Tanimoto and Pavlidis [Tani75]. Of these representations, the pyramid is the closest relative of the region quadtree.

Given a $2^{n} \times 2^{n}$ image array, say $A(n)$, a pyramid is a sequence of arrays $\{A(i)\}$ such that $A(i-1)$ is a version of $A(i)$ at half the scale of $A(i) . A(0)$ is a single pixel. Figure 1.7 shows the structure of a pyramid having three levels. It should be clear that a pyramid can also be defined in a more general way by permitting finer scales of resolution than the power of two scale.

At times, it is more convenient to define a pyramid in the form of a tree. Again, assuming a $2^{n} \times 2^{n}$ image, a recursive decomposition into quadrants is performed, just as in quadtree construction, except that we keep subdividing until we reach the individual pixels. The leaf nodes of the resulting tree represent the pixels, while the nodes immediately above the leaf nodes correspond to the array $A(n-1)$, which is of size $2^{n-1} \times 2^{n-1}$. The nonleaf nodes are assigned a value that is a function of the nodes below them (i.e., their sons) such as the average gray level. Thus we see that a pyramid is a multiresolution representation, whereas the region quadtree is a variable

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 |
| 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 |
| 25 | 26 | 27 | 28 | 29 | 30 | 31 | 32 |
| 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 |
| 49 | 50 | 51 | 52 | 53 | 54 | 55 | 56 |
| 57 | 58 | 59 | 60 | 61 | 62 | 63 | 64 |

Figure 1.8 Example pyramid $A(3)$

| $A$ | $B$ | $C$ | $D$ |
| :---: | :---: | :---: | :---: |
| $E$ | $F$ | $G$ | $H$ |
| I | J | K | $L$ |
| $M$ | $N$ | $O$ | $P$ |

Figure $1.9 \quad A(2)$ corresponding to Figure 1.8

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 |
| 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 |
| 25 | 26 | 27 | 28 | 29 | 30 | 31 | 32 |
| 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 |
| 49 | 50 | 51 | 52 | 53 | 54 | 55 | 56 |
| 57 | 58 | 59 | 60 | 61 | 62 | 63 | 64 |

Figure 1.10 The overlapping blocks in which pixel 28 participates
resolution representation. Another analogy is that the pyramid is a complete quadtree [Knut73a].

The above definition of a pyramid is based on nonoverlapping $2 \times 2$ blocks of pixels. An alternative definition, termed an overlapping pyramid, uses overlapping blocks of pixels. One of the simplest schemes makes use of $4 \times 4$ blocks that overlap by $50 \%$ in both the horizontal and vertical directions [Burt81]. For example, Figure 1.8 is a $2^{3} \times 2^{3}$ array, say $A(3)$, whose pixels are labeled $1-64$. Figure 1.9 is $A(2)$ corresponding to Figure 1.8 with elements labeled A-P. The $4 \times 4$ neighborhood corresponding to element F in Figure 1.9 consists of pixels 10-13, 18-21, 26-29, and 34-37. This method implies that each block at a given level participates in four blocks at the immediately higher level. Thus the containment relations between blocks no longer form a tree. For example, pixel 28 participates in blocks F, G, J, and K in the next higher level (see Figure 1.10 where the four neighborhoods corresponding to $\mathrm{F}, \mathrm{G}, \mathrm{J}$, and K are drawn as squares).

To avoid treating border cases differently, each level in the overlapped pyramid is assumed to be cyclically closed (i.e., the top row at each level is adjacent to the bottom row and similarly for the columns at the extreme left and right of each level). Once again we say that the value of a node is the average of the values of the nodes in its block on the immediately lower level. The overlapped pyramid may be compared with the Quadtree Medial Axis Transform (see Section 9.3.1 of [Same90b]) in the sense that both may result in nondisjoint decompositions of space.

Pyramids have been applied to the problems of feature detection and extraction since they can be used to limit the scope of the search. Once a piece of information of interest is found at a coarse level, the finer resolution levels can be searched. This approach was followed by Davis and Roussopoulos [Davi80] in approximate pattern matching. Pyramids can also be used for encoding information about edges, lines, and curves in an image [Shne81c, Krop86]. One note of caution: the reduction of resolution has an effect on the visual appearance of edges and small objects [Tani76]. In particular, at a coarser level of resolution, edges tend to get smeared, and region separation may disappear. Pyramids have also been used as the starting point for a 'split-and-merge' segmentation algorithm [Piet82].

Quadtree-like decompositions are useful as space-ordering methods. The purpose is to optimize the storage and processing sequences for two-dimensional data by mapping them into one dimension (i.e., linearizing them). This mapping should pre-


Figure 1.11 The result of applying a number of different space-ordering methods to an $8 \times 8$ image whose first element is in the upper left corner of the image: (a) row order, (b) row-prime order, (c) Morton order, (d) Peano-Hilbert order, (e) Cantor-diagonal order, (f) spiral order
serve the spatial locality of the original two-dimensional image in one dimension. The result of the mapping is also known as a space-filling curve [Gold81, Witt83] because it passes through every point in the image.

Goodchild and Grandfield [Good83] discuss a number of space-ordering methods, some of which are illustrated in Figure 1.11. Each has different characteristics. The row (Figure 1.11a), also known as raster-scan, and row-prime orders (Figure 1.11b) are similar in the same way as are the Morton [Mort66, Pean90] (Figure 1.11c) and the Peano-Hilbert [Hilb91] (Figure 1.11d) orders. The primary difference is that in both the row-prime and Peano-Hilbert orders every element is a 4 -adjacent neighbor of the previous element in the sequence, and thus they have a slightly higher degree of locality than the row and Morton orders, respectively. Both the Morton and Peano-Hilbert orders exhaust a quadrant or subquadrant of a square image before exiting it. They are both related to quadtrees; however, as we saw above, the Morton order does not traverse the image in a spatially contiguous manner (the result has the shape of the letter ' N ' or ' Z ' and is also known as N order [Whit82] and Z order [Oren84]).

For both the Morton and Peano-Hilbert orders, there is no need to know the maximum values of the coordinates. The Morton order is symmetric, while the Peano-Hilbert order is not. One advantage of the Morton order is that the position of each element in the ordering (termed its key) can be determined by interleaving the
bits of the $x$ and $y$ coordinates of the element; this is not easy for the Peano-Hilbert order. Another advantage of the Morton order is that the recursion necessary for its generation is quite easy to specify.

Other orders are the Cantor-diagonal order (Figure 1.11e) and the spiral order (Figure 1.11f). The Cantor-diagonal order proceeds outward from the origin and visits the elements in an order similar to row-prime with the difference that elements are visited in order of their increasing 'Manhattan' (or 'city block') distance. ${ }^{7}$ Thus it is good for ordering a space that is unbounded in the two directions emanating from the origin which has been relocated to the center of the image. On the other hand, the spiral order is attractive when ordering a space that is unbounded in the four directions emanating from the origin.

The most interesting orders, as far as we are concerned, are the Morton and Peano-Hilbert orders since they can also be used to order a space that has been aggregated into squares. Of these two orderings, the Morton order is by far the more frequently used as a result of the simplicity of the conversion process between the key and its corresponding element in the multidimensional space. In this book we are primarily interested in Morton orderings. (For further discussion of some of the properties of these two orderings, see [Patr68, Butz71, Alex79, Alex80, Laur85].)

## Exercises

1.11. Write an algorithm to extract the $x$ and $y$ coordinates from a Peano-Hilbert order key.
1.12. Write an algorithm to construct the Peano-Hilbert key for a given point $(x, y)$. Try to make it optimal.
1.13. Suppose that you are given a $2^{n} \times 2^{n}$ array of points such that the horizontal and vertical distances between 4 -adjacent points are 1 . What is the average distance between successive points when the points are ordered according to the orders illustrated in Figure 1.11? What about a random order?
1.14. Suppose that you are given a $2^{n} \times 2^{n}$ image. Assume that the image is stored on disk in pages of size $2^{m} \times 2^{m}$ where $n$ is much larger than $m$. What is the average cost of retrieving a pixel and its 4 -adjacent neighbors when the image is ordered according to the orders illustrated in Figure 1.11?
1.15. The traveling salesman problem [Lawl85] is one where a set of points is given and it is desired to find the path of minimum distance such that each point is visited only once. This is an NP-complete problem [Gare79] and thus there is a considerable amount of work in formulating approximate solutions to it [Bent82]. For example, consider the following approximate solution. Assume that the points are uniformly distributed in the unit square. Let $d$ be the expected Euclidean distance between two independent points. Now, sort the points using the row order and the Morton order. Laurini [Laur85] simulated the average Euclidean distance between successive points in these orders and found it to be $d / 2$ for the row order and $d / 3$ for the Morton order. Can you derive these averages analytically? What are the average values for the other orders illustrated in Figure 1.11? What about a random order?

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## 16 || 1 INTRODUCTION

1.16. Suppose that the traveling salesman problem is solved using a traversal of the points in Morton order as discussed in Exercise 1.15. In particular, assume that the set of points is decomposed in such a way that each square block contains just one point. This yields a point representation that is analogous to the region quadtree (termed a PR quadtree and discussed in Section 2.6.2). How close does such a solution come to optimality?

### 1.4 SPACE DECOMPOSITION METHODS

In general, any planar decomposition used as a basis for an image representation should possess the following two properties:

1. The partition should be an infinitely repetitive pattern so that it can be used for images of any size.
2. The partition should be infinitely decomposable into increasingly finer patterns (i.e., higher resolution).

In this section, the discussion is restricted to two-dimensional data. Thus we are dealing with planar space decompositions. Space decompositions can be classified into two categories, depending on the nature of the pattern. The pattern can consist of polygonal shapes or nonpolygonal shapes. The polygonal shapes are generally computationally simpler since their sides can be expressed in terms of linear relations (e.g., equations of lines). They are good for approximating the interior of a region. The nonpolygonal shapes are more flexible since they provide good approximations, in terms of measures, of the boundaries (e.g., perimeter) of regions as well as their interiors (e.g., area). ${ }^{8}$

Moreover, the normals to the boundaries of nonpolygonal shapes are not restricted to a fixed set of directions. For example, in the case of rectangular tiles, there is a 90 degree discontinuity between the normals to boundaries of adjacent tiles. This lack of continuity is a drawback in applications in fields such as computer graphics where such tasks as shading make use of the directions of the surface. However, working with nonpolygonal shapes generally requires use of floating point arithmetic, and hence it is usually more complex.

The remainder of this section expands on a number of polygonal decompositions and compares them. It also contains a brief discussion of one nonpolygonal decomposition that consists of a collection of sector-like objects whose arcs are not necessarily part of a circle. This method is based on polar coordinates where the arc joining two distinct points is formed by linear interpolation. The term sector tree is used to describe it. This discussion is of an advanced nature and can be skipped on an initial reading.

[^6]
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### 1.4.1 Polygonal Tilings

Bell, Diaz, Holroyd, and Jackson [Bell83] discuss a number of polygonal tilings of the plane (i.e., tessellations) that satisfy property 1 . Figure 1.12 illustrates some of these tessellations. They also present a taxonomy of criteria to distinguish between the various tilings. The tilings, consisting of polygonal tiles, are described by use of a notation based on the degree of each vertex as the edges (i.e., sides) of the 'atomic' tile are visited in order, forming a cycle. For example, the tiling described by [4.8 ${ }^{2}$ ] (Figure 1.12c) has the shape of a triangle where the first vertex has degree four while the remaining two vertices have degree eight apiece.

A tiling is said to be regular if the atomic tiles are composed of regular polygons (i.e., all sides are of equal length as are the interior angles). A molecular tile is an aggregation of atomic tiles to form a hierarchy. It is not necessarily constrained to have the same shape as the atomic tile. When a tile at level $k$ (for all $k>0$ ) has the same shape as a tile at level 0 (i.e., it is a scaled image of a tile at level 0 ), then the tiling is said to be similar.

Bell et al. focus on the isohedral tilings where a tiling is said to be isohedral if all the tiles are equivalent under the symmetry group of the tiling. A more intuitive


e

Figure 1.12 Sample tessellations: (a) $\left[4^{4}\right]$ square; (b) $\left[6^{3}\right]$ equilateral triangle; (c) $\left[4.8^{2}\right]$ isoceles triangle; (d) [4.6.12] 30 -60 right triangle; (e) $\left[3^{6}\right]$ hexagon


Figure 1.13 Examples of (a) isohedral and (b) nonisohedral tilings
way to conceptualize this definition is to assume the position of an observer who stands in the center of a tile having a given orientation and scans the surroundings. If the view is independent of the tile, the tiling is isohedral. For example, consider the two tilings in Figure 1.13 consisting of triangles (Figure 1.13a) and trapezoids (Figure 1.13b). The triangles are isohedral, whereas the trapezoids are not, as can be seen by the view from tiles A and B.

In the case of the trapezoidal tiling, the viewer from A is surrounded by an infinite number of concentric hexagons, whereas this is not the case for B. In other words, the trapezoidal tiling is not periodic. Also note that all of the tiles in Figure 1.13a are described by $\left[6^{3}\right]$, while those in Figure 1.13 b are either $\left[3^{2} .4^{2}\right],\left[3^{2} .6^{2}\right]$, or [3.4.6 ${ }^{2}$ ] (i.e., tiles labeled 1, 2, and 3, respectively, in Figure 1.13b). When the isohedral tilings are classified by the action of their symmetry group, there are 81 different types [Grün77, Grün87]. When they are classified by their adjacency structure, as done here, there are 11 types.

The most relevant criterion to the discussion is the distinction between limited and unlimited hierarchies of tilings. A limited tiling is not similar. A tiling that satisfies property 2 is said to be unlimited. Equivalently, in a limited tiling, no change of scale lower than the limit tiling can be made without great difficulty. An alternative characterization of an unlimited tiling is that each edge of a tile lies on an infinite straight line composed entirely of edges. Interestingly the hexagonal tiling $\left[3^{6}\right]$ is limited. Bell et al. claim that only four tilings are unlimited. These are the tilings given in Figure 1.12a-d. Of these, [ $4^{4}$ ], consisting of square atomic tiles (Figure 1.12a), and [ $6^{3}$ ], consisting of equilateral triangle atomic tiles (Figure 1.12b), are well-known regular tessellations [Ahuj83]. For these two tilings we consider only the molecular tiles given in Figures 1.14a and 1.14b.

The tilings [ $4^{4}$ ] and [ $6^{3}$ ] can generate an infinite number of different molecular tiles where each molecular tile at the first level consists of $n^{2}$ atomic tiles $(n>1)$. The remaining nonregular unlimited triangular tilings, $\left[4.8^{2}\right.$ ] (Figure 1.12c) and [4.6.12] (Figure 1.12 d ), are less well understood. One way of generating [4.8 ${ }^{2}$ ] and [4.6.12] is to join the centroids of the tiles of $\left[4^{4}\right]$ and $\left[6^{3}\right]$, respectively, to both their vertices and midpoints of their edges. Each of the tilings [4.8 ${ }^{2}$ ] and [4.6.12] has two


Figure 1.14 Examples illustrating unlimited tilings: (a) [44] hierarchy, (b) $\left[6^{3}\right]$ hierarchy, (c) ordinary $\left[4.8^{2}\right]$ hierarchy, (d) ordinary [4.6.12] hierarchy, (e) rotation [4.8 ${ }^{2}$ ] hierarchy, (f) reflection [4.6.12] hierarchy
types of hierarchy. [4.8 ${ }^{2}$ ] has an ordinary (Figure 1.14 c ) and a rotation hierarchy (Figure 1.14 e ) requiring a rotation of 135 degrees between levels. [4.6.12] has an ordinary (Figure 1.14 d ) and a reflection hierarchy (Figure 1.14 f ), which requires a reflection of the basic tile between levels.

The distinction between the two types of hierarchies for [4.8 ${ }^{2}$ ] and [4.6.12] is necessary because the tiling is not similar without a rotation or a reflection when the hierarchy is not ordinary. This can be seen by observing the use of dots in Figure 1.14 to delimit the atomic tiles in the first molecular tile. Similarly broken lines are used to delimit the components of tiles at the second level (assuming atomic tiles are at level 0 ). For the ordinary [ $4.8^{2}$ ] and [4.6.12] hierarchies, each molecular tile at the first level consists of $n^{2}(n>1)$ atomic tiles. In the reflection hierarchy of [4.6.12], each molecular tile at the first level consists of $3 \cdot n^{2}(n>1)$ atomic tiles, while for the rotation hierarchy of $\left[4.8^{2}\right], 2 \cdot n^{2}(n>1)$ atomic tiles comprise a molecular tile at the first level.

To represent data in the Euclidean plane, any of the unlimited tilings could have been chosen. For a regular decomposition, the tilings [4.8 ${ }^{2}$ ] and [4.6.12] are ruled out. Comparing 'square' $\left[4^{4}\right]$ and 'triangular' $\left[6^{3}\right]$ quadtrees, we find that they differ in terms of adjacency and orientation. Let us say that two tiles are neighbors if they are

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adjacent either along an edge or at a vertex. A tiling is uniformly adjacent if the distances between the centroid of one tile and the centroids of all its neighbors are the same. The adjacency number of a tiling is the number of different intercentroid distances between any one tile and its neighbors. In the case of [ $4^{4}$ ], there are only two adjacency distances, whereas for $\left[6^{3}\right]$ there are three adjacency distances.

A tiling is said to have uniform orientation if all tiles with the same orientation can be mapped into each other by translations of the plane that do not involve rotation or reflection. Tiling [ $4^{4}$ ] displays uniform orientation, while $\left[6^{3}\right]$ does not. Under the assumption that uniform orientation and a minimal adjacency distance is preferable, we say that $\left[4^{4}\right]$ is more useful than $\left[6^{3}\right]$. It is also very easy to implement. Nevertheless, $\left[6^{3}\right]$ has its uses. For example, Yamaguchi, Kunii, Fujimura, and Toriya [Yama84] use a triangular quadtree to generate an isometric view from an octree representation of an object (see Section 7.1.4 of [Same90b]).

Of the limited tilings, many types of hierarchies may be generated [Bell83]; however, in general, they cannot be decomposed beyond the atomic tiling without changing the basic tile shape. This is a serious deficiency of the hexagonal tessellation [ $3^{6}$ ] (Figure 1.12 e ) since the atomic hexagon can be decomposed only into triangles. Nevertheless the hexagonal tessellation is of considerable interest. It is regular, has a uniform orientation, and, most important, displays a uniform adjacency (i.e., each neighbor of a tile is at the same distance from it).

There are a number of different hexagonal hierarchies distinguished by classifying the shape of the first-level molecular tile on the basis of the number of hexagons that it contains. Three of these tiling hierarchies are given in Figure 1.15 and are called $n$-shapes where $n$ denotes the number of atomic tiles in the first-level molecular tile. Of course, these $n$-shapes are not unique.


Figure 1.15 Three different hexagonal tiling hierarchies: (a) 4-shape, (b) 7-shape, (c) 9-shape

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1.4 SPACE DECOMPOSITION METHODS II

The 4 -shape and the 9 -shape have an unusual adjacency property in the sense that no matter how large the molecular tile becomes, contact with two of the tiles (i.e., the one above and the one below) is along only one edge of a hexagonal atomic tile, while contact with the remaining four molecular tiles is along nearly one-quarter of the perimeter of the corresponding molecular tile. The hexagonal pattern of the 4 shape and 9 -shape molecular tiles has the shape of a rhombus. In contrast, a 7 -shape molecular tile has a uniform contact with its six neighboring molecular tiles.

The type of quadtree used often depends on the grid formed by the image sampling process. Square quadtrees are appropriate for square grids and triangular quadtrees for triangular grids. In the case of a hexagonal grid [Burt80], the 7-shape hierarchy is frequently used since the shape of its molecular tile is more like a hexagon. It is usually described as rosette-like (i.e., a septree). Note that septrees have jagged edges as they are merged to form larger units (e.g., Figure 1.15b). The septree is used by Gibson and Lucas [Gibs82] (who call it a generalized balanced ternary or GBT for short) in the development of algorithms analogous to those existing for quadtrees.

Although the septree can be built up to yield large septrees, the smallest resolution in the septree must be decided upon in advance since its primitive components (i.e., hexagons) cannot later be decomposed into septrees. Therefore the septree yields only a partial hierarchical decomposition in the sense that the components can always be merged into larger units, but they cannot always be broken down. For region data, a pixel is generally an indivisible unit, and thus unlimited decomposition is not absolutely necessary. However, in the case of other data types such as points (see Chapter 2) and lines (see Chapter 4), we will see that the decomposition rules of some representations require that two entities be separated, which may lead to a level of decomposition not known in advance (e.g., a decomposition rule that restricts each square to contain at most one point). In this book the discussion is limited to square quadtrees and their variants.

When the data are spherical, a number of researchers have proposed the use of a representation based on an icosahedron (a 20 -faced polyhedron whose faces are regular triangles) [Dutt84, Feke84]. The icosahedron is attractive because, in terms of the number of faces, it is the largest possible regular polyhedron. Each of the triangular faces can be further decomposed in a recursive manner into $n^{2}(n>1)$ spherical triangles (the [ $6^{3}$ ] tiling).

Fekete and Davis [Feke84] let $n=2$, which means that at each level of decomposition, three new vertices are generated by halving each side of the triangle; connecting them together yields four triangles. They use the term property sphere to describe their representation. The property sphere has been used in object recognition; it is also of potential use in mapping the globe because it can enable accurate modeling of regions around the poles. For example, see Figure 1.16, which is a property sphere representation of some spherical data. In contrast, planar quadtrees are less attractive the farther we get from the equator due to distortions in planarity caused by the earth's curvature. Of course, for true applicability for mapping, we need a closer approximation to a sphere than is provided by the 20 triangles of the icosahedron. Moreover, we want a way to distinguish between different elevations.


C
Figure 1.16 Property sphere representation of some spherical data: (a) data, (b) decomposition on a sphere, (c) decomposition on a plane

Dutton [Dutt84] lets $n=\sqrt{3}$, which means that at each level of decomposition, one new vertex is created by connecting the centroid of the triangle to its vertices. The result is an alternating sequence of triangles so that each level is fully contained in the level that was created two steps previously and has nine times as many triangles as that level. Dutton uses the term triacon to describe the resulting hierarchy. As an example, consider Figure 1.17, which illustrates four levels of a triacon decomposition. The initial and odd-numbered decompositions are shown with heavy lines, and the even-numbered decompositions are shown with broken and thin lines.


Figure 1.17 Example of a triacon hierarchy

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The icosahedron is not the only regular polyhedron that can be used to model spherical data. Others include the tetrahedron, hexahedron, octahedron, and dodecahedron, which have $4,6,8$, and 12 faces, respectively. Collectively these five polyhedra are known as the Platonic solids [Peuq84]. The faces of the tetrahedron and octahedron are equilateral triangles, while the faces of the hexahedron and dodecahedron are squares and regular pentagons, respectively.

The dodecahedron is not an appropriate primitive because the pentagonal faces cannot be further decomposed into pentagons or other similar shapes. The tetrahedron and hexahedron (the basis of the octree) have internal angles that are too small to model a sphere properly, thereby leading to shape distortions.

Dutton [Dutt84] points out that the octahedron is attractive for modeling spherical data such as the globe because it can be aligned so that the poles are at opposite vertices and the prime meridian and the equator intersect at another vertex. In addition, one subdivision line of each face is parallel to the equator. Of course, for all of the Platonic solids, only the vertices of the solids touch the sphere; the facets of the solids are interior to the sphere.

Other decompositions for spherical data are also possible. Tobler and Chen [Tobl86] point out the desirability of a close relationship to the commonly used system of latitude and longitude coordinates. In particular, any decomposition that is chosen should enable the use of meridians and parallels to refer to the data. An additional important goal is for the partition to be into units of equal area, which rules out the use of equally spaced lines of latitude (of course, the lines of longitude are equally spaced). In this case, the sphere is projected into a plane using Lambert's cylindrical projection [Adam49], which is locally area preserving. Authalic coordinates [Adam49], which partition the projection into rectangles of equal area, are then derived. (For more details, see [Tobl86].)

The quadtree decomposition has the property that at each subdivision stage, the image is subdivided into four equal-sized parts. When the original image is a square, the result is a collection of squares, each of which has a side whose length is a power of 2. The binary image tree (termed bintree) [Know80, Tamm84a, Same88b] is an alternative decomposition defined in a manner analogous to the region quadtree except that at each subdivision stage we subdivide the image into two equal-sized parts. In two dimensions, at odd stages. we partition along the $x$ coordinate, and at even stages, along the $y$ coordinate. The bintree is equivalent to the region quadtree if we replace all leaf nodes at odd stages of subdivision by two identically colored sons.

The bintree is related to the region quadtree in the same way as the k -d tree [Bent75b] (see Section 2.4) is related to the point quadtree [Fink74]. The difference is that region quadtrees and bintrees are used to represent region data with fixed subdivision points, while point quadtrees and k - d trees are used to represent point data where the values of the points determine the subdivision. For example. Figure 1.18 is the bintree representation corresponding to the image of Figure 1.1. We assume that for the $x(y)$ partition, the left subtree corresponds to the west (south) half of the image and the right subtree corresponds to the east (north) half. Once again, as in Figure 1.1, all leaf nodes are labeled with numbers, and the nonleaf nodes are labeled with letters.

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Figure 1.18 Bintree representation corresponding to Figure 1.1: (a) block decomposition, (b) bintree representation of blocks in (a)

The quadtree and bintree decompose a region into equal-sized parts. Kanatani [Kana85] suggests using splitting rules based on the Fibonacci sequence of numbers. The Fibonacci numbers consist of the sequence of numbers $f_{i}$ that satisfy the relation $f_{i}=f_{i-1}+f_{i-2}$, with $f_{0}=1$ and $f_{1}=1$. We can try to devise both quadtree and bintree splitting rules based on such a sequence. Generally for a decomposition scheme to be useful in geometric applications, it must have pixel-sized squares (i.e., $1 \times 1$ ) as the primitive tiles. At first glance, it appears that the Fibonacci sequence gives quite a bit of leeway in deciding on a splitting sequence and on the sizes of the regions corresponding to the subtrees and the primitive tiles.

One possible quadtree splitting rule is to restrict all shapes to squares with sides whose lengths are Fibonacci numbers. Clearly not all the shapes can be squares since we cannot aggregate these squares into larger squares that obey this rule. Another possibility is to restrict the shapes to rectangles the length of whose sides are either equal Fibonacci numbers or are successive Fibonacci numbers (see Exercise 1.26). We term this condition the 2-d Fibonacci condition.

In this discussion, we have assumed splitting rules that ensure that vertical subdivision lines at the same level are colinear as well as for horizontal lines at the same level. For example, when using a quadtree splitting rule, the vertical lines that subdivide the NW and SW quadrants are colinear, as well as for the horizontal lines that subdivide the NW and NE quadrants. An alternative is to relax the colinearity restriction; however, the sides of the shapes must still satisfy the 2-d Fibonacci condition (see Exercise 1.27).

As can be seen in Exercises 1.26 and 1.27, neither a quadtree nor a bintree can


Figure 1.19 (a) An arbitrary space decomposition and (b) its BSP tree. The arrows indicate the direction of the positive halfspaces.
be used by itself as a basis for Fibonacci-based space decomposition; however, a combination of the two structures could be used. When the lengths of the sides of a rectangle are equal, the rectangle is split into four rectangles such that the lengths of the sides satisfy the 2-d Fibonacci condition. When the lengths of the sides of a rectangle are not equal, the rectangle is split into two rectangles with the split along a line (an axis) parallel to the shorter (longer) of the two sides. Interestingly the dimensions of the A-series of European paper are based on a Fibonacci sequence-that is, the elements of the series are of dimension $f_{i} \times f_{i-1}$ multiplied by an appropriate scale factor.

Another variation on the bintree idea, termed adaptive hierarchical coding (AHC), is proposed by Cohen, Landy, and Pavel [Cohe85b]. In this case, the image is again split into two equal-sized parts at each stage, but there is no need to alternate between the $x$ and $y$ coordinates. The decision as to the coordinate on which to partition depends on the image. This technique may require some work to get the optimal partition from the point of view of a minimum number of nodes (see Exercise 1.29).

An even more general variation on the bintree is the $B S P$ tree of Fuchs, Kedem, and Naylor [Fuch80, Fuch83]. Its variants are used in some hidden-surface elimination algorithms (see Section 7.1.5 of [Same90b]) and in some implementations of beam tracing (see Section 7.3 of [Same90b]). It is applicable to data of arbitrary dimension, although here it is explained in the context of two-dimensional data. At each subdivision stage, the image is subdivided into two parts of arbitrary size. Note that successive subdivision lines need be neither orthogonal nor parallel. Therefore the resulting decomposition consists of arbitrarily shaped convex polygons.

The BSP tree is a binary tree. To be able to assign regions to the left and right subtrees, we associate a direction with each subdivision line. In particular, the subdivision lines are treated as separators between two halfspaces. ${ }^{9}$ Let the line have the

[^7]
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equation $a \cdot x+b \cdot y+c=0$. We say that the right subtree is the 'positive' side and contains all subdivision lines formed by separators that satisfy $a \cdot x+b \cdot y+c \geq 0$. Similarly we say that the left subtree is 'negative' and contains all subdivision lines formed by separators that satisfy $a \cdot x+b \cdot y+c<0$. As an example, consider Figure 1.19 a , which is an arbitrary space decomposition whose BSP tree is given in Figure 1.19 b . Notice the use of arrows to indicate the direction of the positive halfspaces.

## Exercises

1.17. Given a $\left[6^{3}\right]$ tiling such that each side of an atomic tile has a unit length, compute the three adjacency distances from the centroid of an atomic tile.
1.18. Repeat Exercise 1.17 for $\left[3^{6}\right]$ and $\left[4^{4}\right]$, again assuming that each side of an atomic tile has a unit length.
1.19. Suppose that you are given an image in the form of a binary array of pixels. The result is a square grid. How can you view this grid as a hexagonal grid?
1.20. Show how the property sphere data structure can be used to model the earth. In particular, discuss how to represent landmass features, such as mountain ranges and crevices.
1.21 Suppose that you use an icosahedron to model spherical data. Initially there are 20 faces. How many faces are there after the first level of decomposition when $n=2$ ? $n=\sqrt{3}$ ?
1.22. What is the ratio of leaf nodes to nonleaf nodes in a bintree for a $d$-dimensional image?
1.23. What is a lower bound on the ratio of leaf nodes in a bintree to that in a quadtree for a $d$ dimensional image? What is an upper bound? What is the average?
1.24. Is it true that the total number of nodes in a bintree is always less than that in the corresponding quadtree?
1.25. The Fibonacci numbers are defined by the relation $f_{n}=f_{n-1}+f_{n-2}$. Devise a twodimensional analog of this relation to correspond to a splitting rule that would have to be satisfied in a Fibonacci-based space decomposition that yields four parts. Generalize this result to $n$ dimensions.
1.26. Give a counterexample to the use of a quadtree splitting rule in a Fibonacci-based space decomposition.
1.27. Give a counterexample to the use of a bintree splitting rule in a Fibonacci-based space decomposition.
1.28. Suppose that you use the combination quadtree-bintree approach to a Fibonacci-based space decomposition. Prove that any image such that the lengths of its sides satisfy the 2-d Fibonacci condition can be decomposed into subimages whose sides obey this property and with a primitive tile of size $1 \times 1$.
1.29. Suppose that you use the AHC method. How many different rectangles and positions must be examined in building such a structure for a $2^{n} \times 2^{n}$ image?

### 1.4.2 Nonpolygonal Tilings

In the previous section we focused on space decompositions based on polygonal tiles. This is the prevalent method in use today. For certain applications, however, the use of polygonal tiles can lead to problems. For example, suppose that we have a decomposition based on square tiles. In this case, as the resolution is increased, the area of the approsimated region approaches the true value of the area; however, this is not

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true for a boundary measure such as the perimeter. To see this, consider a quadtree approximation of an isosceles right triangle where the ratio of the approximated perimeter to the true perimeter is $4 /(2+\sqrt{2})$ (see Exercise 1.30). Other problems include the discontinuity of the normals to the boundaries of adjacent tiles.

There are a number of ways of attempting to overcome these problems. The hierarchical probe model of Chen [Chen85b] is an approach based on treating space as a polar plane and recursively decomposing it into sectors. We say that each sector consists of an origin, two sides (labeled 1 and 2 corresponding to the order in which they are encountered when proceeding in a counterclockwise direction), and an arc. The points at which the sides of the sector intersect (or touch) the object are called contact points. $(\rho, \theta)$ denotes a point in the polar plane. Let $\left(\rho_{i}, \theta_{i}\right)$ be the contact point with the maximum value of $\rho$ in direction $\theta_{i}$. Each sector represents a region bounded by the points $(0,0),\left(\rho_{1}, \theta_{1}\right)$, and $\left(\rho_{2}, \theta_{2}\right)$, where $\theta_{1}=2 k \pi / 2^{n}$ and $\theta_{2}=\theta_{1}+2 \pi / 2^{\prime \prime}$ such that $k$ and $n$ are nonnegative integers $\left(k<2^{\prime \prime}\right)$. The arc between the two nonorigin contact points $\left(\rho_{1}, \theta_{1}\right)$ and $\left(\rho_{2}, \theta_{2}\right)$ of a sector is approximated by the linear parametric equations ( $0 \leq t \leq 1$ ):

$$
\rho(t)=\rho_{1}+\left(\rho_{2}-\rho_{1}\right) \cdot t \quad \theta(t)=\theta_{1}+\left(\theta_{2}-\theta_{1}\right) \cdot t .
$$

Note that the interpolation curves are arcs of spirals due to the linear relation between $\rho$ and $\theta$.

The sector tree is a binary tree that represents the result of recursively subdividing sectors in the polar plane into two sectors of equal angular intervals. Thus the recursive decomposition is only with respect to $\theta$, not $\rho$. The decomposition stops whenever the approximation of a part of an object by a sector is deemed to be adequate. The computation of the stopping condition is implementation dependent. For example, it can be the maximum deviation in the value of $\rho$ between a point on the boundary and the corresponding point (i.e., at the same value of $\theta$ ) on the approximating arc. Initially the universe is the interval $[0,2 \pi)$.

In the presentation, we assume that the origin of the polar plane is contained within the object. See Exercise 1.36 for a discussion of how to represent an object that does not contain the origin of the polar plane. The simplest case arises when the object is convex. The result is a binary tree where each leaf node represents a sector and contains the contact points of its corresponding arc. For example, consider the object in Figure 1.20. The construction of its sector tree approximation is shown in


Figure 1.20
Example convex object

a


c

d

Figure 1.21 Successive sector tree approximations for the object of Figure 1.20: (a) $\pi$ intervals, (b) $\pi / 2$ intervals, (c) $\pi / 4$ intervals, (d) $\pi / 8$ intervals

Figures $1.21 \mathrm{a}-\mathrm{d}$. The final binary tree is given in Figure 1.22 with interval endpoints labeled according to Figure 1.21 d .

The situation is more complex when the object is not convex. This means that each side of a sector may intersect the boundary of the object at an arbitrary, and possibly different, number of contact points. In the following, each sector will be seen to consist of a set of alternating regions within and outside the object. These regions are three-sided or four-sided and have at least one side that is colinear with a side of the sector. The discussion is illustrated with the object of Figure 1.23 a whose sector tree decomposition is given in Figure 1.23b. The final binary tree is given in Figure 1.24. A better indication of the quality of the approximation can be seen by examining Figure 1.23 c , which contains an overlay of Figures 1.23 a and 1.23 b .

When the boundary of the object intersects a sector at two successive contact points, say $P$ and $Q$, that lie on the same side, say $S$, of the sector, then the region


Figure 1.22 Binary tree representation of the sector tree of Figure 1.20


Figure 1.23 (a) Example object, (b) its sector tree description, and (c) a comparison of the sector tree approximation (thin lines) with the original object (thick lines). Note the creation of a hole corresponding to the region formed by points $A, B, 6,7, C, D$, and 5
bounded by $S$ and $P Q$ must be approximated. Without loss of generality, assume that the region is inside the object. There are two choices. An inner approximation ignores the region by treating the segment of $S$ between $P$ and $Q$ as part of the approximated boundary (e.g., the region between points 9 and 10 in sector $[9 \pi / 8,5 \pi / 4$ ) in Figure 1.23b).

An outer approximation inserts two identical contact points, say $R$ and $T$, on the other side of the sector and then approximates the region by the three-sided region formed by the segment of $S$ between $P$ and $Q$ and the spiral arc approximations of $P R$ and $Q T$. The value of $R$ (and hence $T$ ) is equal to the average of the value of $\rho$ at $P$ and $Q$. For example, the region between points 4 and 5 in sector [ $5 \pi / 4,3 \pi / 2$ ) in Figure 1.23 b is approximated by the region formed with points C and D.

Of course, the same approximation process is applied to the part of the region outside the object. In Figure 1.23b, we have an inner approximation for the region between points 7 and 8 in sector $[3 \pi / 2,2 \pi)$, and an outer approximation for the region between points 5 and 6 in sector $[9 \pi / 8,5 \pi / 4$ ), by virtue of the introduction of points A and $B$.

One of the problems with the sector tree is that its use can lead to the creation of holes that do not exist in the original object. This situation arises when the decomposition is not carried out to a level of sufficient depth. For example, consider Figure 1.23 b , which has a hole bounded by the arcs formed by points $\mathrm{A}, \mathrm{B}, 6,7, \mathrm{C}, \mathrm{D}$, and 5 . This is a result of the inner approximation for the region between points 7 and 8 in sector $[3 \pi / 2,2 \pi)$ and an outer approximation for the region between points 4 and 5 in sector $[5 \pi / 4,3 \pi / 2$ ). This situation can be resolved by further decomposition in either or both of sectors $[3 \pi / 2,2 \pi)$ and $[5 \pi / 4,3 \pi / 2$ ).

The result of the approximation process is that each sector consists of a collection of three-sided and four-sided regions that approximate the part of the object contained in the sector. This collection is stored in the leaf node of the sector tree as a list of pairs of points in the polar plane. It is interesting to observe that the boundaries of the interpolated regions are not stored explicitly in the tree. Instead each pair of points corresponds to the boundary of a region. Since the origin of the polar plane is within the object, an odd number of pairs of points is associated with each leaf node. For

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Figure 1.24 Binary tree representation of the sector tree of Figure 1.23
example, consider the leaf node in Figure 1.24 corresponding to the sector $[5 \pi / 4,3 \pi / 2$ ). The first pair, together with the origin, defines the first region (e.g., $(6,7)$ ). The next two pairs of points define the second region (e.g., $(5, \mathrm{c})$ and (4,D)), with each successive two pairs of points defining the remaining regions.

The sector tree is a partial polar decomposition, as the subdivision process is based only on the value of $\theta$. A total polar decomposition would partition the polar plane on the basis of both $\rho$ and $\theta$. The result is analogous to a quadtree, and it is termed a polar quadtree. There are a number of possible rules for the decomposition process (see Exercise 1.42). For example, consider a decomposition that recursively halves both $\rho$ and $\theta$ at each level. In general, the polar quadtree is a variant of a maximal block representation. As in the sector tree, the blocks are disjoint. Unlike the sector tree, blocks in the polar quadtree do have standard sizes. In particular, all blocks in the polar quadtree are either three sided (i.e., sectors) or four sided (i.e., quadrilaterals, two of whose sides are arcs). Thus the sides of polar quadtree blocks are not based on interpolation.

The primary motivation for presenting the sector tree is to show that space decompositions could also be based on nonpolygonal tiles. In the rest of this book the primary concern is with space decompositions based on rectangles (especially squares) and showing how a number of operations can be performed when they serve as the underlying representation. The techniques are quite general and can be applied to most space decomposition methods. Thus the sector tree is not discussed further except in the context of its adaptation to the representation of three-dimensional data (see Section 5.6). Nevertheless, the following contains a brief mention of some of the operations to which the sector tree lends itself.

Set operations such as union and intersection are straightforward. Scaling is trivial as the sector tree need not be modified; all values of $\rho$ are interpreted as scaled

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by the appropriate scale factor. The number of nodes in a sector tree is dependent on its orientation-that is, on the points chosen as the origin and the contact point chosen to serve as ( $\rho, 0$ ). Rotation is not so simple; it cannot be implemented by simply rearranging pointers (but see Exercise 1.40). Translation is computationally expensive since the change in the relative position of the object with respect to the origin means that the entire sector tree must be reconstructed.

## Exercises

1.30. Prove that for an isosceles right triangle represented by a region quadtree, the ratio of the approximated perimeter to the true perimeter is $4 /(2+\sqrt{2})$.
1.31. Repeat Exercise 1.30 for a circle (i.e., find the ratio).
1.32. When the objects have linear sides, polygonal tiles are superior. How would you use the sector tree decomposition method with polygonal tiles?
1.33. In the discussion of the situation arising when the boundary of the object intersects a sector at two successive contact points, say $P$ and $Q$, that lie on the same side, say $S$, of the sector, we assumed that the region bounded by $S$ and $P Q$ was inside the object. Suppose that this region is outside the object. How does this affect the inner and outer approximations?
1.34. Can you traverse the boundary of an object represented by a sector tree by visiting each leaf node just once?
1.35. When using a sector tree, how would you handle the situation that the boundary of the object just touches the side of a sector without crossing it (i.e., a tangent if the boundary is differentiable)?
1.36. How would you use a sector tree to represent an object that does not contain the origin of the polar plane?
1.37. The outer approximation used in building a sector tree always yields a three-sided region. Two of the sides are arcs of spirals with respect to a common origin. This implies a sharp discontinuity of the derivative at the point at which they meet. Can you devise a way to smoothe this discontinuity?
1.38. Does the inner approximation used in building a sector tree always underestimate the area? Similarly does the outer approximation always overestimate the area?
1.39. Compare the inner and outer approximations used in building a sector tree. Is there ever a reason for the outer approximation to be preferred over the inner approximations (or vice-versa)?
1.40. Define a complete sector tree in an analogous manner to a complete binary tree-that is, all leaf nodes are at the same level, say $n$. Prove that a complete sector tree is invariant under rotation in multiples of $2 \pi / 2^{n}$.
1.41. Write an algorithm to trace the boundary of an object represented by a sector tree.
1.42. Suppose that it is desired to decompose space into nonpolygonal shapes. Develop a quadtree-like data structure based on polar coordinates (i.e., $\rho$ and $\theta$ ). Investigate different splitting rules for polar quadtrees. In particular, you do not need to alternate the splits-that is, you could split on $\rho$ several times in a row, and so on. This technique is used in the adaptive k -d tree [Frie77] (see Section 2.4.1) by decomposing the quartering process into two splitting operations-one for the $x$ coordinate and one for the $y$ coordinate. What are the possible shapes for the quadrants of such trees (e.g., a lorus, doughnut, wheels with spokes)?

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### 1.5 SPACE REQUIREMENTS

The primary motivation for the development of the quadtree was the desire to reduce the amount of space necessary to store data through the use of aggregation of homogeneous blocks. As we will see in subsequent chapters, an important by-product of this aggregation is the reduction of the execution time of a number of operations (e.g., connected component labeling, component counting). However, a quadtree implementation does have overhead in terms of the nonleaf nodes. For an image with $B$ and $W$ black and white blocks, respectively, $4 \cdot(B+W) / 3$ nodes are required. In contrast, a binary array representation of a $2^{n} \times 2^{n}$ image requires only $2^{2 n}$ bits; however, this quantity grows quite quickly. Furthermore, if the amount of aggregation is minimal (e.g., a checkerboard image), the quadtree is not very efficient.

The overhead for the nonleaf nodes can be reduced at times by using a pointerless representation. Pointer-less representations can be grouped into two categories. The first, termed a DF-expression, represents the quadtree as a traversal of its constituent nodes [Kawa80a]. For example, letting ' $B$ ', ' $W$ ', and ' $G$ ' correspond to black, white, and gray nodes, respectively, and assuming a traversal in the order NW, NE, SW, and SE, the quadtree of Figure 1.1 would be represented by GWGWWBBGWGw bBbwbgbbgbbbww.

The second approach treats the quadtree as a collection of the leaf nodes comprising it. Each node is represented by a pair of numbers [Garg82c]. The first number is the level of the tree at which the node is located. The second number is termed a locational code. It is formed by a concatenation of base 4 digits corresponding to directional codes that locate the node along a path from the root of the quadtree. The directional codes take on the values $0,1,2,3$ corresponding to quadrants NW , NE, SW, SE, respectively. For exampie, node 15 in Figure 1.1 is represented by the pair of numbers $(0,320)$, which is decoded as follows. The base 4 locational code is 320 . The pair denotes a node at level 0 that is reached by a sequence of transitions, SE, SW, and NW , starting at the root. A quadtree representation based on the use of locational codes is called linear quadtree by Gargantini [Garg82a, Garg82c] (because the addresses are keys in a linear list of nodes). Pointer-less representations are discussed in greater detail in Chapter 2 of [Same90b].

The worst case for a quadtree of a given depth in terms of storage requirements occurs when the region corresponds to a checkerboard pattern as in Figure 1.25. The amount of space required is obviously a function of the resolution (i.e., the number of levels in the quadtree), the size of the image (i.e., its perimeter), and its positioning in the grid within which it is embedded. As a simple example, Dyer [Dyer82] has shown that arbitrarily placing a square of size $2^{m} \times 2^{n \prime}$ at any position in a $2^{n} \times 2^{n}$ image requires an average of $O\left(2^{m+2}+n-m\right)$ quadtree nodes. An alternative characterization of this result is that the average amount of space necessary is $O(p+n)$ where $p$ is the perimeter (in pixel widths) of the block.

Dyer's $O(p+n)$ result for a square image is merely an instance of the earlier work of Hunter and Steiglitz [Hunt78, Hunt79a] who proved some fundamental theorems on the space requirements of images represented by quadtrees. In their


Figure 1.25 A checkerboard and its quadtree
studies, Hunter and Steiglitz used simple polygons (polygons with nonintersecting edges and without holes); however, these theorems have been observed to hold in arbitrary images (see [Rose82b] for empirical results in a cartographic environment).

In Hunter and Steiglitz's formulation, a polygon is represented by a three-color variant of the quadtree. In essence, there are three types of nodes: interior, boundary, and exterior. A node is said to be of type boundary if an edge of the polygon passes through it. Interior and exterior nodes correspond to areas within, and outside, respectively, the polygon and can be merged to yield larger nodes. The resulting quadtree is analogous to the MX quadtree representation of point data described below (for more details, see Section 2.6.1), and this term will be used to describe it. In particular, boundary nodes are analogous to black nodes, while interior and exterior nodes are analogous to white nodes.

Figure 1.26 illustrates a sample polygon and its MX quadtree. One disadvantage of the MX quadtree representation for polygonal lines is that a width is associated with them, whereas in a purely technical sense these lines have a width of zero. Also shifting operations may result in information loss. (For more appropriate representations of polygonal lines, see Chapter 4.)

An upper bound on the number of nodes in such a representation of a polygon can be obtained in the following manner. First, we observe that a curve of length $d+\varepsilon(\varepsilon>0)$ can intersect at most six squares of side width $d$. Now consider a polygon, say $G$, having perimeter $p$, that is embedded in a grid of squares each of side width $d$. Mark the points at which $G$ enters and exits each square. Choose one of these points, say $P$, as a starting point for a decomposition of $G$ into a sequence of curves. Define the first curve in $G$ to be the one extending from $P$ until six squares have been intersected and a crossing is made into a different seventh square. This is the starting point for another curve in $G$ that intersects six new squares, not counting those intersected by any previous curve.

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Figure 1.26 Hunter and Steiglitz's quadtree representation of a polygon

We now decompose $G$ into a series of such curves. Since each curve adds at most six new squares and has length of at least $d$, we see that a polygon with perimeter $p$ cannot intersect more than $6 \cdot\lceil p / d\rceil$ squares. Given a quadtree with a root at level $n$ (i.e., the grid of squares is of width $2^{\prime \prime}$ ), at level $i$ each square is of width $2^{i}$. Therefore polygon $G$ cannot intersect more than $B(i)=6 \cdot\left\lceil p / 2^{i}\right\rceil$ quadrants at level $i$. Recall that our goal is to derive an upper bound on the total number of nodes. This bound is attained when each boundary node at level $i$ has three brother nodes that are not intersected. Of course, only boundary nodes can have sons, and thus no more than $B(i)$ nodes at level $i$ have sons. Since each node at level $i$ is a son of a node at level $i+1$, there are at most $4 \cdot B(i+1)$ nodes at level $i$. Summing up over $n$ levels (accounting for a root node at level $n$ and four sons), we find that the total number of nodes in the tree is bounded by

$$
\begin{aligned}
& 1+4+\sum_{i=0}^{n-2} 4 \cdot B(i+1) \\
& \leq 5+24 \cdot \sum_{i=0}^{n-2}\left\lceil\frac{p}{2^{i+1}}\right\rceil \\
& \leq 5+24 \cdot \sum_{i=0}^{n-2}\left(1+\frac{p}{2^{i+1}}\right) \\
& \leq 5+24 \cdot(n-1)+24 \cdot p \cdot \sum_{i=0}^{n-2} \frac{1}{2^{i+1}} \\
& \leq \\
& \leq 4 \cdot n-19+24 \cdot p .
\end{aligned}
$$

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Therefore, we have proved:

Theorem 1.1 The quadtree corresponding to a polygon with perimeter $p$ embedded in a $2^{n} \times 2^{n}$ image has a maximum of $24 \cdot n-19+24 \cdot p$ (i.e., $O(p+n)$ ) nodes.

The proof of Theorem 1.1 is based on a decomposition of the polygon into a sequence of curves, each of which intersects at most six squares. This bound can be tightened by examining patterns of squares to obtain minimum lengths and corresponding ratios of possible squares per unit length. For example, observe that once a curve intersects six squares, the next curve of length $d$ in the sequence can intersect at most two new squares. In contrast, it is easy to construct a sequence of curves of length $d+\varepsilon(\varepsilon>0)$ such that almost each curve intersects two squares of side length $d$. Such a construction leads to an upper bound of the form $a \cdot n+b+8 \cdot p$ where $a$ and $b$ are constants (see Exercise 1.48). Hunter and Steiglitz use a slightly different construction to obtain a bound of $16 \cdot n-11+16 \cdot p$ (see Exercise 1.49).

Nevertheless, the bound of Theorem 1.1 is attainable as demonstrated by the following examples. First, consider a square of side width 2 that consists of the central four squares in a $2^{n} \times 2^{n}$ image (see Figure 1.27). Its quadtree has $16 \cdot n-11$ nodes (see Exercise 1.50). Second, consider a curve that follows a vertical line through the center of a $2^{\prime \prime} \times 2^{n}$ image. Now, make it a bit longer by making it intersect all of the pixels on either side of the vertical line (see Figure 1.28). As $n$ increases, the total number of nodes in the quadtree approaches $8 \cdot p$ where $p=2^{n}$ (see Exercise 1.51 ). A polygon having a number of nodes approaching $8 \cdot p$ can be constructed in a similar manner by approximating a square in the center of the image whose side is one-fourth the side of the image (see Exercise 1.52). In fact, it has been shown by Hunter [Hunt78] that $O(p+n)$ is a least upper bound on the number of nodes in a quadtree corresponding to a polygon (see Exercise 1.53).


Figure 1.27 Example quadtree with $16 \cdot n-11$ nodes


Figure 1.28 Example quadtree with approximately 8.p nodes

Theorem 1.1 can be recast by measuring the perimeter $p$ in terms of the length of a side of the image in which the polygon is embedded-i.e., for a $2^{n} \times 2^{n}$ image $p=p^{\prime} \cdot 2^{n}$. Thus the value of the perimeter no longer depends on the resolution of the image. Restating Theorem 1.1 in terms of $p^{\prime}$ results in a quadtree having $O\left(p^{\prime} \cdot 2^{n}+n\right)$ nodes. This leads to the following important corollary:

Corollary 1.1 The maximum number of nodes in a quadtree corresponding to an image is directly proportional to the resolution of the image.

The significance of Corollary 1.1 is that when using quadtrees, increasing the image resolution leads to a linear growth in the number of nodes. This is in contrast to the binary array representation where doubling the resolution leads to a quadrupling of the number of pixels.

Since in most practical cases the perimeter, $p$, dominates the resolution, $n$, the results of Theorem 1.1 are usually interpreted as stating that the number of nodes in a quadtree is proportional to the perimeter of the regions contained therein. ${ }^{10}$ Meagher [Meag80] has shown that this theorem also holds for three-dimensional data (i.e., for polyhedra represented by octrees) when the perimeter is replaced by the surface area. The perimeter and the surface area correspond to the size of the boundary of the polygon and polyhedron-that is, in two and three dimensions, respectively. In $d$ dimensions this result can be stated as follows:

Theorem 1.2: $\quad$ The size of a $d$-dimensional quadtree of a $d$-dimensional polyhedron is proportional to the sum of the resolution and the size of the boundary of the object.

[^8]Aside from their implications on the storage requirements, Theorems 1.1 and 1.2 also directly affect the analysis of the execution time of algorithms. In particular, most algorithms that execute on a quadtree representation of an image instead of an array representation have an execution time proportional to the number of blocks in the image rather than the number of pixels. In its most general case, this means that the application of a quadtree algorithm to a problem in $d$-dimensional space executes in time proportional to the analogous array-based algorithm in the ( $d-1$ )-dimensional space of the surface of the original $d$-dimensional image. Thus quadtrees are somewhat like dimension-reducing devices.

Theorem 1.2 assumes that the image consists of a polyhedron. Walsh [Wals85] lifts this restriction and obtains a weaker complexity bound. Assuming an image of resolution $n$ and measuring the perimeter, say $p$, in terms of the number of border pixels, he proves that the total number of nodes in a $d$-dimensional quadtree is less than or equal to $4 \cdot n \cdot p$. Furthermore he shows that the number of black nodes is less than or equal to $\left(2^{d}-1\right) \cdot n \cdot p / d$.

The complexity measures discussed above do not explicitly reflect the fact that the amount of space occupied by a quadtree corresponding to a region is extremely sensitive to its orientation (i.e., where it is partitioned). For example, in Dyer's experiment, the number of nodes required for the arbitrary placement of a square of size $2^{m} \times 2^{m}$ at any position in a $2^{n} \times 2^{n}$ image ranged between $4 \cdot(n-m)+1$ and $4 \cdot p+16 \cdot(n-m)-27$, with the average being $O(p+n-m)$. Clearly shifting the image within the space in which it is embedded can reduce the total number of nodes. The problem of finding the optimal position for a quadtree can be decomposed into two parts. First, we must determine the optimal grid resolution and, second, the partition points.

Grosky and Jain [Gros83] have shown that for a region such that $w$ is the maximum of its horizontal and vertical extent (measured in pixel widths) and $2^{n-1}<w \leq 2^{n}$, the optimal grid resolution is either $n$ or $n+1$. In other words embedding the region in a larger area than $2^{n+1} \times 2^{n+1}$ and shifting it around will not result in fewer nodes. Using similar reasoning, it can be shown that translating a region by $2^{k}$ pixels in any direction does not change the number of black or white blocks of size less than $2^{k} \times 2^{k}$ [Li82].

Armed with the above results, Li, Grosky, and Jain [Li82] developed the following algorithm that treats the image as a binary array and finds the configuration of the region in the image so that its quadtree requires a minimum number of nodes. First, enlarge the image to be $2^{n+1} \times 2^{n+1}$, and place the region within it so that the region's northernmost and westernmost pixels are adjacent to the northern and western borders, respectively, of the image. Next apply successive translations to the image of magnitude power of two in the vertical, horizontal, and corner directions and keep count of the number of leaf nodes required. Initially $2^{2 n+2}$ leaf nodes are necessary. The following is a more precise statement of the algorithm:

1. Attempt to translate the image by $(x, y)$ where $x$ and $y$ correspond to unit translations in the horizontal and vertical directions, respectively. Each of $x$ and $y$ takes on the values 0 or 1 .

## APPENDIX B

2. For the result of each translation in step 1, construct a new array at one-half the resolution. Each entry in the new array corresponds to a $2 \times 2$ block in the translated array. For each entry in the new array that corresponds to a single color (not gray) $2 \times 2$ block in the translated array. decrement the leaf node count by 3 .
3. Recursively apply steps 1 and 2 to each result of steps 1 and 2 . This process stops when no single-color $2 \times 2$ block is found in step 2 (i.e., they are all gray) or if the new array is a $1 \times 1$ block. Record the total translation and the minimum leaf node count.

Step 2 makes use of the property that for a translation of $2^{k}$, there is a need to check only if single-color blocks of size $2^{k} \times 2^{k}$ or more are formed. In fact, because of the recursion, at each step we check only for the formation of blocks of size $2^{k+1} \times 2^{k+1}$. Note that the algorithm tries every possible translation since any integer can be decomposed into a summation of powers of two (i.e., use its binary representation). In fact this is why a translation of $(0,0)$ is part of step 1 . Although the algorithm computes the positioning of the quadtree with the minimum number of leaf nodes, it is also the positioning of the quadtree with the minimum total number of nodes since the number of nonleaf nodes in a quadtree of $T$ leaf nodes is $(T-1) / 3$.

As an example of the algorithm, consider the region given in Figure 1.29a whose block decomposition is shown in Figure 1.29b. Its quadtree requires 52 leaf nodes. The first step is to enlarge the image, place the region in the upper left corner, and form the array (Figure 1.30). The optimal positioning is such that Figure 1.30 is shifted 7 units in the horizontal direction and 3 units in the vertical direction. This corresponds to a sequence of translations ( 1,1 ), ( 1,1 ), and ( 1,0 ). The intermediate translated arrays are shown in Figure 1.31. All gray nodes in the translated arrays are labeled with a ' $G$ ' while black nodes are shaded. The optimal quadtree contains 46 leaf nodes and is given in Figure 1.32.

Now let us trace the algorithm as it applies the optimal sequence of translations, in more detail. Initially the leaf node count is 256 . A translation of (1,1) leads to Figure 1.31 a where 58 of the array entries correspond to single-color $2 \times 2$ blocks in the translated array. The leaf node count is decremented by $58 \cdot 3=174$, resulting in


Figure 1.29 Example (a) image and (b) its block decomposition used to demonstrate the optimal positioning process


Figure 1.30 The array corresponding to the image in Figure 1.29 prior to the start of the optimal positioning process
82. The next translation of $(1,1)$ leads to Figure 1.31 b, where 11 of the array entries correspond to single-color $2 \times 2$ blocks. Therefore $11 \cdot 3=33$ is subtracted from 82 , and the leaf node count is now 49. The final translation of $(1,0)$ leads to Figure 1.31c, where only one of the array entries corresponds to a single-color $2 \times 2$ block in the translated array. Decrementing the leaf node count results in 46 nodes, and the process terminates. Of course, we have failed to describe the remaining $4^{n}-3$ translations that were also attempted.

Despite trying all possible translations, the algorithm is quite efficient. The key is that for each translation, only the blocks whose motion can lead to space saving need to be considered. This is a direct consequence of the property that a translation of $2^{k}$ does not change the number of blocks of size less than $2^{k} \times 2^{k}$. For an image that has been enlarged to fit in a $2^{n+1} \times 2^{n+1}$ array, the algorithm will have a maximum depth of recursion of $n$. Since at each level of recursion we need an array at half the resolution of the previous level, the total amount of space required is $(4 / 3) \cdot 2^{2 n+2}$.

1.31 The successive translated arrays at halfresolution after application of (a) (1,1) and (b) (1,1), and (c) $(1,0)$ to the original image array of Figure 1.30


Figure 1.32 Optimal positioning of the quadtree of Figure 1.29

The basic computational task of the algorithm is to count $2 \times 2$ blocks of a single color. It can be shown that $4 \cdot n \cdot 2^{2 n+2}$ array elements are examined in this process (see Exercise 1.63). Thus the algorithm uses $O\left(2^{2 n}\right)$ space and takes $O\left(n \cdot 2^{2 n}\right)$ time. Nevertheless experiments with typical images show that the algorithm has little effect (e.g., [Same84c]).

## Exercises

1.43. Consider the arbitrary placement of a square of size $2^{m} \times 2^{m}$ at any position in a $2^{n} \times 2^{n}$ image. Prove that in the best case $4 \cdot(n-m)+1$ nodes are required, while the worst case requires $4 \cdot p+16 \cdot(n-m)-27$ nodes. How many of these nodes are black and white, assuming that the square is black? Prove that on the average, the number of nodes that is required is $O(p+n-m)$.
1.44. What are the worst-case storage requirements of storing an arbitrary rectangle in a quadtree corresponding to a $2^{n} \times 2^{n}$ image? Give an example of the worst case and the number of nodes it requires.
1.45 Assume that the probability of a particular pixel's being black is one-half and likewise for being white. Given a $2^{n} \times 2^{n}$ image represented by a quadtree, what is the expected number of nodes, say $E(n)$, in the quadtree? Also compute the expected number of black, white, and gray nodes.
1.46 Suppose that instead of knowing the probability a particular pixel is black or white, we know the percentage of the total pixels in the image that are black. Given a $2^{n} \times 2^{n}$ image represented by a quadtree, what is the expected number of nodes in the quadtree?
1.47. The proof of Theorem 1.1 and the subsequent discussion raise the question of how $N$ squares should be arranged so that each is intersected by a curve of minimum length extending to the outside of the squares on each end. Such a configuration leads to a minimal curve in the sense that it has a maximal ratio of squares to length. For which value of $N$ is this ratio the smallest?
1.48. Try to prove that the upper bound of Theorem 1.1 can be tightened to be $a \cdot n+b+8 \cdot p$ where $a$ and $b$ are constants.

## APPENDIX B

1.49. Decompose the polygon used in the proof of Theorem 1.1 into a sequence of curves in the following manner. Mark the points where $G$ enters and exits each square of side width $d$. Choose one of these points, say $P$, and define the first curve in $G$ as extending from $P$ until four squares have been intersected and a crossing is made into a different fifth square. This is the starting point for another curve in $G$ that intersects four new squares, not counting those intersected by any previous curve. Prove that all of the curves, except for the last one, must be at least of length $d$. Using this result, prove that the upper bound on the number of nodes in the quadtree is $16 \cdot n-11+16 \cdot p$.
1.50. Prove that the quadtree corresponding to a square of side width 2 consisting of the central four squares in a $2^{\prime \prime} \times 2^{n}$ image has $16 \cdot n-11$ nodes (see Figure 1.27).
1.51. Take a curve that follows a vertical line through the center of a $2^{n} \times 2^{n}$ image and lengthen it slightly by making it intersect all of the pixels on either side of the vertical line (see Figure 1.28). Prove that as $n$ increases, the total number of nodes in the quadtree approaches $8 \cdot p$ where $p=2^{n}$.
1.52. Using a technique analogous to that used in Exercise 1.51 , construct a polygon of perimeter $p$ by approximating a square in the center of the image whose side is one-fourth the side of the image. Prove that its quadtree has approximately $8 \cdot p$ nodes.
1.53. Prove that $O(p+n)$ is a least upper bound on the number of nodes in a quadtree corresponding to a polygon. Assume that $p \leq 2^{2 n}$ (i.e., the number of pixels in the image). Equivalently the polygon boundary can touch all of the pixels in the most trivial way but can be no longer. Decompose your proof into two parts depending on whether $p$ is greater than $4 \cdot n$.
1.54. Can you prove that for an arbitrary quadtree (not necessarily a polygon), the number of nodes doubles as the resolution is doubled?
1.55. Derive a result analogous to Theorem 1.1 for a three-dimensional polyhedron represented as an octree. In this case the perimeter corresponds to the surface area.
1.56. Prove Theorem 1.2.
1.57. Assuming an image of resolution $n$ and measuring the perimeter, say $p$, in terms of the number of border pixels, prove that the total number of nodes in a $d$-dimensional quadtree is less than or equal to $4 \cdot n \cdot p$.
1.58. Assuming an image of resolution $n$ and measuring the perimeter, say $p$, in terms of the number of border pixels, prove that the total number of black nodes in a $d$-dimensional quadtree is less than or equal to $\left(2^{d}-1\right) \cdot n \cdot p / d$.
1.59. How tight are the bounds obtained in Exercises 1.57 and 1.58 for the number of nodes in a $d$-dimensional quadtree for an arbitrary region? Are they realizable?
1.60. Prove that for a region such that $w$ is the maximum of its horizontal and vertical extent (measured in pixel widths) and $2^{n-1}<w \leq 2^{n}$, the optimal grid resolution is either $n$ or $n+1$.
1.61. Prove that translating a region by $2^{k}$ pixels in any direction does not change the number of black or white blocks of size less than $2^{k} \times 2^{k}$.
1.62. Can you formally prove that the method described in the text does indeed yield the optimal quadtree?
1.63. Prove that $4 \cdot n \cdot 2^{2 n+2}$ array elements are examined in the process of constructing the optimal quadtree.
1.64. How would you find the optimal bintree?

# Date of Patent: Nov. 16, 1993 

[54] SYSTEM FOR MANAGING TILED IMAGES
USING MULTIPLE RESOLUTIONS
Inventors: John R. DeAguiar, Sebastopol; Ross M. Larkin, Rollings Hills, both of Calif.

Assignee: Optigraphics Corporation, San Diego, Calif.
Appl. No.: 694,416
[22] Filed:
Apr. 30, 1991
Int. Cl. ${ }^{5}$ $\qquad$ G06F 15/20
[52] U.S. Cl. $\qquad$ ............. 395/164; 345/201 395/162, 164, 166, 128-130; 340/798, 799; 358/452, 455

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Primary Examiner-Dale M. Shaw
Assistant Examiner-Kee M. Tung
Attorney, Agent, or Firm-Knobbe, Martens, Olson \& Bear
[57]
ABSTRACT
An image memory management system for tiled images. The system defines an address space for a virtual memory that includes an image data cache and a disk. An image stack for each source image is stored as a full resolution image and a set of lower-resolution subimages. Each tile of an image may exist in one or more of five different states as follows: uncompressed and resident in the image data cache, compressed and resident in the image data cache, uncompressed and resident on disk, compressed and resident on disk and not loaded but re-creatable using data from higher-resolution image tiles.

17 Claims, 39 Drawing Sheets



Fig. 2




Fig. 8

Fig. 94 Document Information Structure
300

| SELF-REFERENCE TO DOCUMENT HAMDLE | 302 | $\begin{gathered} \text { "OVERVIEWS INVALID" } \\ \text { FLAG } \end{gathered}$ | 304 | $\begin{aligned} & \text { CACHE MAGE } \\ & \text { COMPRESSIOMALGOR } \end{aligned}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| IMAGE COLDR TYPE | 308 | BITS PER IMAGE PIXEL | 310 | TILE SIZE INFORMATION | 312 |
| NUMBER OF SUBIMAGES IN DOC | 314 | INPUT FILE INFO | 316 | OUTPUT FILE IMFO | 318 |
| LIST OF SUBIMAGE HEADERS |  |  |  | 320 |  |

## Fig. $9 B$



Fig. 10 Tile Header
350





Memory Block State Diagram
Fig. 14



TO STATE 554 IN FIG. I5B


FROM STATE 572
Fig. 15C


Sheet 12 of 39


TO STATE 700 IM FIG.ITA


Fig. 17B

LoadTiff
Fig. 18


CREATE SKELETON DOCUMENT AND LOCK DOC HANDIE


## LoadTiff Tiles Słd <br> Fig. 19



LoadSubImDiskCache Fig. 20


BeginUndoableRasOp




Fig. 23A



IN FIG.23A


UndoPreviousRasOp
Fig. 25A


## Fig.25B



## EndCache Manager <br> Fiq. 26




## Fig. 28




UnlockExpHandle



Alloc Exp Handle
Fig. 32


ExpandTile


## Fig. 34



Fig. 35


CollectfreeCache



Free Exp Handle
Fig. 37


## Fig. 38



## SYSTEM FOR MANAGING TILED IMAGES USING MULTIPLE RESOLUTIONS

## MICROFICHE APPENDIX

A microfiche appendix containing computer source code is attached. The microfiche appendix comprises one (1) sheet of microfiche having 74 frames.

## BACKGROUND OF THE INVENTION

1. Field of the Invention

The present invention relates to memory management systems and, more particularly, to the memory management of large digital images.
2. Description of the Prior Art

The present invention comprises a memory management system for large digital images. These digital, or raster, images are made up of a matrix of individually addressable pixels, which are ultimately represented inside of a computer as bit-maps. Large digital images, such as those associated with engineering drawings, topographic maps, satellite images, and the like, are often manipulated by a computer for the purpose of viewing or editing by a user. The size of, such images are often on the order of tens and even hundreds of Megabytes. Given the current cost of semiconductor memory it is economically impracticable to dedicate a random access memory (RAM) to storing even a single large digital image (hereinafter just referred to as a "digital image"). Thus, the image is usually stored on a slower, secondary storage medium such as a magnetic disk, and only the sections being used are copied into main memory (also called RAM memory).

However, as is well known by users of computer aided design ("CAD") systems, a simplistic memory transfer scheme will cause degraded performance during many typical operations, including zooming or panning. Essentially, during such operations, the computer cannot transfer data between disk and main memory fast enough so that the user must wait for a video display to be refreshed. Clearly, these periods of waiting on memory transfers are wasteful of engineering time.

Presently, to enhance main memory storage of only relevant sections of a digital image, the image is logically segmented into rectangular regions called "tiles". Two currently preferred standards for segmenting an image into tiles are promulgated by the Computer Aided Logistics Support (CALS) organization of the United States government (termed the "CALS standard" herein) and by Aldus Corporation of Seattle, Washington, as defined in the Tagged Image Format File (TIFF) definition (e.g., "TIFF Specification, Revision 5.0, Appendix L). Among other tile sizes, both standards define a square tile having dimensions of $512 \times 512$ pixels. Thus, if each pixel requires one byte of storage, the storage of one such tile would require a minimum of 256 kilobytes of memory.
Others, such as Thayer, et al. (U.S. Pat. No. $4,965,751$ ) and Sawada, et al. (U.S. Pat. No. $4,920,504$ ) have discussed tiling or blocking a memory. However, such computer hardware is generally associated with a graphics board for improving the speed of pixel transfers between a frame buffer and a video display by addressing a group of pixels simultaneously. These systems have no relationship to tiling of the image itself and thus do not require knowledge of image size. Tiling has also been used to refer to polygon filling as in Dal-
rymple, et al. (U.S. Pat. No. 4,951,230), which is unrelated to the notion of tiling discussed herein.

The patent to Ewart (U.S. Pat. No. 4,878,183) discusses interlaced cells, each cell containing one or more 5 pixels, for storing continuous tone images such as photographs. The variable size cells are used to vary the resolution of an image according to a distance which is to be perceived by a user. However, the Ewart disclosure does not discuss rasterized binary images contain-
10 ing line drawings, nor does Ewart discuss virtual memory management for modifying or editing images, as will be more fully discussed below.
Even when stored in a mass storage system, an image library, containing a number of digital images, will con-
15 sume disk space very quickly. Furthermore, "raw" digital images are generally too large to transfer from mass storage to portable floppy disks, or between computer systems (by telephone, for example), in a timely and inexpensive manner unless some means is used to reduce the size of the image. Hence, users of binary images employ image compression techniques to improve storage and transfer efficiencies. One existing compression standard applicable to facsimile transmission, CCITT Group IV, or T. 6 compression, is now being used for digital images. Like many other compression techniques, however, the CCITT standard uses statistical techniques to compress data and, hence, it does not always produce a compressed image that is smaller than the original, uncompressed image. That means that image libraries will often contain a mix of compressed and uncompressed binary images. Similar compression standards exist for color and gray-scale images such as those promulgated by the JPEG (Joint Photog. Exp. Group) Standards Committee of the 35 CCITT as SGV III Draft Standard.

At the present time, digital images are typically viewed and modified with an image editor using an off-the-shelf computer workstation. These workstations usually come with a sophisticated operating system, such as UNIX, that employs a virtual memory to effectively manage memory accesses in secondary and main memories. In an operating system having virtual memory, the data that represents the executable instructions for a program or the variables used by that program do not need to reside entirely in main memory. Instead, the operating system brings portions of the program into main memory only as needed. (The data that is not stored in main memory being stored on magnetic disk or other like nonvolatile memory.) The address space that is available to any one application program is generally managed in blocks of convenient sizes called "pages" or "segments".
In general, a virtual memory system allows application programs to be written and executed without concern for the management of virtual memory carried out by the operating system. Thus, independence of the size of main memory is achieved by creating a "virtual" address space for the program. The operating system translates virtual addresses into physical addresses (in a 60 main or cache memory) with the aid of an "address translation table". This table contains one entry per virtual memory segment of status information. For instance, segment status will commonly include information about whether a segment is currently in main memory, when a segment was last used, a disk address at which the disk copy of the segment resides, and a RAM address at which the segment resides (only valid if the segment is currently loaded in main memory).

When the program attempts to access data in a segment that is not currently resident in main memory, the operating system reads the segment from disk into main memory. The operating system may need to discard another segment to make room for the new one (by overwriting the area of main memory occupied by the old segment), so some method of determining which segment to discard is required. Usually the method is to discard the least recently used segment. If the discarded segment was modified then it must be written back to disk. The operating system completes the "swap" operation by updating the address translation table entries of the new and discarded segments.
In summary, the conventional memory management schemes consider data to be in one of two states: resident or not resident in main memory. Which segments are stored in main memory at any given time is generally determined only by past usage, with no way of predicting future memory demands. For instance, just because a segment is the least recently used does not mean that it will not be used at the very next memory access.
However, the management of virtual memory for images departs significantly from conventional virtual memory schemes because images and computer programs are accessed in very different ways. Computer programs tend to access one small neighborhood of virtual address, and then jump to some distant, essentially random, location. However, during normal image processing operations an image is accessed in one of a finite set of predictable patterns. It is not surprising then that conventional memory management systems can significantly degrade performance when used in image processing applications by applying inappropriate memory management rules. Rules which should be abided by a memory management system for large digital images are the following:

1. Image memory must be managed as rectangular image regions (called "tiles"), not as linear memory address ranges.
2. An image tile can exist in five forms: uncompressed memory-resident, compressed memory-resident, uncompressed disk-resident, compressed disk-resident and "can be derived from other available image tiles", in contrast to the two basic forms of memory-resident and disk-resident available in conventional virtual memory schemes.
3. The image region that will be affected by a particular image processing operation is known before the operation begins, and that information can be conveyed to the memory manager.
4. An image memory manager must be tunable to different system capabilities and image types. For example, many computers can decompress a tile of binary data much faster that they can retrieve the uncompressed version of the same tile from disk. On the other hand, some images cannot be compressed at all.
5. An image memory management system should support the capability to "undo" editing operations which is built into the memory manager for optimal performance and ease of use. Thus, the memory manager could easily save copies of the compressed tiles in the affected region, and quickly restore the image to the original state by simply modifying the tile directory entries to point to the old version.

Reader, et al., ("Address Generation and Memory Management for Memory Centered Image Processing Systems", SPIE, Vol. 757, Methods for Handling and

Processing Imagery, 1987) discuss a primitive memory management system for images. However, in that system, image tiles are only stored in memory and not on disk. Furthermore, in the Reader, et al., system, there is no capability to handle images in compressed form, nor is there any discussion of "undoing" editing operations.

Consequently, a need exists for an image memory management system that provides: linkages with a raster image editor which includes modify and undo operations, true virtual memory for large images specifying locations on disk and in memory, simultaneous handling of compressed and uncompressed images, and a method for rapidly constructing reduced resolution views of the image for display. The latter need is particularly important when viewing a large image reduced to fit on a video display.

## SUMMARY OF THE INVENTION

The above-mentioned needs are satisfied by the present invention which includes a memory management system for tiled images. The memory management system includes a tile manager for maintaining a virtual memory comprising a main memory and a secondary memory such as a disk. The tiled images may include tiles in compressed or uncompressed form.

The tile manager selects the form of image tile that most appropriately matches a request. Each tile of an image may exist in one or more of five different forms, or states, as follows: uncompressed and resident in the image data cache, compressed and resident in the image data cache, uncompressed and resident on disk, compressed and resident on disk and not loaded but re-creatable using data from higher-resolution image tiles.
An image stack having successively lower-resolution subimages is constructed from a full resolution source image. The lower-resolution images in the image stack may be used to enhance such standard image accesses as zooming and panning where high speed image reduction is advantageous.

The image memory management system provides linkages with image processing applications that facilitate image modifications. The tile manager need only store compressed tiles that relate to so-called undoable operations.

These and other objects and features of the present invention will become more fully apparent from the following description and appended claims taken in conjunction with the accompanying drawings.

## BRIEF DESCRIPTION OF THE DRAWINGS

FIG. 1 is a perspective view of an image stack comprising full, half, quarter and eighth resolution tiled images;

FIG. 2 is a full resolution image of a mechanical part;
FIG. 3 is a half resolution image of the mechanical part shown in FIG. 2;

FIG. 4 is a quarter resolution image of the mechanical part shown in FIG. 2;

FIG. 5 is an eighth resolution image of the mechanical part shown in FIG. 2;

FIG. 6 is a block diagram showing one preferred embodiment of a computer system that includes the present invention;

FIG. 7 is a memory map showing the general arrangement of cache memory according to the present invention;

FIG. 8 is a state diagram defining the flow of tile data between different storage states according to the present invention;
FIGS. 9A and B are a diagram of one preferred data structure defining document information according to the present invention;
FIG. 10 is a diagram of one preferred data structure defining a tile header for maintaining the status of compressed or uncompressed tiles;
FIG. 11 is a diagram of a partial calling hierarchy for 10 the various functions of the presently preferred embodiment of the tile manager of the present invention;
FIG. 12 is a flow diagram of one preferred embodiment of the tile manager;
FIG. 13 is a flow diagram defining the "initialize cache manager" function referred to in the flow diagram of FIG. 12;
FIG. 14 is a state diagram of the locking and unlocking of a memory, state, according to the present invention;

FIGS. 15A, 15B, and 15C are a flow diagram defining the "create image access context" function referred to in FIG. 12;
FIG. 16 is a diagram, of a data structure defining the access context referred to in FIGS. 15A,B;
FIGS. 17A and 17B are a flow diagram defining the "save region for undo" function referred to in FIG. 15B;
FIG. 18 is a flow diagram defining the "load tiled raster image" function referred to in FIG. 12;
FIG. 19 is a flow diagram defining the "load TIFF subimage tile information into tile headers" function referred to in FIG. 18;
FIG. 20 is a flow diagram defining a "store tile info in tile headers" function referred to in FIG. 12;
FIG. 21 is a flow diagram defining the "begin undoable raster operation" function referred to in FlG. 12;
FIGS. 22A and 22B are a flow diagram defining the "read rows from region" function referred to in FIG. 12;

FIGS. 23A and 23B are a flow diagram defining the "write rows to region" function referred to in FIG. 12;
FIG. 24 is a flow diagram defining the "close image access context" function referred to in FIG. 12;
FIGS. 25A and 25B are a flow diagram defining the "undo previous raster operations" function referred to in FIG. 12;
FIG. 26 is a flow diagram defining the "quit cache manager" function referred to in FIG. 12;
FIG. 27 is a flow diagram defining the "lock ex- 50 panded image tile group" function referred to in FIG. 22A;
FIG. 28 is a flow diagram defining the "lock expanded tile" function referred to in FIG. 27;
FIG. 29 is a flow diagram defining the "unlock expanded image tile group" function referred to in FIG. 27;
FIG. 30 is a flow diagram defining the "unlock expanded tile" function referred to in FIG. 29;
FIG. 31 is a flow diagram defining the "create tile 60 from higher-resolution tiles" function referred to in FIG. 28;
FIG. 32 is a flow diagram defining the "allocate space for uncompressed version of tile" function referred to in FIG. 28;
FIG. 33 is a flow diagram defining the "create uncompressed version of tile from compressed version" function referred to in FIG. 28;

FIG. 34 is a flow diagram defining the "create compressed low resolution tile from compressed higherresolution tiles" function referred to in FIG. 31;
FIG. 35 is a flow diagram defining the "copy uncom5 pressed high resolution tile to uncompressed low reso lution tiles" function referred to in FIG. 31;
FIGS. 36A and 36B are a flow diagram defining the "collect freeable cache memory" function referred to in FIG. 32;
FIG. 37 is a flow diagram defining the "free uncompressed version of tile" function referred to in FIGS. 36A,B; and

FIG. 38 is a flow diagram defining the "create compressed version of tile from uncompressed version" function referred to in FIG. 17B.

## DETAILED DESCRIPTION OF THE PREFERRED EMBODIMENTS

Reference is now made to the drawings wherein like parts are designated with like numerals throughout

FIG. 1 illustrates an image stack, generally indicated at 100. The design of the image stack 100 is based on the idea that image memory can be managed as small square regions, called tiles, that are mostly independent of one another. In general, a tile may be either uncompressed (also termed expanded) or compressed. While the basic uncompressed tile size could be a variable, it is presently preferred to be fixed at 32 kilobytes, or 512 pixels by 512 pixels to conform with the Computer Aided Logistics Support (CALS) raster file format standard for binary images. (Note that the present invention allows binary and color images to coexist in a common image memory management system.)

In order to compensate for lower performance expected with a virtual memory management system for images, particularly when reducing large portions (by combining pixels) of the image for display, the present invention automatically maintains a series of reduced resolution copies, called subimages, of the full resolution image. Preferably, the resolution (i.e., pixels per inch) of each subimage is reduced by exactly half rela tive to the next higher-resolution subimage. Thus, the image stack 100 can be visualizing as an inverted pyramid, wherein the images can be stacked beginning with a full resolution subimage (or image) 102 at the top, followed by a half resolution subimage 104, then a quarter resolution subimage 106, and an eighth resolution subimage 108. (In FIG. 1, the subimages 102-108 are outlined by bolded lines.)

The subimages 102, 104, 106, 108 are superimposed on a set of tiled subimages $110 a, 110 b, 110 c, 110 d$, respectively, defining sets of tiles. The extent of the image stack 100 ends at the resolution that allows the entire subimage to be stored within a single tile 108 (preferably $512 \times 512$ pixels square). Each lower-resolution subimage 104-108 is a faithful representation of the full resolution subimage 102 at all times, with the exception of certain times during operations that modify the appearance of the full resolution subimage 102.

FIG. 2 illustrates an $8 \frac{1}{2} \times 11^{\prime \prime}$, A-size mechanical drawing (to scale) as the full resolution subimage 102 showing a mechanical part $120 a$. Of course, other larger drawings such as, for example, D-size and E-size may be used by the present invention. Also, other image processing applications besides mechanical drawings may be used with the present invention including electrical schematics, topographical maps, satellite images, hea-
ting/ventilating/air conditioning (HVAC) drawings, and the like.

FIG. 3 illustrates the corresponding half resolution subimage 104 showing the half resolution part $120 b$. FIG. 4 illustrates the corresponding quarter resolution subimage 106 showing the quarter resolution part 120 c . Lastly, FIG. 5 illustrates an eighth resolution subimage 108 showing the eighth resolution part 120d. In the preferred embodiment, reduced resolution subimages can be used any time that a reduction factor of $2: 1$ or higher would be used to scale a region of interest in the full resolution subimage 102 for display, plotting or copying.

The subimages 102-108 can be loaded from a source image file, if they exist, or they can be created on demand by the image memory management system of the present invention. The present invention includes editing capabilities that allow a user to trade off between "quick flash" pan/zoom performance and file size as measured by the number of reduced resolution subimages stored with each image. Depending on the application, the user will normally opt to store one or more reduced resolution subimages with each source image file.

The lower-resolution subimages, for example, subimages 104-108, are utilized by the image memory management system to produce the illusion of instant access to any region of the image at any scale factor (not just the scale factor of the overview subimage). Increasing the number of lower-resolution subimages gives a higher quality "first flash" image during panning and zooming and reduces the time to get the final version of the image to the screen.

FIG. 6 illustrates a computer workstation generally indicated at 150 which is representative of the type of computer that is used with the present invention. The workstation 150 comprises a computer 152, a color monitor 154, a mouse 156, a keyboard 158, a floppy disk drive 160, a hard disk drive 162 and an Ethernet communications port 164. The computer 152 includes a motherboard bus 166 and an I/O bus 168. The I/O bus 168, in one preferred embodiment, is an IBM PC/AT $®$ bus, also known as an Industry Standard Architecture (ISA) bus. The two buses 166, 168 are electrically connected by an I/O bus interface and controller 170.

The I/O bus 168 provides an electromechanical communication path for a number of I/O circuits. For example, a graphics display controller 172 connects the monitor 154 to the I/O bus 168. In the presently preferred embodiment, the monitor 154 is a 19 -inch color monitor having a $1,024 \times 768$ pixel resolution. A serial communications controller 174 connects the mouse 156 to the I/O bus 168. The mouse 156 is used to "pick" an image entity displayed on the monitor 154.

The I/O bus 168 also supports the hard disk drive 162, and the Ethernet communications port 164. A hard disk controller 176 connects the hard disk drive 162 to the I/O bus 168. The hard disk drive 162, in one possible configuration of the workstation generally indicated at 150, stores 60 megabytes of data. An Ethernet communications controller 178 connects an Ethernet communications port 164 with the I/O bus 168. The Ethernet communications controller 178 supports the industry standard communications protocol TCP/IP which includes FTP and Telnet functions. The Ethernet communications port 164 of the preferred embodiment allows the Workstation 150 to be connected to a network
which may include, among other things, a document scanner (not shown) and a print server (not shown).

The motherboard bus 166 also supports certain basic I/O peripherals. For example, the motherboard bus 166
5 is connected to a keyboard and floppy disk controller 180 which supports the keyboard 158 and the floppy disk drive 160 . The floppy disk drive 160 , in one present configuration, can access floppy disks which store up to 1.2 megabytes of data.

The fundamental processing components of the computer 152 are a microprocessor 182 such as, for example, an 80386 microprocessor manufactured by Intel, a math coprocessor 184 such as, for example, a 80387 math coprocessor also manufactured by Intel and a main memory generally indicated at 186 comprising, for example, 4 megabytes of random access memory (RAM). The main memory 186 is used to store certain computer software including a Unix compatible operating system 188 such as, for example, SCO Xenix licensed by Santa
20 Cruz Operation of Santa Cruz, California, a subsidiary of Microsoft Corporation, an image processing application 190, a tile manager 192, and an image data cache 194. The image processing application 190 includes editing functions such as zoom and pan.
Another presently preferred computer workstation 150 having somewhat different processing components from those just described is available from Sun Microsystems, Inc. of Mountain View, California, under the tradename "SPARCstation 1". In such an embodiment, the UNIX compatible operating system would be licensed directly from Sun.

Although a representative workstation has been shown and described, one skilled in the applicable technology will understand that many other computer and workstation configurations are available to support the present invention.
FIG. 7 illustrates a representative configuration of the image data cache 194 some time after the tile manager 192 (FIG. 6) begins operation. A set of compressed tiles 222 are kept at the low addresses of the image data cache 194, and a set of uncompressed (or expanded) tiles 224 at the high addresses of the image data cache 194. The terms expanded or uncompressed are used interchangeably. In between the two sets of tiles 222, 224 is a reserved area 226 (free cache memory). As the operation of the tile manager 192 continues, the image data cache 194 becomes more unordered. As the cache requirement for compressed or uncompressed tiles increases, each set of tiles 222, 224 approach the reserve area 226 from each end. In fact, the reserve area 226 can become completely exhausted.

Since the memory management schemes that apply to compressed data allocation are very different from that of uncompressed data, it is desirable to keep the two sets 55 of tiles 222, 224 separate. Compressed tiles are variable sized tiles (blocks of memory) 222a, b,c,d,e,f whereas the uncompressed tiles are all fixed sized tiles $224 a, b, c, d$ and therefore the locations of the fixed sized tiles 224 are interchangeable. Linked lists of allocated memory are kept sorted according to size and address for compressed tiles. The number of linked lists is a variable number but presently there are about 64 different size categories for compressed tiles and only one size category for uncompressed tiles (for binary images).
To use the image data cache 194, the memory management functions begin by determining how much fast memory (RAM) and slow memory (disk or host memory) is available for image memory uses. When an image
is loaded, the system allocates memory for image information and related tile directory structures. Cache management parameters are modified as necessary to balance the requirements for expanded tile and compressed tile cache memory. The expanded tile cache memory pool and the compressed tile cache memory pool allow tiles from different images to intermingle. Expanded and compressed tiles are kept in separate areas as much as possible so that memory allocation can be optimized for each of two different situations (i.e., fixed allocation block size versus variable size). However, the storage ranges of compressed and expanded tiles are allowed to mingle so as to maximize the flexibility of the cache usage.

FIG. 8 is a state diagram illustrating the flow of image data or tiles between different storage states 250. A tile can contain data in one or more of five states or forms as illustrated by ovals in FIG. 8. The possible forms are: uncompressed and resident in cache memory (state 252); compressed and resident in cache memory (state 256); uncompressed and resident on disk (state 268); compressed and resident on disk (state 262); "not loaded" but re-creatable using information from higherresolution image tiles (state 272).
For most image access operations, the image data must be uncompressed and resident in cache memory 252. However, that form consumes the most cache memory of any of the five forms. Therefore, a primary function of the tile manager 192 is to transform image tile data between state 252 and the other states which consume less (in the case of state 256) or no cache memory whatsoever (in the cases of states 268, 262 and 272).
The eight transformation operations, shown in square boxes in FIG. 8, constitute the main computational operations associated with managing image memory. The operation "load compressed tile image data from disk into cache memory" 264 is typically the first operation performed on a tile because most pre-scanned images are stored in compressed form in disk files. (A discussion of this "virtual loading" is provided hereinbelow.) The load operation 264 is performed by the Load CompFromDisk function which simply copies data from the disk into cache memory. The disk location and number of bytes to read is stored in the tile header fields 368 and 376 shown in FIG. 10.
The function LoadCompFromDisk is normally used by the function LockCompHandle when the tile manager 192 needs to access the compressed form of data associated with a tile. LockCompHandle is analogous to LockExpHandle, described in FIG. 28. The LockCompH andle function is also included in source code form in the Microfiche Appendix, in the file tilealloc.c.
Compressed data in cache 256 can be written back to the disk by the operation $\mathbf{2 6 0}$. This is the reverse of the LoadCompFromDisk function. The present embodiment is capable of writing to disk in a wide variety of file formats. One skilled in the art can easily create a function to perform this task.
Compressed data in cache can be uncompressed (also termed "expanded") into another region of cache memory by the expand operation 258 . The expand operation 258 is controlled by the "Expand Tile" function 440 which is described with respect to FIG. 33. The method of image compression varies according to image type (e.g. binary, 8 -bit color, 24 -bit color). Commonly used compression techniques include CCITT T. 6 for binary images and CCITT SGVIII (draft standard) for color and gray-scale images. The ExpandTile function 440
selects the appropriate compression algorithm by referring to field 306 of the Document Information Structure shown in FIG. 9.

Uncompressed data in cache 252 can be compressed and written to a separate region of cache memory by the compress operation 254. The compress operation 254 is controlled by the CompressTile function 450 described with respect to FIG. 38. Like ExpandTile, the CompressTile function 450 uses an image compression algorithm appropriate to the image type.

Uncompressed data on disk 268 can also be read directly into cache memory by the load operation 270. The load operation 270 is performed by the LoadExpFromDisk function, which appears in source code form in the Microfiche Appendix, in file diskcach.c. The LoadExpFromDisk function is analogous to LoadCompFromDisk. The LoadExpFromDisk function refers to the fields 362 and 374 of the tile header 350 shown in FIG. 10, for the location and number of bytes of the expanded file data on the disk.

Uncompressed data in cache 252 can be written back to the disk by the save to disk operation 266 . This operation is analogous to the save to disk operation 260 which operates on compressed data. The present embodiment can write compressed or uncompressed tile data to disk in a variety of formats. One skilled in the art can easily implement an equivalent function.

Image data for tiles in the "not loaded" state $\mathbf{2 7 2}$ must be constructed by resampling higher-resolution tiles. (During normal operation, only lower-resolution tiles can exist in this state-the full resolution subimage tiles are always "loaded".) The present embodiment provides two operations from the "not loaded" state 272 to the "loaded" state 252, 256. Uncompressed higher-resolution tile data is resampled to create uncompressed data in cache 252 by the resample operation 274. Similarly, in the resample operation 276, compressed data in cache 256 can be created from compressed higher-resolution tile data.

In both resampling operations, extensive advantage is taken of the fact that the resolutions of adjacent subimages in the subimage stack are related by a power of 2 . This greatly simplifies and speeds the resampling operation. Basic resampling techniques are well-known (See, for example, A. Rosenfeld and A. C. Kab, Digital Picture Processing, Academic Press, 1976). The resampling operation 274 and 276 are controlled by the function LoadSubImTile 436 described with respect to FIG. 31.

In summary, FIG. 8 shows that a great part of the tile manager's utility derives from its ability to coordinate a variety of forms of image data in the course of complex image processing operations.

Generally, the way data starts out on the disk 162 is by loading a tiled image file into an application 190 via 5 the tile manager 192. An image file, like a Tagged Image File Format (TIFF) or CALS tiled image file, for example, can be loaded instantaneously, in a virtual sense. In the tiled formats, there are tiled image data that is stored in the image file and at the beginning of the file there is a directory with entries that locate the tiles (for example, the disk file version of tile 0 in subimage $0,(0,0)$, is located at one address in the file and the disk file version of tile 1 , subimage $0(0,1)$ is located at another address in the file). When an image file is 5 loaded, the tile manager 192 gets the tile offsets and stores them in the tile directory and does nothing else. Hence, the image file is basically loaded without copying any data from the disk 162 into the image data cache

194, and a directory is created that maps the tiles in the virtual image memory space onto the disk 162.
FIG. 9A illustrates a document information structure 300. Each image, or document, in the system is associated with (and described by) a document information structure (called "docinfo", defined in FIG. 9). The docinfo structure contains information about the image as a whole, such as color and pixel organization, etc. It also contains a list of subimages contained in the image. Each subimage entry in the docinfo structure contains information about that subimage, such as width and height, etc. The intention is to make this data visible only to cache management functions and low-level access functions. The overall docinfo data structure 300 contains the following information:
302 Self-reference to document handle. Handle value assigned to this document by the host procedure which created the document. This value is unique over the entire system.
304 "Overviews Invalid" flag. This flag is true if the 20 document is in the middle of a write operation.
306 Cache image compression algorithm. Compression algorithm used by the memory manager for this image.
308 Image color type. How the image is displayed.
310 Bits per image pixel. Number of bits per image pixel.
312 Tile size information. Size of expanded tile in pixels. The tiles are assumed to be square.
314 Number of subimages in doc. Number of subim- 30 ages maintained in this document. The minimum value is one (the full resolution subimage).
316 Input file info. Input raster file information.
318 Output file info. Output raster file information.
320 List of subimage headers. Array of pointers to subimage header structures 321. The first entry in the array is always the full resolution image. Each position thereafter corresponds to a $2 \times$ resolution reduction from the previous subimage.
The subimage header structure 321 is illustrated in 40 FIG. 9B. Each subimage has its own entry with each field as follows:

312 Pointer to tile headers.
314 Pointer to tile directory. Pointer to array of pointers to tile header records. This two-dimensional table provides an easy way to access individual tile headers on a (row,col) basis.
326 Subimage width and height. The width (x extent) and height ( $y$ extent) of the document measured in pixels.
328 Number of tile rows \& cols in subimage. Number of tile rows in the image and the number of tile columns (i.e., the number of tiles needed to span the height and width of the image).
330 Image stack index of this subimage. This is the position of the subimage in the docinfo structure subimage list. It can also be used to determine the factor by which the subimage resolution is reduced relative to the full resolution subimage.
332 Pixel resolution of this subimage. Scan resolution 60 in pixels per millimeter.
FIG. 10 illustrates the tile header 350. The tile manager's analog to the conventional address translation table is the tile directory. The tile directory is a two-dimensional array of entries corresponding to the two-dimensional array of tiles that form the image. Each full and reduced resolution image has its own tile directory. The tile directory record contains a list of pointers to

The top level in the program hierarchy is Main 402. Main initiates the functions calls to the lower level functions. Main embodies the top level control flow of 5 the present invention.

The first function called by Main is Initialize Cache Manager 404 (InitCacheManager). InitCacheManager allocates the RAM and disk swap space needed for a
particular raster image. It must be called before attempting to load any image tiles into memory.

The next function Main may call is Load Tiled Raster Image 408 (LoadTIFF). LoadTIFF manages the loading of tiled images. This is the process where an existing image file on disk is mapped into memory.

Main will then call the function Begin Undoable Raster Operation 410 (BeginUndoableRasOp). BeginUndoableRasOp marks the beginning of a distinct, "undoable" raster image operation. This function does not save any region of image memory but only creates a new entry on the undo stack. The current version of the tiles in the affected region are saved by InitImageAccess.

The following function called by Main is Create Image Access Context 412 (InitImageAccess). InitImageAccess prepares the tile cache manager for upcoming accesses to a particular region of the specified image. This function creates a data structure called an "access context" (defined in FIG. 16) that is used by the sequential access functions.

Main optionally calls the function Read Rows From Region 414 (ReadRowToRow) next according to the operation performed by the user. ReadRowToRow causes one input/output buffer row or strip to be read and transformed from tiled image memory as specified in the associated InitImageAccess call and the resulting access context.

The next optional function called by Main is Write Rows To Region 416 (WriteRowToRow), again according to the operation performed by the user. WriteRowToRow causes one input/output buffer row or strip to be transformed and written to tiled image memory as specified in the associated InitImageAccess call and the resulting access context.

It should be understood that other access functions, such as random pixel accesses, may optionally be called by Main.

Main then calls the function Close Image Access Context 418 (EndImageAccess). EndImageAccess terminates and discards an image access context. The memory allocated for the access context structure is freed. The tile manager is informed that the specified region of image memory is no longer needed by this operator.

The next function, Undo Previous Raster Operations 420 (UndoPreviousRasOp), is optionally called by Main. UndoPreviousRasOp restores the specified region to its original state using information from the undo stack.

The last function Main calls is Quit Cache Manager 422 (EndCacheManager). EndCacheManager frees the RAM and disk swap space. This function basically reverses what InitCacheManager does.
The second level of functions on the calling hierarchy 400 is shown starting with Load TIFF Subimage Tile Information into Tile Headers 424 (LoadTiffTilesStd) which is called by function LoadTIFF 408. LoadTiffTilesStd manages the loading of TIFF images with strip structure.

The LoadTiffTilesStd function 424 calls a function Store Tile Information in Tile Headers 425 (LoadSubImDiskCache). LoadSubImDiskCache loads the tile directory of the specified subimage with information about the location, size and format of individual image tiles contained in a disk-resident tiled image file. It is the low-level interface for the "indirect file load"
capability. The tile headers are assumed to be completely zeroed when this function is called.

The InitlmageAccess function 412 calls a function Save Region For Undo 426 (SaveRegionForUndo). SaveRegionForUndo saves the specified region on the undo stack. It is called from within InitImageAccess if the SaveForUndo flag is true. It can also be used for low level operations that do not go through InitImageAccess. SaveRegionForUndo can then be called multiple times for different documents and different regions within a document so that arbitrarily complex editing operations can be easily undone.
The ReadRowToRow function 414 calls a function Lock Expanded Image Tile Group 428 (ExpTileLock). ExpTileLock "locks" memory handles referring to expanded image tiles. (The notion of locking and unlocking memory blocks is further discussed below with reference to FIG. 14.) It also updates the associated tile header structure as appropriate for the operating system.
The ReadRowToRow function 414 also calls a function Unlock Expanded Image Tile Group 430 (ExpTileUnlock). ExpTileUnlock unlocks memory handles referring to expanded image tiles. It also updates the associated tile header structure as appropriate for the operating system.
The function ExpTileUnlock 430 calls a function Unlock Expanded Tile 432 (UnlockExpHandle). UnlockExpHandle unlocks an individual expanded tile handle. The lock count is decremented as appropriate. The tile is not actually swapped out of cache at this point but it becomes a candidate for swapping.
The function ExpTileLock 428 calls a function Lock Expanded Tile 434 (LockExpHandle). LockExpHandle locks an individual expanded tile handle. The lock count is incremented and the status flags are set as appropriate.
The LockExpHandle function calls a function Create Tile From Higher-Resolution Tiles 436 (LoadSublmTile). LoadSubImTile creates a valid expanded version of the specified tile by scaling down from the next high-er-resolution subimage. This function is called recursively as necessary to get to a higher-resolution subimage where there is valid data. (Note: the tiles in the full-resolution subimage are always valid and loaded although not necessarily present in the cache memory.)
The function LockExpHandle 434 next calls a function Allocate Space for Uncompressed Version of Tile 438 (AllocExpHandle). AllocExpHandle allocates space in cache memory for a single expanded tile.
The function LockExpHandle 434 also calls a function Create Uncompressed Version of Tile From Compressed Version 440 (ExpandTile). ExpandTile uses a tile that exists in compressed form but not expanded form, allocates space for an expanded tile and decompresses the image data into that space.

The function LoadSubImTile 436 calls a function Create Compressed Lower-Resolution Tile From Compressed Higher-Resolution Tiles 442 (CompCopyToOview). CompCopyToOview creates a valid compressed version of the specified tile by scaling down from compressed or expanded version of the given higher-resolution subimage tiles. The function LoadSubImTile 436 also calls a function Copy Uncompressed High-Resolution Tiles to Uncompressed LowResolution Tile 444 (CopyTileToOview). CopyTileToOview updates the region of the next low-
er-resolution overview corresponding to the specified tile.
The Function CompCopyToOview 442 calls a function Collect Freeable Cache Memory 446 (CollectFreeCache). CollectFreeCache collects freed memory states or enlarges the cache file and adds the new memory capacity to the reserve list. This function is called when the cache manager usage exceeds preset limits. Therefore it makes sense to take time to free up as much memory as is convenient at this opportunity.
The function CollectFreeCache calls a function Free Uncompressed Version of Tile 448 (FreeExpHandle). FreeExpHandle frees space used for storage of expanded image tiles.
The function CollectFreeCache 446 also calls a function Create Compressed Version of Tile From Uncompressed Version 450 (CompressTile). CompressTile uses a tile that exists in expanded form but not compressed form, allocates space for a compressed tile and compresses the image data into that space.
FIG. 12 is the top-level control flow for the tile manager 192 (also called "Main"). The tile manager 192 can be executed on a number of operating systems or without an operating system. However, the workstation 150 (FIG. 6) preferably includes the Unix compatible operating system 188. Another preferred operating system is Microsoft MS-DOS running with or without Microsoft Windows 3.0.

Moving from a start state 470 to an initialization state 404, the tile manager 192 performs an initialization of the image data cache 194 to determine the available memory space, or the amount of physical RAM and disk space available for a cache "file". At this point, the cache appears to the tile manager 192 as one contiguous range of physical addresses in memory. If the tile cache has already been initialized, this step is skipped. The possibility of multiple image access contexts (discussed below) allows multiple simultaneous requests.

The tile manager 192 has another parameter which is called the fast memory portion of the image data cache 194. This parameter is particularly relevant when working on top of another virtual operating system such as Unix. The fast memory limit specifies approximately how much of the image cache file is actually kept in RAM memory at any moment by the native operating system (e.g., Unix). The balance of data (the less recently used portion) is likely to have been swapped out to the disk. The tile manager attempts to limit the amount of cache space used to store expanded tiles to less than the fast memory limit, but the limit can be exceeded if necessary with some degradation in performance. However, the total cache size limit is never exceeded. In operating systems without virtual memory capabilities built in (e.g., MS-DOS), the fast memory limit is the same as the total cache size limit.
Then the tile manager 192 moves to a function 472 wherein the tile manager 192 loads a tiled raster image file. The function 472 (comprising the function 408 , for example) loads any type of image file, and preferably a tiled image, into the memory address space configured by the tile manager 192. If the image to be modified is already loaded, this step is skipped. Then the tile manager 192 moves to a function 410 where the tile manager 192 marks the beginning of an undoable raster operation if the tile manager 192 is writing to the image. The function 410 is an optional state and it is only used if the user wants to be able to undo the operation that modifies the image.

FIG. 13 illustrates the initializing of the cache manager function 404. The function 404 is entered by the task manager 192 at a state 488. Then, moving to a state 490, the task manager 192 initializes the cache usage 5 variables. Of course, in the beginning, all of the cache space is available for use, in what is called the free-memory reserve list. That is, no cache memory is being used for expanded or compressed image data.

At state 492, the task manager 192 allocates tile cache memory by requesting a portion of the address space from the memory space owned by the operating system. In a virtual memory system such as Unix, the request is handled by memory mapping a large file. The operating system does not allocate any memory, but it reserves an address space. Moving to a state 494, the task manager 192 allocates a common blank tile. When dealing with binary images, space is reserved for one blank tile, which is kept around at all times for common usage by any number of operations, or access contexts.

At state 496 a compression buffer is allocated to be used as a scratch buffer when compressing data since, in general, the size of the resulting compressed data is unknown before a tile of image data is compressed. Hence, compressed data blocks will be variable sized. The tile manager 192 then exits the InitCacheManager function 404 at an end state 498.

FIG. 14 illustrates a general memory state diagram with reference to a block of memory being "locked" or "unlocked". In the diagram, ovals are states and rectangular blocks are operations.
The state diagram is entered at a start state $\mathbf{5 0 2}$ by a new memory block. There are three basics states. "FREE" is a state 504 where there is no memory allocated. Actually, a block of memory is considered free if it is in one of the memory free lists, i.e., the "reserve free list", the "compressed free list" or the "expanded tile free list". It should be understood that the free list for the compressed tiles are actually composed of many lists based on the varying sizes of memory blocks.
Within a tile header (FIG. 10) the tile manager 192 controls a memory handle which is a structure that has a pointer to (or location of) image data in the cache and a lock count (not shown) for both compressed and expanded versions of a tile.
A memory block transitions from the free state to unlocked, but allocated is through a state 506 for allocating the memory handle, which moves the block out of the free list and into use by a tile. As opposed to free, unlocked means that the memory block contains valid data and that it is associated with a tile but not currently being accessed. That is, the block is not being read or written at the time.
Now, the tile is unlocked at a state $\mathbf{5 0 8}$ but it contains valid data. Therefore, the next step is to lock the block, or lock the memory handle at a state 512 and then it becomes a locked memory state at a state 514. That means it contains valid data and it is currently in use. The block can be locked more than once, each time just incrementing the lock count.

The lock count may be incremented multiple times, for example, when two access contexts (operations) are accessing the same region of memory. Hence, both contexts lock the block of memory or tile by incrementing the lock count. When the first access context is done it decrements the lock count. But the tile manager 192 knows that that tile is still in use by an access because the locked count is still non-zero.
The inverse operation is to unlock the handle at a state 516 and as long as the lock count is not decremented to zero at state 518, it stays locked. Once the lock count is decremented to zero, it becomes unlocked again at the state 508.

An unlocked tile is fair game for the tile manager 192 when the memory manager needs to find some space to lock a new tile. Therefore, when the tile manager 192 is parameters are validated. If there is an error with the input parameters, the function ends immediately at an end state 534.
Input parameters include a document handle indicating which image that the user wants to read or write 15 from. Thus, the document handle must be validated. Another parameter is whether the user wants to read or write to the image. A transformation matrix, also input, basically directs how to scale, rotate, shear, etc., the image data.
If the input parameters are valid, the tile manager 192 locks the document handle at a state 536. The document handle locks and unlocks just like other structures and resources in the tile manager and it prevents one user of a particular document or image from modifying or deleting that image while another operation or another access context is still using that document.
Then, at a state 538, the tile manager 192 tests whether a non-orthogonal rotation has been specified. For example, a rotation of $30^{\circ}$ causes the tile manager
30192 go into a special operation that initializes the access with rotation. That also creates an access context but after a more involved process. Then the tile manager 192 ends the function 412 at a state 534 with a valid access context for rotations.
If an orthogonal rotation is specified then the tile manager 192, allocates a conventional access context at a state 542. Then the tile manager 192 continues to a decision state 544 wherein the subimage selection criterion is specified. For instance, the user may request the "low resolution" option which selects the lowest resolution subimage in the document's image stack. (In the context of an image editor, this may be the best solution during zooming or panning.) The user may also specify "most available"-i.e., whatever subimage has tiles 45 currently in cache memory, regardless of the resolution. In either case, the tile manager 192 proceeds to a state 546 to select the reduced resolution subimage that is appropriate to that particular choice, i.e., either the one that has the resolution just greater than what was requested or a subimage whose tiles covering the access region are currently in cache. Now, at a state 548, the tile manager 192 adjusts the transformation matrix so as to now refer to the reduced resolution subimage rather than the full resolution subimage by adjusting scale factors.

Alternatively, if the state $\mathbf{5 4 4}$ determines that the full resolution subimage is selected then the transformation matrix is unchanged. Proceeding to a state 552, the pixel and tile limits of the affected image region are calculated. Knowing these limits, in a state 554, the tile manager 192 creates a temporary directory for the tiles in that region. This directory is a two-dimensional array that references the tiles that contains the affected pixels. Later on the tile manager 192 refers to the region tile affected region.

The tile manager 192 then initializes the image scaling functions in a state $\mathbf{5 5 6}$. Such scaling functions presently

## APPENDIX C

used are the subject of applicant's concurrent application entitled "Process for High Speed Rescaling of Binary Images" (U.S. Ser. No. 08/014,085, filed Feb. 4, 1993, which is a continuation of Ser. No. 07/949,761 filed Sep. 23,1992, now abandoned, which is a continuation of Ser. No. 07/693,010 filed Apr. 30, 1991 now abandoned.
Moving on, the tile manager 192 tests whether polygonal clipping is required at a state 558 . For example, a request may be made to only read from within a specific polygonal region. If that is the case, the tile manager 192 initializes the polygonal region clipping functions in the tile manager 192 by passing in the boundary lists. The polygonal clipping function translates the boundary lists into edge lists that are used to very efficiently read out the rows or columns of data.

For example, suppose a "flood" request is made to turn all of the pixels black within an octagonal region. One way to accomplish the operation is to specify the points of the corners of the octagon in image coordinates and pass that in with the initialization of access context request, which would pass those vertices of the polygon into the polygonal clipping function set up function.

Then the tile manager 192 comes to a state 562, where the tile manager 192 allocates buffers for scaling, if necessary. This is the situation where intermediate copies of the rows or columns of data may need to be kept during the process of scaling. Then the tile manager 192 tests whether the user specified that the region needed to be saved for undoing, at a decision state 564 .

An important feature of the present invention is an "undo" operation that is integrated with the image memory management so that only compressed tiles need to be saved after an undoable edit operation. In this way, a user can easily and quickly retract an edit operation that is no longer desired. For example, in mapping applications, e.g., USGS Quadrangle maps, the impression of a very large map is desired, but it is really composed of smaller map quadrants that were separately scanned, trimmed, adjusted and fit together. The smaller maps can be visually and logically joined into a single, large image. Using the present invention, a user can add a feature, such as a new sub-division, town, or road, that crosses a map boundary, specifying that the feature is undoable. Later, the user can remove the feature modification to the image by specifying the undo operation.

Now at a decision state 568, the question is whether to update the subimages during the operation. If this is a write operation the tile manager 192 always writes into the full resolution subimage and the changes "trickle down" into the low resolution subimages. But the tile manager 192 has an option as to whether the lower-resolution tiles are updated during the modification operation or later when the tiles are requested for viewing operations. There are advantages in doing them both ways.

For example, if the affected region is small, it is more efficient to update the subimages while progressing through the operation. In this mode, when the tile is unlocked, the manager 192 immediately copies the data down into the next lower subimage tile but only one of the comers of the tile is affected. Thus, only portions of the low resolution subimage tiles need to be modified.

If, however, the subimages are not updated during the operation, then as soon as the image access context is created all of the subimage tiles that overlap the af-
fected region are invalidated (they become "not loaded"). Hence, when the memory manager goes to access them again at some later time, it has to reconstruct them from the higher-resolution tiles. The advantage of that is that the memory requirement at any one moment is half of that of if the tile manager 192 was updating all of the tiles simultaneously. In this way, the tile manager 192 sets a flag at a state 570 .

In state 572 the tile manager 192 "preserves" the affected tiles in the affected subimages. Again, it relates to whether the tile manager 192 is updating subimages or not. If the tile manager 192 is reading, then it preserves only the tiles in the region of the subimage that will be accessed.

The ability to "preserve", or preferentially retain tiles that will be accessed in the course of the operation, is an important feature of the present invention that can yield significantly higher performance in certain situations where memory capacity limitations are encountered. When a tile is "preserved" for a particular access operation, it's preserve count 360 is incremented. The cache manager treats tiles with non-zero preserve counts differently from tiles with zero preserve count. The cache manager will discard unlocked unpreserved tiles before discarding older preserved tiles. (The cache manager normally discards older or less recently used tiles before discarding newer or more recently used tiles.)

Then, within the creation of the access context, the tile manager 192 actually locks down the first row or column of tiles in the region to establish the cache memory requirement for this operation, at a state 574. If this succeeds, then the caller is assured that there will be sufficient cache space for the entire operation.

The tile manager 192 can perform row or column accesses. However, the following discussion only refers to a row access.
Then, at a decision state 576, if the tile manager 192 cannot satisfy the request to lock down that first row of tiles, the function 412 terminates at the end state 578. Otherwise, at state 580 the tile manager 192 initializes the row access functions.

Now, once the tile manager 192 has initialized the row access function in state 580 the tile manager 192 invalidates the affected subimage tiles if the tile manager 192 is writing to the full resolution subimage at a state 582. Finally, in a state $\mathbf{5 8 4}$ the tile manager 192 returns the handle or a pointer to this access context to the user. From then on the user just uses this pointer to the access context and pointers to input and output buffers to get the next row or column of data.

FIG. 16 illustrates the access context structure 600. The structure 600 operates on a high level to hide the low level operation from the user and contains bookkeeping information along with some memory management information. The access context 600 contains the following information:

602 Pointer to affected doc. Pointer to the document being accessed.
604 "Subimage Choice" option value. Specifies how to choose which of the subimages will be read from or written to.
606 Index of affected subimage. Index of the specific subimage directly affected by this access context.
608 Access quantum. Specifies "granularity" of image access.
610 Read/write option. Specifies what type of image memory accesses to prepare for (e.g., read or write).

612 Basic orthogonal rotation value. Specifies the image rotation in terms of how the bits in each buffer row are read from or written to the image (e.g., write buffer row to image column with increasing " $y$ " coordinate).
614 Pixel combination operation. Specifies the pixel operation performed when combining the buffer contents and image contents. The results of the operation are stored in the output buffer when reading. The results go into image memory when writing.
616 Scaler type operation. Specifies the type of scaler preferred. In other embodiments, this may include fast low-accuracy scaling and line width-preserving scaling.
618 "Update overviews" flag. True flag indicates overview subimages should be updated in the course of this modification of the full resolution image. This causes the overviews to be correct when the access is complete.
620 I/O buffer width \& height. Width (i.e., row length), total number of rows to process and pitch in pixels of the input/output bitmap.
622 I/O buffer pitch (bytes/row). Pitch of the input/output buffer in bytes used for multi-row accesses. The input/output buffer is assumed to be a contiguous memory bitmap at least as large as the access quanta. It is always read or written in the natural order (by rows, low address to high). Flipping and rotation is always done on the image memory side.
624 I/O buffer bit offset to start of run. Indicates where the buffer's $x=0$ pixel lies within the first long word of the buffer's storage space. It must be between 0 and 31 inclusive. This parameter allows the caller to match up with arbitrary bit alignments.
626 Rows per strip (for AQ_STRIP access quantum). When operating in the AQ_STRIP mode, this specifies the maximum number of rows per input/output strip. Fewer rows may be written into the last strip if the end of the access region is hit before the strip is filled.
628 Number of I/O buffer rows yet to be processed. This variable is used in the access routines to keep track of the number of input/output rows remaining for the access operation.
630 Pointer to access function used in "SeqBufImageAccess". Pointer to the image access function that is tailored to the specific access mode requested.
632 Stepping directions for image row and column indices. The stepping increment each time the input/output buffer is advanced one row and one pixel. The allowed values are $+1,0$, and -1 .
634 Pointer to polygon clipping information. Refers to an edge table structure for controlling polygonal boundary clipping.
636 Pointer to raster scaling information. Tile level access information used by lower level modules in the course of the operation.
638 Pointer to uncompressed data in currently locked tiles. Pointer to an array of pointers directly into expanded tile image data. This list is used to accelerate sequential access into image memory. As each new tile row or column is encountered in a sequential access, this array is set to point directly into the affected tiles, which have been brought into cache memory and locked down. In other Region for Undo" function 426 as referenced in FIG. 15. The tile manager 192 starts at a state 680 , moves to 682 where the tile manager 192 locks the document handle of the affected document that contains the re5 gion to save for undo. The tile manager 192 can save multiple regions from multiple documents sequentially and then undo them all in one operation later. Thus, the application programmer is allowed to easily undo multi-ple-region operations with a single undo call at a later 60 point.

Moving to a state 684, the tile manager 192 clips the modified region to the image boundaries since there is no information to save outside of the image. Then the tile manager 192 moves to a decision state 686 wherein 5 the tile manager 192 tests whether the affected region overlaps the image. If there is no overiap, that is to say, there is no image data to save, then the tile manager 192 moves to a state 688 where the tile manager 192 unlocks
the document handle and terminates the function 426 at an end state 690.
If, however at state 686, the modified region does overlap the image, the tile manager 192 moves to a state 692 wherein the tile manager 192 allocate memory for an "undo region header". The undo region header is similar to a document header, but reduced comparatively in the amount of data conveyed therein. The undo region header will be associated with tile header information, etc.
The tile manager 192 then moves to a state 694 where the tile manager 192 allocates memory for "undo region tile headers". These tile headers will be used to store copies of the original versions of the tiles in the affected region. The tile manager 192 then proceeds to a state 696 wherein the tile manager 192 makes an "undo tile directory".
Then the tile manager 192 moves to a loop state 698 where the tile manager 192 loops for each tile row in the region. The tile manager 192 then transitions to a loop state 700 wherein the tile manager 192 loops again for each tile column in the region (Thus, there is a two-dimensional loop.)
The tile manager 192 moves from the state 700 to a decision state 702 where the tile manager 192 checks to see if that particular tile in the document is loaded in the image cache memory. If the tile is not loaded, the tile manager 192 skips to the next tile in the region by returning to the loop state 700 . OtherWise, if the tile is loaded, the tile manager 192 marks the undo copy of the tile as loaded in a state 704.
Note that there are two tiles. One is the original version of the tile that is still associated with the document and the second is the copy that the tile manager 192 is going to make and associate with the undo region header.
At a decision state 706, a test determines whether the document tile is blank. If the tile is blank (i.e., all background color), then the tile manager 192 moves to a state 708 and simply marks the undo tile as "blank" and returns to the FOR-loop at 700. If the document tile is not blank, then the tile manager 192 moves to a state 710 and the tile manager 192 marks the undo tile as "not blank" and moves to a state 712 Wherein the tile manager 192 tests whether the document tile has a valid copy of compressed data on the disk.
If a valid copy of compressed data does reside on disk, the tile manager 192 moves to a state 714 and simply copies the compressed tile disk location and size information from the document tile header to the undo tile header. Note that it is possible for a particular tile to have multiple representations of the same data. That is, a compressed version and an expanded version of the tile may exist in cache simultaneously. And a tile may have a compressed version in cache as well as on the disk. For undo, the strategy is to store the most compact version possible. The most compact version with regard to cache memory usage is to have a copy of the compressed tile on the disk.
If there is no compressed copy of the tile on the disk, the tile manager 192 proceeds to a decision state 716 wherein the tile manager 192 determines whether an uncompressed copy of the document tile resides on the disk. If the test succeeds, the tile manager 192 enters a state 718 and copies the uncompressed tile disk location and size information from the document tile to the undo tile and then returns to the inner FOR-loop at a loop state 700.

If there is an error than the tile manager 192 unlocks the document handle at a state 724 and terminates with an error condition at the end state 726. If there was no error in locking the compressed version of the tile then the tile manager 192 moves from the state $\mathbf{7 2 2}$ to a state 728 wherein the tile manager 192 allocates and locks down cache memory for a copy of the compressed data to be associated with the undo header. There is another error possibility at this point and the tile manager 192 checks for an error at a decision state 730. If there is an error then the tile manager 192 returns to a state 724 and thereafter terminates the function 426.

If there was no error in locking cache memory at the state 730, the tile manager 192 moves to a state 732 and copies the compressed data from the document tile to the undo tile. The tile manager 192 actually copies the data that is stored within the tile-i.e., the compressed image data is copied from the document version to the undo version. Then the tile manager 192 moves to a state 734 and unlocks the compressed version of the document tile. Now, at a state 736, the tile manager 192 unlocks the compressed version of the undo tile and the tile manager 192 returns to the inner FOR-loop at state 700 on FIG. 17A where the tile manager 192 loops back to continue the loop for all of the tiles in the affected region.

When the tile manager 192 is done with all of the tiles in the affected region, the tile manager 192 moves to a state 738 where the tile manager 192 links the new undo header into the undo region list. Thus, multiple regions can be saved in the undo list and then in one operation, by calling undo previous raster operation, all of the operations that had been accumulated, can be undone. Then the tile manager 192 moves to a state $\mathbf{7 4 2}$ wherein the tile manager 192 unlocks the document handle and terminates the function 426 normally.

FIG. 18 shows the load tile to raster image function (LoadTiff). FIG. 18 is a flow diagram for the part of LoadTiff that loads tiled images only. In reference to FIG. 18, the overall process may be understood whereby an existing file on the disk, i.e., an image file on disk, is mapped into memory. As described below, the overall process permits loading large images in a short time period relative to how long it would take to actually copy all of the image data into the computer's memory. In accordance with the present invention, the process shown in FIG. 18 is called the indirect loading capability. As shown in FIG. 18, the tile manager 192 begins the LoadTIFF function 408 at a start state 750 and moves to a state 752 where the tile manager 192 opens the input file that is on the disk. If there is an error on the disk, the tile manager 192 prints an error message at a state 754 and terminates at an end state 756. If no error exists, then the tile manager 192 moves to a state 758 and checks for the TIFF header structure that identifies that the input file is in fact a TIFF file. While the disclosure below discusses a TIFF file, it is to be understood that the process shown in FIG. 18 may be per-
formed on all types of tiled files, such as a MIL-R28002A Type II file or an IBM IOCA tiled file.

Still referring to FIG. 18, if the tile manager 192 finds something other than TIFF header structure at state 758, the tile manager 192 moves to state 754 to indicate an error, and then exits at the end state 756. If the tile manager 192 finds a TIFF header structure while at state 758, the tile manager 192 move to a state 760 wherein the tile manager 192 counts the number of subimages in the TIFF file, one or more of which may exist in a TIFF file.

Next, the tile manager 192 moves to a state 762 and reads the full resolution subimage information which constitutes the basic information about the image, e.g., the image width and height, the size of the tiles, the compression format that is used, and the resolution. If the basic image information is not present and in proper form, the tile manager 192 moves to the state 754 to indicate an error. On the other hand, if no error is indicated at state 762, the tile manager 192 moves to state 764, wherein the tile manager 192 creates a skeleton document and locks that document. The skeleton document at this point contains no cache memory but only tile directory and tile headers that represent in a virtual sense the tiles that compose the image.

The tile manager 192 next moves to a state 766 where the TIFF full resolution subimage tile information is loaded into the tile headers for the full resolution subimage, as more fully disclosed below in reference to FIG. 19. Next, the tile manager 192 moves to a loop state 768 where there is a loop for each of the remaining lower resolution subimages. While in this loop, the tile manager 192 accesses a decision state 770, wherein the tile manager 192 determines whether

$$
f r / l r=2^{n}
$$

where
fr is the full resolution subimage resolution in pixels per inch; and
Ir is the particular low resolution subimage resolution in pixels per inch.
If the ratio of fr to lr is a power of two, then a successful test is indicated, and the tile manager 192 moves to a function 424 and loads the TIFF subimage tile information into the tile headers for that particular subimage level. On the other hand, if the ratio of fr to lr is not a power of two, as indicated at the decision state 770, then the tile manager 192 ignores the particular subimage under test and returns to the state 768 until all of the subimages in the file are processed. When all subimages have been processed, the tile manager 192 moves to a state 772 and unlocks the document handle of the newly created document and terminates normally at an end state 756

Now referring to FIG. 19, the function 424 whereby the tile manager 192 loads the TIFF subimage tile information into tile headers is shown. More particularly, the tile manager 192 begins at a start state 780 and moves to a state 782 wherein the tile manager 192 reads the number of tiles in the subimage. Then the tile manager 192 moves to a state 784 wherein the tile manager 192 allocates temporary buffers for the tile mode offset and byte count lists. These three lists have one entry each per tile in the subimage. If the tile manager 192 cannot properly allocate the temporary buffers, then the tile manager 6 192 exits with an error condition at an end state 786.

Upon successful allocation of the buffers, the tile manager 192 moves to a state 788 where the tile man- particular tile is not blank.
In the event that the tile manager determines at state 814 that the tile data is not compressed, the tile manager

192 moves to a decision state 818 where the tile manager 192 checks to see if the data is uncompressed. If the data is uncompressed on the disk, the tile manager 192 stores the file offset byte count information in the uncompressed tile handle in state 820 . From state 818, the tile manager moves to state 828 , wherein the tile manager sets a flag to indicate that the particular tile is not blank.
If the tile manager 192 determines at state 818 that the tile data is not uncompressed, then the tile manager 192 moves to state 822 , wherein the tile manager 192 checks to see whether the tile is all foreground at a state 822. For example, in a black and white drawing engineering document, foreground color is black, so the tile manager 192 treats a foreground as a black tile. If the tile is determined to be a foreground tile, the tile manager 192 proceeds to state 824, wherein the tile manager 192 creates an all foreground tile, and then sets the flag as not blank at state 828. As an example, if the image being processed is a color image, the tile manager 192 could fill the tile with the foreground color at the state 824.
On the other hand, if the tile is not all foreground, the tile manager proceeds to state 826 to determine whether the tile is all background. As discussed above, binary images usually have background pixels which are white or zero value. If a particular tile is blank, the tile manager 192 moves to a state 828 where the tile manager 192 sets the blank flag to indicate that the tile is indeed a blank tile. If at the state 826 the tile manager 192 determines that the tile is not all background, the tile manager 192 terminates with an error at an end state 830. In other words, having determined at state 822 that the particular tile was not all foreground, the only possibility left at state 826 is that the tile is all background. Consequently, a determination at state 826 that the tile is not all background indicates an error
From state 828, the tile manager 192 moves to a state 832 and sets the loaded flag to true indicating that a valid image information set has been associated with the particular tile. The tile manager 192 completes the loop described above for each tile. After having processed each tile in the particular image, the tile manager 192 exits the two FOR-loops and moves to a state 834 where the tile manager 192 unlocks the document handle and then terminates normally at the end state 830 .
Now referring to FIG. 21, the tile manager 192 performs a function which for purposes of the present invention will be termed "Undoable Raster Operation". The function shown in FIG. 21 is performed by the tile master 192 in the function "Begin Undoable Ras-Op", and is a relatively simple function, the purpose of which is to clear the undo region list. More particularly, in the process shown in FIG. 21, the tile manager 192 frees all of the undo regions associated with the previous operation to prepare for a new undo operation. Indeed, the present invention could be configured to have multiple level undo, i.e., the system of the present invention could undo two or three or more operations going into the past and also to be able to redo all of those operations at the user's choice. For example, the last three operations could be undone and then the oldest of those operations redone
In specific reference to FIG. 21, the tile manager 192 begins at a start state 840 and then proceeds to loop state 842, in which the tile manager 192 executes a FOR-loop for each undo region in the current list. The tile manager 192 loops to a state 844 where the tile manager 192 frees all of the memory associated with that undo re-
gion. This may include freeing compressed data that is stored in cache or expanded data that is stored in cache and associated with the undo region. When the tile manager 192 finishes all of the regions, the tile manager 192 terminates at an end state 846.

Now referring to FIGS. 22A and 22B, there is shown the control flow for the ReadRowToRow function 414 which produces one or more rows of scaled image data each time it is performed. It is one of the basic image access functions. It should be understood that the tile manager 192 can also read columns of an image, etc., so as to produce a rotated output

The tile manager 192 enters the function 414 by moving to a start state 850 and proceeds to a decision state 852 where the tile manager 192 checks for a region overrun. In other words, when the access context is created, the region that is going to be read in the course of the overall operation is specified, and in the event that the read row to row subfunction is accessed too many times, the region will be overrun. Any such overrun is detected by the tile manager 192 at state 852 and reported at state 854. In the event of an overrun, the tile manager 192 terminates at an end state 856.

If, on the other hand, no region overrun has occurred, the tile manager 192 moves to a decision state 858 where the tile manager 192 checks to see whether old results are carried over to the new strip. Such a carryover could occur when, for example, raster data is being enlarged by expanding one or more lines from the image. For example, when raster data is being enlarged by $4 \times$, each line of input generates four (4) lines of output. Accordingly, three (3) output rows could be carried over for later strips. With this eventuality in mind, the tile manager 192 ascertains whether any data is being carried over and if so, the tile manager 192 uses the carried-over data before generating a new row Consequently, if there is new data carried over, the tile manager 192 moves to a state 860 where new rows are generated from the carried over data.

Next, the tile manager 192 moves to a state 862 where the tile manager 192 checks to see if a particular strip is full. For purposes of the present invention, a strip is a collection of rows, i.e., a set of numbers arranged in rows As indicated at state 862, if the strip is full, then the tile manager 192 ends at the end state 856.

If the strip is not full and the tile manager 192 has used up all the carried over data, then the tile manager 192 moves to a decision state 864 where the tile manager 192 checks for ghosting, i.e., the skipping of some rows of data in order to produce a low quality image while panning or zooming. If ghosting is in effect, the tile manager 192 moves to state 866 , wherein the tile manager 192 calculates the number of blank lines to create. The system then moves to a state 868 where the tile manager 192 writes the blank lines to the output strip buffer.

From state 864, if no ghosting was detected, or state 868, if ghosting is not in effect, the system moves to state 870 where the tile manager 192 again checks to see if the strip buffer is full. If it is, the tile manager 192 exits at the end state 856. If it is not, the tile manager 192 checks to see that there are still input rows to read in a decision state 872. If there aren't, the tile manager 192 has reached the end of the specified image region, and proceeds to state 874 to obtain another row of output data by flushing the scaler buffers. In accordance with the present invention, in the state 874 the tile manager 192 sets a flag that is subsequently passed down to the
scaler functions to flush intermediate results from the scaler functions. This is the case when for reducing data, i.e., if a plurality of rows is being combined into one output row. That is how the last output row is produced.

From state 874, the system moves to state 894, shown in FIG. 22B. On the other hand, in the event that there are no unread image rows at state 872 , the system moves to decision state 876, where the system determines whether the row is outside of the valid image boundaries. If yes, the system moves to a state 878, where the tile manager 192 substitutes blank lines for the input. The tile manager proceeds from state 878 to a state 894 , shown in FIG. 22B. If the answer to the decision at state 876 is no, the system moves to a decision state 880, shown in FIG. 22B, to check whether the row is contained in the currently locked tile row.

At state 880, the tile manager 192 moves down the image, and the system sequentially passes through successive tile rows. Each tile contains, e.g., 512 rows, so when a particular tile row is locked it stays locked until all 512 image rows in that tile row have been read. Each time the system arrives at a new row it tests to see that the row is contained in the currently locked tile row. If it is not, the system moves to the state 430 (function ExpTileUnlock) to unlock the old tile row and lock down the new tile row (at state 428). In addition, the tile manager 192 has to unpreserve the row of tiles that was just unlocked. Unpreserving them tells the memory manager that those tiles are no longer needed for this access operation and it can do what it wishes with them.

Next, the system proceeds to a decision state 882 to determine whether any tiles are blank. If they are, the tile manager 192 substitutes a reference to a "common blank tile" and that common blank tile is used, as indicated at state 884. All tiles that are blank are mapped onto this common blank tile. Consequently, the tile manager 192 uses less image memory.

From state 884, 882, or 880, as appropriate, tile manager 192 proceeds to a decision state 886 to check for polygonal clipping. If the tile manager 192 is doing polygonal clipping then each input row of data is clipped as appropriate for that polygon in states 888 and 890. The loop allows multiple clipped regions within each row. If there is no clipping, then the tile manager 192 simply copies the entire input row from the image into the input row buffer in a state 892. Then the tile manager 192 move to a state 894 where the tile manager 192 passes these input rows through the scaler if the tile manager 192 is scaling the data. Finally, the tile man- 50 ager 192 takes the results of the scalers and copies that information to the output strip buffer if necessary at a state 896. The tile manager 192 then returns to the state 870 (shown in FIG. 22A) where the tile manager 192 continues the process of retrieving input rows and scaling them until the tile manager 192 has filled the output strip buffer. The system then moves to the termination condition at the end state 856.

Now referring to FIG. 23A, a process which will be referred to as "Write Rows to Region" will be described. The tile manager 192 starts at state 900 and moves to state 902 where the tile manager 192 tests for region overrun. Region overrun can occur when the calling function attempts to write more rows to the image than was specified when the access context was created. If the region was overrun, the tile manager 192 reports an error at state 904 and terminates with an error at state 906. If there is no region overrun, the tile 192 moves to state 930 in FIG. 23B. At state 930, the tile manager 192 determines whether polygonal clipping is activated. If it is, the tile manager 192 computes the clip points for the current image row, as indicated at state 932, which results in a list of clip point pairs.

The tile manager 192 then moves to state 934 , wherein the tile manager 192 conducts a FOR-loop for each of the clip point pairs that the tile manager 192 computed in state 930. As shown in FIG. 23B, the tile manager 192 loops to state 936 where the tile manager 192 copies pixels from a scaler output buffer to the image row between each pair of clip points. When that loop terminates, the tile manager 192 returns to state

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914 in FIG. 22A. On the other hand, if the tile manager determines at state 930 that polygonal clipping is not active, the tile manager 192 moves to state 938, wherein the tile manager 192 copies the scaler output buffer pixels to the image row without clipping. The tile manager 192 then proceeds to state 914.

Now referring to FIG. 24, the tile manager starts at state 950 in the end access function shown in FIG. 24 and proceeds to state 952. At state 952, the system cleans up after row or column access functions by freeing buffers used by the row or column access functions.

Next, at state 954, the tile manager 192 unlocks the last row or column of tiles accessed. Then, the system moves to state 956 where the tile manager 192 unpreserves any tiles in the region that are still preserved. The system may perform the functions at states 954, 956 when an operation was aborted in mid-progress and it cleans up after those partially completed operations.

At state 958, the tile manager 192 cleans up after the polygonal clipping function. If there was polygonal 20 clipping involved in this access context the tile manager 192 has to free the buffers that contain the polygon edge information.

Next, the system moves to state 960 , where the tile manager 192 frees scaler buffers, the temporary tile directory, etc.. From state 960 , the system moves to state 962 , wherein the tile manager 192 unlocks the document handle to indicate to the memory manager that the access context no longer is referring to the particular document associated with the document han- 30 dle.

The tile manager 192 next moves to state 964 where the memory that was used to store the data for the access context is freed. Then, the system ends the clean up function at state 966 .

Referring now to FIGS. 25A,B, a function is shown which, for purposes of the present invention, will be termed the "Undo Previous Raster Operations". The tile manager 192 starts at state 970 and moves to state 972, wherein the tile manager determines whether any undo regions exist in the list or if the list is empty. If no regions exist then the tile manager 192 moves to end state 974 and terminates normally.

If the tile manager 192 determines at state 972 that "undo" regions do exist, the tile manager 192 moves to 4 state 976, where the tile manager 192 enters a loop for each undo region in the list. In this loop, the tile manager 192 moves to state 978 where the tile manager 192 locks the affected document handle. The document handle that is locked is the one that was stored in the undo region header that tells where that particular undo region came from. The tile manager 192 moves from state 978 to state 980 where the tile manager 192 saves the current document region to support redo (i.e. an "undo" operation following by another "undo" operation). Then the tile manager 192 moves to state 982 to invalidate the affected tiles in the lower-resolution subimages. The strategy represented by states 980,982 in FIG. 25A is to save the minimum amount of information that is needed to reconstruct the image, which 60 means the tile manager 192 saves only the affected tiles in the full res subimage.

Next, the system moves to a loop indicated by the states 984, 986. In this loop, for each tile, the tile manager 192 moves to state 988 , discarding the document tile image data. Then the tile manager 192 moves to state $\mathbf{9 9 0}$ to determine whether the undo tile is loaded. If it is not loaded, the tile manager 192 moves to state 992

For each tile in the specified region, the system moves to state 1046, wherein the tile manager 192 determines whether the particular tile is blank. To make this determination, the system examines flags in the tile header itself or checks the image data for that tile to determine if there are any non-background pixels. If it is not a blank tile, the tile manager 192 move to state 434 where the tile manager 192 locks the uncompressed version of the tile. Then the tile manager 192 proceeds to state 1050, wherein the tile manager 192 determines whether an error had occurred in the process of creating the uncompressed version of the tile. If no error is found at state 1050, the tile manager 192 continues to loop to the next tile in the region by returning to state 1044. If an error did occur, as determined at state 1050, the system proceeds to state $\mathbf{4 3 0}$ to unlock previously locked tiles, and then ends at state 1056.

In the event that the tile manager 192 at state 1046 detected that the particular tile was a virtual blank tile, i.e., a tile that exists only by virtue of the fact that there is a tile directory entry for that tile, the tile manager 192 take no action, other than to loop back to state 1044 for further processing.

FIG. 28 illustrates the control flow for the "lock expanded tile" function 434 wherein the tile manager 2 192 takes a single tile and locks the expanded version of the tile in the image data cache 194. The tile manager 192 enters the function 434 at a start state 1060 , and proceeds to a decision state 1062 wherein the tile manager 192 tests whether the tile is marked as "loaded". As already mentioned, a loaded tile is one that either contains or references valid image data, is either uncompressed or compressed image data, and it either resides in cache memory or on the disk. If the tile is not loaded, the tile manager 192 moves to a function 436 wherein the tile must be created from higher resolution tiles which are loaded. Afterwards, the tile manager 192 determines if there was an error in a decision state 1066. If there was an error, the tile manager 192 terminates the function 434 at an end state 1068 and reports the error condition. Otherwise, if there was no error in creating the tile, the tile manager 192 continues, moving from the state $\mathbf{1 0 6 6}$ to a decision state 1070.

The tile to be locked is now loaded so the tile manager 192 tests whether the uncompressed version of the tile is in cache memory. The objective of the function 434 is to guarantee that there is an uncompressed version of the tile in cache memory. Now, if the uncompressed version is not in the cache, the tile manager 192 proceeds to a decision state 1072 to determine whether the selected tile is a blank tile.

If the tile is blank, the tile manager 192 proceeds to a state 438 to create a blank tile. Note here that the function ExpTileLock 428 (FIG. 27) will detect a blank tile before calling the function 434 if it can take advantage of using a common blank tile at a higher level. In other words, if the tiles are locked for reading only, i.e., the image data will not be modified in any way, then all blank tiles can refer to the same section of blank memory. However, if the tiles are locked for writing, all tiles must have their own memory because different image data can be written to the different tiles.

At this point, state 438, memory has presumably been allocated for a blank tile. Moving to a state 1074, the tile manager 192 tests whether there was an error and 6 moves to the end state 1068 if there was an error.

Returning in the discussion to the decision state 1072, if the tile is not blank, then the tile manager 192 transi- expanded version in cache, which at this point is locked. Then the tile manager 192 continues to a state 1092 to move the newly locked, expanded ver-
sion of the tile to the front of the "most recently used (MRU)" list of uncompressed tiles.

The MRU list is a doubly-linked list wherein, starting at the beginning, the tile is found that was most recently used, then the next most recently used, and so on, the last tile was used the longest time ago. That list is used by the cache manager to determine which tiles are least likely to be used again as a second level of criteria.
Finally, the tile manager 192 terminates the LockExpHandle at the end state 1068.
FIG. 29 illustrates the control flow for the "unlocking expanded image tile group" function 430 . The function 430 is just the reverse of lock expanded image tile group. In other words, there is a region of locked tiles which must be unlocked because the access to the tiles is complete. Generally, the two functions, ExpTileLock and ExpTileUnlock are called for a row or column of image data rather than a region but an entire region lock/unlock is possible.

The tile manager 192 enters the function 430 at a start state 1110. The loop states 1102 and 1104 represent the beginning of nested FOR-loops. That is, the outer loop, beginning at the state 1102 , unlocks a row of tiles, and the inner loop, beginning at the state 1104 unlocks a column of tiles. Moving from the state 1102, to the state 1104, and then to the function 432, the tile manager 192 unlocks the uncompressed version of the tile. When all the tiles in the region are unlocked, the tile manager 192 terminates the function 430 at an end state 1108.
Now referring to FIG. 30, the tile manager 192 enters the UnlockExpHandle function 432, referred to in FIG. 29, at a start state 1110. The tile manager 192 proceeds to a decision state 1112 to test whether the uncompressed version of the currently selected tile is in fact locked, i.e., whether the lock count is non-zero. If the tile is not locked, the tile manager 192 exits the function 432 at an end state 1114.
If, at the state 1112, the tile is found to be locked, the tile manager 192 moves to a state 1116 to decrement the lock count. Thereafter, the execution continues to a decision state 1118 wherein the tile manager 192 tests whether the "update overview" flag is set true. If the flag is set, the tile manager 192 moves to a state $\mathbf{1 1 2 0}$ to update the corresponding lower-resolution tiles. In the process of modifying tiles, the tile manager 192 locks a tile down in the image data cache to write to it. When the tile is unlocked, that is a signal to the memory manager to update the lower resolution tiles that correspond to the higher resolution tile. Thus, the image data in the high resolution tile being unlocked is copied down into the lower resolution tiles, all the way down to the bottom of the image stack.

Once the lower resolution images are modified, or if the overviews are not being updated, the tile manager 192 proceeds to a decision state 1122 to test whether the lock count is exactly zero. If the lock count is not zero, the tile manager 192 terminates the function 432 at the end state 1114.
Otherwise, the tile manager 192 moves to a state 1124 to clear the "cache collection delay" flag. The cache collection delay flag is set by the tile manager after unsuccessfully trying to reduce the expanded memory usage of the cache file. It is cleared in the function 432 because there is now the possibility of freeing the tile that was just unlocked. In other words, the tile can be removed from the cache to create some space. This flag prevents the tile manager or the cache manager from making repeated, unsuccessful attempts to create space. the preferred resolution step between subimage levels is two in the presently preferred embodiment. Thus, since there are two dimensions, four higher-resolution tiles are required to produce each next lower resolution tile.

Thereafter, the tile manager 192 enters a FOR-loop at a loop state 1152. For each of the four higher-resolution tiles, the tile manager 192 tests whether the tile is loaded in the image data cache, at a decision state 1154. If the tile is not loaded, then the tile manager 192 moves to a state 1156 wherein a recursive call is made to the "load subimage tile" function to create the corresponding higher-resolution tile from yet higher-resolution tiles. This case occurs if a the tile is a few layers down in the image stack and the tiles in all but the full resolution subimage had been invalidated. Therefore, the function 436 invokes itself to work all the way back up to the top level, recreate the higher-resolution tiles and then work back down to the tile of interest. Only higher-resolution tiles that map to the particular lower-resolution tile need be loaded

Assuming that all the higher-resolution tiles have been loaded, the FOR-loop terminates and the tile manager 192 proceeds to test whether all of the higher-resolution tiles are blank. If all four of the high resolution tiles mapped to this low resolution are blank, the tile manager 192 transitions to a state 1160 to mark the low resolution tile as blank. The tile manager 192 does not create any image data for the blank, lower-resolution tile. The tile manager 192 and terminates the function 436 at the end state 1144.

If, however, one or more of the higher-resolution tiles is not blank, the tile manager 192 moves to a state 1162 to make a determination as to whether it is faster to create the lower-resolution tile by scaling the com-
pressed version of the higher-resolution tiles or the expanded version of the higher-resolution tiles. An algorithm is used at the state 1162 to decide which is faster and depends on the machine that the program is running on, and other considerations. If it is faster to scale the compressed data the tile manager 192 moves to the function 442 to create the compressed, lower-resolution tile directly from the compressed higher-resolution tiles.

Now, if it is determined that it is faster to scale the expanded version of the data, the tile manager 192 moves from the state 1162 to a state 1166 to allocate memory for the uncompressed version of the lowerresolution tile. From the state 1166, the tile manager 192 moves to the beginning of a FOR-loop at a loop state 1168 wherein for each of the higher-resolution tiles the tile manager 192 scales the expanded version of the higher-resolution tile directly into the proper position in the lower-resolution tile using the function 444. When the tile manager 192 has scaled each of the four high 20 resolution tiles, the tile manager 192 has completed the creation of the expanded version of the low resolution tile.
The tile manager 192 then proceeds, from either of the states 1168 or $\mathbf{4 4 2}$ to a decision state 256 wherein the tile manager 192 determines if an error was incurred in that process. If there was an error, the tile manager 192 moves to a state 1172 to report the error. From either of the states $\mathbf{1 1 7 0}$ (if no error) or 1172, the tile manager terminates the function 436 at the end state 1144.

FIG. 32 contains the flow diagram for the "allocate space for uncompressed version of tile" function 438 referred to in FIG. 28. The tile manager 192 enters the function 438 at a start state 1180 and moves to a decision state 1182 to test whether the "soft" uncompressed cache usage limit is exceeded. The soft uncompressed cache limit is a number that is cast into the tile manager 192 during initialization and it basically sets a guideline for how much of the image data cache is to be devoted to uncompressed image data. If the cache manager gets a request for uncompressed cache space and finds that this soft limit has been exceeded, it attempts to reduce the amount of expanded image data that is held in cache either by compressing expanded tiles or by discarding expanded tiles that have valid compressed versions or some other way to recreate them.

If the tile manager 192 finds that the soft limit is exceeded, the tile manager 192 moves to a state 1184 to first check whether the "cache collection delay" flag is set. This flag is set after an unsuccessful attempt to reduce cache memory usage and prevents repeated unsuccessful calls to collect free cache at a state 1186.

Thus, the tile manager 192 will not try to reduce the expanded memory usage until the flag is cleared in the "unlock expanded tile handle" function 432 (FIG. 30).

If the cache collection delay flag is not set, the tile manager moves to a state 1186 to collect free cache memory by freeing uncompressed tiles. After that, the tile manager 192 moves to a decision state 1188 to test whether the soft uncompressed cache usage limit is still exceeded after an attempt to reduce the memory usage. If the usage is still exceeded, the tile manager 192 prints a warning message on the video display 154 (FIG. 6) at a state 1190 and then sets the cache collection delay flag at a state 1192.

Returning in the discussion to the state 1182, if the soft limit was not exceeded, or if it was not exceeded at the state 1188, the tile manager 192 moves to a decision state 1224, the tile manager 192 moves to state 1228 to terminate the process.

From state $\mathbf{1 2 2 6}$, if compressed data was successfully loaded from the disk or from state 1222 if it was in cache
to begin with, the tile manager 192 moves to state $\mathbf{1 2 3 0}$, wherein the tile manager 192 locks the compressed tile image data. This step simply increments the lock count on the compressed memory state. From state 1230, the system moves to state 1232, wherein the tile manager 192 allocates and locks the uncompressed tile memory block. The system then moves to state 1234 to determine whether an error occurred at state 1232. If so, the tile manager 192 moves to state 1236 and unlocks the compressed tile data. From state 1236, the system moves to state 1238 to report the error. The system then terminates at end state 1228.
On the other hand, if no error existed as determined at state 1234, the system moves to state 1240 , wherein the tile manager 192 uncompresses the compressed data. Next, the tile manager 192 moves to state 1242 to determine whether an error occurred at state $\mathbf{1 2 4 0}$. If an error occurred at state 1240, the tile manager 192 moves to state 1236 and functions as described previously. Otherwise, the tile manager 192 moves to stat 1244 to unlock the compressed and uncompressed data, and then terminates at end state 1228.
FIG. 34 illustrates a process for creating compressed low resolution tiles from compressed higher resolution tiles. The tile manager 192 starts at start state 1250 and proceeds to state 1252, wherein the system enters a loop which is followed by the system for each of the four high resolution tiles required to produce a single low resolution tile. More specifically, at state $\mathbf{1 2 5 2}$ the tile manager 192 locks the compressed version of the high resolution tile. The system then proceeds to state 1256, wherein the tile manager 192 determines whether an error occurred at state 1254. In the event that an error occurred, the tile manager proceeds to end state 1258 and terminates. If no error occurred, the tile manager 192 returns to state 1252 and continues the loop described above for each of the four high resolution tiles.

After processing all four high resolution tiles as described, the system proceeds to state 1260 where the tile manager 192 scales the compressed data to half resolution. The process performed at state 1260 results in a compressed version of the low resolution tile. Then the tile manager 192 moves to a loop represented by states 1262, 1264, wherein for each of the high resolution tiles the tile manage 192 unlocks the compressed version of the tile.
Next, the tile manager 192 moves to state 1266 where the tile manager 192 allocates and locks memory for the compressed version of the low resolution tile. At state 1266, the tile manager 192 actually puts the compressed version of the low resolution tile in a general, common buffer that is large enough to hold the maximum possible size of the compressed results. The actual valid data is usually much less than that than the maximum possible size, so the tile manager 192 only saves the valid amount of data.
From state 1266, the system moves to state 1268 to determine whether an error occurred at state 1266. If an error occurred, the system moves to end state 1258 and terminates. Otherwise, the system moves to state 1270 where the tile manager 192 copies the compressed data out of the temporary compressed data buffer into the newly allocated space in the cache. Then the tile manager 192 moves to state 1272 where the tile manager 192 unlocks the compressed version of the low resolution tile that now contains valid data. The system then terminates normally at state 1258 .

Now referring to FIG. 35, a process is shown whereby the system resamples uncompressed high resolution tiles to an uncompressed low resolution tile. The tile manager 192 starts at start state 1280 and moves to 5 state 1282, wherein the tile manager 192 locks the uncompressed version of a single high resolution tile. This function scales a single high resolution tile to update one quarter of a tile in the half-resolution subimage. That quarter tile is rescaled to update one-sixteenth of a 10 tile in the quarter-resolution subimage. This continues to the lowest resolution subimage. Next, the tile manager 192 proceeds to state $\mathbf{1 2 8 4}$ to determine whether an error occurred in locking the uncompressed version of the high resolution tile. If there Was an error, then the tile manager 192 proceeds to state 1286 and terminates with an error condition. Otherwise, the tile manager 192 moves to state 1288 where the tile manager 192 determines how many levels of the subimage are to be updated. This function can be used to update a subset of subimages or the entire image stack in the case where a single tile is modified in the full resolution subimage. It will propagate that change all the way down to the lowest-resolution subimage in the image stack.

Next, the tile manager 192 proceeds to state 1290 where the tile manage 192 determines the tile index that is to be updated. In accordance with the present invention, when a change is propagated from the higher resolution down to the low resolution of tiles, the system calculates which tile corresponds to the affected area. Then the tile manager 192 moves to state 1290 where the tile manager 192 determines whether the low resolution tile that the tile manager 192 is about to update is marked as loaded or not. This step is intended for the situation in which not all of the low resolution substates are populated during the loading of a raster image.

If the system determines that one or more low resolution tiles are not loaded, the system proceeds to state 1294, wherein the tile manager 192 invalidates all of the the change. The system then exits normally at end state 1286. If the low resolution tile is about to be modified is loaded, as determined at state 1292, the tile manager 192 moves to state 1296, wherein the system locks the uncompressed version of the low resolution tile. The tile manager 192 then moves to state 1298 to determine whether an error occurred at state 1296 and, if so, the system moves to end state 1286 to terminate. Otherwise, the system moves to state 1300 . wherein the tile manager 192 scales the raster data from the high resolution tile down to the low resolution tile. Then the tile manager 192 moves to state 1302 where the tile manager 192 unlocks the high resolution tile.

Next, the system moves to state 1304, wherein the tile manager 192 recursively modifies the loop variables such that the low resolution tiles that the tile manager 192 just finished updating become the high resolution tiles for the next succeeding iteration. Once all the subimages have been updated as described, the system 0 exits at end state 1286.

Now referring to FIGS. 36A and 36B, a process to collect free cache is shown. This process can be called from several other processes. The tile manager 192 begins at start state 1310 in FIG. 36A and moves to state 1312 to determine whether a cache collection operation is in process. If so, the system exits at end state 1314. This prevents recursive calls to collect free cache which might otherwise occur. If the system at state

1312 determines that no collection is in progress, then the tile manager 192 moves to state 1316 where the tile manager 192 sets a flag indicating that a collection is in progress.
From state 1316, the system moves to state 1320 , where the tile manager 192 estimates the number of memory blocks to free in this operation. The reason for freeing a number of blocks instead of just one block is to reduce the computational overhead associated with the cache collection operations. The tile manager 192 typically estimates the amount of memory required to equal the number of tiles in a single row of the full resolution subimage of the document associated with the most recently used tile.
Once this estimate has been made, the system proceeds to state 1322 wherein the tile manager 192 considers the options that the tile manager 192 passed into this function. There are three options. One, as indicated at state 1324, is to reduce the uncompressed cache usage only while not affecting the compressed data that is currently held in cache. The second option, indicated at state 1328, is to reduce the compressed cache memory usage only. The third option, indicated at state 1326, is to reduce the total cache memory usage including both compressed and uncompressed data.

From state 1324 or state 1326, the tile manager 192 moves to state 1330, where the tile manager 192 stores all of the free states currently in the uncompressed free list into the cache reserve list. As the tile manager 192 performs the process in state 1330, the tile manager 192 attempts to consolidate the memory blocks. That is, if there are two free blocks that are adjacent to one another, the system automatically turns them into a single, larger contiguous block. From state 1328, on the other hand, the system moves to state 1358, shown in FIG. 36B and discussed below.
From state 1330, the tile manager 192 moves to state 1332, wherein the tile manager 192 determines whether the tile manager 192 has created a memory block large enough to satisfy the initial request. If so, the tile manager 192 terminates normally at end state 1314. Otherwise, the tile manager 192 moves to state 1334 where the tile manager 192 frees any unlocked, uncompressed tiles which are blank. The tile manager 192 then moves to state 1336 where the tile manager 192 determines whether the tile manager 192 has free sufficient memory. If so, the tile manager 192 exits at end state 1314. Otherwise, the tile manager 192 moves to state 1338 where the tile manager 192 frees unlocked, unpreserved uncompressed tiles that have valid compressed versions in cache or are on a disk, or that have valid, uncompressed versions on the disk beginning with the least recently used tile. After having freed that particular class of tiles, if the tile manager 192 determines, at state 1340, that the memory request has been satisfied, the tile manager 192 moves to state 1314 and terminates. Otherwise, the tile manager 192 moves to state 1342 , shown in FIG. 36B.

Now referring to FIG. 36B, the tile manager 192 begins at state 1342, wherein the tile manager 192 compresses the free unlocked, unpreserved uncompressed tiles that don't have a valid compressed version or other source from which the tile can be recreated. To do this the tile manager 192 processes expanded tile data through a compression algorithm. The tile manager 192 then creates a compressed version of that tile so that the uncompressed version of the tile can be discarded.

Next, the tile manager 192 moves to state 1344 wherein the system determines whether the request made at state 1342 has been satisfied. If so, the system terminates at end state 1346. Otherwise, the system moves to state 1348, wherein the tile manager 192 frees unlocked, but preserved uncompressed tiles that have valid compressed or uncompressed copies. The tile manager 192 preferentially frees the oldest such tiles.
From the state 1348, the tile manager 192 proceeds to a decision state 1350 to test whether the request made at the state 1348 was satisfied. If so, the function 446 is terminated at the end state 1346. Otherwise, the tile manager 192 moves to a state 1352 to compress and then free unlocked, but preserved, uncompressed tiles that do not have valid compressed versions.

Next, the tile manager 192 moves to state 1354, wherein the system determines whether the request made at state 1352 has been satisfied. If so, the system terminates at end state 1346. Otherwise, the system moves to state 1356, wherein the tile manager 192 determines whether to free data memory blocks. If not, the system terminates at state 1346 . Otherwise, the system moves to state 1358, to free unlocked preserved, uncompressed tiles that don't have valid compressed versions 5 already.

The system next moves to state $\mathbf{1 3 6 0}$ to determine whether the request has been satisfied. If so, the system terminates at state 1346. Otherwise, the system moves to state 1362 to print an error message, and then terminate at state 1346.

Now referring to FIG. 37, the tile manager 192 starts at state 1380 and moves to state 1382 where the tile manager 192 determines whether the uncompressed version is in fact still locked-that is if the lock count 5 for uncompressed version of that tile is non-zero. If the tile is still locked then the tile manager 192 moves to state 1384 and prints a warning message. Then the tile manager 192 terminates at end state 1386.

If, at state 1382, the system determined that the un0 compressed version is not locked, then the tile manager 192 moves to state 1388 where the tile manager 192 determines whether the uncompressed data has already been freed. If it has then the tile manager 192 terminates at end state 1386. Otherwise, the tile manager 192 moves to state 1390 where the tile manager 192 unlinks the uncompressed memory state from the most recently used list.

From state 1390 , the tile manager 192 moves to state 1392 where the tile manager 192 updates and decre0 ments the total uncompressed memory usage counter by the appropriate amount. The tile manager 192 then moves to state 1394 where the tile manager 192 moves the memory block to the uncompressed memory free list. In accordance with the present invention, the tile manager 192 keeps the list sorted by decreasing address. Consequently, when the tile manager 192 allocates expanded memory blocks, the tile manager 192 tends to choose the preferred blocks that have higher addresses because they are at the front of the free list.
Next, the tile manager 192 moves to state 1396, wherein the tile manager 192 sets a pointer in the tile header to null and the tile manager 192 sets the uncompressed tile status flags. This ensures that the tile header reflects the fact that it no longer has an uncompressed 5 data associated with it. Then the tile manager 192 terminates at end state 1386.

Now referring to FIG. 38, a process by which the system compresses a tile is shown. The system begins at
start state 1400 , and moves to state 1402 , wherein the tile manager 192 determines whether the uncompressed tile data is in cache memory. If it is not, the tile manager 192 moves to state 1404 and loads the uncompressed data into cache memory from the disk. The system then moves to state 1406, to determine whether an error occurred at state 1404. If so, the system terminates at end state 1408. Otherwise, the system proceeds to state 1410.

At state 1410, the tile manager 192 locks the uncompressed tile data, and then moves to state 1412, to determine whether an error occurred at state 1410. If an error occurred, the system terminates at end state 1408. Otherwise, the system moves to state 1414, wherein the tile manager 192 compresses the image data into a common buffer. For binary images of text and line drawings, the tile manager 192 uses a CCITT group 4 encoding.
From state 1414, the tile manager 192 moves to state 1416 to determine whether an error occurred at state 1414. If an error indeed occurred, the system moves to state 1418 to unlock the uncompressed tiles, and then exits at end state 1408. Otherwise, the system proceeds to state 1420, wherein the tile manager 192 allocates and locks cache memory space for the compressed tile data.

From state 1420, the system proceeds to state 1422 to determine whether an error occurred at state 1420 . If an error occurred, the system moves to state 1418 and proceeds as described above. Otherwise, the system moves to state 1424, wherein the tile manager 192 copies the compressed data from the common buffer into the newly allocated cache memory state. The system moves from state 1424 to state 1426; wherein the tile manager 192 unlocks the compressed and uncompressed tile data and then terminates at end state 1408.

While the above detailed description has shown, described and pointed out the fundamental novel features of the invention as applied to various embodiments, it will be understood that various omissions and substitutions and changes in the form and details of the device illustrated may be made by those skilled in the art, without departing from the spirit of the invention.

What is claimed is:

1. An image memory management system, comprising:
a computer having a processor and an image memory, the image memory comprising a main memory and a secondary memory;
an image stack, located in the image memory, comprising a plurality of similar digital images, each digital image having a plurality of pixels grouped into at least one tile, and each digital image having a resolution different from the other digital images;
means for accessing a selected one of the tiles in the image stack;
first means for transferring a selected one of the tiles from the secondary memory to the main memory when the tile is accessed by the accessing means and the tile is absent from the main memory; and
second means for transferring a selected one of the tiles from the main memory to the secondary memory when the main memory is full.
2. The system defined in claim 1, additionally comprising means for modifying a selected one of the tiles.
3. The system defined in claim 2 , wherein the second transferring means only transfer tiles that have been modified by the modifying means.
4. The system defined in claim 1, wherein the main 5 memory is semiconductor memory.
5. The system defined in claim 1 , wherein the secondary memory is a magnetic disk.
6. The system defined in claim 1, wherein each tile is square.
7. The system defined in claim 1, wherein a lowest resolution digital image comprises one tile.
8. The system defined in claim 1, wherein a preselected digital image in the image stack is resampled to obtain another digital image in the image stack.
9. The system defined in claim 1, wherein at least one of the digital images is compressed.
10. The system defined in claim 1 , wherein the accessing means is responsive to an image access operation selected by a user.
11. The system defined in claim 10 , wherein the image access operation is zooming or panning the image.
12. The system defined in claim 10, wherein the image access operation is reversible.
13. A method of managing images in a computer having a processor and an image memory comprising a slower access memory and a faster access memory, comprising the steps of:
creating a digital image;
resampling the digital image so as to form an image stack comprising the digital image and one or more lower resolution digital images;
dividing each image into equal sized, rectangular tiles; and
evaluating a location in the image memory of tiles in each digital image of the image stack in a given region of interest.
14. The method defined in claim 13, additionally comprising updating modified regions of all images when an edit operation is completed.
15. The method defined in claim 13, wherein the evaluating step includes the following order of decreasing availability:
exists in the faster access memory in uncompressed form;
exists in the slower access memory in uncompressed form;
exists in the faster access memory in compressed form;
exists in the slower access memory in compressed form; and
must be constructed from higher resolution tiles.
16. The method defined in claim 13, wherein the evaluating step includes the following order of decreasing availability:
exists in the faster access memory in uncompressed form;
exists in the slower access memory in uncompressed form;
exists in the slower access memory in compressed form; and
must be constructed from higher resolution tiles.
17. The method defined in claim 13, wherein the evaluating step includes selecting the digital image with
the lowest resolution higher than a requested resolution at a given view scale.


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"Equal-Area Projections for World Statistical Maps",

McBryde and Thomas, U.S. Dept. of Commerce, Coast and Geodetic Survey, Spec. Pub. 245, 1949.
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Primary Examiner-Jerry Smith
Assistant Examiner-Kim T. Bui
Attorney, Agent, or Firm-Sughrue, Mion, Zinn, Macpeak \& Seas

## [57] ABSTRACT

A global mapping system which organizes mapping data into a hierarchy of successive magnitudes or levels for presentation of the mapping data with variable resolution, starting from a first or highest magnitude with lowest resolution and progressing to a last or lowest magnitude with highest resolution. The idea of this hierarchical structure can be likened to a pyramid with fewer stones or "tiles" at the top, and where each successive descending horizontal level or magnitude contains four times as many "tiles" as the level or magnitude directly above it. The top or first level of the pyramid contains 4 tiles, the second levle contains 16 tiles, the third contains 64 tiles and so on, such that the base of a 16 magnitude or level pyramid would contain 4 to the 16 th power or $4,294,967,296$ tiles. This total includes "hyperspace" which is later clipped or ignored. Digital data corresponding to each of the separate data base tiles is stored in the database under a unique filename.

33 Claims, 9 Drawing Sheets



FIG. 2

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FIG.3A


FIG. 3 C


FIG. $3 E$


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FIG.3B


FIG. 30


FIG. 3 F


FIG. 4


FIG.5A
FIG.58


FIG. 6


FIG 7


FIG. 8



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FIG. I9


FIG. 20
ILLUSTRATION OF POLAR COMPRESSION AT THE 8th MAGNITUDE


# APPENDIX D 

## ELECTRONIC GLOBAL MAP GENERATING SYSTEM

## BACKGROUND OF THE INVENTION

## 1. Technical Field

This invention relates to a new variable resolution global map generating system for structuring digital mapping data in a new data base structure. managing and controlling the digital mapping data according to new mapping data access strategies, and displaying the mapping data in a new map projection of the earth.

## 2. Background Art

Numerous approaches have been forwarded to provide improved geographical maps, for example:
U.S. Pat. No. 4,315,747, issued to McBryde on Feb. 16, 1982, describes a new map "projection" and intersecting array of coordinate lines known as the "graticule", which is a composite of two previously known forms of projection. In particular, the equatorial portions of the world are represented by a fusiform equal area projection in which the meridian curves, if extended, would meet at points at the respective poles, referred to as "pointed poles". In contrast, the polar regions of the world map are represented by a flat polar equal area projection in which the poles are depicted as straight horizontal lines with the meridians intersecting along its length. Thus, in a flat polar projection the meridian curves converge toward the poles but do not meet at a point and, instead, intersect a horizontal linear pole. The two component portions of the flat world map are joined where the parallels are of equal length. The composite is said to be "homolinear" because all of the meridian curves are similar curves, for exampie, sine, cosine or tangent curves, which merge where the two forms of projection are joined where the respective parallels are equal. The flat polar projections in the polar portions of the map provide a compromise with the Mercator cylinder projections, thereby greatly reducing distortion.
U.S. Pat. No. 1,050,596, issued to Bacon on Jan. 14, 1913, describes another composite projection for world maps and charts which uses a Mercator or cylindrical projection for the central latitudes of the earth and a convergent projection at the respective poles. In the central latitudes, the grids of the Mercator projection net or graticule are rectangular. In the polar regions, the converging meridians may be either straight or curved.
U.S. Pat. No $1,620,413$, issued to Balch on Dec. 14, 1926, discusses gnomic projections from a conformal sphere to a tangent plane and Mercator or cylindrical projections from the conformal sphere to a tangent cylinder. Balch is concerned with taking into account the non-spherical shape of the earth, and therefore, devises the so-called "conformal sphere" which represents the coordinates from the earth whose shape is actually that of a spheroid or ellipsoid of revolution, without material distortion.
U.S. Pat. No. 752,957, issued to Colas on Feb. 23, 1904, describes a map projection in which a map of the entire world is plotted or transcribed on an oval constructed from two adjacent side by side circles with arcs joining the two circles. The meridians are smooth curves equally spaced at the equator, while the latitude lines are non-parallel curves.
U.S. Pat. No. 400,642 issued to Beaumont on Apr. 2, 1889, describes a map of the earth on two intersecting
spheres, on which the coordinate lines of latitude and longitude are all arcs of circles.
U.S. Pat. No. 751,226, issued to Grinten on Feb. 2, 1904, represents the whole world upon the plane sur5 face of a single circle with twice the diameter of the corresponding globe, the circle being delineated by a graticule of coordinates of latitude and longitude which are also arcs of circles.
U.S. Pat. No. 3,248,806, issued to Schrader on May 3, 0 1966, discloses a subdivision of the earth into a system of pivotally mounted flat maps, each map segment representing only a portion of the earth's surface in spherical projection on an equilateral spherical triangle to minimize distortion.
U.S. Pat. No. 2,094,543, issued to Lackey et al on Sept. 28, 1937, describes a projector for optically producing a variety of different map projections, including orthographic, stereographic and globular projections onto flat translucent screens and a variety of other projections on shaped screens.
U.S. Pat. No. 2,650,517, issued to Falk on Sept. 1, 1953, describes a photographic method for making geographical maps.
U.S. Pat. No. 2,354,785, issued to Rohl on Aug. 1, 1944, discloses two circular maps which are mounted side by side, and an arrangement for rotating the two maps in unison so that corresponding portions of the earth's surface are at all times in proper relationship.
U.S. Pat. No. 3,724,079, issued to Jasperson et al on Apr. 3, 1973, discloses a navigational chart display device which is adapted to display a portion of a map and enable a pilot to fix his position, to plot courses and to measure distances.
U.S. Pat. No. 2,431,847 issued to Van Dusen on Dec. 2, 1947, discloses a projection arrangement, in which a portion of the surface of a spherical or curved map may be projected in exact scale and in exact proportional relationship.
McBryde and Thomas, Equal Area Projections for World Statistical Maps, Special Publication No. 245, Coast \& Geodetic Survey 1949.

In addition to the above further teachings as to geographical mapping can be found in the Elements of Cartooraphy, 4th edition which was written by Arthur Robinson, Randall Sale and Joel Morrison, and published by John Wiley \& Sons (1978).

The present invention seeks to provide a low cost and efficient mapping system which allows the quick and easy manipulation of and access to an extraordinary amount of mapping information, i.e., a mapping system which allows a user to quickly and easily access a detailed map of any geographical area of the world.

Map information can be stored using at least three different approaches, i.e., paper, analog storage and digital storage, each approach having its own advantages and disadvantages as detailed below.

The paper mapping approach has been around since papyrus and will probably exist for the next thousand 60 years.

Advantages of paper storage:
inexpensive.
once printed, no further processing is required to access the map information, so not subject to processing breakdown.

Disadvantages of paper storage:
can become bulky and unwieldy when dealing with a large geographical area, or a large amount of maps.
paper does not have the processing capabilities or "intelligence" of computers, and therefore does not support automated search or data processing capabilities.
cannot be updated cheaply and easily.
The analog mapping approach is used to provide what is commonly known as videodisc maps. The information is stored as still frames under N.T.S.C. (National Television Standards Committee) conventions. To make maps, a television camera moves across a paper map lying on a workbench. Every few inches a frame is recorded on videotape. After one row of the map is completely recorded, the camera is moved down to the next row of frames to be recorded. This process is repeated until frames representing a checkerboard pattern of the entire map are recorded. The recorded videotape could be used to view the map: however, access time to scan to different areas of the recorded map is usually excessive. As a result, a videodisc, with its quicker access time, is typically used as the medium for analog map storage. The recorded videotape is sent to a production house which "stamps" out 8 inch or 12 inch diameter, videodiscs.

Advantages of the analog storage approach:
one side of a 12 inch videodisc can hold 54.000 "frames" of a paper map. A frame is typically equal to $2 \frac{1}{2} \times 3$ inches of the paper map.
access time to any frame can be fast usually under 5 seconds.
once located on the videodisc, the recorded analog map information will be used to control the raster scan of a monitor and to produce a reproduction of the map in $1 / 30$ th of a second.
through additional hardware and software, mapping symbols, text and/or patterhsn can be overlaid on top of the recorded frame.

Disadvantages of the analog storage approach:
the "frames" are photographed from paper maps, which, as mentioned above, cannot be updated cheaply or easily.
due to paper map projections, mechanical camera movements, lens distortions and analog recording electronics, the videodisc image which is reproduced is not as accurate as the original paper map.
as a result of the immediately above phenomena, latitude and longitude information which is extracted from the reproduced image cannot be fully trusted.
if a major error is made in recording any one of the 54,000 frames, it usually requires redoing and re-stamping.
since frames cannot be scrolled, most implementations employ a $50 \%$ overlap technique. This allows the viewer to jump around the database with a degree of visual continuity: however, this is at a sacrifice of storage capacity. If the frame originally covered $2 \frac{1}{2} \times 3$ inches or approximately 8 square inches of the paper map, the redundant overlap information is 6 square inches, leaving only 2 square inches of new information in the centroid of each frame.
as a result of the immediately above deficiency, a $2 \times 3$ foot map containing 864 square inches would require 432 frames; thus, only 125 paper maps could be stored on one side of a 12 inch videodisc.
must take hundreds of video screen dumps to make a hard copy of a map area of interest and, even then, the screens do not immediately splice together because of the overlap areas.
the biggest disadvantage is that, since frames have to be arranged in a checkerboard fashion, there is no way to jump in directions other that north, south, east or west and maintain visual continuity. As an example, the
5 visual discontinuity in viewing a "great circle" route from Alaska to New York would be unbearable for all but the most hearty.
The digital mapping approach has been around for at least 20 years and is much more frequently used than the 0 analog approach. Digital data bases are stored in computers in a format similar to text of other databases. Unlike map information on a videodisc, the outstanding map features are stored as a list of objects to be drawn, each object being defined by a plurality of vector "dot" coordinates which define the crude outline of the object. As one example, a road is drawn by connecting a series of dots which were chosen to define the path (i.e., the "outline") of the road. Once drawn, further data and processing can be used to smooth the crude outline of the object, place text, such as the name or description of the object in a manner similar to what happens when drawing on a paper map.

Advantages of the digital approach:
digital maps are the purest form of geographical map25 ping data: from them, paper and analog maps can be produced.
digital maps can be quickly and easily updated in near real-time, and this updating can be in response to data input from external sources (e.g., geographical monitoring devices such as satellite photography).
digital maps can be easily modified to effect desirable mapping treatments such as uncluttering, enhancing, coloring, etc.
digital maps can be easily and accurately scaled, ro3 tated and drawn at any perspective view point.
digital maps can be caused to reproduce maps in 3-D.
digital maps can drive pen-plotters (for easy paper reproductions), robots, etc.
digital maps can be stored on any mass storage de40 vice.

Disadvantages of the digital approach:
digital maps require the use or creation of a digital database: this is a very time-consuming and expensive process, but once it is made, the data base can be very 5 easily copied and used for many different projects.

The digital approach is utilized with the present invention, as this approach provides overwhelming advantages over the above-described paper and analog approaches.
In designing any mapping system, several features are highly desirable:

First, it is highly desirable that the mapping system be of low cost.

Second, and probably most important, is access time. Not only is it generally desirable that the desired map section be accessible and displayed within a reasonable amount of time, but in some instances, this access time is critical.

In addition to the above, the present invention (as 0 mentioned above), seeks to provide a third important feature,-a mapping system which allows the manipulation of and access to an extraordinary amount of mapping information, i.e., a mapping system which allows a user to quickly and easily access a detailed map of any geographical area of the world.

A tremendous barrier is encountered in any attempt to provide this third feature. In utilizing the digital approach to map a large geographical area in detail
(e.g., the earth), one should be able to appreciate that the storage of mapping data sufficient to accurately define all the geographical features would represent a tremendous data base.

While there have been digital mapping implementations which have successfully been able to manipulate a tremendous data base, these implementations involve tremendous cost (i.e., for the operation and maintenance of massive mainframe computer and data storage facilities). Furthermore, there is much room for improvement in terms of access time as these mainframe implementations result in access times which are only as quick as 20 seconds. Thus, there still exists a need for a low-cost digital mapping system which can allow the storage, manipulation and quick (i.e., "real time") access and visual display of a desired map section from a tremendous mapping data base.

There are several additional mapping system features which are attractive.

It is highly desirable that a mapping system be sensitive to and compensate for distortions caused by mapping curved geographical (i.e., earth) surfaces onto a flat, two-dimensional representation. While prior art approaches have provided numerous methods with varying degrees of success, there is a need for further improvements which are particularly applicable to the digital mapping system of the present invention.

It is additionally attractive for a mapping system to easily allow a user to change his/her "relative viewing position", and that in changing this relative position, the change in the map display should reflect a feeling of continuity. Note that the "relative viewing position should be able to be changed in a number of different ways. First, the mapping system should allow a user to selectively cause the map display to scroll or "fly" along the geographical map to view a different (i.e., "lateral") position of the geographical map while maintaining the same degree of resolution as the starting position. Second, the mapping system should allow a user to selectively vary the size of the geographical area being displayed (i.e., "zoom") while still maintaining an appropriate degree of resolution, i.e., allow a user to selectively zoom to a higher "relative viewing position" to view a larger geographical area with lower resolution regarding geographical, political and cultural characteristics, or zoom to a lower "relative viewing position" to view a smaller geographical area with higher resolution. (Note that maintaining the appropriate amount of resolution is important to avoid map displays which are effectively barren or are cluttered with geographical, political and cultural features.) Again, while prior art approaches have provided numerous methods with varying degrees of success, there is a need for further improvements which are particularly applicable to the digital mapping system of the present invention.

The final feature concerns compatibility with existing mapping formats. As mentioned above, the creation of a digital database is a very tedious, time-consuming and expensive process. Tremendous bodies of mapping data are available from many important mapping authorities, for example, the U.S. Geological Survey (USGS), Defense Mapping Agency (DMA), National Aeronautics and Space Administration (NASA), etc. In terms of both being able to easily utilize the mapping data produced by these agencies, and represent an attractive mapping system to these mapping agencies, it would be highly desirable for a mapping system to be compatible with all of the mapping formats used by these respective
agencies. Prior art mapping systems have been deficient in this regard; hence, there still exists a need for such a mapping system.

## SUMMARY OF THE INVENTION

The present invention provides a digital mapping method and system of a unique implementation to satisfy the aforementioned needs.
The present invention provides a computer implemented method and system for manipulating and accessing digital mapping data in a tremendous data base, and for the reproduction and display of electronic display maps which are representative of the geographical, political and cultural features of a selected geographical area. The system includes a digital computer, a mass storage device (optical or magnetic), a graphics monitor, a graphics controller, a pointing device, such as a mouse, and a unique approach for structuring, managing, controlling and displaying the digital map data.
The global map generating system organizes the mapping data into a hierarchy of successive magnitudes or levels for presentation of the mapping data with variable resolution, starting from a first or highest magnitude with lowest resolution and progressing to a last or lowest magnitude with highest resolution. The idea of this hierarchical structure can be likened to a pyramid with fewer stones or "tiles" at the top, and where each successive descending horizontal level or magnitude contains four times as many "tiles" as the level or magnitude directly above it. The top or first level of the pyramid contains 4 tiles, the second level contains 16 tiles, the third contains 64 tiles and so on, such that the base of a 16 magnitude or level pyramid would contain 4 to the 16 th power or $4,294,967,296$ tiles. This total includes "hyperspace" which is later clipped or ignored. Hyperspace is that excess imaginary space left over from mapping of 360 deg , space to a zero magnitude virtual or imaginary space of 512 deg , square.

A first object of the present invention is to provide a digital mapping method and system which are of low cost.

A second and more important object of the present invention is to provide a unique digital mapping method and system which allow access to a display of the geo5 graphical, political and cultural features of a selected geographical area within a minimum amount of time.

A third object of the present invention is to provide a digital mapping method and system which allow the manipulation of and access to an extraordinary amount of mapping information, i.e., a mapping method and system which allow a user to quickly and easily access a detailed map of any geographical area of the world.

Another object of the present invention is to provide a digital mapping method and system which recognize and compensate for distortion introduced by the representation of curved (i.e., earth) surfaces onto a flat twodimensional display.

Still a further object of the present invention is to provide a digital mapping method and system which allow a user to selectively change his/her "relative viewing position", i.e., to cause the display monitor to scroll or "fly" to display a different "lateral" mapping position of the same resolution, and to cause the display monitor to "zoom" to a higher or lower position to 5 display a greater or smaller geographical area, with an appropriate degree of resolution.

A fifth object of the present invention is to provide a digital mapping method and system utilizing a unique

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mapping graticule system which allows mapping data to be compatibly adopted from several widely utilized mapping graticule systems.

## BRIEF DESCRIPTION OF THE DRAWINGS

The foregoing and other objects, structures and features of the present invention will become more apparent from the following detailed description of the preferred mode for carrying out the invention; in the description to follow, reference will be made to the accompanying drawings in which:
FIG. 1 is an illustration corresponding to a flat projection of the earth's surface.
FIG. 2 is an illustration of a digital computer and mass storage devices which can be utilized in implementing the present invention.
FIGS. 3A-3F are illustrations of monitor displays showing the ability of the present invention to display varying sizes of geographical areas at varying degrees of resolution.
FIG. 4 is a cross-sectional diagram of a simple building example explaining the operation of the present invention.
FIG. 5A and $B$ are plan view representations of a paper 450 as it is viewed from the relative viewing position A shown in FIG. 4.
FIG. 6 is a plan view representation of a paper 450 as it is viewed from the relative viewing position $B$ shown in FIG. 4.
FIG. 7 is a plan view representation of a paper 450 as it is viewed from the relative viewing position C shown in FIG. 4.
FIG. 8 is a pyramidal hierarchy of the data base file structure showing an example of the ancestry which exits between files.
FIG. 9A is a plan view representation of a paper 450, with the paper being divided into a first level of quadrant areas.
FIG. 9B is an illustration of a monitor displaying a digital map of the area enclosed by the dashed portions in FIG. 9A.

FIG. 10A is a plan view representation of a paper 450, with the upper-left and lower-right paper quadrant areas being further divided into quadrants.
FIG. 10B is an illustration of a monitor displaying a digital map of the area enclosed by the upper-left dashed portion in FIG. 10A.
FIG. 11A is a plan view representation of a paper 450, with several sections of the second level of quadrants being further divided into additional quadrants.
FIG. 11B is a higher resolution display of the area enclosed within the dashed portion in FIG. 11A.
FIG. 12 is a plan view illustration of a quadrant area division, with a two-bit naming protocol being assigned to each of the quadrant areas.
FIG. 13 is a pyramidal hierarchy of the data base files using the two-bit naming protocol of FIG. 12, and showing an example of the ancestry which exits between files.
FIG. 14 is a plan view illustration of a $360^{\circ} \times 180^{\circ}$ flat projection of the earth being impressed in the $512^{\circ} \times 512^{\circ}$ mapping area of the present invention, with a first quadrant division dividing the mapping area into four equal $250^{\circ} \times 256^{\circ}$ mapping areas.
FIG. 15 is the same plan view illustration of FIG. 14, with a second quadrant division dividing the mapping area into 16 equal $126^{\circ} \times 128^{\circ}$ mapping areas. line of the object. (Note: the reproduction of a digital map from a list of objects and "dot" vectors is well known the art, and is not the subject matter of the present invention; instead, the invention relates to a unique

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method and system for storing and accessing the list of objects and "dot" vectors contained in a tremendous digital data base.)
Once a geographical map has been "digitized",-i.e., converted to a list of objects to be drawn and a plurality of vector "dot" coordinates which define the crude outline of the object -, the mapping database must be stored in the memory of a mass storage device. Thus, the digital computer 200, which is to be used with the mapping method and system of the the present invention, is shown associated with the magnetic disk 260 (which represents any well-known magnetic mass storage medium, e.g., floppy disks, hard disks. magnetic tape, etc.), and the CD-ROM 270 (which represents any well-known optical storage medium, e.g. a laser-read compact disk). Alternatively, the digital mapping database can be stored on, and the digital computer can be associated with any well known electronic mass storage memory medium (e.g., ROM, RAM, etc.). Because of every increasing availability. reductions in cost, and tremendous storage capacities, the preferred memory mass storage medium is the CD-ROM, i.e., a laser-read compact disk.

The discussion now turns to FIGS. 3A-F, showing illustrations of monitor displays which provide a brief illustration of the operation of the present invention. Although the digital nature of the maps of FIGS. $3 \mathrm{~A}-3 \mathrm{~F}$ can easily be detected due to the jagged outlines, it should be understood that these geographical outlines could easily be smoothed using any of a number of "smoothing" techniques which are well-known to those skilled in the digital mapping art.

In FIG. 3A. the digital computer has retrieved relevant mapping information from the digital mapping database, and has produced a monitor display of a digital map substantially corresponding to the flat projection of the earth's surface which was shown in FIG. 1. In FIG. 3A, the monitor display reflects a "relative viewing position" which is a great distance in space, and hence, only the crude geographical outline of the continents is shown with sparse detail.

Suppose a user wishes to view a map of the states of Virginia and Maryland in greater detail. By entering the appropriate commands using the keyboard 220 or the mouse device 240, a user can cause the monitor display to "zoom" to a lower "relative viewing position", such that the monitor displays a digital map of a smaller geographical area which is shown at a higher degree of resolution. Thus, in FIG. 3B the a digital map of the continents of the western hemisphere is displayed in greater detail.

By entering additional commands, a user can cause the monitor display to further "zoom" to the following displays: FIG. 3C showing North America in greater detail; FIG. 3D showing the eastern half of the United States in greater detail: FIG. 3E showing the east coast of the United States in greater detail; and. FIG. 3F showing Virginia and Maryland in greater detail.

Although in this example, the monitor display was caused to "zoom" to Virginia and Maryland, it should, be appreciated that the present invention allowed a user to selectively zoom into any geographical area of the earth, and once a user has reached the desired degree of mapping resolution, the mapping system of the present invention also allows the user to "scroll" or "fly" to a 65 different lateral position on the map.

Furthermore, although the drawings illustrate the monitor display zooming to display state boundaries, separate database file. Thus, 16 files can be used to reproduce a digital map of the paper 450, as viewed from the relative viewing position B (FIG. 4).

In order to digitize and record data corresponding to a third (or higher) degree of resolution. the next "relative viewing position" C (FIG. 4) is taken to view the paper 450. At this level, paper 450 now appears larger (FIG. 7) and has visual features of higher resolution.

In moving down one level in the pyramidal structure,, the filenames for each of the respective files on the second level is increased to two characters.
In calculating the filenames, it is convenient to first 5 divide the second level files into groups of four, according to parentage. To maintain a record of ancestry, the ancestor filename of each file is maintained as the first part of the filename. In determining the second part, the naming protocol which was utilized to name the quadrant files of the top level, is also utilized in naming the respective quadrant files on the second level. Thus, parent file $A$ is shown as being related to descendent (i.e., brother and sister) files $\mathrm{AA}, \mathrm{AB}, \mathrm{AC}, \mathrm{AD}$. Similar discussion can be made for the remaining files along these two level.

A similar process can be utilized in providing the unique filenames to the third level files. At this level, the filenames consist of three characters. Again, the ancestor filename of each file would be maintained as a first filename part, in order to maintain a record of ancestry. In the example illustrated (FIG. 8), parent file AD is shown as being related to descendent (i.e., brother and sister) files ADA, ADB, ADC, ADD. Similar discussions can be made for the remaining files along these two levels, and furthermore, similar discussions can be made each time a pyramidal level is added.
From the above discussion, one should be able to realize that the above-described naming convention is particularly useful in programming a digital computer to move through the pyramidal file structure to access the appropriate data corresponding to varying degrees of resolution. More particularly, one should be able to realize that, since file names increase one character in length each time there is a downward movement through the pyramidal structure and the protocol for naming descendent files is known, the digital computer can be programmed to quickly and easily access the appropriate files for a smaller mapping area with a greater degree of resolution. Similarly, one should be able to realize that, since the filenames decrease one character in length each time there is an upward movement through the pyramidal structure, the digital computer can be programmed to quickly and easily access the appropriate files for a greater mapping area with a smaller degree of resolution.

The following example is believed to provide an increase in the understanding of the present invention.
In the example, it is assumed that the digital database corresponding to the three resolutions of the paper 450 (as shown in FIGS. 4, 5A-B, 6, 7 ) have been loaded to be accessible from the memory mass storage device, and furthermore, it is assumed that the mapping system is programmed to initially access and display a digital map corresponding to the digital mapping data in the files A, B, C, D (FIG. 8). Thus, the monitor (FIG. 9B) would display (in low resolution) the entire area enclosed within dashed portion 900 illustrated on the paper 450 (FIG. 9A). (Note: The reproduction of a digital map from digital data from several different files or sources 60 is well-known in the art and is not the subject matter of the present invention.)

Suppose the user notices the dotted area on the low resolution map and wishes to investigate this area further. By using the appropriate keys (e.g. , , , , , >) 65 and/or a mouse device, a user can give the mapping system an indication that he/she wishes to see the smaller area (i.e., quadrant A) at a higher degree of resolution. Upon receiving this preference, the mapping

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system can use its knowledge of the file naming operations to quickly determine the names of the files which must be accessed. More specifically, using $A$ as the parent file name and following the existing quadrant naming protocol the mapping system is quickly and easily able to calculate that it is files AA, AB. AC, AD which it needs to access. Once these files are accessed, the monitor in FIG. 10B displays (in higher resolution) the area enclosed within the dashed portion 1000 as illustrated on the paper 450 (FIG. 10A).

If a user is still not satisfied with the degree of mapping resolution, the user can again use the appropriate keys or mouse device to indicate that he/she wishes to see the smaller area (e.g., quadrant D; FIG. 10A) in a higher degree of resolution. In using AD as the parent filename and following the existing quadrant naming protocol, the mapping system is quickly and easily able to calculate that it is files ADA, ADB, ADC, ADD which it needs to access. Once these files are accessed, the monitor (FIG. 11B) displays (in higher resolution), the area enclosed within the dashed portion 1100 as illustrated on the paper 450 (FIG. 11A).

One skilled in the digital mapping and computer programming art should recognize that "scrolling" or "flying" to different lateral "relative viewing positions" to display a different lateral portion of the map is also provided by the present invention. Instead of adding or removing filename characters as in a change of resolution, in this instance, the mapping system must be programmed to keep track of the filenames of the current position and also, the orderly arrangement of filenames so that the appropriate filenames corresponding to the desired lateral position can be determined. As an example if the user desired to scroll to the right border of the paper 450, the mapping system would respond by accessing and causing the monitor to display the digital maps corresponding to the following sequence of files: (Note: In this example, it is assumed that it takes 4 files to provide sufficient digital data to display a full digital map on a monitor) ADA, ADB, ADC, ADD; ADB, ADD, BCA, BCC; BCA, BCB, BCC, BCD; BCB, BCD, BDA, BDC; and BDA, BDB, BDC, BDD. If the user, then desired to scroll to the bottom (right corner) of the paper $\mathbf{4 5 0}$, the mapping system would respond by accessing and causing the monitor to display the digital maps corresponding to the following files: BDA, BDB, BDC, BDD; BDC, BDD, DBA, DBB; DBA, DBB, DBC. DBD; DBC, DBD, DDH, DDB; DDA, DDB, DDC, DDD. In effect as all of the files in the above example correspond to the same level of resolution all these files (and any group of files which exist on the same level of resolution) can be taken as being related as cousins.

FIGS. 9A, 10A, 11A can also be used to illustrate the operation of moving toward the display of a larger mapping area with a lower degree of resolution.

Assume that after lateral "scrolling" or "flying", that the monitor is now displaying (not shown) a digital map corresponding to the enclosed area 1110 shown in FIG. 11A. (Note: at this position the mapping system is accessing and display a digital map corresponding to the digital data in the files DCA, DCB, DCC, DCD). Suppose the user now wishes to cause the "relative viewing position" to zoom upward, such that the monitor will display a larger portion of the paper 450 at a lower degree of resolution. By using the appropriate keys or a mouse device, the user indicates his/her preference to the mapping system. Upon receiving this preference,
the mapping system is programmed to quickly determine the names of the files which must be accessed. More specifically, the mapping system is able to look at the first portion of the filenames currently being used (i.e., DCA, DCB, DCC, DCD), to immediately determine that these files have the ancestry DC , i.e., have a grandfather D and a parent DC . The mapping system then immediately determines brother and sister files of parent file DC as being DA, DB and DD. The mapping system then accesses these files and causes the monitor to display a digital map (not shown) corresponding to the enclosed portion 1010 (FIG. 10A) of the paper 450.

Suppose the user again indicate a preference to cause the "relative viewing position" zoom upward. Upon receiving this preference, the mapping system again goes through a process similar to that discussed immediately above. However, this time the mapping system looks at the filenames currently being used (i.e., DA, DB, DC, DD) and determines that parent file D has brother and sister files A, B and C. The mapping system then immediately accesses these files and causes the monitor to display a digital map (FIG. 9B) corresponding to the enclosed portion 900 (FIG. 9A) of the paper 450.

The text now turns to a description of the operation for assigning unique filenames in the currently preferred embodiment, i.e., in a digital mapping system which is implemented in a DOS operating system.

As anyone skilled in the computer art will know. every computer operating system has its own unique set of rules which must be followed. In an implementation of the present invention in a DOS operating system. the DOS rules must be followed. Since a critical feature of the present invention is the division of the digital mapping database into a plurality of files (each having a unique filename), of particular concern with the present invention is the DOS rules regarding the naming of filenames.
A DOS filename may be up to eight (8) characters long, and furthermore. may contain three (3) additional trailing characters which can represent a file specification. Thus, a valid DOS filename can be represented by the following form:
where "-" can be replaced by any ASCII character (including blanks), except for the following ASCII characters:

```
"/\[]:|<> +;,
```

and ASCII characters below 20H. The currently preferred embodiment stays within these DOS filename rules by using the file naming operations which are detailed below.

Because the assigned filenames will be seen to be related to hexadecimals, a useful chart containing the hexadecimal base and also a conversion list (which will be shown to be convenient ahead), is reproduced below:

|  |  |  |  |
| :---: | :---: | :---: | :---: |
|  | Column 1 | Column 2 | Column 3 |
| 65 | 0000 | 0 | G |
|  | 0001 | 1 | H |
|  | 0010 | 2 | I |
|  | 0011 | 3 | J |
|  | 0100 | 4 | L |
|  | 0101 | 5 | M |


| -Continued |  |  |
| :---: | :---: | :---: |
| Column 1 | Column 2 | Column 3 |
| 0111 | 7 | N |
| 1000 | 8 | O |
| 1001 | 9 | P |
| 1010 | A | Q |
| 1011 | B | R |
| 1100 | C | S |
| 1101 | D | T |
| 1110 | E | U |
| 1111 | F | V |

The first column contains a list of all the possible 4-bit binary combinations: the second column contains the hexadecimal equivalent of these binary numbers: and the third column concerns a "mutant-hex" conversions which will be shown to be important in the discussion to follow. In the operatidns to assign unique filenames for use in a DOS operating system, the present invention looks at each of the eight DOS filename characters as hexadecimal characters rather than ASCII characters. Hence, while the following discussion will center around determining unique filenames using hexadecimal (and "mutant-hexadecimal") characters, it should be understood in an actual DOS implementation, the hexadecimal filenames must be further converted into the equivalent ASCII characters such that the appropriate DOS file naming rules are followed.
At this point, it is also useful to note that the file naming operation of the preferred embodiment is not concerned with the trailing three character filename extension. However, it should be further noted that this three character filename extension may prove useful in specifying data from different sources, and allowing the different types of data to reside in the same database. As examples, the filename extension ".spm" might specify data from scanned paper maps, the filename extension ".si" might specify data from satellite imagery, the filename extension ".ged" might specify gridded elevation data, etc.
As a result of the foregoing and following discussions, it will be seen that the naming operation of the preferred embodiment is concerned only with a filename of the following form:
where each "-" represents a character which is a hexadecimal character within the character set of " $0-9$ " and "A-F", or is a "mutant-hexadecimal" character within the character set of " $\mathrm{G}-\mathrm{V}$ ".
Several more important file naming details should be discussed.
First, it should be pointed out that the first four (4) filename characters is designated as corresponding to the " $x$ " coordinate characters, and the last four (4) filename characters are designated as corresponding to the " y " coordinate characters.
Second, during the file naming operations, often it is necessary to convert the filename characters into the equivalent binary representation. As each hexadecimal character can be converted into a four bit binary number, it can be seen that the first four (4) filename characters (designated as "x" coordinate characters) can be converted into sixteen (16) binary bits designated as " $x$ " bits, and similarly, that the last four (4) filename characters (designated as " $y$ " coordinate characters) can be converted into sixteen (16) binary bits designated as " y " bits. As will become more apparent ahead, each of these
sixteen (16) " $x$ " and " $y$ " bits corresponds to a filename bit which can be manipulated when assigning filenames at a corresponding magnitude or level of mapping resolution, e.g., the first " $x$ " and first " $y$ " bits correspond to filename bits which can be manipulated when assigning unique filenames at the first magnitude, the second " x " and second " $y$ " bits correspond to filename bits which can be manipulated when assigning unique filenames at the second magnitude, etc.

Third, FIG. 12 corresponds to the naming protocols which are utilized to modify and relate a parent filename to four (4) quadrant filenames. Note that there is a two-bit naming protocol in each of the quadrant files. As will become more clear ahead, the first bit of each protocol determines whether the current " $x$ " filename bit will be modified (i.e., if the first protocol bit is a " 1 ", the current " $x$ " filename bit is changed to a " 1 ", and if first protocol bit is a " 0 ", the current " $x$ " filename bit is maintained as a " 0 "), and the second bit determines whether the current " $y$ " filename bit will be modified (in a similar manner).

The text now turns to a file naming example which is believed to provide further teachings and clarity to the currently preferred file naming operation.

FIG. 13 is an illustration of a portion of the preferred digital data base, with the plurality of files (partially shown) being arranged in a conceptual pyramidal manner in a manner similar to that which was described with reference to FIG. 8. More specifically, there are shown four files $\mathbf{1 3 0 0}$ having digital data corresponding to a first level or magnitude of mapping resolution, sixteen files $\mathbf{1 3 1 0}$ having digital data corresponding to a second level or magnitude of mapping resolution, sixtyfour files $\mathbf{1 3 2 0}$ having digital data corresponding to a third level or magnitude of mapping resolution, and a partial cut-away of a plurality of files $\mathbf{1 3 3 0}$ having data corresponding to a fourth level or magnitude of mapping resolution. Although not shown, it is to be understood that, in the preferred embodiment, additional pyramidal structure corresponding to levles magnitudes five through sixteen similarly exist. As examples of the file naming operation, filenames will now be calculated for the files which essentially occupy the same positions 5 as the files which were outlined in FIG. 8.

We begin with the initializing eight (8) character filename:

0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

which can be converted to the binary equivalent:

| 0000 | 0000 | 0000 | 0000 | 0000 | 0000 | 0000 | 0000 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

This binary representation is the basic foundation which will be used to calculate all of the filenames for the files on the first level (1300). Note, that the first and last four filename characters, and the first and last sixteen bits are slightly separated in order to conveniently distinguish the " $x$ " and " $y$ " coordinate characters and bits. Both the first (leftmost) " $x$ " bit and the first (leftmost) " $y$ " bit are the bits which can be manipulated in assigning a unique filename to the files on the first level.

File naming begins with the first (upper-rightmost) file on the first level 1300. The naming protocol assigned to this quadrant file is the two-bit protocol " 10 ".

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As the first protocol bit is a " 1 ", this means that the current " $x$ " bit must be changed to a " 1 ". As the second protocol bit is a " 0 ", this means that the current " y " bit is maintained as a " 0 ". As a result of the foregoing, the first (upper-rightmost) file is assigned the filename having the binary equivalent of:

| 1000 | 0000 | 0000 | 0000 | 0000 | 0000 | 0000 | 0000 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

which can be converted to the hex characters:

| 8 | 0 | 0 | 0 | 0 | 0 | 0 | 0. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |

In proceeding clockwise, next is the second (lowerrightmost) file on the first level 1300 . The naming protocol assigned to this quadrant file is the two-bit protocol " 11 ". As the first protocol bit is a " 1 ", the current " $x$ " bit is changed to a " 1 ": similarly, as the second protocol bit is a " 1 ", the current " y " bit is changed to a " 1 ". As a result of the foregoing, the second (lowerrightmost) file is assigned the filename having the binary equivalent of:

| 1000 | 0000 | 0000 | 0000 | 1000 | 0000 | 0000 | 0000 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

which can be converted to the hex characters:

| 8 | 0 | 0 | 0 | 8 | 0 | 0 | 0. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |

Continuing clockwise, next is the third (lower-leftmost) file on the first level $\mathbf{1 3 0 0}$. The naming protocol assigned to this quadrant file is the two-bit protocol " 01 ". As the first protocol bit is a " 0 ", the current " x " bit is maintained at 0 . As the second protocol bit is a " 1 ", the current " $y$ " bit is changed to a " 1 ". As a result of the foregoing. the third (lower-leftmost) file is as- 40 signed the filename having the binary equivalent of:

| 0000 | 0000 | 0000 | 0000 | 1000 | 0000 | 0000 | 0000 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

which can be converted to the hex characters:

| 0 | 0 | 0 | 0 | 8 | 0 | 0 | 0. |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

Finally, there is the fourth (upper-leftmost) file on the first level 1300. The naming protocol assigned to this quadrant is the two-bit protocol " 00 ". As neither of the protocol bits is a " 1 ", it can be easily seen that neither of the current " $x$ " and " $y$ " bits changes, and hence, the fourth (upper-leftmost) file is assigned the filename having the binary equivalent of:

| 0000 | 0000 | 0000 | 0000 | 0000 | 0000 | 0000 | 0000 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

which can be converted to the hex characters:

| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0. |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

In further discussions of the example, it is important to note that the initializing (8) character filename of 00000000 (which was utilized to calculate the filenames
of the files on the first level 1300) is not utilized in assigning filenames on subsequent levels. In naming files from the second level or magnitude downward, the binary equivalent of the parent file's name is utilized as 5 the foundation from which the descendent file's name is derived. It is only coincidental that the filename of the parent file 00000000 (located in the user-left most corner of the first level 1300 ) is the same as the initializing filename. Use of the parent's filename to calculate the 10 descendent's filename will become more readily apparent ahead in the example.

In continuing the file naming example, the fourth (upper-leftmost) file (having filename 00000000 ) in the first level 1300 can be viewed as being the parent file of 15 the four (highlighted) quadrant files in the second level 1310. As stated above, the binary equivalent of parent file's 00000000 name is utilized as the foundation for calculating the descendent file's filenames. At this second level or magnitude, the second " $x$ " and " $y$ " bits from the left in the parent's binary filename are taken as the "current" bits which can be manipulated to provide a unique filename for the descendent files.

As the calculation of the filename for the fourth (up-per-leftmost) file of the second level 1310 illustrates a very important modification in the file naming operation, the example will first continue with discussions corresponding to this file.
As the naming protocol assigned to the fourth (upperleftmost) file of the second level 1310 is two-bit proto30 col " 00 ", it can be seen that neither of the current " $x$ " and " $y$ " bit would be changed. Hence the parent's filename 00000000 is unchanged, and is attempted to be adopted as the descendent's filename. However, note that this is extremely undesirable as the operation of the present invention is based on assigning each data file a unique filename, and furthermore, a DOS operation system will not allow the same filename to be assigned to two different files. To avoid this clash. the preferred file naming operation of the present invention incor prates a further step which can be detailed as follows:
First calculate the filename as explained above. Once the binary filename is obtained, convert to the eight character hexadecimal equivalent.
Next, take the decimal number of the current level or magnitude modifier Convert the decimal magnitud modifier into a four-bit binary magnitude modifier, and line these four bits up with the four hexadecimal " $x$ " filename characters. Whenever a " 1 " appears in the binary magnitude modifier. the corresponding aligned " $x$ " filename character is converted to a "mutant-hexadecimal" character. i.e., a decimal 16 value is added to convert the aligned filename character into a one of the "mutant-hexadecimal" characters in the character set of 55 "G-V".

Conversions from a hexadecimal character to a "mu-tant-hexadecimal" character can be most readily made using the chart detailed above. As an example, if decimal 16 is added to the hex character " 0 " (Column 2), acter " $G$ " (Column 3). Similarly, if decimal 16 is added to the hex character " 1 " (Column 2), there is a conversion to the "mutant-hexadecimal" character " H " (Column 3). Similar discussion can be made for the remain-

Once correspondingly aligned filename characters are converted to "mutant-hexadecimal", the resultant
eight (8) characters correspond to the file's unique filename.

The above processing will now be applied to the fourth (upper-rightmost) file of the second level 1310 (which was recently discussed above). The resultant binary filename:

| 0000 | 0000 | 0000 | 0000 | 0000 | 0000 | 0000 | 0000 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

is converted to the hex characters:

| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |

The level or magnitude two (2) minus one (1) results in a decimal magnitude modifier of one (1). The decimal magnitude modifier is converted to the four-bit binary equivalent and is aligned with the " $x$ " filename characters above, as follows:

| 0 | 0 | 0 | 1 |
| :---: | :---: | :---: | :---: |

Only the fourth bit of the binary magnitude modifier is 2 a " 1 ", so only the fourth " $x$ " filename character needs to be converted to "mutant-hexadecimal". From the chart, the hexadecimal character " 0 " is shown to convert to a "mutant-hexadecimal" character " $G$ ". Thus. the unique filename which is assigned to the fourth (upper-leftmost) file of the second level 1310, is:

| 0 | 0 | 0 | $G$ | 0 | 0 | 0 | 0. |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

$\ln$ continuing the example to calculate the filename for the first (upper-right-quadrant) file of the second level 1310. it can be seen that this file is assigned the two-bit naming protocol " 10 ". The first protocol bit is a " 1 " which indicates that the current (second from the left) " $x$ " bit of the parent file's binary filename must be changed to a " 1 ", In contrast, the second protocol bit is a " 0 ", which indicates that the current (second from the left) " $y$ " bit is maintained as " 0 " Thus the parent filename:

| 0000 | 0000 | 0000 | 0000 | 0000 | 0000 | 0000 | 0000 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

is converted to:

| 0100 | 0000 | 0000 | 0000 | 0000 | 0000 | 0000 | 0000 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

which results in the hex characters:

| 4 | 0 | 0 | 0 | 0 | 0 | 0 | 0. |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

The level or magnitude two (2) minus one (1) results in 60 a decimal magnitude modifier of one (1). The decimal magnitude modifier is converted to the four-bit binary equivalent and is aligned with the " $x$ " filename characters above, as follows:

| 0 | 0 | 0 | 1 |
| :---: | :---: | :---: | :---: |

Only the fourth bit of the binary magnitude modifier is a " 1 ", so only the fourth " $x$ " filename character needs to be converted to "mutant-hexadecimal". From the chart, the hexadecimal character " 0 " is shown to convert to a "mutant-hexadecimal" character " $G$ ". Thus, the unique filename which is assigned to the first (upper-right-quadrant) file of the second level 1310, is:

| 4 | 0 | 0 | $G$ | 0 | 0 | 0 | 0. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |

Turning now to the second (lower-right-quadrant) file, this file is assigned the two-bit naming protocol " 11 ". The first protocol bit is a " 1 " which indicates that the current (second from the left) " $x$ " bit of the parent file's binary filename must be changed to a " 1 ", and similarly, the second protocol bit is a " 1 ", which indicates that the current (second from the left) " $y$ " bit of the parent file's binary filename must be changed to a " 1 " Thus the parent filename:

| 0000 | 0000 | 0000 | 0000 | 0000 | 0000 | 0000 | 0000 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

is converted to:

| 0100 | 0000 | 0000 | 0000 | 0100 | 0000 | 0000 | 0000 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

which results in the hex characters:

| 4 | 0 | 0 | 0 | 4 | 0 | 0 | 0. |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

In applying the above operations to the third (lower-left-quadrant) file of the second level 1310, it can be easily calculated that the resultant filename is:

| 0 | 0 | 0 | $G$ | 4 | 0 | 0 | 0. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |

The example of the file naming operation is further extended to the third level or magnitude. as this exam65 ple is illustrative of both the use of the parent file's binary filename to calculate the descendent's filename, and the removal of "mutant-hexadecimal" conversions before calculating the descendent's filename.

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In FIG. 13. the third (lower-right-quadrant) file of the second level 1310 is shown as being the parent of the four (4) quadrant files highlighted in the third level or magnitude 1320.

The discussion centers on the calculation of the unique filename for the second (lower-right-quadrant) file in the third level 1320 . Before the parent filename can be used as the foundation for calculating the descendent's filename. all "mutant-hexadecimal" conversions must be removed. Thus the parent filename:

| 4 | 0 | 0 | $G$ | 4 | 0 | 0 | 0. |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

is converted back to:

| 4 | 0 | 0 | 0 | 4 | 0 | 0 | 0. |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

which is further converted to the binary equivalent:

| 0100 | 0000 | 0000 | 0000 | 0100 | 0000 | 0000 | 0000 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

In continuing the calculation, this second (lower-right-quadrant) file is assigned the two-bit naming protocol " 11 ". The first protocol bit is a " 1 " which indicates that the current (third from the left) "x" bit of the parent file's binary filename must be changed to a " 1 ", and similarly, the second protocol bit is a " 1 ", which indicates that the current (third from the left) " y " bit of the parent file's binary filename must be changed to a " 1 ". Thus the parent filename:

| 0100 | 0000 | 0000 | 0000 | 0100 | 0000 | 0000 | 0000 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

is converted to:

| 0110 | 0000 | 0000 | 0000 | 0110 | 0000 | 0000 | 0000 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

which results in the hex characters:

| 6 | 0 | 0 | 0 | 6 | 0 | 0 | 0. |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

The level or magnitude three (3) minus one (1) results in a decimal magnitude modifier of two (2). The decimal magnitude modifier is converted to the four-bit binary equivalent and is aligned with the " $x$ " filename characters above, as follows:

| 0 | 0 | 1 | 0 |
| :--- | :--- | :--- | :--- |

Only the third bit of the binary magnitude modifier is a " 1 ", so only the third " $x$ " filename character needs to be converted to "mutant-hexadecimal". From the chart, the hexadecimal character " 0 " is shown to convert to a "mutant-hexadecimal" character " G ". Thus, the unique filename which is assigned to the second (lower-rightquadrant) file of the third level 1320, is:


The filenames for several additional third level files will be given to give the patent reader further practice.
In applying the above operations to the first (upper-right-quadrant) file of the third level 1320, it can be easily calculated that the resultant filename is:

| 6 | 0 | $G$ | 0 | 4 | 0 | 0 | 0. |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

In applying the above operations to the third (lower-left-quadrant) file of the third level 1320, it can be easily calculated that the resultant filename is:

| 4 | 0 | $G$ | 0 | 6 | 0 | 0 | 0. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |

Finally, in applying the above operations to the fourth (upper-left-quadrant) file of the third level 1320 , it can be easily calculated that the resultant filename is:

As a result of all of the foregoing teachings, one skilled in the art should now be able to calculate the filename of any other of the 1.4 billion files which would be required to provide digital maps corresponding to sixteen (16) resolutions of any geographical area on earth. Furthermore, once a file is being accessed, by understanding the rules and operations of the file naming operation one skilled in the are should be able to calculate any other related files, i.e., parent files. and brother/sister/cousin files.

While the unique approach for storing and accessing files in the pyramidal file structure has been particularly pointed out. further discussion is needed as to an additional advantageous feature of the present invention.

As mentioned previously, the creation of a digital database is a very tedious, time consuming and expensive process. Tremendous bodies of mapping data are available from many important mapping authorities, for example, the U.S. Geological Survey (USGS), Defense Mapping Agency (DMA), National Aeronautics and 5 Space Administration (NASA), etc.

The maps and mapping information produced by the above recited agencies, is always based on well established mapping area divisions. As a few examples, the Defense Mapping Agency (DMA) produces maps and mapping information based on the following mapping areas: GNC maps which are $2^{\circ} \times 2^{\circ}:$ JNC maps which are $1^{\circ} \times 1^{\circ}$; ONC maps which are $30^{\prime} \times 30^{\prime}$ : TPC maps which are $15^{\prime} \times 15^{\prime}$; and JOG maps which are $7.5^{\prime} \times 7.5^{\prime}$. As a further example, the U.S. Geological Survey (USGS) also produces maps and utilizes mapping information based on $15^{\prime} \times 15^{\prime}$ and $7.5^{\prime} \times 7.5^{\prime}$.

In terms of both being able to easily utilize the mapping data produced by these agencies, and represent an attractive mapping system to these mapping agencies, it 0 would be highly desirable for the mapping system of the present invention to be compatible with all of the mapping formats used by these respective agencies. Such is not the case when the mapping database is based on a graticule system corresponding to $360^{\circ}$

If one were to apply multiple quadrant divisions to the $360^{\circ} \times 180^{\circ}$ flat map projection of the earth (FIG. 1). one would result in the following mapping area subdivisions:
less complicated, the non-DOS file naming operation will be used in the discussion.

The digital mapping of the earth surfaces begins in FIG. 14. The visual perception of the earth surfaces is 5 experienced as being centered, and occupying only a portion of the $512^{\circ} \times 512^{\circ}$ projection. A first quadrant division is applied to result in four equal $256^{\circ} \times 256^{\circ}$ mapping areas. The visual information in each of the areas is digitized, and stored in a separate file, Thus, it 10 can be seen that one would have to access four files $a, b$, $c, d$ in order to reproduce a digital map corresponding to the earth surfaces as viewed from this "relative viewing position."
One skilled in the art, might, at this point, wonder if 15 the massive blank portions of the $512^{\circ} \times 512^{\circ}$ projections result in large blank portions on the digital map display. The preferred embodiment avoid this phenomena, through a simple watchdog operation, i.e., the computer is programmed to keep track of longitudinal and latitudinal movements from an initial position of $0^{\circ}$ longitude and $0^{\circ}$ latitude, and the computer does not allow scrolling of the monitor display beyond $90^{\circ}$ north or south.
As to side to side movements, the computer allows 25 scrolling beyond $180^{\circ}$ east or west by patching the appropriate data files together to perform a "wrap around" operation. Note that, with the knowledge of the logical file naming operation, the computer can quickly and easily calculate the appropriate files to 30 access.

Before moving to the next level or magnitude of mapping resolution, it is beneficial to note the correspondence between our findings and the enties in the

| $\begin{gathered} \text { MAG- } \\ \text { NI- } \\ \text { TUDE } \\ \hline \end{gathered}$ | Window Size without overlap | MAGNITUDE EQUIVALENCY CHART FOR DELORME PROJECTION Chart assumes 69 statute miles per degree at equator |  |  |  |  |  | Equivalent <br> Paper Map <br> Scales | Size of paper map image at equator (in) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Ht of window statute miles | Ht of window kilometers | \# <br> Windows per MAG | \# <br> Windows/ MAG w/polar compression | Pixel resolution 480 monitor <br> (ft) | Data reso- <br> lution (ft) <br> 1024-based window |  |  |
| 1 | $256^{\circ} \times 256^{\circ}$ | 17664 | 28421 | 4 | 4 |  | 91080 |  |  |
| 2 | $128^{\circ} \times 128^{\circ}$ | 8832 | 14211 | 8 | 8 |  | 45540 |  |  |
| 3 | $64^{\circ} \times 64^{\circ}$ | 4416 | 7105 | 24 | 24 | 48576 | 22770 | 1:100 million | $2.8 \times 2.8$ |
| 4 | $32^{\circ} \times 32^{\circ}$ | 2208 | 3553 | 72 | 72 | 24288 | 11385 | 1:50 million | $2.8 \times 2.8$ |
| 5 | $16^{\circ} \times 16^{\circ}$ | 1104 | 1776 | 288 | 288 | 12144 | 5693 | 1:30 million | $2.3 \times 2.3$ |
| 6 | $8^{\circ} \times 8^{\circ}$ | 552 | 888 | 1152 | 858 | 6072 | 2846 | 1:16 million | $2.2 \times 2.2$ |
| 7 | $4^{\circ} \times 4^{\circ}$ | 276 | 444 | 4232 | 3432 | 3036 | 1423 | $1: 10$ million | $1.7 \times 1.7$ |
| 8 | $2^{\circ} \times 2^{\circ}$ | 138 | 222 | 16200 | 12808 | 1518 | 712 | 1:5 million | $1.7 \times 1.7$ |
| 9 | $1^{\circ} \times 1^{\circ}$ | 69 | 111 | 64800 | 51210 | 759 | 356 | 1:2 million | $2.2 \times 2.2$ |
| 10 | $30^{\prime} \times 30^{\prime}$ | 34.5 | 55.5 | 259000 | 204840 | 380 | 178 | 1:1 million | $2.2 \times 2.2$ |
| 11 | $15^{\prime} \times 15^{\prime}$ | 17.25 | 27.8 | 1036800 | 813600 | 190 | 89 | 1:500,000 | $2.2 \times 2.2$ |
| 12 | $7.5^{\prime} \times 7.5^{\prime}$ | 8.625 | 13.9 | 4147200 | 3277440 | 95 | 44 | 1:250,000 | $2.2 \times 2.2$ |
| 13 | $3.75^{\prime} \times 3.75^{\prime}$ | 4.312 | 6.9 | 16588800 | 13109760 | 47.4 | 22 | 1:125,000 | $2.2 \times 2.2$ |
|  |  |  |  |  |  |  |  | 1:100,000 | $2.73 \times 2.73$ |
|  |  |  |  |  |  |  |  | 1:80,000 | $3.4 \times 3.4$ |
| 14 | $1.875^{\prime} \times 1.875^{\prime}$ | 2.156 | 3.5 | 66355200 | 52439040 | 23.7 | 11.1 | 1:62,500 | $2.2 \times 2.2$ |
|  |  |  |  |  |  |  |  | 1:50,000 | $2.73 \times 2.73$ |
|  |  |  |  |  |  |  |  | 1:40,000 | $3.4 \times 3.4$ |
| 15 | $0.9375^{\prime} \times 0.9375^{\prime}$ | 1.078 | 1.7 | 265420800 | 209756160 | 11.9 | 5.6 | 1:24,000 | $2.8 \times 2.8$ |
|  |  |  |  |  |  |  |  | 1:20,000 | $3.4 \times 3.4$ |
| 16 | $0.46875^{\prime} \times 0.46875^{\prime}$ | 0.539 | 0.9 | 1016683200 | 839024640 | 5.9 | 2.8 | 1:12,000 | $2.8 \times 2.8$ |

The best way to see the advantages of the $512^{\circ} \times 512^{\circ}$ mapping projection, is to use it with the previously, taught, quadrant division and pyrimidal file structure to 6 show how this unique mapping projection can provide digital maps of any geographical areas of the earth, with 16 levels or magnitudes of resolution. As it is slightly
above-indicated chart.
In looking at the left-most column, and tracing down to magnitude 1 , note that the $256^{\circ} \times 256^{\circ}$ window size exactly matches our determination. Furthermore, note that our findings is also in agreement with the number of widows i.e., 4. It is also interesting to note from the third column, that the height or "relative viewing posi-

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tion" of this magnitude or level would be 17, 664 statute miles above the earth's surface.

Turning now to the second level or magnitude of resolution (FIG. 15). a further quadrant division is applied, resulting in sixteen (16) mapping areas of $128^{\circ} \times 128^{\circ}$. The respective filenames which are assigned to each of the mapping areas is shown. In viewing FIG. 15, note that there are eight (8) mapping areas which are not intersected by the earth's surface. In order to save valuable memory space, the preferred embodiment will ignore, and in fact will never create these files. Note that there is no use for these files as they do not contain any digital mapping data nor will they ever have any descendents which hold mapping data. In order to implement this "file selectivity", the preferred embodiment again utilizes a watchdog approach. More specifically, as the computer already knows the degree ( ${ }^{\circ}$ ) size of the earth's surface and the degree $\left({ }^{\circ}\right)$ size of each of the mapping areas (i.e., at each level or magnitude of resolution), it can be seen that the computer can easily calculate the filenames which will not intersect the earth's surface.

Again it is useful to correspond our findings with the entries in the chart.

Our findings are substantiated, as, at a magnitude of 2, 25 the window size is shown as being $128^{\circ} \times 128^{\circ}$, and there are shown to be eight (8) pertinent windows or files at this magnitude. Again, it is interesting to note that the height or "relative viewing position" of this window would be 8,832 statute miles above the earths earth's surface.
It is important to note that, although the "relative viewing position" of each level or magnitude is moving closer to the earth, the visual perception of the earth (as seen in FIGS. 14-19 is not illustrated as getting larger with a greater degree of detail. This is because or the paper size limitations.

In the third level or magnitude of resolution (FIG. 16). a further quadrant division is applied, resulting in sixty-four (64) mapping areas of of $64^{\circ} \times 64^{\circ}$. As the projection is beginning to represent a large plurality of mapping areas, the filenames have been ommitted However, it should be understood that the filename assigned to a respective file in this and subsequent degrees of resolution, can easily be calculated by following the previously described file naming operation. In this projection, it can be seen that 40 mapping areas or files are not used, resulting in 24 files which contain the digital mapping data of this resolution. Note that the observed window, and used files again correlates to the entries in the chart. Furthermore, it can be seen that the height or "relative viewing position" is at 4,416 statute miles above the earth.
Further quadrant divisions and the corresponding data can be seen in the FIGS. 17-19 and the chart. From the foregoing discussions, prior teachings, and data from the chart, one skilled in the art should be able to quickly appreciate that a mapping system can be constructed which can provide digital maps corresponding to a plurality of resolutions, of any geographical area of the world.

The chart can now be used to observe the tremendous advantage provided by the $512^{\circ} \times 512^{\circ}$ projection. In the second column of the chart, one can view the sizes of the mapping area divisions which are produced as a result of the continued quadrant division of the $512^{\circ} \times 512^{\circ}$ projection. One skilled in the mapping art will be able to fully appreciate that the resultant map-
ping area divisions exactly correspond to well settled and widely used mapping area formats.
Having described all of the important operations of the present invention, the following further conclu5 sions, comments and teachings can be made.

With the mapping system of the present invention, the mapping data are structured at each magnitude or level into windows, frames or tiles representing subdivisions or partitions of the surface area at the specified magnitude. The windows, frames or tiles of all magnitudes for whatever resolution are structured to receive substantially the same amount or quantity of mapping data for segmented visual presentation of the mapping data by window.

As a further improvement, the lapping system of the present invention can further store and organize mapping data into attributed or coded geographical and cultural features according to the classification and level or resolution or magnitude for presentation on the map display. Several examples of this was previously discussed with regard to the use of the filename extension. If this further improvement is used, the computer can be programmed and arranged for managing and accessing the mapping data, and excluding or including coded features in tiles of a particular magnitude according to the resolution and density of mapping data appropriate to the particular magnitude of the window. The selective display of attributed geographical and cultural features according to resolution maintains or limits the mapping data entered in each tile to no greater than a specified full complement of mapping data for whatever magnitude.

In reviewing the file naming operations which were described, one can see that the global map generating system data base structure relates tiles of the same magnitude by tile position coordinates that are keyed to the control corner of each tile and maintained in the name of the "tile-file". Continuity of same scale tiles is maintained during scrolling between adjacent or neighboring tiles in any direction. The new data base structure also relates tiles of different magnitudes by vertical lineage through successive magnitudes. Each tile of a higher magnitude and lower resolution is an "ancestor tile" encompassing a lineage of "descendant tiles" of 5 lower magnitude and high resolution in the next lower magnitude. Thus the present invention permits accessing, displaying and presenting the structured mapping data by tile, by scrolling between adjacent or neighboring tiles of different magnitude in the same vertical lineage for varying the resolution.

In its simplest form the coordinate system is Cartesian, but the invention contemplates a variety of virtual tile manifestations of windowing the mapping data at each magnitude: for example: tilting the axes; scaling one axis relative to another; having one or both axes logarithmic; or rendering the coordinate space as nonEuclidean all together.
When dealing with vector or point information and gridded data, the most common method is to describe individual points as an $x-y$ offset from the control corner of the tile. In this way the mapping data exist as pre-processed relative points on a spherical surface in a de-projected space. The mapping data can then be projected at the user interface with an application program. When projected, all data ultimately represent points of latitude and longitude. Tiles may also contain mapping data as variable offsets of arc in the x and y directions. The tile header may carry an internal descriptor defin-
ing what type of mapping data is contained. The application or display program may then decode and project the data to the appropriate latitude or longitude positions.

The map generating system contemplates storing analog mapping data in electronic mapping frames in which the raw analog data would be scanned and converted digitally to the tile structure and then later accessed and projected for the purpose of displaying continuous analog mapping data.
In the preferred example embodiment, the digital mapping data are structured by window or tile in a substantially rectangular configuration encompassing defined widths and heights in degrees of latitude and longitude for each magnitude. The mapping data representing each magnitude or level are stored in a deprojected format according to mapping on an imaginary cylindrical surface. For display of the maps, however, the data base manager accesses and presents the tiles in a projected form, according to the real configuration of the mapped surface, by varying the aspect ratio of latitude to longitude dimensions of the tiles according to the absolute position of the window on the surface area.

For example, for a spherical or spheroidal globe having an equator and poles, such as the earth, the mapping data are accessed and displayed by aspecting or narrowing the width in the west-east dimension of the tiles of the same magnitude, while scrolling from the equator to the poles. This is accomplished by altering the width of the tile relative to the height. In the graphics display of each window or tile on the monitor, the tiles are presented essentially as rectangles having an aspect ratio substantially equal to the center latitude encompassed by the tile. Thus, the width of the visual display windows is corrected in two respects. First, the overall width is corrected by aspecting to a narrower width, during scrolling in the direction of the poles, and to a wider width during scrolling in the direction of the equator. Second, the width of the tile is averaged to the center latitude width encompassed by the tile throughout the tile height to conserve the rectangular configuration. Alternatively, or in addition, further compensation may be provided by increasing the number of degrees of longitude encompassed by the tiles during scrolling from the equator to the poles to compensate for the compound curvature of the globe.

A feature and advantage of this new method and new system of map projection are that the dramatic and perverse distortion of the globe near the poles, introduced by the traditional and conventional Mercator projection is substantially eliminated. According to the invention, the compensating aspect ratio of latitudinal to longitudinal dimension of aspecting is a function of the distance from the equator, where the aspect ratio is one, to the poles where the aspect ratio approaches zero, all as described for example in Elements of Cartography, 4th edition. John Wiley \& Sons (1978) by Arthur Robinson, Randall Sale and Joel Morrison.
The new system contemplates "polar compression" (FIG. 20) in the following manner. Starting at 64 degrees latitude, the width of each tile doubles for every eight degrees of latitude. From 72 degrees to 80 degrees latitude, there are 4 degrees of longitude for 1 degree of latitude. From 80 degrees to 88 degrees latitude, it becomes eight to one, and from 88 degrees to the pole ( 90 degrees) it becomes 16 to one (see illustration of polar compression). (FIG. 20)

Another feature and advantage of the way in which the new map system and new projection handle polar mapping data are in the speed required to access and display polar data. The new polar compression method drastically minimizes tile or window seeks and standard I/O time. Also, without compressing the poles, the Creation/Edit Software would have to work on increasingly narrow tiles as the aspect ratio approached zero at the poles.

The invention embodies an entirely new cartographic organization for an automated atlas of the earth or other generally spherical or spheroidal globe with 360 degrees of longitude and 180 degrees of latitude, an equator and poles. The digital mapping data for the earth is structured on an imaginary surface space having 512 degrees of latitude and longitude. The imaginary 512 degree square surface represents the zero magnitude or root node at the highest level above the earth for a hierarchial type quadtree data base structure. In fact, the 512 degree square plane at the zero magnitude encompasses the entire earth in a single tile. The map of the earth, of course, fills only a portion of the root node window of 512 degrees square, and the remainder may be deemed imaginary space or "hyperspace".

In the preferred example embodiment from a zero magnitude virtual or imaginary space 512 degrees square, the data base structure of the global map generating system descends to a first magnitude of mapping data in four tiles, windows or quadrants, each comprising 256 degrees of latitude and longitude. Each quadrant represents mapping data for one-quarter of the earth thereby mapping 180 degrees of longitude and 90 degrees of latitude in the imaginary surface of the tile or frame comprising 256 degrees square, leaving excess imaginary space or "hyperspace". In the second magnitude, the digital mapping data are virtually mapped and stored in an organization of 16 tiles or windows each comprising 128 degrees of latitude and longitude.

The map generating system supports two windowing formats, one based on the binary system of the 512 degree square zero magnitude root node with hyperspace and the other based on a system of a 360 degree square root node without hyperspace. A feature and advantage of the virtual 512 degree data base structure with hyperspace are that the tiles or windows to be displayed at respective magnitudes are consistent with conventional mapping scale divisions, for example, those followed by the U.S. Geological Survey (USGS). Defense Mapping Agency (DMA). National Aeronautics and Space Administration (NASA) and other government mapping agencies. Thus, typical mapping scale divisions of the USGS and military mapping agencies include scale divisions in the same range of $1 \mathrm{deg}, 30$ minutes. 15 minutes. 7.5 minutes of arc on the earth s surface. This common subdivision of mapping space does not exist in a data structure based on a 360 degree model without hyperspace (see chart).

Thus, according to the present invention, the world is represented in an assemblage of magnitudes, with each magnitude divided into adjacent tiles or windows on a virtual or imaginary two-dimensional plane or cylinder. At higher magnitudes the quadtree tiles of mapping data do not fill the imaginary projection space. However, from the seventh magnitude down, the mapping data fills a virtual closed cylinder, and no hyperspace exists at these levels.

In the preferred example embodiment the invention (running on a 16 bit computer) has sixteen magnitudes

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or levels (with extensions to 20 levels) representing sixteen altitudes or distances above the surface of the earth. At the lowest (16th) magnitude of highest resolution and closest to the earth, the data base structure contains over one billion tiles or windows (excluding hyperspace), each encompassing a tile height of approximately one half statute mile. At this level of resolution, one pixel on a monitor of 480 pixels in height represents approximately 6 feet on the ground. Mapping data are positioned within each tile using a 0 to 1023 offset coordinate structure, resulting in a data resolution of approximately 3 feet at this level of magnitude (see chart). The contemplated 20th magnitude tile or window height is approximately 175 feet, which results in a pixel resolution of about 4 inches on a monitor of 480 pixels in height and a data resolution of about 2 inches, when utilizing the 0 to 1023 offset coordinate structure. Alternatively, the map-generating system contemplates an extended offset from 10 bits ( 0 to 1023) to an offset of 16 bits ( 0 to 65,535 ). In this case, the extended 20th magnitude results in a data resolution of 3 hundredths of an inch.
For still more resolution, the map generating system contemplates 32 magnitudes on a 32 bit computer and representing 32 altitudes or distances about the surface of the earth. Each level of magnitude may define mapping data within each tile using a 32 bit offset coordinate structure, thereby giving relative mathematical accuracy to a billionth of an inch. In all practicality, 20 separate magnitudes or levels are more than sufficient to carry the necessary levels of resolution and accuracy.
The new invention provides users with the ability graphically to view mapping data from any part of the world-wide data base graphically on a monitor, either by entering coordinates and a level of zoom (or magnitude) on the keyboard, or by "flying" to that location in the "step-zoom" mode using consecutive clicks of the mouse or other pointing device. Once a location has been chosen (this point becomes the user-defined screen center). the mapping software accesses all adjacent tiles needed to fill the entire view window of the monitor and, then, projects the data to the screen. Same scale scrolling is accomplished by simply choosing a new screen center and maintaining the same magnitude.
Vertical zooming up or down is accomplished by choosing another magnitude or level from the menu area with the pointing device or by directly entering location and magnitude on the keyboard. An advantage of this vertical lineage of tiles organized in a quadtree structure is that it affords the efficient and easily followed zooming continuity inherent in the present invention. Further discussion of such quadtree data organization is found in the article. "The Quadtree and Related Hierarchical Data Structures", by Hannan Samet, Computer Surveys. Volume 16 , No. 2, (June 1984), Pages 187 et seq.
The map-generating system also supports many types of descriptive information such as that contained in tabular or relational data bases. This descriptive information can be linked to the mapping data with a latitude and longitude coordinate position but may need to be displayed in alternate ways. Descriptive information is better suited for storage in a relational format and can be linked to the map with a "spatial hook".
In summary, the present invention provides a new 65 automated world atlas and global map generating system having a multi-level hierarchial quadtree data base structure and a data base manager or controller which
accessing and displaying or presenting mapping data for different positions of a selected magnitude by
scrolling between adjacent or neighboring windows of a same magnitude in predetermined north, south, each and west directions;
and accessing and displaying or presenting mapping data for different selected magnitudes having different resolutions by zooming between windows of different magnitudes in a same vertical lineage.
2. The method of claim 1 further comprising:
organizing said mapping data of said surface area by degrees of latitude and longitude;
structuring each said window of mapping data to represent a substantially rectangular surface area configuration encompassing defined degrees of latitude and longitude for each magnitude, and storing the mapping data for each magnitude in a vertical Mercator projection format;
accessing and presenting said windows of mapping data in a corrected or compensated projection format departing from said Mercator projection format according to a real configuration of said surface area, by varying an aspect ratio of latitude to longitudinal dimensions of each window according to a coordinate position of said window with respect to a coordinate layout of said surface area.
3. The method of claim 2 wherein said surface area comprises a spherical or spheroidal globe having an equator and poles, said method comprising the further steps of:
accessing and presenting mapping data in a corrected projection format by aspecting or narrowing, in a direction from an equator to pole, the width or latitudinal dimension of windows, of a same magnitude, which encompass the same number of degrees of latitude and longitude;
and periodically increasing a number of degrees of longitude encompassed by said windows in said direction from equator to pole to compensate for compound curvature of said globe.
4. The method of claim 1 wherein said surface area comprises a generally spherical or spheroidal globe with 360 degrees of longitudinal, 180 degrees of latitude. and an equator and poles, said method comprising the further steps of:
relating windows of different magnitudes by vertical lineage in a hierarchical quadtree database structure, by successively partitioning or subdividing ancestor windows of a vertical lineage into four descent windows or quadrants at a next lower magnitude or level, and incorporating additional records of features in said descendant windows to incorporate mapping data for a next higher resolution.
5. The method of claim 4 wherein said hierarchical quadtree database structure comprises at least sixteen degrees of magnitudes or levels.
6. The method of claim 4 comprising the further steps of:
mapping and storing mapping data for said globe in a virtual Mercator projection format representing an imaginary surface having 512 degrees of longitude and latitude comprising a zero magnitude or root node of said hierarchical quadtree database structure;
mapping and storing a first degree or highest magnitude of mapping data in four windows or quadrants each comprising 256 degrees of longitude and latitude, each window of said first degree of magnitude comprising mapping data for one quarter of
said globe thereby mapping 180 degrees of surface area longitude and 90 degrees of surface area latitude in said imaginary surface of 256 degrees of longitude and latitude and leaving excess imaginary space;
mapping and storing a second degree of magnitude of mapping data in sixteen windows each comprising 128 degrees of longitude and latitude of said imaginary surface, each window of said second degree of magnitude comprising mapping data for a further subdivision or partition of said globe;
and mapping and storing third through twelfth degrees of magnitude thereby forming additional levels of a hierarchical quadtree database structure so that an eleventh magnitude comprises windows encompassing 15 seconds of latitude and a twelfth magnitude comprises windows encompassing seven and a half seconds of latitude;
whereby, as a result of the foregoing, windows of said electronic map at respective magnitudes or levels are consistent with conventional mapping scale divisions.
7. The method of claim 6 wherein said hierarchical quadtree database structure comprises sixteen degree of magnitudes or levels including a sixteenth magnitude comprising over 1.4 billion windows, each encompassing approximately a fraction of a minute of a degree of latitude.
8. The method of claim 6 wherein each said window corresponds to a trapezoidal surface area configuration.
9. The method of claim 6 comprising the step of floating mapping data records of selected features from a window of one magnitude to a window of the same vertical lineage in another magnitude.
10. The method of claim 6 comprising the further steps of: generating analog mapping data, structuring said analog mapping data according to a same format as digital mapping data, and overlaying and presenting said digital mapping data and analog mapping data during generation, display and presentation of an electronic map.
11. The method of claim 6 comprising the further step of selectively filling said windows with mapping data so that some windows contain a full complement of mapping data appropriate to a degree of mapping resolution being afforded at said magnitude, and other windows, each of which correspond to a subdivision of surface area containing few or no geographical or cultural features, contain less than a full complement of mapping data.
12. The method of claim 6 comprising the further steps of:
accessing and presenting mapping data in a corrected projection format by aspecting or narrowing, in a direction from an equator to pole, a width or latitudinal dimension of windows, of a same magnitude, which encompass the same number of degrees of latitude and longitude;
and periodically increasing a number of degrees of longitude encompassed by said windows in said direction from equator to pole to compensate for a compound curvature of said globe.
13. The method of claim 12 comprising the further steps of accessing and presenting mapping data in corrected projection format, with each window having a width substantially equal to a center latitude width of said window throughout said window, so that said window is of rectangular configuration.

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14. An electronic map generating system including a digital computer, a mass storage device, a display monitor, graphics controller, and system software for structuring, managing, controlling and displaying digital mapping data for a surface area having cultural and geographical features, said system comprising:
a database structure comprising a hierarchical database structure programmed and arranged for organizing said digital mapping data into a hierarchy of a plurality of successive magnitudes or levels for presentation of mapping data with variable resolution, each magnitude for presentation of said mapping data with a different degree of mapping resolution from a first or highest magnitude of lowest resolution to a last or lowest magnitude of lowest resolution to a last or lowest magnitude of highest resolution, and for structuring said digital mapping data at each magnitude into a plurality of windows, frames or files representing subdivisions or partitions of said surface area, said windows of a respective magnitude including mapping data which are appropriate to a degree of mapping resolution being afforded at said magnitude while excluding mapping data which are not appropriate to said degree of mapping resolution, at least a portion of said windows of all magnitudes being structured to receive substantially a same predetermined amount of mapping data for segmented presentation of said mapping data by window, said mapping data being organized into coded records of geographical and cultural features within each window;
a database manager or controller programmed and arranged for managing said mapping data by magnitude or level by excluding or including coded records of features in-each window of a particular magnitude according to a resolution and density of mapping data appropriate to the particular magnitude of said each window, and maintaining a quantity of mapping data entered in each window to no greater than a specified full complement whatever the magnitude of the window;
said database structure being programmed to relate windows of a same magnitude by position coordinates or names, and to structure windows of a same magnitude with overlap of mapping data between adjacent or neighboring windows of a magnitude to achieve display continuity during generation, display and presentation of an electronic map, and to relate windows of different magnitude by vertical lineage through successive magnitudes, each window of a higher magnitude and lower resolution being an ancestor window of a plurality of descendant windows of lower magnitude and higher resolution in a next lower magnitude;
said database manager being programmed to access and display or present mapping data for different positions of a selected magnitude by scrolling between adjacent or neighboring windows of a same magnitude in predetermined north, south, east and west directions, and being programmed to access and display or present mapping data for different magnitudes having different resolutions by zooming between windows of different magnitudes in a same vertical lineage.
15. The system of claim 14 wherein said hierarchical 6 database structure is programmed to organize said mapping data by degrees of latitude and longitude and to structure each window of mapping data to represent a
substantially rectangular surface area configuration encompassing predetermined degrees of latitude and longitude, said windows for each magnitude being stored in virtual Mercator projection format, said database manager being programmed to access and present windows of mapping data in a corrected or compensated projection format departing from Mercator projection format according to a real configuration of said surface area by varying an aspect ratio of latitude and longitude dimensions of each window according to a coordinate position of said each window with respect to a coordinate layout of said surface area.
16. The system of claim 15 wherein said surface area comprises a spherical or spheroidal globe having an equator and poles, and wherein said database manager is programmed to access and present mapping data in a corrected projection format by aspecting or narrowing, in a direction from an equator to pole, the width or latitudinal dimension of windows, of a same magnitude, which encompass the same number of degrees of longitude, said database manager being further programmed to periodically increase a number of degrees of longitude encompassed by said windows in said direction from equator to pole to compensate for compound curvature of said globe.
17. The system of claim 16 wherein said hierarchical database structure comprises a hierarchical quadtree database structure successively partitioning or subdividing ancestor windows of a vertical lineage into four descendant windows or quadrants at a next lower magnitude or level, and incorporating additional coded records of features in said descendant windows to incorporate mapping data for a next higher resolution.
18. The system of claim 17 wherein said database structure is programmed and arranged to store the mapping data in a virtual Mercator projection representing an imaginary surface having 512 degrees of longitude and latitude comprising a zero magnitude or root node of said hierarchical quadtree database structure, wherein a first degree or first magnitude of mapping data comprises four windows, each window of said first magnitude comprising mapping data for one quarter of said globe on an imaginary surface area of 256 degrees of longitude and latitude, said hierarchical quadtree database structure comprising, in addition to first through tenth magnitudes each having windows which are predetermined subdivisions of said imaginary surface having 512 degrees of longitude and latitude, at least an eleventh magnitude having windows encompassing 15 minutes of latitude, and a twelfth magnitude having windows encompassing 7.5 minutes of latitude, so that windows of a resultant electronic map at respective said eleventh and twelfth magnitudes or levels are consistent with conventional mapping scale divisions.
19. The system of claim 18 wherein said hierarchical quadtree database structure comprises at least 16 degrees of magnitudes or levels, said sixteenth magnitude comprising over 1.4 billion windows, each encompassing degrees of latitude of approximately a fraction of a second of a degree.
20. The system of claim 19 further comprising a database of digital mapping data selectively entered in said database structure, such that some of said windows contain a full complement of mapping data appropriate to a degree of mapping resolution being afforded at said magnitude, and other windows, each of which correspond to a subdivision of surface area containing few or
no geographical or cultural features, contain less than a full complement of mapping data.
21. The system of claim 19 further comprising a database of analog data structured according to a same format as said digital data, and means for overlaying said digital and analog data for electronic map presentation.
22. An electronic map generating system for generating reproductions of a map with selectable degrees of mapping resolution, said map generating system comprising:
database means storing a plurality of computer files containing mapping data corresponding to respective surface areas of a mapping surface, wherein said plurality of computer files is organized into a plurality of successive magnitudes, each magnitude for presentation of said mapping data with a different degree of mapping resolution from a first or highest magnitude with lowest resolution to a last or lowest magnitude with highest resolution, files of a respective magnitude including mapping data which are appropriate to a degree of mapping resolution being afforded at said respective magnitude while excluding mapping data which are not appropriate to said degree of mapping resolution, and wherein a predetermined file naming procedure is utilized to assign, to each respective computer file, a unique filename which:
relates said respective computer file to all other computer files having mapping data corresponding to a same magnitude or degree of mapping resolution; and
relates said respective computer file to any computer file comprising mapping data corresponding to a same surface area of a mapping surface as said respective computer file; and
database manager means for accessing said plurality of computer files using said predetermined file naming procedure, to generate a reproduction of a selected area of a map at a selected degree of mapping resolution.
23. An electronic map generating system as claimed in claim 22,
wherein each said unique filename is represented by a value contained in a plurality of bits, and
wherein said predetermined file naming procedure: utilizes a first predetermined subset of said plurality of bits to relate said respective files having mapping data corresponding to a same magnitude or degree of mapping resolution; and
utilizes a second predetermined subset of said plurality of bits to relate said respective computer file to any computer file comprising mapping data corresponding to a same surface area of a mapping surface as said respective computer file.
24. An electronic map generating system as claimed in claim 23, wherein said unique filename also includes geographical information which can be used to relate a geographical coordinate position of a respective computer file with respect to a coordinate layout of surface areas of said mapping surface.
25. An electronic map generating system as claimed in claim 22,
wherein an assignment of said unique filenames using 65 said predetermined file naming procedure results in said respective computer files of said plurality to be related in a quadtree database structure.
26. An electronic map generating system as claimed in claim 25, wherein the respective area of a mapping surface covered within the computer files of consecutive magnitudes or degrees of mapping resolution changes at a predetermined rate in that, when a computer file at a reference magnitude or degree of mapping resolution contains mapping data corresponding to an $\mathrm{N} \times \mathrm{N}$ area of a mapping surface (where N is a real number, and is associated with one of the conventional degree ${ }^{\circ}$, minute ${ }^{\prime}$, or second " mapping scale divisions), then a computer file at a next consecutive magnitude having a higher degree of mapping resolution contains mapping data corresponding to an $(\mathrm{N} / 2) \times(\mathrm{N} / 2)$ area of said mapping surface.
27. An electronic map generating system as claimed in claim 26, wherein the value of N at said reference magnitude or degree of mapping resolution, corresponds to one of the following values: $512^{\circ}, 256^{\circ}, 128^{\circ}$, $64^{\circ}, 32^{\circ}, 16^{\circ}, 8^{\circ}, 4^{\circ}, 2^{\circ}, 1^{\circ}, 30^{\prime}, 15^{\prime}, 7.5^{\prime}, 3.75^{\prime}, 1.875^{\prime}$, $0.9375^{\prime}$ and $0.46875^{\prime}$.
28. A method for providing an electronic map generating system for generating reproductions of a map with selectable degrees of mapping resolution, said method comprising the steps of:
storing a plurality of computer files containing mapping data corresponding to respective surface areas of a mapping surface, wherein said plurality of computer files is organized into a plurality of successive magnitudes, each magnitude for presentation of said mapping data with a different degree of mapping resolution from a first or highest magnitude with lowest resolution to a last or lowest magnitùde with highest resolution, files of a respective magnitude including mapping data which are appropriate to a degree of mapping resolution being afforded at said respective magnitude while excluding mapping data which are not appropriate to said degree of mapping resolution, and wherein a predetermined file naming procedure is utilized to assign, to each respective computer file, a unique filename which:
relates said respective computer file to all other computer files having mapping data corresponding to a same magnitude or degree of mapping resolution; and
relates said respective computer file to any computer file comprising mapping data corresponding to a same surface area of a mapping surface as said respective computer file; and
accessing said plurality of computer files using said predetermined file naming procedure, to generate a reproduction of a selected area of a map at a selected degree of mapping resolution.
29. A method as claimed in claim 28,
wherein each said unique filename is represented by a value contained in a plurality of bits, and
wherein said predetermined file naming procedure;
utilizes a first predetermined subset of said plurality of bits to relate said respective computer file to all other computer files having mapping data corresponding to a same magnitude or degree of mapping resolution; and
utilizes a second predetermined subset of said plurality of bits to relate said respective computer file to any computer file comprising mapping data corresponding to a same surface area of a mapping surface as said respective computer file.

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30. A method as claimed in claim 29, wherein said unique filename also includes geographical information which can be used to relate a geographical coordinate position of a respective computer file with respect to a coordinate layout of surface areas of said mapping surface.
31. A method as claimed in claim 28,
wherein an assignment of said unique filenames using said predetermined file naming procedure results in said respective computer files of said plurality to be related in a quadtree database structure.
32. A method as claimed in claim 31, wherein the respective area of a mapping surface covered within the computer files of consecutive magnitudes or degrees of mapping resolution changes at a predetermined rate in 15
that, when a computer file at a reference magnitude or degree of mapping resolution contains mapping data corresponding to an $\mathrm{N} \times \mathrm{N}$ area of a mapping surface (where $\mathbf{N}$ is a real number, and is associated with one of the conventional degree ${ }^{\circ}$, minute ', or second " mapping scale divisions), then a computer file at a next consecutive magnitude having a higher degree of mapping resolution contains mapping data corresponding to an (N/2) $\times(\mathrm{N} / 2)$ area of said mapping surface.
33. A method as claimed in claim 32, wherein the value of N at said reference magnitude or degree of mapping resolution, corresponds to one of the following values: $512^{\circ}, 256^{\circ}, 128^{\circ}, 64^{\circ}, 32^{\circ}, 16^{\circ}, 8^{\circ}, 4^{\circ}, 2^{\circ}, 1^{\circ}$, $30^{\prime}, 15^{\prime}, 7.5^{\prime}, 3.75^{\prime}, 1.875^{\prime}, 0.9375^{\prime}$ and $0.46875^{\prime}$.

# The M AG IC Project From Vision to Reality 

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#### Abstract

In the MAGIC project, three major components - an ATM internetwork, a distributed, network-based storage system, and a terrain visualization application - were designed, implemented, and integrated to create a testbed for demonstrating real-time, interactive exchange of data at high speeds among distributed resources. The testbed was developed as a system, with special consideration to how performance was affected by interactions among the components. This article presents an overview of the project, with emphasis on the challenges associated with implementing a complex distributed system, and with coordinating a multi-organization collaborative project that relied on distributed development. System-level design issues and performance measurements are described, as is a tool that was developed for analyzing performance and diagnosing problems in a distributed system. The management challenges that were encountered and some of the lessons learned during the course of the three-year project are discussed, and a brief summary of MAGIC-II, a recently initiated follow-on project, is given.


Gigabit-per-second networks offer the promise of a major advance in computing and communications: high-speed access to remote resources, including archives, time-critical data sources, and processing power. O ver the past six years, there have been several efforts to develop gigabit networks and to demonstrate their utility, the most notable being the five testbeds that were supported by ARPA and N ational Science Foundation (NSF) funding: A urora, BLANCA, CASA, Nectar, and VISTA net [1]. E ach of these testbeds comprised a mix of applications and networking technology, with some focusing more heavily on applications and others on networking. The groundbreaking work done in these testbeds had a significant impact on the development of high-speed networking technology and on the rapid progress in this area in the 1990s.

It became clear, however, that a new paradigm for application development was needed in order to realize the full benefits of gigabit networks. Specifically, networkbased applications and their supporting resources. such as data servers, must be designed explicitly to operate effectively in a high-speed networking environment. For example, an interactive application working with remote storage devices must compensate for network delays. The M A GIC project, which is the subject of this article, is the first highspeed networking testbed that was implemented according to this paradigm. The major components of the testbed were considered to be interdependent parts of a system, and wherever possible they were designed to optimize end-

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to-end system performance rather than individual component performance.

The objective of the MAGIC (which stands for "M ultidimensional A pplications and Gigabit Internetwork Consortium") project was to build a testbed that could demonstrate real-time, interactive exchange of data at gigabit-per-second rates among multiple distributed resources. This objective was pursued through a multidisciplinary effort involving concurrent development and subsequent integration of three testbed components:

- An innovative terrain visualization application that requires massive amounts of remotely stored data
- A distributed image server system with performance sufficient to support the terrain visualization application
- A standards-based high-speed internetwork to link the computing resources required for real-time rendering of the terrain
The three-year project began in mid-1992 and involved the participation, support, and close cooperation of many diverse organizations from government, industry, and academia. These organizations had complementary skills and had the foresight to recognize the benefits of collaboration. The principal MAGIC research participants were:
- E arth R esources Observation System D ata C enter, U.S. Geological Survey (EDC) ${ }^{1}$
- Lawrence Berkeley National Laboratory, U .S. D epartment of Energy (LBNL) ${ }^{1}$
- M innesota Supercomputer Center, Inc. (M SCI) ${ }^{1}$
- MITRE Corporation ${ }^{1}$
- Sprint
- SRI International (SRI)¹

[^9]

Figure 1. Planned functionality of the MAGIC testbed.

- U niversity of $K$ ansas (K U ) ${ }^{1}$
- U S WEST Communications, Inc.

Other MAGIC participants that contributed equipment, facilities, and/or personnel to the effort were:

- Army High-Performance Computing Research Center (AHPCRC)
- Battle Command Battle Laboratory, U.S. Army Combined Arms Command (BCBL)
- Digital Equipment Corporation (DEC)
- N ortel, Inc./B ell N orthern R esearch
- Southwestern Bell Telephone
- Splitrock Telecom

This article presents an overview of the MAGIC project with emphasis on the challenges associated with implementing a complex distributed system. Companion articles [2, 3] focus on a LAN/W AN gateway and a performance analysis tool that were developed for the MAGIC testbed. The article is organized as follows. The following section briefly describes the three major testbed components: the internetwork, the image server system, and the application. The third section discusses some of the system-level considerations that were addressed in designing these components, and the fourth section presents some high-level performance measurements. The fifth (affectionately entitled "H erding Cats") and sixth sections describe how this multi-organizational collaborative project was coordinated, and the technical and managerial lessons learned. Finally, the last section provides a brief summary of MAGIC-II, a follow-on project begun in early 1996.

## O verview of the MAG IC Testbed

0ne of the primary goals of the MAGIC project was to create a testbed to demonstrate advanced capabilities that would not be possible without a very high-speed internetwork. MA GIC accomplished this goal by implementing an interactive terrain visualization application, TerraV ision, that relies on a distributed image server system (ISS) to provide it with massive amounts of data in real time. The planned functionality of the MAGIC testbed is depicted in Fig. 1. Currently, TerraVision uses data processed off-line and stored on the ISS. In the future the application will be redesigned to enable real-time image processing as well as real-time terrain visualization (see the last section). N ote that the workstations which house the application, the servers of the ISS, and the "over-the-shoulder" tool (see subsection entitled "The Terrain V isualization A pplication"), as well as those that will perform the online image processing, can reside anywhere on the network.

## The MAGIC Internetwork

The MAGIC internetwork, depicted in Fig. 2, includes six high-speed local area networks (LANs) interconnected by a wide area network (WAN) backbone. The backbone, which spans a distance of approximately 600 miles, is based on synchronous optical network (SONET) technology and provides OC-48 ( $2.4 \mathrm{~Gb} / \mathrm{s}$ ) trunks, and OC-3 (155 $\mathrm{Mb} / \mathrm{s}$ ) and OC-12 ( $622 \mathrm{Mb} / \mathrm{s}$ ) access ports. The LANs are based on asynchronous transfer mode (ATM) technology. Five of the LANs - those at BCBL in Fort Leavenworth, K ansas, EDC in Sioux Falls, South D akota, M SCI in M inneapolis, M innesota, Sprint in O verland Park, K ansas, and U S WEST in M inneapolis, Minnesota - use FORE Systems models A SX-100 and A SX-200 switches with OC-3c and $100 \mathrm{Mb} / \mathrm{s}$ TAXI interfaces. The ATM LAN at KU in Lawrence, K ansas, uses a DEC AN2 switch, a precursor to the DEC GigaSwitch/A TM, with OC-3c interfaces. The network uses permanent virtual circuits (PVCs) as well as switched virtual circuits (SVCs) based on both SPANS, a FORE Systems signaling protocol, and the ATM Forum U ser-N etwork Interface (UNI) 3.0 Q . 2931 signaling stan-


Figure 2. Configuration of the MAGIC ATM internetwork.
dard. The workstations at the MAGIC sites include models from DEC, SGI, and Sun. As part of MAGIC, an AN 2/SONET gateway with an OC-12c interface was developed to link the AN2LAN at KU to the MAGIC backbone [2].

In addition to implementing the internetwork, a variety of advanced networking technologies were developed and studied under MAGIC. A high-performance parallel interface ( HIPPI )/ATM gateway was developed to interface an existing HIPPI network at MSCI to the MAGIC backbone. The gateway is an IP router rather than a network-layer device such as a broadband integrated services digital network (B-ISDN) terminal adapter, and was implemented in software on a high-performance workstation (an SGI Challenge). This architecture provides a programmable platform that can be modified for network research, and in the future can readily take advantage of more powerful workstation hardware. In addition, the platform is general-purpose; that is, it is capable of supporting multiple HIPPI interfaces as well as other interfaces such as fiber distributed data interface (FDDI).

Software was developed to enable UNIX hosts to communicate using Internet Protocol (IP) over an ATM network. This IP/ATM software currently runs on SPARCstations under Sun OS 4.1 and includes a device driver for the FORE SBA series of ATM adapters. It supports PVCs, SPANS, and UNI 3.0 signaling, as well as the "classical" IP and Address Resolution Protocol (ARP) over ATM model [4]. The software should be extensible to other UNIX operating systems, ATM interfaces, and IP/A TM address-resolution and routing strategies, and will facilitate research on issues associated with the integration of ATM networks into IP internets.

In order to enhance network throughput, flow-control schemes were evaluated and applied, and IP/ATM host parameters were tuned. Experiments showed that throughput close to the maximum theoretically possible could be attained on OC-3 links over long distances. To achieve high throughput, both the maximum transmission unit (MTU) and the Transmission Control Protocol (TCP) window must be large, and flow control must be used to ensure fairness and to avoid cell loss if there are interacting traffic patterns $[5,6]$.

## The Terrain Visualization Application

TerraVision allows a user to view and navigate through (i.e., "fly over") a representation of a landscape created from aerial or satellite imagery [7]. The data used by TerraV ision are derived from raw imagery and elevation information which have been preprocessed by a companion application known as TerraF orm. TerraV ision requires very Iarge amounts of data in real time, transferred at both very bursty and high steady rates. Steady traffic occurs when a user moves smoothly through the terrain, whereas bursty traffic occurs when the user jumps ("teleports") to a new position. TerraV ision is designed to use imagery data that are located remotely and supplied to the application as needed by means of a high-speed network. This design enables TerraV ision to provide high-quality, interactive visualization of very large data sets in real time. TerraV ision is of direct interest to a variety of organizations, including the Department of D efense. For example, the ability of a military officer to see a battlefield and to share a common view with others can be very effective for command and control.

Terrain visualization with TerraV ision involves two activities: generating the digital data set required by the appli-


Figure 3. Relationship between tile resolutions and perspective view. (Source: SRI International)
cation, and rendering the image. MAGIC's approach to accomplishing these activities is described below. E nhancements to the application that provide additional features and capabilities are also described.

Data Preparation - In order to render an image, TerraV ision requires a digital description of the shape and appearance of the subject terrain. The shape of the terrain is represented by a two-dimensional grid of elevation values known as a digital elevation model (DEM). The appearance of the terrain is represented by a set of aerial images, known as orthographic projection images (ortho-images), that have been specially processed (i.e., ortho-rectified) to eliminate the effects of perspective distortion, and are in precise alignment with the DEM. To facilitate processing, distributed storage, and high-speed retrieval over a network, the DEM and images are divided into small fixedsize units known as tiles.

Low-resolution tiles are required for terrain that is distant from the viewpoint, whereas high-resolution tiles are required for close-in terrain. In addition, multiple resolutions are required to achieve perspective. These requirements are addressed by preparing a hierarchy of increasingly lower-resolution representations of the DEM and ortho-image tiles in which each level is at half the resolution of the previous level. The tiled, multiresolution hierarchy and the use of multiple resolutions to achieve perspective are shown in Fig. 3.

R endering of the terrain on the screen is accomplished by combining the DEM and ortho-image tiles for the selected area at the appropriate resolution. A s the user travels over the terrain, the DEM tiles and their corresponding ortho-image tiles are projected onto the screen using a perspective transform whose parameters are determined by factors such as the user's viewpoint and field of view. The mapping of a transformed ortho-image to its DEM and the rendering of that image are shown in Fig. 4.

The data set currently used in M A GIC covers a 1200 $\mathrm{km}^{2}$ exercise area of the $N$ ational Training Center at Fort Irwin, California, and is about 1 G pixel in size. It is derived from aerial photographs obtained from the $N$ ational $A$ erial Photography Program archives and DEM data obtained from the U.S. Geological Survey. The images are at approximately 1 m resolution (i.e., the spacing between pixels in the image corresponds to 1 m on the ground). The DEM data are at approximately 30 m resolution (i.e., elevation values in meters are at 30 m intervals).

Software for producing the ortho-images and creating the multiresolution hierarchy of DEM and ortho-image tiles was developed as part of the M A GIC effort. These processes were performed "off-line" on a Thinking $M$ achines Corporation Connection $M$ achine ( $C M-5$ ) supercomputer owned by the AHPCRC and located at M SCI. The tiles were then stored on the distributed servers of the ISS and used by terrain visualization software residing on rendering engines at several locations.


Aerial terrain image is mapped onto elevation model


Elevation data rendered with orthographic image of terrain
Figure 4. M apping an ortho-image onto its digital elevation model. (Source: SRI International)

Image Rendering - TerraVision provides for two modes of visualization: two-dimensional (2-D) and three-dimensional (3-D). The 2-D mode allows the user to fly over the terrain, looking only straight down. The user controls the view by means of a 2-D input device such as a mouse. Since virtually no processing is required, the speed at which images are generated is limited by the throughput of the system comprising the ISS, the network, and the rendering engine.

In the 3-D mode, the user controls the visualization by means of an input device that allows six degrees of freedom in movement. The 3-D mode is computationally intensive, and satisfactory visualization requires both high frame rates (i.e., 15-30 frames/s) and low latencies (i.e., no more than 0.1 s between the time the user moves an input device and the time the new frame appears on the screen).

High frame rates are achieved by using a local very-high-speed rendering engine, an SGI Onyx, with a cache of tiles covering not only the area currently visible to the user, but also adjacent areas that are likely to be visible in the near future. A high-speed search algorithm is used to identify the tiles required to render a given view. For example, as noted above, perspective (i.e., 3-D ) views require higher-resolution tiles in the foreground and lower-resolution tiles in the background. TerraVision requests the tiles from the ISS, places them in memory, and renders the view. Latency is minimized by separating image rendering from data input/output (I/O) so that the two activities can proceed simultaneously rather than sequentially (see the section entitled "D esign Considerations").

Additional Features and Capabilities - TerraVision includes two additional features: superposition of fixed and mobile objects on the terrain, and registration of the user's viewpoint to a map. Both of these features are made
possible by precisely aligning the DEM and imagery data with a world coordinate system as well as with each other.

A number of buildings and vehicles have been created and stored on the rendering engine for display as an overlay on the terrain. The locations of vehicles can be updated periodically by transferring vehicle location data, acquired with a global positioning system receiver, to the rendering engine for integration into the terrain visualization displays. R egistration of the user's viewpoint to a map enables the user to specify the area he wishes to explore by pointing to it, and it aids the user in orienting himself.

In addition, an over-the-shoulder (OTS) tool was developed to allow a user at a remote workstation to view the terrain as it is rendered. The OTS tool is based on a client/server design and uses XW indow system calls. The user can view the entire image on the SGI screen at low resolution, and can also select a portion of the screen to view at higher resolution. The frame rate varies with the size and resolution of the viewed image, and with the throughput of the workstation.

## The Image Server System

The ISS stores, organizes, and retrieves the processed imagery and elevation data required by TerraV ision for interactive rendering of the terrain. The ISS consists of multiple coordinated workstationbased data servers that operate in parallel and are designed to be distributed around a W AN. This architecture compensates for the performance limitations of current disk technology. A single disk can deliver data at a rate that is about an order of magnitude slower than that needed to support a high-performance application such as TerraV ision. By using multiple workstations with multiple disks and a high-speed network, the ISS can deliver data at an aggregate rate sufficient to enable real-time rendering of the terrain. In addition, this architecture permits location-independent access to databases, allows for system scalability, and is low in cost. A lthough redundant arrays of inexpensive disks (RAID) systems can deliver higher throughput than traditional disks, unlike the ISS they are implemented in hardware and, as such, do not support multiple data layout strategies; furthermore, they are relatively expensive. Such systems are therefore not appropriate for distributed environments with numerous data repositories serving a variety of applications.

The ISS, as currently used in M A GIC, comprises four or five UNIX workstations (including Sun SPARCstations, DEC Alphas, and SGI Indigos), each with four to six fast SCSI disks on two to three SCSI host adapters. Each server is also equipped with either a SONET or a TAXI network interface. The servers, operating in parallel, access the tiles and send them over the network, which delivers the aggregate stream to the host. This process is illustrated in Fig. 5. M ore details about the design and operation of the ISS can be found in [8].

## Design C onsiderations

In MAGIC, the single most perspicuous criterion of successful operation is that the end user observes satisfactory performance of the interactive TerraV ision application. W hen the user flies over the terrain, the displayed scene must flow smoothly, and when he teleports to an entirely
different location, the new scene must appear promptly. Obtaining such performance might be relatively straightforward if the terrain data were collocated with the rendering engine. However, one of the original premises underlying the MAGIC project is that the data set and the application are not collocated. There are several reasons for this, the most important being that the data set could be extremely large, so it might not be feasible to transfer it to the user's site. M oreover, experience has shown that in many cases the "owner" of a data set is also its "curator" and may be reluctant to distribute it, preferring instead to keep the data locally to simplify maintenance and updates. Finally, it was anticipated that future versions of the application might work with a mobile user and with fused data from multiple sources, and neither of these capabilities would be practical with local data. Therefore, since the data will not be local, the MAGIC components must be designed to compensate for possible delays and other degradations in the end-to-end operation of the system.

In order to understand system-level design issues, it is necessary to outline the sequence of events that occurs when the user moves the input device, causing a new scene to be generated. TerraV ision first produces a list of new tiles required for the scene. This list is sent to an ISS master, which performs a name translation, mapping the logical address of each tile (the tile identifier) to its physical address (server/disk/location on disk). The master then sends each server an ordered list of the tiles it must retrieve. The server discards the previous list (even if it has not retrieved all the tiles on that list) and begins retrieving the tiles on the new list. Thus, the design for the system comprising TerraV ision, the ISS, and the internetwork must address the following questions:

- H ow can TerraV ision compensate for tiles it needs for the next image but have not yet been received?
- How often should TerraV ision request tiles from the ISS?
-W here should the ISS master be located?
- How should tiles be distributed among the ISS disks?
- How can cell loss be minimized near the rendering site where the tile traffic becomes aggregated and congestion may occur?


## M issing Tiles

Network congestion, an overload at an ISS server, or a component failure could result in the late arrival or loss of tiles that are requested by the application. Several mechanisms were implemented to deal with this problem. First, although the entire set of high-resolution tiles cannot be collocated with the application, it is certainly feasible to store a complete set of lower-resolution tiles. For example, if the entire data set comprises 1 Tbyte of high-resolution tiles, then all of the tiles that are five or more levels coarser would occupy less than 1.5 M byte, a readily affordable amount of local storage. If a tile with resolution at, say, level 3 is requested but not delivered in time for the image to be rendered, then, until the missing level-3 tile arrives, the locally available coarser tile from level 5 would be


Figure 5. Schematic representation of the operation of the ISS. (Source: Lawrence Berkeley National Laboratory)
used in place of the 16 level- 3 tiles. This substitution manifests itself by the affected portion of the rendered image appearing "fuzzy" for a brief period of time. Temporary substitution of low-resolution tiles for high-resolution tiles is particularly effective for teleporting because that operation requires a large number of new tiles, so it is more likely that one or more will be delayed.

Second, TerraVision attempts to predict the path the user will follow, requesting tiles that might soon be needed, and assigning one of three levels of priority to each tile requested. Priority-1 tiles are needed as soon as possible; the ISS retrieves and dispatches these first. This set of tiles is ordered by TerraV ision, with the coarsest assigned the highest priority within the set. The reasons are:

- The rendering algorithm needs the coarse tiles before it needs the next-higher-resolution tiles.
- There are fewer tiles at the coarser resolutions, so it is less likely that they will be delayed.
The priority-2 tiles are those that the ISS should retrieve but should transmit only if there are no priority-1 tiles to be transmitted; that is, priority- 2 tiles are put on a lowerpriority transmit queue in the I/O buffer of each ISS server. (ATM switches would be allowed to drop the cells carrying these tiles.) Priority-3 tiles are those that should be retrieved and cached at the ISS server; these tiles are less likely to be needed by TerraV ision. Note that there is a trade-off between "overpredicting" - requesting too many tiles - which would result in poor ISS performance and high network load, and "underpredicting," which would result in poor application performance.

Finally, a tile will continue to be included in Terra$V$ ision's request list if it is still needed and has not yet been delivered. Thus, tiles or tile requests that are dropped or otherwise "lost" in the network will likely be delivered in response to a subsequent request from the application.

## Frequency of Requests

A nother trade-off pertains to the frequency at which TerraV ision sends its request list to the ISS. If the interval between requests is too large, then some tiles will not arrive when needed, resulting in a poor-quality display; in addition, the ISS will be idle and hence not used efficiently. On the other hand, if the interval is too short, then the request list might contain tiles that are currently in transit from servers to the application; this would result in poor ISS performance and redundant network traffic. F or a typical MAGIC configuration, the interval between requests is currently set at 200 ms , a value that was found empirically to yield satisfactory performance. This value is based roughly on the measured latency of the ISS (about 100 ms ) and on the estimated time required for a tile request to travel through the network from the TerraV ision host to the ISS master and then to the most distant ISS server, plus the time for the tile itself to travel back to the host (perhaps a total of 50 ms ). Additional measurements and analysis are needed to more precisely determine the appropriate request frequency as a function of the performance and location of system components and of network parameters.

## Location of ISS M aster

Since tile requests flow from TerraV ision to the ISS master and thence to the servers themselves, the time for delivering the requests to the servers is minimized when the master is collocated with the TerraVision host. H owever, locating the master with the host is neither desirable nor practical for several reasons. The master is logically part of the ISS; therefore, its location should not be constrained by the application. Also, an ISS may be used with several applications concurrently, by multiple simultaneous users of a particular application, or by a user whose host may be unable to support any ISS functionality (e.g., a mobile user). M oreover, replication of the master would introduce problems associated with maintaining consistency among multiple masters when the ISS is in a read/write environment, as it would be when real-time data are being stored on the servers.

To first order, the delivery time of tile requests is limited by the time $\tau$ for a request to travel from TerraV ision to the ISS server most distant from the TerraV ision host. $H$ ence, if the master is approximately on the path from the TerraV ision host to that server, then $\tau$ will not be much greater than when the master and host are collocated. Furthermore, in the current M A GIC testbed, $\tau$ is much smaller than the sum of the disk latency and the network transit time. In other words, there is considerable freedom in choosing the location of the ISS master. Satisfactory system performance has been demonstrated, for example, with the TerraV ision host in K ansas City, the I SS master in Sioux Falls, and servers in M inneapolis and Lawrence. Of course, this conclusion might change if faster servers reduce ISS Iatency considerably, or the geographic span of the network were substantially larger.

## Distribution of Tiles on ISS Servers

The manner in which data are distributed among the servers determines the degree of parallelism and hence the

> For a typical MAGIC configuration, the interval between requests is currently set at 200 ms, a value that was found empirically to yield sa tisfa ctory performance.
aggregate throughput which can be obtained from the ISS. The data placement strategy depends on the application and is a function of data type and access patterns. For example, the retrieval pattern for a database of video clips would be quite different from that for a database of images. A strategy was developed for a terrain visualization type of application that minimizes the retrieval time for a set of tiles: the tiles assigned to a given disk are as far apart as possible in the terrain in order to maximize parallelism by minimizing the probability that tiles on a request list are on the same disk; and on each disk, tiles that are near each other in the terrain are placed as close as possible to minimize retrieval time. A lthough this was shown to be an optimal strategy for terrain path-following as in TerraV ision [9], it was subsequently shown that ISS performance with random placement of tiles was only slightly worse. This was partly because tile retrieval time is much less than the latency in the ISS servers and network transit time, and is therefore not currently a significant factor in overall performance. R andom placement is simpler to implement and is expected to be satisfactory for many other applications. H owever, as discussed for the location of the ISS master, this conclusion may have to be revisited if the performance or the geographic distribution of system components changes significantly.

## Avoiding Cell Loss

When initially implemented, the M A GIC internetwork exhibited very low throughput in certain configurations. One cause of the low throughput was found to be mismatches between the burst rates of components in the communications path. Examples of such rate mismatches were:

- An OC-3 workstation interface transmitting cells at full rate across the network to a 100 Mb b TAXI interface on another workstation
- Two or more OC-3 input ports at an ATM switch sending data to the same OC-3 output port
A mismatch, coupled with small buffers at the output ports of ATM switches, caused cells to be dropped, which in turn resulted in the retransmission of entire TCP packets, exacerbating the problem. In some cases the measured useful throughput was less than one percent of the capacity of the lower speed line.

Previously it was noted that in many cases a large M TU can increase throughput. However, once again there is a trade-off. A s the M TU size is increased, the number of ATM cells needed to carry the M TU increases. The probability that one or more cells from the MTU will be dropped by the network therefore increases, which in turn increases the probability that the M TU will have to be retransmitted, thus possibly decreasing the effective throughput. Flow-control techniques together with Iarge switch buffers and proper choice of protocol parameters did provide satisfactory performance. Nevertheless, the overriding conclusions are that the parameters of the entire end-to-end system, not just those of a single host or switch, must be tuned, each direction of the data path must be evaluated separately, and every component in each direction of the data path must be considered in the evaluation.

## Performance

This section presents highlights of systemlevel performance issues and measurements of the MAGIC testbed. The input data rates that are needed to support the TerraVision application are calculated first, to provide the context for the subsequent discussion. Then the data rates that the network, the ISS, and the application host can actually support are described. Finally, a diagnostic tool that was developed to help analyze system performance is explained. M ore detailed information about all of the above topics can be found in [3, 5, 6 , 10].

TerraV ision is used in one of two modes, flyover or teleport, and the characteristics of the data flow for the two modes are quite different. Flyover requires a relatively steady flow over a relatively long period of time (many seconds), whereas teleport requires a large burst of data but occurs relatively infrequently. Quantitative requirements can be estimated as follows. A high-resolution full-screen display comprises about 100 tiles, each tile containing $128 \times 128$ pixels with 24 bits of color information, or approximately 0.4 Mb . If 10 new tiles are needed for a typical frame update during flyover, then at 30 frames/s, the average data rate is

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(30 frames/s) x (10 tiles/frame) x (0.4 M b/tile)
    \approx 120 M b/s
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at the application level in the host. Protocol overhead might add approximately 15 percent to this value, resulting in a line rate of about $140 \mathrm{M} \mathrm{b} / \mathrm{s}$. For a teleport, the burst rate is considerably higher because the entire screen must be repainted within, say, a quarter of a second after the user selects the new location. If the total latency between the instant the user enters the selection and the instant the first bit of the first tile arrives at the TerraV ision host is 150 ms , then the full screen of data must be transferred in the remaining (250-150) $=100 \mathrm{~ms}$, and the capacity needed to support the transfer is
( 100 tiles) $\times(0.4 \mathrm{M} \mathrm{b} /$ tile $) /(0.1 \mathrm{~s}) \approx 400 \mathrm{M} \mathrm{b} / \mathrm{s}$
at the application level, or about $450 \mathrm{Mb} / \mathrm{s}$ on the transmission line.

The line capacity needed near the TerraV ision host site can be determined from these required rates and from the end-to-end throughput that can be attained in the network. M easurements on the MAGIC network showed that if the M TU and the TCP window sizes were large enough, and if flow control were used, then end-to-end TCP rates corresponding to about 80 percent of the line rate could be sustained; this is about $120 \mathrm{Mb} / \mathrm{s}$ on an OC-3 line. Thus, a flyover would completely fill a single OC-3 line, so in practice two lines are needed to allow for possible degradations and for variations around the average rate derived above. Similarly, one OC-12 or four OC-3 lines are needed to support a low-response-time teleport. Lower line capacity on the path near the host would degrade the response time (although the degradation would be less than linear because of the additive factor of ISS latency). In summary, the equivalent of two OC-3 lines into the host should give satisfactory flyover performance and a teleport response time less than 0.5 s , but more capacity is needed to reduce the response time and to provide some cushion for contention near the host site.


Figure 6. Timing data from a configuration with two ISS servers. (Source: L aurence Berkeley National Laboratory)

The next question is, "H ow many ISS servers are needed to support the application?" Early measurements of a variety of workstations configured as ISS servers showed that a typical SCSI disk delivered data at a steady rate of about $20 \mathrm{Mb} / \mathrm{s}$; a single SCSI adapter with multiple disks could provide about $60 \mathrm{Mb} / \mathrm{s}$; and a workstation with multiple adapters could deliver about $80 \mathrm{Mb} / \mathrm{s}$. Additional disks or adapters did not increase throughput - the bottleneck apparently being memory bandwidth - but did increase the probability that the throughput could be sustained by ensuring that the server was not idle. These data indicate that tiles must be distributed over at least five servers to obtain the 400 Mb /s rate needed for good teleport performance.

The data streams from the ISS servers converge at the TerraV ision host, and recent measurements showed that with four servers transmitting to a host with two OC-3 ATM ports, the aggregate application-level throughput was only about $100 \mathrm{Mb} / \mathrm{s}$, and in fact was slightly less than the throughput with a single server. (The peak throughput was about $150 \mathrm{Mb} / \mathrm{s}$, with two input streams.) Cells are apparently being dropped at the ATM interface. This is a serious bottleneck in overall system performance; the host and interface vendors are aware of the problem and are working on a solution.

Clearly, understanding the overall performance of a net-work-based distributed system such as MAGIC is an appreciably more complex undertaking than simply "concatenating" the standalone performance of the individual components because there are interactions among the components. It is important to be able to measure and correlate these interactions in order to understand and predict the performance of the system as a whole. Stated in concrete terms, a problem observed by a user could have a variety of causes. For example, in MAGIC it would be acceptable if low-resolution tiles are used occasionally in place of high-resolution tiles that are delayed or lost in transit (as described in the previous section), but it would be unacceptable if this occurred frequently. If such observable degradation did occur, the cause could be the application host dropping cells, A TM switches dropping cells, excessive delay somewhere in the ISS, Iow ISS throughput because of the way tiles are distributed among servers, processing limitations of the TerraV ision host, or a combination of these and other phenomena.

To aid in pinpointing potential problems, accurately synchronized clocks were deployed at MAGIC sites, many components were instrumented to log traffic data, and a
tool was developed for collecting, processing, and displaying the logged data [3]. The tool's graphical portrayal of measured data gives a readily comprehendible view of the overall operation of the system, permits performance estimates to be calculated easily, and provides an indication of which components may be causing performance problems. This tool, which was developed toward the end of the MAGIC project, has proved to be extremely valuable in diagnosing problems and in providing insight into techniques for improving performance. The tool is applicable to many high-speed distributed systems. A brief description of its use is given below.

Figure 6 displays a representative sample of 4 s of data from a configuration with the application host in $K$ ansas City ("tioc" in the legend), the ISS master in Sioux Falls ("edc"), and one server at each. (The host was not running TerraVision, but an application that emulates TerraV ision by sending the identical tile request lists which were sent during a previously recorded TerraV ision session.) The diagram traces a time history for each requested tile, showing: - When the application sends a request list (e.g., at 6800 $\mathrm{ms})$ and when it is received by the ISS master $(\sim 6810)^{2}$

- When the master sends tile lists to the two servers (6820) and when they are received ( $\sim 6840$ and $\sim 6850$ )
- When the servers start and complete their read operations
- When the tile data are transmitted by the servers and received by the host
In this example, the time between the request list leaving the application host and the first tile arriving at the host is 180 ms . The diagram shows that excluding the server time, the largest component of this 180 ms delay was queuing at the server, a result of TCP retransmissions of previously transmitted tiles that were, in effect, blocking transmission of subsequent tiles. (The shallow-sloped lines between "server send" and "app receive" represent tiles with TCP transmissions.) Rough calculations of throughput at each measurement point can readily be made by counting the number of tiles processed in a selected interval of time; for example, 15 tiles were received by the application between 6980 and 7130 ms , for a throughput of about 40 $\mathrm{Mb} / \mathrm{s}$.


## Herding C ats

AIthough the MAGIC project was an ambitious undertaking, it nevertheless was able to achieve most of its goals. The success of the project seems all the more remarkable if one considers the degree of interorganizational collaboration that was required to design, develop, test, and integrate the individual testbed components and to ensure their interoperability. I ndeed, fostering this collaboration was one of the most significant nontechnical challenges facing the project - and one of its noteworthy accomplishments.

M ore than a dozen diverse, geographically dispersed organizations participated in MAGIC, and many of the individuals involved in the project were experienced

[^10]

Figure 7. In the beginning, things looked difficult.
researchers who were used to working independently. A lthough five of these organizations were funded by ARPA, each had its own contract and a statement of work that was complementary to the others but theoretically could be executed separately from the rest. In addition, the commercial carriers and other organizations that were expected to be major contributors were not externally funded and therefore were under no obligation to participate actively in the effort. Thus, the situation at the outset was not unlike the metaphorical herding of cats (Fig. 7).

The authors of this article were funded by A R PA to oversee and coordinate the research and development ( $R$ \& D ) efforts of the five ARPA -funded research participants, and to help facilitate their collaboration with the carriers and with the other organizations contributing to the project. This was a challenging assignment because none of these organizations was contractually bound to answer to a third party, so voluntary compliance of all organizations was required. Considering the cast of players and the circumstances of their affiliation, it would have been imprudent to attempt to dictate direction or to impose preferences. Furthermore, to do so not only would have been ineffective but would have been counterproductive because a heavy-handed management style would have stifled the innovation that was critical to the success of the project. In other words, peremptory management might have led to passive obedience (Fig. 8), but the results would have been uninspired [11].

The challenge was to create an environment that facilitated progress and encouraged cooperation while at the same time promoting creativity and initiative. The approach used was to obtain mutual agreement on a common set of goals and related milestones which could not be achieved without the contributions of all of the participants. In this way, the focus of the work shifted from the pursuit of individual goals to the pursuit of common goals, and collaboration was implicitly understood to be essential for success. In retrospect, the reasons why this approach worked well seem obvious. H aving a common set of goals engendered an esprit de corps among the participants which gave the sense of a "virtual" organization dedicated to the success of MAGIC.

However, participants soon recognized that while camaraderie and commitment were vital to success, team spirit alone was not sufficient to ensure that success. Differences in work styles, conflicting priorities, geographical dispersion of people and resources, and the sheer magnitude of the interdependencies underscored the need for centralized leadership and for "formal" procedures for coordinating activities. A s a result, members of the MAGIC team willingly consented to, and complied with, a set of management practices that they perceived as facilitating the achievement of their technical objectives. The management style was collegial with the authors serving as facilitators for defining and prioritizing project activities, as mediators for resolving disputes, as liaison with the project sponsor (ARPA), and as catalysts for promoting the team interactions required to move forward. Thus, as indicated in Fig. 9, M A GIC took a hybrid approach to managing and coordinating its $R \& D$, with
progress toward common goals achieved through high-level con-sensus-building among the participants.

Three practices stand out as being most critical to the success of the project: demonstrations, planning with flexibility, and ongoing communications.

Demonstrations - Although the components of the MAGIC testbed were designed to operate as parts of a system, they were developed independently by organizations that were not collocated. Therefore, interoperability testing and debugging were difficult. To deal with this problem, demonstrations for external observers were scheduled to mark the achievement of milestones. These demonstrations provided a strong incentive for overcoming the logistical obstacles to testing, and for uncovering and finding solutions to tough problems. At first glance, these events appeared to be distractions from the research and a drain on people and resources, and initially they were deemed antithetical to an R \& D project. In actuality they were the single most important factor in accelerating progress. Often, it was in the typically frantic last hours before a crucial demonstration that creative solutions to unforeseen problems were conceived.

A number of major demonstrations were scheduled in conjunction with quarterly project meetings or technical symposia. The first, which took place approximately halfway into the three-year project duration, marked the completion of the first phase of the MAGIC testbed: initial versions of TerraV ision and the ISS working together over a partially completed backbone. The second, which occurred about six months later, demonstrated improved versions of both TerraV ision and the ISS working together over the full internetwork. This demonstration was attended by prospective end users of the system who provided valuable feedback, including suggestions for additional capabilities which were subsequently incorporated into TerraV ision, substantially improving the utility of the application.

Planning ... with Flexibility - R esearchers are notoriously reluctant to document their ideas and approaches in advance for fear of forfeiting their flexibility or limiting their options; however, failure to do so can spell disaster in a collaborative venture involving multiple organizations. Therefore, one of the first priorities of the M A GIC team was to develop a comprehensive research plan for the project. If truth be told, the process of planning was far more valuable than the plan itself. In creating the plan, each organization was forced to clearly define its tasks and milestones, to explore alternative approaches to accomplishing the work, and, most important, to identify interorganizational relationships and dependencies. It was understood that tasks and milestones, as well as technical approaches, would most likely change and evolve over the course of the three-year effort, and the plan was considered a working document to be revised and revisited as appropriate. However, at the conclusion of the project, it was gratifying to discover that the participants had accomplished most of the work they had intended to do within the allotted time and budget constraints.


Figure 8. This wouldn't work either.

Ongoing Communications O ngoing communication was an important factor in maintaining cohesiveness among team members, and was essential for accomplishing the work. Regular interaction was achieved by holding weekly teleconferences and quarterly project meetings to discuss technical issues and interorganizational dependencies, to plan joint activities and events, and to identify and resolve problems. In addition, a variety of mechanisms for exchanging information were established, including multiple mailers, and a project server for storing and retrieving documents such as project plans, papers, and reports. To facilitate collaboration on documents, a common desktop publishing package, which was available for multiple platforms, was adopted by the team very early in the project.

## Lessons Learned

The previous section described the challenges of managing the MAGIC project, and discussed some of the factors that promoted cooperation and collaboration among the participants in this multidisciplinary, multi-organizational effort. Below are some additional lessons that were learned - sometimes with pain - during the course of the three-year project.

## Technology for R\&D Projects

R \& D projects such as MAGIC depend on state-of-the-art technology to achieve their goals. There are two alternatives for obtaining this technology: develop it as part of the project, or procure it from vendors or other sources. W here possible, M A GIC opted for the latter alternative, and milestones were planned based on vendors' stated intentions regarding the capabilities of and projected delivery dates for critical hardware and software. A s a consequence of this decision, M A GIC researchers learned two important lessons.
Be Prepared to Deal with the Limitations of Vendor Products Some of the vendor-supplied state-of-the-art products required by MAGIC, for example, the SONET terminals and the ATM switches, were available on schedule and performed satisfactorily. Others, however, were either not available in the time frame expected (e.g., OC-12 cards for the ATM switches) or did not function as anticipated. Specifically, MAGIC researchers had to deal with three types of limitations:

- Product (im)maturity: E arly production versions of products required a significant amount of tuning and debugging that would be unacceptable in a mature product. For example, some workstation operating systems initially had hard-coded upper limits on the TCP window size, limiting the achievable throughput across a network having a large bandwidth-delay product.
- Standalone performance vs. system performance: Products did not perform per their standalone specifications when incorporated into a system. For example, the measured rate of a disk on an ISS server was typically less than half the specified rate (perhaps caused by interactions with the SCSI adapter).
- Single-component performance vs. multiple-component
performance: W hen multiple components were made to operate in parallel, their performance did not scale linearly. For example, the rate at which the TerraVision host could absorb data increased only slightly as the number of ATM interfaces was increased.
Encourage the Active Involvement of Vendors in the R\&D Effort MAGIC depended on products that were under development or "on the horizon" when the project was initiated, and progress often hinged on timely access to early releases or upgrades. In some cases, market pressures on vendors took precedence over research needs, and the products were delayed, or anticipated features were postponed or eliminated. In other cases, products were released but were not robust, and vendor support was difficult to obtain. If equipment vendors had been more actively involved in the R \& D effort, the other researchers, as well as ARPA and the carriers, would have been in a better position to influence vendor priorities and development schedules, and would have been more likely to gain the support and assistance they needed to correct shortcomings. A ctive vendor participation would have been beneficial to the vendors as well, providing them with insight into the strengths and limitations of their products, and helping them identify additional features and performance enhancements that might improve their competitive advantage.

D espite the difficulties associated with relying on vendors for supporting technology, using vendor-supplied products was preferable to developing customized products as part of the project. Such development would have been time- and resource-intensive, and possibly a duplication of effort. In addition, customized technology is expensive to replicate and difficult to transfer to other domains.

## Support for Demonstrations

A s discussed previously, demonstrations were sometimes scheduled to coincide with major project events or milestones. In addition, requests to demonstrate the capabilities of the testbed were occasionally made by ARPA, by the management of the participating organizations, or by prospective end users. While there were significant benefits associated with holding these demonstrations, preparing for them was time-consuming because it was frequently necessary to reconfigure the network and to relocate and assemble the required hardware. The MAGIC team learned two lessons that helped facilitate the conduct of demonstrations during the later stages of the project.

Establish a Reliable Testbed Configuration to Support Demonstrations - Although demonstrations proved to be a significant stimulus to progress, they sometimes conflicted with planned experiments or with development and testing activities. This was particularly troubling when work-inprogress was interrupted or put on hold for a relatively long period of time in order to reconfigure the network (or to test modifications to TerraV ision or the ISS) to support a scheduled event. This situation was remedied by implementing stable versions of TerraV ision and the ISS and deploying them at selected locations. These versions were used to support demonstrations, performance measurements, and related activities. U pdates to the demon-


Figure 9. Heterogeneous collaborative interoperability.
stration versions of TerraV ision and the ISS were coordinated to ensure their compatibility.

Plan Equipment Logistics C arefully and in Advance - Another problem, pertinent to development as well as demonstrations, is the availability of equipment. Since budgets are finite, choices must be made regarding what equipment to purchase and where this equipment should be located. While it is impossible to foresee all contingencies, equipment needs should be determined as far in advance as possible. Doing so will minimize the disruptions and stress associated with disassembling and transporting hardware over long distances, and acquiring essential components on short notice. It is especially important to develop strategies for supporting off-site demonstrations, particularly those that involve relocating large, cumbersome equipment or require expensive hardware which cannot easily be moved and is difficult to borrow or lease.

O ne way of helping to ensure that demonstrations can be accommodated without undue disruption is to purchase spares of inexpensive equipment. These spares would be available not only for demonstrations, but for development and experimentation in the event that an original malfunctions. It is less feasible to duplicate expensive equipment; however, if vendors of critical components are actively involved in the project, they might be willing to support demonstrations by providing the necessary hardware.

## Support for Development

The MAGIC testbed consists of components that were designed to interoperate but were developed independently by organizations that were geographically separated. In addition, the end users of the system were not research participants in the project. The following lessons were learned regarding how to work more effectively and efficiently under such conditions.

Build Tools to Enable Independent Development of Interoperable Components - Interoperability testing of a given component was challenging because it required that other components possess a level of functionality or performance that was not always available when the tests were ready to be conducted. One way to alleviate this problem was to implement component simulators that enabled interoperability testing. In MAGIC, the implementation of a TerraV ision simulator hastened progress on the ISS, whereas the decision not to implement an ISS simulator increased the time needed to complete TerraV ision.

Provide High-Speed Network Connections for All Major Participants - Proper testing of TerraVision and the ISS required high-speed interconnectivity. H owever, SRI and LBNL, the respective developers of these components, did not have such connectivity. A s a result, interoperability testing could not be performed locally, and testing at remote sites was both burdensome and inefficient. In the MAGIC project, both of these organizations would have benefited from having high-speed links to the backbone.

Solicit Periodic Input from End Users - Getting input from end users helps to ensure that the final product has useful
features, satisfactory performance, and a welldesigned interface. Input regarding desired capabilities should be solicited early in the effort and regularly thereafter as development progresses. Although, as noted in the previous section, MAGIC did benefit from such input, the project would have benefited even more if that input had been obtained earlier and more frequently.

## Future W ork

The MA GIC project has demonstrated a high-speed, wide-area IP/A TM internetwork that supports a real-time terrain visualization application and a distributed storage system. ARPA recently approved funding for a three-year follow-on effort, MAGIC-II, which will build on the technology developed in the original MAGIC project and on the existing MAGIC network facilities. There are two major interrelated goals in MAGIC-II:

- To enhance and upgrade the testbed to demonstrate the utility and capabilities of distributed processing and networkbased storage, coupled with high-speed networks, to support a new generation of real-time applications.
- To create a very large internetwork with many end users that will be a realistic test environment for ATM technology and for the above type of application.
The MAGIC-II testbed will demonstrate the scalability of the distributed storage and distributed processing concepts by configuring systems that have a large number of servers and processors on many ATM networks spanning a large geographic area, and have multiple sets of data and multiple simultaneous users.

The MAGIC-II testbed is based on a very general paradigm in which high-performance computing, storage, and communications are used to provide rapid access to large amounts of distributed data, including real-time data that must be processed and delivered to an end user on demand. A pplications that use this paradigm arise in a variety of situations, including military operations, intelligence imagery analysis, and natural disaster response. The exact type, location, and ownership of the data used by these applications may not be known in advance, and these data may require a large amount of processing to be transformed into useful information. In addition, the processed data may have to be delivered to end users with a range of communications speeds, link qualities, computational powers, and display capabilities. The data, as well as the computing and storage resources required to process them, may reside in multiple administrative domains that have different usage and access control policies.

Specific work to be done in MAGIC-II includes augmenting the MAGIC internetwork with wireless nodes and interconnecting it with other IP/ATM internetworks to create a nation-wide, high-speed, wide-area testbed. This testbed will be used for experimentation with protocols, with routing techniques, and with mobile access to backbone services. A new version of TerraV ision that can perform on-the-fly rectification coupled with algorithms for

The MaGic-II
testbed will demonstrate the scalability of the distributed storage and distributed processing concepts by configuring systems that have a large number of servers and
processors on many ATM networks spanning a large geographic area, and have multiple sets of data and multiple simultaneous users.
"in-transit" processing will permit near-real-time visualization of raw imagery, enabling data from sensors to be viewed within minutes (rather than hours) after being generated. (Fig. 1.) D ata fusion techniques will allow disparate data types to be overlaid. The processing will be performed by sets of distributed devices that are constructed from resources owned by multiple administrative domains. Algorithms that dynamically determine the current state of the network will provide information to the application so that it can adapt to current system performance and to available system resources.
The MAGIC-II project will certainly benefit from the lessons learned in the original MAGIC project. Nevertheless, as with any research effort, new challenges will be encountered, and new lessons, both technical and organizational, will be learned in meeting these challenges. Stay tuned.

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# CCITT 

T. 81

THE INTERNATIONAL
(09/92)
TELEGRAPH AND TELEPHONE CONSULTATIVE COMMITTEE

# TERMINAL EQUIPMENT AND PROTOCOLS FOR TELEMATIC SERVICES 

# INFORMATION TECHNOLOGY DIGITAL COMPRESSION AND CODING OF CONTINUOUS-TONE STILL IMAGES REQUIREMENTS AND GUIDELINES 

## Foreword

ITU (International Telecommunication Union) is the United Nations Specialized Agency in the field of telecommunications. The CCITT (the International Telegraph and Telephone Consultative Committee) is a permanent organ of the ITU. Some 166 member countries, 68 telecom operating entities, 163 scientific and industrial organizations and 39 international organizations participate in CCITT which is the body which sets world telecommunications standards (Recommendations).

The approval of Recommendations by the members of CCITT is covered by the procedure laid down in CCITT Resolution No. 2 (Melbourne, 1988). In addition, the Plenary Assembly of CCITT, which meets every four years, approves Recommendations submitted to it and establishes the study programme for the following period.

In some areas of information technology, which fall within CCITT's purview, the necessary standards are prepared on a collaborative basis with ISO and IEC. The text of CCITT Recommendation T. 81 was approved on 18th September 1992. The identical text is also published as ISO/IEC International Standard 10918-1.

CCITT NOTE

In this Recommendation, the expression "Administration" is used for conciseness to indicate both a telecommunication administration and a recognized private operating agency.

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## Introduction

This CCITT Recommendation | ISO/IEC International Standard was prepared by CCITT Study Group VIII and the Joint Photographic Experts Group (JPEG) of ISO/IEC JTC 1/SC 29/WG 10. This Experts Group was formed in 1986 to establish a standard for the sequential progressive encoding of continuous tone grayscale and colour images.

Digital Compression and Coding of Continuous-tone Still images, is published in two parts:

- Requirements and guidelines;
- Compliance testing.

This part, Part 1, sets out requirements and implementation guidelines for continuous-tone still image encoding and decoding processes, and for the coded representation of compressed image data for interchange between applications. These processes and representations are intended to be generic, that is, to be applicable to a broad range of applications for colour and grayscale still images within communications and computer systems. Part 2, sets out tests for determining whether implementations comply with the requirments for the various encoding and decoding processes specified in Part 1.

The user's attention is called to the possibility that - for some of the coding processes specified herein - compliance with this Recommendation | International Standard may require use of an invention covered by patent rights. See Annex L for further information.

The requirements which these processes must satisfy to be useful for specific image communications applications such as facsimile, Videotex and audiographic conferencing are defined in CCITT Recommendation T.80. The intent is that the generic processes of Recommendation T. 80 will be incorporated into the various CCITT Recommendations for terminal equipment for these applications.

In addition to the applications addressed by the CCITT and ISO/IEC, the JPEG committee has developped a compression standard to meet the needs of other applications as well, including desktop publishing, graphic arts, medical imaging and scientific imaging.

Annexes A, B, C, D, E, F, G, H and J are normative, and thus form an integral part of this Specification. Annexes K, L and M are informative and thus do not form an integral part of this Specification.

This Specification aims to follow the guidelines of CCITT and ISO/IEC JTC 1 on Rules for presentation of CCITT | ISO/IEC common text.

# INFORMATION TECHNOLOGY - DIGITAL COMPRESSION AND CODING OF CONTINUOUS-TONE STILL IMAGES REQUIREMENTS AND GUIDELINES 

## 1 Scope

This CCITT Recommendation | International Standard is applicable to continuous-tone - grayscale or colour - digital still image data. It is applicable to a wide range of applications which require use of compressed images. It is not applicable to bi-level image data.

This Specification

- specifies processes for converting source image data to compressed image data;
- specifies processes for converting compressed image data to reconstructed image data;
- gives guidance on how to implement these processes in practice;
- specifies coded representations for compressed image data.

NOTE - This Specification does not specify a complete coded image representation. Such representations may include certain parameters, such as aspect ratio, component sample registration, and colour space designation, which are applicationdependent.

## 2 Normative references

The following CCITT Recommendations and International Standards contain provisions which, through reference in this text, constitute provisions of this CCITT Recommendation | International Standard. At the time of publication, the editions indicated were valid. All Recommendations and Standards are subject to revision, and parties to agreements based on this CCITT Recommendation | International Standard are encouraged to investigate the possibility of applying the most recent edition of the Recommendations and Standards listed below. Members of IEC and ISO maintain registers of currently valid International Standards. The CCITT Secretariat maintains a list of currently valid CCITT Recommendations.

- CCITT Recommendation T. 80 (1992), Common components for image compression and communication Basic principles.


## 3 Definitions, abbreviations and symbols

### 3.1 Definitions and abbreviations

For the purposes of this Specification, the following definitions apply.
3.1.1 abbreviated format: A representation of compressed image data which is missing some or all of the table specifications required for decoding, or a representation of table-specification data without frame headers, scan headers, and entropy-coded segments.
3.1.2 AC coefficient: Any DCT coefficient for which the frequency is not zero in at least one dimension.
3.1.3 (adaptive) (binary) arithmetic decoding: An entropy decoding procedure which recovers the sequence of symbols from the sequence of bits produced by the arithmetic encoder.
3.1.4 (adaptive) (binary) arithmetic encoding: An entropy encoding procedure which codes by means of a recursive subdivision of the probability of the sequence of symbols coded up to that point.
3.1.5 application environment: The standards for data representation, communication, or storage which have been established for a particular application.
3.1.6 arithmetic decoder: An embodiment of arithmetic decoding procedure.
3.1.7 arithmetic encoder: An embodiment of arithmetic encoding procedure.
3.1.8 baseline (sequential): A particular sequential DCT-based encoding and decoding process specified in this Specification, and which is required for all DCT-based decoding processes.
3.1.9 binary decision: Choice between two alternatives.
3.1.10 bit stream: Partially encoded or decoded sequence of bits comprising an entropy-coded segment.
3.1.11 block: An $8 \times 8$ array of samples or an $8 \times 8$ array of DCT coefficient values of one component.
3.1.12 block-row: A sequence of eight contiguous component lines which are partitioned into $8 \times 8$ blocks.
3.1.13 byte: A group of 8 bits.
3.1.14 byte stuffing: A procedure in which either the Huffman coder or the arithmetic coder inserts a zero byte into the entropy-coded segment following the generation of an encoded hexadecimal X'FF' byte.
3.1.15 carry bit: A bit in the arithmetic encoder code register which is set if a carry-over in the code register overflows the eight bits reserved for the output byte.
3.1.16 ceiling function: The mathematical procedure in which the greatest integer value of a real number is obtained by selecting the smallest integer value which is greater than or equal to the real number.
3.1.17 class (of coding process): Lossy or lossless coding processes.
3.1.18 code register: The arithmetic encoder register containing the least significant bits of the partially completed entropy-coded segment. Alternatively, the arithmetic decoder register containing the most significant bits of a partially decoded entropy-coded segment.
3.1.19 coder: An embodiment of a coding process.
3.1.20 coding: Encoding or decoding.
3.1.21 coding model: A procedure used to convert input data into symbols to be coded.
3.1.22 (coding) process: A general term for referring to an encoding process, a decoding process, or both.
3.1.23 colour image: A continuous-tone image that has more than one component.
3.1.24 columns: Samples per line in a component.
3.1.25 component: One of the two-dimensional arrays which comprise an image.
3.1.26 compressed data: Either compressed image data or table specification data or both.
3.1.27 compressed image data: A coded representation of an image, as specified in this Specification.
3.1.2 compression: Reduction in the number of bits used to represent source image data.
3.1.29 conditional exchange: The interchange of MPS and LPS probability intervals whenever the size of the LPS interval is greater than the size of the MPS interval (in arithmetic coding).
3.1.30 (conditional) probability estimate: The probability value assigned to the LPS by the probability estimation state machine (in arithmetic coding).
3.1.31 conditioning table: The set of parameters which select one of the defined relationships between prior coding decisions and the conditional probability estimates used in arithmetic coding.
3.1.32 context: The set of previously coded binary decisions which is used to create the index to the probability estimation state machine (in arithmetic coding).
3.1.33 continuous-tone image: An image whose components have more than one bit per sample.
3.1.34 data unit: An $8 \times 8$ block of samples of one component in DCT-based processes; a sample in lossless processes.

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3.1.35 DC coefficient: The DCT coefficient for which the frequency is zero in both dimensions.
3.1.36 DC prediction: The procedure used by DCT-based encoders whereby the quantized DC coefficient from the previously encoded $8 \times 8$ block of the same component is subtracted from the current quantized DC coefficient.
3.1.37 (DCT) coefficient: The amplitude of a specific cosine basis function - may refer to an original DCT coefficient, to a quantized DCT coefficient, or to a dequantized DCT coefficient.
3.1.38 decoder: An embodiment of a decoding process.
3.1.39 decoding process: A process which takes as its input compressed image data and outputs a continuous-tone image.
3.1.40 default conditioning: The values defined for the arithmetic coding conditioning tables at the beginning of coding of an image.
3.1.41 dequantization: The inverse procedure to quantization by which the decoder recovers a representation of the DCT coefficients.
3.1.42 differential component: The difference between an input component derived from the source image and the corresponding reference component derived from the preceding frame for that component (in hierarchical mode coding).
3.1.43 differential frame: A frame in a hierarchical process in which differential components are either encoded or decoded.
3.1.44 (digital) reconstructed image (data): A continuous-tone image which is the output of any decoder defined in this Specification.
3.1.45 (digital) source image (data): A continuous-tone image used as input to any encoder defined in this Specification.
3.1.46 (digital) (still) image: A set of two-dimensional arrays of integer data.
3.1.47 discrete cosine transform; DCT: Either the forward discrete cosine transform or the inverse discrete cosine transform.
3.1.48 downsampling (filter): A procedure by which the spatial resolution of an image is reduced (in hierarchical mode coding).
3.1.49 encoder: An embodiment of an encoding process.
3.1.50 encoding process: A process which takes as its input a continuous-tone image and outputs compressed image data.
3.1.51 entropy-coded (data) segment: An independently decodable sequence of entropy encoded bytes of compressed image data.
3.1.52 (entropy-coded segment) pointer: The variable which points to the most recently placed (or fetched) byte in the entropy encoded segment.
3.1.53 entropy decoder: An embodiment of an entropy decoding procedure.
3.1.54 entropy decoding: A lossless procedure which recovers the sequence of symbols from the sequence of bits produced by the entropy encoder.
3.1.55 entropy encoder: An embodiment of an entropy encoding procedure.
3.1.56 entropy encoding: A lossless procedure which converts a sequence of input symbols into a sequence of bits such that the average number of bits per symbol approaches the entropy of the input symbols.
3.1.57 extended (DCT-based) process: A descriptive term for DCT-based encoding and decoding processes in which additional capabilities are added to the baseline sequential process.
3.1.58 forward discrete cosine transform; FDCT: A mathematical transformation using cosine basis functions which converts a block of samples into a corresponding block of original DCT coefficients.
3.1.59 frame: A group of one or more scans (all using the same DCT-based or lossless process) through the data of one or more of the components in an image.
3.1.60 frame header: A marker segment that contains a start-of-frame marker and associated frame parameters that are coded at the beginning of a frame.
3.1.61 frequency: A two-dimensional index into the two-dimensional array of DCT coefficients.
3.1.62 (frequency) band: A contiguous group of coefficients from the zig-zag sequence (in progressive mode coding).
3.1.63 full progression: A process which uses both spectral selection and successive approximation (in progressive mode coding).
3.1.64 grayscale image: A continuous-tone image that has only one component.
3.1.65 hierarchical: A mode of operation for coding an image in which the first frame for a given component is followed by frames which code the differences between the source data and the reconstructed data from the previous frame for that component. Resolution changes are allowed between frames.
3.1.66 hierarchical decoder: A sequence of decoder processes in which the first frame for each component is followed by frames which decode an array of differences for each component and adds it to the reconstructed data from the preceding frame for that component.
3.1.67 hierarchical encoder: The mode of operation in which the first frame for each component is followed by frames which encode the array of differences between the source data and the reconstructed data from the preceding frame for that component.
3.1.68 horizontal sampling factor: The relative number of horizontal data units of a particular component with respect to the number of horizontal data units in the other components.
3.1.69 Huffman decoder: An embodiment of a Huffman decoding procedure.
3.1.70 Huffman decoding: An entropy decoding procedure which recovers the symbol from each variable length code produced by the Huffman encoder.
3.1.71 Huffman encoder: An embodiment of a Huffman encoding procedure.
3.1.72 Huffman encoding: An entropy encoding procedure which assigns a variable length code to each input symbol.
3.1.73 Huffman table: The set of variable length codes required in a Huffman encoder and Huffman decoder.
3.1.74 image data: Either source image data or reconstructed image data.
3.1.75 interchange format: The representation of compressed image data for exchange between application environments.
3.1.76 interleaved: The descriptive term applied to the repetitive multiplexing of small groups of data units from each component in a scan in a specific order.
3.1.77 inverse discrete cosine transform; IDCT: A mathematical transformation using cosine basis functions which converts a block of dequantized DCT coefficients into a corresponding block of samples.
3.1.78 Joint Photographic Experts Group; JPEG: The informal name of the committee which created this Specification. The "joint" comes from the CCITT and ISO/IEC collaboration.
3.1.79 latent output: Output of the arithmetic encoder which is held, pending resolution of carry-over (in arithmetic coding).
3.1.80 less probable symbol; LPS: For a binary decision, the decision value which has the smaller probability.
3.1.81 level shift: A procedure used by DCT-based encoders and decoders whereby each input sample is either converted from an unsigned representation to a two's complement representation or from a two's complement representation to an unsigned representation.

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3.1.82 lossless: A descriptive term for encoding and decoding processes and procedures in which the output of the decoding procedure(s) is identical to the input to the encoding procedure(s).
3.1.83 lossless coding: The mode of operation which refers to any one of the coding processes defined in this Specification in which all of the procedures are lossless (see Annex H).
3.1.84 lossy: A descriptive term for encoding and decoding processes which are not lossless.
3.1.85 marker: A two-byte code in which the first byte is hexadecimal FF ( $X^{\prime}$ FF') and the second byte is a value between 1 and hexadecimal FE ( $\mathrm{X}^{\prime} \mathrm{FE}^{\prime}$ ).
3.1.86 marker segment: A marker and associated set of parameters.
3.1.87 MCU-row: The smallest sequence of MCU which contains at least one line of samples or one block-row from every component in the scan.
3.1.88 minimum coded unit; MCU: The smallest group of data units that is coded.
3.1.89 modes (of operation): The four main categories of image coding processes defined in this Specification.
3.1.90 more probable symbol; MPS: For a binary decision, the decision value which has the larger probability.
3.1.91 non-differential frame: The first frame for any components in a hierarchical encoder or decoder. The components are encoded or decoded without subtraction from reference components. The term refers also to any frame in modes other than the hierarchical mode.
3.1.92 non-interleaved: The descriptive term applied to the data unit processing sequence when the scan has only one component.
3.1.93 parameters: Fixed length integers 4,8 or 16 bits in length, used in the compressed data formats.
3.1.94 point transform: Scaling of a sample or DCT coefficient.
3.1.95 precision: Number of bits allocated to a particular sample or DCT coefficient.
3.1.96 predictor: A linear combination of previously reconstructed values (in lossless mode coding).
3.1.97 probability estimation state machine: An interlinked table of probability values and indices which is used to estimate the probability of the LPS (in arithmetic coding).
3.1.98 probability interval: The probability of a particular sequence of binary decisions within the ordered set of all possible sequences (in arithmetic coding).
3.1.99 (probability) sub-interval: A portion of a probability interval allocated to either of the two possible binary decision values (in arithmetic coding).
3.1.100 procedure: A set of steps which accomplishes one of the tasks which comprise an encoding or decoding process.
3.1.101 process: See coding process.
3.1.102 progressive (coding): One of the DCT-based processes defined in this Specification in which each scan typically improves the quality of the reconstructed image.
3.1.103 progressive DCT-based: The mode of operation which refers to any one of the processes defined in Annex G.
3.1.104 quantization table: The set of 64 quantization values used to quantize the DCT coefficients.
3.1.105 quantization value: An integer value used in the quantization procedure.
3.1.106 quantize: The act of performing the quantization procedure for a DCT coefficient.
3.1.107 reference (reconstructed) component: Reconstructed component data which is used in a subsequent frame of a hierarchical encoder or decoder process (in hierarchical mode coding).
3.1.108 renormalization: The doubling of the probability interval and the code register value until the probability interval exceeds a fixed minimum value (in arithmetic coding).
3.1.109 restart interval: The integer number of MCUs processed as an independent sequence within a scan.
3.1.110 restart marker: The marker that separates two restart intervals in a scan.
3.1.111 run (length): Number of consecutive symbols of the same value.
3.1.112 sample: One element in the two-dimensional array which comprises a component.
3.1.113 sample-interleaved: The descriptive term applied to the repetitive multiplexing of small groups of samples from each component in a scan in a specific order.
3.1.114 scan: A single pass through the data for one or more of the components in an image.
3.1.115 scan header: A marker segment that contains a start-of-scan marker and associated scan parameters that are coded at the beginning of a scan.
3.1.116 sequential (coding): One of the lossless or DCT-based coding processes defined in this Specification in which each component of the image is encoded within a single scan.
3.1.117 sequential DCT-based: The mode of operation which refers to any one of the processes defined in Annex F.
3.1.118 spectral selection: A progressive coding process in which the zig-zag sequence is divided into bands of one or more contiguous coefficients, and each band is coded in one scan.
3.1.119 stack counter: The count of X'FF' bytes which are held, pending resolution of carry-over in the arithmetic encoder.
3.1.120 statistical conditioning: The selection, based on prior coding decisions, of one estimate out of a set of conditional probability estimates (in arithmetic coding).
3.1.121 statistical model: The assignment of a particular conditional probability estimate to each of the binary arithmetic coding decisions.
3.1.122 statistics area: The array of statistics bins required for a coding process which uses arithmetic coding.
3.1.123 statistics bin: The storage location where an index is stored which identifies the value of the conditional probability estimate used for a particular arithmetic coding binary decision.
3.1.124 successive approximation: A progressive coding process in which the coefficients are coded with reduced precision in the first scan, and precision is increased by one bit with each succeeding scan.
3.1.125 table specification data: The coded representation from which the tables used in the encoder and decoder are generated and their destinations specified.
3.1.126 transcoder: A procedure for converting compressed image data of one encoder process to compressed image data of another encoder process.
3.1.127 (uniform) quantization: The procedure by which DCT coefficients are linearly scaled in order to achieve compression.
3.1.128 upsampling (filter): A procedure by which the spatial resolution of an image is increased (in hierarchical mode coding).
3.1.129 vertical sampling factor: The relative number of vertical data units of a particular component with respect to the number of vertical data units in the other components in the frame.
3.1.130 zero byte: The $X^{\prime} 00^{\prime}$ byte.
3.1.131 zig-zag sequence: A specific sequential ordering of the DCT coefficients from (approximately) lowest spatial frequency to highest.
3.1.132 3-sample predictor: A linear combination of the three nearest neighbor reconstructed samples to the left and above (in lossless mode coding).

## 3.2

Symbols
The symbols used in this Specification are listed below.

| A | probability interval |
| :---: | :---: |
| AC | AC DCT coefficient |
| $\mathrm{AC}_{\mathrm{ji}}$ | AC coefficient predicted from DC values |
| Ah | successive approximation bit position, high |
| Al | successive approximation bit position, low |
| $\mathrm{Ap}_{\mathrm{i}}$ | $i$ th 8-bit parameter in $\mathrm{APP}_{\mathrm{n}}$ segment |
| $\mathrm{APP}_{\mathrm{n}}$ | marker reserved for application segments |
| B | current byte in compressed data |
| B2 | next byte in compressed data when $\mathrm{B}=\mathrm{X}^{\prime} \mathrm{FF}$ ' |
| BE | counter for buffered correction bits for Huffman coding in the successive approximation process |
| BITS | 16-byte list containing number of Huffman codes of each length |
| BP | pointer to compressed data |
| BPST | pointer to byte before start of entropy-coded segment |
| BR | counter for buffered correction bits for Huffman coding in the successive approximation process |
| Bx | byte modified by a carry-over |
| C | value of bit stream in code register |
| $\mathrm{C}_{i}$ | component identifier for frame |
| $\mathrm{C}_{\mathrm{u}}$ | horizontal frequency dependent scaling factor in DCT |
| $\mathrm{C}_{\mathrm{v}}$ | vertical frequency dependent scaling factor in DCT |
| CE | conditional exchange |
| C-low | low order 16 bits of the arithmetic decoder code register |
| $\mathrm{Cm}_{\mathrm{i}}$ | $i$ th 8-bit parameter in COM segment |
| CNT | bit counter in NEXTBYTE procedure |
| CODE | Huffman code value |
| CODESIZE(V) | code size for symbol V |
| COM | comment marker |
| Cs | conditioning table value |
| $\mathrm{Cs}_{\mathrm{i}}$ | component identifier for scan |
| CT | renormalization shift counter |
| Cx | high order 16 bits of arithmetic decoder code register |
| CX | conditional exchange |
| $\mathrm{d}_{\mathrm{ji}}$ | data unit from horizontal position i , vertical position j |
| $\mathrm{d}_{\mathrm{j} 1} \mathrm{k}^{\text {b }}$ | $\mathrm{d}_{\mathrm{ji}}$ for component k |
| D | decision decoded |

Da

DAC
Db
DC
$\mathrm{DC}_{\mathrm{i}}$
$\mathrm{DC}_{\mathrm{k}}$
DHP
DHT
DIFF
DNL
DQT
DRI
E
EC
ECS
$\mathrm{ECS}_{\mathrm{i}}$
Eh
EHUFCO
EHUFSI
EOB
EOBn
EOBx
EOB0, EOB1, ..., EOB14
EOI
Ev
EXP
FREQ(V)
$\mathrm{H}_{\mathrm{i}}$
$\mathrm{H}_{\text {max }}$
HUFFCODE
HUFFSIZE
HUFFVAL
i
I

Index(S)
j

J
in DC coding, the DC difference coded for the previous block from the same component; in lossless coding, the difference coded for the sample immediately to the left
define-arithmetic-coding-conditioning marker
the difference coded for the sample immediately above
DC DCT coefficient
DC coefficient for $i$ th block in component
$k$ th DC value used in prediction of AC coefficients
define hierarchical progression marker
define-Huffman-tables marker
difference between quantized DC and prediction
define-number-of-lines marker
define-quantization-tables marker
define restart interval marker
exponent in magnitude category upper bound event counter
entropy-coded segment
$i$ th entropy-coded segment
horizontal expansion parameter in EXP segment
Huffman code table for encoder
encoder table of Huffman code sizes
end-of-block for sequential; end-of-band for progressive
run length category for EOB runs
position of EOB in previous successive approximation scan
run length categories for EOB runs
end-of-image marker
vertical expansion parameter in EXP segment
expand reference components marker
frequency of occurrence of symbol V
horizontal sampling factor for $i$ th component
largest horizontal sampling factor
list of Huffman codes corresponding to lengths in HUFFSIZE
list of code lengths
list of values assigned to each Huffman code
subscript index
integer variable
index to probability estimation state machine table for context index S
subscript index
integer variable

| JPG | ker reserved for JPEG extensions |
| :---: | :---: |
| JPG ${ }_{\text {n }}$ | marker reserved for JPEG extensions |
| k | subscript index |
| K | integer variable |
| Kmin | index of 1st AC coefficient in band (1 for sequential DCT) |
| Kx | conditioning parameter for AC arithmetic coding model |
| L | DC and lossless coding conditioning lower bound parameter |
| $L_{i}$ | element in BITS list in DHT segment |
| $\mathrm{L}_{\mathrm{i}}(\mathrm{t})$ | element in BITS list in the DHT segment for Huffman table t |
| La | length of parameters in $\mathrm{APP}_{\mathrm{n}}$ segment |
| LASTK | largest value of K |
| Lc | length of parameters in COM segment |
| Ld | length of parameters in DNL segment |
| Le | length of parameters in EXP segment |
| Lf | length of frame header parameters |
| Lh | length of parameters in DHT segment |
| Lp | length of parameters in DAC segment |
| LPS | less probable symbol (in arithmetic coding) |
| Lq | length of parameters in DQT segment |
| Lr | length of parameters in DRI segment |
| Ls | length of scan header parameters |
| LSB | least significant bit |
| m | modulo 8 counter for $\mathrm{RST}_{\mathrm{m}}$ marker |
| $\mathrm{m}_{\mathrm{t}}$ | number of $\mathrm{V}_{\mathrm{i}, \mathrm{j}}$ parameters for Huffman table t |
| M | bit mask used in coding magnitude of V |
| Mn | $n$th statistics bin for coding magnitude bit pattern category |
| MAXCODE | table with maximum value of Huffman code for each code length |
| MCU | minimum coded unit |
| $\mathrm{MCU}_{\mathrm{i}}$ | $i$ th MCU |
| MCUR | number of MCU required to make up one MCU-row |
| MINCODE | table with minimum value of Huffman code for each code length |
| MPS | more probable symbol (in arithmetic coding) |
| MPS(S) | more probable symbol for context-index S |
| MSB | most significant bit |
| M2, M3, M4, ... , M15 | designation of context-indices for coding of magnitude bits in the arithmetic coding models |
| n | integer variable |
| N | data unit counter for MCU coding |
| N/A | not applicable |

Nb
Next_Index_LPS
Next_Index_MPS
Nf
NL
Ns
OTHERS(V)
P
Pq
Pq(t)
PRED
Pt
Px
$\mathrm{Q}_{\mathrm{ji}}$
$\mathrm{Q}_{\mathrm{vu}}$
Q00
$\mathrm{QAC}_{\mathrm{ji}}$
$\mathrm{QDC}_{\mathrm{k}}$
Qe
Qe(S)
Qk
$\mathrm{r}_{\mathrm{vu}}$
R
$\mathrm{R}_{\mathrm{vu}}$
Ra
Rb
Rc
Rd
RES
Ri
RRRR
RS
RST $_{\mathrm{m}}$
$S_{y x}$
S
$S_{\mathrm{vu}}$
number of data units in MCU
new value of Index(S) after a LPS renormalization
new value of $\operatorname{Index}(\mathrm{S})$ after a MPS renormalization
number of components in frame
number of lines defined in DNL segment
number of components in scan
index to next symbol in chain
sample precision
quantizer precision parameter in DQT segment
quantizer precision parameter in DQT segment for quantization table $t$ quantized DC coefficient from the most recently coded block of the component point transform parameter
calculated value of sample
quantizer value for coefficient $\mathrm{AC}_{\mathrm{ji}}$
quantization value for DCT coefficient $\mathrm{S}_{\mathrm{vu}}$
quantizer value for DC coefficient
quantized AC coefficient predicted from DC values
$k$ th quantized DC value used in prediction of AC coefficients
LPS probability estimate
LPS probability estimate for context index S
$k$ th element of 64 quantization elements in DQT segment
reconstructed image sample
length of run of zero amplitude AC coefficients
dequantized DCT coefficient
reconstructed sample value
reconstructed sample value
reconstructed sample value
rounding in prediction calculation
reserved markers
restart interval in DRI segment
4-bit value of run length of zero AC coefficients
composite value used in Huffman coding of AC coefficients
restart marker number m
reconstructed value from IDCT
context index
DCT coefficient at horizontal frequency $u$, vertical frequency v

SLL
SLL $\alpha \beta$
SN
$\mathrm{SOF}_{0}$
$\mathrm{SOF}_{1}$
$\mathrm{SOF}_{2}$
$\mathrm{SOF}_{3}$
$\mathrm{SOF}_{5}$
$\mathrm{SOF}_{6}$
$\mathrm{SOF}_{7}$
$\mathrm{SOF}_{9}$
$\mathrm{SOF}_{10}$
SOF $_{11}$
SOF $_{13}$
SOF $_{14}$
$\mathrm{SOF}_{15}$
SOI
SOS
SP
$\mathrm{Sq}_{\mathrm{vu}}$
SRL
SRL $\alpha \beta$
Ss
SS
SSSS
ST
Switch_MPS
Sz
S0
t
T
context-index for coding of correction bit in successive approximation coding end of spectral selection band in zig-zag sequence context-index for coding of end-of-block or end-of-band Huffman code size

1 if decoded sense of sign is negative and 0 if decoded sense of sign is positive length of a Huffman code
shift left logical operation
logical shift left of $\alpha$ by $\beta$ bits
context-index for coding of first magnitude category when V is negative
baseline DCT process frame marker
extended sequential DCT frame marker, Huffman coding progressive DCT frame marker, Huffman coding lossless process frame marker, Huffman coding differential sequential DCT frame marker, Huffman coding differential progressive DCT frame marker, Huffman coding differential lossless process frame marker, Huffman coding sequential DCT frame marker, arithmetic coding progressive DCT frame marker, arithmetic coding lossless process frame marker, arithmetic coding differential sequential DCT frame marker, arithmetic coding differential progressive DCT frame marker, arithmetic coding differential lossless process frame marker, arithmetic coding start-of-image marker start-of-scan marker context-index for coding of first magnitude category when V is positive quantized DCT coefficient shift right logical operation
logical shift right of $\alpha$ by $\beta$ bits start of spectral selection band in zig-zag sequence context-index for coding of sign decision 4-bit size category of DC difference or AC coefficient amplitude stack counter
parameter controlling inversion of sense of MPS parameter used in coding magnitude of V context-index for coding of $\mathrm{V}=0$ decision summation index for parameter limits computation temporary variable

| Taj | AC entropy table destination selector for $j$ th component in scan |
| :---: | :---: |
| Tb | arithmetic conditioning table destination identifier |
| Tc | Huffman coding or arithmetic coding table class |
| Td ${ }_{\text {j }}$ | DC entropy table destination selector for $j$ th component in scan |
| TEM | temporary marker |
| Th | Huffman table destination identifier in DHT segment |
| Tq | quantization table destination identifier in DQT segment |
| Tqi | quantization table destination selector for $i$ th component in frame |
| U | DC and lossless coding conditioning upper bound parameter |
| V | symbol or value being either encoded or decoded |
| $\mathrm{V}_{\mathrm{i}}$ | vertical sampling factor for $i$ th component |
| $\mathrm{V}_{\mathrm{i}, \mathrm{j}}$ | $j$ th value for length $i$ in HUFFVAL |
| $\mathrm{V}_{\text {max }}$ | largest vertical sampling factor |
| $\mathrm{V}_{\mathrm{t}}$ | temporary variable |
| VALPTR | list of indices for first value in HUFFVAL for each code length |
| V1 | symbol value |
| V2 | symbol value |
| $\mathrm{x}_{1}$ | number of columns in $i$ th component |
| X | number of samples per line in component with largest horizontal dimension |
| $\mathrm{X}_{\mathrm{i}}$ | $i$ th statistics bin for coding magnitude category decision |
| $\mathrm{X} 1, \mathrm{X} 2, \mathrm{X} 3, \ldots, \mathrm{X} 15$ | designation of context-indices for coding of magnitude categories in the arithmetic coding models |
| XHUFCO | extended Huffman code table |
| XHUFSI | table of sizes of extended Huffman codes |
| X'values' | values within the quotes are hexadecimal |
| $\mathrm{y}_{\mathrm{i}}$ | number of lines in $i$ th component |
| Y | number of lines in component with largest vertical dimension |
| ZRL | value in HUFFVAL assigned to run of 16 zero coefficients |
| ZZ(K) | Kth element in zig-zag sequence of quantized DCT coefficients |
| ZZ(0) | quantized DC coefficient in zig-zag sequence order |

## 4 General

The purpose of this clause is to give an informative overview of the elements specified in this Specification. Another purpose is to introduce many of the terms which are defined in clause 3 . These terms are printed in italics upon first usage in this clause.

### 4.1 Elements specified in this Specification

There are three elements specified in this Specification:
a) An encoder is an embodiment of an encoding process. As shown in Figure 1, an encoder takes as input digital source image data and table specifications, and by means of a specified set of procedures generates as output compressed image data.
b) A decoder is an embodiment of a decoding process. As shown in Figure 2, a decoder takes as input compressed image data and table specifications, and by means of a specified set of procedures generates as output digital reconstructed image data.
c) The interchange format, shown in Figure 3, is a compressed image data representation which includes all table specifications used in the encoding process. The interchange format is for exchange between application environments.


Figure 1 - Encoder


Figure 2 - Decoder

Figures 1 and 2 illustrate the general case for which the continuous-tone source and reconstructed image data consist of multiple components. (A colour image consists of multiple components; a grayscale image consists only of a single component.) A significant portion of this Specification is concerned with how to handle multiple-component images in a flexible, application-independent way.


Figure 3 - Interchange format for compressed image data

These figures are also meant to show that the same tables specified for an encoder to use to compress a particular image must be provided to a decoder to reconstruct that image. However, this Specification does not specify how applications should associate tables with compressed image data, nor how they should represent source image data generally within their specific environments.

Consequently, this Specification also specifies the interchange format shown in Figure 3, in which table specifications are included within compressed image data. An image compressed with a specified encoding process within one application environment, A , is passed to a different environment, B , by means of the interchange format. The interchange format does not specify a complete coded image representation. Application-dependent information, e.g. colour space, is outside the scope of this Specification.

### 4.2 Lossy and lossless compression

This Specification specifies two classes of encoding and decoding processes, lossy and lossless processes. Those based on the discrete cosine transform (DCT) are lossy, thereby allowing substantial compression to be achieved while producing a reconstructed image with high visual fidelity to the encoder's source image.

The simplest DCT-based coding process is referred to as the baseline sequential process. It provides a capability which is sufficient for many applications. There are additional DCT-based processes which extend the baseline sequential process to a broader range of applications. In any decoder using extended DCT-based decoding processes, the baseline decoding process is required to be present in order to provide a default decoding capability.

The second class of coding processes is not based upon the DCT and is provided to meet the needs of applications requiring lossless compression. These lossless encoding and decoding processes are used independently of any of the DCT-based processes.

A table summarizing the relationship among these lossy and lossless coding processes is included in 4.11.

The amount of compression provided by any of the various processes is dependent on the characteristics of the particular image being compressed, as well as on the picture quality desired by the application and the desired speed of compression and decompression.

### 4.3 DCT-based coding

Figure 4 shows the main procedures for all encoding processes based on the DCT. It illustrates the special case of a singlecomponent image; this is an appropriate simplification for overview purposes, because all processes specified in this Specification operate on each image component independently.


Figure 4 - DCT-based encoder simplified diagram

In the encoding process the input component's samples are grouped into $8 \times 8$ blocks, and each block is transformed by the forward DCT (FDCT) into a set of 64 values referred to as $D C T$ coefficients. One of these values is referred to as the $D C$ coefficient and the other 63 as the $A C$ coefficients.

Each of the 64 coefficients is then quantized using one of 64 corresponding values from a quantization table (determined by one of the table specifications shown in Figure 4). No default values for quantization tables are specified in this Specification; applications may specify values which customize picture quality for their particular image characteristics, display devices, and viewing conditions.

After quantization, the DC coefficient and the 63 AC coefficients are prepared for entropy encoding, as shown in Figure 5. The previous quantized DC coefficient is used to predict the current quantized DC coefficient, and the difference is encoded. The 63 quantized AC coefficients undergo no such differential encoding, but are converted into a onedimensional zig-zag sequence, as shown in Figure 5.

The quantized coefficients are then passed to an entropy encoding procedure which compresses the data further. One of two entropy coding procedures can be used, as described in 4.6. If Huffman encoding is used, Huffman table specifications must be provided to the encoder. If arithmetic encoding is used, arithmetic coding conditioning table specifications may be provided, otherwise the default conditioning table specifications shall be used.

Figure 6 shows the main procedures for all DCT-based decoding processes. Each step shown performs essentially the inverse of its corresponding main procedure within the encoder. The entropy decoder decodes the zig-zag sequence of quantized DCT coefficients. After dequantization the DCT coefficients are transformed to an $8 \times 8$ block of samples by the inverse DCT (IDCT).

### 4.4 Lossless coding

Figure 7 shows the main procedures for the lossless encoding processes. A predictor combines the reconstructed values of up to three neighbourhood samples at positions $\mathrm{a}, \mathrm{b}$, and c to form a prediction of the sample at position x as shown in Figure 8. This prediction is then subtracted from the actual value of the sample at position x , and the difference is losslessly entropy-coded by either Huffman or arithmetic coding.


Figure 5 - Preparation of quantized coefficients for entropy encoding


Figure 6 - DCT-based decoder simplified diagram


Figure 7 - Lossless encoder simplified diagram

#  

|  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
|  | c | b |  |  |
|  | a | x |  |  |
|  |  |  |  |  |
|  |  |  |  |  |

Figure 8 - 3-sample prediction neighbourhood

This encoding process may also be used in a slightly modified way, whereby the precision of the input samples is reduced by one or more bits prior to the lossless coding. This achieves higher compression than the lossless process (but lower compression than the DCT-based processes for equivalent visual fidelity), and limits the reconstructed image's worst-case sample error to the amount of input precision reduction.

### 4.5 Modes of operation

There are four distinct modes of operation under which the various coding processes are defined: sequential DCT-based, progressive DCT-based, lossless, and hierarchical. (Implementations are not required to provide all of these.) The lossless mode of operation was described in 4.4. The other modes of operation are compared as follows.

For the sequential DCT-based mode, $8 \times 8$ sample blocks are typically input block by block from left to right, and blockrow by block-row from top to bottom. After a block has been transformed by the forward DCT, quantized and prepared for entropy encoding, all 64 of its quantized DCT coefficients can be immediately entropy encoded and output as part of the compressed image data (as was described in 4.3), thereby minimizing coefficient storage requirements.

For the progressive DCT-based mode, $8 \times 8$ blocks are also typically encoded in the same order, but in multiple scans through the image. This is accomplished by adding an image-sized coefficient memory buffer (not shown in Figure 4) between the quantizer and the entropy encoder. As each block is transformed by the forward DCT and quantized, its coefficients are stored in the buffer. The DCT coefficients in the buffer are then partially encoded in each of multiple scans. The typical sequence of image presentation at the output of the decoder for sequential versus progressive modes of operation is shown in Figure 9.

There are two procedures by which the quantized coefficients in the buffer may be partially encoded within a scan. First, only a specified band of coefficients from the zig-zag sequence need be encoded. This procedure is called spectral selection, because each band typically contains coefficients which occupy a lower or higher part of the frequency spectrum for that $8 \times 8$ block. Secondly, the coefficients within the current band need not be encoded to their full (quantized) accuracy within each scan. Upon a coefficient's first encoding, a specified number of most significant bits is encoded first. In subsequent scans, the less significant bits are then encoded. This procedure is called successive approximation. Either procedure may be used separately, or they may be mixed in flexible combinations.

In hierarchical mode, an image is encoded as a sequence of frames. These frames provide reference reconstructed components which are usually needed for prediction in subsequent frames. Except for the first frame for a given component, differential frames encode the difference between source components and reference reconstructed components. The coding of the differences may be done using only DCT-based processes, only lossless processes, or DCT-based processes with a final lossless process for each component. Downsampling and upsampling filters may be used to provide a pyramid of spatial resolutions as shown in Figure 10. Alternatively, the hierarchical mode can be used to improve the quality of the reconstructed components at a given spatial resolution.

Hierarchical mode offers a progressive presentation similar to the progressive DCT-based mode but is useful in environments which have multi-resolution requirements. Hierarchical mode also offers the capability of progressive coding to a final lossless stage.


Figure 9 - Progressive versus sequential presentation


Figure 10 - Hierarchical multi-resolution encoding

### 4.6 Entropy coding alternatives

Two alternative entropy coding procedures are specified: Huffman coding and arithmetic coding. Huffman coding procedures use Huffman tables, determined by one of the table specifications shown in Figures 1 and 2. Arithmetic coding procedures use arithmetic coding conditioning tables, which may also be determined by a table specification. No default values for Huffman tables are specified, so that applications may choose tables appropriate for their own environments. Default tables are defined for the arithmetic coding conditioning.

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The baseline sequential process uses Huffman coding, while the extended DCT-based and lossless processes may use either Huffman or arithmetic coding.

### 4.7 Sample precision

For DCT-based processes, two alternative sample precisions are specified: either 8 bits or 12 bits per sample. Applications which use samples with other precisions can use either 8 -bit or 12 -bit precision by shifting their source image samples appropriately. The baseline process uses only 8 -bit precision. DCT-based implementations which handle 12 -bit source image samples are likely to need greater computational resources than those which handle only 8 -bit source images. Consequently in this Specification separate normative requirements are defined for 8 -bit and 12-bit DCT-based processes.

For lossless processes the sample precision is specified to be from 2 to 16 bits.

### 4.8 Multiple-component control

Subclauses 4.3 and 4.4 give an overview of one major part of the encoding and decoding processes - those which operate on the sample values in order to achieve compression. There is another major part as well - the procedures which control the order in which the image data from multiple components are processed to create the compressed data, and which ensure that the proper set of table data is applied to the proper data units in the image. (A data unit is a sample for lossless processes and an $8 \times 8$ block of samples for DCT-based processes.)

### 4.8.1 Interleaving multiple components

Figure 11 shows an example of how an encoding process selects between multiple source image components as well as multiple sets of table data, when performing its encoding procedures. The source image in this example consists of the three components A, B and C, and there are two sets of table specifications. (This simplified view does not distinguish between the quantization tables and entropy coding tables.)


Figure 11 - Component-interleave and table-switching control

In sequential mode, encoding is non-interleaved if the encoder compresses all image data units in component A before beginning component B , and then in turn all of B before C . Encoding is interleaved if the encoder compresses a data unit from A, a data unit from B, a data unit from C, then back to A, etc. These alternatives are illustrated in Figure 12, which shows a case in which all three image components have identical dimensions: X columns by Y lines, for a total of n data units each.




Data unit encoding order, non-interleaved


Data unit encoding order, interleaved

Figure 12 - Interleaved versus non-interleaved encoding order

These control procedures are also able to handle cases in which the source image components have different dimensions. Figure 13 shows a case in which two of the components, $B$ and $C$, have half the number of horizontal samples relative to component A. In this case, two data units from A are interleaved with one each from B and C. Cases in which components of an image have more complex relationships, such as different horizontal and vertical dimensions, can be handled as well. (See Annex A.)


Figure 13 - Interleaved order for components with different dimensions

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### 4.8.2

Minimum coded unit
Related to the concepts of multiple-component interleave is the minimum coded unit (MCU). If the compressed image data is non-interleaved, the MCU is defined to be one data unit. For example, in Figure 12 the MCU for the noninterleaved case is a single data unit. If the compressed data is interleaved, the MCU contains one or more data units from each component. For the interleaved case in Figure 12, the (first) MCU consists of the three interleaved data units $\mathrm{A}_{1}, \mathrm{~B}_{1}$, $\mathrm{C}_{1}$. In the example of Figure 13, the (first) MCU consists of the four data units $\mathrm{A}_{1}, \mathrm{~A}_{2}, \mathrm{~B}_{1}, \mathrm{C}_{1}$.

### 4.9 Structure of compressed data

Figures 1, 2, and 3 all illustrate slightly different views of compressed image data. Figure 1 shows this data as the output of an encoding process, Figure 2 shows it as the input to a decoding process, and Figure 3 shows compressed image data in the interchange format, at the interface between applications.

Compressed image data are described by a uniform structure and set of parameters for both classes of encoding processes (lossy or lossless), and for all modes of operation (sequential, progressive, lossless, and hierarchical). The various parts of the compressed image data are identified by special two-byte codes called markers. Some markers are followed by particular sequences of parameters, as in the case of table specifications, frame header, or scan header. Others are used without parameters for functions such as marking the start-of-image and end-of-image. When a marker is associated with a particular sequence of parameters, the marker and its parameters comprise a marker segment.

The data created by the entropy encoder are also segmented, and one particular marker - the restart marker - is used to isolate entropy-coded data segments. The encoder outputs the restart markers, intermixed with the entropy-coded data, at regular restart intervals of the source image data. Restart markers can be identified without having to decode the compressed data to find them. Because they can be independently decoded, they have application-specific uses, such as parallel encoding or decoding, isolation of data corruptions, and semi-random access of entropy-coded segments.

There are three compressed data formats:
a) the interchange format;
b) the abbreviated format for compressed image data;
c) the abbreviated format for table-specification data.

### 4.9.1 Interchange format

In addition to certain required marker segments and the entropy-coded segments, the interchange format shall include the marker segments for all quantization and entropy-coding table specifications needed by the decoding process. This guarantees that a compressed image can cross the boundary between application environments, regardless of how each environment internally associates tables with compressed image data.

### 4.9.2 Abbreviated format for compressed image data

The abbreviated format for compressed image data is identical to the interchange format, except that it does not include all tables required for decoding. (It may include some of them.) This format is intended for use within applications where alternative mechanisms are available for supplying some or all of the table-specification data needed for decoding.

### 4.9.3 Abbreviated format for table-specification data

This format contains only table-specification data. It is a means by which the application may install in the decoder the tables required to subsequently reconstruct one or more images.

### 4.10 Image, frame, and scan

Compressed image data consists of only one image. An image contains only one frame in the cases of sequential and progressive coding processes; an image contains multiple frames for the hierarchical mode.

A frame contains one or more scans. For sequential processes, a scan contains a complete encoding of one or more image components. In Figures 12 and 13, the frame consists of three scans when non-interleaved, and one scan if all three components are interleaved together. The frame could also consist of two scans: one with a non-interleaved component, the other with two components interleaved.

For progressive processes, a scan contains a partial encoding of all data units from one or more image components. Components shall not be interleaved in progressive mode, except for the DC coefficients in the first scan for each component of a progressive frame.

### 4.11 Summary of coding processes

Table 1 provides a summary of the essential characteristics of the various coding processes specified in this Specification. The full specification of these processes is contained in Annexes F, G, H, and J.

Table 1 - Summary: Essential characteristics of coding processes

|  | Baseline process (required for all DCT-based decoders) |
| :--- | :--- |
| - DCT-based process |  |
| - Source image: 8-bit samples within each component |  |
| - Sequential |  |
| Huffman coding: 2 AC and 2 DC tables |  |
| - Decoders shall process scans with 1, 2, 3, and 4 components |  |

## Extended DCT-based processes

- DCT-based process
- Source image: 8-bit or 12-bit samples
- Sequential or progressive
- Huffman or arithmetic coding: 4 AC and 4 DC tables
- Decoders shall process scans with $1,2,3$, and 4 components
- Interleaved and non-interleaved scans

|  | Lossless processes |
| :--- | :--- |
| Predictive process (not DCT-based) |  |
| - Source image: P-bit samples $(2 \leq \mathrm{P} \leq 16)$ |  |
| Sequential |  |
| Huffman or arithmetic coding: 4 DC tables |  |
| - |  |
| Decoders shall process scans with 1, 2, 3, and 4 components |  |

Hierarchical processes

- Multiple frames (non-differential and differential)
- Uses extended DCT-based or lossless processes
- Decoders shall process scans with 1,2,3, and 4 components
- Interleaved and non-interleaved scans


## 5 Interchange format requirements

The interchange format is the coded representation of compressed image data for exchange between application environments.

The interchange format requirements are that any compressed image data represented in interchange format shall comply with the syntax and code assignments appropriate for the decoding process selected, as specified in Annex B.

Tests for whether compressed image data comply with these requirements are specified in Part 2 of this Specification.

## 6 Encoder requirements

An encoding process converts source image data to compressed image data. Each of Annexes F, G, H, and J specifies a number of distinct encoding processes for its particular mode of operation.

An encoder is an embodiment of one (or more) of the encoding processes specified in Annexes F, G, H, or J. In order to comply with this Specification, an encoder shall satisfy at least one of the following two requirements.

An encoder shall
a) with appropriate accuracy, convert source image data to compressed image data which comply with the interchange format syntax specified in Annex B for the encoding process(es) embodied by the encoder;
b) with appropriate accuracy, convert source image data to compressed image data which comply with the abbreviated format for compressed image data syntax specified in Annex B for the encoding process(es) embodied by the encoder.

For each of the encoding processes specified in Annexes F, G, H, and J, the compliance tests for the above requirements are specified in Part 2 of this Specification.

NOTE - There is no requirement in this Specification that any encoder which embodies one of the encoding processes specified in Annexes F, G, H, or J shall be able to operate for all ranges of the parameters which are allowed for that process. An encoder is only required to meet the compliance tests specified in Part 2, and to generate the compressed data format according to Annex B for those parameter values which it does use.

## 7 Decoder requirements

A decoding process converts compressed image data to reconstructed image data. Each of Annexes F, G, H, and J specifies a number of distinct decoding processes for its particular mode of operation.

A decoder is an embodiment of one (or more) of the decoding processes specified in Annexes F, G, H, or J. In order to comply with this Specification, a decoder shall satisfy all three of the following requirements.

## A decoder shall

a) with appropriate accuracy, convert to reconstructed image data any compressed image data with parameters within the range supported by the application, and which comply with the interchange format syntax specified in Annex B for the decoding process(es) embodied by the decoder;
b) accept and properly store any table-specification data which comply with the abbreviated format for tablespecification data syntax specified in Annex B for the decoding process(es) embodied by the decoder;
c) with appropriate accuracy, convert to reconstructed image data any compressed image data which comply with the abbreviated format for compressed image data syntax specified in Annex B for the decoding process(es) embodied by the decoder, provided that the table-specification data required for decoding the compressed image data has previously been installed into the decoder.

Additionally, any DCT-based decoder, if it embodies any DCT-based decoding process other than baseline sequential, shall also embody the baseline sequential decoding process.

For each of the decoding processes specified in Annexes F, G, H, and J, the compliance tests for the above requirements are specified in Part 2 of this Specification.

# Annex A <br> Mathematical definitions <br> (This annex forms an integral part of this Recommendation | International Standard) 

## A. 1 Source image

Source images to which the encoding processes specified in this Specification can be applied are defined in this annex.

## A.1.1 Dimensions and sampling factors

As shown in Figure A.1, a source image is defined to consist of Nf components. Each component, with unique identifier $C_{i}$, is defined to consist of a rectangular array of samples of $x_{i}$ columns by $y_{i}$ lines. The component dimensions are derived from two parameters, $X$ and $Y$, where $X$ is the maximum of the $x_{i}$ values and $Y$ is the maximum of the $y_{i}$ values for all components in the frame. For each component, sampling factors $H_{i}$ and $V_{i}$ are defined relating component dimensions $x_{i}$ and $y_{i}$ to maximum dimensions $X$ and $Y$, according to the following expressions:

$$
x_{i}=\left\lceil X \times \frac{H_{i}}{H_{\max }}\right\rceil \text { and } y_{i}\left\lceil Y \times \frac{V_{i}}{V_{\max }}\right\rceil \text {, }
$$

where $H_{\max }$ and $V_{\max }$ are the maximum sampling factors for all components in the frame, and $\rceil$ is the ceiling function.
As an example, consider an image having 3 components with maximum dimensions of 512 lines and 512 samples per line, and with the following sampling factors:

| Component 0 | $H_{0}=4$, | $V_{0}=1$ |
| :--- | :--- | :--- |
| Component 1 | $H_{1}=2$, | $V_{1}=2$ |
| Component 2 | $H_{2}=1$, | $V_{2}=1$ |

Then $X=512, Y=512, H_{\max }=4, V_{\max }=2$, and $x_{i}$ and $y_{i}$ for each component are

Component 0
Component 1
Component 2

$$
\begin{array}{ll}
x_{0}=512, & y_{0}=256 \\
x_{1}=256, & y_{1}=512 \\
x_{2}=128, & y_{2}=256
\end{array}
$$

NOTE - The $X, Y, H_{i}$, and $V_{i}$ parameters are contained in the frame header of the compressed image data (see B.2.2), whereas the individual component dimensions $x_{i}$ and $y_{i}$ are derived by the decoder. Source images with $x_{i}$ and $y_{i}$ dimensions which do not satisfy the expressions above cannot be properly reconstructed.

## A.1.2 Sample precision

A sample is an integer with precision P bits, with any value in the range 0 through $2^{\mathrm{P}}-1$. All samples of all components within an image shall have the same precision $P$. Restrictions on the value of $P$ depend on the mode of operation, as specified in B. 2 to B.7.

## A.1.3 Data unit

A data unit is a sample in lossless processes and an $8 \times 8$ block of contiguous samples in DCT-based processes. The leftmost 8 samples of each of the top-most 8 rows in the component shall always be the top-left-most block. With this top-leftmost block as the reference, the component is partitioned into contiguous data units to the right and to the bottom (as shown in Figure A.4).

## A.1.4 Orientation

Figure A. 1 indicates the orientation of an image component by the terms top, bottom, left, and right. The order by which the data units of an image component are input to the compression encoding procedures is defined to be left-to-right and top-to-bottom within the component. (This ordering is precisely defined in A.2.) Applications determine which edges of a source image are defined as top, bottom, left, and right.

a) Source image with multiple components

b) Characteristics of an image component

Figure A. 1 - Source image characteristics

## A. 2 Order of source image data encoding

The scan header (see B.2.3) specifies the order by which source image data units shall be encoded and placed within the compressed image data. For a given scan, if the scan header parameter $\mathrm{Ns}=1$, then data from only one source component - the component specified by parameter $\mathrm{Cs}_{1}$ - shall be present within the scan. This data is non-interleaved by definition. If Ns $>1$, then data from the Ns components $\mathrm{Cs}_{1}$ through $\mathrm{Cs}_{\mathrm{Ns}}$ shall be present within the scan. This data shall always be interleaved. The order of components in a scan shall be according to the order specified in the frame header.

The ordering of data units and the construction of minimum coded units (MCU) is defined as follows.

## A.2.1 Minimum coded unit (MCU)

For non-interleaved data the MCU is one data unit. For interleaved data the MCU is the sequence of data units defined by the sampling factors of the components in the scan.

## A.2.2 $\operatorname{Non-interleaved~order~}(\mathbf{N s}=1)$

When $\mathrm{Ns}=1$ (where Ns is the number of components in a scan), the order of data units within a scan shall be left-to-right and top-to-bottom, as shown in Figure A.2. This ordering applies whenever Ns $=1$, regardless of the values of $\mathrm{H}_{1}$ and $\mathrm{V}_{1}$.


Figure A. 2 - Non-interleaved data ordering

## A.2.3 Interleaved order (Ns > 1)

When $N s>1$, each scan component $\mathrm{Cs}_{\mathrm{i}}$ is partitioned into small rectangular arrays of $\mathrm{H}_{\mathrm{k}}$ horizontal data units by $\mathrm{V}_{\mathrm{k}}$ vertical data units. The subscripts k indicate that $\mathrm{H}_{\mathrm{k}}$ and $\mathrm{V}_{\mathrm{k}}$ are from the position in the frame header componentspecification for which $\mathrm{C}_{\mathrm{k}}=\mathrm{Cs}_{\mathrm{i}}$. Within each $\mathrm{H}_{\mathrm{k}}$ by $\mathrm{V}_{\mathrm{k}}$ array, data units are ordered from left-to-right and top-to-bottom. The arrays in turn are ordered from left-to-right and top-to-bottom within each component.

As shown in the example of Figure A.3, $\mathrm{Ns}=4$, and $\mathrm{MCU}_{1}$ consists of data units taken first from the top-left-most region of $\mathrm{Cs}_{1}$, followed by data units from the corresponding region of $\mathrm{Cs}_{2}$, then from $\mathrm{Cs}_{3}$ and then from $\mathrm{Cs}_{4} . \mathrm{MCU}_{2}$ follows the same ordering for data taken from the next region to the right for the four components.


Figure A. 3 - Interleaved data ordering example

## A.2.4 Completion of partial MCU

For DCT-based processes the data unit is a block. If $\mathrm{x}_{\mathrm{i}}$ is not a multiple of 8 , the encoding process shall extend the number of columns to complete the right-most sample blocks. If the component is to be interleaved, the encoding process shall also extend the number of samples by one or more additional blocks, if necessary, so that the number of blocks is an integer multiple of $H_{i}$. Similarly, if $y_{i}$ is not a multiple of 8 , the encoding process shall extend the number of lines to complete the bottom-most block-row. If the component is to be interleaved, the encoding process shall also extend the number of lines by one or more additional block-rows, if necessary, so that the number of block-rows is an integer multiple of $\mathrm{V}_{\mathrm{i}}$.

NOTE - It is recommended that any incomplete MCUs be completed by replication of the right-most column and the bottom line of each component.

For lossless processes the data unit is a sample. If the component is to be interleaved, the encoding process shall extend the number of samples, if necessary, so that the number is a multiple of $\mathrm{H}_{\mathrm{i}}$. Similarly, the encoding process shall extend the number of lines, if necessary, so that the number of lines is a multiple of $V_{i}$.

Any sample added by an encoding process to complete partial MCUs shall be removed by the decoding process.

## A. 3 DCT compression

## A.3.1 Level shift

Before a non-differential frame encoding process computes the FDCT for a block of source image samples, the samples shall be level shifted to a signed representation by subtracting $2^{P-1}$, where P is the precision parameter specified in B.2.2. Thus, when $\mathrm{P}=8$, the level shift is by 128 ; when $\mathrm{P}=12$, the level shift is by 2048.

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After a non-differential frame decoding process computes the IDCT and produces a block of reconstructed image samples, an inverse level shift shall restore the samples to the unsigned representation by adding $2^{\mathrm{P}-1}$ and clamping the results to the range 0 to $2^{\mathrm{P}-1}$.

## A.3.2 Orientation of samples for FDCT computation

Figure A. 4 shows an image component which has been partitioned into $8 \times 8$ blocks for the FDCT computations. Figure A. 4 also defines the orientation of the samples within a block by showing the indices used in the FDCT equation of A.3.3.

The definitions of block partitioning and sample orientation also apply to any DCT decoding process and the output reconstructed image. Any sample added by an encoding process to complete partial MCUs shall be removed by the decoding process.


Figure A. 4 - Partition and orientation of $8 \times 8$ sample blocks

## A.3.3 FDCT and IDCT (informative)

The following equations specify the ideal functional definition of the FDCT and the IDCT.
NOTE - These equations contain terms which cannot be represented with perfect accuracy by any real implementation. The accuracy requirements for the combined FDCT and quantization procedures are specified in Part 2 of this Specification. The accuracy requirements for the combined dequantization and IDCT procedures are also specified in Part 2 of this Specification.

$$
\begin{array}{ll}
\text { FDCT: } & S_{v u}=\frac{1}{4} C_{u} C_{v} \sum_{x=0}^{7} \sum_{y=0}^{7} s_{y x} \cos \frac{(2 x+1) u \pi}{16} \cos \frac{(2 y+1) v \pi}{16} \\
\text { IDCT: } & s_{y x}=\frac{1}{4} \sum_{u=0}^{7} \sum_{v=0}^{7} C_{u} C_{v} S_{v u} \cos \frac{(2 x+1) u \pi}{16} \cos \frac{(2 y+1) v \pi}{16}
\end{array}
$$

where

$$
\begin{aligned}
& C_{u}, C_{v}=1 / \sqrt{2} \text { for } u, v=0 \\
& C_{u}, C_{v}=1 \text { otherwise }
\end{aligned}
$$

otherwise.

## A.3.4 DCT coefficient quantization (informative) and dequantization (normative)

After the FDCT is computed for a block, each of the 64 resulting DCT coefficients is quantized by a uniform quantizer. The quantizer step size for each coefficient $S_{v u}$ is the value of the corresponding element $Q_{v u}$ from the quantization table specified by the frame parameter $T q_{i}$ (see B.2.2).

The uniform quantizer is defined by the following equation. Rounding is to the nearest integer:

$$
S q_{v u}=\text { round }\left(\frac{S_{v u}}{Q_{v u}}\right)
$$

$S q_{v u}$ is the quantized DCT coefficient, normalized by the quantizer step size.
NOTE - This equation contains a term which may not be represented with perfect accuracy by any real implementation. The accuracy requirements for the combined FDCT and quantization procedures are specified in Part 2 of this Specification.

At the decoder, this normalization is removed by the following equation, which defines dequantization:

$$
R_{v u}=S q_{v u} \times Q_{v u}
$$

NOTE - Depending on the rounding used in quantization, it is possible that the dequantized coefficient may be outside the expected range.

The relationship among samples, DCT coefficients, and quantization is illustrated in Figure A.5.

## A.3.5 Differential DC encoding

After quantization, and in preparation for entropy encoding, the quantized DC coefficient $\mathrm{Sq}_{00}$ is treated separately from the 63 quantized AC coefficients. The value that shall be encoded is the difference (DIFF) between the quantized DC coefficient of the current block ( $D C_{i}$ which is also designated as $\mathrm{Sq}_{00}$ ) and that of the previous block of the same component (PRED):

$$
D I F F=D C_{i}-P R E D
$$

## A.3.6 Zig-zag sequence

After quantization, and in preparation for entropy encoding, the quantized AC coefficients are converted to the zig-zag sequence. The quantized DC coefficient (coefficient zero in the array) is treated separately, as defined in A.3.5. The zigzag sequence is specified in Figure A.6.

## A. 4 Point transform

For various procedures data may be optionally divided by a power of 2 by a point transform prior to coding. There are three processes which require a point transform: lossless coding, lossless differential frame coding in the hierarchical mode, and successive approximation coding in the progressive DCT mode.

In the lossless mode of operation the point transform is applied to the input samples. In the difference coding of the hierarchical mode of operation the point transform is applied to the difference between the input component samples and the reference component samples. In both cases the point transform is an integer divide by 2 Pt , where Pt is the value of the point transform parameter (see B.2.3).

In successive approximation coding the point transform for the AC coefficients is an integer divide by 2 Al , where Al is the successive approximation bit position, low (see B.2.3). The point transform for the DC coefficients is an arithmetic-shiftright by Al bits. This is equivalent to dividing by $2^{\mathrm{Pt}}$ before the level shift (see A.3.1).

The output of the decoder is rescaled by multiplying by 2 Pt . An example of the point transform is given in K.10.


Figure A. 5 - Relationship between $8 \times 8$-block samples and DCT coefficients

| 0 | 1 | 5 | 6 | 14 | 15 | 27 | 28 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | 4 | 7 | 13 | 16 | 26 | 29 | 42 |
| 3 | 8 | 12 | 17 | 25 | 30 | 41 | 43 |
| 9 | 11 | 18 | 24 | 31 | 40 | 44 | 53 |
| 10 | 19 | 23 | 32 | 39 | 45 | 52 | 54 |
| 20 | 22 | 33 | 38 | 46 | 51 | 55 | 60 |
| 21 | 34 | 37 | 47 | 50 | 56 | 59 | 61 |
| 35 | 36 | 48 | 49 | 57 | 58 | 62 | 63 |

Figure A.6 - Zig-zag sequence of quantized DCT coefficients

## A. 5 Arithmetic procedures in lossless and hierarchical modes of operation

In the lossless mode of operation predictions are calculated with full precision and without clamping of either overflow or underflow beyond the range of values allowed by the precision of the input. However, the division by two which is part of some of the prediction calculations shall be approximated by an arithmetic-shift-right by one bit.

The two's complement differences which are coded in either the lossless mode of operation or the differential frame coding in the hierarchical mode of operation are calculated modulo 65536 , thereby restricting the precision of these differences to a maximum of 16 bits. The modulo values are calculated by performing the logical AND operation of the two's complement difference with X'FFFF'. For purposes of coding, the result is still interpreted as a 16 bit two's complement difference. Modulo 65536 arithmetic is also used in the decoder in calculating the output from the sum of the prediction and this two's complement difference.

## Annex B <br> Compressed data formats

(This annex forms an integral part of this Recommendation | International Standard)

This annex specifies three compressed data formats:
a) the interchange format, specified in B. 2 and B.3;
b) the abbreviated format for compressed image data, specified in B.4;
c) the abbreviated format for table-specification data, specified in B.5.
B. 1 describes the constituent parts of these formats. B.1.3 and B.1.4 give the conventions for symbols and figures used in the format specifications.

## B. 1 General aspects of the compressed data format specifications

Structurally, the compressed data formats consist of an ordered collection of parameters, markers, and entropy-coded data segments. Parameters and markers in turn are often organized into marker segments. Because all of these constituent parts are represented with byte-aligned codes, each compressed data format consists of an ordered sequence of 8-bit bytes. For each byte, a most significant bit (MSB) and a least significant bit (LSB) are defined.

## B.1. 1 Constituent parts

This subclause gives a general description of each of the constituent parts of the compressed data format.

## B.1.1.1 Parameters

Parameters are integers, with values specific to the encoding process, source image characteristics, and other features selectable by the application. Parameters are assigned either 4-bit, 1-byte, or 2-byte codes. Except for certain optional groups of parameters, parameters encode critical information without which the decoding process cannot properly reconstruct the image.

The code assignment for a parameter shall be an unsigned integer of the specified length in bits with the particular value of the parameter.

For parameters which are 2 bytes ( 16 bits) in length, the most significant byte shall come first in the compressed data's ordered sequence of bytes. Parameters which are 4 bits in length always come in pairs, and the pair shall always be encoded in a single byte. The first 4-bit parameter of the pair shall occupy the most significant 4 bits of the byte. Within any $16-, 8$-, or 4 -bit parameter, the MSB shall come first and LSB shall come last.

## B.1.1.2 Markers

Markers serve to identify the various structural parts of the compressed data formats. Most markers start marker segments containing a related group of parameters; some markers stand alone. All markers are assigned two-byte codes: an X'FF' byte followed by a byte which is not equal to 0 or X'FF' (see Table B.1). Any marker may optionally be preceded by any number of fill bytes, which are bytes assigned code X'FF'.

NOTE - Because of this special code-assignment structure, markers make it possible for a decoder to parse the compressed data and locate its various parts without having to decode other segments of image data.

## B.1.1.3 Marker assignments

All markers shall be assigned two-byte codes: a X'FF' byte followed by a second byte which is not equal to 0 or $X^{\prime}{ }^{\prime} F F$ '. The second byte is specified in Table B. 1 for each defined marker. An asterisk (*) indicates a marker which stands alone, that is, which is not the start of a marker segment.

Table B. 1 - Marker code assignments

| Code Assignment | Symbol | Description |
| :---: | :---: | :---: |
| Start Of Frame markers, non-differential, Huffman coding |  |  |
| X'FFC0' <br> X'FFC1' <br> X'FFC2' <br> X'FFC3' | $\begin{aligned} & \mathrm{SOF}_{0} \\ & \mathrm{SOF}_{1} \\ & \mathrm{SOF}_{2} \\ & \mathrm{SOF}_{3} \end{aligned}$ | Baseline DCT <br> Extended sequential DCT <br> Progressive DCT <br> Lossless (sequential) |
| Start Of Frame markers, differential, Huffman coding |  |  |
| X'FFC5' <br> X'FFC6' <br> X'FFC7' | $\begin{aligned} & \mathrm{SOF}_{5} \\ & \mathrm{SOF}_{6} \\ & \mathrm{SOF}_{7} \end{aligned}$ | Differential sequential DCT <br> Differential progressive DCT <br> Differential lossless (sequential) |
| Start Of Frame markers, non-differential, arithmetic coding |  |  |
| X'FFC8' <br> X'FFC9' <br> X'FFCA' <br> X'FFCB' | $\begin{aligned} & \text { JPG } \\ & \text { SOF }_{9} \\ & \text { SOF }_{10} \\ & \text { SOF }_{11} \end{aligned}$ | Reserved for JPEG extensions <br> Extended sequential DCT <br> Progressive DCT <br> Lossless (sequential) |
| Start Of Frame markers, differential, arithmetic coding |  |  |
| X'FFCD' <br> X'FFCE' <br> X'FFCF' | $\begin{aligned} & \mathrm{SOF}_{13} \\ & \text { SOF }_{14} \\ & \text { SOF }_{15} \end{aligned}$ | Differential sequential DCT <br> Differential progressive DCT <br> Differential lossless (sequential) |
| Huffman table specification |  |  |
| X'FFC4' | DHT | Define Huffman table(s) |
| Arithmetic coding conditioning specification |  |  |
| X'FFCC' | DAC | Define arithmetic coding conditioning(s) |
| Restart interval termination |  |  |
| X'FFD0' through X'FFD7' | $\mathrm{RST}_{\mathrm{m}}$ * | Restart with modulo 8 count "m" |
| Other markers |  |  |
| X'FFD8' <br> X'FFD9' <br> X'FFDA' <br> X'FFDB' <br> X'FFDC' <br> X'FFDD' <br> X'FFDE' <br> X'FFDF' <br> X'FFE0' through X'FFEF' <br> X'FFF0' through X'FFFD' <br> X'FFFE' | $\begin{aligned} & \text { SOI* } \\ & \text { EOI* } \\ & \text { SOS } \\ & \text { DQT } \\ & \text { DNL } \\ & \text { DRI } \\ & \text { DHP } \\ & \text { EXP }^{\text {APP }_{n}} \\ & \text { JPG }_{n} \\ & \text { COM } \end{aligned}$ | Start of image <br> End of image <br> Start of scan <br> Define quantization table(s) <br> Define number of lines <br> Define restart interval <br> Define hierarchical progression <br> Expand reference component(s) <br> Reserved for application segments <br> Reserved for JPEG extensions <br> Comment |
| Reserved markers |  |  |
| X'FF01' <br> X'FF02' through X'FFBF' | $\begin{aligned} & \text { TEM* } \\ & \text { RES } \end{aligned}$ | For temporary private use in arithmetic coding Reserved |

## B.1.1.4 Marker segments

A marker segment consists of a marker followed by a sequence of related parameters. The first parameter in a marker segment is the two-byte length parameter. This length parameter encodes the number of bytes in the marker segment, including the length parameter and excluding the two-byte marker. The marker segments identified by the SOF and SOS marker codes are referred to as headers: the frame header and the scan header respectively.

## B.1.1.5 Entropy-coded data segments

An entropy-coded data segment contains the output of an entropy-coding procedure. It consists of an integer number of bytes, whether the entropy-coding procedure used is Huffman or arithmetic.

## NOTES

1 Making entropy-coded segments an integer number of bytes is performed as follows: for Huffman coding, 1-bits are used, if necessary, to pad the end of the compressed data to complete the final byte of a segment. For arithmetic coding, byte alignment is performed in the procedure which terminates the entropy-coded segment (see D.1.8).

2 In order to ensure that a marker does not occur within an entropy-coded segment, any X'FF' byte generated by either a Huffman or arithmetic encoder, or an X'FF' byte that was generated by the padding of 1 -bits described in NOTE 1 above, is followed by a "stuffed" zero byte (see D.1.6 and F.1.2.3).

## B.1.2 Syntax

In B. 2 and B. 3 the interchange format syntax is specified. For the purposes of this Specification, the syntax specification consists of:

- the required ordering of markers, parameters, and entropy-coded segments;
- identification of optional or conditional constituent parts;
- the name, symbol, and definition of each marker and parameter;
- the allowed values of each parameter;
- any restrictions on the above which are specific to the various coding processes.

The ordering of constituent parts and the identification of which are optional or conditional is specified by the syntax figures in B. 2 and B.3. Names, symbols, definitions, allowed values, conditions, and restrictions are specified immediately below each syntax figure.

## B.1.3 Conventions for syntax figures

The syntax figures in B. 2 and B. 3 are a part of the interchange format specification. The following conventions, illustrated in Figure B.1, apply to these figures:

- parameter/marker indicator: A thin-lined box encloses either a marker or a single parameter;
- segment indicator: A thick-lined box encloses either a marker segment, an entropy-coded data segment, or combinations of these;
- parameter length indicator: The width of a thin-lined box is proportional to the parameter length $(4,8$, or 16 bits, shown as E, B, and D respectively in Figure B.1) of the marker or parameter it encloses; the width of thick-lined boxes is not meaningful;
- optional/conditional indicator: Square brackets indicate that a marker or marker segment is only optionally or conditionally present in the compressed image data;
- ordering: In the interchange format a parameter or marker shown in a figure precedes all of those shown to its right, and follows all of those shown to its left;
- entropy-coded data indicator: Angled brackets indicate that the entity enclosed has been entropy encoded.


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Figure B. 1 - Syntax notation conventions

## B.1.4 Conventions for symbols, code lengths, and values

Following each syntax figure in B. 2 and B.3, the symbol, name, and definition for each marker and parameter shown in the figure are specified. For each parameter, the length and allowed values are also specified in tabular form.

The following conventions apply to symbols for markers and parameters:

- all marker symbols have three upper-case letters, and some also have a subscript. Examples: SOI, SOF
- all parameter symbols have one upper-case letter; some also have one lower-case letter and some have subscripts. Examples: $\mathrm{Y}, \mathrm{Nf}, \mathrm{H}_{\mathrm{i}}, \mathrm{Tq}_{\mathrm{i}}$.


## B. 2 General sequential and progressive syntax

This clause specifies the interchange format syntax which applies to all coding processes for sequential DCT-based, progressive DCT-based, and lossless modes of operation.

## B.2. 1 High-level syntax

Figure B. 2 specifies the order of the high-level constituent parts of the interchange format for all non-hierarchical encoding processes specified in this Specification.


Figure B. 2 - Syntax for sequential DCT-based, progressive DCT-based, and lossless modes of operation

The three markers shown in Figure B. 2 are defined as follows:
SOI: Start of image marker - Marks the start of a compressed image represented in the interchange format or abbreviated format.
EOI: End of image marker - Marks the end of a compressed image represented in the interchange format or abbreviated format.
$\mathbf{R S T}_{\mathbf{m}}$ : Restart marker - A conditional marker which is placed between entropy-coded segments only if restart is enabled. There are 8 unique restart markers ( $\mathrm{m}=0-7$ ) which repeat in sequence from 0 to 7 , starting with zero for each scan, to provide a modulo 8 restart interval count.

The top level of Figure B. 2 specifies that the non-hierarchical interchange format shall begin with an SOI marker, shall contain one frame, and shall end with an EOI marker.

## 

The second level of Figure B. 2 specifies that a frame shall begin with a frame header and shall contain one or more scans. A frame header may be preceded by one or more table-specification or miscellaneous marker segments as specified in B.2.4. If a DNL segment (see B.2.5) is present, it shall immediately follow the first scan.

For sequential DCT-based and lossless processes each scan shall contain from one to four image components. If two to four components are contained within a scan, they shall be interleaved within the scan. For progressive DCT-based processes each image component is only partially contained within any one scan. Only the first scan(s) for the components (which contain only DC coefficient data) may be interleaved.

The third level of Figure B. 2 specifies that a scan shall begin with a scan header and shall contain one or more entropycoded data segments. Each scan header may be preceded by one or more table-specification or miscellaneous marker segments. If restart is not enabled, there shall be only one entropy-coded segment (the one labeled "last"), and no restart markers shall be present. If restart is enabled, the number of entropy-coded segments is defined by the size of the image and the defined restart interval. In this case, a restart marker shall follow each entropy-coded segment except the last one.

The fourth level of Figure B. 2 specifies that each entropy-coded segment is comprised of a sequence of entropycoded MCUs. If restart is enabled and the restart interval is defined to be Ri, each entropy-coded segment except the last one shall contain Ri MCUs. The last one shall contain whatever number of MCUs completes the scan.

Figure B. 2 specifies the locations where table-specification segments may be present. However, this Specification hereby specifies that the interchange format shall contain all table-specification data necessary for decoding the compressed image. Consequently, the required table-specification data shall be present at one or more of the allowed locations.

## B.2. 2 Frame header syntax

Figure B. 3 specifies the frame header which shall be present at the start of a frame. This header specifies the source image characteristics (see A.1), the components in the frame, and the sampling factors for each component, and specifies the destinations from which the quantized tables to be used with each component are retrieved.


Frame component-specification parameters


Figure B. 3 - Frame header syntax

The markers and parameters shown in Figure B. 3 are defined below. The size and allowed values of each parameter are given in Table B.2. In Table B. 2 (and similar tables which follow), value choices are separated by commas (e.g. 8, 12) and inclusive bounds are separated by dashes (e.g. 0-3).

SOF $_{\mathrm{n}}$ : Start of frame marker - Marks the beginning of the frame parameters. The subscript n identifies whether the encoding process is baseline sequential, extended sequential, progressive, or lossless, as well as which entropy encoding procedure is used.

SOF $\mathbf{0}_{0}$ Baseline DCT
SOF 1 : Extended sequential DCT, Huffman coding

SOF 2 : Progressive DCT, Huffman coding

SOF $_{3}$ : Lossless (sequential), Huffman coding
SOF9: Extended sequential DCT, arithmetic coding
SOF $_{10}$ : Progressive DCT, arithmetic coding
SOF $_{11}$ : Lossless (sequential), arithmetic coding
Lf: Frame header length - Specifies the length of the frame header shown in Figure B. 3 (see B.1.1.4).
P: Sample precision - Specifies the precision in bits for the samples of the components in the frame.
Y: Number of lines - Specifies the maximum number of lines in the source image. This shall be equal to the number of lines in the component with the maximum number of vertical samples (see A.1.1). Value 0 indicates that the number of lines shall be defined by the DNL marker and parameters at the end of the first scan (see B.2.5).

X: Number of samples per line - Specifies the maximum number of samples per line in the source image. This shall be equal to the number of samples per line in the component with the maximum number of horizontal samples (see A.1.1).
Nf: Number of image components in frame - Specifies the number of source image components in the frame. The value of Nf shall be equal to the number of sets of frame component specification parameters $\left(\mathrm{C}_{\mathrm{i}}, \mathrm{H}_{\mathrm{i}}, \mathrm{V}_{\mathrm{i}}\right.$, and $\mathrm{Tq}_{\mathrm{i}}$ ) present in the frame header.
$\mathbf{C}_{\mathbf{i}}$ : Component identifier - Assigns a unique label to the $i$ th component in the sequence of frame component specification parameters. These values shall be used in the scan headers to identify the components in the scan. The value of $\mathrm{C}_{\mathrm{i}}$ shall be different from the values of $\mathrm{C}_{1}$ through $\mathrm{C}_{\mathrm{i}-1}$.
$\mathbf{H}_{\mathbf{i}}$ : Horizontal sampling factor - Specifies the relationship between the component horizontal dimension and maximum image dimension X (see A.1.1); also specifies the number of horizontal data units of component $\mathrm{C}_{\mathrm{i}}$ in each MCU, when more than one component is encoded in a scan.
$\mathbf{V}_{\mathbf{i}}$ : Vertical sampling factor - Specifies the relationship between the component vertical dimension and maximum image dimension $Y$ (see A.1.1); also specifies the number of vertical data units of component $C_{i}$ in each MCU, when more than one component is encoded in a scan.
$\mathbf{T q}_{\mathbf{i}}$ : Quantization table destination selector - Specifies one of four possible quantization table destinations from which the quantization table to use for dequantization of DCT coefficients of component $\mathrm{C}_{\mathrm{i}}$ is retrieved. If the decoding process uses the dequantization procedure, this table shall have been installed in this destination by the time the decoder is ready to decode the scan(s) containing component $\mathrm{C}_{\mathrm{i}}$. The destination shall not be respecified, or its contents changed, until all scans containing $\mathrm{C}_{\mathrm{i}}$ have been completed.

Table B. 2 - Frame header parameter sizes and values

| Parameter | Size (bits) | Values |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Sequential DCT |  | Progressive DCT | Lossless |
|  |  | Baseline | Extended |  |  |
| Lf | 16 | $8+3 \times \mathrm{Nf}$ |  |  |  |
| P | 8 | 8 | 8,12 | 8,12 | 2-16 |
| Y | 16 | 0-65 535 |  |  |  |
| X | 16 | 1-65 535 |  |  |  |
| Nf | 8 | 1-255 | 1-255 | 1-4 | 1-255 |
| $\mathrm{C}_{\mathrm{i}}$ | 8 | 0-255 |  |  |  |
| $\mathrm{H}_{\mathrm{i}}$ | 4 | 1-4 |  |  |  |
| $\mathrm{V}_{\mathrm{i}}$ | 4 | 1-4 |  |  |  |
| Tqi | 8 | 0-3 | 0-3 | 0-3 | 0 |

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## B.2.3 Scan header syntax

Figure B. 4 specifies the scan header which shall be present at the start of a scan. This header specifies which component(s) are contained in the scan, specifies the destinations from which the entropy tables to be used with each component are retrieved, and (for the progressive DCT) which part of the DCT quantized coefficient data is contained in the scan. For lossless processes the scan parameters specify the predictor and the point transform.

NOTE - If there is only one image component present in a scan, that component is, by definition, non-interleaved. If there is more than one image component present in a scan, the components present are, by definition, interleaved.


Figure B. 4 - Scan header syntax

The marker and parameters shown in Figure B. 4 are defined below. The size and allowed values of each parameter are given in Table B.3.

SOS: Start of scan marker - Marks the beginning of the scan parameters.
Ls: Scan header length - Specifies the length of the scan header shown in Figure B. 4 (see B.1.1.4).
Ns: Number of image components in scan - Specifies the number of source image components in the scan. The value of Ns shall be equal to the number of sets of scan component specification parameters $\left(\mathrm{Cs}_{\mathrm{j}}, \mathrm{Td}_{\mathrm{j}}\right.$, and $\left.\mathrm{Ta}_{\mathrm{j}}\right)$ present in the scan header.
$\mathbf{C s}_{\mathbf{j}}$ : Scan component selector - Selects which of the Nf image components specified in the frame parameters shall be the $j$ th component in the scan. Each $\mathrm{Cs}_{j}$ shall match one of the $\mathrm{C}_{\mathrm{i}}$ values specified in the frame header, and the ordering in the scan header shall follow the ordering in the frame header. If Ns $>1$, the order of interleaved components in the MCU is $\mathrm{Cs}_{1}$ first, $\mathrm{Cs}_{2}$ second, etc. If $\mathrm{Ns}>1$, the following restriction shall be placed on the image components contained in the scan:

$$
\sum_{j=1}^{N_{s}} H_{j} \times V_{j} \leq 10
$$

where $H_{j}$ and $V_{j}$ are the horizontal and vertical sampling factors for scan component $j$. These sampling factors are specified in the frame header for component $i$, where $i$ is the frame component specification index for which frame component identifier $\mathrm{C}_{\mathrm{i}}$ matches scan component selector $\mathrm{Cs}_{\mathrm{j}}$.

As an example, consider an image having 3 components with maximum dimensions of 512 lines and 512 samples per line, and with the following sampling factors:

| Component 0 | $H_{0}=4$, | $V_{0}=1$ |
| :--- | :--- | :--- |
| Component 1 | $H_{1}=1$, | $V_{1}=2$ |
| Component 2 | $H_{2}=2$ | $V_{2}=2$ |

Then the summation of $\mathrm{H}_{\mathrm{j}} \times \mathrm{V}_{\mathrm{j}}$ is $(4 \times 1)+(1 \times 2)+(2 \times 2)=10$.
The value of $\mathrm{Cs}_{\mathrm{j}}$ shall be different from the values of $\mathrm{Cs}_{1}$ to $\mathrm{Cs}_{\mathrm{j}-1}$.
$\mathbf{T d}_{\mathbf{j}}$ : DC entropy coding table destination selector - Specifies one of four possible DC entropy coding table destinations from which the entropy table needed for decoding of the DC coefficients of component $\mathrm{Cs}_{\mathrm{j}}$ is retrieved. The DC entropy table shall have been installed in this destination (see B.2.4.2 and B.2.4.3) by the time the decoder is ready to decode the current scan. This parameter specifies the entropy coding table destination for the lossless processes.
$\mathbf{T a}_{\mathbf{j}}$ : AC entropy coding table destination selector - Specifies one of four possible AC entropy coding table destinations from which the entropy table needed for decoding of the AC coefficients of component $\mathrm{Cs}_{\mathrm{j}}$ is retrieved. The AC entropy table selected shall have been installed in this destination (see B.2.4.2 and B.2.4.3) by the time the decoder is ready to decode the current scan. This parameter is zero for the lossless processes.

Ss: Start of spectral or predictor selection - In the DCT modes of operation, this parameter specifies the first DCT coefficient in each block in zig-zag order which shall be coded in the scan. This parameter shall be set to zero for the sequential DCT processes. In the lossless mode of operations this parameter is used to select the predictor.
Se: End of spectral selection - Specifies the last DCT coefficient in each block in zig-zag order which shall be coded in the scan. This parameter shall be set to 63 for the sequential DCT processes. In the lossless mode of operations this parameter has no meaning. It shall be set to zero.

Ah: Successive approximation bit position high - This parameter specifies the point transform used in the preceding scan (i.e. successive approximation bit position low in the preceding scan) for the band of coefficients specified by Ss and Se. This parameter shall be set to zero for the first scan of each band of coefficients. In the lossless mode of operations this parameter has no meaning. It shall be set to zero.

Al: Successive approximation bit position low or point transform - In the DCT modes of operation this parameter specifies the point transform, i.e. bit position low, used before coding the band of coefficients specified by Ss and Se . This parameter shall be set to zero for the sequential DCT processes. In the lossless mode of operations, this parameter specifies the point transform, Pt.

The entropy coding table destination selectors, $\mathrm{Td}_{\mathrm{j}}$ and $\mathrm{Ta}_{\mathrm{j}}$, specify either Huffman tables (in frames using Huffman coding) or arithmetic coding tables (in frames using arithmetic coding). In the latter case the entropy coding table destination selector specifies both an arithmetic coding conditioning table destination and an associated statistics area.

Table B. 3 - Scan header parameter size and values

| Parameter | Size (bits) | Values |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Sequential DCT |  | Progressive DCT | Lossless |
|  |  | Baseline | Extended |  |  |
| Ls | 16 | $6+2 \times \mathrm{Ns}$ |  |  |  |
| Ns | 8 | 1-4 |  |  |  |
| Csj | 8 | 0-255a) |  |  |  |
| Tdj | 4 | 0-1 | 0-3 | 0-3 | 0-3 |
| Taj | 4 | 0-1 | 0-3 | 0-3 | 0 |
| Ss | 8 | 0 | 0 | 0-63 | 1-7b) |
| Se | 8 | 63 | 63 | Ss-63c) | 0 |
| Ah | 4 | 0 | 0 | 0-13 | 0 |
| Al | 4 | 0 | 0 | 0-13 | 0-15 |
| Cs $\mathrm{j}_{\mathrm{j}}$ shall be a member of the set of $\mathrm{C}_{\mathrm{i}}$ specified in the frame header. <br> 0 for lossless differential frames in the hierarchical mode (see B.3). <br> 0 if Ss equals zero. |  |  |  |  |  |

## B.2. 4 Table-specification and miscellaneous marker segment syntax

Figure B. 5 specifies that, at the places indicated in Figure B.2, any of the table-specification segments or miscellaneous marker segments specified in B.2.4.1 through B.2.4.6 may be present in any order and with no limit on the number of segments.

If any table specification for a particular destination occurs in the compressed image data, it shall replace any previous table specified for this destination, and shall be used whenever this destination is specified in the remaining scans in the frame or subsequent images represented in the abbreviated format for compressed image data. If a table specification for a given destination occurs more than once in the compressed image data, each specification shall replace the previous specification. The quantization table specification shall not be altered between progressive DCT scans of a given component.


Figure B. 5 - Tables/miscellaneous marker segment syntax

## B.2.4.1 Quantization table-specification syntax

Figure B. 6 specifies the marker segment which defines one or more quantization tables.


Figure B. 6 - Quantization table syntax

The marker and parameters shown in Figure B. 6 are defined below. The size and allowed values of each parameter are given in Table B.4.

DQT: Define quantization table marker - Marks the beginning of quantization table-specification parameters.
Lq: Quantization table definition length - Specifies the length of all quantization table parameters shown in Figure B. 6 (see B.1.1.4).

Pq: Quantization table element precision - Specifies the precision of the $\mathrm{Q}_{\mathrm{k}}$ values. Value 0 indicates 8-bit $\mathrm{Q}_{\mathrm{k}}$ values; value 1 indicates 16 -bit $\mathrm{Q}_{k}$ values. Pq shall be zero for 8 bit sample precision P (see B.2.2).

Tq: Quantization table destination identifier - Specifies one of four possible destinations at the decoder into which the quantization table shall be installed.
$\mathbf{Q}_{\mathbf{k}}$ : Quantization table element - Specifies the $k$ th element out of 64 elements, where $k$ is the index in the zigzag ordering of the DCT coefficients. The quantization elements shall be specified in zig-zag scan order.

Table B. 4 - Quantization table-specification parameter sizes and values

| Parameter | Size (bits) | Values |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Sequential DCT |  | Progressive DCT | Lossless |
|  |  | Baseline | Extende |  |  |
| Lq | 16 | $2+\sum_{t=1}^{n}(65+64 \times P q(t))$ |  |  | Undefined |
| Pq | 4 | 0 | 0, 1 | 0, 1 | Undefined |
| Tq | 4 | 0-3 |  |  | Undefined |
| $\mathrm{Q}_{\mathrm{k}}$ | 8,16 | 1-255, 1-65 535 |  |  | Undefined |

The value $n$ in Table B. 4 is the number of quantization tables specified in the DQT marker segment.

Once a quantization table has been defined for a particular destination, it replaces the previous tables stored in that destination and shall be used, when referenced, in the remaining scans of the current image and in subsequent images represented in the abbreviated format for compressed image data. If a table has never been defined for a particular destination, then when this destination is specified in a frame header, the results are unpredictable.

An 8-bit DCT-based process shall not use a 16 -bit precision quantization table.

## B.2.4.2 Huffman table-specification syntax

Figure B. 7 specifies the marker segment which defines one or more Huffman table specifications.


$$
\text { Multiple }(t=1, \ldots, n)
$$

Symbol-length assignment parameters


Figure B. 7 - Huffman table syntax

The marker and parameters shown in Figure B. 7 are defined below. The size and allowed values of each parameter are given in Table B.5.

DHT: Define Huffman table marker - Marks the beginning of Huffman table definition parameters.
Lh: Huffman table definition length - Specifies the length of all Huffman table parameters shown in Figure B. 7 (see B.1.1.4).

Tc: Table class $-0=\mathrm{DC}$ table or lossless table, $1=\mathrm{AC}$ table.
Th: Huffman table destination identifier - Specifies one of four possible destinations at the decoder into which the Huffman table shall be installed.
$\mathbf{L}_{\mathbf{i}}$ : Number of Huffman codes of length i - Specifies the number of Huffman codes for each of the 16 possible lengths allowed by this Specification. $\mathrm{L}_{\mathrm{i}}$ 's are the elements of the list BITS.
$\mathbf{V}_{\mathbf{i}, \mathbf{j}}$ : Value associated with each Huffman code - Specifies, for each i , the value associated with each Huffman code of length $i$. The meaning of each value is determined by the Huffman coding model. The $\mathrm{V}_{\mathrm{i}, \mathrm{j}}$ 's are the elements of the list HUFFVAL.

Table B. 5 - Huffman table specification parameter sizes and values

| Parameter | Size (bits) | Values |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Sequential DCT |  | Progressive DCT | Lossless |
|  |  | Baseline | Extended |  |  |
| Lh | 16 | $2+\sum_{t=1}^{n}\left(17+m_{t}\right)$ |  |  |  |
| Tc | 4 | 0,1 |  |  | 0 |
| Th | 4 | 0,1 | 0-3 |  |  |
| $L_{i}$ | 8 | 0-255 |  |  |  |
| $\mathrm{V}_{\mathrm{i}, \mathrm{j}}$ | 8 | 0-255 |  |  |  |

The value n in Table B. 5 is the number of Huffman tables specified in the DHT marker segment. The value $\mathrm{m}_{\mathrm{t}}$ is the number of parameters which follow the $16 \mathrm{~L}_{\mathrm{i}}(\mathrm{t})$ parameters for Huffman table t , and is given by:

$$
m_{t}=\sum_{i=1}^{16} L_{i}
$$

In general, $m_{t}$ is different for each table.

Once a Huffman table has been defined for a particular destination, it replaces the previous tables stored in that destination and shall be used when referenced, in the remaining scans of the current image and in subsequent images represented in the abbreviated format for compressed image data. If a table has never been defined for a particular destination, then when this destination is specified in a scan header, the results are unpredictable.

## B.2.4.3 Arithmetic conditioning table-specification syntax

Figure B. 8 specifies the marker segment which defines one or more arithmetic coding conditioning table specifications. These replace the default arithmetic coding conditioning tables established by the SOI marker for arithmetic coding processes. (See F.1.4.4.1.4 and F.1.4.4.2.1.)


Figure B. 8 - Arithmetic conditioning table-specification syntax

The marker and parameters shown in Figure B. 8 are defined below. The size and allowed values of each parameter are given in Table B. 6 .

DAC: Define arithmetic coding conditioning marker - Marks the beginning of the definition of arithmetic coding conditioning parameters.

La: Arithmetic coding conditioning definition length - Specifies the length of all arithmetic coding conditioning parameters shown in Figure B. 8 (see B.1.1.4).

Tc: Table class $-0=$ DC table or lossless table, $1=$ AC table.
Tb: Arithmetic coding conditioning table destination identifier - Specifies one of four possible destinations at the decoder into which the arithmetic coding conditioning table shall be installed.

Cs: Conditioning table value - Value in either the AC or the DC (and lossless) conditioning table. A single value of Cs shall follow each value of Tb . For AC conditioning tables Tc shall be one and Cs shall contain a value of Kx in the range $1 \leq \mathrm{Kx} \leq 63$. For DC (and lossless) conditioning tables Tc shall be zero and Cs shall contain two 4-bit parameters, $U$ and $L$. $U$ and $L$ shall be in the range $0 \leq L \leq U \leq 15$ and the value of Cs shall be $\mathrm{L}+16 \times \mathrm{U}$.

The value n in Table B. 6 is the number of arithmetic coding conditioning tables specified in the DAC marker segment. The parameters $L$ and $U$ are the lower and upper conditioning bounds used in the arithmetic coding procedures defined for DC coefficient coding and lossless coding. The separate value range 1-63 listed for DCT coding is the Kx conditioning used in AC coefficient coding.

Table B. 6 - Arithmetic coding conditioning table-specification parameter sizes and values

| Parameter | Size (bits) | Values |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Sequential DCT |  | Progressive DCT | Lossless |
|  |  | Baseline | Extended |  |  |
| La | 16 | Undefined | $2+2 \times n$ |  |  |
| Tc | 4 | Undefined | 0, 1 |  | 0 |
| Tb | 4 | Undefined | 0-3 |  |  |
| Cs | 8 | Undefined | 0-255 (T | $1-63(\mathrm{Tc}=1)$ | 0-255 |

## B.2.4.4 Restart interval definition syntax

Figure B. 9 specifies the marker segment which defines the restart interval.


Figure B. 9 - Restart interval definition syntax

The marker and parameters shown in Figure B. 9 are defined below. The size and allowed values of each parameter are given in Table B.7.

DRI: Define restart interval marker - Marks the beginning of the parameters which define the restart interval.
Lr: Define restart interval segment length - Specifies the length of the parameters in the DRI segment shown in Figure B. 9 (see B.1.1.4).

Ri: Restart interval - Specifies the number of MCU in the restart interval.

In Table B. 7 the value n is the number of rows of MCU in the restart interval. The value MCUR is the number of MCU required to make up one line of samples of each component in the scan. The SOI marker disables the restart intervals. A DRI marker segment with Ri nonzero shall be present to enable restart interval processing for the following scans. A DRI marker segment with Ri equal to zero shall disable restart intervals for the following scans.

Table B. 7 - Define restart interval segment parameter sizes and values

| Parameter | Values |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Sequential DCT |  |  | Progressive DCT | Lossless

## B.2.4.5 Comment syntax

Figure B. 10 specifies the marker segment structure for a comment segment.


Figure B. 10 - Comment segment syntax

The marker and parameters shown in Figure B. 10 are defined below. The size and allowed values of each parameter are given in Table B.8.

COM: Comment marker - Marks the beginning of a comment.
Lc: Comment segment length - Specifies the length of the comment segment shown in Figure B. 10 (see B.1.1.4).
$\mathbf{C m}_{\mathbf{i}}$ : Comment byte - The interpretation is left to the application.
Table B. 8 - Comment segment parameter sizes and values

| Parameter | Size (bits) | Values |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  | Sequential DCT | Progressive DCT | Lossless |
|  |  | Baseline |  |  |
| Lc | 16 |  | $2-65535$ |  |
| $\mathrm{Cm}_{\mathrm{i}}$ | 8 |  | $0-255$ |  |

## B.2.4.6 Application data syntax

Figure B. 11 specifies the marker segment structure for an application data segment.


Figure B. 11 - Application data syntax

The marker and parameters shown in Figure B. 11 are defined below. The size and allowed values of each parameter are given in Table B.9.
$\mathbf{A P P}_{\mathrm{n}}$ : Application data marker - Marks the beginning of an application data segment.
Lp: Application data segment length - Specifies the length of the application data segment shown in Figure B. 11 (see B.1.1.4).
Api: Application data byte - The interpretation is left to the application.
The $\mathrm{APP}_{\mathrm{n}}$ (Application) segments are reserved for application use. Since these segments may be defined differently for different applications, they should be removed when the data are exchanged between application environments.

Table B. 9 - Application data segment parameter sizes and values

| Parameter | Size (bits) | Values |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Sequential DCT | Progressive DCT | Lossless |  |
|  |  | Baseline |  |  |  |
| Lp | 16 |  | $2-65535$ |  |  |
| $\mathrm{Ap}_{\mathrm{i}}$ | 8 |  | $0-255$ |  |  |

## B.2.5

 Define number of lines syntaxFigure B. 12 specifies the marker segment for defining the number of lines. The DNL (Define Number of Lines) segment provides a mechanism for defining or redefining the number of lines in the frame (the Y parameter in the frame header) at the end of the first scan. The value specified shall be consistent with the number of MCU-rows encoded in the first scan. This segment, if used, shall only occur at the end of the first scan, and only after coding of an integer number of MCUrows. This marker segment is mandatory if the number of lines $(\mathrm{Y})$ specified in the frame header has the value zero.


Figure B. 12 - Define number of lines syntax

The marker and parameters shown in Figure B. 12 are defined below. The size and allowed values of each parameter are given in Table B. 10 .

DNL: Define number of lines marker - Marks the beginning of the define number of lines segment.

Ld: Define number of lines segment length - Specifies the length of the define number of lines segment shown in Figure B. 12 (see B.1.1.4).

NL: Number of lines - Specifies the number of lines in the frame (see definition of Y in B.2.2).

Table B. 10 - Define number of lines segment parameter sizes and values

| Parameter | Size (bits) | Values |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Sequential DCT |  | Progressive DCT | Lossless |
|  |  | Baseline | Extended |  |  |
| Ld | 16 | 4 |  |  |  |
| NL | 16 | $1-65535^{\text {a }}$ |  |  |  |
| The value specified shall be consistent with the number of lines coded at the point where the DNL segment terminates the compressed data segment. |  |  |  |  |  |

## B. 3 Hierarchical syntax

## B.3.1 High level hierarchical mode syntax

Figure B. 13 specifies the order of the high level constituent parts of the interchange format for hierarchical encoding processes.

Compressed image data


Figure B. 13 - Syntax for the hierarchical mode of operation

Hierarchical mode syntax requires a DHP marker segment that appears before the non-differential frame or frames. The hierarchical mode compressed image data may include EXP marker segments and differential frames which shall follow the initial non-differential frame. The frame structure in hierarchical mode is identical to the frame structure in nonhierarchical mode.

The non-differential frames in the hierarchical sequence shall use one of the coding processes specified for $\mathrm{SOF}_{\mathrm{n}}$ markers: $\mathrm{SOF}_{0}, \mathrm{SOF}_{1}, \mathrm{SOF}_{2}, \mathrm{SOF}_{3}, \mathrm{SOF}_{9}, \mathrm{SOF}_{10}$ and $\mathrm{SOF}_{11}$. The differential frames shall use one of the processes specified for $\mathrm{SOF}_{5}, \mathrm{SOF}_{6}, \mathrm{SOF}_{7}, \mathrm{SOF}_{13}, \mathrm{SOF}_{14}$ and $\mathrm{SOF}_{15}$. The allowed combinations of SOF markers within one hierarchical sequence are specified in Annex J.

The sample precision ( P ) shall be constant for all frames and have the identical value as that coded in the DHP marker segment. The number of samples per line ( X ) for all frames shall not exceed the value coded in the DHP marker segment. If the number of lines $(\mathrm{Y})$ is non-zero in the DHP marker segment, then the number of lines for all frames shall not exceed the value in the DHP marker segment.

## B.3.2 DHP segment syntax

The DHP segment defines the image components, size, and sampling factors for the completed hierarchical sequence of frames. The DHP segment shall precede the first frame; a single DHP segment shall occur in the compressed image data.

The DHP segment structure is identical to the frame header syntax, except that the DHP marker is used instead of the $\mathrm{SOF}_{\mathrm{n}}$ marker. The figures and description of B.2.2 then apply, except that the quantization table destination selector parameter shall be set to zero in the DHP segment.

## B.3.3 EXP segment syntax

Figure B. 14 specifies the marker segment structure for the EXP segment. The EXP segment shall be present if (and only if) expansion of the reference components is required either horizontally or vertically. The EXP segment parameters apply only to the next frame (which shall be a differential frame) in the image. If required, the EXP segment shall be one of the table-specification segments or miscellaneous marker segments preceding the frame header; the EXP segment shall not be one of the table-specification segments or miscellaneous marker segments preceding a scan header or a DHP marker segment.


Figure B. 14 - Syntax of the expand segment

The marker and parameters shown in Figure B. 14 are defined below. The size and allowed values of each parameter are given in Table B.11.

EXP: Expand reference components marker - Marks the beginning of the expand reference components segment.

Le: Expand reference components segment length - Specifies the length of the expand reference components segment (see B.1.1.4).

Eh: Expand horizontally - If one, the reference components shall be expanded horizontally by a factor of two. If horizontal expansion is not required, the value shall be zero.

Ev: Expand vertically - If one, the reference components shall be expanded vertically by a factor of two. If vertical expansion is not required, the value shall be zero.
Both Eh and Ev shall be one if expansion is required both horizontally and vertically.
Table B. 11 - Expand segment parameter sizes and values

| Parameter | Size (bits) | Values |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Sequential DCT |  | Progressive DCT | Lossless |
|  |  | Baseline | Extended |  |  |
| Le | 16 | 3 |  |  |  |
| Eh | 4 | 0, 1 |  |  |  |
| Ev | 4 | 0,1 |  |  |  |

## B. 4 Abbreviated format for compressed image data

Figure B. 2 shows the high-level constituent parts of the interchange format. This format includes all table specifications required for decoding. If an application environment provides methods for table specification other than by means of the compressed image data, some or all of the table specifications may be omitted. Compressed image data which is missing any table specification data required for decoding has the abbreviated format.

## B. 5 Abbreviated format for table-specification data

Figure B. 2 shows the high-level constituent parts of the interchange format. If no frames are present in the compressed image data, the only purpose of the compressed image data is to convey table specifications or miscellaneous marker segments defined in B.2.4.1, B.2.4.2, B.2.4.5, and B.2.4.6. In this case the compressed image data has the abbreviated format for table specification data (see Figure B.15).


Figure B. 15 - Abbreviated format for table-specification data syntax

## B. 6 Summary

The order of the constituent parts of interchange format and all marker segment structures is summarized in Figures B. 16 and B.17. Note that in Figure B. 16 double-lined boxes enclose marker segments. In Figures B. 16 and B. 17 thick-lined boxes enclose only markers.

The EXP segment can be mixed with the other tables/miscellaneous marker segments preceding the frame header but not with the tables/miscellaneous marker segments preceding the DHP segment or the scan header.


$\xrightarrow{(\mathrm{DNL} \text { segment) }} \rightarrow \mathrm{DNL} \rightarrow \mathrm{Ld} \rightarrow$
$\xrightarrow{\text { (EXP segment) }} \rightarrow \mathrm{EXP} \rightarrow \mathrm{Eh} \rightarrow \mathrm{Ev} \rightarrow \mathrm{O}$

Figure B. 17 - Flow of marker segment

# Annex C <br> Huffman table specification <br> (This annex forms an integral part of this Recommendation | International Standard) 

A Huffman coding procedure may be used for entropy coding in any of the coding processes. Coding models for Huffman encoding are defined in Annexes F, G, and H. In this Annex, the Huffman table specification is defined.

Huffman tables are specified in terms of a 16-byte list (BITS) giving the number of codes for each code length from 1 to 16 . This is followed by a list of the 8 -bit symbol values (HUFFVAL), each of which is assigned a Huffman code. The symbol values are placed in the list in order of increasing code length. Code lengths greater than 16 bits are not allowed. In addition, the codes shall be generated such that the all-1-bits code word of any length is reserved as a prefix for longer code words.

NOTE - The order of the symbol values within HUFFVAL is determined only by code length. Within a given code length the ordering of the symbol values is arbitrary.

This annex specifies the procedure by which the Huffman tables (of Huffman code words and their corresponding 8-bit symbol values) are derived from the two lists (BITS and HUFFVAL) in the interchange format. However, the way in which these lists are generated is not specified. The lists should be generated in a manner which is consistent with the rules for Huffman coding, and it shall observe the constraints discussed in the previous paragraph. Annex K contains an example of a procedure for generating lists of Huffman code lengths and values which are in accord with these rules.

NOTE - There is no requirement in this Specification that any encoder or decoder shall implement the procedures in precisely the manner specified by the flow charts in this annex. It is necessary only that an encoder or decoder implement the function specified in this annex. The sole criterion for an encoder or decoder to be considered in compliance with this Specification is that it satisfy the requirements given in clause 6 (for encoders) or clause 7 (for decoders), as determined by the compliance tests specified in Part 2.

## C. 1 Marker segments for Huffman table specification

The DHT marker identifies the start of Huffman table definitions within the compressed image data. B.2.4.2 specifies the syntax for Huffman table specification.

## C. 2 Conversion of Huffman table specifications to tables of codes and code lengths

Conversion of Huffman table specifications to tables of codes and code lengths uses three procedures. The first procedure (Figure C.1) generates a table of Huffman code sizes. The second procedure (Figure C.2) generates the Huffman codes from the table built in Figure C.1. The third procedure (Figure C.3) generates the Huffman codes in symbol value order.

Given a list BITS ( 1 to 16 ) containing the number of codes of each size, and a list HUFFVAL containing the symbol values to be associated with those codes as described above, two tables are generated. The HUFFSIZE table contains a list of code lengths; the HUFFCODE table contains the Huffman codes corresponding to those lengths.

Note that the variable LASTK is set to the index of the last entry in the table.


Figure C. 1 - Generation of table of Huffman code sizes

A Huffman code table, HUFFCODE, containing a code for each size in HUFFSIZE is generated by the procedure in Figure C.2. The notation "SLL CODE 1" in Figure C. 2 indicates a shift-left-logical of CODE by one bit position.


Figure C. 2 - Generation of table of Huffman codes

Two tables, HUFFCODE and HUFFSIZE, have now been generated. The entries in the tables are ordered according to increasing Huffman code numeric value and length.

The encoding procedure code tables, EHUFCO and EHUFSI, are created by reordering the codes specified by HUFFCODE and HUFFSIZE according to the symbol values assigned to each code in HUFFVAL.

Figure C. 3 illustrates this ordering procedure.


Figure C. 3 - Ordering procedure for encoding procedure code tables

## C. 3 Bit ordering within bytes

The root of a Huffman code is placed toward the MSB (most-significant-bit) of the byte, and successive bits are placed in the direction MSB to LSB (least-significant-bit) of the byte. Remaining bits, if any, go into the next byte following the same rules.

Integers associated with Huffman codes are appended with the MSB adjacent to the LSB of the preceding Huffman code.

Annex D<br>Arithmetic coding<br>(This annex forms an integral part of this Recommendation | International Standard)

An adaptive binary arithmetic coding procedure may be used for entropy coding in any of the coding processes except the baseline sequential process. Coding models for adaptive binary arithmetic coding are defined in Annexes F, G, and H . In this annex the arithmetic encoding and decoding procedures used in those models are defined.

In K. 4 a simple test example is given which should be helpful in determining if a given implementation is correct.
NOTE - There is no requirement in this Specification that any encoder or decoder shall implement the procedures in precisely the manner specified by the flow charts in this annex. It is necessary only that an encoder or decoder implement the function specified in this annex. The sole criterion for an encoder or decoder to be considered in compliance with this Specification is that it satisfy the requirements given in clause 6 (for encoders) or clause 7 (for decoders), as determined by the compliance tests specified in Part 2.

## D. 1 Arithmetic encoding procedures

Four arithmetic encoding procedures are required in a system with arithmetic coding (see Table D.1).
Table D. 1 - Procedures for binary arithmetic encoding

| Procedure | Purpose |
| :--- | :--- |
| Code_0(S) | Code a "0" binary decision with context-index S |
| Code_1(S) | Code a "1" binary decision with context-index S |
| Initenc | Initialize the encoder |
| Flush | Terminate entropy-coded segment |

The "Code_0(S)" and "Code_1(S)" procedures code the 0 -decision and 1 -decision respectively; S is a context-index which identifies a particular conditional probability estimate used in coding the binary decision. The "Initenc" procedure initializes the arithmetic coding entropy encoder. The "Flush" procedure terminates the entropy-coded segment in preparation for the marker which follows.

## D.1.1 Binary arithmetic encoding principles

The arithmetic coder encodes a series of binary symbols, zeros and ones, each symbol representing one possible result of a binary decision.

Each "binary decision" provides a choice between two alternatives. The binary decision might be between positive and negative signs, a magnitude being zero or nonzero, or a particular bit in a sequence of binary digits being zero or one.

The output bit stream (entropy-coded data segment) represents a binary fraction which increases in precision as bytes are appended by the encoding process.

## D.1.1.1 Recursive interval subdivision

Recursive probability interval subdivision is the basis for the binary arithmetic encoding procedures. With each binary decision the current probability interval is subdivided into two sub-intervals, and the bit stream is modified (if necessary) so that it points to the base (the lower bound) of the probability sub-interval assigned to the symbol which occurred.

In the partitioning of the current probability interval into two sub-intervals, the sub-interval for the less probable symbol (LPS) and the sub-interval for the more probable symbol (MPS) are ordered such that usually the MPS sub-interval is closer to zero. Therefore, when the LPS is coded, the MPS sub-interval size is added to the bit stream. This coding convention requires that symbols be recognized as either MPS or LPS rather than 0 or 1 . Consequently, the size of the LPS sub-interval and the sense of the MPS for each decision must be known in order to encode that decision.

## 

The subdivision of the current probability interval would ideally require a multiplication of the interval by the probability estimate for the LPS. Because this subdivision is done approximately, it is possible for the LPS sub-interval to be larger than the MPS sub-interval. When that happens a "conditional exchange" interchanges the assignment of the sub-intervals such that the MPS is given the larger sub-interval.

Since the encoding procedure involves addition of binary fractions rather than concatenation of integer code words, the more probable binary decisions can sometimes be coded at a cost of much less than one bit per decision.

## D.1.1.2 Conditioning of probability estimates

An adaptive binary arithmetic coder requires a statistical model - a model for selecting conditional probability estimates to be used in the coding of each binary decision. When a given binary decision probability estimate is dependent on a particular feature or features (the context) already coded, it is "conditioned" on that feature. The conditioning of probability estimates on previously coded decisions must be identical in encoder and decoder, and therefore can use only information known to both.

Each conditional probability estimate required by the statistical model is kept in a separate storage location or "bin" identified by a unique context-index $S$. The arithmetic coder is adaptive, which means that the probability estimates at each context-index are developed and maintained by the arithmetic coding system on the basis of prior coding decisions for that context-index.

## D.1.2 Encoding conventions and approximations

The encoding procedures use fixed precision integer arithmetic and an integer representation of fractional values in which $X^{\prime} 8000^{\prime}$ can be regarded as the decimal value 0.75 . The probability interval, A, is kept in the integer range $X^{\prime} 8000^{\prime} \leq A<X^{\prime} 10000^{\prime}$ by doubling it whenever its integer value falls below $X^{\prime} 8000^{\prime}$. This is equivalent to keeping A in the decimal range $0.75 \leq \mathrm{A}<1.5$. This doubling procedure is called renormalization.

The code register, C , contains the trailing bits of the bit stream. C is also doubled each time A is doubled. Periodically - to keep C from overflowing - a byte of data is removed from the high order bits of the C-register and placed in the entropy-coded segment.

Carry-over into the entropy-coded segment is limited by delaying $X^{\prime}{ }^{\prime} \mathrm{FF}^{\prime}$ output bytes until the carry-over is resolved. Zero bytes are stuffed after each X'FF' byte in the entropy-coded segment in order to avoid the accidental generation of markers in the entropy-coded segment.

Keeping A in the range $0.75 \leq \mathrm{A}<1.5$ allows a simple arithmetic approximation to be used in the probability interval subdivision. Normally, if the current estimate of the LPS probability for context-index S is Qe(S), precise calculation of the sub-intervals would require:

$$
\begin{array}{ll}
\mathrm{Qe}(\mathrm{~S}) \times \mathrm{A} & \text { Probability sub-interval for the LPS; } \\
\mathrm{A}-(\mathrm{Qe}(\mathrm{~S}) \times \mathrm{A}) & \text { Probability sub-interval for the MPS }
\end{array}
$$

Because the decimal value of A is of order unity, these can be approximated by

$$
\begin{array}{ll}
\mathrm{Qe}(\mathrm{~S}) & \text { Probability sub-interval for the LPS; } \\
\mathrm{A}-\mathrm{Qe}(\mathrm{~S}) & \text { Probability sub-interval for the MPS }
\end{array}
$$

Whenever the LPS is coded, the value of $\mathrm{A}-\mathrm{Qe}(\mathrm{S})$ is added to the code register and the probability interval is reduced to $\mathrm{Qe}(\mathrm{S})$. Whenever the MPS is coded, the code register is left unchanged and the interval is reduced to $\mathrm{A}-\mathrm{Qe}(\mathrm{S})$. The precision range required for $A$ is then restored, if necessary, by renormalization of both $A$ and $C$.

With the procedure described above, the approximations in the probability interval subdivision process can sometimes make the LPS sub-interval larger than the MPS sub-interval. If, for example, the value of $\mathrm{Qe}(\mathrm{S})$ is 0.5 and A is at the minimum allowed value of 0.75 , the approximate scaling gives one-third of the probability interval to the MPS and twothirds to the LPS. To avoid this size inversion, conditional exchange is used. The probability interval is subdivided using the simple approximation, but the MPS and LPS sub-interval assignments are exchanged whenever the LPS sub-interval is larger than the MPS sub-interval. This MPS/LPS conditional exchange can only occur when a renormalization will be needed.

Each binary decision uses a context. A context is the set of prior coding decisions which determine the context-index, $S$, identifying the probability estimate used in coding the decision.

Whenever a renormalization occurs, a probability estimation procedure is invoked which determines a new probability estimate for the context currently being coded. No explicit symbol counts are needed for the estimation. The relative probabilities of renormalization after coding of LPS and MPS provide, by means of a table-based probability estimation state machine, a direct estimate of the probabilities.

## D.1.3 Encoder code register conventions

The flow charts in this annex assume the register structures for the encoder as shown in Table D.2.

Table D. 2 - Encoder register connections

|  | MSB |  | LSB |  |
| :--- | :--- | :--- | :--- | :--- |
| C-register | 0000 cbbb, | bbbbbsss, | xxxxxxxx, | xxxxxxxx |
| A-register | 00000000, | 00000000, | aaaaaaaa, | aaaaaaaa |

The "a" bits are the fractional bits in the A-register (the current probability interval value) and the " x " bits are the fractional bits in the code register. The " $s$ " bits are optional spacer bits which provide useful constraints on carry-over, and the "b" bits indicate the bit positions from which the completed bytes of data are removed from the C-register. The "c" bit is a carry bit. Except at the time of initialization, bit 15 of the A-register is always set and bit 16 is always clear (the LSB is bit 0 ).

These register conventions illustrate one possible implementation. However, any register conventions which allow resolution of carry-over in the encoder and which produce the same entropy-coded segment may be used. The handling of carry-over and the byte stuffing following X'FF' will be described in a later part of this annex.

## D.1.4 Code_1(S) and Code_0(S) procedures

When a given binary decision is coded, one of two possibilities occurs - either a 1-decision or a 0 -decision is coded. Code_1(S) and Code_0(S) are shown in Figures D. 1 and D.2. The Code_1(S) and Code_0(S) procedures use probability estimates with a context-index S . The context-index S is determined by the statistical model and is, in general, a function of the previous coding decisions; each value of $S$ identifies a particular conditional probability estimate which is used in encoding the binary decision.


Figure D. 1 - Code_1(S) procedure


Figure D. 2 - Code_0(S) procedure

The context-index S selects a storage location which contains Index(S), an index to the tables which make up the probability estimation state machine. When coding a binary decision, the symbol being coded is either the more probable symbol or the less probable symbol. Therefore, additional information is stored at each context-index identifying the sense of the more probable symbol, MPS(S).

For simplicity, the flow charts in this subclause assume that the context storage for each context-index S has an additional storage field for $\mathrm{Qe}(\mathrm{S})$ containing the value of $\mathrm{Qe}(\operatorname{Index}(\mathrm{S}))$. If only the value of Index(S) and MPS(S) are stored, all references to $\mathrm{Qe}(\mathrm{S})$ should be replaced by $\mathrm{Qe}(\operatorname{Index}(\mathrm{S}))$.

The Code_LPS(S) procedure normally consists of the addition of the MPS sub-interval $\mathrm{A}-\mathrm{Qe}(\mathrm{S})$ to the bit stream and a scaling of the interval to the sub-interval, $\mathrm{Qe}(\mathrm{S})$. It is always followed by the procedures for obtaining a new LPS probability estimate (Estimate_Qe(S)_after_LPS) and renormalization (Renorm_e) (see Figure D.3).

However, in the event that the LPS sub-interval is larger than the MPS sub-interval, the conditional MPS/LPS exchange occurs and the MPS sub-interval is coded.

The Code_MPS(S) procedure normally reduces the size of the probability interval to the MPS sub-interval. However, if the LPS sub-interval is larger than the MPS sub-interval, the conditional exchange occurs and the LPS sub-interval is coded instead. Note that conditional exchange cannot occur unless the procedures for obtaining a new LPS probability estimate (Estimate_Qe(S)_after_MPS) and renormalization (Renorm_e) are required after the coding of the symbol (see Figure D.4).


Figure D. 3 - Code_LPS(S) procedure with conditional MPS/LPS exchange


Figure D. 4 - Code_MPS(S) procedure with conditional MPS/LPS exchange

## D.1.5 Probability estimation in the encoder

## D.1.5.1 Probability estimation state machine

The probability estimation state machine consists of a number of sequences of probability estimates. These sequences are interlinked in a manner which provides probability estimates based on approximate symbol counts derived from the arithmetic coder renormalization. Some of these sequences are used during the initial "learning" stages of probability estimation; the rest are used for "steady state" estimation.

Each entry in the probability estimation state machine is assigned an index, and each index has associated with it a Qe value and two Next_Index values. The Next_Index_MPS gives the index to the new probability estimate after an MPS renormalization; the Next_Index_LPS gives the index to the new probability estimate after an LPS renormalization. Note that both the index to the estimation state machine and the sense of the MPS are kept for each context-index S. The sense of the MPS is changed whenever the entry in the Switch_MPS is one.

The probability estimation state machine is given in Table D.3. Initialization of the arithmetic coder is always with an MPS sense of zero and a Qe index of zero in Table D.3.

The Qe values listed in Table D. 3 are expressed as hexadecimal integers. To approximately convert the 15 -bit integer representation of Qe to a decimal probability, divide the Qe values by $(4 / 3) \times\left(\mathrm{X}^{\prime} 8000\right.$ ' $)$.

Table D. 3 - Qe values and probability estimation state machine

| Index | Qe <br> _Value | Next_Index |  | Switch _MPS | Index | Qe _Value | Next_ Index |  | Switch _MPS |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | _LPS | _MPS |  |  |  | _LPS | _MPS |  |
| 0 | X'5A1D' | 1 | 1 | 1 | 57 | X'01A4 ${ }^{\prime}$ | 55 | 58 | 0 |
| 1 | X'2586' | 14 | 2 | 0 | 58 | X'0160' | 56 | 59 | 0 |
| 2 | X'1114' | 16 | 3 | 0 | 59 | X'0125' | 57 | 60 | 0 |
| 3 | X'080B' | 18 | 4 | 0 | 60 | X'00F6' | 58 | 61 | 0 |
| 4 | X'03D8' | 20 | 5 | 0 | 61 | X'00CB' | 59 | 62 | 0 |
| 5 | X'01DA' | 23 | 6 | 0 | 62 | X'00AB' | 61 | 63 | 0 |
| 6 | X'00E5' | 25 | 7 | 0 | 63 | X'008F' | 61 | 32 | 0 |
| 7 | X'006F' | 28 | 8 | 0 | 64 | X'5B12' | 65 | 65 | 1 |
| 8 | X'0036' | 30 | 9 | 0 | 65 | X'4D04' | 80 | 66 | 0 |
| 9 | X'001A' | 33 | 10 | 0 | 66 | X'412C' | 81 | 67 | 0 |
| 10 | X'000D' | 35 | 11 | 0 | 67 | X'37D8' | 82 | 68 | 0 |
| 11 | X'0006' | 9 | 12 | 0 | 68 | X'2FE8' | 83 | 69 | 0 |
| 12 | X'0003' | 10 | 13 | 0 | 69 | X'293C' | 84 | 70 | 0 |
| 13 | X'0001' | 12 | 13 | 0 | 70 | X'2379' | 86 | 71 | 0 |
| 14 | X'5A7F' | 15 | 15 | 1 | 71 | X'1EDF' | 87 | 72 | 0 |
| 15 | X'3F25, | 36 | 16 | 0 | 72 | X'1AA9' | 87 | 73 | 0 |
| 16 | X'2CF2' | 38 | 17 | 0 | 73 | X'174E' | 72 | 74 | 0 |
| 17 | X'207C' | 39 | 18 | 0 | 74 | X'1424' | 72 | 75 | 0 |
| 18 | X'17B9' | 40 | 19 | 0 | 75 | X'119C' | 74 | 76 | 0 |
| 19 | X'1182' | 42 | 20 | 0 | 76 | X'0F6B' | 74 | 77 | 0 |
| 20 | X'0CEF' | 43 | 21 | 0 | 77 | X'0D51' | 75 | 78 | 0 |
| 21 | X'09A1' | 45 | 22 | 0 | 78 | X'0BB6' | 77 | 79 | 0 |
| 22 | X'072F' | 46 | 23 | 0 | 79 | X'0A40' | 77 | 48 | 0 |
| 23 | X'055C' | 48 | 24 | 0 | 80 | X'5832' | 80 | 81 | 1 |
| 24 | X'0406' | 49 | 25 | 0 | 81 | X'4D1C' | 88 | 82 | 0 |
| 25 | X'0303' | 51 | 26 | 0 | 82 | X'438E' | 89 | 83 | 0 |
| 26 | X'0240' | 52 | 27 | 0 | 83 | X'3BDD' | 90 | 84 | 0 |
| 27 | X'01B1' | 54 | 28 | 0 | 84 | X'34EE' | 91 | 85 | 0 |
| 28 | X'0144' | 56 | 29 | 0 | 85 | X'2EAE' | 92 | 86 | 0 |
| 29 | X'00F5' | 57 | 30 | 0 | 86 | X'299A' | 93 | 87 | 0 |
| 30 | X'00B7' | 59 | 31 | 0 | 87 | X'2516' | 86 | 71 | 0 |
| 31 | $\mathrm{X}^{\prime} 008 \mathrm{~A}^{\prime}$ | 60 | 32 | 0 | 88 | X'5570' | 88 | 89 | 1 |
| 32 | X'0068' | 62 | 33 | 0 | 89 | X'4CA9' | 95 | 90 | 0 |
| 33 | X'004E' | 63 | 34 | 0 | 90 | X'44D9' | 96 | 91 | 0 |
| 34 | X'003B' | 32 | 35 | 0 | 91 | X'3E22' | 97 | 92 | 0 |
| 35 | X'002C' | 33 | 9 | 0 | 92 | X'3824' | 99 | 93 | 0 |
| 36 | X'5AE1' | 37 | 37 | 1 | 93 | X'32B4' | 99 | 94 | 0 |
| 37 | X'484C' | 64 | 38 | 0 | 94 | X'2E17' | 93 | 86 | 0 |
| 38 | X'3A0D' | 65 | 39 | 0 | 95 | X'56A8' | 95 | 96 | 1 |
| 39 | X'2EF1' | 67 | 40 | 0 | 96 | X'4F46' | 101 | 97 | 0 |
| 40 | X'261F' | 68 | 41 | 0 | 97 | X'47E5' | 102 | 98 | 0 |
| 41 | X'1F33' | 69 | 42 | 0 | 98 | X'41CF' | 103 | 99 | 0 |
| 42 | X'19A8' | 70 | 43 | 0 | 99 | X'3C3D' | 104 | 100 | 0 |
| 43 | X'1518' | 72 | 44 | 0 | 100 | X'375E' | 99 | 93 | 0 |
| 44 | X'1177' | 73 | 45 | 0 | 101 | X'5231' | 105 | 102 | 0 |
| 45 | X'0E74' | 74 | 46 | 0 | 102 | X'4C0F' | 106 | 103 | 0 |
| 46 | X'0BFB' | 75 | 47 | 0 | 103 | X'4639' | 107 | 104 | 0 |
| 47 | X'09F8' | 77 | 48 | 0 | 104 | X'415E' | 103 | 99 | 0 |
| 48 | X'0861' | 78 | 49 | 0 | 105 | X'5627' | 105 | 106 | 1 |
| 49 | X'0706' | 79 | 50 | 0 | 106 | X'50E7' | 108 | 107 | 0 |
| 50 | X'05CD' | 48 | 51 | 0 | 107 | X'4B85' | 109 | 103 | 0 |
| 51 | X'04DE' | 50 | 52 | 0 | 108 | X'5597' | 110 | 109 | 0 |
| 52 | X'040F' | 50 | 53 | 0 | 109 | X'504F' | 111 | 107 | 0 |
| 53 | X'0363' | 51 | 54 | 0 | 110 | X'5A10' | 110 | 111 | 1 |
| 54 | X'02D4' | 52 | 55 | 0 | 111 | X'5522' | 112 | 109 | 0 |
| 55 | X'025C' | 53 | 56 | 0 | 112 | X'59EB' | 112 | 111 | 1 |
| 56 | X'01F8' | 54 | 57 | 0 |  |  |  |  |  |

## D.1.5.2 Renormalization driven estimation

The change in state in Table D. 3 occurs only when the arithmetic coder interval register is renormalized. This must always be done after coding an LPS, and whenever the probability interval register is less than $X^{\prime} 8000$ ' ( 0.75 in decimal notation) after coding an MPS.

When the LPS renormalization is required, Next_Index_LPS gives the new index for the LPS probability estimate. When the MPS renormalization is required, Next_Index_MPS gives the new index for the LPS probability estimate. If Switch_MPS is 1 for the old index, the MPS symbol sense must be inverted after an LPS.

## D.1.5.3 Estimation following renormalization after MPS

The procedure for estimating the probability on the MPS renormalization path is given in Figure D.5. Index $(\mathrm{S})$ is part of the information stored for context-index S. The new value of $\operatorname{Index}(\mathrm{S})$ is obtained from Table D. 3 from the column labeled Next_Index_MPS, as that is the next index after an MPS renormalization. This next index is stored as the new value of Index(S) in the context storage at context-index S, and the value of Qe at this new Index(S) becomes the new $\mathrm{Qe}(\mathrm{S})$. MPS(S) does not change.


Figure D. 5 - Probability estimation on MPS renormalization path

## D.1.5.4 Estimation following renormalization after LPS

The procedure for estimating the probability on the LPS renormalization path is shown in Figure D.6. The procedure is similar to that of Figure D. 5 except that when Switch_MPS(I) is 1, the sense of MPS(S) must be inverted.


Figure D. 6 - Probability estimation on LPS renormalization path

## D.1.6 Renormalization in the encoder

The Renorm_e procedure for the encoder renormalization is shown in Figure D.7. Both the probability interval register A and the code register C are shifted, one bit at a time. The number of shifts is counted in the counter CT; when CT is zero, a byte of compressed data is removed from C by the procedure Byte_out and CT is reset to 8 . Renormalization continues until A is no longer less than $X^{\prime} 8000^{\prime}$.


Figure D. 7 - Encoder renormalization procedure

The Byte_out procedure used in Renorm_e is shown in Figure D.8. This procedure uses byte-stuffing procedures which prevent accidental generation of markers by the arithmetic encoding procedures. It also includes an example of a procedure for resolving carry-over. For simplicity of exposition, the buffer holding the entropy-coded segment is assumed to be large enough to contain the entire segment.

In Figure D. 8 BP is the entropy-coded segment pointer and B is the compressed data byte pointed to by BP. T in Byte_out is a temporary variable which is used to hold the output byte and carry bit. ST is the stack counter which is used to count X'FF' output bytes until any carry-over through the X'FF' sequence has been resolved. The value of ST rarely exceeds 3. However, since the upper limit for the value of ST is bounded only by the total entropy-coded segment size, a precision of 32 bits is recommended for ST.

Since large values of ST represent a latent output of compressed data, the following procedure may be needed in high speed synchronous encoding systems for handling the burst of output data which occurs when the carry is resolved.


Figure D. 8 - Byte_out procedure for encoder

When the stack count reaches an upper bound determined by output channel capacity, the stack is emptied and the stacked X'FF' bytes (and stuffed zero bytes) are added to the compressed data before the carry-over is resolved. If a carry-over then occurs, the carry is added to the final stuffed zero, thereby converting the final X'FF00' sequence to the $X^{\prime}$ FF01' temporary private marker. The entropy-coded segment must then be post-processed to resolve the carry-over and remove the temporary marker code. For any reasonable bound on ST this post processing is very unlikely.

Referring to Figure D.8, the shift of the code register by 19 bits aligns the output bits with the low order bits of T. The first test then determines if a carry-over has occurred. If so, the carry must be added to the previous output byte before advancing the segment pointer BP. The Stuff_0 procedure stuffs a zero byte whenever the addition of the carry to the data already in the entropy-coded segments creates a X'FF' byte. Any stacked output bytes - converted to zeros by the carryover - are then placed in the entropy-coded segment. Note that when the output byte is later transferred from T to the entropy-coded segment (to byte B), the carry bit is ignored if it is set.

If a carry has not occurred, the output byte is tested to see if it is $\mathrm{X}^{\prime} \mathrm{FF}^{\prime}$. If so, the stack count ST is incremented, as the output must be delayed until the carry-over is resolved. If not, the carry-over has been resolved, and any stacked X'FF' bytes must then be placed in the entropy-coded segment. Note that a zero byte is stuffed following each X'FF'.

The procedures used by Byte_out are defined in Figures D. 9 through D.11.


Figure D. 9 - Output_stacked_zeros procedure for encoder


Figure D. 10 - Output_stacked_X'FF's procedure for encoder


Figure D. 11 - Stuff_0 procedure for encoder

## D.1.7 Initialization of the encoder

The Initenc procedure is used to start the arithmetic coder. The basic steps are shown in Figure D.12.


Figure D. 12 - Initialization of the encoder

The probability estimation tables are defined by Table D.3. The statistics areas are initialized to an MPS sense of 0 and a Qe index of zero as defined by Table D.3. The stack count (ST) is cleared, the code register (C) is cleared, and the interval register is set to $X^{\prime} 10000^{\prime}$. The counter (CT) is set to 11 , reflecting the fact that when A is initialized to $X^{\prime} 10000^{\prime}$ three spacer bits plus eight output bits in C must be filled before the first byte is removed. Note that BP is initialized to point to the byte before the start of the entropy-coded segment (which is at BPST). Note also that the statistics areas are initialized for all values of context-index $S$ to $\operatorname{MPS}(S)=0$ and $\operatorname{Index}(S)=0$.

NOTE - Although the probability interval is initialized to $X^{\prime} 10000^{\prime}$ in both Initenc and Initdec, the precision of the probability interval register can still be limited to 16 bits. When the precision of the interval register is 16 bits, it is initialized to zero.

## D.1.8 Termination of encoding

The Flush procedure is used to terminate the arithmetic encoding procedures and prepare the entropy-coded segment for the addition of the X'FF' prefix of the marker which follows the arithmetically coded data. Figure D. 13 shows this flush procedure. The first step in the procedure is to set as many low order bits of the code register to zero as possible without pointing outside of the final interval. Then, the output byte is aligned by shifting it left by CT bits; Byte_out then removes it from C. C is then shifted left by 8 bits to align the second output byte and Byte_out is used a second time. The remaining low order bits in C are guaranteed to be zero, and these trailing zero bits shall not be written to the entropycoded segment.


Figure D. 13 - Flush procedure

Any trailing zero bytes already written to the entropy-coded segment and not preceded by a X'FF' may, optionally, be discarded. This is done in the Discard_final_zeros procedure. Stuffed zero bytes shall not be discarded.

Entropy coded segments are always followed by a marker. For this reason, the final zero bits needed to complete decoding shall not be included in the entropy coded segment. Instead, when the decoder encounters a marker, zero bits shall be supplied to the decoding procedure until decoding is complete. This convention guarantees that when a DNL marker is used, the decoder will intercept it in time to correctly terminate the decoding procedure.


Figure D. 14 - Clear_final_bits procedure in Flush


Figure D. 15 - Discard_final_zeros procedure in Flush

## D. 2 Arithmetic decoding procedures

Two arithmetic decoding procedures are used for arithmetic decoding (see Table D.4).

The "Decode(S)" procedure decodes the binary decision for a given context-index S and returns a value of either 0 or 1 . It is the inverse of the "Code_0(S)" and "Code_1(S)" procedures described in D.1. "Initdec" initializes the arithmetic coding entropy decoder.

## Table D. 4 - Procedures for binary arithmetic decoding

| Procedure | Purpose |
| :--- | :--- |
| Decode(S) <br> Initdec | Decode a binary decision with context-index S <br> Initialize the decoder |

## D.2.1 Binary arithmetic decoding principles

The probability interval subdivision and sub-interval ordering defined for the arithmetic encoding procedures also apply to the arithmetic decoding procedures.

Since the bit stream always points within the current probability interval, the decoding process is a matter of determining, for each decision, which sub-interval is pointed to by the bit stream. This is done recursively, using the same probability interval sub-division process as in the encoder. Each time a decision is decoded, the decoder subtracts from the bit stream any interval the encoder added to the bit stream. Therefore, the code register in the decoder is a pointer into the current probability interval relative to the base of the interval.

If the size of the sub-interval allocated to the LPS is larger than the sub-interval allocated to the MPS, the encoder invokes the conditional exchange procedure. When the interval sizes are inverted in the decoder, the sense of the symbol decoded must be inverted.

## D.2.2 Decoding conventions and approximations

The approximations and integer arithmetic defined for the probability interval subdivision in the encoder must also be used in the decoder. However, where the encoder would have added to the code register, the decoder subtracts from the code register.

## D.2.3 Decoder code register conventions

The flow charts given in this section assume the register structures for the decoder as shown in Table D.5:

Table D. 5 - Decoder register conventions

|  | MSB | LSB |
| :--- | :--- | ---: |
| Cx register | xxxxxxxx, | xxxxxxxx |
| C-low | bbbbbbbb, | 00000000 |
| A-register | aaaaaaaa, | aaaaaaaa |

Cx and C-low can be regarded as one 32-bit C-register, in that renormalization of C shifts a bit of new data from bit 15 of C-low to bit 0 of Cx . However, the decoding comparisons use Cx alone. New data are inserted into the "b" bits of C-low one byte at a time.

NOTE - The comparisons shown in the various procedures use arithmetic comparisons, and therefore assume precisions greater than 16 bits for the variables. Unsigned (logical) comparisons should be used in 16-bit precision implementations.

## D.2.4 The decode procedure

The decoder decodes one binary decision at a time. After decoding the decision, the decoder subtracts any amount from the code register that the encoder added. The amount left in the code register is the offset from the base of the current probability interval to the sub-interval allocated to the binary decisions not yet decoded. In the first test in the decode procedure shown in Figure D. 16 the code register is compared to the size of the MPS sub-interval. Unless a conditional exchange is needed, this test determines whether the MPS or LPS for context-index S is decoded. Note that the LPS for context-index S is given by $1-\mathrm{MPS}(\mathrm{S})$.

When a renormalization is needed, the MPS/LPS conditional exchange may also be needed. For the LPS path, the conditional exchange procedure is shown in Figure D.17. Note that the probability estimation in the decoder is identical to the probability estimation in the encoder (Figures D. 5 and D.6).


Figure D. 16 - Decode(S) procedure

For the MPS path of the decoder the conditional exchange procedure is given in Figure D.18.


Figure D. 17 - Decoder LPS path conditional exchange procedure


Figure D. 18 - Decoder MPS path conditional exchange procedure

## D.2.5 Probability estimation in the decoder

The procedures defined for obtaining a new LPS probability estimate in the encoder are also used in the decoder.

## D.2. 6 Renormalization in the decoder

The Renorm_d procedure for the decoder renormalization is shown in Figure D.19. CT is a counter which keeps track of the number of compressed bits in the C-low section of the C-register. When CT is zero, a new byte is inserted into C-low by the procedure Byte_in and CT is reset to 8 .

Both the probability interval register A and the code register C are shifted, one bit at a time, until A is no longer less than X'8000'.


Figure D. 19 - Decoder renormalization procedure

The Byte_in procedure used in Renorm_d is shown in Figure D.20. This procedure fetches one byte of data, compensating for the stuffed zero byte which follows any X'FF' byte. It also detects the marker which must follow the entropy-coded segment. The C-register in this procedure is the concatenation of the Cx and C -low registers. For simplicity of exposition, the buffer holding the entropy-coded segment is assumed to be large enough to contain the entire segment.

B is the byte pointed to by the entropy-coded segment pointer BP . BP is first incremented. If the new value of B is not a X'FF', it is inserted into the high order 8 bits of C-low.


Figure D. 20 - Byte_in procedure for decoder

The Unstuff_0 procedure is shown in Figure D.21. If the new value of B is X'FF', BP is incremented to point to the next byte and this next B is tested to see if it is zero. If so, B contains a stuffed byte which must be skipped. The zero B is ignored, and the X'FF' B value which preceded it is inserted in the C-register.

If the value of B after a $X^{\prime} F F$ ' byte is not zero, then a marker has been detected. The marker is interpreted as required and the entropy-coded segment pointer is adjusted ("Adjust BP" in Figure D.21) so that 0 -bytes will be fed to the decoder until decoding is complete. One way of accomplishing this is to point BP to the byte preceding the marker which follows the entropy-coded segment.


Figure D. 21 - Unstuff_0 procedure for decoder

## D.2.7 Initialization of the decoder

The Initdec procedure is used to start the arithmetic decoder. The basic steps are shown in Figure D.22.


Figure D. 22 - Initialization of the decoder

The estimation tables are defined by Table D.3. The statistics areas are initialized to an MPS sense of 0 and a Qe index of zero as defined by Table D.3. BP, the pointer to the entropy-coded segment, is then initialized to point to the byte before the start of the entropy-coded segment at BPST, and the interval register is set to the same starting value as in the encoder. The first byte of compressed data is fetched and shifted into Cx. The second byte is then fetched and shifted into Cx. The count is set to zero, so that a new byte of data will be fetched by Renorm_d.

NOTE - Although the probability interval is initialized to $X^{\prime} 10000^{\prime}$ in both Initenc and Initdec, the precision of the probability interval register can still be limited to 16 bits. When the precision of the interval register is 16 bits, it is initialized to zero.

## D. 3 Bit ordering within bytes

The arithmetically encoded entropy-coded segment is an integer of variable length. Therefore, the ordering of bytes and the bit ordering within bytes is the same as for parameters (see B.1.1.1).

## Annex E

## Encoder and decoder control procedures

(This annex forms an integral part of this Recommendation | International Standard)

This annex describes the encoder and decoder control procedures for the sequential, progressive, and lossless modes of operation.

The encoding and decoding control procedures for the hierarchical processes are specified in Annex J.

## NOTES

1 There is no requirement in this Specification that any encoder or decoder shall implement the procedures in precisely the manner specified by the flow charts in this annex. It is necessary only that an encoder or decoder implement the function specified in this annex. The sole criterion for an encoder or decoder to be considered in compliance with this Specification is that it satisfy the requirements given in clause 6 (for encoders) or clause 7 (for decoders), as determined by the compliance tests specified in Part 2 .

2 Implementation-specific setup steps are not indicated in this annex and may be necessary.

## E. 1 Encoder control procedures

## E.1. 1 Control procedure for encoding an image

The encoder control procedure for encoding an image is shown in Figure E.1.


Figure E. 1 - Control procedure for encoding an image

## E.1.2 Control procedure for encoding a frame

In all cases where markers are appended to the compressed data, optional X'FF' fill bytes may precede the marker.

The control procedure for encoding a frame is oriented around the scans in the frame. The frame header is first appended, and then the scans are coded. Table specifications and other marker segments may precede the $\mathrm{SOF}_{\mathrm{n}}$ marker, as indicated by [tables/miscellaneous] in Figure E.2.

Figure E. 2 shows the encoding process frame control procedure.


Figure E. 2 - Control procedure for encoding a frame

## E.1.3 Control procedure for encoding a scan

A scan consists of a single pass through the data of each component in the scan. Table specifications and other marker segments may precede the SOS marker. If more than one component is coded in the scan, the data are interleaved. If restart is enabled, the data are segmented into restart intervals. If restart is enabled, a $\mathrm{RST}_{\mathrm{m}}$ marker is placed in the coded data between restart intervals. If restart is disabled, the control procedure is the same, except that the entire scan contains a single restart interval. The compressed image data generated by a scan is always followed by a marker, either the EOI marker or the marker of the next marker segment.

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Figure E. 3 shows the encoding process scan control procedure. The loop is terminated when the encoding process has coded the number of restart intervals which make up the scan. " m " is the restart interval modulo counter needed for the $\mathrm{RST}_{\mathrm{m}}$ marker. The modulo arithmetic for this counter is shown after the "Append $\mathrm{RST}_{\mathrm{m}}$ marker" procedure.


Figure E. 3 - Control procedure for encoding a scan

## E.1.4 Control procedure for encoding a restart interval

Figure E. 4 shows the encoding process control procedure for a restart interval. The loop is terminated either when the encoding process has coded the number of minimum coded units (MCU) in the restart interval or when it has completed the image scan.


Figure E. 4 - Control procedure for encoding a restart interval

The "Reset_encoder" procedure consists at least of the following:
a) if arithmetic coding is used, initialize the arithmetic encoder using the "Initenc" procedure described in D.1.7;
b) for DCT-based processes, set the DC prediction (PRED) to zero for all components in the scan (see F.1.1.5.1);
c) for lossless processes, reset the prediction to a default value for all components in the scan (see H.1.1);
d) do all other implementation-dependent setups that may be necessary.

The procedure "Prepare_for_marker" terminates the entropy-coded segment by:
a) padding a Huffman entropy-coded segment with 1-bits to complete the final byte (and if needed stuffing a zero byte) (see F.1.2.3); or
b) invoking the procedure "Flush" (see D.1.8) to terminate an arithmetic entropy-coded segment.

NOTE - The number of minimum coded units (MCU) in the final restart interval must be adjusted to match the number of MCU in the scan. The number of MCU is calculated from the frame and scan parameters. (See Annex B.)

## E.1.5 Control procedure for encoding a minimum coded unit (MCU)

The minimum coded unit is defined in A.2. Within a given MCU the data units are coded in the order in which they occur in the MCU. The control procedure for encoding a MCU is shown in Figure E.5.


Figure E. 5 - Control procedure for encoding a minimum coded unit (MCU)

In Figure E.5, Nb refers to the number of data units in the MCU. The order in which data units occur in the MCU is defined in A.2. The data unit is an $8 \times 8$ block for DCT-based processes, and a single sample for lossless processes.

The procedures for encoding a data unit are specified in Annexes F, G, and H.

## E. 2 Decoder control procedures

## E.2.1 Control procedure for decoding compressed image data

Figure E. 6 shows the decoding process control for compressed image data.

Decoding control centers around identification of various markers. The first marker must be the SOI (Start Of Image) marker. The "Decoder_setup" procedure resets the restart interval $(\mathrm{Ri}=0)$ and, if the decoder has arithmetic decoding capabilities, sets the conditioning tables for the arithmetic coding to their default values. (See F.1.4.4.1.4 and F.1.4.4.2.1.) The next marker is normally a $\mathrm{SOF}_{\mathrm{n}}$ (Start Of Frame) marker; if this is not found, one of the marker segments listed in Table E. 1 has been received.


Figure E. 6 - Control procedure for decoding compressed image data

Table E. 1 - Markers recognized by "Interpret markers"

| Marker | Purpose |
| :--- | :--- |
| DHT | Define Huffman Tables |
| DAC | Define Arithmetic Conditioning |
| DQT | Define Quantization Tables |
| DRI | Define Restart Interval |
| APP $_{n}$ | Application defined marker |
| COM | Comment |

Note that optional X'FF' fill bytes which may precede any marker shall be discarded before determining which marker is present.

The additional logic to interpret these various markers is contained in the box labeled "Interpret markers". DHT markers shall be interpreted by processes using Huffman coding. DAC markers shall be interpreted by processes using arithmetic coding. DQT markers shall be interpreted by DCT-based decoders. DRI markers shall be interpreted by all decoders. APPn and COM markers shall be interpreted only to the extent that they do not interfere with the decoding.

By definition, the procedures in "Interpret markers" leave the system at the next marker. Note that if the expected SOI marker is missing at the start of the compressed image data, an error condition has occurred. The techniques for detecting and managing error conditions can be as elaborate or as simple as desired.

## E.2.2 Control procedure for decoding a frame

Figure E. 7 shows the control procedure for the decoding of a frame.


Figure E. 7 - Control procedure for decoding a frame

The loop is terminated if the EOI marker is found at the end of the scan.

The markers recognized by "Interpret markers" are listed in Table E.1. Subclause E.2.1 describes the extent to which the various markers shall be interpreted.

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## E.2.3 Control procedure for decoding a scan

Figure E. 8 shows the decoding of a scan.

The loop is terminated when the expected number of restart intervals has been decoded.


Figure E. 8 - Control procedure for decoding a scan

## E.2.4 Control procedure for decoding a restart interval

The procedure for decoding a restart interval is shown in Figure E.9. The "Reset_decoder" procedure consists at least of the following:
a) if arithmetic coding is used, initialize the arithmetic decoder using the "Initdec" procedure described in D.2.7;
b) for DCT-based processes, set the DC prediction (PRED) to zero for all components in the scan (see F.2.1.3.1);
c) for lossless process, reset the prediction to a default value for all components in the scan (see H.2.1);
d) do all other implementation-dependent setups that may be necessary.


Figure E. 9 - Control procedure for decoding a restart interval

At the end of the restart interval, the next marker is located. If a problem is detected in locating this marker, error handling procedures may be invoked. While such procedures are optional, the decoder shall be able to correctly recognize restart markers in the compressed data and reset the decoder when they are encountered. The decoder shall also be able to recognize the DNL marker, set the number of lines defined in the DNL segment, and end the "Decode_restart_interval" procedure.

NOTE - The final restart interval may be smaller than the size specified by the DRI marker segment, as it includes only the number of MCUs remaining in the scan.

## E.2.5 Control procedure for decoding a minimum coded unit (MCU)

The procedure for decoding a minimum coded unit (MCU) is shown in Figure E.10.
In Figure E. 10 Nb is the number of data units in a MCU.
The procedures for decoding a data unit are specified in Annexes F, G, and H.


Figure E. 10 - Control procedure for decoding a minimum coded unit (MCU)

## Annex F

## Sequential DCT-based mode of operation

(This annex forms an integral part of this Recommendation | International Standard)

This annex provides a functional specification of the following coding processes for the sequential DCT-based mode of operation:

1) baseline sequential;
2) extended sequential, Huffman coding, 8 -bit sample precision;
3) extended sequential, arithmetic coding, 8 -bit sample precision;
4) extended sequential, Huffman coding, 12-bit sample precision;
5) extended sequential, arithmetic coding, 12 -bit sample precision.

For each of these, the encoding process is specified in F.1, and the decoding process is specified in F.2. The functional specification is presented by means of specific flow charts for the various procedures which comprise these coding processes.

NOTE - There is no requirement in this Specification that any encoder or decoder which embodies one of the above-named processes shall implement the procedures in precisely the manner specified by the flow charts in this annex. It is necessary only that an encoder or decoder implement the function specified in this annex. The sole criterion for an encoder or decoder to be considered in compliance with this Specification is that it satisfy the requirements given in clause 6 (for encoders) or clause 7 (for decoders), as determined by the compliance tests specified in Part 2.

## F. 1 Sequential DCT-based encoding processes

## F.1.1 Sequential DCT-based control procedures and coding models

## F.1.1.1 Control procedures for sequential DCT-based encoders

The control procedures for encoding an image and its constituent parts - the frame, scan, restart interval and MCU - are given in Figures E. 1 to E.5. The procedure for encoding a MCU (see Figure E.5) repetitively calls the procedure for encoding a data unit. For DCT-based encoders the data unit is an $8 \times 8$ block of samples.

## F.1.1.2 Procedure for encoding an $8 \times 8$ block data unit

For the sequential DCT-based processes encoding an $8 \times 8$ block data unit consists of the following procedures:
a) level shift, calculate forward $8 \times 8 \mathrm{DCT}$ and quantize the resulting coefficients using table destination specified in frame header;
b) encode DC coefficient for $8 \times 8$ block using DC table destination specified in scan header;
c) encode AC coefficients for $8 \times 8$ block using AC table destination specified in scan header.

## F.1.1.3 Level shift and forward DCT (FDCT)

The mathematical definition of the FDCT is given in A.3.3.
Prior to computing the FDCT the input data are level shifted to a signed two's complement representation as described in A.3.1. For 8-bit input precision the level shift is achieved by subtracting 128. For 12-bit input precision the level shift is achieved by subtracting 2048.

## F.1.1.4 Quantization of the FDCT

The uniform quantization procedure described in Annex A is used to quantize the DCT coefficients. One of four quantization tables may be used by the encoder. No default quantization tables are specified in this Specification. However, some typical quantization tables are given in Annex K.

The quantized DCT coefficient values are signed, two's complement integers with 11-bit precision for 8-bit input precision and 15 -bit precision for 12 -bit input precision.

## F.1.1.5 Encoding models for the sequential DCT procedures

The two dimensional array of quantized DCT coefficients is rearranged in a zig-zag sequence order defined in A.3.6. The zig-zag order coefficients are denoted $\mathrm{ZZ}(0)$ through $\mathrm{ZZ}(63)$ with:

$$
\mathrm{ZZ}(0)=\mathrm{Sq}_{00}, \mathrm{ZZ}(1)=\mathrm{Sq}_{01}, \mathrm{ZZ}(2)=\mathrm{Sq}_{10}, \bullet, \bullet, \cdot, \mathrm{ZZ}(63)=\mathrm{Sq}_{77}
$$

$\mathrm{Sq}_{\mathrm{vu}}$ are defined in Figure A.6.
Two coding procedures are used, one for the DC coefficient $\mathrm{ZZ}(0)$ and the other for the AC coefficients $\mathrm{ZZ}(1) . . \mathrm{ZZ}(63)$. The coefficients are encoded in the order in which they occur in zig-zag sequence order, starting with the DC coefficient. The coefficients are represented as two's complement integers.

## F.1.1.5.1 Encoding model for DC coefficients

The DC coefficients are coded differentially, using a one-dimensional predictor, PRED, which is the quantized DC value from the most recently coded $8 \times 8$ block from the same component. The difference, DIFF, is obtained from

$$
\text { DIFF }=\mathrm{ZZ}(0)-\mathrm{PRED}
$$

At the beginning of the scan and at the beginning of each restart interval, the prediction for the DC coefficient prediction is initialized to 0 . (Recall that the input data have been level shifted to two's complement representation.)

## F.1.1.5.2 Encoding model for AC coefficients

Since many coefficients are zero, runs of zeros are identified and coded efficiently. In addition, if the remaining coefficients in the zig-zag sequence order are all zero, this is coded explicitly as an end-of-block (EOB).

## F.1.2 Baseline Huffman encoding procedures

The baseline encoding procedure is for 8 -bit sample precision. The encoder may employ up to two DC and two AC Huffman tables within one scan.

## F.1.2.1 Huffman encoding of DC coefficients

## F.1.2.1.1 Structure of DC code table

The DC code table consists of a set of Huffman codes (maximum length 16 bits) and appended additional bits (in most cases) which can code any possible value of DIFF, the difference between the current DC coefficient and the prediction. The Huffman codes for the difference categories are generated in such a way that no code consists entirely of 1-bits ( $\mathrm{X}^{\prime} \mathrm{FF}$ ' prefix marker code avoided).

The two's complement difference magnitudes are grouped into 12 categories, SSSS, and a Huffman code is created for each of the 12 difference magnitude categories (see Table F.1).

For each category, except $\operatorname{SSSS}=0$, an additional bits field is appended to the code word to uniquely identify which difference in that category actually occurred. The number of extra bits is given by SSSS; the extra bits are appended to the LSB of the preceding Huffman code, most significant bit first. When DIFF is positive, the SSSS low order bits of DIFF are appended. When DIFF is negative, the SSSS low order bits of (DIFF - 1) are appended. Note that the most significant bit of the appended bit sequence is 0 for negative differences and 1 for positive differences.

## F.1.2.1.2 Defining Huffman tables for the DC coefficients

The syntax for specifying the Huffman tables is given in Annex B. The procedure for creating a code table from this information is described in Annex C. No more than two Huffman tables may be defined for coding of DC coefficients. Two examples of Huffman tables for coding of DC coefficients are provided in Annex K.

Table F. 1 - Difference magnitude categories for DC coding

| SSSS | DIFF values |
| :---: | :---: |
| 0 | 0 |
| 1 | $-1,1$ |
| 2 | $-3,-2,2,3$ |
| 3 | $-7 . .-4,4 . .7$ |
| 4 | $-15 . .-8,8 . .15$ |
| 5 | $-31 . .-16,16 . .31$ |
| 6 | $-63 . .-32,32 . .63$ |
| 7 | $-127 . .-64,64 . .127$ |
| 8 | $-255 . .-128,128 . .255$ |
| 9 | $-511 . .-256,256 . .511$ |
| 10 | $-1023 . .-512,512 . .1023$ |
| 11 | $-2047 . .-1024,1024 . .2047$ |

## F.1.2.1.3 Huffman encoding procedures for DC coefficients

The encoding procedure is defined in terms of a set of extended tables, XHUFCO and XHUFSI, which contain the complete set of Huffman codes and sizes for all possible difference values. For full 12-bit precision the tables are relatively large. For the baseline system, however, the precision of the differences may be small enough to make this description practical.

XHUFCO and XHUFSI are generated from the encoder tables EHUFCO and EHUFSI (see Annex C) by appending to the Huffman codes for each difference category the additional bits that completely define the difference. By definition, XHUFCO and XHUFSI have entries for each possible difference value. XHUFCO contains the concatenated bit pattern of the Huffman code and the additional bits field; XHUFSI contains the total length in bits of this concatenated bit pattern. Both are indexed by DIFF, the difference between the DC coefficient and the prediction.

The Huffman encoding procedure for the DC difference, DIFF, is:
SIZE = XHUFSI(DIFF)

CODE $=\mathrm{XHUFCO}(\mathrm{DIFF})$
code SIZE bits of CODE
where DC is the quantized DC coefficient value and PRED is the predicted quantized DC value. The Huffman code (CODE) (including any additional bits) is obtained from XHUFCO and SIZE (length of the code including additional bits) is obtained from XHUFSI, using DIFF as the index to the two tables.

## F.1.2.2 Huffman encoding of AC coefficients

## F.1.2.2.1 Structure of AC code table

Each non-zero AC coefficient in ZZ is described by a composite 8 -bit value, RS, of the form
RS = binary 'RRRRSSSS'

The 4 least significant bits, 'SSSS', define a category for the amplitude of the next non-zero coefficient in ZZ, and the 4 most significant bits, 'RRRR', give the position of the coefficient in ZZ relative to the previous non-zero coefficient (i.e. the run-length of zero coefficients between non-zero coefficients). Since the run length of zero coefficients may exceed 15 , the value 'RRRRSSSS' = $X^{\prime} F 0$ ' is defined to represent a run length of 15 zero coefficients followed by a coefficient of zero amplitude. (This can be interpreted as a run length of 16 zero coefficients.) In addition, a special value 'RRRRSSSS' $={ }^{\prime} 00000000^{\prime}$ is used to code the end-of-block (EOB), when all remaining coefficients in the block are zero.

The general structure of the code table is illustrated in Figure F.1. The entries marked "N/A" are undefined for the baseline procedure.


Figure F. 1 - Two-dimensional value array for Huffman coding

The magnitude ranges assigned to each value of SSSS are defined in Table F.2.

Table F. 2 - Categories assigned to coefficient values

| SSSS | AC coefficients |
| :---: | :---: |
| 1 | $-1,1$ |
| 2 | $-3,-2,2,3$ |
| 3 | $-7 . .-4,4 . .7$ |
| 4 | $-15 . .-8,8 . .15$ |
| 5 | $-31 . .-16,16 . .31$ |
| 6 | $-63 . .-32,32 . .63$ |
| 7 | $-127 . .-64,64 . .127$ |
| 8 | $-255 . .-128,128 . .255$ |
| 9 | $-511 . .-256,256 . .511$ |
| 10 | $-1023 . .-512,512 . .1023$ |

The composite value, RRRRSSSS, is Huffman coded and each Huffman code is followed by additional bits which specify the sign and exact amplitude of the coefficient.

The AC code table consists of one Huffman code (maximum length 16 bits, not including additional bits) for each possible composite value. The Huffman codes for the 8 -bit composite values are generated in such a way that no code consists entirely of 1-bits.

## 

The format for the additional bits is the same as in the coding of the DC coefficients. The value of SSSS gives the number of additional bits required to specify the sign and precise amplitude of the coefficient. The additional bits are either the low-order SSSS bits of $Z Z(K)$ when $Z Z(K)$ is positive or the low-order $S S S S$ bits of $Z Z(K)-1$ when $Z Z(K)$ is negative. $\mathrm{ZZ}(\mathrm{K})$ is the $K$ th coefficient in the zig-zag sequence of coefficients being coded.

## F.1.2.2 2 Defining Huffman tables for the AC coefficients

The syntax for specifying the Huffman tables is given in Annex B. The procedure for creating a code table from this information is described in Annex C.

In the baseline system no more than two Huffman tables may be defined for coding of AC coefficients. Two examples of Huffman tables for coding of AC coefficients are provided in Annex K.

## F.1.2.2.3 Huffman encoding procedures for AC coefficients

As defined in Annex C, the Huffman code table is assumed to be available as a pair of tables, EHUFCO (containing the code bits) and EHUFSI (containing the length of each code in bits), both indexed by the composite value defined above.

The procedure for encoding the AC coefficients in a block is shown in Figures F. 2 and F.3. In Figure F.2, K is the index to the zig-zag scan position and R is the run length of zero coefficients.

The procedure "Append EHUFSI( $\mathrm{X}^{\prime} \mathrm{F} 0$ ') bits of $\mathrm{EHUFCO}\left(\mathrm{X}^{\prime} \mathrm{F} 0\right.$ ')" codes a run of 16 zero coefficients (ZRL code of Figure F.1). The procedure "Code EHUFSI(0) bits of EHUFCO(0)" codes the end-of-block (EOB code). If the last coefficient $(\mathrm{K}=63)$ is not zero, the EOB code is bypassed.

CSIZE is a procedure which maps an AC coefficient to the SSSS value as defined in Table F.2.

## F.1.2.3 Byte stuffing

In order to provide code space for marker codes which can be located in the compressed image data without decoding, byte stuffing is used.

Whenever, in the course of normal encoding, the byte value $X^{\prime} F^{\prime}$ ' is created in the code string, a $X^{\prime} 00^{\prime}$ byte is stuffed into the code string.

If a $X^{\prime} 00^{\prime}$ byte is detected after a $X^{\prime} F F$ ' byte, the decoder must discard it. If the byte is not zero, a marker has been detected, and shall be interpreted to the extent needed to complete the decoding of the scan.

Byte alignment of markers is achieved by padding incomplete bytes with 1-bits. If padding with 1-bits creates a $\mathrm{X}^{\prime} \mathrm{FF}$ ' value, a zero byte is stuffed before adding the marker.

## F.1.3 Extended sequential DCT-based Huffman encoding process for 8-bit sample precision

This process is identical to the Baseline encoding process described in F.1.2, with the exception that the number of sets of Huffman table destinations which may be used within the same scan is increased to four. Four DC and four AC Huffman table destinations is the maximum allowed by this Specification.

## F.1.4 Extended sequential DCT-based arithmetic encoding process for 8-bit sample precision

This subclause describes the use of arithmetic coding procedures in the sequential DCT-based encoding process.
NOTE - The arithmetic coding procedures in this Specification are defined for the maximum precision to encourage interchangeability.

The arithmetic coding extensions have the same DCT model as the Baseline DCT encoder. Therefore, Annex F.1.1 also applies to arithmetic coding. As with the Huffman coding technique, the binary arithmetic coding technique is lossless. It is possible to transcode between the two systems without either FDCT or IDCT computations, and without modification of the reconstructed image.

The basic principles of adaptive binary arithmetic coding are described in Annex D. Up to four DC and four AC conditioning table destinations and associated statistics areas may be used within one scan.

The arithmetic encoding procedures for encoding binary decisions, initializing the statistics area, initializing the encoder, terminating the code string, and adding restart markers are listed in Table D. 1 of Annex D.


Figure F. 2 - Procedure for sequential encoding of AC coefficients with Huffman coding


Figure F. 3 - Sequential encoding of a non-zero AC coefficient

Some of the procedures in Table D. 1 are used in the higher level control structure for scans and restart intervals described in Annex E. At the beginning of scans and restart intervals, the probability estimates used in the arithmetic coder are reset to the standard initial value as part of the Initenc procedure which restarts the arithmetic coder. At the end of scans and restart intervals, the Flush procedure is invoked to empty the code register before the next marker is appended.

## F.1.4.1 Arithmetic encoding of DC coefficients

The basic structure of the decision sequence for encoding a DC difference value, DIFF, is shown in Figure F.4.

The context-index S 0 and other context-indices used in the DC coding procedures are defined in Table F. 4 (see F.1.4.4.1.3). A 0 -decision is coded if the difference value is zero and a 1 -decision is coded if the difference is not zero. If the difference is not zero, the sign and magnitude are coded using the procedure Encode_V(S0), which is described in F.1.4.3.1.

## F.1.4.2 Arithmetic encoding of AC coefficients

The AC coefficients are coded in the order in which they occur in the zig-zag sequence $\mathrm{ZZ}(1, \ldots, 63)$. An end-of-block (EOB) binary decision is coded before coding the first AC coefficient in ZZ , and after each non-zero coefficient. If the EOB occurs, all remaining coefficients in ZZ are zero. Figure F. 5 illustrates the decision sequence. The equivalent procedure for the Huffman coder is found in Figure F.2.


Figure F. 4 - Coding model for arithmetic coding of DC difference

The context-indices SE and S0 used in the AC coding procedures are defined in Table F. 5 (see F.1.4.4.2). In Figure F.5, K is the index to the zig-zag sequence position. For the sequential scan, Kmin is 1 and Se is 63 . The $\mathrm{V}=0$ decision is part of a loop which codes runs of zero coefficients. Whenever the coefficient is non-zero, "Encode_V(S0)" codes the sign and magnitude of the coefficient. Each time a non-zero coefficient is coded, it is followed by an EOB decision. If the EOB occurs, a 1 -decision is coded to indicate that the coding of the block is complete. If the coefficient for $\mathrm{K}=\mathrm{Se}$ is not zero, the EOB decision is skipped.

## F.1.4.3 Encoding the binary decision sequence for non-zero DC differences and AC coefficients

Both the DC difference and the AC coefficients are represented as signed two's complement integer values. The decomposition of these signed integer values into a binary decision tree is done in the same way for both the DC and AC coding models.

Although the binary decision trees for this section of the DC and AC coding models are the same, the statistical models for assigning statistics bins to the binary decisions in the tree are quite different.

## F.1.4.3.1 Structure of the encoding decision sequence

The encoding sequence can be separated into three procedures, a procedure which encodes the sign, a second procedure which identifies the magnitude category, and a third procedure which identifies precisely which magnitude occurred within the category identified in the second procedure.

At the point where the binary decision sequence in Encode_V(S0) starts, the coefficient or difference has already been determined to be non-zero. That determination was made in the procedures in Figures F. 4 and F. 5 .

Denoting either DC differences (DIFF) or AC coefficients as V , the non-zero signed integer value of V is encoded by the sequence shown in Figure F.6. This sequence first codes the sign of V. It then (after converting V to a magnitude and decrementing it by 1 to give Sz ) codes the magnitude category of Sz (code_log2_Sz), and then codes the low order magnitude bits (code_Sz_bits) to identify the exact magnitude value.

## 

There are two significant differences between this sequence and the similar set of operations described in F.1.2 for Huffman coding. First, the sign is encoded before the magnitude category is identified, and second, the magnitude is decremented by 1 before the magnitude category is identified.


Figure F. 5 - AC coding model for arithmetic coding


Figure F. 6 - Sequence of procedures in encoding non-zero values of V

## F.1.4.3.1.1 Encoding the sign

The sign is encoded by coding a 0 -decision when the sign is positive and a 1 -decision when the sign is negative (see Figure F.7).

The context-indices SS, SN and SP are defined for DC coding in Table F. 4 and for AC coding in Table F.5. After the sign is coded, the context-index S is set to either SN or SP, establishing an initial value for Encode_log2_Sz.

## F.1.4.3.1.2 Encoding the magnitude category

The magnitude category is determined by a sequence of binary decisions which compares Sz against an exponentially increasing bound (which is a power of 2 ) in order to determine the position of the leading 1 -bit. This establishes the magnitude category in much the same way that the Huffman encoder generates a code for the value associated with the difference category. The flow chart for this procedure is shown in Figure F.8.

The starting value of the context-index S is determined in Encode_sign_of_V, and the context-index values X1 and X2 are defined for DC coding in Table F. 4 and for AC coding in Table F.5. In Figure F.8, M is the exclusive upper bound for the magnitude and the abbreviations "SLL" and "SRL" refer to the shift-left-logical and shift-right-logical operations - in this case by one bit position. The SRL operation at the completion of the procedure aligns M with the most significant bit of Sz (see Table F.3).

The highest precision allowed for the DCT is 15 bits. Therefore, the highest precision required for the coding decision tree is 16 bits for the DC coefficient difference and 15 bits for the AC coefficients, including the sign bit.


Figure F. 7 - Encoding the sign of V

Table F. 3 - Categories for each maximum bound

| Exclusive upper <br> bound (M) | Sz range | Number of low order <br> magnitude bits |
| :---: | :---: | :---: |
| 1 | 0 | 0 |
| 2 | 1 | 0 |
| 4 | 2,3 | 1 |
| 8 | $4, \ldots, 7$ | 2 |
| 16 | $8, \ldots, 15$ | 3 |
| 32 | $16, \ldots, 31$ | 4 |
| 64 | $32, \ldots, 63$ | 5 |
| 128 | $64, \ldots, 127$ | 6 |
| 256 | $128, \ldots, 255$ | 7 |
| 512 | $256, \ldots, 511$ | 8 |
| 1024 | $512, \ldots, 1023$ | 9 |
| 2048 | $1024, \ldots, 2047$ | 10 |
| 4096 | $2048, \ldots, 4095$ | 11 |
| 8192 | $4096, \ldots, 8191$ | 12 |
| 16384 | $8192, \ldots, 16383$ | 13 |
| 32768 | $16384, \ldots, 32767$ | 14 |



Figure F. 8 - Decision sequence to establish the magnitude category

## F.1.4.3.1.3 Encoding the exact value of the magnitude

After the magnitude category is encoded, the low order magnitude bits are encoded. These bits are encoded in order of decreasing bit significance. The procedure is shown in Figure F.9. The abbreviation "SRL" indicates the shift-rightlogical operation, and $M$ is the exclusive bound established in Figure F.8. Note that M has only one bit set - shifting M right converts it into a bit mask for the logical "AND" operation.

The starting value of the context-index S is determined in Encode_log2_Sz. The increment of S by 14 at the beginning of this procedure sets the context-index to the value required in Tables F. 4 and F.5.


Figure F. 9 - Decision sequence to code the magnitude bit pattern

## F.1.4. 4 Statistical models

An adaptive binary arithmetic coder requires a statistical model. The statistical model defines the contexts which are used to select the conditional probability estimates used in the encoding and decoding procedures.

Each decision in the binary decision trees is associated with one or more contexts. These contexts identify the sense of the MPS and the index in Table D. 3 of the conditional probability estimate Qe which is used to encode and decode the binary decision.

The arithmetic coder is adaptive, which means that the probability estimates for each context are developed and maintained by the arithmetic coding system on the basis of prior coding decisions for that context.

## F.1.4.4.1 Statistical model for coding DC prediction differences

The statistical model for coding the DC difference conditions some of the probability estimates for the binary decisions on previous DC coding decisions.

## F.1.4.4.1.1 Statistical conditioning on sign

In coding the DC coefficients, four separate statistics bins (probability estimates) are used in coding the zero/not-zero ( $\mathrm{V}=$ 0 ) decision, the sign decision and the first magnitude category decision. Two of these bins are used to code the $\mathrm{V}=0$ decision and the sign decision. The other two bins are used in coding the first magnitude decision, $\mathrm{Sz}<1$; one of these bins is used when the sign is positive, and the other is used when the sign is negative. Thus, the first magnitude decision probability estimate is conditioned on the sign of V .

## F.1.4.4.1.2 Statistical conditioning on DC difference in previous block

The probability estimates for these first three decisions are also conditioned on Da, the difference value coded for the previous DCT block of the same component. The differences are classified into five groups: zero, small positive, small negative, large positive and large negative. The relationship between the default classification and the quantization scale is shown in Figure F. 10.


Figure F. 10 - Conditioning classification of difference values

The bounds for the "small" difference category determine the classification. Defining $L$ and $U$ as integers in the range 0 to 15 inclusive, the lower bound (exclusive) for difference magnitudes classified as "small" is zero for $\mathrm{L}=0$, and is $2 \mathrm{~L}-1$ for $\mathrm{L}>0$.

The upper bound (inclusive) for difference magnitudes classified as "small" is 2 U .
$L$ shall be less than or equal to $U$.
These bounds for the conditioning category provide a segmentation which is identical to that listed in Table F.3.

## F.1.4.4.1.3 Assignment of statistical bins to the DC binary decision tree

As shown in Table F.4, each statistics area for DC coding consists of a set of 49 statistics bins. In the following explanation, it is assumed that the bins are contiguous. The first 20 bins consist of five sets of four bins selected by a context-index S 0 . The value of S 0 is given by DC_Context(Da), which provides a value of $0,4,8,12$ or 16 , depending on the difference classification of Da (see F.1.4.4.1.2). The remaining 29 bins, X1,...,X15,M2,..., M15, are used to code magnitude category decisions and magnitude bits.

Table F. 4 - Statistical model for DC coefficient coding

| Context-index | Value | Coding decision |
| :---: | :---: | :---: |
| S0 | DC_Context(Da) | $V=0$ |
| SS | $\mathrm{S} 0+1$ | Sign of V |
| SP | $\mathrm{S} 0+2$ | $\mathrm{Sz}<1$ if $\mathrm{V}>0$ |
| SN | S0 + 3 | $\mathrm{Sz}<1$ if $\mathrm{V}<0$ |
| X1 | 20 | $\mathrm{Sz}<2$ |
| X2 | $\mathrm{X} 1+1$ | Sz<4 |
| X3 | $\mathrm{X} 1+2$ | $\mathrm{Sz}<8$ |
| . | . |  |
| . | $\cdot$ |  |
| X15 | $\mathrm{X} 1+14$ | $\mathrm{Sz}<215$ |
| M2 | $\mathrm{X} 2+14$ | Magnitude bits if $\mathrm{Sz}<4$ |
| M3 | $\mathrm{X} 3+14$ | Magnitude bits if $\mathrm{Sz}<8$ |
| - | . |  |
| - |  |  |
| M15 | $\mathrm{X} 15+14$ | Magnitude bits if $\mathrm{Sz}<215$ |

## F.1.4.4.1.4 Default conditioning for DC statistical model

The bounds, L and U , for determining the conditioning category have the default values $\mathrm{L}=0$ and $\mathrm{U}=1$. Other bounds may be set using the DAC (Define Arithmetic coding Conditioning) marker segment, as described in Annex B.

## F.1.4.4.1.5 Initial conditions for DC statistical model

At the start of a scan and at the beginning of each restart interval, the difference for the previous DC value is defined to be zero in determining the conditioning state.

## F.1.4.4.2 Statistical model for coding the AC coefficients

As shown in Table F.5, each statistics area for AC coding consists of a contiguous set of 245 statistics bins. Three bins are used for each value of the zig-zag index K, and two sets of 28 additional bins $\mathrm{X} 2, \ldots, \mathrm{X} 15, \mathrm{M} 2, \ldots, \mathrm{M} 15$ are used for coding the magnitude category and magnitude bits.

The value of SE (and also S0, SP and SN) is determined by the zig-zag index K. Since K is in the range 1 to 63 , the lowest value for SE is 0 and the largest value for SP is 188 . SS is not assigned a value in AC coefficient coding, as the signs of the coefficients are coded with a fixed probability value of approximately $0.5\left(\mathrm{Qe}=\mathrm{X}^{\prime} 5 \mathrm{~A} 1 \mathrm{D}^{\prime}, \mathrm{MPS}=0\right)$.

The value of X 2 is given by $A C \_$Context $(\mathrm{K})$. This gives $\mathrm{X} 2=189$ when $\mathrm{K} \leq K x$ and $\mathrm{X} 2=217$ when $\mathrm{K}>\mathrm{Kx}$, where Kx is defined using the DAC marker segment (see B.2.4.3).

Note that a X1 statistics bin is not used in this sequence. Instead, the $63 \times 1$ array of statistics bins for the magnitude category is used for two decisions. Once the magnitude bound has been determined - at statistics bin Xn , for example -a single statistics bin, Mn , is used to code the magnitude bit sequence for that bound.

## F.1.4.4.2.1 Default conditioning for AC coefficient coding

The default value of $K x$ is 5 . This may be modified using the DAC marker segment, as described in Annex B.

## F.1.4.4.2.2 Initial conditions for AC statistical model

At the start of a scan and at each restart, all statistics bins are re-initialized to the standard default value described in Annex D.

Table F. 5 - Statistical model for AC coefficient coding

| Context-index | Value | Coding decision |
| :---: | :---: | :---: |
| SE | $3 \times(\mathrm{K}-1)$ | $\mathrm{K}=\mathrm{EOB}$ |
| S0 | $\mathrm{SE}+1$ | $\mathrm{V}=0$ |
| SS | Fixed estimate | Sign of V |
| SN,SP | $\mathrm{S} 0+1$ | Sz<1 |
| X1 | $\mathrm{S} 0+1$ | Sz<2 |
| X2 | AC_Context(K) | $\mathrm{Sz}<4$ |
| X3 | $\mathrm{X} 2+1$ | $\mathrm{Sz}<8$ |
| . | . |  |
| X15 | $\mathrm{X} 2+13$ | Sz<215 |
| M2 | $\mathrm{X} 2+14$ | Magnitude bits if $\mathrm{Sz}<4$ |
| M3 | $\mathrm{X} 3+14$ | Magnitude bits if $\mathrm{Sz}<8$ |
|  | . |  |
| M15 | X15 + 14 | Magnitude bits if $\mathrm{Sz}<22^{15}$ |

## F.1.5 Extended sequential DCT-based Huffman encoding process for 12-bit sample precision

This process is identical to the sequential DCT process for 8-bit precision extended to four Huffman table destinations as documented in F.1.3, with the following changes.

## F.1.5.1 Structure of DC code table for 12-bit sample precision

The two's complement difference magnitudes are grouped into 16 categories, SSSS, and a Huffman code is created for each of the 16 difference magnitude categories.

The Huffman table for DC coding (see Table F.1) is extended as shown in Table F.6.

Table F. 6 - Difference magnitude categories for DC coding

| SSSS | Difference values |
| :---: | :---: |
| 12 | $-4095 .-2048,2048 . .4095$ |
| 13 | $-8191 . .-4096,4096 . .8191$ |
| 14 | $-16383 . .-8192,8192 . .16383$ |
| 15 | $-32767 . .-16384,16384 . .32767$ |

## F.1.5.2 Structure of AC code table for 12-bit sample precision

The general structure of the code table is extended as illustrated in Figure F.11. The Huffman table for AC coding is extended as shown in Table F.7.


Figure F. 11 - Two-dimensional value array for Huffman coding

Table F. 7 - Values assigned to coefficient amplitude ranges

| SSSS | AC coefficients |
| :---: | :---: |
| 11 | $-2047 . .-1024,1024 . .2047$ |
| 12 | $-4095 . .-2048,2048 . .4095$ |
| 13 | $-8191 . .-4096,4096 . .8191$ |
| 14 | $-16383 . .-8192,8192 . .16383$ |

## F.1.6 Extended sequential DCT-based arithmetic encoding process for 12-bit sample precision

The process is identical to the sequential DCT process for 8 -bit precision except for changes in the precision of the FDCT computation.

The structure of the encoding procedure is identical to that specified in F.1.4 which was already defined for a 12-bit sample precision.

## F. 2 Sequential DCT-based decoding processes

## F.2.1 Sequential DCT-based control procedures and coding models

## F.2.1.1 Control procedures for sequential DCT-based decoders

The control procedures for decoding compressed image data and its constituent parts - the frame, scan, restart interval and MCU - are given in Figures E. 6 to E.10. The procedure for decoding a MCU (Figure E.10) repetitively calls the procedure for decoding a data unit. For DCT-based decoders the data unit is an $8 \times 8$ block of samples.

## F.2.1.2 Procedure for decoding an $8 \times 8$ block data unit

In the sequential DCT-based decoding process, decoding an $8 \times 8$ block data unit consists of the following procedures:
a) decode DC coefficient for $8 \times 8$ block using the DC table destination specified in the scan header;
b) decode AC coefficients for $8 \times 8$ block using the AC table destination specified in the scan header;
c) dequantize using table destination specified in the frame header and calculate the inverse $8 \times 8 \mathrm{DCT}$.

## F.2.1.3 Decoding models for the sequential DCT procedures

Two decoding procedures are used, one for the DC coefficient $\mathrm{ZZ}(0)$ and the other for the AC coefficients $\mathrm{ZZ}(1) \ldots \mathrm{ZZ}(63)$. The coefficients are decoded in the order in which they occur in the zig-zag sequence order, starting with the DC coefficient. The coefficients are represented as two's complement integers.

## F.2.1.3.1 Decoding model for DC coefficients

The decoded difference, DIFF, is added to PRED, the DC value from the most recently decoded $8 \times 8$ block from the same component. Thus ZZ $(0)=$ PRED + DIFF.

At the beginning of the scan and at the beginning of each restart interval, the prediction for the DC coefficient is initialized to zero.

## F.2.1.3.2 Decoding model for AC coefficients

The AC coefficients are decoded in the order in which they occur in ZZ . When the EOB is decoded, all remaining coefficients in ZZ are initialized to zero.

## F.2.1.4 Dequantization of the quantized DCT coefficients

The dequantization of the quantized DCT coefficients as described in Annex A, is accomplished by multiplying each quantized coefficient value by the quantization table value for that coefficient. The decoder shall be able to use up to four quantization table destinations.

## F.2.1.5 Inverse DCT (IDCT)

The mathematical definition of the IDCT is given in A.3.3.

After computation of the IDCT, the signed output samples are level-shifted, as described in Annex A, converting the output to an unsigned representation. For 8-bit precision the level shift is performed by adding 128. For 12-bit precision the level shift is performed by adding 2048 . If necessary, the output samples shall be clamped to stay within the range appropriate for the precision ( 0 to 255 for 8 -bit precision and 0 to 4095 for 12-bit precision).

## F.2.2 Baseline Huffman Decoding procedures

The baseline decoding procedure is for 8 -bit sample precision. The decoder shall be capable of using up to two DC and two AC Huffman tables within one scan.

## F.2.2.1 Huffman decoding of DC coefficients

The decoding procedure for the DC difference, DIFF, is:

$$
\begin{aligned}
& \text { T = DECODE } \\
& \text { DIFF = RECEIVE(T) } \\
& \text { DIFF = EXTEND(DIFF,T) }
\end{aligned}
$$

where DECODE is a procedure which returns the 8 -bit value associated with the next Huffman code in the compressed image data (see F.2.2.3) and RECEIVE(T) is a procedure which places the next T bits of the serial bit string into the low order bits of DIFF, MSB first. If T is zero, DIFF is set to zero. EXTEND is a procedure which converts the partially decoded DIFF value of precision T to the full precision difference. EXTEND is shown in Figure F.12.


Figure F. 12 - Extending the sign bit of a decoded value in $V$

## F.2.2.2 Decoding procedure for AC coefficients

The decoding procedure for AC coefficients is shown in Figures F. 13 and F. 14.


Figure F. 13 - Huffman decoding procedure for AC coefficients


Figure F. 14 - Decoding a non-zero AC coefficient

The decoding of the amplitude and sign of the non-zero coefficient is done in the procedure "Decode_ZZ(K)", shown in Figure F. 14.

DECODE is a procedure which returns the value, RS, associated with the next Huffman code in the code stream (see F.2.2.3). The values SSSS and R are derived from RS. The value of SSSS is the four low order bits of the composite value and R contains the value of RRRR (the four high order bits of the composite value). The interpretation of these values is described in F.1.2.2. EXTEND is shown in Figure F.12.

## F.2.2.3 The DECODE procedure

The DECODE procedure decodes an 8-bit value which, for the DC coefficient, determines the difference magnitude category. For the AC coefficient this 8 -bit value determines the zero run length and non-zero coefficient category.

Three tables, HUFFVAL, HUFFCODE, and HUFFSIZE, have been defined in Annex C. This particular implementation of DECODE makes use of the ordering of the Huffman codes in HUFFCODE according to both value and code size. Many other implementations of DECODE are possible.

NOTE - The values in HUFFVAL are assigned to each code in HUFFCODE and HUFFSIZE in sequence. There are no ordering requirements for the values in HUFFVAL which have assigned codes of the same length.

The implementation of DECODE described in this subclause uses three tables, MINCODE, MAXCODE and VALPTR, to decode a pointer to the HUFFVAL table. MINCODE, MAXCODE and VALPTR each have 16 entries, one for each possible code size. MINCODE(I) contains the smallest code value for a given length I, MAXCODE(I) contains the largest code value for a given length I, and VALPTR(I) contains the index to the start of the list of values in HUFFVAL which are decoded by code words of length I. The values in MINCODE and MAXCODE are signed 16-bit integers; therefore, a value of -1 sets all of the bits.

The procedure for generating these tables is shown in Figure F.15. The procedure for DECODE is shown in Figure F.16. Note that the 8 -bit "VALUE" is returned to the procedure which invokes DECODE.


Figure F. 15 - Decoder table generation


Figure F. 16 - Procedure for DECODE

## F.2.2.4 The RECEIVE procedure

RECEIVE(SSSS) is a procedure which places the next SSSS bits of the entropy-coded segment into the low order bits of DIFF, MSB first. It calls NEXTBIT and it returns the value of DIFF to the calling procedure (see Figure F.17).


Figure F. 17 - Procedure for RECEIVE(SSSS)

## F.2.2.5 The NEXTBIT procedure

NEXTBIT reads the next bit of compressed data and passes it to higher level routines. It also intercepts and removes stuff bytes and detects markers. NEXTBIT reads the bits of a byte starting with the MSB (see Figure F.18).

Before starting the decoding of a scan, and after processing a RST marker, CNT is cleared. The compressed data are read one byte at a time, using the procedure NEXTBYTE. Each time a byte, B, is read, CNT is set to 8 .

The only valid marker which may occur within the Huffman coded data is the $\mathrm{RST}_{\mathrm{m}}$ marker. Other than the EOI or markers which may occur at or before the start of a scan, the only marker which can occur at the end of the scan is the DNL (define-number-of-lines).

Normally, the decoder will terminate the decoding at the end of the final restart interval before the terminating marker is intercepted. If the DNL marker is encountered, the current line count is set to the value specified by that marker. Since the DNL marker can only be used at the end of the first scan, the scan decode procedure must be terminated when it is encountered.


Figure F. 18 - Procedure for fetching the next bit of compressed data

## F.2.3 Sequential DCT decoding process with 8-bit precision extended to four sets of Huffman tables

This process is identical to the Baseline decoding process described in F.2.2, with the exception that the decoder shall be capable of using up to four DC and four AC Huffman tables within one scan. Four DC and four AC Huffman tables is the maximum allowed by this Specification.

## F.2.4 Sequential DCT decoding process with arithmetic coding

This subclause describes the sequential DCT decoding process with arithmetic decoding.

The arithmetic decoding procedures for decoding binary decisions, initializing the statistical model, initializing the decoder, and resynchronizing the decoder are listed in Table D. 4 of Annex D.

Some of the procedures in Table D. 4 are used in the higher level control structure for scans and restart intervals described in F.2. At the beginning of scans and restart intervals, the probability estimates used in the arithmetic decoder are reset to the standard initial value as part of the Initdec procedure which restarts the arithmetic coder.

The statistical models defined in F.1.4.4 also apply to this decoding process.

The decoder shall be capable of using up to four DC and four AC conditioning tables and associated statistics areas within one scan.

## F.2.4.1 Arithmetic decoding of DC coefficients

The basic structure of the decision sequence for decoding a DC difference value, DIFF, is shown in Figure F.19. The equivalent structure for the encoder is found in Figure F.4.


Figure F. 19 - Arithmetic decoding of DC difference

The context-indices used in the DC decoding procedures are defined in Table F. 4 (see F.1.4.4.1.3).

The "Decode" procedure returns the value "D" of the binary decision. If the value is not zero, the sign and magnitude of the non-zero DIFF must be decoded by the procedure "Decode_V(S0)".

## F.2.4.2 Arithmetic Decoding of AC coefficients

The AC coefficients are decoded in the order that they occur in $\mathrm{ZZ}(1, \ldots, 63)$. The encoder procedure for the coding process is found in Figure F.5. Figure F. 20 illustrates the decoding sequence.


Figure F. 20 - Procedure for decoding the AC coefficients

The context-indices used in the AC decoding procedures are defined in Table F. 5 (see F.1.4.4.2).

In Figure F.20, K is the index to the zig-zag sequence position. For the sequential scan, $\mathrm{Kmin}=1$ and $\mathrm{Se}=63$. The decision at the top of the loop is the EOB decision. If the EOB occurs ( $\mathrm{D}=1$ ), the remaining coefficients in the block are set to zero. The inner loop just below the EOB decoding decodes runs of zero coefficients. Whenever the coefficient is non-zero, "Decode_V" decodes the sign and magnitude of the coefficient. After each non-zero coefficient is decoded, the EOB decision is again decoded unless $\mathrm{K}=\mathrm{Se}$.

## F.2.4.3 Decoding the binary decision sequence for non-zero DC differences and AC coefficients

Both the DC difference and the AC coefficients are represented as signed two's complement 16 -bit integer values. The decoding decision tree for these signed integer values is the same for both the DC and AC coding models. Note, however, that the statistical models are not the same.

## F.2.4.3.1 Arithmetic decoding of non-zero values

Denoting either DC differences or AC coefficients as V , the non-zero signed integer value of V is decoded by the sequence shown in Figure F.21. This sequence first decodes the sign of V. It then decodes the magnitude category of V (Decode_log2_Sz), and then decodes the low order magnitude bits (Decode_Sz_bits). Note that the value decoded for Sz must be incremented by 1 to get the actual coefficient magnitude.


Figure F. 21 - Sequence of procedures in decoding non-zero values of V

## F.2.4.3.1.1 Decoding the sign

The sign is decoded by the procedure shown in Figure F.22.

The context-indices are defined for DC decoding in Table F. 4 and AC decoding in Table F.5.

If $\operatorname{SIGN}=0$, the sign of the coefficient is positive; if $\operatorname{SIGN}=1$, the sign of the coefficient is negative.


Figure F. 22 - Decoding the sign of V

## F.2.4.3.1.2 Decoding the magnitude category

The context-index S is set in Decode_sign_of_V and the context-index values X1 and X2 are defined for DC coding in Table F. 4 and for AC coding in Table F.5.

In Figure F.23, M is set to the upper bound for the magnitude and shifted left until the decoded decision is zero. It is then shifted right by 1 to become the leading bit of the magnitude of Sz .


Figure F. 23 - Decoding procedure to establish the magnitude category

## F.2.4.3.1.3 Decoding the exact value of the magnitude

After the magnitude category is decoded, the low order magnitude bits are decoded. These bits are decoded in order of decreasing bit significance. The procedure is shown in Figure F. 24.

The context-index S is set in Decode_log2_Sz.


Figure F. 24 - Decision sequence to decode the magnitude bit pattern

## F.2.4.4 Decoder restart

The $\mathrm{RST}_{\mathrm{m}}$ markers which are added to the compressed data between each restart interval have a two byte value which cannot be generated by the coding procedures. These two byte sequences can be located without decoding, and can therefore be used to resynchronize the decoder. $\mathrm{RST}_{\mathrm{m}}$ markers can therefore be used for error recovery.

Before error recovery procedures can be invoked, the error condition must first be detected. Errors during decoding can show up in two places:
a) The decoder fails to find the expected marker at the point where it is expecting resynchronization.
b) Physically impossible data are decoded. For example, decoding a magnitude beyond the range of values allowed by the model is quite likely when the compressed data are corrupted by errors. For arithmetic decoders this error condition is extremely important to detect, as otherwise the decoder may reach a condition where it uses the compressed data very slowly.

NOTE - Some errors will not cause the decoder to lose synchronization. In addition, recovery is not possible for all errors; for example, errors in the headers are likely to be catastrophic. The two error conditions listed above, however, almost always cause the decoder to lose synchronization in a way which permits recovery.

In regaining synchronization, the decoder can make use of the modulo 8 coding restart interval number in the low order bits of the $\mathrm{RST}_{\mathrm{m}}$ marker. By comparing the expected restart interval number to the value in the next $\mathrm{RST}_{\mathrm{m}}$ marker in the compressed image data, the decoder can usually recover synchronization. It then fills in missing lines in the output data by replication or some other suitable procedure, and continues decoding. Of course, the reconstructed image will usually be highly corrupted for at least a part of the restart interval where the error occurred.

## F.2.5 Sequential DCT decoding process with Huffman coding and 12-bit precision

This process is identical to the sequential DCT process defined for 8-bit sample precision and extended to four Huffman tables, as documented in F.2.3, but with the following changes.

## F.2.5.1 Structure of DC Huffman decode table

The general structure of the DC Huffman decode table is extended as described in F.1.5.1.

## F.2.5.2 Structure of AC Huffman decode table

The general structure of the AC Huffman decode table is extended as described in F.1.5.2.

## F.2.6 Sequential DCT decoding process with arithmetic coding and 12-bit precision

The process is identical to the sequential DCT process for 8 -bit precision except for changes in the precision of the IDCT computation.

The structure of the decoding procedure in F.2.4 is already defined for a 12-bit input precision.

## Annex G <br> Progressive DCT-based mode of operation

(This annex forms an integral part of this Recommendation | International Standard)

This annex provides a functional specification of the following coding processes for the progressive DCT-based mode of operation

1) spectral selection only, Huffman coding, 8-bit sample precision;
2) spectral selection only, arithmetic coding, 8-bit sample precision;
3) full progression, Huffman coding, 8-bit sample precision;
4) full progression, arithmetic coding, 8-bit sample precision;
5) spectral selection only, Huffman coding, 12-bit sample precision;
6) spectral selection only, arithmetic coding, 12-bit sample precision;
7) full progression, Huffman coding, 12-bit sample precision;
8) full progression, arithmetic coding, 12-bit sample precision

For each of these, the encoding process is specified in G.1, and the decoding process is specified in G.2. The functional specification is presented by means of specific flow charts for the various procedures which comprise these coding processes.

NOTE - There is no requirement in this Specification that any encoder or decoder which embodies one of the above-named processes shall implement the procedures in precisely the manner specified by the flow charts in this annex. It is necessary only that an encoder or decoder implement the function specified in this annex. The sole criterion for an encoder or decoder to be considered in compliance with this Specification is that it satisfy the requirements given in clause 6 (for encoders) or clause 7 (for decoders), as determined by the compliance tests specified in Part 2.

The number of Huffman or arithmetic conditioning tables which may be used within the same scan is four.

Two complementary progressive procedures are defined, spectral selection and successive approximation.
In spectral selection the DCT coefficients of each block are segmented into frequency bands. The bands are coded in separate scans.

In successive approximation the DCT coefficients are divided by a power of two before coding. In the decoder the coefficients are multiplied by that same power of two before computing the IDCT. In the succeeding scans the precision of the coefficients is increased by one bit in each scan until full precision is reached.

An encoder or decoder implementing a full progression uses spectral selection within successive approximation. An allowed subset is spectral selection alone.

Figure G. 1 illustrates the spectral selection and successive approximation progressive processes.

## G. 1 Progressive DCT-based encoding processes

## G.1.1 Control procedures and coding models for progressive DCT-based procedures

## G.1.1.1 Control procedures for progressive DCT-based encoders

The control procedures for encoding an image and its constituent parts - the frame, scan, restart interval and MCU - are given in Figures E. 1 through E. 5.

The control structure for encoding a frame is the same as for the sequential procedures. However, it is convenient to calculate the FDCT for the entire set of components in a frame before starting the scans. A buffer which is large enough to store all of the DCT coefficients may be used for this progressive mode of operation.

The number of scans is determined by the progression defined; the number of scans may be much larger than the number of components in the frame.


Figure G. 1 - Spectral selection and successive approximation progressive processes

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The procedure for encoding a MCU (see Figure E.5) repetitively invokes the procedure for coding a data unit. For DCT-based encoders the data unit is an $8 \times 8$ block of samples.

Only a portion of each $8 \times 8$ block is coded in each scan, the portion being determined by the scan header parameters Ss , Se , Ah , and Al (see B.2.3). The procedures used to code portions of each $8 \times 8$ block are described in this annex. Note, however, that where these procedures are identical to those used in the sequential DCT-based mode of operation, the sequential procedures are simply referenced.

## G.1.1.1.1 Spectral selection control

In spectral selection the zig-zag sequence of DCT coefficients is segmented into bands. A band is defined in the scan header by specifying the starting and ending indices in the zig-zag sequence. One band is coded in a given scan of the progression. DC coefficients are always coded separately from AC coefficients, and only scans which code DC coefficients may have interleaved blocks from more than one component. All other scans shall have only one component. With the exception of the first DC scans for the components, the sequence of bands defined in the scans need not follow the zig-zag ordering. For each component, a first DC scan shall precede any AC scans.

## G.1.1.1.2 Successive approximation control

If successive approximation is used, the DCT coefficients are reduced in precision by the point transform (see A.4) defined in the scan header (see B.2.3). The successive approximation bit position parameter Al specifies the actual point transform, and the high four bits (Ah) - if there are preceding scans for the band - contain the value of the point transform used in those preceding scans. If there are no preceding scans for the band, Ah is zero.

Each scan which follows the first scan for a given band progressively improves the precision of the coefficients by one bit, until full precision is reached.

## G.1.1.2 Coding models for progressive DCT-based encoders

If successive approximation is used, the DCT coefficients are reduced in precision by the point transform (see A.4) defined in the scan header (see B.2.3). These models also apply to the progressive DCT-based encoders, but with the following changes.

## G.1.1.2.1 Progressive encoding model for DC coefficients

If Al is not zero, the point transform for DC coefficients shall be used to reduce the precision of the DC coefficients. If Ah is zero, the coefficient values (as modified by the point transform) shall be coded, using the procedure described in Annex F. If Ah is not zero, the least significant bit of the point transformed DC coefficients shall be coded, using the procedures described in this annex.

## G.1.1.2.2 Progressive encoding model for AC coefficients

If Al is not zero, the point transform for AC coefficients shall be used to reduce the precision of the AC coefficients. If Ah is zero, the coefficient values (as modified by the point transform) shall be coded using modifications of the procedures described in Annex F. These modifications are described in this annex. If Ah is not zero, the precision of the coefficients shall be improved using the procedures described in this annex.

## G.1.2 Progressive encoding procedures with Huffman coding

## G.1.2.1 Progressive encoding of DC coefficients with Huffman coding

The first scan for a given component shall encode the DC coefficient values using the procedures described in F.1.2.1. If the successive approximation bit position parameter Al is not zero, the coefficient values shall be reduced in precision by the point transform described in Annex A before coding.

In subsequent scans using successive approximation the least significant bits are appended to the compressed bit stream without compression or modification (see G.1.2.3), except for byte stuffing.

## G.1.2.2 Progressive encoding of AC coefficients with Huffman coding

In spectral selection and in the first scan of successive approximation for a component, the AC coefficient coding model is similar to that used by the sequential procedures. However, the Huffman code tables are extended to include coding of runs of End-Of-Bands (EOBs). See Table G.1.

Table G. 1 - EOBn code run length extensions

| EOBn code | Run length |
| :---: | :--- |
| EOB0 | 1 |
| EOB1 | 2,3 |
| EOB2 | $4 . .7$ |
| EOB3 | $8 . .15$ |
| EOB4 | $16 . .31$ |
| EOB5 | $32 . .63$ |
| EOB6 | $64 . .127$ |
| EOB7 | $128 . .255$ |
| EOB8 | $256 . .511$ |
| EOB9 | $512 . .1023$ |
| EOB10 | $1024 . .2047$ |
| EOB11 | 2048.4095 |
| EOB12 | $4096 . .8191$ |
| EOB13 | $8192 . .16383$ |
| EOB14 | 16384.32767 |

The end-of-band run structure allows efficient coding of blocks which have only zero coefficients. An EOB run of length 5 means that the current block and the next four blocks have an end-of-band with no intervening non-zero coefficients. The EOB run length is limited only by the restart interval.

The extension of the code table is illustrated in Figure G.2.


Figure G. 2 - Two-dimensional value array for Huffman coding

The EOBn code sequence is defined as follows. Each EOBn code is followed by an extension field similar to the extension field for the coefficient amplitudes (but with positive numbers only). The number of bits appended to the EOBn code is the minimum number required to specify the run length.

If an EOB run is greater than 32767 , it is coded as a sequence of EOB runs of length 32767 followed by a final EOB run sufficient to complete the run.

At the beginning of each restart interval the EOB run count, EOBRUN, is set to zero. At the end of each restart interval any remaining EOB run is coded.

The Huffman encoding procedure for AC coefficients in spectral selection and in the first scan of successive approximation is illustrated in Figures G.3, G.4, G.5, and G.6.


Figure G. 3 - Procedure for progressive encoding of AC coefficients with Huffman coding

In Figure G.3, Ss is the start of spectral selection, Se is the end of spectral selection, K is the index into the list of coefficients stored in the zig-zag sequence $\mathrm{ZZ}, \mathrm{R}$ is the run length of zero coefficients, and EOBRUN is the run length of EOBs. EOBRUN is set to zero at the start of each restart interval.

If the scan header parameter Al (successive approximation bit position low) is not zero, the DCT coefficient values $\mathrm{ZZ}(\mathrm{K})$ in Figure G. 3 and figures which follow in this annex, including those in the arithmetic coding section, shall be replaced by the point transformed values $\mathrm{ZZ}^{\prime}(\mathrm{K})$, where $\mathrm{ZZ}^{\prime}(\mathrm{K})$ is defined by:

$$
\mathrm{ZZ}^{\prime}(\mathrm{K})=\frac{\mathrm{ZZ}(\mathrm{~K}) \mathrm{x}}{2^{A l}}
$$

EOBSIZE is a procedure which returns the size of the EOB extension field given the EOB run length as input. CSIZE is a procedure which maps an AC coefficient to the SSSS value defined in the subclauses on sequential encoding (see F.1.1 and F.1.3).


Figure G. 4 - Progressive encoding of a non-zero AC coefficient


Figure G. 5 - Encoding of the run of zero coefficients


Figure G. 6 - Encoding of the zero run and non-zero coefficient

## G.1.2.3 Coding model for subsequent scans of successive approximation

The Huffman coding structure of the subsequent scans of successive approximation for a given component is similar to the coding structure of the first scan of that component.

The structure of the AC code table is identical to the structure described in G.1.2.2. Each non-zero point transformed coefficient that has a zero history (i.e. that has a value $\pm 1$, and therefore has not been coded in a previous scan) is defined by a composite 8 -bit run length-magnitude value of the form:

## RRRRSSSS

The four most significant bits, RRRR, give the number of zero coefficients that are between the current coefficient and the previously coded coefficient (or the start of band). Coefficients with non-zero history (a non-zero value coded in a previous scan) are skipped over when counting the zero coefficients. The four least significant bits, SSSS, provide the magnitude category of the non-zero coefficient; for a given component the value of SSSS can only be one.

The run length-magnitude composite value is Huffman coded and each Huffman code is followed by additional bits:
a) One bit codes the sign of the newly non-zero coefficient. A 0 -bit codes a negative sign; a 1 -bit codes a positive sign.
b) For each coefficient with a non-zero history, one bit is used to code the correction. A 0 -bit means no correction and a 1-bit means that one shall be added to the (scaled) decoded magnitude of the coefficient.

Non-zero coefficients with zero history are coded with a composite code of the form:
HUFFCO(RRRRSSSS) + additional bit (rule a) + correction bits (rule b)

In addition whenever zero runs are coded with ZRL or EOBn codes, correction bits for those coefficients with non-zero history contained within the zero run are appended according to rule b above.

For the Huffman coding version of Encode_AC_Coefficients_SA the EOB is defined to be the position of the last point transformed coefficient of magnitude 1 in the band. If there are no coefficients of magnitude 1 , the EOB is defined to be zero.

NOTE - The definition of EOB is different for Huffman and arithmetic coding procedures.

In Figures G. 7 and G. 8 BE is the count of buffered correction bits at the start of coding of the block. BE is initialized to zero at the start of each restart interval. At the end of each restart interval any remaining buffered bits are appended to the bit stream following the last EOBn Huffman code and associated appended bits.

In Figures G. 7 and G.9, BR is the count of buffered correction bits which are appended to the bit stream according to rule b. BR is set to zero at the beginning of each Encode_AC_Coefficients_SA. At the end of each restart interval any remaining buffered bits are appended to the bit stream following the last Huffman code and associated appended bits.

## G.1.3 Progressive encoding procedures with arithmetic coding

## G.1.3.1 Progressive encoding of DC coefficients with arithmetic coding

The first scan for a given component shall encode the DC coefficient values using the procedures described in F.1.4.1. If the successive approximation bit position parameter is not zero, the coefficient values shall be reduced in precision by the point transform described in Annex A before coding.

In subsequent scans using successive approximation the least significant bits shall be coded as binary decisions using a fixed probability estimate of $0.5\left(\mathrm{Qe}=\mathrm{X}^{\prime} 5 \mathrm{~A} 1 \mathrm{D}^{\prime}, \mathrm{MPS}=0\right)$.

## G.1.3.2 Progressive encoding of AC coefficients with arithmetic coding

Except for the point transform scaling of the DCT coefficients and the grouping of the coefficients into bands, the first scan(s) of successive approximation is identical to the sequential encoding procedure described in F.1.4. If Kmin is equated to Ss, the index of the first AC coefficient index in the band, the flow chart shown in Figure F. 5 applies. The EOB decision in that figure refers to the "end-of-band" rather than the "end-of-block". For the arithmetic coding version of Encode_AC_Coefficients_SA (and all other AC coefficient coding procedures) the EOB is defined to be the position following the last non-zero coefficient in the band.

NOTE - The definition of EOB is different for Huffman and arithmetic coding procedures.

The statistical model described in F.1.4 also holds. For this model the default value of $K x$ is 5. Other values of $K x$ may be specified using the DAC marker code (Annex B). The following calculation for Kx has proven to give good results for 8bit precision samples:

$$
\mathrm{Kx}=\mathrm{Kmin}+\mathrm{SRL}(8+\mathrm{Se}-\mathrm{Kmin}) 4
$$

This expression reduces to the default of $\mathrm{Kx}=5$ when the band is from index 1 to index 63 .


Figure G. 7 - Successive approximation coding of AC coefficients using Huffman coding


Figure G. 8 - Transferring BE buffered bits from buffer to bit stream


Figure G. 9 - Transferring BR buffered bits from buffer to bit stream

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## G.1.3.3 Coding model for subsequent scans of successive approximation

The procedure "Encode_AC_Coefficient_SA" shown in Figure G. 10 increases the precision of the AC coefficient values in the band by one bit.

As in the first scan of successive approximation for a component, an EOB decision is coded at the start of the band and after each non-zero coefficient.

However, since the end-of-band index of the previous successive approximation scan for a given component, EOBx, is known from the data coded in the prior scan of that component, this decision is bypassed whenever the current index, K, is less than EOBx. As in the first scan(s), the EOB decision is also bypassed whenever the last coefficient in the band is not zero. The decision $Z Z(K)=0$ decodes runs of zero coefficients. If the decoder is at this step of the procedure, at least one non-zero coefficient remains in the band of the block being coded. If $\mathrm{ZZ}(\mathrm{K})$ is not zero, the procedure in Figure G. 11 is followed to code the value.

The context-indices in Figures G. 10 and G. 11 are defined in Table G. 2 (see G.1.3.3.1). The signs of coefficients with magnitude of one are coded with a fixed probability value of approximately $0.5\left(\mathrm{Qe}=\mathrm{X}^{\prime} 5 \mathrm{~A} 1 \mathrm{D}^{\prime}, \mathrm{MPS}=0\right)$.

## G.1.3.3.1 Statistical model for subsequent successive approximation scans

As shown in Table G.2, each statistics area for subsequent successive approximation scans of AC coefficients consists of a contiguous set of 189 statistics bins. The signs of coefficients with magnitude of one are coded with a fixed probability value of approximately $0.5\left(\mathrm{Qe}=\mathrm{X}^{\prime} 5 \mathrm{~A} 1 \mathrm{D}^{\prime}, \mathrm{MPS}=0\right)$.

## G. 2 Progressive decoding of the DCT

The description of the computation of the IDCT and the dequantization procedure contained in A.3.3 and A.3.4 apply to the progressive operation.

Progressive decoding processes must be able to decompress compressed image data which requires up to four sets of Huffman or arithmetic coder conditioning tables within a scan.

In order to avoid repetition, detailed flow diagrams of progressive decoder operation are not included. Decoder operation is defined by reversing the function of each step described in the encoder flow charts, and performing the steps in reverse order.


Figure G. 10 - Subsequent successive approximation scans for coding of AC coefficients using arithmetic coding


Figure G. 11 - Coding non-zero coefficients for subsequent successive approximation scans

Table G. 2 - Statistical model for subsequent scans of successive approximation coding of AC coefficient

| Context-index | AC coding | Coding decision |
| :---: | :--- | :--- |
| SE | $3 \times(\mathrm{K}-1)$ | $\mathrm{K}=\mathrm{EOB}$ |
| S0 | $\mathrm{SE}+1$ | $\mathrm{~V}=0$ |
| SS | Fixed estimate | Sign |
| SC | $\mathrm{S} 0+1$ | LSB ZZ(K) $=1$ |


#### Abstract

Annex H

\section*{Lossless mode of operation} (This annex forms an integral part of this Recommendation | International Standard)


This annex provides a functional specification of the following coding processes for the lossless mode of operation:

1) lossless processes with Huffman coding;
2) lossless processes with arithmetic coding.

For each of these, the encoding process is specified in H.1, and the decoding process is specified in H.2. The functional specification is presented by means of specific procedures which comprise these coding processes.

NOTE - There is no requirement in this Specification that any encoder or decoder which embodies one of the above-named processes shall implement the procedures in precisely the manner specified in this annex. It is necessary only that an encoder or decoder implement the function specified in this annex. The sole criterion for an encoder or decoder to be considered in compliance with this Specification is that it satisfy the requirements given in clause 6 (for encoders) or clause 7 (for decoders), as determined by the compliance tests specified in Part 2.

The processes which provide for sequential lossless encoding and decoding are not based on the DCT. The processes used are spatial processes based on the coding model developed for the DC coefficients of the DCT. However, the model is extended by incorporating a set of selectable one- and two-dimensional predictors, and for interleaved data the ordering of samples for the one-dimensional predictor can be different from that used in the DCT-based processes.

Either Huffman coding or arithmetic coding entropy coding may be employed for these lossless encoding and decoding processes. The Huffman code table structure is extended to allow up to 16-bit precision for the input data. The arithmetic coder statistical model is extended to a two-dimensional form.

## H. 1 Lossless encoder processes

## H.1.1 Lossless encoder control procedures

Subclause E. 1 contains the encoder control procedures. In applying these procedures to the lossless encoder, the data unit is one sample.

Input data precision may be from 2 to 16 bits/sample. If the input data path has different precision from the input data, the data shall be aligned with the least significant bits of the input data path. Input data is represented as unsigned integers and is not level shifted prior to coding.

When the encoder is reset in the restart interval control procedure (see E.1.4), the prediction is reset to a default value. If arithmetic coding is used, the statistics are also reset.

For the lossless processes the restart interval shall be an integer multiple of the number of MCU in an MCU-row.

## H.1.2 Coding model for lossless encoding

The coding model developed for encoding the DC coefficients of the DCT is extended to allow a selection from a set of seven one-dimensional and two-dimensional predictors. The predictor is selected in the scan header (see Annex B). The same predictor is used for all components of the scan. Each component in the scan is modeled independently, using predictions derived from neighbouring samples of that component.

## H.1.2.1 Prediction

Figure H. 1 shows the relationship between the positions ( $a, b, c$ ) of the reconstructed neighboring samples used for prediction and the position of x , the sample being coded.

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Figure H. 1 - Relationship between sample and prediction samples

Define Px to be the prediction and $\mathrm{Ra}, \mathrm{Rb}$, and Rc to be the reconstructed samples immediately to the left, immediately above, and diagonally to the left of the current sample. The allowed predictors, one of which is selected in the scan header, are listed in Table H.1.

Table H. 1 - Predictors for lossless coding


Selection-value 0 shall only be used for differential coding in the hierarchical mode of operation. Selections 1,2 and 3 are one-dimensional predictors and selections $4,5,6$, and 7 are two-dimensional predictors.

The one-dimensional horizontal predictor (prediction sample Ra) is used for the first line of samples at the start of the scan and at the beginning of each restart interval. The selected predictor is used for all other lines. The sample from the line above (prediction sample Rb ) is used at the start of each line, except for the first line. At the beginning of the first line and at the beginning of each restart interval the prediction value of $2^{P-1}$ is used, where P is the input precision.

If the point transformation parameter (see A.4) is non-zero, the prediction value at the beginning of the first lines and the beginning of each restart interval is $2^{\mathrm{P}-\mathrm{Pt}-1}$, where Pt is the value of the point transformation parameter.

Each prediction is calculated with full integer arithmetic precision, and without clamping of either underflow or overflow beyond the input precision bounds. For example, if Ra and Rb are both 16 -bit integers, the sum is a 17 -bit integer. After dividing the sum by 2 (predictor 7 ), the prediction is a 16 -bit integer.

For simplicity of implementation, the divide by 2 in the prediction selections 5 and 6 of Table H. 1 is done by an arithmetic-right-shift of the integer values.

The difference between the prediction value and the input is calculated modulo $2^{16}$. In the decoder the difference is decoded and added, modulo $2^{16}$, to the prediction.

## H.1.2 2 Huffman coding of the modulo difference

The Huffman coding procedures defined in Annex F for coding the DC coefficients are used to code the modulo 216 differences. The table for DC coding contained in Tables F. 1 and F. 6 is extended by one additional entry. No extra bits are appended after SSSS $=16$ is encoded. See Table H.2.

Table H. 2 - Difference categories for lossless Huffman coding

| SSSS | Difference values |
| :---: | :---: |
| 0 | 0 |
| 1 | $-1,1$ |
| 2 | $-3,-2,2,3$ |
| 3 | $-7 . .-4,4 . .7$ |
| 4 | $-15 . .-8,8 . .15$ |
| 5 | $-31 . .-16,16 . .31$ |
| 6 | $-63 . .-32,32 . .63$ |
| 7 | $-127 . .-64,64 . .127$ |
| 8 | $-255 . .-128,128 . .255$ |
| 9 | $-511 . .-256,256 . .511$ |
| 10 | $-1023 . .-512,512 . .1023$ |
| 11 | $-2047 . .-1024,1024 . .2047$ |
| 12 | $-4095 . .-2048,2048 . .4095$ |
| 13 | $-8191 . .-4096,4096 . .8191$ |
| 14 | $-16383 .-8192,8192 . .16383$ |
| 15 | $-32767 . .-16384,16384 . .32767$ |
| 16 | 32768 |

## H.1.2.3 Arithmetic coding of the modulo difference

The statistical model defined for the DC coefficient arithmetic coding model (see F.1.4.4.1) is generalized to a twodimensional form in which differences coded for the sample to the left and for the line above are used for conditioning.

## H.1.2.3.1 Two-dimensional statistical model

The binary decisions are conditioned on the differences coded for the neighbouring samples immediately above and immediately to the left from the same component. As in the coding of the DC coefficients, the differences are classified into 5 categories: zero $(0)$, small positive $(+S)$, small negative $(-S)$, large positive $(+\mathrm{L})$, and large negative $(-\mathrm{L})$. The two independent difference categories combine to give 25 different conditioning states. Figure H. 2 shows the two-dimensional array of conditioning indices. For each of the 25 conditioning states probability estimates for four binary decisions are kept.

At the beginning of the scan and each restart interval the conditioning derived from the line above is set to zero for the first line of each component. At the start of each line, the difference to the left is set to zero for the purposes of calculating the conditioning.

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Difference above (position b)

|  | Difference above (position b) |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 0 | 0 | $+S$ | $-S$ | $+L$ | $-L$ |
| Difference to left <br> (position a) | 0 | 4 | 8 | 12 | 16 |  |
|  | $-S$ | 20 | 24 | 28 | 32 | 36 |
|  | 40 | 44 | 48 | 52 | 56 |  |
|  | $-L$ | 60 | 64 | 68 | 72 | 76 |

Figure H. $2-5 \times 5$ Conditioning array for two-dimensional statistical model

## H.1.2.3.2 Assignment of statistical bins to the DC binary decision tree

Each statistics area for lossless coding consists of a contiguous set of 158 statistics bins. The first 100 bins consist of 25 sets of four bins selected by a context-index S0. The value of S 0 is given by $\mathrm{L}_{-} \operatorname{Context}(\mathrm{Da}, \mathrm{Db})$, which provides a value of $0,4, \ldots, 92$ or 96 , depending on the difference classifications of Da and Db (see H.1.2.3.1). The value for S 0 provided by L_Context $(\mathrm{Da}, \mathrm{Db})$ is from the array in Figure H.2.

The remaining 58 bins consist of two sets of 29 bins, $\mathrm{X} 1, \ldots, \mathrm{X} 15, \mathrm{M} 2, \ldots, \mathrm{M} 15$, which are used to code magnitude category decisions and magnitude bits. The value of X 1 is given by X1_Context( Db ), which provides a value of 100 when Db is in the zero, small positive or small negative categories and a value of 129 when Db is in the large positive or large negative categories.

The assignment of statistical bins to the binary decision tree used for coding the difference is given in Table H.3.

Table H. 3 - Statistical model for lossless coding

| Context-index | Value | Coding decision |
| :---: | :---: | :---: |
| S0 | L_Context(Da,Db) | $\mathrm{V}=0$ |
| SS | S0 + 1 | Sign |
| SP | $\mathrm{S} 0+2$ | $\mathrm{Sz}<1$ if $\mathrm{V}>0$ |
| SN | S0 + 3 | $\mathrm{Sz}<1$ if $\mathrm{V}<0$ |
| X1 | X1_Context(Db) | Sz<2 |
| X2 | $\mathrm{X} 1+1$ | Sz<4 |
| X3 | $\mathrm{X} 1+2$ | $\mathrm{Sz}<8$ |
| . | . | . |
| - 15 | - 1 |  |
| X15 | $\mathrm{X} 1+14$ | $\mathrm{Sz}<2{ }^{15}$ |
| M2 | X2 +14 | Magnitude bits if $\mathrm{Sz}<4$ |
| M3 | X3 + 14 | Magnitude bits if $\mathrm{Sz}<8$ |
| . | . |  |
| M15 | X15+14 | Magnitude bits if Sz<215 |
| M15 | X15 + 14 | Magnitude bits if $\mathrm{Sz}<215$ |

## H.1.2.3.3 Default conditioning bounds

The bounds, L and U , for determining the conditioning category have the default values $\mathrm{L}=0$ and $\mathrm{U}=1$. Other bounds may be set using the DAC (Define-Arithmetic-Conditioning) marker segment, as described in Annex B.

## H.1.2.3.4 Initial conditions for statistical model

At the start of a scan and at each restart, all statistics bins are re-initialized to the standard default value described in Annex D.

## H. 2 Lossless decoder processes

Lossless decoders may employ either Huffman decoding or arithmetic decoding. They shall be capable of using up to four tables in a scan. Lossless decoders shall be able to decode encoded image source data with any input precision from 2 to 16 bits per sample.

## H.2.1 Lossless decoder control procedures

Subclause E. 2 contains the decoder control procedures. In applying these procedures to the lossless decoder the data unit is one sample.

When the decoder is reset in the restart interval control procedure (see E.2.4) the prediction is reset to the same value used in the encoder (see H.1.2.1). If arithmetic coding is used, the statistics are also reset.

Restrictions on the restart interval are specified in H.1.1.

## H.2.2 Coding model for lossless decoding

The predictor calculations defined in H.1.2 also apply to the lossless decoder processes.
The lossless decoders, decode the differences and add them, modulo $2^{16}$, to the predictions to create the output. The lossless decoders shall be able to interpret the point transform parameter, and if non-zero, multiply the output of the lossless decoder by $2^{\mathrm{Pt}}$.

In order to avoid repetition, detailed flow charts of the lossless decoding procedures are omitted.

#  

## Annex J

## Hierarchical mode of operation

(This annex forms an integral part of this Recommendation | International Standard)

This annex provides a functional specification of the coding processes for the hierarchical mode of operation.
In the hierarchical mode of operation each component is encoded or decoded in a non-differential frame. Such frames may be followed by a sequence of differential frames. A non-differential frame shall be encoded or decoded using the procedures defined in Annexes F, G and H. Differential frame procedures are defined in this annex.

The coding process for a hierarchical encoding containing DCT-based processes is defined as the highest numbered process listed in Table J. 1 which is used to code any non-differential DCT-based or differential DCT-based frame in the compressed image data format. The coding process for a hierarchical encoding containing only lossless processes is defined to be the process used for the non-differential frames.

Table J. 1 - Coding processes for hierarchical mode

| Process | Non-differential frame specification |  |
| :---: | :--- | :--- |
| 1 | Extended sequential DCT, Huffman, 8-bit | Annex F, process 2 |
| 2 | Extended sequential DCT, arithmetic, 8-bit | Annex F, process 3 |
| 3 | Extended sequential DCT, Huffman, 12-bit | Annex F, process 4 |
| 4 | Extended sequential DCT, arithmetic, 12-bit | Annex F, process 5 |
| 5 | Spectral selection only, Huffman, 8-bit | Annex G, process 1 |
| 6 | Spectral selection only, arithmetic, 8-bit | Annex G, process 2 |
| 7 | Full progression, Huffman, 8-bit | Annex G, process 3 |
| 8 | Full progression, arithmetic, 8-bit | Annex G, process 4 |
| 9 | Spectral selection only, Huffman, 12-bit | Annex G, process 5 |
| 10 | Spectral selection only, arithmetic, 12-bit | Annex G, process 6 |
| 11 | Full progression, Huffman, 12-bit | Annex G, process 7 |
| 12 | Full progression, arithmetic, 12-bit | Annex G, process 8 |
| 13 | Lossless, Huffman, 2 through 16 bits | Annex H, process 1 |
| 14 | Lossless, arithmetic, 2 through 16 bits | Annex H, process 2 |

Hierarchical mode syntax requires a DHP marker segment that appears before the non-differential frame or frames. It may include EXP marker segments and differential frames which shall follow the initial non-differential frame. The frame structure in hierarchical mode is identical to the frame structure in non-hierarchical mode.

Either all non-differential frames within an image shall be coded with DCT-based processes, or all non-differential frames shall be coded with lossless processes. All frames within an image must use the same entropy coding procedure, either Huffman or arithmetic, with the exception that non-differential frames coded with the baseline process may occur in the same image with frames coded with arithmetic coding processes.

If the non-differential frames use DCT-based processes, all differential frames except the final frame for a component shall use DCT-based processes. The final differential frame for each component may use a differential lossless process.

If the non-differential frames use lossless processes, all differential frames shall use differential lossless processes.

For each of the processes listed in Table J.1, the encoding processes are specified in J.1, and decoding processes are specified in J.2.

NOTE - There is no requirement in this Specification that any encoder or decoder which embodies one of the above-named processes shall implement the procedures in precisely the manner specified by the flow charts in this annex. It is necessary only that an encoder or decoder implement the function specified in this annex. The sole criterion for an encoder or decoder to be considered in compliance with this Specification is that it satisfy the requirements given in clause 6 (for encoders) or clause 7 (for decoders), as determined by the compliance tests specified in Part 2.

In the hierarchical mode of operation each component is encoded or decoded in a non-differential frame followed by a sequence of differential frames. A non-differential frame shall use the procedures defined in Annexes F, G, and H. Differential frame procedures are defined in this annex.

## J. 1 Hierarchical encoding

## J.1.1 Hierarchical control procedure for encoding an image

The control structure for encoding of an image using the hierarchical mode is given in Figure J.1.


Figure J. 1 - Hierarchical control procedure for encoding an image

In Figure J. 1 procedures in brackets shall be performed whenever the particular hierarchical encoding sequence being followed requires them.

## 

In the hierarchical mode the define-hierarchical-progression (DHP) marker segment shall be placed in the compressed image data before the first start-of-frame. The DHP segment is used to signal the size of the image components of the completed image. The syntax of the DHP segment is specified in Annex B.

The first frame for each component or group of components in a hierarchical process shall be encoded by a non-differential frame. Differential frames shall then be used to encode the two's complement differences between source input components (possibly downsampled) and the reference components (possibly upsampled). The reference components are reconstructed components created by previous frames in the hierarchical process. For either differential or non-differential frames, reconstructions of the components shall be generated if needed as reference components for a subsequent frame in the hierarchical process.

Resolution changes may occur between hierarchical frames in a hierarchical process. These changes occur if downsampling filters are used to reduce the spatial resolution of some or all of the components of the source image. When the resolution of a reference component does not match the resolution of the component input to a differential frame, an upsampling filter shall be used to increase the spatial resolution of the reference component. The EXP marker segment shall be added to the compressed image data before the start-of-frame whenever upsampling of a reference component is required. No more than one EXP marker segment shall precede a given frame.

Any of the marker segments allowed before a start-of-frame for the encoding process selected may be used before either non-differential or differential frames.

For 16-bit input precision (lossless encoder), the differential components which are input to a differential frame are calculated modulo $2^{16}$. The reconstructed components calculated from the reconstructed differential components are also calculated modulo 216.

If a hierarchical encoding process uses a DCT encoding process for the first frame, all frames in the hierarchical process except for the final frame for each component shall use the DCT encoding processes defined in either Annex F or Annex G , or the modified DCT encoding processes defined in this annex. The final frame may use a modified lossless process defined in this annex.

If a hierarchical encoding process uses a lossless encoding process for the first frame, all frames in the hierarchical process shall use a lossless encoding process defined in Annex H, or a modified lossless process defined in this annex.

## J.1.1.1 Downsampling filter

The downsampled components are generated using a downsampling filter that is not specified in this Specification. This filter should, however, be consistent with the upsampling filter. An example of a downsampling filter is provided in K.5.

## J.1.1.2 Upsampling filter

The upsampling filter increases the spatial resolution by a factor of two horizontally, vertically, or both. Bi-linear interpolation is used for the upsampling filter, as illustrated in Figure J.2.


Figure J. 2 - Diagram of sample positions for upsampling rules

The rule for calculating the interpolated value is:

$$
\mathrm{P}_{\mathrm{x}}=(\mathrm{Ra}+\mathrm{Rb}) / 2
$$

where Ra and Rb are sample values from adjacent positions a and b of the lower resolution image and Px is the interpolated value. The division indicates truncation, not rounding. The left-most column of the upsampled image matches the left-most column of the lower resolution image. The top line of the upsampled image matches the top line of the lower resolution image. The right column and the bottom line of the lower resolution image are replicated to provide the values required for the right column edge and bottom line interpolations. The upsampling process always doubles the line length or the number of lines.

If both horizontal and vertical expansions are signalled, they are done in sequence - first the horizontal expansion and then the vertical.

## J.1.2 Control procedure for encoding a differential frame

The control procedures in Annex E for frames, scans, restart intervals, and MCU also apply to the encoding of differential frames, and the scans, restart intervals, and MCU from which the differential frame is constructed. The differential frames differ from the frames of Annexes F, G, and H only at the coding model level.

## J.1.3 Encoder coding models for differential frames

The coding models defined in Annexes F, G, and H are modified to allow them to be used for coding of two's complement differences.

## J.1.3.1 Modifications to encoder DCT encoding models for differential frames

Two modifications are made to the DCT coding models to allow them to be used in differential frames. First, the FDCT of the differential input is calculated without the level shift. Second, the DC coefficient of the DCT is coded directly without prediction.

## J.1.3.2 Modifications to lossless encoding models for differential frames

One modification is made to the lossless coding models. The difference is coded directly - without prediction. The prediction selection parameter in the scan header shall be set to zero. The point transform which may be applied to the differential inputs is defined in Annex A.

## J.1.4 Modifications to the entropy encoders for differential frames

The coding of two's complement differences requires one extra bit of precision for the Huffman coding of AC coefficients. The extension to Tables F. 1 and F. 7 is given in Table J.2.

Table J. 2 - Modifications to table of AC coefficient amplitude ranges

| SSSS | AC coefficients |
| :---: | :--- |
| 15 | $-32767 . .-16384,16384 . .32767$ |

The arithmetic coding models are already defined for the precision needed in differential frames.

## J. 2 Hierarchical decoding

## J.2.1 Hierarchical control procedure for decoding an image

The control structure for decoding an image using the hierarchical mode is given in Figure J.3.


Figure J. 3 - Hierarchical control procedure for decoding an image

The Interpret markers procedure shall decode the markers which may precede the SOF marker, continuing this decoding until either a SOF or EOI marker is found. If the DHP marker is encountered before the first frame, a flag is set which selects the hierarchical decoder at the "hierarchical?" decision point. In addition to the DHP marker (which shall precede any SOF) and the EXP marker (which shall precede any differential SOF requiring resolution changes in the reference components), any other markers which may precede a SOF shall be interpreted to the extent required for decoding of the compressed image data.

If a differential SOF marker is found, the differential frame path is followed. If the EXP was encountered in the Interpret markers procedure, the reference components for the frame shall be upsampled as required by the parameters in the EXP segment. The upsampling procedure described in J.1.1.2 shall be followed.

The Decode_differential_frame procedure generates a set of differential components. These differential components shall be added, modulo $2^{16}$, to the upsampled reference components in the Reconstruct_components procedure. This creates a new set of reference components which shall be used when required in subsequent frames of the hierarchical process.

## J.2.2 Control procedure for decoding a differential frame

The control procedures in Annex E for frames, scans, restart intervals, and MCU also apply to the decoding of differential frames and the scans, restart intervals, and MCU from which the differential frame is constructed. The differential frame differs from the frames of Annexes F, G, and H only at the decoder coding model level.

## J.2.3 Decoder coding models for differential frames

The decoding models described in Annexes F, G, and H are modified to allow them to be used for decoding of two's complement differential components.

## J.2.3.1 Modifications to the differential frame decoder DCT coding model

Two modifications are made to the decoder DCT coding models to allow them to code differential frames. First, the IDCT of the differential output is calculated without the level shift. Second, the DC coefficient of the DCT is decoded directly without prediction.

## J.2.3.2 Modifications to the differential frame decoder lossless coding model

One modification is made to the lossless decoder coding model. The difference is decoded directly - without prediction. If the point transformation parameter in the scan header is not zero, the point transform, defined in Annex A, shall be applied to the differential output.

## J.2.4 Modifications to the entropy decoders for differential frames

The decoding of two's complement differences requires one extra bit of precision in the Huffman code table. This is described in J.1.4. The arithmetic coding models are already defined for the precision needed in differential frames.

## Annex K

## Examples and guidelines

(This annex does not form an integral part of this Recommendation | International Standard)

This annex provides examples of various tables, procedures, and other guidelines.

## K. 1 Quantization tables for luminance and chrominance components

Two examples of quantization tables are given in Tables K.1 and K.2. These are based on psychovisual thresholding and are derived empirically using luminance and chrominance and $2: 1$ horizontal subsampling. These tables are provided as examples only and are not necessarily suitable for any particular application. These quantization values have been used with good results on 8-bit per sample luminance and chrominance images of the format illustrated in Figure 13. Note that these quantization values are appropriate for the DCT normalization defined in A.3.3.

If these quantization values are divided by 2 , the resulting reconstructed image is usually nearly indistinguishable from the source image.

Table K. 1 - Luminance quantization table

| 16 | 11 | 10 | 16 | 24 | 40 | 51 | 61 |
| :---: | :---: | ---: | ---: | ---: | ---: | ---: | :---: |
| 12 | 12 | 14 | 19 | 26 | 58 | 60 | 55 |
| 14 | 13 | 16 | 24 | 40 | 57 | 69 | 56 |
| 14 | 17 | 22 | 29 | 51 | 87 | 80 | 62 |
| 18 | 22 | 37 | 56 | 68 | 109 | 103 | 77 |
| 24 | 35 | 55 | 64 | 81 | 104 | 113 | 92 |
| 49 | 64 | 78 | 87 | 103 | 121 | 120 | 101 |
| 72 | 92 | 95 | 98 | 112 | 100 | 103 | 99 |

Table K. 2 - Chrominance quantization table

| 17 | 18 | 24 | 47 | 99 | 99 | 99 | 99 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 18 | 21 | 26 | 66 | 99 | 99 | 99 | 99 |
| 24 | 26 | 56 | 99 | 99 | 99 | 99 | 99 |
| 47 | 66 | 99 | 99 | 99 | 99 | 99 | 99 |
| 99 | 99 | 99 | 99 | 99 | 99 | 99 | 99 |
| 99 | 99 | 99 | 99 | 99 | 99 | 99 | 99 |
| 99 | 99 | 99 | 99 | 99 | 99 | 99 | 99 |
| 99 | 99 | 99 | 99 | 99 | 99 | 99 | 99 |

## K. 2 A procedure for generating the lists which specify a Huffman code table

A Huffman table is generated from a collection of statistics in two steps. The first step is the generation of the list of lengths and values which are in accord with the rules for generating the Huffman code tables. The second step is the generation of the Huffman code table from the list of lengths and values.

The first step, the topic of this section, is needed only for custom Huffman table generation and is done only in the encoder. In this step the statistics are used to create a table associating each value to be coded with the size (in bits) of the corresponding Huffman code. This table is sorted by code size.

A procedure for creating a Huffman table for a set of up to 256 symbols is shown in Figure K.1. Three vectors are defined for this procedure:

| FREQ(V) | Frequency of occurrence of symbol V |
| :--- | :--- |
| CODESIZE(V) | Code size of symbol V |
| OTHERS(V) | Index to next symbol in chain of all symbols in current branch of code tree |

where V goes from 0 to 256 .
Before starting the procedure, the values of FREQ are collected for $\mathrm{V}=0$ to 255 and the FREQ value for $\mathrm{V}=256$ is set to 1 to reserve one code point. FREQ values for unused symbols are defined to be zero. In addition, the entries in CODESIZE are all set to 0 , and the indices in OTHERS are set to -1 , the value which terminates a chain of indices. Reserving one code point guarantees that no code word can ever be all "1" bits.

The search for the entry with the least value of $\operatorname{FREQ}(\mathrm{V})$ selects the largest value of V with the least value of $\operatorname{FREQ}(\mathrm{V})$ greater than zero.

The procedure "Find V1 for least value of $\operatorname{FREQ}(\mathrm{V} 1)>0$ " always selects the value with the largest value of V1 when more than one V1 with the same frequency occurs. The reserved code point is then guaranteed to be in the longest code word category.


Figure K. 1 - Procedure to find Huffman code sizes

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Once the code lengths for each symbol have been obtained, the number of codes of each length is obtained using the procedure in Figure K.2. The count for each size is contained in the list, BITS. The counts in BITS are zero at the start of the procedure. The procedure assumes that the probabilities are large enough that code lengths greater than 32 bits never occur. Note that until the final Adjust_BITS procedure is complete, BITS may have more than the 16 entries required in the table specification (see Annex C).


Figure K. 2 - Procedure to find the number of codes of each size

Figure K. 3 gives the procedure for adjusting the BITS list so that no code is longer than 16 bits. Since symbols are paired for the longest Huffman code, the symbols are removed from this length category two at a time. The prefix for the pair (which is one bit shorter) is allocated to one of the pair; then (skipping the BITS entry for that prefix length) a code word from the next shortest non-zero BITS entry is converted into a prefix for two code words one bit longer. After the BITS list is reduced to a maximum code length of 16 bits, the last step removes the reserved code point from the code length count.


Figure K. 3 - Procedure for limiting code lengths to 16 bits

The input values are sorted according to code size as shown in Figure K.4. HUFFVAL is the list containing the input values associated with each code word, in order of increasing code length.

At this point, the list of code lengths (BITS) and the list of values (HUFFVAL) can be used to generate the code tables. These procedures are described in Annex C.


Figure K. 4 - Sorting of input values according to code size

## K. 3 Typical Huffman tables for 8-bit precision luminance and chrominance

Huffman table-specification syntax is specified in B.2.4.2.

## K.3.1 Typical Huffman tables for the DC coefficient differences

Tables K. 3 and K. 4 give Huffman tables for the DC coefficient differences which have been developed from the average statistics of a large set of video images with 8 -bit precision. Table K. 3 is appropriate for luminance components and Table K. 4 is appropriate for chrominance components. Although there are no default tables, these tables may prove to be useful for many applications.

Table K. 3 - Table for luminance DC coefficient differences

| Category | Code length | Code word |
| :---: | :---: | :--- |
| 0 | 2 | 00 |
| 1 | 3 | 010 |
| 2 | 3 | 011 |
| 3 | 3 | 100 |
| 4 | 3 | 101 |
| 5 | 3 | 110 |
| 6 | 4 | 1110 |
| 7 | 5 | 11110 |
| 8 | 6 | 111110 |
| 9 | 7 | 1111110 |
| 10 | 8 | 11111110 |
| 11 | 9 | 111111110 |

Table K. 4 - Table for chrominance DC coefficient differences

| Category | Code length | Code word |
| :---: | :---: | :--- |
| 0 | 2 | 00 |
| 1 | 2 | 01 |
| 2 | 2 | 10 |
| 3 | 3 | 110 |
| 4 | 4 | 1110 |
| 5 | 5 | 11110 |
| 6 | 6 | 111110 |
| 7 | 7 | 1111110 |
| 8 | 8 | 11111110 |
| 9 | 9 | 111111110 |
| 10 | 10 | 1111111110 |
| 11 | 11 | 11111111110 |

## K.3.2 Typical Huffman tables for the AC coefficients

Tables K. 5 and K. 6 give Huffman tables for the AC coefficients which have been developed from the average statistics of a large set of images with 8 -bit precision. Table K. 5 is appropriate for luminance components and Table K. 6 is appropriate for chrominance components. Although there are no default tables, these tables may prove to be useful for many applications.

Table K. 5 - Table for luminance AC coefficients (sheet 1 of 4 )

| Run/Size | Code length | Code word |
| :---: | :---: | :---: |
| 0/0 (EOB) | 4 | 1010 |
| 0/1 | 2 | 00 |
| 0/2 | 2 | 01 |
| 0/3 | 3 | 100 |
| 0/4 | 4 | 1011 |
| 0/5 | 5 | 11010 |
| 0/6 | 7 | 1111000 |
| 0/7 | 8 | 11111000 |
| 0/8 | 10 | 1111110110 |
| 0/9 | 16 | 1111111110000010 |
| 0/A | 16 | 1111111110000011 |
| 1/1 | 4 | 1100 |
| 1/2 | 5 | 11011 |
| 1/3 | 7 | 1111001 |
| 1/4 | 9 | 111110110 |
| 1/5 | 11 | 11111110110 |
| 1/6 | 16 | 1111111110000100 |
| 1/7 | 16 | 1111111110000101 |
| 1/8 | 16 | 1111111110000110 |
| 1/9 | 16 | 1111111110000111 |
| 1/A | 16 | 1111111110001000 |
| 2/1 | 5 | 11100 |
| 2/2 | 8 | 11111001 |
| 2/3 | 10 | 1111110111 |
| 2/4 | 12 | 111111110100 |
| 2/5 | 16 | 1111111110001001 |
| 2/6 | 16 | 1111111110001010 |
| 2/7 | 16 | 1111111110001011 |
| 2/8 | 16 | 1111111110001100 |
| 2/9 | 16 | 1111111110001101 |
| 2/A | 16 | 1111111110001110 |
| 3/1 | 6 | 111010 |
| 3/2 | 9 | 111110111 |
| 3/3 | 12 | 111111110101 |
| 3/4 | 16 | 1111111110001111 |
| 3/5 | 16 | 1111111110010000 |
| 3/6 | 16 | 1111111110010001 |
| 3/7 | 16 | 1111111110010010 |
| 3/8 | 16 | 1111111110010011 |
| 3/9 | 16 | 1111111110010100 |
| 3/A | 16 | 1111111110010101 |

Table K. 5 (sheet 2 of 4)

| Run/Size | Code length | Code word |
| :---: | :---: | :---: |
| 4/1 | 6 | 111011 |
| 4/2 | 10 | 1111111000 |
| 4/3 | 16 | 1111111110010110 |
| 4/4 | 16 | 1111111110010111 |
| 4/5 | 16 | 1111111110011000 |
| 4/6 | 16 | 1111111110011001 |
| 4/7 | 16 | 1111111110011010 |
| 4/8 | 16 | 1111111110011011 |
| 4/9 | 16 | 1111111110011100 |
| 4/A | 16 | 1111111110011101 |
| 5/1 | 7 | 1111010 |
| 5/2 | 11 | 11111110111 |
| 5/3 | 16 | 1111111110011110 |
| 5/4 | 16 | 1111111110011111 |
| 5/5 | 16 | 1111111110100000 |
| 5/6 | 16 | 1111111110100001 |
| 5/7 | 16 | 1111111110100010 |
| 5/8 | 16 | 1111111110100011 |
| 5/9 | 16 | 1111111110100100 |
| 5/A | 16 | 1111111110100101 |
| 6/1 | 7 | 1111011 |
| 6/2 | 12 | 111111110110 |
| 6/3 | 16 | 1111111110100110 |
| 6/4 | 16 | 1111111110100111 |
| 6/5 | 16 | 1111111110101000 |
| 6/6 | 16 | 1111111110101001 |
| 6/7 | 16 | 1111111110101010 |
| 6/8 | 16 | 1111111110101011 |
| 6/9 | 16 | 1111111110101100 |
| 6/A | 16 | 1111111110101101 |
| 7/1 | 8 | 11111010 |
| 7/2 | 12 | 111111110111 |
| 7/3 | 16 | 1111111110101110 |
| 7/4 | 16 | 1111111110101111 |
| 7/5 | 16 | 1111111110110000 |
| 7/6 | 16 | 1111111110110001 |
| 7/7 | 16 | 1111111110110010 |
| 7/8 | 16 | 1111111110110011 |
| 7/9 | 16 | 1111111110110100 |
| 7/A | 16 | 1111111110110101 |
| 8/1 | 9 | 111111000 |
| 8/2 | 15 | 111111111000000 |

Table K. 5 (sheet 3 of 4)

| Run/Size | Code length | Code word |
| :---: | :---: | :---: |
| 8/3 | 16 | 1111111110110110 |
| 8/4 | 16 | 1111111110110111 |
| 8/5 | 16 | 1111111110111000 |
| 8/6 | 16 | 1111111110111001 |
| 8/7 | 16 | 1111111110111010 |
| 8/8 | 16 | 1111111110111011 |
| 8/9 | 16 | 1111111110111100 |
| 8/A | 16 | 1111111110111101 |
| 9/1 | 9 | 111111001 |
| 9/2 | 16 | 1111111110111110 |
| 9/3 | 16 | 1111111110111111 |
| 9/4 | 16 | 1111111111000000 |
| 9/5 | 16 | 1111111111000001 |
| 9/6 | 16 | 1111111111000010 |
| 9/7 | 16 | 1111111111000011 |
| 9/8 | 16 | 1111111111000100 |
| 9/9 | 16 | 1111111111000101 |
| 9/A | 16 | 1111111111000110 |
| A/1 | 9 | 111111010 |
| A/2 | 16 | 1111111111000111 |
| A/3 | 16 | 1111111111001000 |
| A/4 | 16 | 1111111111001001 |
| A/5 | 16 | 1111111111001010 |
| A/6 | 16 | 1111111111001011 |
| A/7 | 16 | 1111111111001100 |
| A/8 | 16 | 1111111111001101 |
| A/9 | 16 | 1111111111001110 |
| A/A | 16 | 1111111111001111 |
| B/1 | 10 | 1111111001 |
| B/2 | 16 | 1111111111010000 |
| B/3 | 16 | 1111111111010001 |
| B/4 | 16 | 1111111111010010 |
| B/5 | 16 | 1111111111010011 |
| B/6 | 16 | 1111111111010100 |
| B/7 | 16 | 1111111111010101 |
| B/8 | 16 | 1111111111010110 |
| B/9 | 16 | 1111111111010111 |
| B/A | 16 | 1111111111011000 |
| C/1 | 10 | 1111111010 |
| C/2 | 16 | 1111111111011001 |
| C/3 | 16 | 1111111111011010 |
| C/4 | 16 | 1111111111011011 |

Table K. 5 (sheet 4 of 4)

| Run/Size | Code length | Code word |
| :---: | :---: | :---: |
| C/5 | 16 | 1111111111011100 |
| C/6 | 16 | 1111111111011101 |
| C/7 | 16 | 1111111111011110 |
| C/8 | 16 | 1111111111011111 |
| C/9 | 16 | 1111111111100000 |
| C/A | 16 | 1111111111100001 |
| D/1 | 11 | 11111111000 |
| D/2 | 16 | 1111111111100010 |
| D/3 | 16 | 1111111111100011 |
| D/4 | 16 | 1111111111100100 |
| D/5 | 16 | 1111111111100101 |
| D/6 | 16 | 1111111111100110 |
| D/7 | 16 | 1111111111100111 |
| D/8 | 16 | 1111111111101000 |
| D/9 | 16 | 1111111111101001 |
| D/A | 16 | 1111111111101010 |
| E/1 | 16 | 1111111111101011 |
| E/2 | 16 | 1111111111101100 |
| E/3 | 16 | 1111111111101101 |
| E/4 | 16 | 1111111111101110 |
| E/5 | 16 | 1111111111101111 |
| E/6 | 16 | 1111111111110000 |
| E/7 | 16 | 1111111111110001 |
| E/8 | 16 | 1111111111110010 |
| E/9 | 16 | 1111111111110011 |
| E/A | 16 | 1111111111110100 |
| F/0 (ZRL) | 11 | 11111111001 |
| F/1 | 16 | 1111111111110101 |
| F/2 | 16 | 1111111111110110 |
| F/3 | 16 | 1111111111110111 |
| F/4 | 16 | 1111111111111000 |
| F/5 | 16 | 1111111111111001 |
| F/6 | 16 | 1111111111111010 |
| F/7 | 16 | 1111111111111011 |
| F/8 | 16 | 1111111111111100 |
| F/9 | 16 | 1111111111111101 |
| F/A | 16 | 1111111111111110 |

Table K. 6 - Table for chrominance AC coefficients (sheet 1 of 4)

| Run/Size | Code length | Code word |
| :---: | :---: | :---: |
| 0/0 (EOB) | 2 | 00 |
| 0/1 | 2 | 01 |
| 0/2 | 3 | 100 |
| 0/3 | 4 | 1010 |
| 0/4 | 5 | 11000 |
| 0/5 | 5 | 11001 |
| 0/6 | 6 | 111000 |
| 0/7 | 7 | 1111000 |
| 0/8 | 9 | 111110100 |
| 0/9 | 10 | 1111110110 |
| 0/A | 12 | 111111110100 |
| 1/1 | 4 | 1011 |
| 1/2 | 6 | 111001 |
| 1/3 | 8 | 11110110 |
| 1/4 | 9 | 111110101 |
| 1/5 | 11 | 11111110110 |
| 1/6 | 12 | 111111110101 |
| 1/7 | 16 | 1111111110001000 |
| 1/8 | 16 | 1111111110001001 |
| 1/9 | 16 | 1111111110001010 |
| 1/A | 16 | 1111111110001011 |
| 2/1 | 5 | 11010 |
| 2/2 | 8 | 11110111 |
| 2/3 | 10 | 1111110111 |
| 2/4 | 12 | 111111110110 |
| 2/5 | 15 | 111111111000010 |
| 2/6 | 16 | 1111111110001100 |
| 2/7 | 16 | 1111111110001101 |
| 2/8 | 16 | 1111111110001110 |
| 2/9 | 16 | 1111111110001111 |
| 2/A | 16 | 1111111110010000 |
| 3/1 | 5 | 11011 |
| $3 / 2$ | 8 | 11111000 |
| 3/3 | 10 | 1111111000 |
| 3/4 | 12 | 111111110111 |
| 3/5 | 16 | 1111111110010001 |
| 3/6 | 16 | 1111111110010010 |
| $3 / 7$ | 16 | 1111111110010011 |
| 3/8 | 16 | 1111111110010100 |
| 3/9 | 16 | 1111111110010101 |
| 3/A | 16 | 1111111110010110 |
| 4/1 | 6 | 111010 |

Table K. 6 (sheet 2 of 4)

| Run/Size | Code length | Code word |
| :---: | :---: | :---: |
| 4/2 | 9 | 111110110 |
| $4 / 3$ | 16 | 1111111110010111 |
| 4/4 | 16 | 1111111110011000 |
| 4/5 | 16 | 1111111110011001 |
| 4/6 | 16 | 1111111110011010 |
| 4/7 | 16 | 1111111110011011 |
| 4/8 | 16 | 1111111110011100 |
| 4/9 | 16 | 1111111110011101 |
| 4/A | 16 | 1111111110011110 |
| 5/1 | 6 | 111011 |
| 5/2 | 10 | 1111111001 |
| 5/3 | 16 | 1111111110011111 |
| 5/4 | 16 | 1111111110100000 |
| 5/5 | 16 | 1111111110100001 |
| 5/6 | 16 | 1111111110100010 |
| 5/7 | 16 | 1111111110100011 |
| 5/8 | 16 | 1111111110100100 |
| 5/9 | 16 | 1111111110100101 |
| 5/A | 16 | 1111111110100110 |
| 6/1 | 7 | 1111001 |
| 6/2 | 11 | 11111110111 |
| 6/3 | 16 | 1111111110100111 |
| 6/4 | 16 | 1111111110101000 |
| 6/5 | 16 | 1111111110101001 |
| 6/6 | 16 | 1111111110101010 |
| 6/7 | 16 | 1111111110101011 |
| 6/8 | 16 | 1111111110101100 |
| 6/9 | 16 | 1111111110101101 |
| 6/A | 16 | 1111111110101110 |
| 7/1 | 7 | 1111010 |
| 7/2 | 11 | 11111111000 |
| 7/3 | 16 | 1111111110101111 |
| $7 / 4$ | 16 | 1111111110110000 |
| 7/5 | 16 | 1111111110110001 |
| 7/6 | 16 | 1111111110110010 |
| 7/7 | 16 | 1111111110110011 |
| 7/8 | 16 | 1111111110110100 |
| 7/9 | 16 | 1111111110110101 |
| 7/A | 16 | 1111111110110110 |
| 8/1 | 8 | 11111001 |
| 8/2 | 16 | 1111111110110111 |
| 8/3 | 16 | 1111111110111000 |

Table K. 6 (sheet 3 of 4)

| Run/Size | Code length | Code word |
| :---: | :---: | :---: |
| 8/4 | 16 | 1111111110111001 |
| 8/5 | 16 | 1111111110111010 |
| 8/6 | 16 | 1111111110111011 |
| 8/7 | 16 | 1111111110111100 |
| 8/8 | 16 | 1111111110111101 |
| 8/9 | 16 | 1111111110111110 |
| 8/A | 16 | 1111111110111111 |
| 9/1 | 9 | 111110111 |
| 9/2 | 16 | 1111111111000000 |
| 9/3 | 16 | 1111111111000001 |
| 9/4 | 16 | 1111111111000010 |
| 9/5 | 16 | 1111111111000011 |
| 9/6 | 16 | 1111111111000100 |
| 9/7 | 16 | 1111111111000101 |
| 9/8 | 16 | 1111111111000110 |
| 9/9 | 16 | 1111111111000111 |
| 9/A | 16 | 1111111111001000 |
| A/1 | 9 | 111111000 |
| A/2 | 16 | 1111111111001001 |
| A/3 | 16 | 1111111111001010 |
| A/4 | 16 | 1111111111001011 |
| A/5 | 16 | 1111111111001100 |
| A/6 | 16 | 1111111111001101 |
| A/7 | 16 | 1111111111001110 |
| A/8 | 16 | 1111111111001111 |
| A/9 | 16 | 1111111111010000 |
| A/A | 16 | 1111111111010001 |
| B/1 | 9 | 111111001 |
| B/2 | 16 | 1111111111010010 |
| B/3 | 16 | 1111111111010011 |
| B/4 | 16 | 1111111111010100 |
| B/5 | 16 | 1111111111010101 |
| B/6 | 16 | 1111111111010110 |
| B/7 | 16 | 1111111111010111 |
| B/8 | 16 | 1111111111011000 |
| B/9 | 16 | 1111111111011001 |
| B/A | 16 | 1111111111011010 |
| C/1 | 9 | 111111010 |
| C/2 | 16 | 1111111111011011 |
| C/3 | 16 | 1111111111011100 |
| C/4 | 16 | 1111111111011101 |
| C/5 | 16 | 1111111111011110 |

Table K. 6 (sheet 4 of 4)

| Run/Size | Code length | Code word |
| :---: | :---: | :---: |
| C/6 | 16 | 1111111111011111 |
| C/7 | 16 | 1111111111100000 |
| C/8 | 16 | 1111111111100001 |
| C/9 | 16 | 1111111111100010 |
| C/A | 16 | 1111111111100011 |
| D/1 | 11 | 11111111001 |
| D/2 | 16 | 1111111111100100 |
| D/3 | 16 | 1111111111100101 |
| D/4 | 16 | 1111111111100110 |
| D/5 | 16 | 1111111111100111 |
| D/6 | 16 | 1111111111101000 |
| D/7 | 16 | 1111111111101001 |
| D/8 | 16 | 1111111111101010 |
| D/9 | 16 | 1111111111101011 |
| D/A | 16 | 1111111111101100 |
| E/1 | 14 | 11111111100000 |
| E/2 | 16 | 1111111111101101 |
| E/3 | 16 | 1111111111101110 |
| E/4 | 16 | 1111111111101111 |
| E/5 | 16 | 1111111111110000 |
| E/6 | 16 | 1111111111110001 |
| E/7 | 16 | 1111111111110010 |
| E/8 | 16 | 1111111111110011 |
| E/9 | 16 | 1111111111110100 |
| E/A | 16 | 1111111111110101 |
| F/0 (ZRL) | 10 | 1111111010 |
| F/1 | 15 | 111111111000011 |
| F/2 | 16 | 1111111111110110 |
| F/3 | 16 | 1111111111110111 |
| F/4 | 16 | 1111111111111000 |
| F/5 | 16 | 1111111111111001 |
| F/6 | 16 | 1111111111111010 |
| F/7 | 16 | 1111111111111011 |
| F/8 | 16 | 1111111111111100 |
| F/9 | 16 | 1111111111111101 |
| F/A | 16 | 1111111111111110 |

## K.3.3 Huffman table-specification examples

## K.3.3.1 Specification of typical tables for DC difference coding

A set of typical tables for DC component coding is given in K.3.1. The specification of these tables is as follows:

For Table K. 3 (for luminance DC coefficients), the 16 bytes which specify the list of code lengths for the table are

$$
\begin{array}{llllllllllllllll}
X^{\prime} 00 & 01 & 05 & 01 & 01 & 01 & 01 & 01 & 01 & 00 & 00 & 00 & 00 & 00 & 00 & 00
\end{array}
$$

The set of values following this list is

$$
\begin{array}{llllllllllll}
X^{\prime} 00 & 01 & 02 & 03 & 04 & 05 & 06 & 07 & 08 & 09 & 0 A & 0 B
\end{array}
$$

For Table K. 4 (for chrominance DC coefficients), the 16 bytes which specify the list of code lengths for the table are

```
X'00
```

The set of values following this list is

$$
\begin{array}{llllllllllll}
X^{\prime} & 00 & 01 & 02 & 03 & 04 & 05 & 06 & 07 & 08 & 09 & 0 A \\
0
\end{array}
$$

## K.3.3.2 Specification of typical tables for AC coefficient coding

A set of typical tables for AC component coding is given in K.3.2. The specification of these tables is as follows:

For Table K. 5 (for luminance AC coefficients), the 16 bytes which specify the list of code lengths for the table are

$$
\begin{array}{llllllllllllllll}
X^{\prime} 00 & 02 & 01 & 03 & 03 & 02 & 04 & 03 & 05 & 05 & 04 & 04 & 00 & 00 & 01 & 7 D^{\prime}
\end{array}
$$

The set of values which follows this list is

| X'01 | 02 | 03 | 00 | 04 | 11 | 05 | 12 | 21 | 31 | 41 | 06 | 13 | 51 | 61 | 07 |
| ---: | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 22 | 71 | 14 | 32 | 81 | 91 | A1 | 08 | 23 | 42 | B1 | C1 | 15 | 52 | D1 | F0 |
| 24 | 33 | 62 | 72 | 82 | 09 | $0 A$ | 16 | 17 | 18 | 19 | $1 A$ | 25 | 26 | 27 | 28 |
| 29 | $2 A$ | 34 | 35 | 36 | 37 | 38 | 39 | $3 A$ | 43 | 44 | 45 | 46 | 47 | 48 | 49 |
| $4 A$ | 53 | 54 | 55 | 56 | 57 | 58 | 59 | $5 A$ | 63 | 64 | 65 | 66 | 67 | 68 | 69 |
| 6A | 73 | 74 | 75 | 76 | 77 | 78 | 79 | $7 A$ | 83 | 84 | 85 | 86 | 87 | 88 | 89 |
| 8A | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | $9 A$ | A2 | A3 | A4 | A5 | A6 | A7 |
| A8 | A9 | AA | B2 | B3 | B4 | B5 | B6 | B7 | B8 | B9 | BA | C2 | C3 | C4 | C5 |
| C6 | C7 | C8 | C9 | CA | D2 | D3 | D4 | D5 | D6 | D7 | D8 | D9 | DA | E1 | E2 |
| E3 | E4 | E5 | E6 | E7 | E8 | E9 | EA | F1 | F2 | F3 | F4 | F5 | F6 | F7 | F8 |
| F9 | FA |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

For Table K. 6 (for chrominance AC coefficients), the 16 bytes which specify the list of code lengths for the table are
$\mathrm{X}^{\prime} 00030201$

The set of values which follows this list is:

| X'00 | 01 | 02 | 03 | 11 | 04 | 05 | 21 | 31 | 06 | 12 | 41 | 51 | 07 | 61 | 71 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 13 | 22 | 32 | 81 | 08 | 14 | 42 | 91 | A1 | B1 | C1 | 09 | 23 | 33 | 52 | F0 |
| 15 | 62 | 72 | D1 | 0 A | 16 | 24 | 34 | E1 | 25 | F1 | 17 | 18 | 19 | 1A | 26 |
| 27 | 28 | 29 | 2A | 35 | 36 | 37 | 38 | 39 | 3 A | 43 | 44 | 45 | 46 | 47 | 48 |
| 49 | 4A | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 5A | 63 | 64 | 65 | 66 | 67 | 68 |
| 69 | 6A | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 7A | 82 | 83 | 84 | 85 | 86 | 87 |
| 88 | 89 | 8A | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 9A | A2 | A3 | A4 | A5 |
| A6 | A7 | A8 | A9 | AA | B2 | B3 | B4 | B5 | B6 | B7 | B8 | B9 | BA | C2 | C3 |
| C4 | C5 | C6 | C7 | C8 | C9 | CA | D2 | D3 | D4 | D5 | D6 | D7 | D8 | D9 | DA |
| E2 | E3 | E4 | E5 | E6 | E7 | E8 | E9 | EA | F2 | F3 | F4 | F5 | F6 | F7 | F8 |
| F9 | FA' |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

## K. 4 Additional information on arithmetic coding

## K.4.1 Test sequence for a small data set for the arithmetic coder

The following 256-bit test sequence (in hexadecimal form) is structured to test many of the encoder and decoder paths:
$X^{\prime} 00020051 \quad 000000 \mathrm{C} 0 \quad 0352872 \mathrm{~A}$ AAAAAAAA 82C02000 FCD79EF6 74EAABF7 697EE74C’
Tables K. 7 and K. 8 provide a symbol-by-symbol list of the arithmetic encoder and decoder operation. In these tables the event count, EC, is listed first, followed by the value of Qe used in encoding and decoding that event. The decision D to be encoded (and decoded) is listed next. The column labeled MPS contains the sense of the MPS, and if it is followed by a CE (in the "CX" column), the conditional MPS/LPS exchange occurs when encoding and decoding the decision (see Figures D.3, D. 4 and D.17). The contents of the A and C registers are the values before the event is encoded and decoded. ST is the number of X'FF' bytes stacked in the encoder waiting for a resolution of the carry-over. Note that the A register is always greater than $\mathrm{X}^{\prime} 7 \mathrm{FFF}{ }^{\prime}$. (The starting value has an implied value of $\mathrm{X}^{\prime} 10000^{\prime}$.)

In the encoder test, the code bytes (B) are listed if they were completed during the coding of the preceding event. If additional bytes follow, they were also completed during the coding of the preceding event. If a byte is listed in the Bx column, the preceding byte in column $B$ was modified by a carry-over.

In the decoder the code bytes are listed if they were placed in the code register just prior to the event EC.
For this file the coded bit count is 240 , including the overhead to flush the final data from the C register. When the marker X'FFD9' is appended, a total of 256 bits are output. The actual compressed data sequence for the encoder is (in hexadecimal form)

Table K. 7 - Encoder test sequence (sheet 1 of 7)

| EC | D | MPS | CX | $\begin{gathered} \mathrm{Qe} \\ \text { (hexadecimal) } \end{gathered}$ | $\underset{\text { (hexadecimal) }}{\mathrm{A}}$ | $\begin{gathered} \mathrm{C} \\ \text { (hexadecimal) } \end{gathered}$ | CT | ST | Bx | B |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0 | 0 |  | 5A1D | 0000 | 00000000 | 11 | 0 |  |  |
| 2 | 0 | 0 | CE | 5A1D | A5E3 | 00000000 | 11 | 0 |  |  |
| 3 | 0 | 0 |  | 2586 | B43A | 0000978C | 10 | 0 |  |  |
| 4 | 0 | 0 |  | 2586 | 8EB4 | 0000978C | 10 | 0 |  |  |
| 5 | 0 | 0 |  | 1114 | D25C | 00012F18 | 9 | 0 |  |  |
| 6 | 0 | 0 |  | 1114 | C148 | 00012F18 | 9 | 0 |  |  |
| 7 | 0 | 0 |  | 1114 | B034 | 00012F18 | 9 | 0 |  |  |
| 8 | 0 | 0 |  | 1114 | 9F20 | 00012F18 | 9 | 0 |  |  |
| 9 | 0 | 0 |  | 1114 | 8 EOC | 00012F18 | 9 | 0 |  |  |
| 10 | 0 | 0 |  | 080B | F9F0 | 00025E30 | 8 | 0 |  |  |
| 11 | 0 | 0 |  | 080B | F1E5 | 00025E30 | 8 | 0 |  |  |
| 12 | 0 | 0 |  | 080B | E9DA | 00025E30 | 8 | 0 |  |  |
| 13 | 0 | 0 |  | 080B | E1CF | 00025E30 | 8 | 0 |  |  |
| 14 | 0 | 0 |  | 080B | D9C4 | 00025E30 | 8 | 0 |  |  |
| 15 | 1 | 0 |  | 080B | D1B9 | 00025E30 | 8 | 0 |  |  |
| 16 | 0 | 0 |  | 17B9 | 80B0 | 00327DE0 | 4 | 0 |  |  |
| 17 | 0 | 0 |  | 1182 | D1EE | 0064FBC0 | 3 | 0 |  |  |
| 18 | 0 | 0 |  | 1182 | C06C | 0064FBC0 | 3 | 0 |  |  |
| 19 | 0 | 0 |  | 1182 | AEEA | 0064FBC0 | 3 | 0 |  |  |
| 20 | 0 | 0 |  | 1182 | 9D68 | 0064FBC0 | 3 | 0 |  |  |
| 21 | 0 | 0 |  | 1182 | 8BE6 | 0064FBC0 | 3 | 0 |  |  |
| 22 | 0 | 0 |  | OCEF | F4C8 | 00 C 9 F 780 | 2 | 0 |  |  |
| 23 | 0 | 0 |  | OCEF | E7D9 | 00C9F780 | 2 | 0 |  |  |
| 24 | 0 | 0 |  | OCEF | DAEA | 00C9F780 | 2 | 0 |  |  |
| 25 | 0 | 0 |  | OCEF | CDFB | 00C9F780 | 2 | 0 |  |  |
| 26 | 1 | 0 |  | OCEF | C10C | 00C9F780 | 2 | 0 |  |  |
| 27 | 0 | 0 |  | 1518 | CEF0 | 000AB9D0 | 6 | 0 |  | 65 |
| 28 | 1 | 0 |  | 1518 | B9D8 | 000AB9D0 | 6 | 0 |  |  |
| 29 | 0 | 0 |  | 1 AA 9 | A8C0 | 005AF480 | 3 | 0 |  |  |
| 30 | 0 | 0 |  | 1AA9 | 8E17 | 005AF480 | 3 | 0 |  |  |
| 31 | 0 | 0 |  | 174E | E6DC | 00B5E900 | 2 | 0 |  |  |
| 32 | 1 | 0 |  | 174E | CF8E | 00B5E900 | 2 | 0 |  |  |
| 33 | 0 | 0 |  | 1 AA 9 | BA70 | 00050A00 | 7 | 0 |  | 5B |
| 34 | 0 | 0 |  | 1AA9 | 9 FC 7 | 00050A00 | 7 | 0 |  |  |
| 35 | 0 | 0 |  | 1AA9 | 851E | 00050A00 | 7 | 0 |  |  |
| 36 | 0 | 0 |  | 174E | D4EA | 000A1400 | 6 | 0 |  |  |

Table K. 7 - Encoder test sequence (sheet 2 of 7)

| EC | D | MPS | CX | $\begin{gathered} \mathrm{Qe} \\ \text { (hexadecimal) } \end{gathered}$ | A (hexadecimal) | $\underset{\text { (hexadecimal) }}{\mathrm{C}}$ | CT | ST | Bx | B |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 37 | 0 | 0 |  | 174E | BD9C | 000A1400 | 6 | 0 |  |  |
| 38 | 0 | 0 |  | 174 E | A64E | 000A1400 | 6 | 0 |  |  |
| 39 | 0 | 0 |  | 174 E | 8F00 | 000A1400 | 6 | 0 |  |  |
| 40 | 0 | 0 |  | 1424 | EF64 | 00142800 | 5 | 0 |  |  |
| 41 | 0 | 0 |  | 1424 | DB40 | 00142800 | 5 | 0 |  |  |
| 42 | 0 | 0 |  | 1424 | C71C | 00142800 | 5 | 0 |  |  |
| 43 | 0 | 0 |  | 1424 | B2F8 | 00142800 | 5 | 0 |  |  |
| 44 | 0 | 0 |  | 1424 | 9ED4 | 00142800 | 5 | 0 |  |  |
| 45 | 0 | 0 |  | 1424 | 8AB0 | 00142800 | 5 | 0 |  |  |
| 46 | 0 | 0 |  | 119C | ED18 | 00285000 | 4 | 0 |  |  |
| 47 | 0 | 0 |  | 119C | DB7C | 00285000 | 4 | 0 |  |  |
| 48 | 0 | 0 |  | 119C | C9E0 | 00285000 | 4 | 0 |  |  |
| 49 | 0 | 0 |  | 119C | B844 | 00285000 | 4 | 0 |  |  |
| 50 | 0 | 0 |  | 119C | A6A8 | 00285000 | 4 | 0 |  |  |
| 51 | 0 | 0 |  | 119C | 950 C | 00285000 | 4 | 0 |  |  |
| 52 | 0 | 0 |  | 119C | 8370 | 00285000 | 4 | 0 |  |  |
| 53 | 0 | 0 |  | 0F6B | E3A8 | 0050A000 | 3 | 0 |  |  |
| 54 | 0 | 0 |  | 0F6B | D43D | 0050A000 | 3 | 0 |  |  |
| 55 | 0 | 0 |  | 0F6B | C4D2 | 0050A000 | 3 | 0 |  |  |
| 56 | 0 | 0 |  | 0F6B | B567 | 0050A000 | 3 | 0 |  |  |
| 57 | 1 | 0 |  | 0F6B | A5FC | 0050A000 | 3 | 0 |  |  |
| 58 | 1 | 0 |  | 1424 | F6B0 | 00036910 | 7 | 0 |  | 51 |
| 59 | 0 | 0 |  | 1 AA 9 | A120 | 00225CE0 | 4 | 0 |  |  |
| 60 | 0 | 0 |  | 1AA9 | 8677 | 00225CE0 | 4 | 0 |  |  |
| 61 | 0 | 0 |  | 174 E | D79C | 0044B9C0 | 3 | 0 |  |  |
| 62 | 0 | 0 |  | 174 E | C04E | 0044B9C0 | 3 | 0 |  |  |
| 63 | 0 | 0 |  | 174 E | A900 | 0044B9C0 | 3 | 0 |  |  |
| 64 | 0 | 0 |  | 174 E | 91B2 | 0044B9C0 | 3 | 0 |  |  |
| 65 | 0 | 0 |  | 1424 | F4C8 | 00897380 | 2 | 0 |  |  |
| 66 | 0 | 0 |  | 1424 | E0A4 | 00897380 | 2 | 0 |  |  |
| 67 | 0 | 0 |  | 1424 | CC80 | 00897380 | 2 | 0 |  |  |
| 68 | 0 | 0 |  | 1424 | B85C | 00897380 | 2 | 0 |  |  |
| 69 | 0 | 0 |  | 1424 | A438 | 00897380 | 2 | 0 |  |  |
| 70 | 0 | 0 |  | 1424 | 9014 | 00897380 | 2 | 0 |  |  |
| 71 | 1 | 0 |  | 119C | F7E0 | 0112E700 | 1 | 0 |  |  |
| 72 | 1 | 0 |  | 1424 | 8CE0 | 001E6A20 | 6 | 0 |  | 44 |
| 73 | 0 | 0 |  | 1AA9 | A120 | 00F716E0 | 3 | 0 |  |  |

Table K. 7 - Encoder test sequence (sheet 3 of 7)

| EC | D | MPS | CX | $\begin{gathered} \mathrm{Qe} \\ \text { (hexadecimal) } \end{gathered}$ | A (hexadecimal) | C (hexadecimal) | CT | ST | Bx | B |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 74 | 1 | 0 |  | 1AA9 | 8677 | 00F716E0 | 3 | 0 |  |  |
| 75 | 0 | 0 |  | 2516 | D548 | 00041570 | 8 | 0 |  | F7 |
| 76 | 1 | 0 |  | 2516 | B032 | 00041570 | 8 | 0 |  |  |
| 77 | 0 | 0 |  | 299A | 9458 | 00128230 | 6 | 0 |  |  |
| 78 | 0 | 0 |  | 2516 | D57C | 00250460 | 5 | 0 |  |  |
| 79 | 1 | 0 |  | 2516 | B066 | 00250460 | 5 | 0 |  |  |
| 80 | 0 | 0 |  | 299A | 9458 | 00963EC0 | 3 | 0 |  |  |
| 81 | 1 | 0 |  | 2516 | D57C | 012C7D80 | 2 | 0 |  |  |
| 82 | 0 | 0 |  | 299A | 9458 | 0004B798 | 8 | 0 |  | 96 |
| 83 | 0 | 0 |  | 2516 | D57C | 00096F30 | 7 | 0 |  |  |
| 84 | 0 | 0 |  | 2516 | B066 | 00096F30 | 7 | 0 |  |  |
| 85 | 0 | 0 |  | 2516 | 8B50 | 00096F30 | 7 | 0 |  |  |
| 86 | 1 | 0 |  | 1EDF | CC74 | 0012DE60 | 6 | 0 |  |  |
| 87 | 1 | 0 |  | 2516 | F6F8 | 009C5FA8 | 3 | 0 |  |  |
| 88 | 1 | 0 |  | 299A | 9458 | 0274C628 | 1 | 0 |  |  |
| 89 | 0 | 0 |  | 32B4 | A668 | 0004C398 | 7 | 0 |  | 9D |
| 90 | 0 | 0 |  | 2E17 | E768 | 00098730 | 6 | 0 |  |  |
| 91 | 1 | 0 |  | 2E17 | B951 | 00098730 | 6 | 0 |  |  |
| 92 | 0 | 0 |  | 32B4 | B85C | 002849A8 | 4 | 0 |  |  |
| 93 | 1 | 0 |  | 32B4 | 85A8 | 002849A8 | 4 | 0 |  |  |
| 94 | 0 | 0 |  | 3C3D | CAD0 | 00A27270 | 2 | 0 |  |  |
| 95 | 1 | 0 |  | 3C3D | 8E93 | 00A27270 | 2 | 0 |  |  |
| 96 | 0 | 0 |  | 415 E | F0F4 | 00031318 | 8 | 0 |  | 51 |
| 97 | 1 | 0 |  | 415 E | AF96 | 00031318 | 8 | 0 |  |  |
| 98 | 0 | 0 | CE | 4639 | 82BC | 000702A0 | 7 | 0 |  |  |
| 99 | 1 | 0 |  | 415E | 8C72 | 000E7E46 | 6 | 0 |  |  |
| 100 | 0 | 0 | CE | 4639 | 82BC | 001D92B4 | 5 | 0 |  |  |
| 101 | 1 | 0 |  | 415 E | 8C72 | 003B9E6E | 4 | 0 |  |  |
| 102 | 0 | 0 | CE | 4639 | 82BC | 0077D304 | 3 | 0 |  |  |
| 103 | 1 | 0 |  | 415 E | 8 C 72 | 00F01F0E | 2 | 0 |  |  |
| 104 | 0 | 0 | CE | 4639 | 82BC | 01E0D444 | 1 | 0 |  |  |
| 105 | 1 | 0 |  | 415 E | 8C72 | 0002218 E | 8 | 0 |  | 78 |
| 106 | 0 | 0 | CE | 4639 | 82BC | 0004D944 | 7 | 0 |  |  |
| 107 | 1 | 0 |  | 415 E | 8C72 | 000A2B8E | 6 | 0 |  |  |
| 108 | 0 | 0 | CE | 4639 | 82BC | 0014ED44 | 5 | 0 |  |  |
| 109 | 1 | 0 |  | 415E | 8C72 | 002A538E | 4 | 0 |  |  |
| 110 | 0 | 0 | CE | 4639 | 82BC | 00553D44 | 3 | 0 |  |  |

Table K. 7 - Encoder test sequence (sheet 4 of 7)

| EC | D | MPS | CX | $\begin{gathered} \mathrm{Qe} \\ \text { (hexadecimal) } \end{gathered}$ | A (hexadecimal) | C <br> (hexadecimal) | CT | ST | Bx | B |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 111 | 1 | 0 |  | 415 E | 8C72 | 00AAF38E | 2 | 0 |  |  |
| 112 | 0 | 0 | CE | 4639 | 82 BC | 01567D44 | 1 | 0 |  |  |
| 113 | 1 | 0 |  | 415E | 8C72 | 0005738E | 8 | 0 |  | 55 |
| 114 | 0 | 0 | CE | 4639 | 82BC | 000B7D44 | 7 | 0 |  |  |
| 115 | 1 | 0 |  | 415E | 8C72 | 0017738 E | 6 | 0 |  |  |
| 116 | 0 | 0 | CE | 4639 | 82BC | 002F7D44 | 5 | 0 |  |  |
| 117 | 1 | 0 |  | 415E | 8 C 72 | 005F738E | 4 | 0 |  |  |
| 118 | 0 | 0 | CE | 4639 | 82BC | 00BF7D44 | 3 | 0 |  |  |
| 119 | 1 | 0 |  | 415E | 8C72 | 017F738E | 2 | 0 |  |  |
| 120 | 0 | 0 | CE | 4639 | 82BC | 02FF7D44 | 1 | 0 |  |  |
| 121 | 1 | 0 |  | 415E | 8C72 | 0007738E | 8 | 0 |  | BF |
| 122 | 0 | 0 | CE | 4639 | 82 BC | 000F7D44 | 7 | 0 |  |  |
| 123 | 1 | 0 |  | 415E | 8 C 72 | 001F738E | 6 | 0 |  |  |
| 124 | 0 | 0 | CE | 4639 | 82BC | 003F7D44 | 5 | 0 |  |  |
| 125 | 1 | 0 |  | 415E | 8C72 | 007F738E | 4 | 0 |  |  |
| 126 | 0 | 0 | CE | 4639 | 82BC | 00FF7D44 | 3 | 0 |  |  |
| 127 | 1 | 0 |  | 415 E | 8 C 72 | 01FF738E | 2 | 0 |  |  |
| 128 | 0 | 0 | CE | 4639 | 82BC | 03FF7D44 | 1 | 0 |  |  |
| 129 | 1 | 0 |  | 415 E | 8 C 72 | 0007738 E | 8 | 1 |  |  |
| 130 | 0 | 0 | CE | 4639 | 82BC | 000F7D44 | 7 | 1 |  |  |
| 131 | 0 | 0 |  | 415E | 8 C 72 | 001F738E | 6 | 1 |  |  |
| 132 | 0 | 0 |  | 3C3D | 9628 | 003EE71C | 5 | 1 |  |  |
| 133 | 0 | 0 |  | 375E | B3D6 | 007DCE38 | 4 | 1 |  |  |
| 134 | 0 | 0 |  | 32B4 | F8F0 | 00FB9C70 | 3 | 1 |  |  |
| 135 | 1 | 0 |  | 32B4 | C63C | 00FB9C70 | 3 | 1 |  |  |
| 136 | 0 | 0 |  | 3C3D | CAD0 | 03F0BFE0 | 1 | 1 |  |  |
| 137 | 1 | 0 |  | 3 C 3 D | 8E93 | 03F0BFE0 | 1 | 1 |  |  |
| 138 | 1 | 0 |  | 415 E | F0F4 | 000448D8 | 7 | 0 |  | FF00FC |
| 139 | 0 | 0 | CE | 4639 | 82 BC | 0009F0DC | 6 | 0 |  |  |
| 140 | 0 | 0 |  | 415 E | 8 C 72 | 00145ABE | 5 | 0 |  |  |
| 141 | 0 | 0 |  | 3C3D | 9628 | 0028B57C | 4 | 0 |  |  |
| 142 | 0 | 0 |  | 375 E | B3D6 | 00516AF8 | 3 | 0 |  |  |
| 143 | 0 | 0 |  | 32B4 | F8F0 | 00A2D5F0 | 2 | 0 |  |  |
| 144 | 0 | 0 |  | 32B4 | C63C | 00A2D5F0 | 2 | 0 |  |  |
| 145 | 0 | 0 |  | 32B4 | 9388 | 00A2D5F0 | 2 | 0 |  |  |
| 146 | 0 | 0 |  | 2E17 | C1A8 | 0145ABE0 | 1 | 0 |  |  |

Table K. 7 - Encoder test sequence (sheet 5 of 7)

| EC | D | MPS | CX | $\begin{gathered} \mathrm{Qe} \\ \text { (hexadecimal) } \end{gathered}$ | $\begin{gathered} \mathrm{A} \\ \text { (hexadecimal) } \end{gathered}$ | $\begin{gathered} \mathrm{C} \\ \text { (hexadecimal) } \end{gathered}$ | CT | ST | Bx | B |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 147 | 1 | 0 |  | 2E17 | 9391 | 0145ABE0 | 1 | 0 |  |  |
| 148 | 0 | 0 |  | 32B4 | B85C | 00084568 | 7 | 0 |  | 51 |
| 149 | 0 | 0 |  | 32B4 | 85A8 | 00084568 | 7 | 0 |  |  |
| 150 | 0 | 0 |  | 2E17 | A5E8 | 00108AD0 | 6 | 0 |  |  |
| 151 | 0 | 0 |  | 299A | EFA2 | 002115A0 | 5 | 0 |  |  |
| 152 | 0 | 0 |  | 299A | C608 | 002115A0 | 5 | 0 |  |  |
| 153 | 0 | 0 |  | 299A | 9C6E | 002115A0 | 5 | 0 |  |  |
| 154 | 0 | 0 |  | 2516 | E5A8 | 00422B40 | 4 | 0 |  |  |
| 155 | 0 | 0 |  | 2516 | C092 | 00422B40 | 4 | 0 |  |  |
| 156 | 0 | 0 |  | 2516 | 9B7C | 00422B40 | 4 | 0 |  |  |
| 157 | 0 | 0 |  | 1EDF | ECCC | 00845680 | 3 | 0 |  |  |
| 158 | 0 | 0 |  | 1EDF | CDED | 00845680 | 3 | 0 |  |  |
| 159 | 0 | 0 |  | 1EDF | AFOE | 00845680 | 3 | 0 |  |  |
| 160 | 0 | 0 |  | 1EDF | 902F | 00845680 | 3 | 0 |  |  |
| 161 | 1 | 0 |  | 1AA9 | E2A0 | 0108AD00 | 2 | 0 |  |  |
| 162 | 1 | 0 |  | 2516 | D548 | 000BA7B8 | 7 | 0 |  | 84 |
| 163 | 1 | 0 |  | 299A | 9458 | 00315FA8 | 5 | 0 |  |  |
| 164 | 1 | 0 |  | 32B4 | A668 | 00C72998 | 3 | 0 |  |  |
| 165 | 1 | 0 |  | 3 C 3 D | CAD0 | 031 E 7530 | 1 | 0 |  |  |
| 166 | 1 | 0 |  | 415E | F0F4 | 000C0F0C | 7 | 0 |  | C7 |
| 167 | 0 | 0 | CE | 4639 | 82 BC | 00197D44 | 6 | 0 |  |  |
| 168 | 0 | 0 |  | 415 E | 8 C 72 | 0033738E | 5 | 0 |  |  |
| 169 | 1 | 0 |  | 3C3D | 9628 | 0066E71C | 4 | 0 |  |  |
| 170 | 1 | 0 |  | 415E | F0F4 | 019D041C | 2 | 0 |  |  |
| 171 | 0 | 0 | CE | 4639 | 82 BC | 033B6764 | 1 | 0 |  |  |
| 172 | 1 | 0 |  | 415E | 8C72 | 000747CE | 8 | 0 |  | CE |
| 173 | 0 | 0 | CE | 4639 | 82 BC | 000F25C4 | 7 | 0 |  |  |
| 174 | 1 | 0 |  | 415E | 8C72 | 001EC48E | 6 | 0 |  |  |
| 175 | 1 | 0 | CE | 4639 | 82 BC | 003E1F44 | 5 | 0 |  |  |
| 176 | 1 | 0 |  | 4B85 | F20C | 00F87D10 | 3 | 0 |  |  |
| 177 | 1 | 0 | CE | 504F | 970A | 01F2472E | 2 | 0 |  |  |
| 178 | 0 | 0 | CE | 5522 | 8D76 | 03E48E5C | 1 | 0 |  |  |
| 179 | 0 | 0 |  | 504F | AA44 | 00018D60 | 8 | 0 |  | F9 |
| 180 | 1 | 0 |  | 4B85 | B3EA | 00031AC0 | 7 | 0 |  |  |
| 181 | 1 | 0 | CE | 504F | 970A | 0007064A | 6 | 0 |  |  |
| 182 | 1 | 0 | CE | 5522 | 8D76 | 000E0C94 | 5 | 0 |  |  |
| 183 | 1 | 0 |  | 59EB | E150 | 00383250 | 3 | 0 |  |  |

Table K. 7 - Encoder test sequence (sheet 6 of 7)

| EC | D | MPS | CX | $\begin{gathered} \mathrm{Qe} \\ \text { (hexadecimal) } \end{gathered}$ | $\begin{gathered} \mathrm{A} \\ \text { (hexadecimal) } \end{gathered}$ | $\begin{gathered} \mathrm{C} \\ \text { (hexadecimal) } \end{gathered}$ | CT | ST | Bx | B |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 184 | 0 | 1 |  | 59 EB | B3D6 | 0071736A | 2 | 0 |  |  |
| 185 | 1 | 0 |  | 59 EB | B3D6 | 00E39AAA | 1 | 0 |  |  |
| 186 | 1 | 1 |  | 59EB | B3D6 | 0007E92A | 8 | 0 |  | 38 |
| 187 | 1 | 1 |  | 5522 | B3D6 | 000FD254 | 7 | 0 |  |  |
| 188 | 1 | 1 |  | 504F | BD68 | 001FA4A8 | 6 | 0 |  |  |
| 189 | 0 | 1 |  | 4B85 | DA32 | 003F4950 | 5 | 0 |  |  |
| 190 | 1 | 1 | CE | 504F | 970A | 007FAFFA | 4 | 0 |  |  |
| 191 | 1 | 1 |  | 4B85 | A09E | 00FFED6A | 3 | 0 |  |  |
| 192 | 0 | 1 |  | 4639 | AA32 | 01FFDAD4 | 2 | 0 |  |  |
| 193 | 0 | 1 | CE | 4B85 | 8C72 | 04007D9A | 1 | 0 |  |  |
| 194 | 1 | 1 | CE | 504F | 81DA | 0000FB34 | 8 | 0 | 39 | 00 |
| 195 | 1 | 1 |  | 4B85 | A09E | 0002597E | 7 | 0 |  |  |
| 196 | 1 | 1 |  | 4639 | AA32 | 0004B2FC | 6 | 0 |  |  |
| 197 | 0 | 1 |  | 415E | C7F2 | 000965F8 | 5 | 0 |  |  |
| 198 | 1 | 1 | CE | 4639 | 82 BC | 0013 D 918 | 4 | 0 |  |  |
| 199 | 0 | 1 |  | 415 E | 8C72 | 00282B36 | 3 | 0 |  |  |
| 200 | 0 | 1 | CE | 4639 | 82 BC | 0050EC94 | 2 | 0 |  |  |
| 201 | 1 | 1 |  | 4B85 | F20C | 0003B250 | 8 | 0 |  | 28 |
| 202 | 1 | 1 |  | 4B85 | A687 | 0003B250 | 8 | 0 |  |  |
| 203 | 1 | 1 |  | 4639 | B604 | 000764A0 | 7 | 0 |  |  |
| 204 | 0 | 1 |  | 415E | DF96 | 000EC940 | 6 | 0 |  |  |
| 205 | 1 | 1 | CE | 4639 | 82BC | 001ECEF0 | 5 | 0 |  |  |
| 206 | 0 | 1 |  | 415 E | 8 C 72 | 003E16E6 | 4 | 0 |  |  |
| 207 | 1 | 1 | CE | 4639 | 82 BC | 007CC3F4 | 3 | 0 |  |  |
| 208 | 0 | 1 |  | 415E | 8 C 72 | 00FA00EE | 2 | 0 |  |  |
| 209 | 1 | 1 | CE | 4639 | 82BC | 01F49804 | 1 | 0 |  |  |
| 210 | 0 | 1 |  | 415E | 8C72 | 0001A90E | 8 | 0 |  | 7D |
| 211 | 1 | 1 | CE | 4639 | 82 BC | 0003 E 844 | 7 | 0 |  |  |
| 212 | 0 | 1 |  | 415 E | 8 C 72 | 0008498E | 6 | 0 |  |  |
| 213 | 1 | 1 | CE | 4639 | 82 BC | 00112944 | 5 | 0 |  |  |
| 214 | 0 | 1 |  | 415E | 8 C 72 | 0022 CB 8 E | 4 | 0 |  |  |
| 215 | 1 | 1 | CE | 4639 | 82 BC | 00462D44 | 3 | 0 |  |  |
| 216 | 1 | 1 |  | 415 E | 8 C 72 | 008 CD 38 E | 2 | 0 |  |  |
| 217 | 1 | 1 |  | 3C3D | 9628 | 0119A71C | 1 | 0 |  |  |
| 218 | 1 | 1 |  | 375 E | B3D6 | 00034 E 38 | 8 | 0 |  | 46 |
| 219 | 1 | 1 |  | 32B4 | F8F0 | 00069 C 70 | 7 | 0 |  |  |
| 220 | 1 | 1 |  | 32B4 | C63C | 00069C70 | 7 | 0 |  |  |

Table K. 7 - Encoder test sequence (sheet 7 of 7)

| EC | D | MPS | CX | $\begin{gathered} \mathrm{Qe} \\ \text { (hexadecimal) } \end{gathered}$ | A (hexadecimal) | C (hexadecimal) | CT | ST | Bx | B |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 221 | 0 | 1 |  | 32B4 | 9388 | 00069C70 | 7 | 0 |  |  |
| 222 | 1 | 1 |  | 3C3D | CAD0 | 001 BF 510 | 5 | 0 |  |  |
| 223 | 1 | 1 |  | 3C3D | 8E93 | 001 BF 510 | 5 | 0 |  |  |
| 224 | 1 | 1 |  | 375E | A4AC | 0037EA20 | 4 | 0 |  |  |
| 225 | 0 | 1 |  | 32B4 | DA9C | 006FD440 | 3 | 0 |  |  |
| 226 | 1 | 1 |  | 3C3D | CAD0 | 01C1F0A0 | , | 0 |  |  |
| 227 | 1 | 1 |  | 3C3D | 8E93 | 01C1F0A0 | 1 | 0 |  |  |
| 228 | 0 | 1 |  | 375 E | A4AC | 0003E140 | 8 | 0 |  | 70 |
| 229 | 1 | 1 |  | 3C3D | DD78 | 00113A38 | 6 | 0 |  |  |
| 230 | 0 | 1 |  | 3C3D | A13B | 00113A38 | 6 | 0 |  |  |
| 231 | 0 | 1 |  | 415E | F0F4 | 00467CD8 | 4 | 0 |  |  |
| 232 | 1 | 1 | CE | 4639 | 82BC | 008E58DC | 3 | 0 |  |  |
| 233 | 0 | 1 |  | 415E | 8C72 | 011 D 2 ABE | 2 | 0 |  |  |
| 234 | 1 | 1 | CE | 4639 | 82 BC | 023AEBA4 | 1 | 0 |  |  |
| 235 | 1 | 1 |  | 415E | 8C72 | 0006504E | 8 | 0 |  | 8E |
| 236 | 1 | 1 |  | 3C3D | 9628 | 000CA09C | 7 | 0 |  |  |
| 237 | 1 | 1 |  | 375 E | B3D6 | 00194138 | 6 | 0 |  |  |
| 238 | 1 | 1 |  | 32B4 | F8F0 | 00328270 | 5 | 0 |  |  |
| 239 | 1 | 1 |  | 32B4 | C63C | 00328270 | 5 | 0 |  |  |
| 240 | 0 | 1 |  | 32B4 | 9388 | 00328270 | 5 | 0 |  |  |
| 241 | 1 | 1 |  | 3C3D | CAD0 | 00CB8D10 | 3 | 0 |  |  |
| 242 | 1 | 1 |  | 3 C 3 D | 8E93 | 00 CB 8 D 10 | 3 | 0 |  |  |
| 243 | 1 | 1 |  | 375 E | A4AC | 01971A20 | 2 | 0 |  |  |
| 244 | 0 | 1 |  | 32B4 | DA9C | 032E3440 | 1 | 0 |  |  |
| 245 | 0 | 1 |  | 3C3D | CAD0 | 000B70A0 | 7 | 0 |  | CB |
| 246 | 1 | 1 |  | 415 E | F0F4 | 002 FFCCC | 5 | 0 |  |  |
| 247 | 1 | 1 |  | 415 E | AF96 | 002FFCCC | 5 | 0 |  |  |
| 248 | 1 | 1 |  | 3C3D | DC70 | 005FF998 | 4 | 0 |  |  |
| 249 | 0 | 1 |  | 3C3D | A033 | 005FF998 | 4 | 0 |  |  |
| 250 | 1 | 1 |  | 415E | F0F4 | 01817638 | 2 | 0 |  |  |
| 251 | 0 | 1 |  | 415 E | AF96 | 01817638 | 2 | 0 |  |  |
| 252 | 0 | 1 | CE | 4639 | 82 BC | 0303C8E0 | 1 | 0 |  |  |
| 253 | 1 | 1 |  | 4B85 | F20C | 000F2380 | 7 | 0 |  | C0 |
| 254 | 1 | 1 |  | 4B85 | A687 | 000F2380 | 7 | 0 |  |  |
| 255 | 0 | 1 |  | 4639 | B604 | 001 E 4700 | 6 | 0 |  |  |
| 256 | 0 | 1 | CE | 4B85 | 8C72 | 003D6D96 | 5 | 0 |  |  |
| Flush: |  |  |  |  | 81DA | 007ADB2C | 4 | 0 |  | F6 |
|  |  |  |  |  |  |  |  |  |  | FFD9 |

Table K. 8 - Decoder test sequence (sheet 1 of 7)

| EC | D | MPS | CX | $\begin{gathered} \mathrm{Qe} \\ \text { (hexadecimal) } \end{gathered}$ | A (hexadecimal) | C <br> (hexadecimal) | CT | B |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0 | 0 |  | 5A1D | 0000 | 655B0000 | 0 | 65 5B |
| 2 | 0 | 0 | CE | 5A1D | A5E3 | 655B0000 | 0 |  |
| 3 | 0 | 0 |  | 2586 | B43A | 332AA200 | 7 | 51 |
| 4 | 0 | 0 |  | 2586 | 8EB4 | 332AA200 | 7 |  |
| 5 | 0 | 0 |  | 1114 | D25C | 66554400 | 6 |  |
| 6 | 0 | 0 |  | 1114 | C148 | 66554400 | 6 |  |
| 7 | 0 | 0 |  | 1114 | B034 | 66554400 | 6 |  |
| 8 | 0 | 0 |  | 1114 | 9F20 | 66554400 | 6 |  |
| 9 | 0 | 0 |  | 1114 | 8 EOC | 66554400 | 6 |  |
| 10 | 0 | 0 |  | 080B | F9F0 | CCAA8800 | 5 |  |
| 11 | 0 | 0 |  | 080B | F1E5 | CCAA8800 | 5 |  |
| 12 | 0 | 0 |  | 080B | E9DA | CCAA8800 | 5 |  |
| 13 | 0 | 0 |  | 080B | E1CF | CCAA8800 | 5 |  |
| 14 | 0 | 0 |  | 080B | D9C4 | CCAA8800 | 5 |  |
| 15 | 1 | 0 |  | 080B | D1B9 | CCAA8800 | 5 |  |
| 16 | 0 | 0 |  | 17B9 | 80B0 | 2FC88000 | 1 |  |
| 17 | 0 | 0 |  | 1182 | D1EE | 5F910000 | 0 |  |
| 18 | 0 | 0 |  | 1182 | C06C | 5F910000 | 0 |  |
| 19 | 0 | 0 |  | 1182 | AEEA | 5F910000 | 0 |  |
| 20 | 0 | 0 |  | 1182 | 9D68 | 5F910000 | 0 |  |
| 21 | 0 | 0 |  | 1182 | 8BE6 | 5F910000 | 0 |  |
| 22 | 0 | 0 |  | OCEF | F4C8 | BF228800 | 7 | 44 |
| 23 | 0 | 0 |  | OCEF | E7D9 | BF228800 | 7 |  |
| 24 | 0 | 0 |  | OCEF | DAEA | BF228800 | 7 |  |
| 25 | 0 | 0 |  | OCEF | CDFB | BF228800 | 7 |  |
| 26 | 1 | 0 |  | OCEF | C10C | BF228800 | 7 |  |
| 27 | 0 | 0 |  | 1518 | CEF0 | B0588000 | 3 |  |
| 28 | 1 | 0 |  | 1518 | B9D8 | B0588000 | 3 |  |
| 29 | 0 | 0 |  | 1AA9 | A8C0 | 5CC40000 | 0 |  |
| 30 | 0 | 0 |  | 1 AA 9 | 8E17 | 5 CC 40000 | 0 |  |
| 31 | 0 | 0 |  | 174E | E6DC | B989EE00 | 7 | F7 |
| 32 | 1 | 0 |  | 174 E | CF8E | B989EE00 | 7 |  |
| 33 | 0 | 0 |  | 1 AA 9 | BA70 | 0A4F7000 | 4 |  |
| 34 | 0 | 0 |  | 1 AA 9 | 9 FC 7 | 0A4F7000 | 4 |  |
| 35 | 0 | 0 |  | 1 AA 9 | 851E | 0A4F7000 | 4 |  |
| 36 | 0 | 0 |  | 174E | D4EA | 149EE000 | 3 |  |
| 37 | 0 | 0 |  | 174E | BD9C | 149EE000 | 3 |  |
| 38 | 0 | 0 |  | 174E | A64E | 149EE000 | 3 |  |
| 39 | 0 | 0 |  | 174 E | 8F00 | 149EE000 | 3 |  |
| 40 | 0 | 0 |  | 1424 | EF64 | 293DC000 | 2 |  |

Table K. 8 - Decoder test sequence (sheet 2 of 7)

| EC | D | MPS | CX | $\begin{gathered} \mathrm{Qe} \\ \text { (hexadecimal) } \end{gathered}$ | A (hexadecimal) | $\begin{gathered} \text { C } \\ \text { (hexadecimal) } \end{gathered}$ | CT | B |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 41 | 0 | 0 |  | 1424 | DB40 | 293DC000 | 2 |  |
| 42 | 0 | 0 |  | 1424 | C71C | 293DC000 | 2 |  |
| 43 | 0 | 0 |  | 1424 | B2F8 | 293DC000 | 2 |  |
| 44 | 0 | 0 |  | 1424 | 9ED4 | 293DC000 | 2 |  |
| 45 | 0 | 0 |  | 1424 | 8AB0 | 293DC000 | 2 |  |
| 46 | 0 | 0 |  | 119C | ED18 | 527B8000 | 1 |  |
| 47 | 0 | 0 |  | 119C | DB7C | 527B8000 | 1 |  |
| 48 | 0 | 0 |  | 119C | C9E0 | 527B8000 | 1 |  |
| 49 | 0 | 0 |  | 119C | B844 | 527B8000 | 1 |  |
| 50 | 0 | 0 |  | 119C | A6A8 | 527B8000 | 1 |  |
| 51 | 0 | 0 |  | 119C | 950 C | 527B8000 | 1 |  |
| 52 | 0 | 0 |  | 119C | 8370 | 527B8000 | 1 |  |
| 53 | 0 | 0 |  | 0F6B | E3A8 | A4F70000 | 0 |  |
| 54 | 0 | 0 |  | 0F6B | D43D | A4F70000 | 0 |  |
| 55 | 0 | 0 |  | 0F6B | C4D2 | A4F70000 | 0 |  |
| 56 | 0 | 0 |  | 0F6B | B567 | A4F70000 | 0 |  |
| 57 | 1 | 0 |  | 0F6B | A5FC | A4F70000 | 0 |  |
| 58 | 1 | 0 |  | 1424 | F6B0 | E6696000 | 4 | 96 |
| 59 | 0 | 0 |  | 1 AA 9 | A120 | 1 EEB0000 | 1 |  |
| 60 | 0 | 0 |  | 1 AA 9 | 8677 | 1 EEB0000 | 1 |  |
| 61 | 0 | 0 |  | 174E | D79C | 3DD60000 | 0 |  |
| 62 | 0 | 0 |  | 174E | C04E | 3DD60000 | 0 |  |
| 63 | 0 | 0 |  | 174 E | A900 | 3DD60000 | 0 |  |
| 64 | 0 | 0 |  | 174 E | 91 B 2 | 3DD60000 | 0 |  |
| 65 | 0 | 0 |  | 1424 | F4C8 | 7BAD3A00 | 7 | 9D |
| 66 | 0 | 0 |  | 1424 | E0A4 | 7BAD3A00 | 7 |  |
| 67 | 0 | 0 |  | 1424 | CC80 | 7BAD3A00 | 7 |  |
| 68 | 0 | 0 |  | 1424 | B85C | 7BAD3A00 | 7 |  |
| 69 | 0 | 0 |  | 1424 | A438 | 7BAD3A00 | 7 |  |
| 70 | 0 | 0 |  | 1424 | 9014 | 7BAD3A00 | 7 |  |
| 71 | 1 | 0 |  | 119C | F7E0 | F75A7400 | 6 |  |
| 72 | 1 | 0 |  | 1424 | 8CE0 | 88B3A000 | 3 |  |
| 73 | 0 | 0 |  | 1 AA 9 | A120 | 7FBD0000 | 0 |  |
| 74 | 1 | 0 |  | 1 AA 9 | 8677 | 7FBD0000 | 0 |  |
| 75 | 0 | 0 |  | 2516 | D548 | 9F7A8800 | 5 | 51 |
| 76 | 1 | 0 |  | 2516 | B032 | 9F7A8800 | 5 |  |
| 77 | 0 | 0 |  | 299A | 9458 | 517A2000 | 3 |  |
| 78 | 0 | 0 |  | 2516 | D57C | A2F44000 | 2 |  |
| 79 | 1 | 0 |  | 2516 | B066 | A2F44000 | 2 |  |
| 80 | 0 | 0 |  | 299A | 9458 | 5E910000 | 0 |  |

Table K. 8 - Decoder test sequence (sheet 3 of 7)

| EC | D | MPS | CX | Qe (hexadecimal) | A (hexadecimal) | C <br> (hexadecimal) | CT | B |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 81 | 1 | 0 |  | 2516 | D57C | BD22F000 | 7 | 78 |
| 82 | 0 | 0 |  | 299A | 9458 | 32F3C000 | 5 |  |
| 83 | 0 | 0 |  | 2516 | D57C | 65E78000 | 4 |  |
| 84 | 0 | 0 |  | 2516 | B066 | 65E78000 | 4 |  |
| 85 | 0 | 0 |  | 2516 | 8B50 | 65E78000 | 4 |  |
| 86 | 1 | 0 |  | 1EDF | CC74 | CBCF0000 | 3 |  |
| 87 | 1 | 0 |  | 2516 | F6F8 | F1D00000 | 0 |  |
| 88 | 1 | 0 |  | 299A | 9458 | 7FB95400 | 6 | 55 |
| 89 | 0 | 0 |  | 32B4 | A668 | 53ED5000 | 4 |  |
| 90 | 0 | 0 |  | 2E17 | E768 | A7DAA000 | 3 |  |
| 91 | 1 | 0 |  | 2E17 | B951 | A7DAA000 | 3 |  |
| 92 | 0 | 0 |  | 32B4 | B85C | 72828000 | 1 |  |
| 93 | 1 | 0 |  | 32B4 | 85A8 | 72828000 | 1 |  |
| 94 | 0 | 0 |  | 3C3D | CAD0 | 7E3B7E00 | 7 | BF |
| 95 | 1 | 0 |  | 3C3D | 8E93 | 7E3B7E00 | 7 |  |
| 96 | 0 | 0 |  | 415 E | F0F4 | AF95F800 | 5 |  |
| 97 | 1 | 0 |  | 415E | AF96 | AF95F800 | 5 |  |
| 98 | 0 | 0 | CE | 4639 | 82BC | 82BBF000 | 4 |  |
| 99 | 1 | 0 |  | 415E | 8C72 | 8C71E000 | 3 |  |
| 100 | 0 | 0 | CE | 4639 | 82 BC | 82BBC000 | 2 |  |
| 101 | 1 | 0 |  | 415E | 8C72 | 8C718000 | 1 |  |
| 102 | 0 | 0 | CE | 4639 | 82 BC | 82BB0000 | 0 |  |
| 103 | 1 | 0 |  | 415 E | 8 C 72 | 8C71FE00 | 7 | FF 00 |
| 104 | 0 | 0 | CE | 4639 | 82 BC | 82BBFC00 | 6 |  |
| 105 | 1 | 0 |  | 415E | 8C72 | 8C71F800 | 5 |  |
| 106 | 0 | 0 | CE | 4639 | 82 BC | 82BBF000 | 4 |  |
| 107 | 1 | 0 |  | 415 E | 8 C 72 | 8C71E000 | 3 |  |
| 108 | 0 | 0 | CE | 4639 | 82 BC | 82BBC000 | 2 |  |
| 109 | 1 | 0 |  | 415E | 8C72 | 8C718000 | 1 |  |
| 110 | 0 | 0 | CE | 4639 | 82 BC | 82BB0000 | 0 |  |
| 111 | 1 | 0 |  | 415E | 8C72 | 8C71F800 | 7 | FC |
| 112 | 0 | 0 | CE | 4639 | 82 BC | 82BBF000 | 6 |  |
| 113 | 1 | 0 |  | 415E | 8C72 | 8C71E000 | 5 |  |
| 114 | 0 | 0 | CE | 4639 | 82 BC | 82BBC000 | 4 |  |
| 115 | 1 | 0 |  | 415 E | 8C72 | 8C718000 | 3 |  |
| 116 | 0 | 0 | CE | 4639 | 82 BC | 82BB0000 | 2 |  |
| 117 | 1 | 0 |  | 415 E | 8C72 | 8C700000 |  |  |
| 118 | 0 | 0 | CE | 4639 | 82 BC | 82B80000 | 0 |  |
| 119 | 1 | 0 |  | 415E | 8C72 | 8C6AA200 | 7 | 51 |
| 120 | 0 | 0 | CE | 4639 | 82BC | 82AD4400 | 6 |  |

Table K. 8 - Decoder test sequence (sheet 4 of 7)

| EC | D | MPS | CX | Qe (hexadecimal) | A (hexadecimal) | C <br> (hexadecimal) | CT | B |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 121 | 1 | 0 |  | 415E | 8C72 | 8C548800 | 5 |  |
| 122 | 0 | 0 | CE | 4639 | 82 BC | 82811000 | 4 |  |
| 123 | 1 | 0 |  | 415E | 8C72 | 8BFC2000 | 3 |  |
| 124 | 0 | 0 | CE | 4639 | 82 BC | 81D04000 | 2 |  |
| 125 | 1 | 0 |  | 415 E | 8C72 | 8A9A8000 | 1 |  |
| 126 | 0 | 0 | CE | 4639 | 82BC | 7F0D0000 | 0 |  |
| 127 | 1 | 0 |  | 415E | 8C72 | 85150800 | 7 | 84 |
| 128 | 0 | 0 | CE | 4639 | 82 BC | 74021000 | 6 |  |
| 129 | 1 | 0 |  | 415 E | 8C72 | 6EFE2000 | 5 |  |
| 130 | 0 | 0 | CE | 4639 | 82 BC | 47D44000 | 4 |  |
| 131 | 0 | 0 |  | 415E | 8 C 72 | 16A28000 | 3 |  |
| 132 | 0 | 0 |  | 3C3D | 9628 | 2D450000 | 2 |  |
| 133 | 0 | 0 |  | 375E | B3D6 | 5A8A0000 | 1 |  |
| 134 | 0 | 0 |  | 32B4 | F8F0 | B5140000 | 0 |  |
| 135 | 1 | 0 |  | 32B4 | C63C | B5140000 | 0 |  |
| 136 | 0 | 0 |  | 3C3D | CAD0 | 86331C00 | 6 | C7 |
| 137 | 1 | 0 |  | 3 C 3 D | 8E93 | $86331 \mathrm{C00}$ | 6 |  |
| 138 | 1 | 0 |  | 415 E | F0F4 | CF747000 | 4 |  |
| 139 | 0 | 0 | CE | 4639 | 82BC | 3FBCE000 | 3 |  |
| 140 | 0 | 0 |  | 415 E | 8 C 72 | 0673 C 000 | 2 |  |
| 141 | 0 | 0 |  | 3C3D | 9628 | 0CE78000 | 1 |  |
| 142 | 0 | 0 |  | 375 E | B3D6 | 19 CF 0000 | 0 |  |
| 143 | 0 | 0 |  | 32B4 | F8F0 | 339F9C00 | 7 | CE |
| 144 | 0 | 0 |  | 32B4 | C63C | 339F9C00 | 7 |  |
| 145 | 0 | 0 |  | 32B4 | 9388 | 339F9C00 | 7 |  |
| 146 | 0 | 0 |  | 2E17 | C1A8 | 673F3800 | 6 |  |
| 147 | 1 | 0 |  | 2E17 | 9391 | 673F3800 | 6 |  |
| 148 | 0 | 0 |  | 32B4 | B85C | 0714E000 | 4 |  |
| 149 | 0 | 0 |  | 32B4 | 85A8 | 0714E000 | 4 |  |
| 150 | 0 | 0 |  | 2E17 | A5E8 | 0E29C000 | 3 |  |
| 151 | 0 | 0 |  | 299A | EFA2 | 1C538000 | 2 |  |
| 152 | 0 | 0 |  | 299A | C608 | 1C538000 | 2 |  |
| 153 | 0 | 0 |  | 299A | 9C6E | 1C538000 | 2 |  |
| 154 | 0 | 0 |  | 2516 | E5A8 | 38A70000 | 1 |  |
| 155 | 0 | 0 |  | 2516 | C092 | 38A70000 | 1 |  |
| 156 | 0 | 0 |  | 2516 | $9 \mathrm{B7C}$ | 38A70000 | 1 |  |
| 157 | 0 | 0 |  | 1EDF | ECCC | 714E0000 | 0 |  |
| 158 | 0 | 0 |  | 1EDF | CDED | 714E0000 | 0 |  |
| 159 | 0 | 0 |  | 1EDF | AF0E | 714E0000 | 0 |  |
| 160 | 0 | 0 |  | 1EDF | 902F | 714E0000 | 0 |  |

Table K. 8 - Decoder test sequence (sheet 5 of 7)

| EC | D | MPS | CX | $\begin{gathered} \mathrm{Qe} \\ \text { (hexadecimal) } \end{gathered}$ | A (hexadecimal) | $\begin{gathered} \mathrm{C} \\ \text { (hexadecimal) } \end{gathered}$ | CT | B |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 161 | 1 | 0 |  | 1AA9 | E2A0 | E29DF200 | 7 | F9 |
| 162 | 1 | 0 |  | 2516 | D548 | D5379000 | 4 |  |
| 163 | 1 | 0 |  | 299A | 9458 | 94164000 | 2 |  |
| 164 | 1 | 0 |  | 32B4 | A668 | A5610000 | 0 |  |
| 165 | 1 | 0 |  | 3 C 3 D | CAD0 | C6B4E400 | 6 | 39 |
| 166 | 1 | 0 |  | 415 E | F0F4 | E0879000 | 4 |  |
| 167 | 0 | 0 | CE | 4639 | 82 BC | 61 E 32000 | 3 |  |
| 168 | 0 | 0 |  | 415 E | 8 C 72 | 4AC04000 | 2 |  |
| 169 | 1 | 0 |  | 3C3D | 9628 | 95808000 | 1 |  |
| 170 | 1 | 0 |  | 415 E | F0F4 | EE560000 | 7 | 00 |
| 171 | 0 | 0 | CE | 4639 | 82 BC | 7D800000 | 6 |  |
| 172 | 1 | 0 |  | 415 E | 8 C 72 | 81FA0000 | 5 |  |
| 173 | 0 | 0 | CE | 4639 | 82BC | 6DCC0000 | 4 |  |
| 174 | 1 | 0 |  | 415 E | 8 C 72 | 62920000 | 3 |  |
| 175 | 1 | 0 | CE | 4639 | 82 BC | 2EFC0000 | 2 |  |
| 176 | 1 | 0 |  | 4B85 | F20C | BBF00000 | 0 |  |
| 177 | 1 | 0 | CE | 504F | 970A | 2AD25000 | 7 | 28 |
| 178 | 0 | 0 | CE | 5522 | 8D76 | 55A4A000 | 6 |  |
| 179 | 0 | 0 |  | 504F | AA44 | 3AA14000 | 5 |  |
| 180 | 1 | 0 |  | 4B85 | B3EA | 75428000 | 4 |  |
| 181 | 1 | 0 | CE | 504F | 970A | 19BB0000 | 3 |  |
| 182 | 1 | 0 | CE | 5522 | 8D76 | 33760000 | 2 |  |
| 183 | 1 | 0 |  | 59EB | E150 | CDD80000 | 0 |  |
| 184 | 0 | 1 |  | 59EB | B3D6 | 8CE6FA00 | 7 | 7D |
| 185 | 1 | 0 |  | 59EB | B3D6 | 65F7F400 | 6 |  |
| 186 | 1 | 1 |  | 59EB | B3D6 | 1819E800 | 5 |  |
| 187 | 1 | 1 |  | 5522 | B3D6 | 3033D000 | 4 |  |
| 188 | 1 | 1 |  | 504F | BD68 | 6067A000 | 3 |  |
| 189 | 0 | 1 |  | 4B85 | DA32 | C0CF4000 | 2 |  |
| 190 | 1 | 1 | CE | 504F | 970A | 64448000 | 1 |  |
| 191 | 1 | 1 |  | 4B85 | A09E | 3B130000 | 0 |  |
| 192 | 0 | 1 |  | 4639 | AA32 | 76268 C 00 | 7 | 46 |
| 193 | 0 | 1 | CE | 4B85 | 8C72 | 245B1800 | 6 |  |
| 194 | 1 | 1 | CE | 504F | 81DA | 48B63000 | 5 |  |
| 195 | 1 | 1 |  | 4B85 | A09E | 2E566000 | 4 |  |
| 196 | 1 | 1 |  | 4639 | AA32 | 5CACC000 | 3 |  |
| 197 | 0 | 1 |  | 415 E | C7F2 | B9598000 | 2 |  |
| 198 | 1 | 1 | CE | 4639 | 82 BC | 658B0000 | 1 |  |
| 199 | 0 | 1 |  | 415E | 8C72 | 52100000 | 0 |  |
| 200 | 0 | 1 | CE | 4639 | 82 BC | 0DF8E000 | 7 | 70 |

Table K. 8 - Decoder test sequence (sheet 6 of 7)

| EC | D | MPS | CX | $\begin{gathered} \mathrm{Qe} \\ \text { (hexadecimal) } \end{gathered}$ | A (hexadecimal) | C <br> (hexadecimal) | CT | B |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 201 | 1 | 1 |  | 4B85 | F20C | 37E38000 | 5 |  |
| 202 | 1 | 1 |  | 4B85 | A687 | 37E38000 | 5 |  |
| 203 | 1 | 1 |  | 4639 | B604 | 6FC70000 | 4 |  |
| 204 | 0 | 1 |  | 415E | DF96 | DF8E0000 | 3 |  |
| 205 | 1 | 1 | CE | 4639 | 82BC | 82AC0000 | 2 |  |
| 206 | 0 | 1 |  | 415E | 8C72 | 8C520000 | 1 |  |
| 207 | 1 | 1 | CE | 4639 | 82BC | 827C0000 | 0 |  |
| 208 | 0 | 1 |  | 415E | 8 C 72 | 8BF31C00 | 7 | 8 E |
| 209 | 1 | 1 | CE | 4639 | 82BC | 81 BE3800 | 6 |  |
| 210 | 0 | 1 |  | 415E | 8C72 | 8A767000 | 5 |  |
| 211 | 1 | 1 | CE | 4639 | 82 BC | 7EC4E000 | 4 |  |
| 212 | 0 | 1 |  | 415E | 8C72 | $8483 \mathrm{C000}$ | 3 |  |
| 213 | 1 | 1 | CE | 4639 | 82BC | 72DF8000 | 2 |  |
| 214 | 0 | 1 |  | 415E | 8 C 72 | 6CB90000 | , |  |
| 215 | 1 | 1 | CE | 4639 | 82BC | 434A0000 | 0 |  |
| 216 | 1 | 1 |  | 415E | 8 C 72 | 0D8F9600 | 7 | CB |
| 217 | 1 | 1 |  | 3C3D | 9628 | 1B1F2C00 | 6 |  |
| 218 | 1 | 1 |  | 375E | B3D6 | 363 E 5800 | 5 |  |
| 219 | 1 | 1 |  | 32B4 | F8F0 | 6C7CB000 | 4 |  |
| 220 | 1 | 1 |  | 32B4 | C63C | 6C7CB000 | 4 |  |
| 221 | 0 | 1 |  | 32B4 | 9388 | 6C7CB000 | 4 |  |
| 222 | 1 | 1 |  | 3C3D | CAD0 | 2EA2C000 | 2 |  |
| 223 | 1 | 1 |  | 3C3D | 8E93 | 2EA2C000 |  |  |
| 224 | 1 | 1 |  | 375E | A4AC | 5D458000 | 1 |  |
| 225 | 0 | 1 |  | 32B4 | DA9C | BA8B0000 | 0 |  |
| 226 | 1 | 1 |  | 3C3D | CAD0 | 4A8F0000 | 6 | C0 |
| 227 | 1 | 1 |  | 3C3D | 8E93 | 4A8F0000 | 6 |  |
| 228 | 0 | 1 |  | 375E | A4AC | 951E0000 | 5 |  |
| 229 | 1 | 1 |  | 3C3D | DD78 | 9F400000 | 3 |  |
| 230 | 0 | 1 |  | 3C3D | A13B | 9F400000 | 3 |  |
| 231 | 0 | 1 |  | 415 E | F0F4 | E9080000 | 1 |  |
| 232 | 1 | 1 | CE | 4639 | 82 BC | 72E40000 | 0 |  |
| 233 | 0 | 1 |  | 415E | 8 C 72 | 6CC3EC00 | 7 | F6 |
| 234 | 1 | 1 | CE | 4639 | 82 BC | 435FD800 | 6 |  |
| 235 | 1 | 1 |  | 415E | 8 C 72 | 0DB9B000 | 5 |  |
| 236 | 1 | 1 |  | 3C3D | 9628 | 1B736000 | 4 |  |
| 237 | 1 | 1 |  | 375 E | B3D6 | 36E6C000 | 3 |  |
| 238 | 1 | 1 |  | 32B4 | F8F0 | 6DCD8000 | 2 |  |
| 239 | 1 | 1 |  | 32B4 | C63C | 6DCD8000 | 2 |  |
| 240 | 0 | 1 |  | 32B4 | 9388 | 6DCD8000 | 2 |  |

#  

Table K. 8 - Decoder test sequence (sheet 7 of 7)

| EC | D | MPS | CX | $\begin{gathered} \mathrm{Qe} \\ \text { (hexadecimal) } \end{gathered}$ | $\underset{\text { (hexadecimal) }}{\mathrm{A}}$ | C (hexadecimal) | CT | B |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 241 | 1 | 1 |  | 3C3D | CAD0 | 33E60000 | 0 |  |
| 242 | 1 | 1 |  | 3C3D | 8E93 | 33E60000 | 0 |  |
| Marker detected: zero byte fed to decoder |  |  |  |  |  |  |  |  |
| 243 | 1 | 1 |  | 375E | A4AC | 67CC0000 | 7 |  |
| 244 | 0 | 1 |  | 32B4 | DA9C | CF980000 | 6 |  |
| 245 | 0 | 1 |  | 3C3D | CAD0 | 9 EC 00000 | 4 |  |
| 246 | 1 | 1 |  | 415 E | F0F4 | 40B40000 | 2 |  |
| 247 | 1 | 1 |  | 415 E | AF96 | 40B40000 | 2 |  |
| 248 | 1 | 1 |  | 3C3D | DC70 | 81680000 | 1 |  |
| 249 | 0 | 1 |  | 3C3D | A033 | 81680000 | 1 |  |
| Marker detected: zero byte fed to decoder |  |  |  |  |  |  |  |  |
| 250 | 1 | , |  | 415E | F0F4 | 75 C 80000 | 7 |  |
| 251 | 0 | 1 |  | 415E | AF96 | 75C80000 | 7 |  |
| 252 | 0 | 1 | CE | 4639 | 82BC | 0F200000 | 6 |  |
| 253 | 1 | 1 |  | 4B85 | F20C | 3C800000 | 4 |  |
| 254 | 1 | 1 |  | 4B85 | A687 | 3C800000 | 4 |  |
| 255 | 0 | 1 |  | 4639 | B604 | 79000000 | 3 |  |
| 256 | 0 | 1 | CE | 4B85 | 8C72 | 126A0000 | 2 |  |

## K. 5 Low-pass downsampling filters for hierarchical coding

In this section simple examples are given of downsampling filters which are compatible with the upsampling filter defined in J.1.1.2.

Figure K. 5 shows the weighting of neighbouring samples for simple one-dimensional horizontal and vertical low-pass filters. The output of the filter must be normalized by the sum of the neighbourhood weights.


Figure K. 5 - Low-pass filter example

The centre sample in Figure K. 5 should be aligned with the left column or top line of the high resolution image when calculating the left column or top line of the low resolution image. Sample values which are situated outside of the image boundary are replicated from the sample values at the boundary to provide missing edge values.

If the image being downsampled has an odd width or length, the odd dimension is increased by 1 by sample replication on the right edge or bottom line before downsampling.

## K. 6 Domain of applicability of DCT and spatial coding techniques

The DCT coder is intended for lossy coding in a range from quite visible loss to distortion well below the threshold for visibility. However in general, DCT-based processes cannot be used for true lossless coding.

The lossless coder is intended for completely lossless coding. The lossless coding process is significantly less effective than the DCT-based processes for distortions near and above the threshold of visibility.

The point transform of the input to the lossless coder permits a very restricted form of lossy coding with the "lossless" coder. (The coder is still lossless after the input point transform.) Since the DCT is intended for lossy coding, there may be some confusion about when this alternative lossy technique should be used.

Lossless coding with a point transformed input is intended for applications which cannot be addressed by DCT coding techniques. Among these are

- true lossless coding to a specified precision;
- lossy coding with precisely defined error bounds;
- hierarchical progression to a truly lossless final stage.

If lossless coding with a point transformed input is used in applications which can be met effectively by DCT coding, the results will be significantly less satisfactory. For example, distortion in the form of visible contours usually appears when precision of the luminance component is reduced to about six bits. For normal image data, this occurs at bit rates well above those for which the DCT gives outputs which are visually indistinguishable from the source.

## K. 7 Domain of applicability of the progressive coding modes of operation

Two very different progressive coding modes of operation have been defined, progressive coding of the DCT coefficients and hierarchical progression. Progressive coding of the DCT coefficients has two complementary procedures, spectral selection and successive approximation. Because of this diversity of choices, there may be some confusion as to which method of progression to use for a given application.

## K.7.1 Progressive coding of the DCT

In progressive coding of the DCT coefficients two complementary procedures are defined for decomposing the $8 \times 8 \mathrm{DCT}$ coefficient array, spectral selection and successive approximation. Spectral selection partitions zig-zag array of DCT coefficients into "bands", one band being coded in each scan. Successive approximation codes the coefficients with reduced precision in the first scan; in each subsequent scan the precision is increased by one bit.

A single forward DCT is calculated for these procedures. When all coefficients are coded to full precision, the DCT is the same as in the sequential mode. Therefore, like the sequential DCT coding, progressive coding of DCT coefficients is intended for applications which need very good compression for a given level of visual distortion.

The simplest progressive coding technique is spectral selection; indeed, because of this simplicity, some applications may choose - despite the limited progression that can be achieved - to use only spectral selection. Note, however, that the absence of high frequency bands typically leads - for a given bit rate - to a significantly lower image quality in the intermediate stages than can be achieved with the more general progressions. The net coding efficiency at the completion of the final stage is typically comparable to or slightly less than that achieved with the sequential DCT.

A much more flexible progressive system is attained at some increase in complexity when successive approximation is added to the spectral selection progression. For a given bit rate, this system typically provides significantly better image quality than spectral selection alone. The net coding efficiency at the completion of the final stage is typically comparable to or slightly better than that achieved with the sequential DCT.

## K.7.2 Hierarchical progression

Hierarchical progression permits a sequence of outputs of increasing spatial resolution, and also allows refinement of image quality at a given spatial resolution. Both DCT and spatial versions of the hierarchical progression are allowed, and progressive coding of DCT coefficients may be used in a frame of the DCT hierarchical progression.

The DCT hierarchical progression is intended for applications which need very good compression for a given level of visual distortion; the spatial hierarchical progression is intended for applications which need a simple progression with a truly lossless final stage. Figure K. 6 illustrates examples of these two basic hierarchical progressions.


Lossless path


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Figure K. 6 - Sketch of the basic operations of the hierarchical mode

## K.7.2.1 DCT Hierarchical progression

If a DCT hierarchical progression uses reduced spatial resolution, the early stages of the progression can have better image quality for a given bit rate than the early stages of non-hierarchical progressive coding of the DCT coefficients. However, at the point where the distortion between source and output becomes indistinguishable, the coding efficiency achieved with a DCT hierarchical progression is typically significantly lower than the coding efficiency achieved with a nonhierarchical progressive coding of the DCT coefficients.

While the hierarchical DCT progression is intended for lossy progressive coding, a final spatial differential coding stage can be used. When this final stage is used, the output can be almost lossless, limited only by the difference between the encoder and decoder IDCT implementations. Since IDCT implementations can differ significantly, truly lossless coding after a DCT hierarchical progression cannot be guaranteed. An important alternative, therefore, is to use the input point transform of the final lossless differential coding stage to reduce the precision of the differential input. This allows a bounding of the difference between source and output at a significantly lower cost in coded bits than coding of the full precision spatial difference would require.

## K.7.2.2 Spatial hierarchical progression

If lossless progression is required, a very simple hierarchical progression may be used in which the spatial lossless coder with point transformed input is used as a first stage. This first stage is followed by one or more spatial differential coding stages. The first stage should be nearly lossless, such that the low order bits which are truncated by the point transform are essentially random - otherwise the compression efficiency will be degraded relative to non-progressive lossless coding.

## K. 8 Suppression of block-to-block discontinuities in decoded images

A simple technique is available for suppressing the block-to-block discontinuities which can occur in images compressed by DCT techniques.

The first few (five in this example) low frequency DCT coefficients are predicted from the nine DC values of the block and the eight nearest-neighbour blocks, and the predicted values are used to suppress blocking artifacts in smooth areas of the image.

The prediction equations for the first five AC coefficients in the zig-zag sequence are obtained as follows:

## K.8.1 AC prediction

The sample field in a 3 by 3 array of blocks (each block containing an $8 \times 8$ array of samples) is modeled by a two-dimensional second degree polynomial of the form:

$$
\mathrm{P}(\mathrm{x}, \mathrm{y})=\mathrm{A} 1\left(\mathrm{x}^{2} \mathrm{y}^{2}\right)+\mathrm{A} 2\left(\mathrm{x}^{2} \mathrm{y}\right)+\mathrm{A} 3\left(\mathrm{xy}^{2}\right)+\mathrm{A} 4\left(\mathrm{x}^{2}\right)+\mathrm{A} 5(\mathrm{xy})+\mathrm{A} 6\left(\mathrm{y}^{2}\right)+\mathrm{A} 7(\mathrm{x})+\mathrm{A} 8(\mathrm{y})+\mathrm{A} 9
$$

The nine coefficients A1 through A9 are uniquely determined by imposing the constraint that the mean of $\mathrm{P}(\mathrm{x}, \mathrm{y})$ over each of the nine blocks must yield the correct DC-values.

Applying the DCT to the quadratic field predicting the samples in the central block gives a prediction of the low frequency AC coefficients depicted in Figure K.7.

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Figure K. 7 - DCT array positions of predicted AC coefficients

The prediction equations derived in this manner are as follows:
For the two dimensional array of DC values shown

| $\mathrm{DC}_{1}$ | $\mathrm{DC}_{2}$ | $\mathrm{DC}_{3}$ |
| :--- | :--- | :--- |
| $\mathrm{DC}_{4}$ | $\mathrm{DC}_{5}$ | $\mathrm{DC}_{6}$ |
| $\mathrm{DC}_{7}$ | $\mathrm{DC}_{8}$ | DC 9 |

The unquantized prediction equations are

$$
\begin{aligned}
& \mathrm{AC}_{01}=1,13885\left(\mathrm{DC}_{4}-\mathrm{DC}_{6}\right) \\
& \mathrm{AC}_{10}=1,13885\left(\mathrm{DC}_{2}-\mathrm{DC}_{8}\right) \\
& \mathrm{AC}_{20}=0,27881\left(\mathrm{DC}_{2}+\mathrm{DC}_{8}-2 \times \mathrm{DC}_{5}\right) \\
& \mathrm{AC}_{11}=0,16213\left(\left(\mathrm{DC}_{1}-\mathrm{DC}_{3}\right)-\left(\mathrm{DC}_{7}-\mathrm{DC}_{9}\right)\right) \\
& \mathrm{AC}_{02}=0,27881\left(\mathrm{DC}_{4}+\mathrm{DC}_{6}-2 \times \mathrm{DC}_{5}\right)
\end{aligned}
$$

The scaling of the predicted AC coefficients is consistent with the DCT normalization defined in A.3.3.

## K.8.2

Quantized AC prediction
The prediction equations can be mapped to a form which uses quantized values of the DC coefficients and which computes quantized AC coefficients using integer arithmetic. The quantized DC coefficients need to be scaled, however, such that the predicted coefficients have fractional bit precision.

First, the prediction equation coefficients are scaled by 32 and rounded to the nearest integer. Thus,

$$
\begin{aligned}
& 1,13885 \times 32=36 \\
& 0,27881 \times 32=9 \\
& 0,16213 \times 32=5
\end{aligned}
$$

The multiplicative factors are then scaled by the ratio of the DC and AC quantization factors and rounded appropriately. The normalization defined for the DCT introduces another factor of 8 in the unquantized DC values. Therefore, in terms of the quantized DC values, the predicted quantized AC coefficients are given by the equations below. Note that if (for example) the DC values are scaled by a factor of 4 , the AC predictions will have 2 fractional bits of precision relative to the quantized DCT coefficients.

$$
\begin{aligned}
& \mathrm{QAC}_{01}=\left(\left(\mathrm{R}_{\mathrm{d}} \times \mathrm{Q}_{01}\right)+\left(36 \times \mathrm{Q}_{00} \times\left(\mathrm{QDC}_{4}-\mathrm{QDC}_{6}\right)\right)\right) /\left(256 \times \mathrm{Q}_{01}\right) \\
& \mathrm{QAC}_{10}=\left(\left(\mathrm{R}_{\mathrm{d}} \times \mathrm{Q}_{10}\right)+\left(36 \times \mathrm{Q}_{00} \times\left(\mathrm{QDC}_{2}-\mathrm{QDC}_{8}\right)\right)\right) /\left(256 \times \mathrm{Q}_{10}\right) \\
& \mathrm{QAC}_{20}=\left(\left(\mathrm{R}_{\mathrm{d}} \times \mathrm{Q}_{20}\right)+\left(9 \times \mathrm{Q}_{00} \times\left(\mathrm{QDC}_{2}+\mathrm{QDC}_{8}-2 \times \mathrm{QDC}_{5}\right)\right)\right) /\left(256 \times \mathrm{Q}_{20}\right) \\
& \mathrm{QAC}_{11}=\left(\left(\mathrm{R}_{\mathrm{d}} \times \mathrm{Q}_{11}\right)+\left(5 \times \mathrm{Q}_{00} \times\left(\left(\mathrm{QDC}_{1}-\mathrm{QDC}_{3}\right)-\left(\mathrm{QDC}_{7}-\mathrm{QDC}_{9}\right)\right)\right)\right) /\left(256 \times \mathrm{Q}_{11}\right) \\
& \mathrm{QAC}_{02}=\left(\left(\mathrm{R}_{\mathrm{d}} \times \mathrm{Q}_{02}\right)+\left(9 \times \mathrm{Q}_{00} \times\left(\mathrm{QDC}_{4}+\mathrm{QDC}_{6}-2 \times \mathrm{QDC}_{5}\right)\right)\right) /\left(256 \times \mathrm{Q}_{02}\right)
\end{aligned}
$$

where $\mathrm{QDC}_{\mathrm{x}}$ and $\mathrm{QAC}_{\mathrm{xy}}$ are the quantized and scaled DC and AC coefficient values. The constant Rd is added to get a correct rounding in the division. Rd is 128 for positive numerators, and -128 for negative numerators.

Predicted values should not override coded values. Therefore, predicted values for coefficients which are already non-zero should be set to zero. Predictions should be clamped if they exceed a value which would be quantized to a non-zero value for the current precision in the successive approximation.

## K. 9 Modification of dequantization to improve displayed image quality

For a progression where the first stage successive approximation bit, Al , is set to 3 , uniform quantization of the DCT gives the following quantization and dequantization levels for a sequence of successive approximation scans, as shown in Figure K.8:


Figure K. 8 - Illustration of two reconstruction strategies

The column to the left labelled "Al" gives the bit position specified in the scan header. The quantized DCT coefficient magnitudes are therefore divided by $2^{\mathrm{Al}}$ during that scan.

Referring to the final scan $(\mathrm{Al}=0)$, the points marked with " t " are the threshold values, while the points marked with " r " are the reconstruction values. The unquantized output is obtained by multiplying the horizontal scale in Figure K. 8 by the quantization value.

The quantization interval for a coefficient value of zero is indicated by the depressed interval of the line. As the bit position Al is increased, a "fat zero" quantization interval develops around the zero DCT coefficient value. In the limit where the scaling factor is very large, the zero interval is twice as large as the rest of the quantization intervals.

Two different reconstruction strategies are shown. The points marked " r " are the reconstruction obtained using the normal rounding rules for the DCT for the complete full precision output. This rule seems to give better image quality when high bandwidth displays are used. The points marked " x " are an alternative reconstruction which tends to give better images on lower bandwidth displays. " $x$ " and " $r$ " are the same for slice 0 . The system designer must determine which strategy is best for the display system being used.

## K. 10 Example of point transform

The difference between the arithmetic-shift-right by Pt and divide by $2^{\mathrm{Pt}}$ can be seen from the following:
After the level shift the DC has values from +127 to -128 . Consider values near zero (after the level shift), and the case where $\mathrm{Pt}=1$ :

| Before <br> level shift | Before <br> point transform | After <br> divide by 2 | After <br> 131 |
| :---: | :---: | :---: | :---: |
| +3 | +1 | shift-right-arithmetic 1 |  |
| 130 | +2 | +1 | +1 |
| 129 | +1 | 0 | +1 |
| 128 | 0 | 0 | 0 |
| 127 | -1 | 0 | 0 |
| 126 | -2 | -1 | -1 |
| 125 | -3 | -1 | -1 |
| 124 | -4 | -2 | -2 |
| 123 | -5 | -2 | -2 |
|  |  |  | -3 |

The key difference is in the truncation of precision. The divide truncates the magnitude; the arithmetic shift truncates the LSB. With a divide by 2 we would get non-uniform quantization of the DC values; therefore we use the shift-rightarithmetic operation.

For positive values, the divide by 2 and the shift-right-arithmetic by 1 operations are the same. Therefore, the shift-rightarithmetic by 1 operation effectively is a divide by 2 when the point transform is done before the level shift.

## Annex L

## Patents

(This annex does not form an integral part of this Recommendation | International Standard)

## L. 1 Introductory remarks

The user's attention is called to the possibility that - for some of the coding processes specified in Annexes F, G, H, and J - compliance with this Specification may require use of an invention covered by patent rights.

By publication of this Specification, no position is taken with respect to the validity of this claim or of any patent rights in connection therewith. However, for each patent listed in this annex, the patent holder has filed with the Information Technology Task Force (ITTF) and the Telecommunication Standardization Bureau (TSB) a statement of willingness to grant a license under these rights on reasonable and non-discriminatory terms and conditions to applicants desiring to obtain such a license.

The criteria for including patents in this annex are:
a) the patent has been identified by someone who is familiar with the technical fields relevant to this Specification, and who believes use of the invention covered by the patent is required for implementation of one or more of the coding processes specified in Annexes F, G, H, or J;
b) the patent-holder has written a letter to the ITTF and TSB, stating willingness to grant a license to an unlimited number of applicants throughout the world under reasonable terms and conditions that are demonstrably free of any unfair discrimination.

This list of patents shall be updated, if necessary, upon publication of any revisions to the Recommendation | International Standard.

## L. 2 List of patents

The following patents may be required for implementation of any one of the processes specified in Annexes F, G, H, and J which uses arithmetic coding:

US 4,633,490, December 30, 1986, IBM, MITCHELL (J.L.) and GOERTZEL (G.): Symmetrical Adaptive Data Compression/Decompression System.

US 4,652,856, February 4, 1986, IBM, MOHIUDDIN (K.M.) and RISSANEN (J.J.): A Multiplication-free Multi-Alphabet Arithmetic Code.

US 4,369,463, January 18, 1983, IBM, ANASTASSIOU (D.) and MITCHELL (J.L.): Grey Scale Image Compression with Code Words a Function of Image History.

US 4,749,983, June 7, 1988, IBM, LANGDON (G.): Compression of Multilevel Signals.
US 4,935,882, June 19, 1990, IBM, PENNEBAKER (W.B.) and MITCHELL (J.L.): Probability Adaptation for Arithmetic Coders.

US 4,905,297, February 27, 1990, IBM, LANGDON (G.G.), Jr., MITCHELL (J.L.), PENNEBAKER (W.B.), and RISSANEN (J.J.): Arithmetic Coding Encoder and Decoder System.

US 4,973,961, November 27, 1990, AT\&T, CHAMZAS (C.), DUTTWEILER (D.L.): Method and Apparatus for Carry-over Control in Arithmetic Entropy Coding.

US 5,025,258, June 18, 1991, AT\&T, DUTTWEILER (D.L): Adaptive Probability Estimator for Entropy Encoding/Decoding.

US 5,099,440, March 24, 1992, IBM, PENNEBAKER (W.B.) and MITCHELL (J.L.): Probability Adaptation for Arithmetic Coders.

Japanese Patent Application 2-46275, February 26, 1990, MEL ONO (F.), KIMURA (T.), YOSHIDA (M.), and KINO (S.): Coding System.

The following patent may be required for implementation of any one of the hierarchical processes specified in Annex H when used with a lossless final frame:

US 4,665,436, May 12, 1987, EI OSBORNE (J.A.) and SEIFFERT (C.): Narrow Bandwidth Signal Transmission.

No other patents required for implementation of any of the other processes specified in Annexes F, G, H, or J had been identified at the time of publication of this Specification.

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## Annex M

## Bibliography

(This annex does not form an integral part of this Recommendation | International Standard)

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# Image Compression and the Discrete Cosine Transform 

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#### Abstract

The mathematical equations of the DCT and its uses with image compression are explained.

\section*{Introduction}

As our use of and reliance on computers continues to grow, so too does our need for efficient ways of storing large amounts of data. For example, someone with a web page or online catalog - that uses dozens or perhaps hundreds of images - will more than likely need to use some form of image compression to store those images. This is because the amount of space required to hold unadulterated images can be prohibitively large in terms of cost. Fortunately, there are several methods of image compression available today. These fall into two general categories: lossless and lossy image compression. The JPEG process is a widely used form of lossy image compression that centers around the Discrete Cosine Transform. The DCT works by separating images into parts of differing frequencies. During a step called quantization, where part of compression actually occurs, the less important frequencies are discarded, hence the use of the term "lossy." Then, only the most important frequencies that remain are used retrieve the image in the decompression process. As a result, reconstructed images contain some distortion; but as we shall soon see, these levels of distortion can be adjusted during the compression stage. The JPEG method is used for both color and black-and-white images, but the focus of this article will be on compression of the latter.


## The Process

The following is a general overview of the JPEG process. Later, we will take the reader through a detailed tour of JPEG's method so that a more comprehensive understanding of the process may be acquired.

1. The image is broken into $8 \times 8$ blocks of pixels.
2. Working from left to right, top to bottom, the DCT is applied to each block.
3. Each block is compressed through quantization.
4. The array of compressed blocks that constitute the image is stored in a drastically reduced amount of space.
5. When desired, the image is reconstructed through decompression, a process that uses the Inverse Discrete Cosine Transform (IDCT).

## The DCT Equation

The DCT equation (Eq. 1) computes the $\mathrm{i}, \mathrm{j}^{\text {th }}$ entry of the DCT of an image.

$$
\begin{align*}
D(i, j) & =\frac{1}{\sqrt{2 N}} C(i) C(j) \sum_{x=0}^{N-1} \sum_{y=0}^{N-1} p(x, y) \cos \left[\frac{(2 x+1) i \pi}{2 N}\right] \cos \left[\frac{(2 y+1) j \pi}{2 N}\right]  \tag{1}\\
C(u) & =\left\{\begin{array}{ll}
\frac{1}{\sqrt{2}} & \text { if } u=0 \\
1 & \text { if } u>0
\end{array}\right\}
\end{align*}
$$

$p(x, y)$ is the $\mathrm{x}, \mathrm{y}^{\text {th }}$ element of the image represented by the matrix $p . N$ is the size of the block that the DCT is done on. The equation calculates one entry ( $\mathrm{i}, \mathrm{j}^{\text {th }}$ ) of the transformed image from the pixel values of the original image matrix. For the standard $8 \times 8$ block that JPEG compression uses, $N$ equals 8 and $x$ and $y$ range from 0 to 7 . Therefore $D(i, j)$ would be as in Equation (3).

$$
D(i, j)=\frac{1}{4} C(i) C(j) \sum_{x=0}^{7} \sum_{y=0}^{7} p(x, y) \cos \left[\frac{(2 x+1) i \pi}{16}\right] \cos \left[\frac{(2 y+1) j \pi}{16}\right]
$$

Because the DCT uses cosine functions, the resulting matrix depends on the horizontal, diagonal, and vertical frequencies. Therefore an image black with a lot of change in frequency has a very random looking resulting matrix, while an image matrix of just one color, has a resulting matrix of a large value for the first element and zeroes for the other elements.

## The DCT Matrix

To get the matrix form of Equation (1), we will use the following equation

$$
T_{i, j}=\left\{\begin{array}{ll}
\frac{1}{\sqrt{N}} & \text { if } i=0  \tag{4}\\
\sqrt{\frac{2}{N}} \cos \left[\frac{(2 j+1) i \pi}{2 N}\right] & \text { if } i>0
\end{array}\right\}
$$

For an 8 x 8 block it results in this matrix:

$$
T=\left[\begin{array}{llllllll}
.3536 & .3536 & .3536 & .3536 & .3536 & .3536 & .3536 & .3536 \\
.4904 & .4157 & .2778 & .0975 & -.0975 & -.2778 & -.4157 & -.4904 \\
.4619 & .1913 & -.1913 & -.4619 & -.4619 & -.1913 & .1913 & .4619 \\
.4157 & -.0975 & -.4904 & -.2778 & .2778 & .4904 & .0975 & -.4157 \\
.3536 & -.3536 & -.3536 & .3536 & .3536 & -.3536 & -.3536 & .3536 \\
.2778 & -.4904 & .0975 & .4157 & -.4157 & -.0975 & .4904 & -.2778 \\
.1913 & -.4619 & .4619 & -.1913 & -.1913 & .4619 & -.4619 & .1913 \\
.0975 & -.2778 & .4157 & -.4904 & .4904 & -.4157 & .2778 & -.0975
\end{array}\right]
$$

The first row $(i=1)$ of the matrix has all the entries equal to $1 / \sqrt{8}$ as expected from Equation (4).

The columns of $T$ form an orthonormal set, so $T$ is an orthogonal matrix. When doing the inverse DCT the orthogonality of $T$ is important, as the inverse of $T$ is $T^{\prime}$ which is easy to calculate.

## Doing the DCT on an 8x8 Block

Before we begin, it should be noted that the pixel values of a black-and-white image range from 0 to 255 in steps of 1 , where pure black is represented by 0 , and pure white by 255. Thus it can be seen how a photo, illustration, etc. can be accurately represented by these 256 shades of gray.

Since an image comprises hundreds or even thousands of $8 \times 8$ blocks of pixels, the following description of what happens to one 8 x 8 block is a microcosm of the JPEG process;
what is done to one block of image pixels is done to all of them, in the order earlier specified.

Now, let's start with a block of image-pixel values. This particular block was chosen from the very upper- left-hand corner of an image.

$$
\text { Original }=\left[\begin{array}{llllllll}
154 & 123 & 123 & 123 & 123 & 123 & 123 & 136 \\
192 & 180 & 136 & 154 & 154 & 154 & 136 & 110 \\
254 & 198 & 154 & 154 & 180 & 154 & 123 & 123 \\
239 & 180 & 136 & 180 & 180 & 166 & 123 & 123 \\
180 & 154 & 136 & 167 & 166 & 149 & 136 & 136 \\
128 & 136 & 123 & 136 & 154 & 180 & 198 & 154 \\
123 & 105 & 110 & 149 & 136 & 136 & 180 & 166 \\
110 & 136 & 123 & 123 & 123 & 136 & 154 & 136
\end{array}\right]
$$

Because the DCT is designed to work on pixel values ranging from -128 to 127, the original block is "leveled off" by subtracting 128 from each entry. This results in the following matrix.

$$
M=\left[\begin{array}{cccccccc}
26 & -5 & -5 & -5 & -5 & -5 & -5 & 8 \\
64 & 52 & 8 & 26 & 26 & 26 & 8 & -18 \\
126 & 70 & 26 & 26 & 52 & 26 & -5 & -5 \\
111 & 52 & 8 & 52 & 52 & 38 & -5 & -5 \\
52 & 26 & 8 & 39 & 38 & 21 & 8 & 8 \\
0 & 8 & -5 & 8 & 26 & 52 & 70 & 26 \\
-5 & -23 & -18 & 21 & 8 & 8 & 52 & 38 \\
-18 & 8 & -5 & -5 & -5 & 8 & 26 & 8
\end{array}\right]
$$

We are now ready to perform the Discrete Cosine Transform, which is accomplished by matrix multiplication.

$$
\begin{equation*}
D=T M T^{\prime} \tag{5}
\end{equation*}
$$

In Equation (5) matrix $M$ is first multiplied on the left by the DCT matrix $T$ from the previous section; this transforms the rows. The columns are then transformed by multiplying on the right by the transpose of the DCT matrix. This yields the following matrix.

$$
D=\left[\begin{array}{cccccccc}
162.3 & 40.6 & 20.0 & 72.3 & 30.3 & 12.5 & -19.7 & -11.5 \\
30.5 & 108.4 & 10.5 & 32.3 & 27.7 & -15.5 & 18.4 & -2.0 \\
-94.1 & -60.1 & 12.3 & -43.4 & -31.3 & 6.1 & -3.3 & 7.1 \\
-38.6 & -83.4 & -5.4 & -22.2 & -13.5 & 15.5 & -1.3 & 3.5 \\
-31.3 & 17.9 & -5.5 & -12.4 & 14.3 & -6.0 & 11.5 & -6.0 \\
-0.9 & -11.8 & 12.8 & 0.2 & 28.1 & 12.6 & 8.4 & 2.9 \\
4.6 & -2.4 & 12.2 & 6.6 & -18.7 & -12.8 & 7.7 & 12.0 \\
-10.0 & 11.2 & 7.8 & -16.3 & 21.5 & 0.0 & 5.9 & 10.7
\end{array}\right]
$$

This block matrix now consists of 64 DCT coefficients, $c_{i j}$, where $i$ and $j$ range from 0 to 7. The top-left coefficient, $c_{00}$, correlates to the low frequencies of the original image block. As we move away from $c_{00}$ in all directions, the DCT coefficients correlate to higher and higher frequencies of the image block, where $c_{77}$ corresponds to the highest frequency. It is important to note that the human eye is most sensitive to low frequencies, and results from the quantization step will reflect this fact.

## Quantization

Our $8 \times 8$ block of DCT coefficients is now ready for compression by quantization. A remarkable and highly useful feature of the JPEG process is that in this step, varying levels of image compression and quality are obtainable through selection of specific quantization matrices. This enables the user to decide on quality levels ranging from 1 to 100 , where 1 gives the poorest image quality and highest compression, while 100 gives the best quality and lowest compression. As a result, the quality/compression ratio can be tailored to suit different needs.

Subjective experiments involving the human visual system have resulted in the JPEG standard quantization matrix. With a quality level of 50 , this matrix renders both high compression and excellent decompressed image quality.

$$
Q_{50}=\left[\begin{array}{cccccccc}
16 & 11 & 10 & 16 & 24 & 40 & 51 & 61 \\
12 & 12 & 14 & 19 & 26 & 58 & 60 & 55 \\
14 & 13 & 16 & 24 & 40 & 57 & 69 & 56 \\
14 & 17 & 22 & 29 & 51 & 87 & 80 & 62 \\
18 & 22 & 37 & 56 & 68 & 109 & 103 & 77 \\
24 & 35 & 55 & 64 & 81 & 104 & 113 & 92 \\
49 & 64 & 78 & 87 & 103 & 121 & 120 & 101 \\
72 & 92 & 95 & 98 & 112 & 100 & 103 & 99
\end{array}\right]
$$

If, however, another level of quality and compression is desired, scalar multiples of the JPEG standard quantization matrix may be used. For a quality level greater than 50 (less compression, higher image quality), the standard quantization matrix is multiplied by (100-quality level)/50. For a quality level less than 50 (more compression, lower image quality), the standard quantization matrix is multiplied by $50 /$ quality level. The scaled
quantization matrix is then rounded and clipped to have positive integer values ranging from 1 to 255 . For example, the following quantization matrices yield quality levels of 10 and 90 .

$$
\begin{aligned}
& Q_{10}=\left[\begin{array}{cccccccc}
80 & 60 & 50 & 80 & 120 & 200 & 255 & 255 \\
55 & 60 & 70 & 95 & 130 & 255 & 255 & 255 \\
70 & 65 & 80 & 120 & 200 & 255 & 255 & 255 \\
70 & 85 & 110 & 145 & 255 & 255 & 255 & 255 \\
90 & 110 & 185 & 255 & 255 & 255 & 255 & 255 \\
120 & 175 & 255 & 255 & 255 & 255 & 255 & 255 \\
245 & 255 & 255 & 255 & 255 & 255 & 255 & 255 \\
255 & 255 & 255 & 255 & 255 & 255 & 255 & 255
\end{array}\right] \\
& Q_{90}=\left[\begin{array}{cccccccc}
3 & 2 & 2 & 3 & 5 & 8 & 10 & 12 \\
2 & 2 & 3 & 4 & 5 & 12 & 12 & 11 \\
3 & 3 & 3 & 5 & 8 & 11 & 14 & 11 \\
3 & 3 & 4 & 6 & 10 & 17 & 16 & 12 \\
4 & 4 & 7 & 11 & 14 & 22 & 21 & 15 \\
5 & 7 & 11 & 13 & 16 & 12 & 23 & 18 \\
10 & 13 & 16 & 17 & 21 & 24 & 24 & 21 \\
14 & 18 & 19 & 20 & 22 & 20 & 20 & 20
\end{array}\right]
\end{aligned}
$$

Quantization is achieved by dividing each element in the transformed image matrix $D$ by the corresponding element in the quantization matrix, and then rounding to the nearest integer value. For the following step, quantization matrix $Q_{50}$ is used.

$$
\begin{gathered}
C_{i, j}=\operatorname{round}\left(\frac{D_{i, j}}{Q_{i, j}}\right) \\
C=\left[\begin{array}{cccccccc}
10 & 4 & 2 & 5 & 1 & 0 & 0 & 0 \\
3 & 9 & 1 & 2 & 1 & 0 & 0 & 0 \\
-7 & -5 & 1 & -2 & -1 & 0 & 0 & 0 \\
-3 & -5 & 0 & -1 & 0 & 0 & 0 & 0 \\
-2 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0
\end{array}\right]
\end{gathered}
$$

Recall that the coefficients situated near the upper-left corner correspond to the lower frequencies - to which the human eye is most sensitive - of the image block. In addition, the zeros represent the less important, higher frequencies that have been discarded, giving rise to
the lossy part of compression. As mentioned earlier, only the remaining nonzero coefficients will be used to reconstruct the image. It is also interesting to note the effect of different quantization matrices; use of $Q_{10}$ would give $C$ significantly more zeros, while $Q_{90}$ would result in very few zeros.

## Coding

The quantized matrix $C$ is now ready for the final step of compression. Before storage, all coefficients of $C$ are converted by an encoder to a stream of binary data ( $01101011 \ldots$ ). In-depth coverage of the coding process is beyond the scope of this article. However, we can point out one key aspect that the reader is sure to appreciate. After quantization, it is quite common for most of the coefficients to equal zero. JPEG takes advantage of this by encoding quantized coefficients in the zig-zag sequence shown in Figure 1. The advantage lies in the consolidation of relatively large runs of zeros, which compress very well. The sequence in Figure $1(4 x 4)$ continues for the entire $8 x 8$ block.


Figure 1

## Decompression

Reconstruction of our image begins by decoding the bit stream representing the quantized matrix $C$. Each element of $C$ is then multiplied by the corresponding element of the quantization matrix originally used.

$$
\begin{equation*}
R_{i, j}=Q_{i, j} \times C_{i, j} \tag{7}
\end{equation*}
$$

$$
R=\left[\begin{array}{cccccccc}
160 & 44 & 20 & 80 & 24 & 0 & 0 & 0 \\
36 & 108 & 14 & 38 & 26 & 0 & 0 & 0 \\
-98 & -65 & 16 & -48 & -40 & 0 & 0 & 0 \\
-42 & -85 & 0 & -29 & 0 & 0 & 0 & 0 \\
-36 & 22 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0
\end{array}\right]
$$

The IDCT is next applied to matrix $R$, which is rounded to the nearest integer. Finally, 128 is added to each element of that result, giving us the decompressed JPEG version $N$ of our original $8 \times 8$ image block $M$.

$$
N=\operatorname{round}\left(T^{\prime} R T\right)+128
$$

## Comparison of Matrices

Let us now see how the JPEG version of our original pixel block compares.

$$
\begin{array}{r}
\text { Original }=\left[\begin{array}{llllllll}
154 & 123 & 123 & 123 & 123 & 123 & 123 & 136 \\
192 & 180 & 136 & 154 & 154 & 154 & 136 & 110 \\
254 & 198 & 154 & 154 & 180 & 154 & 123 & 123 \\
239 & 180 & 136 & 180 & 180 & 166 & 123 & 123 \\
180 & 154 & 136 & 167 & 166 & 149 & 136 & 136 \\
128 & 136 & 123 & 136 & 154 & 180 & 198 & 154 \\
123 & 105 & 110 & 149 & 136 & 136 & 180 & 166 \\
110 & 136 & 123 & 123 & 123 & 136 & 154 & 136
\end{array}\right] \\
\text { Decompressed }=\left[\begin{array}{llllllll}
149 & 134 & 119 & 116 & 121 & 126 & 127 & 128 \\
204 & 168 & 140 & 144 & 155 & 150 & 135 & 125 \\
253 & 195 & 155 & 166 & 183 & 165 & 131 & 111 \\
245 & 185 & 148 & 166 & 184 & 160 & 124 & 107 \\
188 & 149 & 132 & 155 & 172 & 159 & 141 & 136 \\
132 & 123 & 125 & 143 & 160 & 166 & 168 & 171 \\
109 & 119 & 126 & 128 & 139 & 158 & 168 & 166 \\
111 & 127 & 127 & 114 & 118 & 141 & 147 & 135
\end{array}\right]
\end{array}
$$

This is a remarkable result, considering that nearly $70 \%$ of the DCT coefficients were discarded prior to image block decompression/reconstruction. Given that similar results will occur with the rest of the blocks that constitute the entire image, it should be no surprise that
the JPEG image will be scarcely distinguishable from the original. Remember, there are 256 possible shades of gray in a black-and-white picture, and a difference of, say, 10 , is barely noticeable to the human eye.

## Pepper Example

We can do the DCT and quantization process on the peppers image.


Figure 2 - Peppers
Each eight by eight block is hit with the DCT, resulting in the image shown in Figure 3.


Figure 3 - DCT of Peppers
Each element in each block of the image is then quantized using a quantization matrix of quality level 50. At this point many of the elements become zeroed out, and the image takes up much less space to store.


Figure 4 - Quantized DCT of Peppers
The image can now be decompressed using the inverse discrete cosine transform. At quality level 50 there is almost no visible loss in this image, but there is high compression. At lower quality levels, the quality goes down by a lot, but the compression does not increase very much.


Figure 5 - Original Peppers


Figure 6 - Quality $50-84 \%$ Zeros


Figure 7 - Quality 20 - 91\% Zeros


Figure 8 - Quality $10-94 \%$ Zeros

## More Examples

We can see what the compression does to other images. High contrast images, or images with a lot of high frequencies do not compress as well as smooth, low frequency images.


Figure 9 - Original


Figure 10 - Quality 15 - 90\% Zeros


Figure 11 - Original


Figure 12 - Quality 15 - 88\% Zeros

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# Image Coding Using Wavelet Transform 

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#### Abstract

Image compression is now essential for applications such as transmission and storage in data bases. This paper proposes a new scheme for image compression taking into account psychovisual features both in the space and frequency domains; this new method involves two steps. First, we use a wavelet transform in order to obtain a set of biorthogonal subclasses of images; the original image is decomposed at different scales using a pyramidal algorithm architecture. The decomposition is along the vertical and horizontal directions and maintains constant the number of pixels required to describe the image. Second, according to Shannon's rate distortion theory, the wavelet coefficients are vector quantized using a multiresolution codebook. Furthermore, to encode the wavelet coefficients, we propose a noise shaping bit allocation procedure which assumes that details at high resolution are less visible to the human eye. Finally, in order to allow the receiver to recognize a picture as quickly as possible at minimum cost, we present a progressive transmission scheme. It is shown that the wavelet transform is particularly well adapted to progressive transmission.


Keywords-Wavelet, biorthogonal wavelet, multiscale pyramidal algorithm, vector quantization, noise shaping, progressive transmission.

## I. Introduction

IN many different fields, digitized images are replacing conventional analog images as photograph or x-rays. The volume of data required to describe such images greatly slow transmission and makes storage prohibitively costly. The information contained in the images must, therefore, be compressed by extracting only the visible elements, which are then encoded. The quantity of data involved is thus reduced substantially.

A fundamental goal of data compression is to reduce the bit rate for transmission or storage while maintaining an acceptable fidelity or image quality. Compression can be achieved by transforming the data, projecting it on a basis of functions, and then encoding this transform. Because of the nature of the image signal and the mechanisms of human vision, the transform used must accept nonstationarity and be well localized in both the space and frequency domains. To avoid redundancy, which hinders compression, the transform must be at least biorthogonal and lastly, in order to save CPU time, the corresponding algorithm must be fast. The two-dimensional wavelet transform defined by Meyer and Lemarié [31], [24], [25],

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together with its implementation as described by Mallat [27], satisfies each of these conditions.
The compression method we have developed associates a wavelet transform and a vector quantization coding scheme. The wavelet coefficients are coded considering a noise shaping bit allocation procedure. This technique exploits the psychovisual as well as statistical redundancies in the image data, enabling bit rate reduction.

Section II describes the wavelet transforms used in this paper. After a quick review of wavelets in general, we explain in more detail the properties and construction of regular biorthogonal wavelet bases. We then extend this one-dimensional construction to a two-dimensional scheme with separable filters. The new coding scheme is next presented in Section III. We focus particularly in this section on the statistical properties of wavelet coefficients, on the asymptotic coding gain that can be achieved using vector quantization in the subimages, and on the optimal allocation across the subimages. Experimental results are given in Section IV for images taken within and outside of the training set.

## II. Wavelets

## A. A Short Review of Wavelet Analysis

Wavelets are functions generated from one single function $\psi$ by dilations and translations

$$
\psi^{a . b}(t)=|a|^{-1 / 2} \psi\left(\frac{t-b}{a}\right)
$$

(For this introduction we assume $t$ is a one-dimensional variable). The mother wavelet $\psi$ has to satisfy $\int d x \psi(x)=0$, which implies at least some oscillations. (Technically speaking, the condition on $\psi$ should be $\int d \omega|\Psi(\omega)|^{2}|\omega|^{-1}<\infty$, where $\Psi$ is the Fourier transform of $\psi$; if $\psi(t)$ decays faster than $|t|^{-1}$ for $t \rightarrow \infty$, then this condition is equivalent to the one above). The definition of wavelets as dilates of one function means that high frequency wavelets correspond to $a<1$ or narrow width, while low frequency wavelets have $a>1$ or wider width.

The basic idea of the wavelet transform is to represent any arbitrary function $f$ as a superposition of wavelets. Any such superposition decomposes $f$ into different scale levels, where each level is then further decomposed with a resolution adapted to the level. One way to achieve such a decomposition writes $f$ as an integral over $a$ and $b$ of $\psi^{a, b}$ with appropriate weighting coefficients [22]. In practice, one prefers to write $f$ as a discrete superposition (sum rather than integral). Therefore, one introduces a discre-
tization, $a=a_{0}^{m}, b=n b_{0} a_{0}^{m}$, with $m, n \in \mathbb{Z}$, and $a_{0}>1$, $b_{0}>0$ fixed. The wavelet decomposition is then

$$
\begin{equation*}
f=\sum c_{m, n}(f) \psi_{m, n} \tag{1}
\end{equation*}
$$

with $\psi_{m, n}(t)=\psi^{a_{0}^{m}, n b_{0} a_{0}^{m}}(t)=a_{0}^{-m / 2} \psi\left(a_{0}^{-m} t-n b_{0}\right)$. Decompositions of this type were studied in [14], [15]. For $a_{0}=2, b_{0}=1$ there exist very special choices of $\psi$ such that the $\psi_{m, n}$ constitute an orthonormal basis, so that

$$
c_{m, n}(f)=\left\langle\psi_{m, n}, f\right\rangle=\int d x \psi_{m, n}(x) f(x)
$$

in this case. Different bases of this nature were constructed by Stromberg [36], Meyer [31], Lemarié [24], Battle [7], and Daubechies [16]. All these examples correspond to a multiresolution analysis, a mathematical tool invented by Mallat [27], which is particularly well adapted to the use of wavelet bases in image analysis, and which gives rise to a fast computation algorithm.
In a multiresolution analysis, one really has two functions: the mother wavelet $\psi$ and a scaling function $\phi$. One also introduces dilated and translated versions of the scaling function, $\phi_{m, n}(x)=2^{-m / 2} \phi\left(2^{-m} x-n\right)$. For fixed $m$, the $\phi_{m, n}$ are orthonormal. We denote by $V_{m}$ the space spanned by the $\phi_{m, n}$; these spaces $V_{m}$ describe successive approximation spaces, $\cdots V_{2} \subset \mathrm{~V}_{1} \subset \mathrm{~V}_{0} \subset \mathrm{~V}_{-1} \subset \mathrm{~V}_{-2}$ $\cdots$, each with resolution $2^{m}$. For each $m$, the $\psi_{m, n}$ span a space $W_{m}$ which is exactly the orthogonal complement in $V_{m-1}$ of $V_{m}$; the coefficients $\left\langle\psi_{m, n}, f\right\rangle$, therefore, describe the information lost when going from an approximation of $f$ with resolution $2^{m-1}$ to the coarser approximation with resolution $2^{m}$. All this is translated into the following algorithm for the computation of the $c_{m, n}(f)=\left\langle\psi_{m, n}, f\right\rangle$ (for more details, see [27]):

$$
\begin{align*}
& c_{m, n}(f)=\sum_{k} g_{2 n-k} a_{m-1, k}(f) \\
& a_{m, n}(f)=\sum_{k} h_{2 n-k} a_{m-1, k}(f) \tag{2}
\end{align*}
$$

where $g_{l}=(-1)^{l} h_{-l+1}$ and $h_{n}=2^{1 / 2} \int d x \phi(x-n) \phi(2 x)$. In fact the $a_{m, n}(f)$ are coefficients characterizing the projection of $f$ onto $V_{m}$. If the function $f$ is given in sampled form, then one can take these samples for the highest order resolution approximation coefficients $a_{0, n}$, and (2) describes a subband coding algorithm on these sampled values, with low-pass filter $h$ and high-pass filter $g$. Because of their association with orthonormal wavelet bases, these filters give exact reconstruction, i.e.:

$$
\begin{equation*}
a_{m-1, l}(f)=\sum_{n}\left[h_{2 n-l} a_{m, n}(f)+g_{2 n-l} c_{m, n}(f)\right] . \tag{3}
\end{equation*}
$$

Most of the orthonormal wavelet bases have infinitely supported $\psi$, corresponding to filters $h$ and $g$ with infinitely many taps. The construction in [16] gives $\psi$ with finite support, and therefore, corresponds to FIR filters. It follows that the orthonormal bases in [16] correspond to a subband coding scheme with exact reconstruction property, using the same FIR filters for reconstruction as
for decomposition. Such filters are well known since the work of Smith and Barnwell [35] and of Vetterli [37]. The extra ingredient in the orthonormal wavelet decomposition is that it writes the signal to be decomposed as a superposition of reasonably smooth elementary building blocks. The filters must satisfy the additional condition:

$$
\prod_{k=1}^{\infty} H\left(2^{-k} \xi\right)
$$

decay faster than $C(1+|\xi|)^{-\epsilon-0.5}$ as $|\xi| \rightarrow \infty$, for some $\epsilon>0$, where

$$
H(\xi)=2^{-1 / 2} \sum_{n} h_{n} e^{-j n \xi} .
$$

This extra regularity requirement is usually not satisfied by the exact reconstruction filters in the ASSP literature.

## B. Applications of Wavelet Bases to Image Analysis

1) Biorthogonal Wavelet Bases: Since images are mostly smooth (except for occasional edges) it seems appropriate that an exact reconstruction subband coding scheme for image analysis should correspond to an orthonormal basis with a reasonably smooth mother wavelet. In order to have fast computation, the filters should be short (short filters lead to less smoothness, however, so they cannot be too short). On the other hand it is desirable that the FIR filters used be linear phase, since such filters can be easily cascaded in pyramidal filter structures without the need for phase compensation. Unfortunately, there are no nontrivial orthonormal linear phase FIR filters with the exact reconstruction property [35], regardless of any regularity considerations. The only symmetric exact reconstruction filters are those corresponding to the Haar basis, i.e., $h_{0}=h_{1}=2^{1 / 2}$ and $g_{0}=-g_{1}=2^{1 / 2}$, with all other $h_{n}, g_{n}=0$.

One can preserve linear phase (corresponding to symmetry for the wavelet) by relaxing the orthonormality requirement, and using biorthogonal bases. It is then still possible to construct examples where the mother wavelets have arbitrarily high regularity.
In such a scheme, we still decompose as in (2), but reconstruction becomes

$$
\begin{equation*}
a_{m-1, l}(f)=\sum_{n}\left[\tilde{h_{2 n-l}} a_{m, n}(f)+\tilde{g}_{2 n-l} c_{m, n}(f)\right] \tag{4}
\end{equation*}
$$

where the filters $\tilde{h}, \tilde{g}$ may be different from $h, g$. In order to have exact reconstruction, we impose:

$$
\begin{align*}
& \tilde{g}_{n}=(-1)^{n} h_{-n+1}  \tag{5}\\
& g_{n}=(-1)^{n} \tilde{h}_{-n+1}
\end{align*} \sum_{n} h_{n} \tilde{h}_{n+2 k}=\delta_{k, 0} .
$$

So far, we have not performed anything differently from the usual exact reconstruction subband coding schemes with synthesis filters different from the decomposition filters. If the filters satisfy the additional condition that:

$$
\begin{equation*}
\prod_{k=1}^{\infty} \tilde{H}\left(2^{-k} \xi\right) \text { and } \prod_{k=1}^{\infty} H\left(2^{-k} \xi\right) \tag{6a}
\end{equation*}
$$

decay faster than $C(1+|\xi|)^{-\epsilon-0.5}$ as $|\xi| \rightarrow \infty$, for some $\epsilon>0$, where

$$
\begin{equation*}
\tilde{H}(\xi)=2^{-1 / 2} \sum_{n} \tilde{h}_{n} e^{-j n \xi} \quad H(\xi)=2^{-1 / 2} \sum_{n} h_{n} e^{-j n \xi} \tag{6b}
\end{equation*}
$$

then we can give the following interpretation to (2) and (4). Define functions $\phi$ and $\tilde{\phi}$ by

$$
\phi(x)=\sum_{n} h_{n} \phi(2 x-n) \quad \text { and } \quad \tilde{\phi}(x)=\sum_{n} \tilde{h_{n}} \tilde{\phi}(2 x-n)
$$

Their Fourier transforms are exactly the infinite products (6a), and they are, therefore, well-defined square integrable functions, compactly supported if the filters $h$ and $\hat{h}$ are FIR. Define also

$$
\psi(x)=\sum_{n} g_{n} \phi(2 x-n) \quad \text { and } \quad \tilde{\psi}(x)=\sum_{n} \tilde{g}_{n} \tilde{\phi}(2 x-n) .
$$

Then, the $a_{m, n}(f)$ and $c_{m, n}(f)$ in (2) can be rewritten as:

$$
\begin{aligned}
& a_{m, n}(f)=\left\langle\phi_{m, n}, f\right\rangle=2^{-m / 2} \int d x \phi_{m, n}(x) f(x) \\
& c_{m, n}(f)=\left\langle\psi_{m, n}, f\right\rangle=2^{-m / 2} \int d x \psi_{m, n}(x) f(x)
\end{aligned}
$$

and reconstruction is simply:

$$
\begin{equation*}
f=\sum_{m, n}\left\langle\psi_{m, n}, f\right\rangle \tilde{\psi}_{m, n} . \tag{7}
\end{equation*}
$$

The filter bank structure with the associating wavelets and scaling functions is depicted on the following subband coding scheme (Fig. 1).

If the infinite products in (6a) decay even faster than imposed above, then $\phi$ and $\tilde{\phi}$ and consequently $\psi$ and $\tilde{\psi}$ will be reasonably smooth. Note that (7) is very similar to the orthonormal decomposition described in Section II-A; the only difference is that the expansion of $f$ with respect to the basis $\tilde{\psi}_{m, n}$ uses coefficients computed via the dual basis $\psi_{m, n}$ with $\tilde{\psi}$ different from $\psi$. This interpretation is not possible for all exact reconstruction subband coding schemes; in particular, convergence of the infinite products (6a) is only possible if

$$
\sum_{n} h_{n}=2^{1 / 2} \text { and } \sum_{n} \tilde{h}_{n}=2^{1 / 2}
$$

Moreover, (7) can only hold if

$$
\sum_{n}(-1)^{n} h_{n}=0 \text { and } \sum_{n}(-1)^{n} \tilde{h}_{n}=0 .
$$

Most exact reconstruction subband coding schemes do not satisfy these conditions.

Biorthogonal bases of wavelets have recently been constructed, with regularity simultaneously but independently, by Cohen, Daubechies and Feauveau [12] and by Herley and Vetterli [38]. Reference [12] contains a detailed mathematical study, with proofs that, under the conditions stated above, the wavelets do indeed constitute numerically stable bases (Riesz bases) and a discussion of necessary and sufficient conditions for regularity. In [18]


Fig. 1. Filter bank structure and the associating wavelets.

Feauveau explores the construction from the point of view of multiresolution spaces rather than from the filters. Basically one has two hierarchies of spaces in the biorthogonal case, each corresponding to one pair of filters.

It is shown in [12] that arbitrarily high regularity can be achieved by both $\psi$ and $\tilde{\psi}$, provided one chooses sufficiently long filters. In particular, if the functions $\psi$ and $\tilde{\psi}$ are, respectively, $(k-1)$ and ( $\tilde{k}-1$ ) times continuously differentiable, then the trigonometric polynomials $H(\xi)$ and $\tilde{H}(\xi)$ have to be divisible by $\left(1+e^{-j \xi}\right)^{k}$ and $\left(1+e^{-j \xi}\right)^{k}$, respectively, so that the length of the corresponding filters $h, \tilde{h}$ has to exceed $k, \tilde{k}$.

By (5), divisibility of $\tilde{H}(\xi)$ by $\left(1+e^{-j \xi}\right)^{k}$ means that $\psi$ will have $\tilde{k}$ consecutive moments zero:

$$
\int d x x^{\prime} \psi(x)=0, \quad \text { for } \quad l=0,1, \cdots, \tilde{k}-1
$$

For more details concerning this discussion, see [12].
It is well known (and it can easily be checked by using Taylor expansions) that if $\psi$ has $\tilde{k}$ moments zero, then the coefficients $\left\langle\psi_{m . n}, f\right\rangle$ will represent functions $f$, which are $\tilde{k}$ times differentiable, with a high compression potential (many coefficients will be negligibly small).

Many examples of biorthogonal wavelet bases with reasonably regular $\psi$ and $\tilde{\psi}$ can be constructed; for our applications, the regularity of the elementary building blocks $\tilde{\psi}_{m, n}$, which is linked to the number of zero moments of $\psi$, is more important than the regularity of the $\psi_{m, n}$ or the number of zero moments of $\tilde{\psi}$. Within the limits imposed by the support widths, we will, therefore, try to choose $\tilde{k}$ as large as possible.

In terms of trigonometric polynomials $H(\xi)$ and $\tilde{H}(\xi)$, the exact reconstruction requirement condition on $h$ and $\tilde{h}$ given in (5) reduces to (for symmetric filters)

$$
\begin{equation*}
H(\xi) \tilde{H}(\xi)+H(\xi+\pi) \tilde{H}(\xi+\pi)=1 \tag{8}
\end{equation*}
$$

Together with divisibility of $H$ and $\tilde{H}$, respectively, by $\left(1+e^{-j \xi}\right)^{k}$ and $\left(1+e^{-j \xi}\right)^{k}$, this leads to (see [12])

$$
\left.\begin{array}{rl}
H(\xi) \tilde{H}(\xi)= & \cos (\xi / 2)^{2 i}\left[\begin{array}{c}
l-1 \\
\sum_{p=0}^{l-1}\binom{l-p}{p} \\
\end{array}\right) \cdot \sin (\xi / 2)^{2 p}+\sin (\xi / 2)^{2 l} R(\xi)
\end{array}\right]
$$

where $R(\xi)$ is an odd polynomial in $\cos (\xi)$, and where $2 l=k+\bar{k}$ (symmetry of $h$ and $\bar{h}$ forces $k+\bar{k}$ to be even).

TABLE I

| Filter Coefficients for the Spline Filters with $l=3, k=4, \tilde{k}=2$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $n$ | 0 | $\pm 1$ | $\pm 2$ | $\pm 3$ | $\pm 4$ |
| $2^{-1 / 2} h_{n}$ | $45 / 64$ | $19 / 64$ | $-1 / 8$ | $-3 / 64$ | $3 / 128$ |
| $2^{-1 / 2} \tilde{h}_{n}$ | $1 / 2$ | $1 / 4$ | 0 | 0 | 0 |

Many examples are possible. We have studied in particular the following three examples, which belong to three different families.
2) Spline Filters: One can choose, e.g., $R \equiv 0$, with $\tilde{H}(\xi)=\cos (\xi / 2)^{k} e^{-j \kappa \xi / 2}$ where $\kappa=0$ if $\tilde{k}$ is even, $\kappa=1$ if $\tilde{k}$ is odd. This corresponds to the filters called "spline filters' ${ }^{\text {in [12] (because the corresponding function } \tilde{\phi} \text { is }}$ a $B$-spline function) or 'binomial filters'" in [38] (because the $\bar{h}$ are simply binomial coefficients). It then follows that:

$$
\begin{align*}
H(\xi)= & \cos (\xi / 2)^{2 l-\hat{k}} e^{j \kappa \xi / 2} \\
& \cdot\left[\sum_{p=0}^{l-1}\binom{l-1+p}{p} \sin (\xi / 2)^{2 p}\right] . \tag{10}
\end{align*}
$$

We have looked at one example from this family; it corresponds to $l=3, \tilde{k}=2$. The coefficients $h_{n}$ and $\tilde{h}_{n}$ are listed in Table I; the corresponding scaling functions and wavelets are plotted in Fig. 2.

It is clear that the two filters in the first example have very uneven length. This is typical for all the examples in this family of "spline filters."
3) A Spline Variant with Less Dissimilar Lengths: This family still uses $R \equiv 0$ in (9), but factorizes the righthand side of (9), breaking up the polynomial of degree $l-1$ in $\sin (\xi / 2)$ into a product of two polynomials in $\sin (\xi / 2)$ with real coefficients, one to be allocated to $H$, the other to $\tilde{H}$, so as to make the lengths of $h$ and $\tilde{h}$ as close as possible.

The example presented here is the "smallest" one in this family (shortest $h$ and $\tilde{h}$ ); it corresponds to $l=4$ and $k=4$. The filter coefficients are listed in Table II; the corresponding scaling functions and wavelets are plotted in Fig. 3.

Note that, unlike examples 1 and 3 where the $2^{-1 / 2} h_{n}$, $2^{-1 / 2} \tilde{h}_{n}$ are rational, the entries in Table II are truncated decimal expansions of irrational numbers. The functions $\phi$ in examples 1 and 2 look very similar (compare Figs. 2(a) and 3(a)); a more detailed analysis shows that the one in example 2 is more regular, however. Both correspond to 4 vanishing moments for $\bar{\psi}$.
4) Filters Close to Orthonormal Filters: Finally, there exist many examples for which $R \neq 0$. In particular there exists a special choice of $R$ for which the two filters are very close to each other, and both very close to an orthonormal wavelet filter.

Surprisingly, for the first example of this series, one of the two filters is a Laplacian pyramid filter proposed in [9]. It corresponds to $l=2, k=2$ and $R(\xi)=48 \cos (\xi) / 175$. The filter coefficients are listed in Table III; the corresponding scaling functions and


Fig. 2. Scaling functions $\phi, \tilde{\phi}$ and wavelets $\psi, \tilde{\psi}$ for example 1 (spline filters with $l=3, k=4, \tilde{k}=2$ ). (a) Scaling function $\phi$. (b) Scaling function $\tilde{\phi}$. (c) Wavelet $\psi$. (d) Wavelet $\tilde{\psi}$.
wavelets are plotted in Fig. 4. It is clear that the scaling functions $\phi$ and $\tilde{\phi}$ are very similar, corresponding to very similar $\psi$ and $\tilde{\psi}$. Note that in this case, the filter coefficients are again rational.

TABLE II
Filter Coefficients for the Spline Variant with Less Dissimilar Lengths, with $l=4=k, \tilde{k}=4$

| $n$ | 0 | $\pm 1$ | $\pm 2$ | $\pm 3$ | $\pm 4$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $2^{-1 / 2} h_{n}$ | 0.602949 | 0.266864 | -0.078223 | -0.016864 | 0.026749 |
| $2^{-1 / 2} \hat{h}_{n}$ | 0.557543 | 0.295636 | -0.028772 | -0.045636 | 0 |



Fig. 3. Scaling functions $\phi, \tilde{\phi}$ and wavelets $\psi . \tilde{\psi}$ for example 2 (spline variant with less dissimilar lengths; $l=4=k, k=4$ ). (a) Scaling function $\phi$. (b) Scaling function $\tilde{\phi}$. (c) Wavelet $\psi$. (d) Wavelet $\psi$.

TABLE III
Filter Coefficients for Example 3. The Entries are Rational, and the Two Filters are very Close. The $h$-Filter Coincides with a Laplacian Pyramid Filter Proposed in [9]. In This Case $l=2=k, \tilde{k}=2$

| $n$ | 0 | $\pm 1$ | $\pm 2$ | $\pm 3$ | $\pm 4$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $2^{-1 / 2} h_{n}$ | 0.6 | 0.25 | -0.05 | 0 | 0 |
| $2^{-1 / 2} \tilde{h}_{n}$ | $17 / 28$ | $73 / 280$ | $-3 / 56$ | $-3 / 280$ | 0 |

The two biorthogonal filters in this example are both close to an orthonormal wavelet filter of length 6 constructed in [17], where it was called a '"coiflet." Being an orthonormal wavelet filter, the coiflet is nonsymmetric. The filters in this example are shorter than in examples 1 and 2, but $k$ is also smaller. The next example in this family corresponds to $k=4$ (and $l=4$ ); the filters $h$ and $\tilde{h}$ then have length 9 and 15; they are both close to a coiflet of length 12.
5) Extension to the Two-Dimensional Case: There ex-
ist various extensions of the one-dimensional wavelet transform to higher dimensions. We follow Mallat [27] and use a two-dimensional wavelet transform in which horizontal and vertical orientations are considered preferential.

In two-dimensional wavelet analysis one introduces, like in the one-dimensional case, a scaling function $\phi(x, y)$ such that:

$$
\begin{equation*}
\phi(x, y)=\phi(x) \phi(y) \tag{11}
\end{equation*}
$$

where $\phi(x)$ is a one-dimensional scaling function.
Let $\psi(x)$ be the one-dimensional wavelet associated with the scaling function $\phi(x)$. Then, the three two-dimensional wavelets are defined as:

$$
\begin{align*}
\psi^{H}(x, y) & =\phi(x) \psi(y) \\
\psi^{D}(x, y) & =\psi(x) \phi(y) \\
\psi^{D}(x, y) & =\psi(x) \psi(y) \tag{12}
\end{align*}
$$



Fig. 4. Scaling functions $\phi, \bar{\phi}$ and wavelets $\psi, \bar{\psi}$ for example 3 (biorthogonal filters close to an orthonormal wavelet filter, $l=2=k, \tilde{k}=2$ ). (a) Scaling function $\phi$. (b) Scaling function $\phi$. (c) Wavelet $\psi$. (d) Wavelet $\tilde{\psi}$.


Fig. 5. One stage in a multiscale image decomposition.

Fig. 5 represents one stage in a multiscale pyramidal decomposition of an image: wavelet coefficients of the image are computed, as in the one-dimensional case (Sections II-A and II-B.1), using a subband coding algorithm. The filters $h$ and $g$ are one-dimensional filters. This decomposition provides subimages corresponding to different resolution levels and orientations (see Fig. 6). The reconstruction scheme of the image is presented Fig. 7.

To compare the three different filters presented in this paper, we have decomposed the image Lena (Fig. 16) with each of these filters. The results are presented in Fig. 8.

In Fig. 8(a) we can see the normalized detail subimages at different resolution levels $m=1, m=2$, and $m=3$ (wavelet coefficients) and in Fig. 8(b) the low resolution level subimages.

## III. Image Coding Application

## A. Statistical Properties of Wavelet Coefficients

The performance of a coder used for a given resolution and direction can be determined by the statistics of the corresponding subimage, i.e., its probability density function (PDF).

| $\mathrm{m} \geq 2$ | $\mathrm{m}=2$ | $\mathrm{m}=1$ |
| :---: | :---: | :---: |
| $\underset{\substack{\text { Low resolution } \\ \text { sub-image }}}{ }$ | Resolution $\mathrm{m}=2$ <br> Horizontal orientation sub-image | Resolution $\mathrm{m}=1$ <br> Horizontal orientation sub-image |
| Resolution $m=2$ <br> Vertical orentation sub-image | Resolution $m=2$ <br> Diagonal orientation sub-image |  |
| Resolut Vert orientation | $\mathrm{n}=1$ <br> al <br> sub-image | Resolution $\mathrm{m}=1$ <br> Diagonal <br> orientation sub-image |

Fig. 6. Image decomposition.


Fig. 7. One stage in a multiscale image reconstruction.

A typical PDF and different approximations are given in Fig. 9, where we plot the true PDF for resolution level $m=1$ and direction $d=$ vertical together with three model functions: a Gaussian, a Laplacian, and an intermediate function, the so-called generalized Gaussian [2].
This generalized Gaussian law is given explicitly by

$$
p_{m, d}(x)=a_{m, d} \exp \left(-\left|b_{m, d} x\right| r_{m, d}\right)
$$

with

$$
\begin{equation*}
a_{m d}=\frac{b_{m, d} r_{m, d}}{2 \Gamma\left(\frac{1}{r_{m, d}}\right)} \text { and } b_{m, d}=\frac{1}{\sigma_{m, d}} \frac{\Gamma\left(\frac{3}{r_{m, d}}\right)^{1 / 2}}{\Gamma\left(\frac{1}{r_{m, d}}\right)^{1 / 2}} \tag{13}
\end{equation*}
$$

where $\sigma_{m, d}$ is the standard deviation of the subimage ( $m, d$ ), and $\Gamma(\cdot)$ is the usual Gamma function.
The general formula (13) contains the other two examples as particular cases:

- $r_{m, d}=2$ leads to the well-known Gaussian PDF;
- $r_{m, d}=1$ leads to a Laplacian PDF.

The variance of this approximation model is set equal to the variance of the corresponding subimage. Thus the parameter $r_{m, d}$ is computed in order to match the real PDF using the well-known chi-squared test. In this case the optimum parameter was 0.7 . Other experiments for other resolutions (except the lowest resolution) lead to very similar results.

We can see in Fig. 9 that the real PDF (scale $m=1$ and vertical orientation) is closely approximated by a generalized Gaussian law with parameter $r_{1,{ }^{\prime}}=0.7$.

## B. Encoding of Wavelet Coefficients Using Vector Quantization

Different techniques involving vector or scalar quantization can be used to encode wavelet coefficients.

According to Shannon's rate distortion theory, better results are always obtained when vectors rather than sca-


Fig. 8. Comparison among the different subimages. (a) Comparison among the normalized detail subimages. (b) Comparison among the low resolution level subimages.
lars are encoded. Therefore, the present application uses vector quantization.

1. Principle of Vector Quantization: Developed recently by Gersho and Gray (1980) [20], [21], vector quantization has proven to be a powerful tool for digital image compression [4], [29], [30], [32], [39]. The principle involves encoding a sequence of samples (vector) rather than encoding each sample individually. Encoding is performed by approximating the sequence to be coded by a vector belonging to a catalogue of shapes, usually known as a codebook.

The codebook is created and optimized using the wellknown Linde-Buzo-Gray (LBG) [26] classification al-
gorithm with a mean squared error (MSE) criterion. This algorithm is designed to perform a classification based on a training set comprised of vectors belonging to different images; it converges iteratively toward a locally optimal codebook.

Each of the vectors in the codebook is indexed. At the encoding stage, the index of the vector in the codebook most closely describing (in terms of MSE criterion) the sample set to be encoded is selected to represent this set. Of course, in order to reconstruct the sample set, the decoder must have the same codebook as the coder.

The encoding/decoding scheme depicted in Fig. 10 was proposed in [29] and [30] for orthonormal wavelets.


Fig. 9. Real PDF of subimage at scale $m=1$ for vertical orientation, and
its different approximations


Fig. 10. Encoding/decoding scheme
2) Comparative Performances of Vector Quantization (VQ) and Scalar Quantization (SQ): According to [3], [13], [19], [43], [30] the asymptotic lower bound distortion gain obtained when VQ, rather than SQ, is applied to a subimage is expressed as:

$$
\begin{align*}
G_{m, d}^{V Q} \geq & \frac{2^{-c}}{(c+1) A\left(k_{m, d}, c\right)} \\
& \times \frac{\left[\int\left[p_{m, d}(x)\right]^{1 /(c+1)} d x\right]^{(c+1)}}{\left[\int\left[p_{m, d}(x)\right]^{k_{m, d} /\left(c+k_{m, d}\right)} d x\right]^{\left(c+k_{m, d}\right)}} \tag{14}
\end{align*}
$$

for a subimage corresponding to resolution $m$ and direction $d . p_{m, d}(x)$ is the PDF of wavelet coefficients of the subimage with resolution $m$ and direction $d$.

Here, the MSE criterion is used as a distortion measure ( $c=2$ ). The values of $A\left(k_{m, d}, 2\right)$ used are the upper bounds of the MSE computed and tabulated by Conway and Sloane for vector size $k_{m, d}$ [13]. This formula gives an indication of the minimum theoretical gain that can be obtained.
However, this approximation is valid only for small quantization errors, i.e., for a high bit rate $R_{m, d}$. Thus the gain $G_{m, d}^{\mathrm{VQ}}$ only gives here an asymptotic indication.

In Fig. 11, the curves of $G_{m, d}^{\mathrm{VQ}}$ are plotted as a function of the vector dimension $k_{m . d}$ for the Laplacian, Gaussian,


Fig. 11. Asymptotic lower bound distortion gain $G_{m, d}^{\mathrm{VQ}}=$ function $\left(k_{m, d}\right)$.
and generalized Gaussian approximation laws, and for a subimage at scale $m=1$ and vertical orientation. Experimental results are closely matched by the theoretical results for a generalized Gaussian law with $r_{m, d}=0.7$ except for the lower subband. Therefore, all computations based on this approximation law show that, in each subband, VQ outperforms SQ (see Fig. 11).
In summary VQ performs better for coding wavelet coefficients
3) Generation of a Multiresolution Codebook: The preceding paragraph explained why VQ outperforms other methods. Nonetheless, major problems are encountered in the VQ of images.

- It is impossible to create a universal codebook (efficient for each image to be encoded).
- The LBG algorithm smooths high frequencies (loss of resolution).
- There is a trade-off between low distortion and high compression rate (computational cost).
- It is not easy to take into account the properties of the human visual system [28], [33].

The use of the wavelet transform (i.e., multiresolution) is one way of overcoming these different problems.

The wavelet decomposition of an image enables the generation of a codebook containing two-dimensional vectors for each resolution level and preferential direction (horizontal, vertical, and diagonal). Each of these subcodebooks (see Fig. 12) is generated using the LBG algorithm.

- The training set is comprised of vectors belonging to different images corresponding to the resolution and orientation under consideration.
- The initial codebook is generated by splitting the centroid (center of gravity) of this training set [21].
A multiresolution codebook can thus be obtained by assembling all of these resulting subcodebooks. Each subcodebook has a low distortion level and contains few words, which clearly facilitates the search for the best coding vector; the coding computational load is reduced, because only the appropriate subcodebook (resolution direction) of the multiresolution codebook is checked for each input vector. In addition, the quality of the coded image is better. The multiresolution codebook is depicted in Fig. 12.
Global codebook design has drawbacks in that it results in edge smoothing while the proposed method preserves edges. In fact, each subcodebook contains the shape of the wavelet coefficients which are most highly representative in terms of the MSE criterion.

Since the spatial and frequency aspects of the image are taken into account in the wavelet decomposition, the classification and search during the encoding of a subimage vector can be achieved using a simple criterion such as least mean squares. This frees us from using distortion measurements such as weighted least mean squares or other measurements involving perceptual factors. These algorithms are indeed costly in computation time.

## C. Optimal Bit Allocation

Multiresolution exploits the eye's masking effects, and therefore, enables us to refine and select the type of coding according to the resolution level and the contour orientation. Although a flat noise shape minimizes the MSE criterion, it is generally not optimal for a subjective quality of image. To apply noise shaping across the VQ subimages, we define a total weighted MSE distortion $D_{T}^{*}\left(R_{T}\right)$ ((17)) for a total bit rate $R_{T}((18))$.

Let us define $D_{m, d}\left(R_{m, d}\right)$ the average distortion in the coding of the subimage ( $m, d$ ) for $R_{m, d}$ bits per pixel:

$$
\begin{equation*}
D_{m, d}\left(R_{m, d}\right)=E\left(|x-q(x)|^{c}\right)=d(x, q(x)) \quad c \geq 1 \tag{15}
\end{equation*}
$$



Fig. 12. Multiresolution codebook
for all coefficients $x$ belonging to the subimage, $q(x)$ being the quantization of $x$.
Total distortion of the image for a total rate of $R_{T}$ bits per pixel is then given by:

$$
\begin{equation*}
D_{T}\left(R_{T}\right)=\frac{1}{2^{2 M}} D_{M}^{\mathrm{SQ}}\left(R_{M}^{\mathrm{SQ}}\right)+\sum_{m=1}^{M} \frac{1}{2^{2 m}} \sum_{d=1}^{3} D_{m, d}\left(R_{m, d}\right) \tag{16}
\end{equation*}
$$

where $D_{M}^{\text {SO }}$ ( $R_{M}^{\text {SO }}$ ) corresponds to the distortion in the subimage of lowest resolution $M$ (texture subimage).
The problem of finding an optimal bit assignment (in bits per pixel) for each subimage vector quantizer is then formulated as:

$$
\begin{align*}
& \operatorname{Min}_{R_{m, d}}[
\end{align*} \quad D_{T}^{*}\left(R_{T}\right)=\frac{1}{2^{2 M}} D_{M}^{\mathrm{SQ}}\left(R_{M}^{\mathrm{SQ}}\right) .
$$

where $R_{M}^{\text {SQ }}$ corresponds to the bit allocation, in bits per pixel, of lowest resolution $M$ subimage.

Assignment of the weights is based on the fact that the human eye is not equally sensitive to signals at all spatial frequencies. On the basis of contrast sensitivity data collected by Campbell and Robson [10], and to obtain a controlled degree of noise shaping across the subimages, we consider a function $B_{m . d}$ such that:

$$
\begin{equation*}
B_{m, d}=\gamma^{m} \log \left(\sigma_{m . d}^{2 \beta_{m, d}}\right) \tag{19}
\end{equation*}
$$

where $\sigma_{m . d}$ is the standard deviation corresponding to subimage ( $m, d$ ) and the values of $\gamma$ and $\beta_{m \cdot d}$ are chosen experimentally in order to match human vision.
$D_{T}^{*}\left(R_{T}\right)$ is the total weighted encoding distortion function, and $M$ is the lowest resolution considered.

The expression of $D_{m . d}\left(R_{m, d}\right)$ is given by [19]

$$
D_{m, d}\left(R_{m, d}\right)=2^{-c R_{m, d}} \times \alpha_{m, d}(p, c), \quad c \geq 1
$$

with

$$
\begin{align*}
\alpha_{m, d}(p, c)= & A\left(k_{m, d}, c\right) \\
& \times\left[\int\left[p_{m, d}(x)\right]^{k_{n, d} /\left(c+k_{m, d}\right)} d x\right]^{\left(c+k_{m, d}\right)} . \tag{20}
\end{align*}
$$

This minimization problem can be solved by using Lagrangian multipliers. Using this technique, we must solve the following equation:

$$
\begin{gather*}
\frac{\partial}{\partial R_{m, d}}\left[D_{T}^{*}\left(R_{T}\right)-\lambda\left(R_{T}-\frac{1}{2^{2 M}} R_{M}^{S Q}\right.\right. \\
\left.\left.\quad-\sum_{m=1}^{M} \frac{1}{2^{2 m}} \sum_{d=1}^{3} R_{m, d}\right)\right]=0 \tag{21}
\end{gather*}
$$

where $\lambda$ is a Lagrangian multiplier.
Using (17) and (20), this equation becomes:

$$
\begin{aligned}
& \frac{\partial}{\partial R_{m, d}}\left[\frac{1}{2^{2 m}} D_{M}^{\mathrm{SQ}}\left(R_{M}^{\mathrm{SQ}}\right)\right. \\
& \quad+\sum_{m=1}^{M} \frac{1}{2^{2 m}} \sum_{d=1}^{3}\left(2^{-c R_{m . d}} \alpha_{m, d}(p, c) B_{m \cdot d}\right) \\
& \left.\quad-\lambda\left(R_{T}-\frac{1}{2^{2 M}} R_{M}^{\mathrm{SQ}}-\sum_{m=1}^{M} \frac{1}{2^{2 m}} \sum_{d=1}^{3} R_{m, d}\right)\right]=0
\end{aligned}
$$

Taking the partial derivative with respect to $R_{m, d}$ yields an expression for $R_{m, d}$ in terms of $\lambda$ :

$$
\begin{equation*}
R_{m, d}=\frac{1}{c} \log _{2}\left[\frac{(c \ln 2) \alpha_{m, d}(p, c) B_{m, d}}{\lambda}\right] . \tag{23}
\end{equation*}
$$

By substituting (23) into the constraint (18) of the minimization problem we obtain an expression of the Lagrangian multiplier $\lambda$

$$
\begin{align*}
\lambda= & c \ln 2\left[2^{-c\left(R_{T}-\left(1 / 4^{M}\right) R_{M}^{\mathrm{SQ}}\right)} \prod_{m=1}^{M} \prod_{d=1}^{3}\right. \\
& \left.\cdot\left[\alpha_{m, d}(p, c) B_{m, d}\right]^{1 / 4^{m}}\right]^{4^{M / 4^{M-1}}} \tag{24}
\end{align*}
$$

Finally, substituting $\lambda$ into (23) results in an expression of the optimal bit assignment $R_{m, d_{p p}}$ (in bits per pixel (bpp)) to the vector quantizer of subimage ( $m, d$ ):

$$
\begin{equation*}
R_{m, d_{0 p x}}=\frac{4^{M} R_{T}-R_{M}^{S 0}}{4^{M}-1}+\frac{1}{c} \log _{2}\left[\frac{\alpha_{m, d}(p, c) B_{m, d}}{\left[\prod_{m^{\prime}=1}^{M} \prod_{d^{\prime}=1}^{3}\left[\alpha_{m^{\prime}, d^{\prime}}(p, c) B_{m^{\prime} \cdot d^{\prime}}\right]^{1 / 4^{\prime} 1^{4} / 4^{M}-1}\right.}\right] . \tag{25}
\end{equation*}
$$

This expression requires the knowledge of the subimage's PDF's.
The optimal distortion of the quantizer, $D_{T_{\text {tp }}}^{*}\left(R_{T}\right)$, is then computed by combining (25) and (17). We find:

$$
\begin{align*}
D_{T_{\mathrm{opt}}}^{*}\left(R_{T}\right)= & \frac{1}{2^{2 M}} D_{M}^{\mathrm{SQ}}\left(R_{M}^{\mathrm{SQ}}\right)+\frac{4^{M}-1}{4^{M}} 2^{-c\left(4^{M} R_{T}-R_{M}^{\mathrm{SO}}\right) / 4^{M}-1} \\
& \cdot\left[\prod_{m=1}^{M} \sum_{d=1}^{3}\left[\alpha_{m . d}(p, c) \bar{B}_{m, d}\right]^{1 / 4^{m}}\right]^{4^{M /} / 4^{M}-1} \tag{26}
\end{align*}
$$

Finally, bit allocation which is a function of the image will be transmitted as side information requiring only a few bits.

## IV. Experimental Results

The images used are sampled 256 by 256 black and white images. The intensity of each pixel is coded on 256 grey levels ( 8 bpp ).

The numerical evaluation of the coder's performance is achieved by computing the peak signal-to-noise ratio (PSNR) between the original image and the coded image.

For each coded image, we can use a variable length code. We also give the corresponding $\mathbb{R}_{T}$ if an optimal entropy coding was performed, defined as follows.

To the $L$ codewords $w_{j} ; j=1,2, \cdots, L$ of the vector quantizer corresponds to $L$ regions (clusters) of $\mathbb{R}^{k}$, $\mathscr{P}_{j} ; j=1,2, \cdots, L$. The $j$ th region is defined by

$$
\mathscr{O}_{j}=\left\{x \in \mathbb{R}^{k} / Q(x)=w_{j}\right\}
$$

and represents the subset of vectors of $\mathbb{R}^{k}$ which are well matched by the codeword $w_{j}$ of the codebook.

Thus for each resolution and direction, we can introduce the average information of the codebook, called the entropy measure:

$$
\begin{equation*}
\mathfrak{R}_{m . d}=-\frac{1}{k_{m, d}} \times \sum_{j=1}^{L} p\left(w_{j}\right) \log _{2} p\left(w_{j}\right) \text { bpp } \tag{22}
\end{equation*}
$$

where $p\left(w_{j}\right)$ is the probability of selecting the source vector $w_{j}$, belonging to the codebook at scale $m$ and corresponding to the orientation $d$, during the coding of the image ( $m, d$ ).

Then, as in (18), $\mathscr{R}_{T}$ is the sum of the estimated entropy in each subimage as follows:

$$
\mathfrak{R}_{T}=\frac{1}{2^{2 M}} \mathfrak{R}_{M}^{S Q}+\sum_{m=1}^{M} \frac{1}{2^{2 m}} \sum_{d=1}^{3} \mathfrak{R}_{m, d} \mathrm{bpp}
$$

The vector quantizer used is a full search quantizer, i.e., during the coding, all of the vectors in the subcodebook corresponding to the resolution and direction to be encoded are searched. The selection criterion used is the MSE criterion.

## A. Comparison Between the Different Wavelets

In the following, we present results obtained with the Lena image (image within the training set) for a real bit rate of 1 bpp and using the three different filters proposed in Section II-B. (Fig. 13 corresponds to filters 9-3 presented in example 1, Fig. 14 corresponds to filters $9-7$ presented in example 2, and Fig. 15 corresponds to filters 5-7 presented in example 3.) Here, the Lena image is taken as part of the training set in order to minimize the effects of quantization noise: this enables the influence of the filters to be taken into account.

For a given set of filters, separate codebooks are trained for each resolution-orientation subimage, and bit alloca-


Fig. 13. Filters no. 19-3, $\operatorname{PSNR}=31.82 \mathrm{~dB}, \boldsymbol{R}_{T}=0.80 \mathrm{bpp}$.


Fig. 14. Filters no. 2, 9-7, $\operatorname{PSNR}=32.10 \mathrm{~dB}, \mathbb{R}_{T}=0.78 \mathrm{bpp}$.
tion is carried out according to (25). For the Lena image, the bit assignment is represented in Fig. 17. Resolution 1 (diagonal orientation) is discarded. Resolution 1 (horizontal and vertical orientations) and resolution 2 (diagonal orientation) are coded using 256 -vector codebooks (codeword size 4 by 4 ) resulting in a $0.5-\mathrm{b} /$ pixel rate, while resolution 2 (horizontal and vertical orientations) is coded at a $2-\mathrm{b} /$ pixel rate using 256 -vector codebooks


Fig. 15. Filters no. 3, 5-7, $\operatorname{PSNR}=31.46 \mathrm{~dB}, \mathbb{R}_{T}=0.80 \mathrm{bpp}$.


Fig. 16. Original 256 by 256 Lena, 8 bpp.
(codeword size 2 by 2). Finally, the lowest resolution is coded at $8 \mathrm{~b} /$ pixel.

## B. Results as a Function of Regularity and Vanishing <br> Moments

In Section II-B, we mentioned our belief that both the regularity of the reconstruction wavelet $\tilde{\psi}$ and the number

| $\mathrm{m} \geq 2$ | $\mathrm{m}=2$ | $\mathrm{m}=1$ |
| :---: | :---: | :---: |
| Texture <br> 8 bpp <br> Scalar <br> Quantization | $\begin{array}{\|c\|} \hline 2 \mathrm{bpp} \\ \mathrm{~N}=256 \\ \text { Size } 2 \times 2(\mathrm{k}=4) \\ \mathrm{VQ} \end{array}$ | Horizontal orientation $0.5 \mathrm{bpp}$ |
| $\begin{gathered} 2 \mathrm{bpp} \\ \mathrm{~N}=256 \\ \text { Size } 2 \times 2(\mathrm{k}=4) \\ \mathrm{VQ} \end{gathered}$ | $\begin{array}{\|c\|} 0.5 \mathrm{bpp} \\ \mathrm{~N}=256 \\ \text { Size } 4 \times 4(\mathrm{k}=16) \\ \mathrm{VQ} \end{array}$ | Size $4 \times 4$ ( $k=16$ ) VQ |
| Vertical orientation <br> 0.5 bpp <br> $\mathrm{N}=256$ codewords <br> Size $4 \times 4$ ( $k=16$ ) <br> VQ |  | Diagonal orientation |
|  |  | 0 bpp |
| Same bit rate |  |  |

Fig. 17. Subimages bit rate allocation: example of a bit allocation for a total bit rate of 1 bpp and for the 256 by 256 Lena image.
of vanishing moments of the analyzing wavelet $\psi$ are important in applications. To illustrate this we carried out the following experiments. For a given pair, $h, \bar{h}$, we analyzed the same image twice: once as described above, and a second time after exchanging the roles of the filters $h$ and $\tilde{h}$.

The filter pairs in example 2 both have the same number of vanishing moments, $k=\tilde{k}=4$. However, $\tilde{\psi}$ is considerably more regular than $\psi$ (see Fig. 3). With this filter pair, our experiment on the Lena image led to a PSNR of 32.10 dB in the first case, and to a PSNR of 31.51 dB if the roles of $h$ and $\bar{h}$ are inverted. The case where the reconstruction wavelet has the highest regularity, therefore, performs best.
In example 1 the functions $\psi$ and $\psi$ have comparable regularity: both are continuous and neither has a continuous derivative. In fact $\tilde{\psi}$ is a bit more regular than $\psi: \tilde{\psi}$ is differentiable almost everywhere, and is Hölder continuous with exponent 1 , while $\psi$ is Hölder continuous with the exponent only at 0.83 . On the other hand, $\psi$ has 2 vanishing moments, while $\tilde{\psi}$ has $4(k=4, \tilde{k}=2)$. The same experiment, again with the Lena image, now leads to a PSNR of 31.82 dB if $h, \tilde{h}$ are taken as in Table I, and to a PSNR of 31.13 dB when the roles of $h$ and $\tilde{h}$ are reversed. The situation where $\tilde{\psi}$ is most regular but $\psi$ has fewer vanishing moments, therefore, performs better (gain of 0.69 dB ) than the case where $\psi$ has more vanishing moments but $\tilde{\psi}$ is less regular. This seems to suggest that the regularity of $\tilde{\psi}$ has a larger effect than the number of vanishing moments of $\psi$. However, in this example the difference in overall regularity, as measured by the differences between Hölder exponents, is much smaller here
than in example 2 ( 0.17 as compared to 0.63 in example 2 ), and it seems hard to explain how this smaller difference in Hölder exponent could account for a comparable gain in PSNR. In fact, the Hölder exponent is not a very good measure for the regularity of $\tilde{\psi}$ in this case: it is completely determined by the discontinuity of the derivative of $\tilde{\psi}$ in only a few points, and it is insensitive to the fact that $\tilde{\psi}$ is infinitely differentiable in all other points. If this is taken into account, then $\tilde{\psi}$ looks much more regular than $\psi$ (the Hölder exponent of which is determined by its behavior near a dense set of points), which might explain the gain in PSNR.

We conclude from all this that: 1) for the same number of vanishing moments for $\psi$, the scheme with most regular $\tilde{\psi}$ is likely to perform best; and 2 ) increasing the regularity of $\tilde{\psi}$, even at the expense of the number of vanishing moments for $\psi$, may lead to better results.
Based on theoretical arguments (Taylor expansions) and results from numerical analysis [8], we also expect: 3) for comparable regularity of $\bar{\psi}$, the scheme with largest vanishing moments for $\psi$ is likely to perform best.

## C. Comparison with Other Coders

If the PSNR is chosen as a criterion of comparison, these results are close to those obtained by Woods and O'Neil [42] and Westerink et al. [40]. However, in their subband coding algorithm, they use 32 -taps Johnston filters, while only 9 or 7 taps are necessary for our method. According to Westerink's results in [41], the PSNR decreases by about 2 dB when using 8-taps Johnston filters. However, some others new QMF designs can also lead to good results with about 9 taps for image coding [1].

In this section, we present both numerical and qualitative comparison between our coding scheme and other previously published results. Since the most popular image in the recent literature has been the 512 by 512 Lena image, the comparison is made using this image taken outside the training set.

Among the different methods published, we consider the three following well-known methods: Ho and Gersho obtained a $30.93-\mathrm{dB}$ PSNR at 0.36 bpp , result using "variable-rate multi stage VQ" [23]. Riskin and Gray improved on the full search VQ $($ PSNR $=29.29 \mathrm{~dB}, 0.32$ bpp ) using pruned tree structured VQ (PSNR $=30.92 \mathrm{~dB}$, 0.32 bpp ) [34]. High PSNR values were obtained by Woods and Cohen using entropy coded and predictive VQ $($ PSNR $=32.5 \mathrm{~dB}, 0.45 \mathrm{bpp})$ [11].

Our aim is not to optimize the PSNR but rather a weighted function of the MSE in order to match human vision. We give two examples at low bit rate using wavelet VQ.
Our initial result at 0.37 bpp presented Fig. 18 with a 30.85-dB PSNR is very close to those of Ho and Gersho [23] and Riskin et al. [34]. The perceptual quality of our coded images is better than indicated by the PSNR value


Fig. 18. 512 by 512 Lena image. Filters no. 2 9-7, $\mathrm{PSNR}=30.85 \mathrm{~dB}$, $\mathfrak{R}_{T}=0.37 \mathrm{bpp}$.


Fig. 19. 512 by 512 Lena image. Filters no. 29-7, $\operatorname{PSNR}=29.11 \mathrm{~dB}$, $\mathfrak{P}_{T}=0.21 \mathrm{bpp}$.
mainly due to the regularity of the wavelet and the bit allocation. These images do not suffer from the blocking effects obtained when using VQ in the spatial domain. No ringing effects can be observed.

The second result at 0.21 bpp presented in Fig. 19 with a 29.11-dB PSNR shows that a very low bit rate can be achieved with our method, without severe degradation.

Our method using a new class of filters derived from
wavelet theory using full search VQ can be improved by any of the three above-mentioned methods.

In fact the LBG clustering algorithm is a very simple algorithm but not optimal for variable length code. The PSNR of the method could be improved by about 3 dB , for example, using ECVQ [34] but CPU time becomes prohibitively expensive.

## D. Progressive Transmission Scheme

The main objective of progressive transmission is to allow the receiver to recognize a picture as quickly as possible at minimum cost, by sending a low resolution level picture first. Then, it can be decided to receiver further picture details or to abort the transmission. Further details of the picture are obtained by sequentially receiving the encoded wavelet coefficients at different resolution levels and directions.

Following the example of [40], we will display each picture level during the progressive transmission with a size that matches the resolution of that particular level.

To test the efficiency of the vector quantizer, the image to be coded is taken outside the training set.

Fig. 20 represents 5 stages in the progressive transmission of a 256 by 256 image using filters $9-7$ given in example 2. According to the bit allocation procedure (Section III-C) with a generalized Gaussian PDF approximation law, only the wavelet coefficients corresponding to the $m=1$ and $m=2$ high resolution levels are vector quantized, while the low level subimages ( $m \geq 2$ ) are scalar quantized.

## V. Conclusion

This paper describes a new image coding scheme combining the wavelet transform and VQ.

A new family of filters has been derived from the wavelet theory. We have shown the importance of regularity and vanishing moments for image coding. Furthermore, these filters require few taps, unlike standard QMF methods.

The wavelet transform used here attempts to exploit the masking effect of the human eye, yielding encouraging results. Indeed, the proposed method enables high compression bit rates while maintaining good visual quality through the use of bit allocation in the subimages. The blocking effects seen when spatial VQ is performed are ' avoided.

This method is well adapted to progressive transmission as well as very low bit rate compression. Furthermore, using a simple full-search VQ provides good results, comparable to the best results published currently.

Further research should include some new derivation such as entropy constraint and predictive VQ. We would improve this coding scheme, if we accept a heavier computational load.


Fig. 20. Progressive transmission-filters no. 29-7.

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United States Patent
Inga et al.
[54] AUTOMATED HIGH DEFINITION/RESOLUTION IMAGE STORAGE, RETRIEVAL AND TRANSMISSION SYSTEM
[75] Inventors: Jorge J. Inga; Thomas V. Saliga, both of Tampa, Fla.
[73] Assignee: Automated Medical Access
Corporation, Tampa, Fla.
[21] Appl. No.: 915,298
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[51]
Int. Cl. $\qquad$ H04N 1/21; H04N 1/41
[52]
U.S. Cl.

358/403; 358/426;
358/428
[58] Field of Search .................... 358/403, 426, 261.1,
358/444, 428; 395/114
[56]

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ABSTRACT
An automated high definition/resolution image storage retrieval and transmission system for use with medical X-ray film or other documents to provide simultaneous automated access to a common data base by a plurality of remote subscribers upon request, the automated high definition/resolution image storage, retrieval and transmission system comprising an image scanning and digitizing subsystem to scan and digitize visual image information from an image film or the like; an image data storage and retrieval subsystem to receive and store the digitized information and to selectively provide the digitized information upon request from a remote site, a telecommunication subsystem to selectively transmit the requested digitized information from the image data storage and retrieval subsystem to the requesting remote visual display terminal for conversion to a visual image at the remote site to visually display the requested information from the image data storage and retrieval subsystem.

12 Claims, 9 Drawing Sheets




# APPENDIX I 




Fig. 4



## APPENDIX I

5,321,520


Fig. 7


Fig. 8


Fig. 9


Fig. 10


Fig. 11


Fig. 12
Fig. 13

# APPENDIX I 



Fig. $14-A$


Fig. 14-C


Fig. $14-E$


Fig. 14-G


Fig. 14-B


Fig. 14-D


Fig. 14-F


Fig. 14-H
U.S. Pat. No. $5,019,975$ teaches a method for constructing a data base in a medical image filing system comprising the steps or recording information indicating the time at which each medical image is recorded

## BACKGROUND OF THE INVENTION

1. Field of the Invention

An automated high definition/resolution image storage, retrieval and transmission system for use with medical X-ray films and the like.

## 2. Description of the Prior Art

Many industries have their own unique inventory control means for the particular needs of the respective trade. The food industry, for example, has largely standardized on bar-code technology to track food items. The medical profession, however, in many areas has not kept technological pace notwithstanding the obvious need therefor. Storage and retrieval systems for medical image data such as X-ray films, CAT scans, angiograms, tomograms and MRI are commonly antiquated and often employing methods of the 1920 's. For example, when image films are used in the physician must display these photo films on a light box.
Moreover, due to the diffuse responsibilities of multiple attending physicians and treatment sites involving patients with particularly complex conditions, image data for such patients is often misplaced, lost, or at best, difficult to find when needed. Hospitals maintain large "file rooms" to store the patient image data. The film image data is typically stored in a large brown envelope approximately 14 by 17 inches and open at one end. These become bulky to handle and store especially in a complex situation in which several of these folders are needed. Weight alone can build up to 15 pounds. It has proven time consuming to obtain image data from file rooms either due to administrative backlogs, lack of specialized filing personnel and misfiling.

Typically, the physician examines the patient in his office after the radiographical studies have been made in a hospital or diagnostic facility. These films and the information contained therein are often unavailable at the time of the examination. Thus, there is a need for remote access to these image data for rapid patient assessment and therapy recommendation.
U.S. Pat. No. 4,603,254 teaches a stimulable phosphor sheet carrying a radiation image stored therein scanned with stimulating rays. The light emitted from the stimulable phosphor sheet in proportion to the radiation energy stored therein is detected and converted into an electric signal converted to a digital signal. Digital data is created to reproduce the radiation image for use in diagnosis and storage.
U.S. Pat. No. 4,764,870 describes a system for transferring medical diagnostic information from the diagnostic site to remote stations. An internal analog video signal from imaging diagnostic equipment such as a CAT scanner or MRI equipment, is converted to an analog video signal of different, preferably standard, format that is stored and transmitted in the reformatted image information to the remote terminal. The received signal is stored, decoded and applied in appropriate analog video form to an associated CRT display for reproduction of the diagnostic images.
U.S. Pat. No. $5,005,126$ shows a system for transferring medical diagnostic information from the diagnostic site to remote stations similar to that found in U.S. Pat. No. 4,764,870.
image taken by a plurality of shooting methods, and when the regions or interest are specific, a plurality of appropriate images are further selected using the previously stored aptitude values for the regions and shooting methods and displayed on the plurality of CRT display screens. In order that the segments to be inspected can be pointed to on the screen on which the image of the patient is displayed, a memory is provided which is adapted to previously store codes corresponding to the specific image of the patient and to specify the respective regions of the image in such a manner that they correspond to the pixel positions of the image.
U.S. Pat. No. 4,879,665 teaches a medical picture filing system composed of a picture data memory device, a picture data input-output device for inputting/outputting the picture data, a retrieving device for storing the picture data into the memory device and extracting it therefrom on the basis of retrieving data, a retrieving data input device for inputting the retrieving data into the retrieving device, a retrieving data storing device for storing the retrieving data, the retrieving data being classified by block of information obtained in one-time examination. When medical pictures are filed, retrieving data collected for each examination is utilized for reducing the amount of retrieving data, while when reproduced, retrieval is carried out for each one-time examination thereby shortening the time required for retrieval.

In light of recent advances in computer data basing, digitization and compression of image data, image enhancement algorithms and cost effective computer technology, the means for improved storage and retrieval of vital patient image data is now possible.

Such system should include the following major features:

1) means to more compactly store and more efficiently retrieve image data and automatically identify the data by patient name, image type, date and the like;
2) means for physicians to quickly and remotely access particular patient image data at the medical facility even if achieved at several different locations;
3) means to prevent loss of vital image data due to ordinary human handling and misplacement errors;
4) means to quickly and affordably access image data from the physician's office;
5) means to enhance the medical images by both contrast enhancement and zooming for improved diagnostics and/or surgical guidance; and
6) means to quickly and conveniently access image data and display on a large screen in the operating room with any desired enhancement or expansion.
As described more fully hereinafter, the present invention provides means to accomplish these goals. The system uses both general purpose system elements well known to those practiced in electronic arts and specific elements having significant novelty.

## SUMMARY OF THE INVENTION

The present invention relates to an automated high definition/resolution image storage, retrieval and transmission system capable for storing, transmitting and displaying medical diagnostic quality images for use with medical X-ray films or the like.
The system comprises means to process the image data from patient imaging to physician usage. The major or significant processing stages are described hereinafter. Specifically, the major steps in the image data flow include:

PATIENT RADIOGRAPHY: The patient's body is imaged and a film is exposed as in an X ray room, MRI or CAT scan lab.

FILM PREPARATION: The film(s) is developed to 5 create a visible image with OCR readable patient identification information superimposed thereon.

FILM INTERPRETATION: Commonly, a radiologist drafts an opinion letter for the film(s). This document preferably includes an optical character reader, or OCR, readable patient identification label or standard marking area.
IMAGE SCANNING AND DIGITIZING SUBSYSTEM: A scanner subsystem digitizes each patient image film and/or document on a high resolution scanner. This digitized data is transmitted by a local high speed data link to a separate or remote master storage unit. Patient identification information is read from a standard format on each file by OCR techniques and efficiently stored with the digitized image data. Enhanced scanner resolution and gray scale requirements are provided. Further, to reduce data rate requirements, data compaction or compression is accomplished within the scanner subsystem.
To back-up possible data link down time or scanner down time, the scanner subsystem may include a CDROM data storage drive so that image data may continue to be digitized. The CD-ROM disk may then be manually delivered to the file room unit for subsequent use.

In an optional embodiment, the digitized data of one or two images may be written to a compact semi-conductor memory card "RAM Cards". This form of data storage may be used to send selected images for special purposes such as when the image data is needed in an35 other city for second opinion purposes.

At this point in the image data flow, there is a split in which the original film data is stored as a "master" in a file room and the image disk is made available for active "on-line" use in an image storage and retrieval subsys40 tem.

FILM FILING: The patient image films may be placed in the industry standard 14 by 17 inch brown paper folders and placed on conventional filing shelves. However, it is preferred that older films be tagged and stored off-site to reduce the current excessive bulk of films in many hospital file rooms. The system would now make this practical since the original films would seldom need to be accessed.
In the preferred embodiment of the system, the pa50 tient may have his entire image data collected and written to one or more of the storage CD-ROM disks for archiving at the hospital.
IMAGE STORAGE AND RETRIEVAL SUB SYSTEM: This subsystem is a remotely controllable, automatically accessable image data subsystem to store and automatically retrieve, on-demand, the compressed digital information contained on the CD-ROM disks.

The image storage and retrieval subsystem has a high-speed data link connection to the scanning and digitizing subsystem and has a write drive recording mechanism which is dedicated to receiving the data from the scanning and digitizing subsystem. This CDROM write drive can operate without interrupting remote access operations.

Remote access may be made to the image storage and retrieval subsystem by a variety of telecommunication links. Access will be granted only if a valid user code has been presented. By means of several read-only CD

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disk drives and electronic buffering, virtually simultaneous access can be granted to several or more users.
As explained more fully hereinafter, the medical image disk will contain relatively huge quantities of data making it impractical to send over conventional data communication links without very efficient data compression technology. While there are a variety of data compression techniques available, none are well tailored to this application. Thus, novel compression means are in the a remote telecommunication access subsystem.

TELECOMMUNICATION SUBSYSTEM: Occasionally circumstances may warrant manually making an extra copy of the patient's image files to be physically delivered to an authorized requester. However, for the system to fulfill broad service to the health care industry it must be able to efficiently telecommunicate image files to remote locations both cost effectively and within a reasonable time interval.

A novel medical facsimile technology is in the pre- 20 ferred embodiment which works interactively with a remote requester to send only what is needed at acceptable resolutions, and the presented image is progressively updated as the communications connection is maintained until the resolution limits of the user display are reached, after which time, other images are either sent or further enhanced.

The specific technical means for accomplishing this uses the following novel technologies: a) guided image selection and transmission (GIST); b) progressive image enhancement (PIE); c) display compatible resolution (DCR); d) hexagonal pattern classification compression (HexPac) and e) run length coding (RLC), RLC is well known to those skilled in the arts.

It appears practical to send immediately useful patient data in less than one minute over a phone line ( 9600 baud) whereas it take many hours by conventional coding and transmission means. When wide-band telecommunications as satellite, fiber optic, micro-wave links becomes more generally available at affordable prices, then the more complex data compression techniques described here will be less important, but until that time, these types of techniques are believed essential to overall system success.

This combination of technologies to efficiently compress the image data and transmit remotely comprises the telecommunication access subsystem. In practice, these technologies may be implemented for the most part with available computer modules although several special signal processor boards are needed.

REMOTE DISPLAY TERMINAL: The quality of the image available to the user is limited or determined by the receiving presentation terminal or monitor. Two specific presentation terminal types are envisioned in the preferred embodiment of the system, a modified personal computer terminal for use in a physician's office, hospital nurses' station and the like, and a large screen presentation terminal with remote controlled interaction primarily for operating room use.

Both terminals have means to show the available patient directory of images, and means to select an image, enhancement and zoom on selected areas. Image enhancement has heretofore been impractical for film based images and thus much subtle but important pathological information has been largely lost. This is especially true of X-ray data The ability to enhance subtle contrasted tissues areas is considered to be an important feature and benefit of the system.

An optional high-resolution printer ( 300 dpi or better) permits the physician to print out selected images. This will be especially valuable when the physician expands and enhances selected critical image areas since a cost effective printer would otherwise not have adequate gray scale or pixel resolution to give diagnostically useful output.

Each terminal consists of a standard high performance personal computer with one or more data source interfaces such as RAM card, CD-ROM disk or data modem, a decompression graphics interface circuit and graphics display. The large screen presentation terminal has a large screen display for easy viewing for a surgeon who may be ten or more feet distant. The large screen presentation terminal also has an optional remote control so that an attending technician or nurse can scroll images, enhance and zoom, at the surgeon's request.

A keynote of each terminal design is a very simple user interface based upon a limited selection menu and obviously pointed-to graphical icons.

The invention accordingly comprises the features of construction, combination of elements, and arrangement of parts which will be exemplified in the construction hereinafter set forth, and the scope of the invention will be indicated in the claims.

## BRIEF DESCRIPTION OF THE DRAWINGS

For a fuller understanding of the nature and object of the invention, reference should be had to the following detailed description taken in connection with the accompanying drawings in which:

FIG. 1 is a functional block diagram of the entire system of the present invention.
FIG. 2 is a functional block diagram of the image scanning and digitizing means.
FIG. 3 is a functional block diagram of the image data storage and retrieval means.
FIG. 4 is a perspective view of the image data storage and retrieval means.
FIG. 5 is a functional block diagram of the telecommunication means.
FIG. 6 is a functional block diagram of the remote display terminal means.
FIG. 7 depicts the hexagonal pattern of the hexagonal compression method.

FIG. 8 depicts an actual hexagonal pattern from an X-ray film. FIG. 9 depicts the selected predetermined hexagonal pattern most closely corresponding to the actual hexagonal pattern shown in FIG. 8.

FIG. 10 graphically represents the predetermined rotational orientations for the predetermined hexagonal patterns.

FIG. 11 graphically depicts a selected gray level slope of the selected predetermined hexagonal pattern of FIG. 9.

FIG. 12 depicts a single pixel from the predetermined hexagonal pattern.

FIG. 13 depicts a hexagonal pattern reconstructed by a remote display terminal means corresponding to the actual hexagonal pattern shown in FIG. 8.

FIGS. 14-A through 14-H depict the predetermined set of orthogonal gray level patterns.

Similar reference characters refer to similar parts throughout the several views of the drawings.

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## DETAILED DESCRIPTION OF THE PREFERRED EMBODIMENT

As shown in FIG. 1, the present invention relates to an automated high definition/resolution image storage, retrieval and transmission system generally indicated as 10 for use with medical X-ray film 12 or other documents to provide simultaneous automated access to a common data base by a plurality of remote subscribers upon request from the remote subscribers.

The automated high definition/resolution image storage, retrieval and transmission system 10 comprises an image scanning and digitizing means 14 to transform the visual image from the medical X-ray film 12 or other documents into digital data, an image data storage and retrieval means 16 to store and selectively transfer digital data upon request, a telecommunication means 18 to selectively receive digital data from the image data storage and retrieval means 16 for transmission to one of a plurality of remote visual display terminals each indicated as 20 upon request from the respective remote visual display terminal 20 through a corresponding communications network 21 such as a telephone line, satellite link, cable network or local area network such as Ethernet or an ISDN service for conversion to a visual image for display at the remote requesting site.

To improve automation and tracking, a machine readable indicia or label 22 containing key patient information may be used in association with the medical X-ray film 12. As shown, the machine readable indicia or label 22 is affixed to the medical X-ray film 12 prior to scanning by the image scanning and digitizing means 14 to provide file access and identification. Furthermore, digital data from alternate digitized image sources collectively indicated as 24 and file identification may be fed to the image data storage and retrieval means 16 for storage and retrieval.

FIG. 2 is a functional block diagram of the image scanning and digitizing means 14 capable of converting the visual image from the medical X-ray film 12 to digitized image data for transmission to the image data storage and retrieval means 16 over a bi-directional high speed data link 25 . Specifically, the image scanning and digitizing means 14 comprises a film loading and scanning section and a data compression and transmission section generally indicated as 26 and 27 respectively and a display and control section generally indicated as 28. The film loading and scanning section 26 comprises a film input loader 30, alignment and sizing chamber 32, optical character reader 34 and film scanner/digitizer 36 capable of at least 500 dots per inch resolution 36; while, the data compression and transmission section 27 comprises a data buffer memory 38, low-loss data compression means 40 , local data modem 42 and transmission connector 44 to operatively couple the image scanning and digitizing means 14 to the image data storage and retrieval means 16. The low-loss data compressor 40 is also operatively coupled to a compact disk data storage drive 46 capable of writing or storing compressed digitized patient image data on a compact disk 48. The display and control section 28 comprises a keyboard/control console 50, display terminal 52 and control computer 54 which is operatively coupled to the other components of the image scanning and digitizing means 14 through a plurality of conductors each indicated as 55. A film collector tray 56 may be disposed adjacent the film scanner/digitizer 36 to receive the medical X-ray film 12 therefrom following processing.

To reduce the approximately 238 Megapixels required to digitize a 14 inch by 17 inch, medical X-ray film 12 with 700 dots or pixels per inch with a two byte level to a manageable size without significant information loss, a linear gray level prediction, modified run-length code generating logic circuitry is embodied within the lowloss data compression means 40 to dynamically compress the digitized data before storage or recording. The image data is compressed with acceptable diagnostic resolution loss. The low-loss data compression means 40 measures the "local" slope of the pixel gray level and continues to compare that estimated gray level for up to an entire scan line until a pixel region is reached which differs from the linear estimate by more than a predetermined amount. The data actually sent for that region consists of the slope of the line, actual level at the origin of the slope line and the number of pixels comprising that region. The circuitry will discard linear gray level slope differences of the original film which can be reliably determined to be noise or image "artifacts". A sudden pixel (if at 1000 dots per inch) dramatic change in gray level could be rejected as dust or film noise for example. The compressed data is a trade-off between complexity, speed and minimum data loss to reduce the total data quantity stored by a factor of approximately three. Thus, about 80 Megapixels of data may still have to be stored per 14 inch by 17 inch film image.

In the preferred embodiment, the bi-directional high speed communications link 25 transmits the low-loss compressed digitized data from the developing lab room to the hospital file room where the image data storage and retrieval means 16 will transfer and store the patient and image data in a new patient file on a compact disk 48.

Two way communications between the image scanning and digitizing means 14 and the image data storage and retrieval means 16 minimizes data loss by insuring that a compact disk 48 be available to receive and store data. Moreover, the compact disk data storage drive 46 with re-writable ROM technology can record data even if communications with the image data storage and retrieval means 16 is disrupted. Thus the image scanning and digitizing means 14 can automatically start writing data to the compact disk data storage drive 46 as soon as a image data storage and retrieval means 16 fault is sense. The display and control section 28 informs the operator of the system status.

In operation, the film lab technician may stack one or more medical X-ray films 12 onto the input loader 30 as shown in FIG. 2. A "read" button is depressed on the keyboard/control console 50 and each film 12 is thereafter fed in automatically, digitized and transmitted to the image data storage and retrieval means 16 located in the file room. As the reading of each film 12 is completed, the film 12 is deposited into the film collector tray 56. System status, number-of-films read logging and so forth are shown on the display terminal 52.

Initially, the image scanning and digitizing means 14 positions the film 12 in the alignment and sizing chamber 32 on a precision carrying platen for subsequent optical scanning. This platen contains optical sensors to sense the exact film size so only the useful image area is digitized. Once the film 12 is secured onto the movable platen, the film 12 is passed through the optical character reader 34 and then to the film scanner/digitizer 36.

The patient data and image identification is first recorded onto the remote CD-ROM file directory in the image data storage and retrieval means 16 from the

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OCR "pass" and then the compressed scanned image data is sequentially written to a compact disk 48 by a CD write drive for storage with the CD library storage of the image data storage and retrieval means 16 as described more fully hereinafter as the film 12 slowly passes through the film scanner/digitizer 36.
Specifically, the film scanner/digitizer 36 converts the image to a digital representation of preferably at least a 700 dot per inch resolution. This digital data is temporarily stored in the data buffer memory 38 where the patient data from the optical character reader 34 and corresponding digitized image data from the file scanner/digitizer 36 are properly formatted for subsequent compression and transmission to the image data storage and retrieval means 16. The stored data is then accessed by and compressed by the data compression means 40 as previously described and transmitted through the local data modem 42 and transmission connector 44 to the image data storage and retrieval means 16 or a compact disk data storage drive 46. The display and control section 28 permits the X-ray lab staff to monitor system status, report quantity of documents and films processed and allow for scheduling local recording of image data on compact disks 48.

FIGS. 3 and 4 show the image data storage and re- 25 trieval means 16 to receive and store the low-loss compressed digitized patient information and image data from the image scanning and digitizing means 14 and to selectively transmit the stored low-loss compressed digitized patient information and image data to one or more of the remote visual display terminal(s) 20 through corresponding telecommunication means 18 and corresponding communications network(s) 21 upon request from one or more of the remote display terminal(s) 20.

The image data and retrieval means 16 is essentially a central data storage library for medical subscribers to remotely access and visually display patient data and information.

As described hereinafter, the image data storage and retrieval means 16 is robotically automated to minimize hospital staff requirements. At any given time, it is estimated that a typical hospital may have several hundred active patients with requirements for physician access to corresponding image files. An active patient may require one to three compact disks 48. Thus, the image data storage and retrieval means 16 should have sufficient means to store and retrieve at least 500 compact disks 48.
Further, to minimize personnel requirements, the image data storage and retrieval means 16 has a semiautomatic log-in mechanism for updating the compact disk inventory and an automatic mechanism for retrieving and reading the compact disks 48 remotely via communication link interfaces similar to juke box playback mechanisms. Except for the occasional loading of new empty compact disks 48 and removal of inactive compact disks 48, the operation of the image data storage and retrieval means 16 is fully automatic permitting authorized access at any time.
As described more fully hereinafter, several playback drives with electronic buffering are incorporated so that essentially simultaneous access can be provided to several remote requesting users. An optional duplicating CD write drive and RAM-Card drive permits additional copies to be made locally upon demand for either back-up or other use. The image data storage and retrieval means 16 has an operator's console/desk ar-
rangement for file maintenance and duplicating control by the hospital file room clerk. Control software is a simple menu selection design so that relatively unskilled personnel can maintain the central data storage library or image data bank.

As shown in the functional block diagram of FIG. 3, the image data storage and retrieval means 16 comprises a local data modem 58 operatively coupled between the image scanning and digitizing means 14 through the transmission connectors 44 and bi-directional high speed communication link 25 , and a selector or multiplexer 60 . A format convertor 62 is operatively coupled between the alternate digitized image source(s) 24 such as CAT 64, MRI 66 and/or video 68 and control computer 70 which is, in turn, coupled to a control console 72 including a visual display and input means such as a keyboard. The local data mode 58 is also coupled to the hard disk (H/D) of the control computer 70 through a conductor 71. The other components of the image data storage and retrieval means 16 are coupled to the control computer 70 through a plurality of conductors each indicated as 73. A CD write drive 74 is operatively coupled between the multiplexer or selector 60 and an auto disk storage/retrieve mechanism 76 which is, in turn, operatively coupled to a CD library storage 78, a manual load/purge box 80 and a plurality of data retrieval and transmission channels each indicated as 81. Each data retrieval and transmission channel 81 comprises a CD reader drive 82 operatively coupled through a corresponding data interface 84 to a corresponding transmission connector 86 . In addition, one of the CD reader drives 82 is operatively coupled through a selector switch 88 to an optional CD write/RAM card drive 90 configured to manually receive a compact disk 48 or RAM card.

As shown in FIG. 4, the CD library storage 78 comprises at least one cabinet 200 to operatively house 800 compact disks 48 arranged or four shelves each indicated as 202 and the auto disk storage/retrieval mechanism 76 which comprises a CD coupler 204 to engage and grasp a selected compact disk 48 and move horizontally on a support member 206 that moves vertically on a pair of end support members each indicated as 208. An access door 210 permits movement of compact disks 48 to and from the cabinet 200 . However, in normal operation, "old" patient data is removed by writing collected image data to a single compact disk 48 through the CD write/RAM card drive 90 thus freeing internally disposed compact disks 48 for new data. The CD write/RAM card drive 90 may also be used to collect a patient's image data on a single compact disk 48 for use in the operating room's display terminal. This obviates the need for a high speed internal hospital local area network.

The computer associated with the CD robotic arm and drive mechanism performs ordinary library maintenance functions such as retrieval of outdated files, access statistics, entry of access validation codes, and so forth. This computer subsystem also handles data communication interface functions.
Internal to the environmentally controlled cabinet 200 are a plurality of playback mechanisms (field expandable to six) which are automatically controlled by 65 the accessing physicians via the coupled communications system. Yet another CD-ROM write drive can record new data from the image scanning and digitizing means 14 or perform library functions such as consoli-

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dation of a patient's data from several compact disks 48 to a single patient-dedicated compact disk 48.

The internal computer maintains a file log of which compact disks 48 are empty and where each patient's image data is stored by disk number and track on a disk location. When the image scanning and digitizing means 14 requests to down-load data, the auto disk storage/retrieval mechanism 76, of the image data storage and retrieval means 16 retrieves the "current" compact disk 48 which is being written with data (if not already loaded), then loads the compact disk 48 into the CD write drive 74, and signals to the image scanning and digitizing means 14 to transmit. Image data is then recorded with a typical record time of 4 minutes for a full-size, high density image.

Once the robotic arm has delivered the compact disk 48 to the CD write drive 74, the robotic arm is free to access and place other compact disks 48 onto $C D$ reader drive 82 as commanded by its communications interface. The robotic arm can find and place a disk 48 into the appropriate CD reader 82 in approximately 10 seconds. Thus, there is minimal waiting time for disk access unless all CD readers drives 82 are in use.

As shown in FIG. 3, data is received through the input transmission connector 44 to the CD write drive 74 through the selector switch 60 . Alternately, other image data from other sources such as CAT scanners 64 or MRI medical equipment 66 may be fed through the format convertor 62 for storage on a compact disk 48 . If the other image sources are written to CD write drive 74, file identification data must be supplied to the format convertor 62 from the control computer 70.

The image file data received from the image scanning and digitizing means 14 is directly written to free space on a compact disk 48 in the CD write drive 74. No other data compression or special formatting is required as the image scanning and digitizing means 14 has performed these functions. As new image data is received from the image scanning and digitizing means 14 or another image source 24, the image data is sequentially appended to the last file on the compact disk 48 currently being written to. Thus, no attempt is made to organize a single patient's image files onto a single compact disk 48. However, each file received is logged into the control computer 70 through the conductor 71. Therefore, the control computer 70 always knows what disk location in the CD library storage 78 contains any specified file. Once a compact disk 48 is filled with image data, the auto disk storage/retrieve mechanism 76 removes the compact disk 48 from the CD write drive 74 and stores the compact disk 48 in an empty location in the CD library storage 78.

The plurality of data retrieval and transmission storage 78. channels 81 service the data requests from subscribers. As previously indicated, a single data retrieval and transmission channel 81 includes the select switch 88 to direct image file data to the optional CD write/RAM card drive 90 . By this means, all image data for an individual patient may be collected on one or more selected compact disks 48 for archiving or other use. However, normally, the control computer 70 will automatically remove old image data by removing the compact disk 48 from the CD library storage 78 and placing the compact disk 48 in the manual load/purge box 80. The removal age and exceptions information are selected by the system operator from the control console 72.

The control console 72 is also used to enter and maintain subscriber access identification codes in an "authorization file". This updated user authorization file data is sent through a transmission connector 92 to the tele5 communications means 18 internal computer memory accessed by the control computer 70 as needed to accept or reject subscriber data link access requests. The user authorization file normally residing in the telecommunications means 18 may be remotely updated by authorized persons.

The number of data retrieval and transmission channels 81 depends on intended subscriber demand. The image data storage and retrieval means 16 is modular and may be upgraded as demand increases. Each data interface 84 operates cooperatively with the telecom$\dot{\text { munications means }} 18$ to send only as much information as the telecommunications means 18 can compress and transmit to a remote visual display terminal 20 of a requesting subscriber in a given time interval. Thus, the interface is an asynchronous block-buffered type.

Since the entire system 10 is designed to provide easy and quick access to a patient's medical images, it is vital that these images be transmitted to a variety of locations in a timely and cost effective manner and further data compression is imperative. The telephone network is still the most commonly available network but has a severe data rate limitation of about 1200 bytes per second ( 9600 baud). While other high speed telecommunication channels such as time-shared cable, satellite link may eventually become commonly available, for the immediately forseeable future, the "phone" network must be used if system $\mathbf{1 0}$ is to be practical today.

As noted earlier, a typical medical image may be stored as 119 megabytes of data. At 1200 bytes per second, it could take 27 hours to completely transmit the already compressed medical image data. This is obviously unacceptable. To overcome this obstacle, the telecommunications means 18 as shown in FIG. 5 utilizes five distinct data handling technologies to achieve useful data image transmission in less than one minute:
(1) Guided Image Selection and Transmission or GIST depends upon interactive use by the physician to identify what portions of an image are needed for enhancement or better resolution. Thus the data actually transmitted to the subscriber's visual display terminal 20 is guided by the subscriber observing the image. In particular, once the user has an image displayed on his or her visual display terminal 20, the user may outline a specific region of interest such as a lesion or tumerous growth for more detailed study. The operator may select this region using a "mouse" or light pen or similar well-known computer display terminal peripheral device Having selected this region, the visual display terminal 20 will display the more detailed pixel data be 5 sent on this region. The telecommunications means 18 will continue to send further precision data until the natural resolution limits of the display are reached or all available data is sent and received. This process of expanding an image region is known as "zooming" in 60 computer-aided design systems. The novel feature here is that the image is further refined in resolution when "zoomed". The means for doing this and knowing when to "stop" further pixel transmission is defined by the PIE and DCR technology described hereinafter,
(2) Progressive Image Enhancement or PIE utilizes the transmission time from the instant a first "crude" image is presented to the subscriber to the present time of observation to progressively enhance the quality of
the presented image. The longer the user observes a selected image, the "better" the image becomes in the sense of pixel resolution and quantity of gray levels. In the preferred embodiment, hexagonal pixel groups are first transmitted using the HexPac pattern compression technology described hereinafter. Once a full terminal screen display has been made composed of these hexag onal patterns, then the telecommunications means 18 transmits more precise pixel detail First all pixels located on the periphery of each hexagonal group are updated with their exact gray level values and thereafter, all inner pixels are similarly updated. If the display terminal's resolution is less than the 1000 dots per inch of the source image data, then pixel groups are sent, such as a square of four pixels, which match the display resolution and "zoom" expansion selected. This display matching technique is further defined hereinafter as DCR,
(3) Display Compatible Resolution or DCR transmits information about the user's terminal 20 back to the telecommunications means 18. Only data with a resolution compatible with that terminal 20 will be sent. Any excess data-link connect time can be used to send other image data which is likely to be requested or has been pre-specified to be sent.
(4) An image pattern compression method comprising a Hexagonal Pattern Classification or HexPac exploits the two dimensional nature of images. The data received by telecommunications means 18 is first uncompressed and placed into a multi-scanline digital buffer. This image data is then divided up into hexagonal cells and matched against predefined patterns. Many fewer bits of data can be used to represent these predefined patterns thus substantially compressing the image data for phone-line transmission. The pixels of these hexagonal patterns may easily be "refined" by the PIE technology described earlier. If the DCR subsystem determines that the user terminal has a pixel area of, say, 1500 by 1000 dots, then the HexPac technology recreates a new super pixel which is the average gray level of all actual pixels within that super pixel area. This immediately reduces the quantity of pixels to be sent (to only 1500 by 1000 pixels). Without further data compression, this quantity of data would still require about 26 minutes of data transmission time at 9600 baud, the highest available phone network data rate.
(5) Run length coding or RLC permits data to be compressed by specifying how many pixels have the same gray level in a sequence or "run length" of scanning. The image data sent by a $C D$ reader drive 82 to telecommunications means 18 is compressed with runlength coding but is nearly loss-less in the duplication of the original film data. To substantially reduce the quantity of data needed to send an acceptable medical image to a remote user terminal 20 over the data-rate limited phone-line modem, a "lossy" compression is used. Since the PIE and DCR techniques described earlier will eventually provide any degree of diagnostic image integrity desired, it is believed acceptable to initially transmit a "lossy" image provided it gives adequate resolution for the user to begin the analysis and guided image selection. Many fewer bits can describe this "run" of similar gray levels thus compressing the amount of data sent. This technique is well known and often used in facsimile transmission A one dimensional RLC is incorporated in the preferred embodiment but since HexPac elements are being coded, it can be con-
sidered more accurately a quasi two dimensional RLC compression.

FIG. 5 is a functional block diagram of the telecommunications means 18 including a control computer 94 operatively coupled to the image data storage and retrieval means 16 through a transmission connector 96. The various components of the telecommunications means 18 including a status panel 98 with a plurality of system indicators each indicated as 99 and a plurality of data compression channels each generally indicated as 100 coupled to the control computer 94 by a plurality of conductors each indicated as 101.

Each data compression channel 100 comprises a transmission connector 86, a communications data interface 102, a first compression processor or means 104 including logic means to generate the GIST and DCR data compressions and corresponding first data memory 106, a second compression processor or means 108 including logic means to generate the PIE and HEXPAC data compressions and corresponding second data memory 110 and a third compression processor or means 12 including logic means to generate the RLC data compression and corresponding third data memory 114, a corresponding modem 116 and a transmission connector 118.

The control computer 94 coordinates or controls data flow to and from the plurality of data compression channels 100 through the transmission connectors 86 and 118 respectively. Validated subscriber image data requests are transmitted to the image data storage and retrieval means 16 which searches the image library file 78 for availability of the requested compact disk 48 . If available, the image data storage and retrieval means 16 loads the appropriate disk 48 from CD library storage 78 into a CD reader drive 82 and informs telecommunications means from 18 through the transmission connector 96 to the control computer 94 that a specific data interface 84 has data available to be transmitted through the corresponding transmission connectors 86. Once a subscriber transaction has been turned over to a specific data retrieval and transmission channel 81, the data compression channel 100 receives the data therefrom unless commanded to stop by a feedback control line. The data interface $\mathbf{1 0 2}$ is used to inform the CD reader drive 82 as to what portion of the image is requested by the first compression means 104. Generally, the complete image is first requested. Thus the CD reader drive 82 is requested to read the image data from the start.

The data is temporarily stored in the first data memory 106. Here the pixel data is first expanded from the RLC code into uncompressed pixel data. This is only done on a relatively few number of scan lines-about one tenth of an inch height of original image data. This uncompressed data is then remapped by the first compression means 104 into "larger" pixels whose average intensity is the average of all combined pixels compatible with the display resolution receiving remote visual display terminal 20 . This "super pixel" data is then fed to the second data memory 110. The super pixel data in memory 110 is then processed by the second compression means 108. Initially, the lowest resolution image will be transmitted to rapidly form a useful remote image on the requesting remote visual display terminal 20 through a communications network 21. This will be done by combining super pixels in the second data memory 110 into hexagonal patterns which approximate the group of super pixels. These HexPac data packets are then sent to the third data memory 114. There the Hex-

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Pac data packets are further compressed by the third compression means 112. These packets of run-length coded HexPac data packets are then transmitted through the corresponding modem 116 and transmission connector 118 over the selected communications network 21. The modem 116 includes state of the art error control techniques such as block retransmission when a remote error has been detected. Thus, data transmission is essentially error free as needed for compressed data handling.
The control computer 94 includes circuitry means to monitor the activity of each data channel. The identification of each subscriber is logged along with the total connect time for billing purposes. Thus the control computer 94 generally coordinates the plurality of communication links and their connections to the particular data retrieval and transmission channel 81 within the image data storage and retrieval means 16 as well as granting access and performing connection accounting tasks. The status panel 98 , connected to the control computer 94 is used to aide in system debug and indicate operation of the data compression channels 100 . The status panel 98 would not normally be used by hospital personnel but by system service technicians.
The control computer 94 also has a permanent memory such as a hard disk to record subscriber usage data and internally sensed hardware problems. This data may be downloaded on any of the transmission connectors 118 when a correct authorization code has been received. Thus, the servicing company can acquire subscriber usage information remotely for billing purposes and system diagnostic purposes.

The preferred embodiment of the telecommunications means 18 uses modular communication channel hardware. Thus, the module may be customized to function with any type of communication channel such as satellite links, cable networks or a local area network such as Ethernet or ISDN services.

It is important to note that all communications is bidirectional so that if, say, a remote visual display terminal 20 should become temporarily "overloaded" with image data due to decompression processing delays or due to a detected data error, then, the remote visual display terminal 20 may request that data transmission be stopped or a block of data be repeated until it is received correctly.

FIG. 7 graphically shows a hexagonal group of the hexagonal compression method comprising a group of square image pixels partitioned into a hexagonal group. The pixels are numbered for convenience of reference from the inside to the outside in a clock-wise manner. Each hexagonal group or packet comprises 24 super pixels as earlier described but other numbers are possible. It is assumed that each pixel is gray level coded using 2 bytes of data. Thus, the hexagonal group requires ( $24 \times 2$ ) 48 bytes of data to fully represent the 24 super pixels comprising the image pattern at the user terminal 20.

FIG. 8 shows a typical pattern as may occur in a region of an X -ray film 12. The method predefines a 6 group of likely patterns, one of which is represented as a "best" match as in FIG. 9 with the actual pattern in FIG. 8. As shown in FIGS. 14A through 14H, there are 8 possible predetermined representative gray level patterns represented by 3 bits. These patterns are specifically selected to be essentially uncorrelated with each other even rotated relative to each other. As shown in FIG. 10, these patterns may be rotated through 8 equal
angles (another 3 bits of data) to best match the actual pattern. Rotation angle " 1 " is shown in FIG. 10 as the best match for the given example. Thus far, six bits have been used to approximate the actual pattern of FIG. 8. As shown in FIGS. 14A through 14H, each fictitious pattern includes a dark and light regions and origin. Although FIG. 11 discloses a straight gray level slope corresponding to the pattern shown in FIG. 14A, the gray level slope will vary with the fictitious pattern. For example, the gray level slope of the fictitious pattern shown in FIG. 14D would closely approximate a V shape.

FIG. 11 shows how the gray level slope may be discretely selected to best match the slope of the actual pattern. Two bits are used to approximate this slope.

FIG. 12 shows that one particular pixel, such as the darkest pixel, has been selected to be fairly precisely gray level represented by means of 8 bits ( 256 gray levels).
The total bits required to approximate the actual pattern is 16 or two bytes. FIG. 13 shows how this fictitious or reconstructed pattern may be reproduced at the user terminal 20 when decoded.

In this example, only two bytes were required to represent "adequately" an original 48 bytes of image data. Thus, a 24 to 1 compression ratio has been achieved. Further, run-length encoding (RLC) may be used on these HexPac Groups to further reduce redundant spans of white and black. It is estimated that the combined compression ratio of HexPac and RLC on the super-pixel image is about 36 to 1 for this particular set of parameters. This combined compression technology reduces data transmission time (at 9600 baud) to approximately 43 seconds for an initial useful medical image.
For medical images, further enhancements through the PIE compression should favor the elimination of artificial lining between hexagonal patterns first. As the user continues to view the same image, then the PIE compression will progressively improve the gray level integrity by updating all number 24 pixels to 8 bits of gray level resolution and updating all number 23 pixels to 8 bits of gray level and so forth for all remaining pixels in descending order. This process takes about 10 minutes at 9600 baud to update all peripheral hexagonal pixels and about 20 minutes total for all pixels.

If the user continues to observe or request further image resolution, the telcommunication means 20 causes each pixel gray level to be updated by one additional bit in descending order again until the full 16 bits of gray level is received and stored at the terminal 20 for each super pixel. Each doubling of gray level resolution takes between 1 and 2.6 minutes at 9600 baud depending on the run length statistics of the gray levels.

FIG. 6 is a functional block diagram of a remote visual display terminal 20 to be operatively coupled to one of the data compression channels 100 of the telecommunication means 18 by a communications network 21 and a transmission connector 118. The visual display terminal 20 comprises a data communications modem 120 operatively coupled to a control computer 122 and RLC decompression means 124. The RLC decompression means 124 is, in turn, operatively coupled to a memory 126, a PIE bypass 128 and a pattern select and modifier 130 which is operatively coupled to a Hexpac pattern ROM 132 and the control computer 122. A memory 134 is operatively coupled between the PIE bypass 128 and pattern selector and modifier 130 and a display drive 136 which is operatively coupled to an

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image display 138. In addition, an image enhancing processor means 139 including circuitry to generate edge contrast enhancement, gray level contrast enhancement by means of gray level region expansion or differential gray level tracking and gray level enhancement or other state of the art image enhancement method well known to those skilled in the art. The control computer 122 is operatively coupled to an interface 140 to a first control or selector means 142 and a second control or selector means including a radio receiver 144 and signal command decoder 146 for use with portable keyboard transmitter 148. In addition, an optional CD read/write drive 150 may be provided for use with a compact disk 48.

The modem 120 has built-in compatible error correction technology to communicate with corresponding transmitting data compression channel 100. After the user has selected the image data storage and retrieval means 16 and validated authority by swiping through an identification magnetic card 152 or otherwise through a magnetic card reader 154 entered an assigned security code, the operator may select a patient and one or more image files presented to him on the display screen 138. Selection is accomplished by a touch-screen overlay on the first control or selector means 142 or by the keyboard transmitter 148 of the second control or selector means.

Once one or more images have been selected by the user, the modem 120 writes image data to the temporary memory 126 which is actively accessed by the RLC decompression means 124. This decompressed data describes the HexPac patterns or packets as stripes of the image running, for example sequentially from left to right. These Hexpac pattern specifications, typically 2 data bytes or 16 bits are then routed to a pattern selection processor 130 which accesses the predefined patterns from Read-Only Memory device 132. Each pattern is then rotated and gray-level modified by processor 130 according to the HexPac 16 bit pattern specification received from the RLC decompression means 124. Each modified pattern is then written to a graphics display memory circuit 134. As the graphics display memory circuit 134, develops the pattern data, the display driver 136 and image display 138 show the image on the screen as it is received. In this manner, the entire "first pass" medical image is painted on the image display 138 screen.

If the user makes no further intervention, then once the image is fully displayed on this "first pass", then the progressive image enhancement technology requests pixel enhancement data. This enhancement data bypasses pattern selector and modifier 130 and is routed through the PIE bypass 128. In the PIE bypass 128, the enhanced pixel information is directed to the correct graphic memory locations in the graphics display means circuit 134'. Thus, the display driver 136 and image display 138 are continually resolution enhanced.
If the image is fully enhanced to the limits set by the DCR in the control computer 122, the image storage and retrieval means 16 is directed by the control computer 122 to begin sending new image data on the next selected image and begin storing this image data in a second graphics display memory circuit 134". This second data memory $134^{\prime \prime}$ can hold one more images and may be selected immediately by the user when he is finished inspecting an earlier image. The user may further direct by touch screen command 142 that these be

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 il such time as the DCR informs it that once again the natural display resolution limit has been reached.The following image enhancement means present in the instant invention: edge contrast enhancement, gray level contrast enhancement by means of gray level re0 gion expansion or differential gray level tracking and gray level enhancement and may be accomplished by the image enhancing processor means 139 in the visual display terminals 20.

The human eye cannot reliably discern gray level 65 differences less than approximately $2 \%$. Yet, significant tissue density information causes X-ray gray level differences in this range and below. The enhancement technologies above will cause these tissue density differ-

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ences to be magnified thus revealing hitherto unseen image data.

To ensure ease of use, the following features are incorporated: touch-screen selection of commands, magnetic card identification of the subscriber or user, icon based menus or selection buttons on the CRT display and split image display screen overlays

It will thus be seen that the objects set forth above, among those made apparent from the preceding description are efficiently attained and since certain changes may be made in the above construction without departing from the scope of the invention, it is intended that all matter contained in the above description or shown in the accompanying drawing shall be interpreted as illustrative and not in a limiting sense.

It is also to be understood that the following claims are intended to cover all of the generic and specific features of the invention herein described, and all statements of the scope of the invention which, as a matter of language, might be said to fall therebetween.
Now that the invention has been described,
What is claimed is:

1. A medical image storage, retrieval and transmission system providing simultaneous automated access to an image data base by a plurality of remote subscribers upon request over a communications network, said system comprising
image digitizing means forming a first digitized representation of said image,
first data compression means generating from said first digitized representation a low-loss second digitized representation of said image,
image data storage and retrieval means comprising means to receive and store said second digitized representation and to selectively provide said second digitized representation to data channel compression means compressing said second digitized representation to form a third digitized representation, and
telecommunication means including means to selectively transmit said requested third digitized representation to a requesting remote visual display terminal, said telecommunication means initially telecommunicating a first portion of said third digital representation, said remote terminal including means to convert said first portion of said third representation to a visual image having an initial resolution less than a resolution limit of said requesting terminal, said telecommuncation means subsequently telecommunicating a second portion of said third digital representation, said second portion usable with said first portion to form an image having a resolution intermediate said initial resolution and said resolution limit.
2. A system of claim 1 wherein said first data compression means includes logic means to generate a runlength compressed digitized image data signal as said second representation.
3. A system of claim 1 wherein said first data compression means is operatively coupled to an external data storage drive to store said second representation.
4. A system of claim 1 wherein said image data storage and retrieval means comprises a data modem coupled to said image scanning and digitizing means, a write drive operatively coupled to said data modem to receive and to store said second digitized representation, and a plurality of data retrieval and transmission channels, each said channel comprising an image data reader means operatively coupled to said telecommunication means to selectively receive said second digitized representation of said image for transmission to a said requesting remote visual display terminal.
5. A system of claim 4, wherein a said image data reader means is operatively coupled to an external data write drive configured to receive a storage medium and to store compressed digital image data thereon.
6. A system of claim 4 wherein said telecommunication means comprises a control computer operatively coupled to said image data storage and retrieval means to selectively control data flow between said image data storage and retrieval means and said remote visual display terminal and a plurality of data compression channels coupled to said control computer, wherein each said data compression channel comprises a data memory including means to decompress said low-loss second representation of said image data received from said data retrieval and transmission channel and a compression means including logic means to compress and decompress second representation of said image data to form said third digitized representation of said image for transmission over said communication network to a said requesting remote visual display terminal.
7. A system of claim 1 wherein said first portion of said third representation of said image comprises a plurality of super pixels, and said second portion of said third representation comprises data representative of exact gray levels of a first subset of said super pixels and wherein a third portion of said third representation comprises similar data for a third subset of said super pixels.
8. A system of claim 1 wherein said remote terminal further includes means to select a region of a said image and said telecommunication means includes means to transmit a third portion of said third digitized representation, said third portion specific to said selected region, thereby providing an expanded visual display of said selected region, said expanded visual display containing more pixels than were included in said selected region.
9. A system of claim 1 wherein said remote visual display terminal further includes logic means to enhance an edge contrast of a displayed image.
10. A system of claim 1 wherein said remote visual display terminal further includes logic means to enhance gray level contrast by means of gray level region expansion.
11. A system of claim 1 wherein said remote visual display terminal further includes logic means for differential gray level tracking and gray level enhancement.
12. A system of claim 1 wherein individual patient information corresponding to said image is read by an optical character reader for compression and transmission with a said corresponding second digital representation to said image data storage and retrieval means.

## UNITED STATES PATENT AND TRADEMARK OFFICE CERTIFICATE OF CORRECTION

PATENT NO. : 5,321,520
DATED : June 14, 1994
INVENTOR(S) : Jorge J. Inga, et al
It is certified that error appears in the above-indentified patent and that said Letters Patent is hereby corrected as shown below:

Column 20, lines 27 and 28 , "and decompress" should read --said decompressed--.

Signed and Sealed this
Twenty-fifth Day of October, 1994

Attest:


BRUCE LEHMAN
Attesting Officer
(12) EX PARTE REEXAMINATION CERTIFICATE (8039th)

United States Patent
Inga et al.
(10) Number: US 5,321,520 C1
(45) Certificate Issued: Feb. 22, 2011
(54) AUTOMATED HIGH

DEFINITION/RESOLUTION IMAGE
STORAGE, RETRIEVAL AND
TRANSMISSION SYSTEM
(75) Inventors: Jorge J. Inga, Tampa, FL (US); Thomas V. Saliga, Tampa, FL (US)
(73) Assignee:

Automated Medical Access
Corporation, Tampa, FL (US)
Reexamination Request:
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See application file for complete search history.
(56)

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Primary Examiner-Henry N Tran

## ABSTRACT

An automated high definition/resolution image storage, retrieval and transmission system for use with medical X-ray film or other documents to provide simultaneous automated access to a common data base by a plurality of remote subscribers upon request, the automated high definition/ resolution image storage, retrieval and transmission system comprising an image scanning and digitizing subsystem to scan and digitize visual image information from an image film or the like; an image data storage and retrieval subsystem to receive and store the digitized information and to selectively provide the digitized information upon request from a remote site, a telecommunication subsystem to selectively transmit the requested digitized information from the image data storage and retrieval subsystem to the requesting remote visual display terminal for conversion to a visual image at the remote site to visually display the requested information from the image data storage and retrieval subsystem.


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1<br>EX PARTE<br>REEXAMINATION CERTIFICATE ISSUED UNDER 35 U.S.C. 307<br>NO AMENDMENTS HAVE BEEN MADE TO THE PATENT

## United States Patent <br> Yap et al.

(10) Patent No.: US 6,182,114 B1
(45) Date of Patent:

## APPARATUS AND METHOD FOR REALTIME VISUALIZATION USING USER-DEFINED DYNAMIC, MULTIFOVEATED IMAGES

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(*) Notice: Under 35 U.S.C. 154(b), the term of this patent shall be extended for 0 days.
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(22) Filed: Jan. 9, 1998
(51) Int. Cl. ${ }^{7}$ $\qquad$ G06F 15/16
(52) U.S. Cl.
. 203; 709/246
Field of Search ................................. 709/217, 219,
709/246, 247, 203; 707/10; 382/103, 233, $235,232,240,302$

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Primary Examiner-Zarni Maung Assistant Examiner-Patrice Winder (74) Attorney, Agent, or Firm-Baker Botts, L.L.P.

## (57)

## ABSTRACT

A client apparatus which enables a realtime visualization of at least one image. The client apparatus includes a storage device which stores first data corresponding to a multifoveated representation of an original image, and a user input device which providing second data corresponding to at least one visualization command of at least one user. In addition, the client apparatus includes a processing arrangement which generates third data corresponding to a multifoveated image using the first data, the second data and a foveation operator.

8 Claims, 6 Drawing Sheets


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F:G. 1

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FIG. 2A

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FIG. 2B



FIG. 4


FIG. 5

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## APPARATUS AND METHOD FOR REALTIME VISUALIZATION USING USERDEFINED DYNAMIC, MULTI-FOVEATED IMAGES

## FIELD OF THE INVENTION

The present invention relates to a method and apparatus for serving images, even very large images, over a "thinwire" (c.g., over the Internet or any other network or application having bandwidth limitations).

## BACKGROUND INFORMATION

The Internet, including the World Wide Web, has gained in popularity in recent years. The Internet enables clients/ users to access information in ways never before possible over existing communications lines.

Often, a client/viewer desires to view and have access to relatively large images. For example, a client/viewer may wish to explore a map of a particular geographic location. The whole map, at highest (full) level of resolution will likely require a pixel representation beyond the size of the viewer screen in highest resolution mode.

One response to this restriction is for an Internet server to pre-compute many smaller images of the original image. The smaller images may be lower resolution (zoomed-out) views and/or portions of the original image. Most image archives use this approach. Clearly this is a sub-optimal approach since no preselected set of views can anticipate the needs of all users.

Some map servers (see, e.g., URLs http:// www.mapquest.com and http://www.MapOnUs.com) use an improved approach in which the user may zoom and pan over a large image. However, transmission over the Internet involves significant bandwidth limitations (i.e transmission is relatively slow). Accordingly, such map servers suffer from at least three problems:

Since a brand new image is served up for each zoom or pan request, visual discontinuities in the zooming and panning result. Another reason for this is the discrete nature of the zoom/pan interface controls.
Significantly less than realtime response.
The necessarily small fixed size of the viewing window (typically about 3 " $\times 4.5$ "). This does not allow much of a perspective.
To generalize, what is needed is an apparatus and method which allows realtime visualization of large scale images over a "thinwire" model of computation. To put it another way, it is desirable to optimize the model which comprises an image server and a client viewer connected by a low bandwidth line.
One approach to the problem is by means of progressive transmission. Progressive transmission involves sending a relatively low resolution version of an image and then successively transmitting better resolution versions. Because the first, low resolution version of the image requires far less data than the full resolution version, it can be viewed quickly upon transmission. In this way, the viewer is allowed to see lower resolution versions of the image while waiting for the desired resolution version. This gives the transmission the appearance of continuity. In addition, in some instances, the lower resolution version may be sufficient or may in any event exhaust the display capabilities of the viewer display device (e.g., monitor).

Thus, R. L. White and J. W. Percival, "Compression and Progressive Transmission of Astronomical Images," SPIE

Technical Conference 2199, 1994, describes a progressive transmission technique based on bit planes that is effective for astronomical data.
However, utilizing progressive transmission barely begins 5 to solve the "thinwire" problem. A viewer zooming or panning over a large image (e.g., map) desires realtime response. This of course is not achieved if the viewer must wait for display of the desired resolution of a new quadrant or view of the map each time a zoom and pan is initiated. Progressive transmission does not achieve this realtime response when it is the higher resolution versions of the image which are desired or needed, as these are transmitted later.

The problem could be effectively solved, if, in addition to variable resolution over time (i.e, progressive transmission), resolution is also varied over the physical extent of the image.

Specifically, using foveation techniques, high resolution data is transmitted at the user's gaze point but with lower resolution as one moves away from that point. The very simple rationale underlying these foveation techniques is that the human field of vision (centered at the gaze point) is limited. Most of the pixels rendered at uniform resolution are wasted for visualization purposes. In fact, it has been shown that the spatial resolution of the human eye decreases exponentially away from the center gaze point. E. L. Schwartz, "The Development of Specific Visual Projections in the Monkey and the Goldfish: Outline of a Geometric Theory of Receptotopic Structure," Journal of Theoretical 30 Biology, 69:655-685, 1977

The key then is to mimic the movements and spatial resolution of the eye. If the user's gaze point can be tracked in realtime and a truly multi-foveated image transmitted (i.e., a variable resolution image mimicking the spatial 35 resolution of the user's eye from the gaze point), all data necessary or useful to the user would be sent, and nothing more. In this way, the "thinwire" model is optimized, whatever the associated transmission capabilities and bandwidth limitations.

In practice, in part because eye tracking is imperfect, using multi-foveated images is superior to atempting display of an image portion of uniform resolution at the gaze point.

There have in fact been attempts to achieve multifoveated images in a "thinwire" environment.
F. S. Hill Jr., Sheldon Walker Jr. and Fuwen Gao, "Interactive Image Query System Using Progressive Transmission," Computer Graphics, 17(3), 1983, describes progressive transmission and a form of foveation for a browser of images in an archive. The realtime requirement does not appear to be a concern.
T. H. Reeves and J. A. Robinson, "Adaptive Foveation of MPEG Video," Proceedings of the $4{ }^{\text {th }}$ ACM International Multimedia Conference, 1996, gives a method to foveate MPEG-standard video in a thin-wire environment. MPEG55 standard could provide a few levels of resolution but they consider only a 2 -level foveation. The client/viewer can interactively specify the region of interest to the server/ sender.
R. S. Wallace and P. W. Ong and B. B. Bederson and E. 60 L. Schwartz, "Space-variant image processing". Intl. J. Of Computer Vision, 13:1 (1994) 71-90 discusses spacevariant images in computer vision. "Space-Variant" may be regarded as synonymous with the term "multifoveated" used above. A biological motivation for such images is the 65 complex logmap model of the transformation from the retina to the visual cortex (E. L. Schwartz, "A quantitative model of the functional architecture of human striate cortex with

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application to visual illusion and cortical texture analysis", Biological Cybernetics, 37(1980) 63-76).

Philip Kortum and Wilson S. Geisler, "Implementation of a Foveated Image Coding System For Image Bandwidth Reduction," Human Vision and Electronic Imaging, SPIE Proceedings Vol. 2657, 350-360, 1996, implement a real time system for foveation-based visualization. They also noted the possibility of using foveated images to reduce bandwidth of transmission.
M. H. Gross, O. G. Staadt and R. Gatti, "Efficient triangular surface approximations using wavelets and quadtree data structures", IEEE Trans, On Visualization and Computer Graphics, 2(2), 1996, uses wavelets to produce multifoveated images.

Unfortunately, each of the above attempts are essentially based upon fixed super-pixel geometries, which amount to partitioning the visual field into regions of varying (predetermined) sizes called super-pixels, and assigning the average value of the color in the region to the super-pixel. The smaller pixels (higher resolution) are of course intended to be at the gaze point, with progressively larger super-pixels (lower resolution) about the gaze point.

However, effective real-time visulization over a "thin wire" requires precision and flexibility. This cannot be achieved with a geometry of predetermined pixel size. What is needed is a flexible foveation technique which allows one to modify the position and shape of the basic foveal regions, the maximum resolution at the foveal region and the rate at which the resolution falls away. This will allow the "thinwire" model to be optimized.

In addition, none of the above noted references addresses the issue of providing multifoveated images that can be dynamically (incrementally) updated as a function of user input. This property is crucial to the solution of the thinwire problem, since it is essential that information be "streamed" at a rate that optimally matches the bandwidth of the network with the human capacity to absorb the visual information.

## SUMMARY OF THE INVENTION

The present invention overcomes the disadvantages of the prior art by utilizing means for tracking or approximating the user's gaze point in realtime and, based on the approximation, transmitting dynamic multifoveated image (s) (i.e., a variable resolution image over its physical extent mimicking the spatial resolution of the user's eye about the approximated gaze point) updated in realtime.
"Dynamic" means that the image resolution is also varying over time. The user interface component of the present invention may provide a variety of means for the user to direct this multifoveation process in real time.

Thus, the invention addresses the model which comprises an image server and a client viewer connected by a low bandwidth line. In effect, the invention reduces the bandwidth from server to client, in exchange for a very modest increase of bandwidth from the client to the server

Another object of the invention is that it allows realtime visualization of large scale images over a "thinwire" model of computation.

An additional advantage is the new degree of user control provided for realtime, active, visualization of images (mainly by way of foveation techniques). The invention allows the user to determine and change in realtime, via input means (for example, without limitation, a mouse pointer or eye tracking technology), the variable resolution over the space of the served up image(s).

An additional advantage is that the invention demonstrates a new standard of performance that can be achieved by large-scale image servers on the World Wide Web at current bandwidth or even in the near future.

Note also, the invention has advantages over the traditional notion of progressive transmission, which has no interactivity. Instead, the progressive transmission of an image has been traditionally predetermined when the image file is prepared. The invention's use of dynamic (constantly changing in realtime based on the user's input) multifoveated images allows the user to determine how the data are progressively transmitted.

Other advantages of the invention include that it allows the creation of the first dynamic and a more general class of multifoveated images. The present invention can use wavelet technology. The flexibility of the foveation approach based on wavelets allows one to easily modify the following parameters of a multifoveated image: the position and shape of the basic foveal region(s), the maximum resolution at the foveal region(s), and the rate at which the resolution falls away. Wavelets can be replaced by any multi resolution pyramid schemes. But it seems that wavelet-based approaches are preferred as they are more flexible and have the best compression properties.

Another advantage is the present invention's use of dynamic data structures and associated algorithms. This helps optimize the "effective real time behavior" of the system. The dynamic data structures allow the use of "partial information" effectively. Here information is partial in the sense that the resolution at each pixel is only partially known. But as additional information is streamed in, the partial information can be augmented. Of course, this principle is a corollary to progressive transmission.

Another advantage is that the dynamic data structures may be well exploited by the special architecture of the client program. For example, the client program may be multi-threaded with one thread (the "manager thread") designed to manage resources (especially bandwidth resources). This manager is able to assess network congestion, and other relevant parameters, and translate any literal user request into the appropriate level of demand for the network. For example, when the user's gaze point is focused on a region of an image, this may be translated into requesting a certain amount, say, $X$ bytes of data. But the manager can reduce this to a request over the network of (say) $X / 2$ bytes of data if the traffic is congested, or if the user is panning very quickly.

Another advantage of the present invention is that the server need send only that information which has not yet been served. This has the advantage of reducing communication traffic.

Further objects and advantages of the invention will become apparent from a consideration of the drawings and ensuing description.

## BRIEF DESRIPTION OF DRAWINGS

FIG. 1 shows an embodiment of the present invention including a server, and client(s) as well as their respective components.

FIG. $2 a$ illustrates one level of a particular wavelet transform, the Haar wavelet transform, which the server may execute in one embodiment of the present invention.

FIG. $2 b$ illustrates one level of the Haar inverse wavelet transform.

FIG. 3 is a flowchart showing an algorithm the server may execute to perform a Haar wavelet transform in one embodiment of the present invention.

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FIG. 4 shows Manager, Display and Network threads, which the client(s) may execute in one embodiment of the present invention.

FIG. 5 is a more detailed illustration of a portion of the Manager thread depicted in FIG. 4.

## DETAILED DESCRIPTION OF THE INVENTION

FIG. 1 depicts an overview of the components in an exemplary embodiment of the present invention. A server 1 is comprised of a storage device 3 , a memory device 7 and a computer processing device $\mathbf{4}$. The storage device $\mathbf{3}$ can be implemented as, for example, an internal hard disk, Tape Cartridge, or CD-ROM. The faster access and greater storage capacity the storage device $\mathbf{3}$ provides, the more preferable the embodiment of the present invention. The memory device 7 can be implemented as, for example, a collection of RAM chips.

The processing device 4 on the server 1 has network protocol processing element 12 and wavelet transform element 13 running off it. The processing device $\mathbf{4}$ can be implemented with a single microprocessor chip (such as an Intel Pentium chip), printed circuit board, several boards or other device. Again, the faster the speed of the processing device 4, the more preferable the embodiment. The network protocol processing element 12 can be implemented as a separate "software" (i.e., a program, sub-process) whose instructions are executed by the processing device 4 . Typical examples of such protocols include TCP/IP (the Internet Protocol) or UDP (User Datagram Protocol). The wavelet transform element 13 can also be implemented as separate "software" (i.e., a program, sub-process) whose instructions are executed by the processing device 4 .

In a preferred embodiment of the present invention, the server 1 is a standard workstation or Pentium class system. Also, TCP/IP processing may be used to implement the network protocol processing element 12 because it reduces complexity of implementation. Although a TCP/IP implementation is simplest, it is possible to use the UDP protocol subject to some basic design changes. The relative advantage of using TCP/IP as against UDP is to be determined empirically. An additional advantage of using modern, standard network protocols is that the server 1 can be constructed without knowing anything about the construction of its client(s) 2.

According to the common design of modern computer systems, the most common embodiments of the present invention will also include an operating system running off the processing means device $\mathbf{4}$ of the server 1. Examples of operating systems include, without limitation, Windows 95, Unix and Windows NT. However, there is no reason a processing device 4 could not provide the functions of an "operating system" itself.

The server $\mathbf{1}$ is connected to a client(s) $\mathbf{2}$ in a network. Typical examples of such servers 1 include image archive servers and map servers on the World Wide Web.

The client(s) 2 is comprised of a storage device 3, memory device 7 , display 5 , user input device 6 and processing device 4 . The storage device $\mathbf{3}$ can be implemented as, for example, an internal hard disks, Tape Cartridge, or CD-ROM. The faster access and greater storage capacity the storage device $\mathbf{3}$ provides, the more preferable the embodiment of the present invention. The memory device 7 can be implemented as, for example, a collection of RAM chips. The display 5 can be implemented as, for example, any monitor, whether analog or digital. The user input device 660

 of the present invention will also include an operating system running off the processing device $\mathbf{4}$ of the client(s) 2.

In addition, if the server $\mathbf{1}$ is connected to the client(s) 2 via a telephone system line or other systems/lines not carrying digital pulses, the server $\mathbf{1}$ and client(s) $\mathbf{2}$ both also include a communications converter device 15. A communications converter device $\mathbf{1 5}$ can be implemented as, for example, a modem. The communications converter device 15 converts digital pulses into the frequency/signals carried by the line and also converts the frequency/signals back into digital pulses, allowing digital communication.

In the operation of the present invention, the extent of computational resources (e.g., storage capacity, speed) is a more important consideration for the server 1 , which is generally shared by more than one client 2 , than for the client(s) 2.
In typical practice of the present invention, the storage device $\mathbf{3}$ of the server $\mathbf{1}$ holds an image file, even a very large image file. A number of client 2 users will want to view the image.

Prior to any communication in this regard between the server $\mathbf{1}$ and client(s) 2, the wavelet transform element $\mathbf{1 3}$ on the server 1 obtains a wavelet transform on the image and stores it in the storage device 3 .

There has been extensive research in the area of wavelet theory. However, briefly, to illustrate, "wavelets" are defined by a group of basis functions which, together with coefficients dependant on an input function, can be used to approximate that function over varying scales, as well as represent the function exactly in the limit. Accordingly, wavelet coefficients can be categorized as "average" or "approximating coefficients" (which approximate the function) and "difference coefficients" (which can be used to reconstruct the original function exactly). The particular approximation used as well as the scale of approximation depend upon the wavelet bases chosen. Once a group of basis functions is chosen, the process of obtaining the relevant wavelet coefficients is called a wavelet transform.

In the preferred embodiment, the Haar wavelet basis functions are used. Accordingly, in the preferred embodiment, the wavelet transform element 13 on the server 1 performs a Haar wavelet transform on a file representation 65 of the image stored in the storage device 3, and then stores the transform on the storage device 3 . However, it is readily apparent to anyone skilled in the art that any of the wavelet

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family of transforms may be chosen to implement the present invention.

Note that once the wavelet transform is stored, the original image file need not be kept, as it can be reconstructed exactly from the transform.

FIG. 2 illustrates one step of the Haar wavelet transform. Start with an $n$ by $n$ matrix of coefficients 17 whose entries correspond to the numeric value of a color component (say, Red, Green or Blue) of a square screen image of $n$ by $n$ pixels. Divide the original matrix 17 into 2 by 2 blocks of four coefficients, and for each $2 \times 2$ block, label the coefflcient in the first column, first row "a,"; second column, first row "b"; second row, first column "c"; and second row, second column "d."

Then one step of the Haar wavelet transform creates four $\mathrm{n} / 2$ by $\mathrm{n} / 2$ matrices. The first is an $\mathrm{n} / 2$ by $\mathrm{n} / 2$ approximation matrix 8 whose entries equal the "average" of the corresponding 2 by 2 block of four coefficients in the original matrix 17. As is illustrated in FIG. 2, the coefficient entries in the approximation matrix 8 are not necessarily equal to the average of the corresponding four coefficients $\mathrm{a}, \mathrm{b}, \mathrm{c}$ and d (i.e., $\left.a^{\prime}=(a+b+c+d) / 4\right)$ in the original matrix 17. Instead, here, the "average" is defined as $(a+b+c+d) / 2$.

The second is an $\mathrm{n} / 2$ by $\mathrm{n} / 2$ horizontal difference matrix 10 whose entries equal $b^{\prime}=(a+b-c-d) / 2$, where $a, b, c$ and $d$ are, respectively, the corresponding $2 \times 2$ block of four coefficients in the original matrix 17. The third is an $n / 2$ by $n / 2$ vertical difference matrix 9 whose entries equal $\mathrm{c}^{\prime}=(\mathrm{a}-\mathrm{b}+\mathrm{c}-$ d) $/ 2$, where $\mathrm{a}, \mathrm{b}, \mathrm{c}$ and d are, respectively, the corresponding $2 \times 2$ block of four coefficients in the original matrix 17. The fourth is an $\mathrm{n} / 2$ by $\mathrm{n} / 2$ diagonal difference matrix 11 whose entries equal $d^{\prime}=(a-b-c+d) / 2$, where $a, b, c$ and $d$ are, respectively, the corresponding $2 \times 2$ block of four coefficients in the original matrix 17.

A few notes are worthy of consideration. First, the entries $a^{\prime}, b^{\prime}, c^{\prime}, d^{\prime}$ are the wavelet coefficients. The approximation matrix $\mathbf{8}$ is an approximation of the original matrix $\mathbf{1 7}$ (using the "average" of each $2 \times 2$ group of 4 pixels) and is one fourth the size of the original matrix 17 .

Second, each of the $2 \times 2$ blocks of four entries in the original matrix $\mathbf{1 7}$ has one corresponding entry in each of the four $\mathrm{n} / 2$ by $\mathrm{n} / 2$ matrices. Accordingly, it can readily be seen from FIG. 2 that each of the $2 \times 2$ blocks of four entries in the original matrix 17 can be reconstructed exactly, and the transformation is invertible. Therefore, the original matrix 17 representation of an image can be discarded during processing once the transform is obtained.

Third, the transform can be repeated, each time starting with the last approximation matrix 8 obtained, and then discarding that approximation matrix 8 (which can be reconstructed) once the next wavelet step is obtained. Each step of the transform results in approximation and difference matrices $1 / 2$ the size of the approximation matrix 8 of the prior step.

Retracing each step to synthesize the original matrix 17 is called the inverse wavelet transform, one step of which is depicted in FIG. $2 b$.

Finally, it can readily be seen that the approximation matrix $\mathbf{8}$ at varying levels of the wavelet transform can be used as a representation of the relevant color component of the image at varying levels of resolution.

Conceptually then, the wavelet transform is a series of approximation and difference matrices at various levels (or resolutions). The number of coefficients stored in a wavelet transform is equal to the number of pixels in the original
matrix 17 image representation. (However, the number of bits in all the coefficients may differ from the number of bits in the pixels. Applying data compression to coefficients turns out to be generally more effective on coefficients.) If we assume the image is very large, the transform matrices must be further decomposed into blocks when stored on the storage means 3.

FIG. 3 is a flowehart showing one possible implementation of the wavelet transform element 13 which performs a wavelet transform on each color component of the original image. As can be seen from the flowchart, the transform is halted when the size of the approximation matrix is $256 \times$ 256 , as this may be considered the lowest useful level of resolution.
Once the wavelet transform element $\mathbf{1 3}$ stores a transform of the image(s) in the storage means 3 of the server $\mathbf{1}$, the server $\mathbf{1}$ is ready to communicate with client(s) 2 .

In typical practice of the invention the client 2 user initiates a session with an image server 1 and indicates an image the user wishes to view via user input means 6 . The client 2 initiates a request for the 256 by 256 approximation matrix $\mathbf{8}$ for each color component of the image and sends the request to the server 1 via network protocol processing element 12. The server 1 receives and processes the request via network protocol processing element 12. The server 1 sends the 256 by 256 approximation matrices $\mathbf{8}$ for each color component of the image, which the client $\mathbf{2}$ receives in similar fashion. The processing device $\mathbf{4}$ of the client $\mathbf{2}$ stores the matrices in the storage device $\mathbf{3}$ and causes a display of the 256 by 256 version of the image on the display 5 . It should be appreciated that the this low level of resolution requires little data and can be displayed quickly. In a map server application, the 256 by 256 , coarse resolution version of the image may be useful in a navigation window of the display 5 , as it can provide the user with a position indicator with respect to the overall image.

A more detailed understanding of the operation of the client 2 will become apparent from the discussion of the further, continuous operation of the client 2 below.

Continuous operation of the client(s) $\mathbf{2}$ is depicted in FIG. 4. In the preferred embodiment, the client(s) 2 processing device may be constructed using three "threads," the Manager thread 18, the Network Thread 19 and the Display Thread 20. Thread programming technology is a common feature of modern computers and is supported by a variety of platforms. Briefly, "threads" are processes that may share a common data space. In this way, the processing means can perform more than one task at a time. Thus, once a session is initiated, the Manager Thread 18, Network Thread 19 and Display Thread 20 run simultaneously, independently and continually until the session is terminated. However, while "thread technology" is preferred, it is unnecessary to implement the client(s) 2 of the present invention.
The Display Thread 20 can be based on any modern windowing system running off the processing device 4 . One function of the Display Thread 20 is to continuously monitor user input device 6. In the preferred embodiment, the user input device 6 consists of a mouse or an eye-tracking device, though there are other possible implementations. In a typical embodiment, as the user moves the mouse position, the current position of the mouse pointer on the display 5 determines the foveal region. In other words, it is presumed the user gaze point follows the mouse pointer, since it is the user that is directing the mouse pointer. Accordingly, the display thread $\mathbf{2 0}$ continuously monitors the position of the mouse pointer.

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In one possible implementation, the Display Thread 20 places user input requests (i.e., foveal regions determined from user input device 6) as they are obtained in a request queue. Queue's are data structures with first-in-first-out characteristics that are generally known in the art.

The Manager Thread $\mathbf{1 8}$ can be thought of as the brain of the client 2. The Manager Thread $\mathbf{1 8}$ converts the user input request in the request queue into requests in the manager request queue, to be processed by the Network Thread 19. The user input conversion mechanism 16 converts the user determined request into a request for coefficients.

A possible implementation of user input conversion mechanism 16 is depicted in the flow chart in FIG. 5. Essentially, the user input conversion mechanism 16 requests all the coefficient entries corresponding to the foveal region in the horizontal difference $\mathbf{1 0}$ matrices, vertical difference 9 matrices, diagonal difference matrices 11 and approximation matrix $\mathbf{8}$ of the wavelet transform of the image at each level of resolution. (Recall that only the last level approximation matrix $\mathbf{8}$ needs to be stored by the server 1.) That is, wavelet coefficients are requested such that it is possible to reconstruct the coefficients in the original matrix 17 corresponding to the foveal region.

As the coefficients are included in the request, they are masked out. The use of a mask is commonly understood in the art. The mask is maintained to determine which coefficients have been requested so they are not requested again. Each mask can be represented by an array of linked lists (one linked list for each row of the image at each level of resolution).

As shown in FIG. 5, the input conversion mechanism 16 determines the current level of resolution ("L") of an image (" $\mathrm{M}_{L}$ ") such that the image $\mathrm{M}_{L}$ is, e.g., $128 \times 128$ pixel matrix (for example, the lowest supported resolution), as shown in Step 200. Then, the input conversion mechanism 16 determines if the current level L is the lowest resolution level (Step 210). If so, it is determined if the three color coefficients (i.e., $\mathrm{M}_{L}(\mathrm{R}), \mathrm{M}_{L}(\mathrm{G})$, and $\mathrm{M}_{L}(\mathrm{~B})$ ) correspond to the foveal region that has been requested (Step 220). If that is the case, then the input conversion mechanism 16 confirms that the current region $\mathbf{L}$ is indeed the lowest resolution region (Step 240), and returns the control to the Manager Thread 18 (Step 250). If, in Step 220, it is determined that the three color coefficients have not been requested, these coefficients are requested using the mask described above, and the process continues to Step 240, and the control is returned to the Manager Thread 18 (Step 250).

If, in Step 210, it is determined that the current level L is not the lowest resolution level, then the input conversion mechanism 16 determines whether the horizontal, vertical and diagonal difference coefficients (which are necessary to reconstruct the three color coefficients) have been requested (Step 260). If so, then the input conversion mechanism 16 skips to Step $\mathbf{2 8 0}$ to decrease the current level L by 1. Otherwise a set of difference coefficients may be requested. This set depends on the mask and the foveal parameters (e.g., a shape of the foveal region, a maximum resolution, a rate of decay of the resolution, etc.). The user may select "formal" values for these foveal parameters, but the Manager Thread 18 may, at this point, select the "effective" values for these parameters to ensure a trade-off between (1) achieving a reasonable response time over the estimated current network bandwidth, and (2) achieving a maximum throughput in the transmission of data. The process then continues to Step 280. Thereafter, the input conversion mechanism 16 determines whether the current level $L$ is
greater or equal to zero (Step 240). If that is the case, the process loops back to step $\mathbf{2 6 0}$. Otherwise, the control is returned to the Manager Thread 18 (Step 250).

The Network Thread 19 includes the network protocol processing element 12. The Network Thread obtains the (next) multi-resolution request for coefficients corresponding to the foveal region from request queue and processes and sends the request to the server 1 via network protocol processing element 12.
Notice that the data requested is "local" because it represents visual information in the neighborhood of the indicated part of the image. The data is incremental because it represents only the additional information necessary to increase the resolution of the local visual information. (Information already available locally is masked out).

The server 1 receives and processes the request via network protocol processing element 12, and sends the coefficients requested. When the coefficients are sent, they are masked out. The mask is maintained to determine which coefficients have been sent and for deciding which blocks of data can be released from main memory. Thus, an identical version of the mask is maintained on both the client 2 side and server 1 side.

The Network Thread 19 of the client 2 receives and processes the coefficients. The Network Thread 19 also includes inverse wavelet transform element 14. The inverse wavelet transform element $\mathbf{1 4}$ performs an inverse wavelet transform on the received coefficients and stores the resulting portion of an approximation matrix 8 each time one is obtained (i.e., at each level of resolution) in the storage device 3 of the client 2. The sub-image is stored at each (progressively higher, larger and less course) level of its resolution.

Note that as the client 2 knows nothing about the image until it is gradually filled in as coefficients are requested. Thus, sparse matrices (sparse, dynamic data structures) and associated algorithms can be used to store parts of the image received from the server 1. Sparse matrices are known in the art and behave like normal matrices except that the memory space of the matrix are not allocated all at once. Instead the memory is allocated in blocks of sub-matrices. This is reasonable as the whole image may require a considerable amount of space.
Simultaneously, the Display thread 20 (which can be implemented using any modern operating system or windowing system) updates the display 5 based on the pyramid representation stored in the storage device 3 .

Of course, the Display thread 20 continues its monitoring of the user input device 6 and the whole of client 2 processing continues until the session is terminated.

A few points are worthy of mention. Notice that since lower, coarser resolution images will be stored on the client 2 first, they are displayed first Also, the use of foveated images ensures that the incremental data to update the view is small, and the requested data can arrive within the round trip time of a few messages using, for example, the TCP/IP protocol.

Also notice, that a wavelet coefficient at a relatively coarser level of resolution corresponding to the foveal region affects a proportionately larger part of the viewer's screen than a coefficient at a relatively finer level of resolution corresponding to the foveal region (in fact, the resolution on the display 5 exponentially away from the mouse pointer). Also notice the invention takes advantage of progressive transmission, which gives the image perceptual continuity. But unlike the traditional notion of progressive
transmission, it is the client 2 user that is determining transmission ordering, which is not pre-computed because the server 1 doesn't know what the client(s) 2 next request will be. Thus, as noted in the objects and advantages section, the "thinwire" model is optimized.

Note that in the event the thread technology is utilized to implement the present invention, semaphores data structures are useful if the threads share the same data structures (e.g., the request queue). Semaphores are well known in the art and ensure that only one simultaneous process (or "thread") can access and modify a shared data structure at one time. Semaphores are supported by modern operating systems.

## CONCLUSION

It is apparent that various useful modifications can be made to the above description while remaining within the scope of the invention.

For example, without limitation, the user can be provided with two modes for display: to always fill the pixels to the highest resolution that is currently available locally or to fill them up to some user specified level. The client 2 display 5 may include a re-sizable viewing window with minimal penalty on the realtime performance of the system. This is not true of previous approaches. There also may be an auxiliary navigation window (which can be re-sized but is best kept fairly small because it displays the entire image at a low resolution). The main purpose of such a navigation window would be to let the viewer know the size and position of the viewing window in relation to the whole image.

It is readily seen that further modifications within the scope of the invention provide further advantages to the user. For example, without limitation, the invention may have the following capabilities: continuous realtime panning, continuous realtime zooming, foveating, varying the foveal resolution and modification of the shape and size of the foveal region. A variable resolution feature may also allow the server 1 to dynamically adjust the amount of transmitted data to match the effective bandwidth of the network.

While the above description contains many specificities, these should not be construed as limitations on the scope of the invention, but rather as an exemplification of one preferred embodiment thereof. Many other variations are possible. Accordingly, the scope of the invention should be determined not by the embodiment(s) illustrated, but by the appended claims and their legal equivalents.

What is claimed is:

1. A client apparatus for enabling a realtime visualization of at least one image, the client apparatus comprising:
a storage device storing first data corresponding to a multifoveated representation of an original image,
a user input device providing second data corresponding to at least one visualization command of at least one user; and
a processing arrangement generating third data corresponding to a multifoveated image using the first data, the second data and a foveation operator.
2. The client apparatus of claim $\mathbf{1}$, further comprising a network protocol processing element which provides the third data using a TCP/IP protocol.
3. The client apparatus of claim 1 , wherein the processing element transmits the third data to the at least one client via the Internet.
4. The client apparatus of claim 1 , wherein the user input device includes a mouse device.
5. The client apparatus of claim $\mathbf{1}$, wherein the user input device includes at least one of an eye-tracking device and a keyboard.
6. The client apparatus of claim 1 , wherein the foveation operator is specified using parameters that include at least one of:
a set of foveation points,
a shape of a foveated region,
a maximum resolution of the foveated region, and
a rate at which a maximum resolution of the foveal region decays.
7. The client apparatus of claim 1 ,
wherein the processing arrangement receives the original image from a server, and
wherein the memory arrangement stores a data structure representing the multifoveated image, the data structure that is optimized for the client apparatus being independent of an image representation provided by a server.
8. The client apparatus of claim 1, wherein the third data corresponding to the multifoveated image is generated for at least one of
a first arbitrary-shaped foveal region,
a second arbitrarily-fine foveal region, and
an arbitrary union of the first and second foveal regions.

## Dawson et al.

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[54] METHOD AND APPARATUS FOR GENERATING A TEXTURE MAPPED PERSPECTIVE VIEW
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[52] U.S. Cl.
395/125; 395/127;
395/130
[58] Field of Search 395/125, 126, 127, 130; 364/443, 723; 340/729

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## [57] ABSTRACT

A method and apparatus for providing a texture mapped perspective view for digital map systems. The system includes apparatus for storing elevation data, apparatus for storing texture data, apparatus for scanning a projected view volume from the elevation data storing apparatus, apparatus for processing, apparatus for generating a plurality of planar polygons and apparatus for rendering images. The processing apparatus further includes apparatus for receiving the scanned projected view volume from the scanning apparatus, transforming the scanned projected view volume from object space to screen space, and computing surface normals at each vertex of each polygon so as to modulate texture space pixel intensity. The generating apparatus generates the plurality of planar polygons from the transformed vertices and supplies them to the rendering apparatus which then shades each of the planar polygons. In one alternate embodiment of the invention, the polygons are shaded by apparatus of the rendering apparatus assigning one color across the surface of each polygon. In yet another alternate embodiment of the invention, the rendering apparatus interpolates the intensities between the vertices of each polygon in a linear fashion as in Gouraud shading.

8 Claims, 7 Drawing Sheets


Fig.-1





Fig.-9



Fig.-10D


## METHOD AND APPARATUS FOR GENERATING A TEXTURE MAPPED PERSPECTIVE VIEW

The present invention is directed generally to graphic display systems and, more particularly, to a method and apparatus for generating texture mapped perspective views for a digital map system.

## RELATED APPLICATIONS

The following applications are included herein by reference:
(1) U.S. Pat. No. 4,876,651 filed May 11, 1988, issued Oct. 24, 1989 entitled "Digital Map System" which was assigned to the assignee of the present invention:
(2) Assignee copending application Ser. No. 09/514,685 filed Apr. 26, 1990, entitled "High Speed Processor for Digital Signal Processing";
(3) U.S. Pat. No. $4,884,220$ entitled "Generator with Variable Scan Patterns" filed Jun. 7. 1988, issued Nov. 28,1989 , which is assigned to the assignee of the present invention;
(4) U.S. Pat. No. 4,899,293 entitled "A method of Storage and Retrieval of Digital Map Data Based Upon a Tessellated Geoid System", filed Dec. 14, 1988, issued Feb. 6, 1990:
(5) U.S. Pat. No. 5,020,014 entitled "Generic Interpolation Pipeline Processor", filed Feb. 7, 1989, issued May 28, 1991, which is assigned to the assignee of the present invention;
(6) Assignee's copending patent application Ser. No. 07/732,725 filed Jul. 18, 1991 entitled "Parallel Polygon/Pixel Rendering Engine Architecture for Computer Graphics" which is a continuation of patent application $07 / 419,722$ filed Oct. 11, 1989 now abandoned;
(7) Assignee's copending patent application Ser. No. 07/514,724 filed Apr. 26, 1990 entitled "Polygon Tiling Engine";
(8) Assignee's copending patent application Ser. No. 07/514,723 filed Apr. 26, 1990 entitled "Polygon Sort Engine"; and
(9) Assignee's copending patent application Ser. No. 07/514,742 filed Apr. 26, 1990 entitled "Three Dimensional Computer Graphic Symbol Generator".

## BACKGROUND OF THE INVENTION

Texture mapping is a computer graphics technique which comprises a process of overlaying aerial reconnaissance photographs onto computer generated three dimensional terrain images. It enhances the visual reality of raster scan images substantially while incurring a relatively small increase in computational expense. A frequent criticism of known computer-generated synthesized imagery has been directed to the extreme smoothness of the image. Prior art methods of generating images provide no texture, bumps, outcroppings, or natural abnormalities in the display of digital terrain elevation data (DTED).

In general, texture mapping maps a multidimensional image to a multidimensional space. A texture may be 60 thought of in the usual sense such as sandpaper, a plowed field, a roadbed, a lake, woodgrain and so forth or as the pattern of pixels (picture elements) on a sheet of paper or photographic film. The pixels may be arranged in a regular pattern such as a checkerboard or may exhibit high frequencies as in a detailed photograph of high resolution LandSat imagery. Texture may also be three dimensional in nature as in marble or
woodgrain surfaces. For the purposes of the invention, texture mapping is defined to be the mapping of a texture onto a surface in three dimensional object space. As is illustrated schematically in FIG. 1, a texture space object $T$ is mapped to a display screen by means of a perspective transformation.

The implementation of the method of the invention comprises two processes. The first process is geometric warping and the second process is filtering. FIG. 2 illustrates graphically the geometric warping process of the invention for applying texture onto a surface. This process applies the texture onto an object to be mapped analogously to a rubber sheet being stretched over a surface. In a digital map system application, the texture typically comprises an aerial reconnaissance photograph and the object mapped is the surface of the digital terrain data base as shown in FIG. 2. After the geometric warping has been completed, the second process of filtering is performed. In the second process, the image is resampled on the screen grid.
The invention provides a texture mapped perspective view architecture which addresses the need for increased aircraft crew effectiveness, consequently reducing workload, in low altitude flight regimes characterized by the simultaneous requirement to avoid certain terrain and threats. The particular emphasis of the invention is to increase crew situational awareness. Crew situational awareness has been increased to some degree through the addition of a perspective view map display to a plan view capability which already exists in digital map systems. See, for example, assignee's copending application Ser. No. 07/192,798, for a DIGITAL MAP SYSTEM, filed May 11, 1988, issued Oct. 24, 1989 as U.S. Pat. No. $4,876,651$ which is incorporated herein by reference in its entirety. The present invention improves the digital map system capability by providing a means for overlaying aerial reconnaissance photographs over the computer generated three dimensional terrain image resulting in a one-to-one correspondence from the digital map image to the real world. In this way the invention provides visually realistic cues which augment the informational display of such a computer generated terrain image. Using these cues an aircraft crew can rapidly make a correlation between the display and the real world.

The architectural challenge presented by texture mapping is that of distributing the processing load to achieve high data throughput using parallel pipelines and then recombining the parallel pixel flow into a single memory module known as a frame buffer. The resulting contention for access to the frame buffer reduces the effective throughput of the pipelines in addition to requiring increased hardware and board space to implement the additional pipelines. The method and apparatus of the invention addresses this challenge by effectively combining the low contention attributes of a single high speed pipeline with the increased processing throughput of parallel pipelines.

## SUMMARY OF THE INVENTION

A method and apparatus for providing a texture mapped perspective view for digital map systems is provided. The invention comprises means for storing elevation data, means for storing texture data, means for scanning a projected view volume from the elevation data storing means, means for processing the projected view volume, means for generating a plurality of planar polygons and means for rendering images. The process-
ing means further includes means for receiving the scanned projected view volume from the scanning means, transforming the scanned projected view volume from object space to screen space, and computing surface normals at each vertex of each polygon so as to modulate texture space pixel intensity. The generating means generates the plurality of planar polygons from the transformed vertices and supplies them to the rendering means which then shades each of the planar polygons.

A primary object of the invention is to provide a technology capable of accomplishing a fully integrated digital map display system in an aircraft cockpit.

In one alternate embodiment of the invention, the polygons are shaded by means of the rendering means assigning one color across the surface of each polygon.

In yet another alternate embodiment of the invention, the rendering means interpolates the intensities between the vertices of each polygon in a linear fashion as in Gouraud shading.
It is yet another object of the invention to provide a digital map system including capabilities for perspective view, transparency, texture mapping, hidden line removal, and secondary visual effects such as depth cues and artifact (i.e., anti-aliasing) control.

It is yet another object of the invention to provide the capability for displaying forward looking infrared (FLIR) data and radar return images overlaid onto a plan and perspective view digital map image by fusing images through combining or subtracting other sensor video signals with the digital map terrain display.
It is yet another object of the invention to provide a digital map system with an arbitrary warping capability of one data base onto another data base which is accommodated by the perspective view texture mapping capability of the invention.
Other objects, features and advantages of the invention will become apparent to those skilled in the art through the drawings, description of the preferred embodiment and claims herein. In the drawings, like numerals refer to like elements.

## BRIEF DESCRIPTION OF THE DRAWINGS

FIG. 1 shows the mapping of a textured object to a display screen by a perspective transformation.
FIG. 2 illustrates graphically the geometric warping process of the invention for applying texture onto a surface.
FIG. 3 illustrates the surface normal calculation as employed by the invention.
FIG. 4 presents a functional block diagram of one embodiment of the invention.
FIG. 5 illustrates a top level block diagram of one embodiment of the texture mapped perspective view architecture of the invention.
FIG. 6 schematically illustrates the frame buffer configuration as employed by one embodiment of the invention.
FIGS. $7 a, 7 b$ and $7 c$ illustrate three examples of display format shapes.
FIG. 8 graphs the density function for maximum pixel counts.
FIG. 9 is a block diagram of one embodiment of the geometry array processor as employed by the invention.
FIGS. 10A, 10B, 10C and 10D illustrated the tagged architectural texture mapping as provided by the invention.

## DESCRIPTION OF THE PREFERRED EMBODIMENT

Generally, perspective transformation from texture 5 space having coordinates U, V to screen space having coordinates X , Y requires an intermediate transformation from texture space to object space having coordinates $\mathrm{X}_{0}, \mathrm{Y}_{0}, \mathrm{Z}_{0}$. Perspective transformation is accomplished through the general perspective transform equation as follows:

$$
\left[\begin{array}{lll}
X & Y & H
\end{array}\right]=\left[\begin{array}{lll}
X & Y & Z
\end{array}\right] X X\left[\begin{array}{lllll}
A & B & C & \mid & P \\
D & E & F & \mid & Q \\
G & H & I & \mid & R \\
L & M & N & \mid & S
\end{array}\right]
$$

where a point ( $\mathrm{X}, \mathrm{Y}, \mathrm{Z}$ ) in 3 -space is represented by a four dimensional position vector [ X Y Z H ] in homogeneous coordinates.

The $3 \times 3$ sub-matrix

$$
\left[\begin{array}{lll}
A & B & C \\
D & E & F \\
G & H & I
\end{array}\right]
$$

0 accomplishes scaling, shearing, and rotation.
The $1 \times 3$ row matrix [ L M N ] produces translation.
The $3 \times 1$ column matrix

$$
\left[\begin{array}{l}
P \\
Q \\
R
\end{array}\right]
$$

produces perspective transformation.
The $1 \times 1$ scalar $[\mathrm{S}]$ produces overall scaling.
The Cartesian cross-product needed for surface normal requires a square root. As shown in FIG. 3, the surface normal shown is a vector $\mathrm{A} \times \mathrm{B}$ perpendicular to the plane formed by edges of a polygon as repre5 sented by vectors $A$ and $B$, where $A \times B$ is the Cartesian cross-product of the two vectors. Normalizing the vector allows calculation for sun angle shading in a perfectly diffusing Lambertian surface. This is accomplished by taking the vector dot product of the surface 0 normal vector with the sun position vector. The resulting angle is inversely proportional to the intensity of the pixel of the surface regardless of the viewing angle. This intensity is used to modulate the texture hue and intensity value.

$$
\frac{A \times B}{\prod A\|\|B\|} \text { where } \begin{gathered}
A=A x^{2}+A y^{2}+A z^{2} \\
B=B x^{2}+B y^{2}+B z^{2}
\end{gathered}
$$

A terrain triangle TT is formed by connecting the endpoints of vectors A and B , from point $\mathrm{B}_{X}, \mathrm{~B}_{Y}, \mathrm{~B}_{Z}$ to point $A_{X}, A_{Y}, A_{Z}$.

Having described some of the fundamental basis for the invention, a description of the method of the inven65 tion will now be set out in more detail below.

Referring now to FIG. 4, a functional block diagram of one embodiment of the invention is shown. The invention functionally comprises a means for storing ele-
vation data 10, a means for storing texture data 24 , a means for scanning a projected view volume from the elevation data storing means $\mathbf{1 2}$, means for processing view volume 14 including means for receiving the scanned projected view volume from the scanning means 12, means for generating polygon fill addresses 16 , means for calculating texture vertices addresses 18 , means for generating texture memory addresses 20 , means for filtering and interpolating pixels 26, a fullframe memory 22, and video display 9 . The processing means 14 further includes means for transforming the scanned projected view volume from object space to screen space and means for computing surface normals at each vertex of each polygon so as to calculate pixel intensity.

The means for storing elevation data 10 may preferably be a cache memory having at least a 50 nsec access time to achieve 20 Hz bi-linear interpolation of a $512 \times 512$ pixel resolution screen. The cache memory further may advantageously include a $256 \times 256$ bit buffer segment with 2 K bytes of shadow RAM used for the display list. The cache memory may arbitrarily be reconfigured from 8 bits deep (data frame) to 64 bits (i.e., comprising the sum of texture map data ( 24 bits) + DTED ( 16 bits)+aeronautical chart data ( 24 bits)). A buffer segment may start at any cache address and may be written horizontally or vertically. Means for storing texture data 24 may advantageously be a texture cache memory which is identical to the elevation cache memory except that it stores pixel information for warping onto the elevation data cache. Referring now to FIG. 5, a top level block diagram of the texrure mapped perspective view architecture is shown. The architecture implements the functions as shown in FIG. 4 and the discussion which follows shall refer to functional blocks in FIG. 4 and corresponding elements in FIG. 5. In some cases, such as element 14 , there is a one-to-one correspondence between the functional blocks in FIG. 4 and the architectural elements of FIG. 5. In other cases, as explained hereinbelow, the functions depicted in FIG. 4 are carried out by a plurality of elements shown in FIG. 5. The elements shown in FIG. 5 comprising the texture mapped perspective view system 300 of the invention include elevation cache memory 10, shape address generator (SHAG) 12, texture engine 30 , rendering engine 34 , geometry engine 36 , symbol generator 38 , tiling engine 40 , and display memory 42 . These elements are typically part of a larger digital map system including a digital map unit (DMU) 109, DMU interface 111, IC/DE 113, a display stream manager (DSM) 101, a general purpose processor (GPP) 105, RV MUX 121, PDQ 123, master time 44, video generator 46 and a plurality of data bases. The latter elements are described in assignee's Digital Map System U.S. Pat. No. 4,876,651.

## GEOMETRY ENGINE

The geometry engine 36 is comprised of one or more geometry array processors (GAPs) which process the $4 \times 4$ Euler matrix transformation from object space (sometimes referred to as "world" space) to screen space. The GAPs generate X and Y values in screen coordinates and Zvv values in range depth. The GAPs also compute surface normals at each vertex of a polygon representing an image in object space via Cartesian cross-products for Gouraud shading, or they may assign one surface normal to the entire polygon for flat shading and wire mesh. Intensity calculations are performed
using a vector dot product between the surface normal or normals and the illumination source to implement a Lambertian diffusely reflecting surface. Hue and intensity values are then assigned to the polygon. The method and apparatus of the invention also provides a dot rendering scheme wherein the GAPs only transform one vertex of each polygon and the tiling engine 40, explained in more detail below, is inhibited. In this dot rendering format, hue and intensity are assigned based on the planar polygon containing the vertex and the rendering engine is inhibited. Dot polygons may appear in the same image as multiple vertex polygons or may comprise the entire image itself. The "dots" are passed through the polygon rendering engine 34. A range to the vertices or polygon ( Zvv ) is used if a fog or "DaVinci" effect are invoked as explained below. The GAPs also transform three dimensional overlay symbols from world space to screen space.

Referring now to FIG. 9, a block diagram of one example embodiment of a geometry array processor (GAP) is shown. The GAP comprises a data register file memory 202, a floating point multiplier 204, a coefficient register file memory 206, a floating point accumulator $\mathbf{2 0 8}$, a 200 MHz oscillator 210 , a microsequencer 212, a control store RAM 214, and latch 216.

The register file memory may advantageously have a capacity of 512 by 32 bits. The floating point accumulator 208 includes two input ports 209A and 209B with independent enables, one output port 211, and a condition code interface 212 responsive to error codes. The floating point accumulator operates on four instructions, namely, multiply, no-op, pass A, and pass B. The microsequencer 212 operates on seven instructions including loop on count, loop on condition, jump, continue, call, return and load counter. The microsequencer includes a debug interface having a read/write ( $\mathrm{R} / \mathrm{W}$ ) internal register, $\mathrm{R} / \mathrm{W}$ control store memory, halt on address, and single step, and further includes a processor interface including a signal interrupt, status register and control register. The GAP is fully explained in the assignee's co-pending application No. 07/514,685 filed Apr. 26, 1990 entitled High Speed Processor for Digital Signal Processing which is incorporated herein by reference in its entirety.

In one alternative embodiment of the invention, it is possible to give the viewer of the display the visual effect of an environment enshrouded in fog. The fog option is implemented by interpolating the color of the triangle vertices toward the fog color. As the triangles get smaller with distance, the fog particles become denser. By using the known relationship between distance and fog density, the fog thickness can be "dialed" or adjusted as needed. The vertex assignment interpolates the vertex color toward the fog color as a function of range toward the horizon. The fog technique may be implemented in the hardware version of the GAP such as may be embodied in a GaAs semiconductor chip. If a linear color space (typically referred to as "RGB" to reflect the primary colors, red, green and blue) is assumed, the amount of fog is added as a function of range to the polygon vertices' color computation by well known techniques. Thus, as the hue is assigned by elevation banding or monochrome default value, the fog color is tacked on. The rendering engine 34, explained in more detail below, then straight forwardly interpolates the interior points.

In another alternative embodiment of the invention, a DaVinci effect is implemented. The DaVinci effect
causes the terrain to fade into the distance and blend with the horizon. It is implemented as a function of range of the polygon vertices by the GAP. The horizon color is added to the vertices similarly to the fog effect.

## SHAPE ADDRESS GENERATOR (SHAG)

The SHAG 12 receives the orthographically projected view volume outline onto cache from the DSM. It calculates the individual line lengths of the scans and the delta x and delta y components. It also scans the elevation posts out of the elevation cache memory and passes them to the GAPs for transformation. In one embodiment of the invention, the SHAG preferably includes two arithmetic logic units (ALUs) to support the $\mathbf{5 0}$ nsec cache 10. In the SHAG, data is generated for the GAPs and control signals are passed to the tiling engine 40. DFAD data is downloaded into overlay RAM (not shown) and three dimensional symbols are passed to the GAPs from symbol generator 38. Elevation color banding hue assignment is performed in this function. The SHAG generates shapes for plan view, perspective view, intervisibility, and radar simulation. These are illustrated in FIG. 7. The SHAG is more fully explained in assignee's copending application, Ser. No. 203,660, Generator With Variable Scan Patterns, filed Jun. 7, 1988 issued as U.S. Pat. No. 4,884,220 on Nov. 28, 1989 which is incorporated herein by reference in its entirety.
A simple Lambertian lighting diffusion model has proved adequate for generating depth cueing in one embodiment of the invention. The sun angle position is completely programmable in azimuth and zenith. It may also be self-positioning based on time of day, time of year, latitude and longitude. A programmable intensity with gray scale instead of color implements the moon angle position algorithm. The display stream manager (DSM) programs the sun angle registers. The illumination intensities of the moon angle position may be varied with the lunar waxing and waning cycles.

## TILING ENGINE AND TEXTURE ENGINE

Still referring to FIGS. 4 and 5, the means for calculating texture vertex address 18 may include the tiling engine 40 . Elevation posts are vertices of planar triangles modeling the surface of the terrain. These posts are "tagged" with the corresponding U,V coordinate address calculated in texture space. This tagging eliminates the need for interpolation by substituting an address lookup. Referring to FIGS. 10A, 10B, 10C and 10D, with continuing reference to FIGS. 4 and 5, the tagged architectural texture mapping as employed by the invention is illustrated. FIG. 10A shows an example of DTED data posts, DP, in world space. FIG. 10B shows the co-located texture space for the data posts. FIG. 10C shows the data posts and rendered polygon in screen space. FIG. 10D illustrates conceptually the interpolation of tagged addresses into a rendered polygon RP. The texture engine $\mathbf{3 0}$ performs the tagged data structure management and filtering processes. When the triangles are passed to the rendering engine by the tiling engine for filling with texture, the tagged texture address from the elevation post is used to generate the texture memory address. The texture value is filtered by filtering and interpolation means 26 before being written to full-frame memory $\mathbf{2 2}$ prior to display.
The tiling engine generates the planar polygons from the transformed vertices in screen coordinates and passes them to the rendering engine. For terrain poly-
gons, a connectivity offset from one line scan to the next is used to configure the polygons. For overlay symbols, a connectivity list is resident in a buffer memory (not shown) and is utilized for polygon generation. The tiling engine also informs the GAP if it is busy. In one embodiment 512 vertices are resident in a 1 K buffer.

All polygons having surface normals more than 90 degrees from LOS are eliminated from rendering. This is known in the art as backface removal. Such polygons do not have to be transformed since they will not be visible on the display screen. Additional connectivity information must be generated if the polygons are nonplanar as the transformation process generates implied edges. This requires that the connectivity information be dynamically generated. Thus, only planar polygons with less than 513 vertices are implemented. Non-planar polygons and dynamic connectivity algorithms are not implemented by the tiling engine. The tiling engine is further detailed in assignee's copending applications of even filing date herewith entitled Polygon Tiling Engine, as referenced hereinabove and Polygon Sort Engine, as referenced hereinabove, both of which are incorporated herein by reference.

## RENDERING ENGINE

Referring again to FIG. 5, the rendering engine 34 of the invention provides a means of drawing polygons in a plurality of modes. The rendering engine features may include interpolation algorithms for processing coordinates and color, hidden surface removal, contour lines, aircraft relative color bands, flat shading, Gourand shading, phong shading, mesh format or screen door effects, ridgeline display, transverse slice, backface removal and RECE (aerial reconnaissance) photo modes. With most known methods of image synthesis, the image is generated by breaking the surfaces of the object into polygons, calculating the color and intensity at each vertex of the polygon, and drawing the results into a frame buffer while interpolating the colors across the polygon. The color information at the vertices is calculated from light source data, surface normal, elevation and/or cultural features.

The interpolation of coordinate and color (or intensity) across each polygon must be performed quickly and accurately. This is accomplished by interpolating the coordinate and color at each quantized point or pixel on the edges of the polygon and subsequently interpolating from edge to edge to generate the fill lines. For hidden surface removal, such as is provided by a Z-buffer in a well-known manner, the depth or Z -value for each pixel is also calculated. Furthermore, since color components can vary independently across a surface or set of surfaces, red, green and blue intensities are interpolated independently. Thus, a minimum of six different parameters (X,Y,Z,R,G,B) are independently calculated when rendering polygons with Gouraud shading and interpolated Z -values.

Additional features of the rendering engine include a means of providing contour lines and aircraft relative color bands. For these features the elevation also is interpolated at each pixel. Transparency features dictate that an alpha channel be maintained and similarly interpolated. These requirements imply two additional axes of interpolation bringing the total to eight. The rendering engine is capable of processing polygons of one vertex in its dot mode, two vertices in its line mode, and three to 512 coplanar vertices in its polygon mode.

In the flat shading mode the rendering engine assigns the polygon a single color across its entire surface. An arbitrary vertex is selected to assign both hue and intensity for the entire polygon. This is accomplished by assigning identical RGB values to all vertices. Interpolation is performed normally but results in a constant value. This approach will not speed up the rendering process but will perform the algorithm with no hardware impact.

The Gouraud shading algorithm included in the rendering engine interpolates the intensities between the vertices of each polygon rendered in a linear fashion. This is the default mode. The Phong shading algorithm interpolates the surface normals between the vertices of the polygon between applying the intensity calculations. The rendering engine would thus have to perform an illumination calculation at each pixel after interpolation. This approach would significantly impact the hardware design. This algorithm may be simulated, however, using a weighing function (typically a function of cosine $(\theta)$ ) around a narrow band of the intensities. This results in a non-linear interpolation scheme and provides for a simulated specular reflectance. In an alternative embodiment, the GAP may be used to assign the vertices of the polygon this non-linear weighing via the look-up table and the rendering engine would interpolate as in Gouraud shading.

Transparency is implemented in the classical sense using an alpha channel or may be simulated with a screen door effect. The screen door effect simply renders the transparent polygon as normal but then only outputs every other or every third pixel. The mesh format appears as a wire frame overlay with the option of rendering either hidden lines removed or not. In the case of a threat dome symbol, all polygon edges must be displayed as well as the background terrain. In such a case, the fill algorithm of the rendering engine is inhibited and only the polygon edges are rendered. The intensity interpolation is performed on the edges which may have to be two pixels wide to eliminate strobing. In one embodiment, an option for terrain mesh includes the capability for tagging edges for rendering so that the mesh appears as a regular orthogonal grid.

Typical of the heads up display (HUD) format used in aircraft is the ridgeline display and the transverse slice. In the ridgeline format, a line drawing is produced from polygon edges whose slopes change sign relative to the viewpoint. All polygons are transformed, tiled, and then the surface normals are computed and compared to the viewpoint. The tiling engine strips away the vertices of non-ridge contributing edges and passes only the ridge polygons to the rendering engine. In transverse slice mode, fixed range bins relative to the aircraft are defined. A plane orthogonal to the view LOS is then passed through for rendering. The ridges then appear to roll over the terrain as the aircraft flies along. These algorithms are similar to backface removal. They rely upon the polygon surface normal being passed to the tiling engine.

One current implementation of the invention guarantees non-intersecting polygon sides by restricting the polygons rendered to be planar. They may have up to 512 vertices. Polygons may also consist of one or two vertices. The polygon "end" bit is set at the last vertex and processed by the rendering engine. The polygon is tagged with a two bit rendering code to select mesh, transparent, or Gouraud shading. The rendering engine

A Level I DTED data base is included in one embodiment of the invention and is advantageously sampled on three arc second intervals. Buffer segments are preferably stored at the highest scales ( 104.24 nm ) and the densest data ( 13.03 nm ). With such a scheme, all other scales can be created. A Level II DTED data base is also included and is sampled at one arc second inter-

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vals. Buffer segments are preferably stored only at the densest data ( 5.21 nm ).
A DFAD cultural feature data base is stored in a display list of 2 K words for each buffer segment. The data structure consists of an icon font call, a location in cache, and transformation coefficients from model space to world space consisting of scaling, rotation, and position (translation). A second data structure comprises a list of polygon vertices in world coordinates and a color or texture. The DFAD data may also be rasterized and overlaid on a terrain similar to aerial reconnaissance photos.

Aeronautical charts at the various scales are warped into the tessellated geoid. This data is 24 bits deep. Pixel data such as LandSat, FLIR, data frames and other scanned in source data may range from one bit up to 24 bits in powers of two ( $1,2,4,8,16,24$ ).

## FRAME BUFFER CONFIGURATION

Referring again to FIG. 6, the frame buffer configuration of one embodiment of the invention is shown schematically. The frame buffer configuration is implemented by one embodiment of the invention comprises a polygon rendering chip 34 which supplies data to full-frame memory 42. The full-frame memory 42 advantageously includes first-in, first-out buffers (FIFO) $F_{1}, F_{2}, F_{3}$ and $F_{4}$. As indicated above with respect to the discussion of the rendering engine, the memory is divided up into one pixel wide columns as shown in FIG. 6. By doing so, however, chip select must changed on every pixel when the master timer 44 shown in FIG. 5 reads the memory. However, by orienting the SHAG scan lines at 90 degrees to the master timer scan lines, the chip select will change on every line. The SHAG starts scanning at the bottom left corner of the display and proceeds to the upper left corner of the display.

With the image broken up in this way, the probability that the GIPP will write to the same FIFO two times in a row, three times, four, and so on can be calculated to determine how deep the FIFO must be. Decoding on the lower order address bits means that the only time the rendering engine will write to the same FIFO twice in a row is when a new scan line is started. At four deep as shown in the frame buffer graph 100 , the chances of the FIFO filling up are approximately one in 6.4 K . With an image of 1 million pixels, this will occur an acceptably small number of times for most applications. The perspective view transformations for 10,000 polygons with the power and board area constraints that are imposed by an avionics environment is significant. The data throughput for a given scene complexity can be achieved by adding more pipeline in parallel to the architecture. It is desirable to have as few pipelines as possible, preferably one, so that the image reconstruction at the end of the pipeline does not suffer from an arbitration bottleneck for a Z-buffered display memory.

In one embodiment of the invention, the processing throughput required has been achieved through the use of GaAs VSLI technology for parallel pipelines and a parallel frame buffer design has eliminated contention bottlenecks. A modular architecture allows for additional functions to be added to further the integration of the digital map into the avionics suite. The system architecture of the invention has high flexibility while maintaining speed and data throughput. The polygonal data base structure approach accommodate arbitrary scene complexity and a diversity of data base types.

The data structure of the invention is tagged so that any polygon may be rendered via any of the implemented schemes in a single frame. Thus, a particular image may have Gouraud shaded terrain, transparent threat domes. flat shaded cultural features, lines, and dots. In addition, since each polygon is tagged, a single icon can be comprised of differently shaded polygons. The invention embodies a 24 bit color system, although a production map would be scaled to 12 bits. A 12 bit system provides 4 K colors and would require a 32 K by 8 RGB RAM look-up table (LUT).

## MISCELLANEOUS FEATURES

The display formats in one example of the invention are switchable at less than 600 milliseconds between paper chart, DLMS plan and perspective view. A large cache ( 1 megabit D-RAMs) is required for texture mapping. Other format displays warp chart data over DTED, or use DTED to pseudo-color the map. For example, change the color palate LUT for transparency. The GAP is used for creating a true orthographic projection of the chart data.

An edit mode for three dimensions is supported by the apparatus of the invention. A three dimensional object such as a "pathway in the sky" may be tagged for editing. This is accomplished by first, moving in two dimensions at a given AGL, secondly, updating the AGL in the three dimensional view, and finally, updating the data base.

The overlay memory from the DMC may be video mixed with the perspective view display memory.

Freeze frame capability is supported by the invention. In this mode, the aircraft position is updated using the cursor. If the aircraft flies off the screen, the display will snap back in at the appropriate place. This capability is implemented in plan view only. There is data frame software included to enable roaming through cache memory. This feature requires a two axis roam joystick or similar control. Resolution of the Z-buffer is 16 bits. This allows 64 K meters down range.

The computer generated imagery has an update rate of 20 Hz . The major cycle is programmable and variable with no frame extend invoked. The system will run as fast as it can but will not switch ping-pong display memories until each functional unit issues a "pipeline empty" message to the display memory. The major cycle may also be locked to a fixed frame in multiples of 16.6 milliseconds. In the variable frame mode, the processor clock is used for a smooth frame interpolation for roam or zoom. The frame extend of the DMC is eliminated in perspective view mode. Plan view is implemented in the same pipeline as the perspective view. The GPP 105 loads the countdown register on the master timer to control the update rate.

The slowest update rate is 8.57 Hz . The image must be generated in this time or the memories will switch. This implies a pipeline speed of 40 million pixels per second. In a $512 \times 512$ image, it is estimated that there would be 4 million pixels rendered worst case with heavy hidden surface removal. In most cases, only million pixels need be rendered. FIG. 8 illustrates the analysis of pixel over-writes. The minimum requirement for surface normal resolution so that the best image is achieved is 16 bits. Tied to this is the way in which the normal is calculated. Averaging from surrounding tiles gives a smoother image on scale change or zoom. Using one tile is less complex, but results in poorer image
quality. Surface normal is calculated on the fly in accordance with known techniques.

## DISPLAY MEMORY

This memory is a combination of scene and overlay with a Z-buffer. It is distributed or partitioned for optimal loading during write, and configured as a frame buffer during read-out. The master time speed required is approximately 50 MHz . The display memory resolution can be configured as $512 \times 512 \times 12$ or as $1024 \times 1024 \times 12$. The Z -buffer is 16 bits deep and $1 \mathrm{~K} \times 1 \mathrm{~K}$ resolution. At the start of each major cycle, the $Z$-values are set to plus infinity (FF Hex). Infinity ( $\mathrm{Zmax}_{\text {m }}$ ) is programmable. The back clipping plane is set by the DSM over the control bus.

At the start of each major cycle, the display memory is set to a background color. In certain modes such as mesh or dot, this color will change. A background color register is loaded by the DSM over the configuration bus and used to fill in the memory.

## VIDEO GENERATOR/MASTER TIMER

The video generator 46 performs the digital to analog conversion of the image data in the display memory to send to the display head. It combines the data stream from the overlay memory of the DMC with the display memory from the perspective view. The configuration bus loads the color map.

A 30 Hz interlaced refresh rate may be implemented in a system employing the present invention. Color pallets are loadable by the GPP. The invention assumes a linear color space in RGB. All colors at zero intensity go to black.

## THREE DIMENSIONAL SYMBOL GENERATOR

The three-dimensional symbol generator 38 performs the following tasks:

1. It places the model to world transformation coefficients in the GAP.
2. It operates in cooperation with the geometry engine to multiply the world to screen transformation matrix by the model to world transformation matrix to form a model to screen transformation matrix. This matrix is stored over the model to world transformation matrix.
3. It operates in cooperation with the model to screen transformation matrix to each point of the symbol from the vertex list to transform the generic icon to the particular symbol.
4. It processes the connectivity list in the tiling engine and forms the screen polygons and passes them to the rendering engine.

One example of a three-dimensional symbol generator is described in detail in the assignee's aforereferenced patent application entitled "Three Dimensional Computer Graphic Symbol Generator".

The symbol generator data base consists of vertex list library and 64 K bytes of overlay RAM and a connectivity list. Up to 18 K bytes of DFAD (i.e., 2 K bytes display list from cache shadow RAM $\times 9$ buffer segments) are loaded into the overlay RAM for cultural feature processing. The rest of the memory holds the threat/intelligence file and the mission planning file for the entire gaming area. The overlay RAM is loaded over the control bus from the DSM processor with the threat and mission planning files. The SHAG loads the DFAD files. The symbol libraries are updated via the configuration bus.

The vertex list contains the relative vertex positions of the generic library icons. In addition, it contains a 16 bit surface normal, a one bit end of polygon flag, and a one bit end of symbol flag. The table is $32 \mathrm{~K} \times 16$ bits. A maximum of 512 vertices may be associated with any given icon. The connectivity list contains the connectivity information of the vertices of the symbol. A 64 K by 12 bit table holds this information.

A pathway in the sky format may be implemented in this system. It consists of either a wire frame tunnel or an elevated roadbed for flight path purposes. The wire frame tunnel is a series of connected transparent rectangles generated by the tiling engine of which only the edges are visible (wire mesh). Alternatively, the polygons may be precomputed in world coordinates and stored in a mission planning file. The roadbed is similarly comprised of polygons generated by the tiler along a designated pathway. In either case, the geometry engine must transform these polygons from object space (world coordinate system) to screen space. The transformed vertices are then passed to the rendering engine. The parameters (height, width, frequency) of the tunnel and roadbed polygons are programmable.

Another symbol used in the system is a waypoint flag. Waypoint flags are markers consisting of a transparent or opaque triangle on a vertical staff rendered in perspective. The waypoint flag icon is generated by the symbol generator as a macro from a mission planning file. Alternatively, they may be precomputed as polygons and stored. The geometry engine receives the vertices from the symbol generator and performs the perspective transformation on them. The geometry engine passes the rendering engine the polygons of the flag staff and the scaled font call of the alphanumeric symbol. Plan view format consists of a circle with a number inside and is not passed through the geometry engine.

DFAD data processing consists of a generalized polygon renderer which maps 32 K points possible down to 256 polygons or less for a given buffer segment. These polygons are then passed to the rendering engine. This approach may redundantly render terrain and DFAD for the same pixels but easily accommodates declutter of individual features. Another approach is to rasterize the DFAD and use a texture warp function to color the terrain. This would not permit declutter of individual features but only classes (by color). Terrain color show-through in sparse overlay areas would be handled by a transparent color code (screen door effect). No verticality is achieved.

There are 298 categories of aerial, linear, and point features. Linear features must be expanded to a double line to prevent interlace strobing. A point feature contains a length, width, and height which can be used by the symbol generator for expansion. A typical lake contains 900 vertices and produces 10 to 20 active edges for rendering at any given scan line. The number of vertices is limited to 512 . The display list is 64 K bytes for a 1:250K buffer segment. Any given feature could have 32 K vertices.

Up to 2 K bytes of display list per buffer segment DTED is accommodated for DFAD. The DSM can tag the classes or individual features for clutter/declutter by toggling bits in the overlay RAM of the SHAG.
The symbol generator processes macros and graphic primitives which are passed to the rendering engine. These primitives include lines, arcs, alphanumerics, and two dimensional symbology. The rendering engine
draws these primitives and outputs pixels which are anti-aliased. The GAP transforms these polygons and passes them to the rendering engine. A complete $4 \times 4$ Euler transformation is performed. Typical macros include compass rose and range scale symbols. Given a macro command, the symbol generator produces the primitive graphics calls to the rendering engine. This mode operates in plan view only and implements two dimensional symbols. Those skilled in the art will appreciate that the invention is not limited to specific fonts.

Three dimensional symbology presents the problem of clipping to the view volume. A gross clip is handled by the DSM in the cache memory at scan out time. The base of a threat dome, for example, may lie outside the orthographic projection of the view volume onto cache, yet a part of its dome may end up visible on the screen. The classical implementation performs the functions of tiling, transforming, clipping to the view volume (which generates new polygons), and then rendering. A gross clip boundary is implemented in cache around the view volume projection to guarantee inclusion of the entire symbol. The anomaly under animation to be avoided is that of having symbology sporadically appear and disappear in and out of the frame at the frame boundaries. A fine clip to the screen is performed downstream by the rendering engine. There is a 4 K boundary around the screen which is rendered. Outside of this boundary, the symbol will not be rendered. This causes extra rendering which is clipped away.

Threat domes are represented graphically in one embodiment by an inverted conic volume. A threat/intelligence file contains the location and scaling factors for the generic model to be transformed to the specific threats. The tiling engine contains the connectivity information between the vertices and generates the planar polygons. The threat polygons are passed to the rendering engine with various viewing parameters such as mesh, opaque, dot, transparent, and so forth.

Graticles represent latitude and longitude lines, UTM klicks, and so forth which are warped onto the map in 40 perspective. The symbol generator produces these lines.

Freeze frame is implemented in plan view only. The cursor is flown around the screen, and is generated by the symbol generator.

Programmable blink capability is accommodated in 45 the invention. The DSM updates the overlay RAM toggle for display. The processor clock is used during variable frame update rate to control the blink rate.

A generic threat symbol is modeled and stored in the three dimensional symbol generation library. Parameters such as position, threat range, and angular threat view are passed to the symbol generator as a macro call (similar to a compass rose). The symbol generator creates a polygon list for each threat instance by using the parameters to modify the generic model and place it in the world coordinate system of the terrain data base. The polygons are transformed and rendered into screen space by the perspective view pipeline. These polygons form only the outside envelope of the threat cone.

This invention has been described herein in consider- 60 able detail in order to comply with the Patent Statues and to provide those skilled in the art with the information needed to apply the novel principles and to construct and use such specialized components as are required. However, it is to be understood that the invention can be carried out by specifically different equipment and devices, and that various modifications, both as to the equipment details and operating procedures,
can be accomplished without departing from the scope of the invention itself.

What is claimed is:

1. A system for providing a texture mapped perspec5 tive view for a digital map system wherein objects are transformed from texture space having $\mathrm{U}, \mathrm{V}$ coordinates to screen space having $\mathrm{X}, \mathrm{Y}$ coordinates comprising:
(a) a cache memory means for storing terrain data including elevation posts, wherein the cache memory means includes an output and an address bus;
(b) a shape address generator means for scanning cache memory having an ADDRESS SIGNAL coupled to the cache memory means address bus wherein the shape address generator means scans the elevation posts out of the cache memory means;
(c) a geometry engine coupled to the cache memory means output to receive the elevation posts scanned from the cache memory by the shape address generator means, the geometry engine including means for
i. transformation of the scanned elevation posts from object space to screen space so as to generate transformed vertices in screen coordinates for each elevation post, and
ii. generating three dimensional coordinates;
(d) a tilling engine coupled to the geometry engine for generating planar polygons from the generated three dimensional coordinates;
(e) a symbol generator to the geometry engine for transmitting a vertex list to the geometry engine wherein the geometry engine operates on the vertex list to transform the vertex list into screen space $\mathrm{X}, \mathrm{Y}$ coordinates and passes the screen space $\mathrm{X}, \mathrm{Y}$ coordinates to the tilling engine for generating planar polygons which form icons for display and processing information from the tilling engine into symbols,
(f) a texture engine means coupled to receive the ADDRESS SIGNAL from the shape address generator means including a texture memory and including a means for generating a texture vertex address to texture space correlated to an elevation post address and further including a means for generating a texture memory address for scanning the texture memory wherein the texture memory provides texture data on a texture memory data bus in response to being scanned by the texture memory address;
(g) a rendering engine having an input coupled to the tilling engine and the texture memory data bus for generating image data from the planar polygons; and
(h) a display memory for receiving image data from the rendering engine output wherein the display memory includes at least four first-in, first-out memory buffers.
2. The apparatus of claim $\mathbf{1}$ wherein each polygon has a surface and the rendering means assigns one color across the surface of each polygon.
3. The apparatus of claim $\mathbf{1}$ wherein the vertices of each polygon have an intensity and the rendering means interpolates the intensities between the vertices of each polygon in a linear fashion.
4. The apparatus of claim 1 wherein the rendering means further includes means for generating transparent polygons and passing the transparent polygon to the display memory.
5. A method for providing a texture mapped perspective view for a digital map system having a cache memory, a geometry engine coupled to the cache memory, a shape address generator coupled to the cache memory, a tiling engine coupled to the geometry engine, a symbol generator coupled to the geometry engine and the tiling engine, a texture engine coupled to the cache memory, a rendering engine coupled to the tiling engine and the texture engine, and a display memory coupled to the rendering engine, wherein objects are transformed from texture space having $\mathrm{U}, \mathrm{V}$ coordinates to screen space having $\mathrm{X}, \mathrm{Y}$ coordinates, the method comprising the steps of:
(a) storing terrain data, including elevation posts, in the cache memory;
(b) scanning the cache memory to retrieve the elevation posts;
(c) transforming the terrain data from elevation posts in object space to transformed vertices in screen space, and
(d) generating planar polygons from the generated three dimensional coordinates;
(e) transmitting a vertex list to the geometry engine, operating the geometry engine to transform the vertex list into screen space $X, Y$ coordinates and passing the screen space $\mathrm{X}, \mathrm{Y}$ coordinates to the further includes the steps of assigning one color across the surface of each polygon.
6. The method of claim 5 wherein the vertices of each polygon have an intensity and the step of generating image data further includes the step of interpolating the intensities between the vertices of each polygon in a linear fashion.
7. The method of claim $\mathbf{5}$ wherein the step of generating image data further includes the step of generating transparent polygons and passing the transparent polygons to the display memory.


## UNITED STATES PATENT AND TRADEMARK OFFICE

## CERTIFICATE OF CORRECTION

```
PATENT NO. : 5,179,638
DATED : January 12, 1993
INVENTOR(S): John F. Dawson, Thomas D. Snodgrass, and
    James A. Cousens
```

It is certified that error appears in the above-indentified patent and that said Letters Patent is hereby corrected as shown below:

Column 17, line 21, after "and" insert --generating three dimensional coordinates for the transformed vertices in screen space--.

Signed and Sealed this
Twenty-second Day of March, 1994


Gen

# Pyramidal Parametrics 

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## Abstract

The mapping of images onto surfaces may substantially increase the realism and information content of computer-generated imagery. The projection of a flat source image onto a curved surface may involve sampling difficulties, however, which are compounded as the view of the surface changes. As the projected scale of the surface increases, interpolation between the original samples of the source image is necessary; as the scale is reduced, approximation of multiple samples in the source is required. Thus a constantly changing sampling window of view-dependent shape must traverse the source image.

To reduce the computation implied by these requirements, a set of prefiltered source images may be created. This approach can be applied to particular advantage in animation, where a large number of frames using the same source image must be generated. This paper advances a "pyramidal parametric" prefiltering and sampling geometry which minimizes aliasing effects and assures continuity within and between target images.

Although the mapping of texture onto surfaces is an excellent example of the process and provided the original motivation for its development, pyramidal parametric data structures admit of wider application. The aliasing of not only surface texture, but also highlights and even the surface representations themselves, may be minimized by pyramidal parametric means.

General Terms: Algorithms.
Keywords and Phrases: Antialiasing, Illumination Models, Modeling, Pyramidal Data Structures, Reflectance Mapping, Texture Mapping, Visible Surface Algorithms.

CR Categories: I.3.3 [Computer Graphics]: Picture/Image Generation--display algorithms; I.3.5 [Computer Graphics]: Computational Geometry and Object Modeling-curve, surface, solid and object representations, geometric algorithms, languages and systems; I.3.7 [Computer Graphics]: Three-Dimensional Graphics and Realism-color, shading, shadowing, and texture.

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## 1. Pyramidal Data Structures

Pyramidal data structures may be based on various subdivisions: binary trees, quad trees, oct trees, or ndimensional hierarchies [17]. The common feature of these structures is a succession of levels which vary the resolution at which the data is represented.

The decomposition of an image by two-dimensional binary subdivision was a pioneering strategy in computer graphics for visible surface determination [15]. The approach was essentially a synthesis-by-analysis: the image plane was subdivided into quadrants recursively until analysis of a subsection showed that surface ordering was sufficiently simple to permit rendering. Such subdivision and analysis has been subsequently adopted to generate spatial data structures [5], which have been used to represent images [9] both for pattern recognition [13] and for transmission [10], [14]. In the field of computer graphics, such data structures have been adopted for texture mapping [4], [16], and generalized to represent objects in space [11].

The application of pyramidal data to image storage and transmission may permit significant compression of the data to be stored or transmitted. This is so because highly detailed features may be localized within an otherwise low-frequency image, permitting the sampling rate to be reduced for large sections of the image. Besides permitting bandwidth compression, the representation orders data in such a way that the general character of images may be recalled or transmitted before the specific details.

Pattern recognition and classification often require the comparison of a candidate image against a set of canonical patterns. This is an operation the expense of which increases as the square of the resolution at which it is performed. The use of pyramidal data structures in pattern recognition and classification permits the comparison of the gross features of two-dimensional functions preliminary to the minute particulars; a good general reference on this application is [12].
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In computer graphics, pyramidal texture maps may be used to perform arbitrary mappings of a function with minimal aliasing artifacts and reduced computation. once again, images may be represented at different spatial bandwidths. The concern is that inappropriate resolution misrepresents the data; that is, sampling high-resolution data at larger sample intervals invites aliasing.

## 2. Parametric Interpolation

By a pyramidal parametric data structure, we will mean simply a pyramidal structure with both intra- and inter-level interpolation. Consider the case of an image represented as a two-dimensional array of samples. Interpolation is necessary to produce a continuous function of two parameters, U and V. If, in addition, a third parameter (call it D) moves us up and down a hierarchy of corresponding two-dimensional functions, with interpolation between (or among) the levels of the pyramid providing continuity, the structure is pyramidal parametric.

The practical distinction between such a structure and an ordinary interpolant over an n-dimensional array of samples is that the number of samples representing each level of the pyramid may be different.

## 3. Mip Mapping

"Mip" mapping is a particular format for two-dimensional parametric functions, which, along with its associated addressing scheme, has been used successfully to bandimit texture mapping at New York Institute of Technology since 1979. The acronym "mip" is from the Latin phrase "multum in parvo," meaning "many things in a small place." Mip mapping supplements bilinear interpolation of pixel values in the texture map (which may be used to smoothly translate and magnify the texture) with interpolation between prefiltered versions of the map (which may be used to compress many pixels into a small place). In this latter capacity, mip offers much greater speed than texturing algorithms which perform explicit convolution over an area in the texture map for each pixel rendered [1], [6].

Mip owes its speed in compressing texture to two factors. First, a fair amount of filtering of the original texture takes place when the mip map is first created. Second, subsequent filtering is approximated by blending different levels of the mip map. This means that all filters are approximated by linearly interpolating a set of square box filters, the sides of which are powers-of-two pixels in length. Thus, mapping entails a fixed overhead, which is independent of the area filtered to compute a sample.


Figure (1)
Structure of a Color Mip Map
Smaller and smaller images diminish into the upper left corner of the map. Each of the images is averaged down from its larger predecessor.
(Below:)
Mip maps are indexed by three coordinates: U, V, and D. U and V are spatial coordinates of the map; $D$ is the variable used to index, and interpolate between, the different levels of the pyramid.

samples) of its parent. Successive divisions by four partition the frame buffer equally among the three components, with a single unused pixel remaining in the upper left-hand corner.

The concept behind this memory organization is that corresponding points in different prefiltered maps can be addressed simply by a binary shift of an input $U, V$ coordinate pair. Since the filtering and sampling are performed at scales which are powers of two, indexing the maps is possible with inexpensive binary scaling. In a hardware implementation, the addresses in all the corresponding maps (now separate memories) would be instantly and simultaneously available from the $U, V$ input.

The routines for creating and accessing mip maps at NYIT are based on simple box (Fourier) window prefiltering, bilinear interpolation of pixels within each map instance, and linear interpolation between two maps for each value of $D$ (the pyramid's vertical coordinate). For each of the three components of a color mip map, this requires 8 pixel reads and 7 multiplications. This choice of filters is strictly for the sake of speed. Note that the bilinear interpolation of pixel values at the extreme edges of each map instance must be performed with pixels from the opposite edge(s) of that map, for texture which is periodic. For nonperiodic texture, scaling or clipping of the $U, V$ coordinates prevents the intrusion of an inappropriate map or color component into the interpolation.

The box (Fourier) window used to create the mip maps illustrated here, and the tent (Bartlett) window used to interpolate them, are far from ideal; yet probably the most severe compromise made by mip filtering is that it is symmetrical. Each of the prefiltered levels of the map is filtered equally in $X$ and $Y$. Choosing a value of $D$ trades off aliasing against blurring, which becomes a tricky proposition as a pixel's projection in the texture map deviates from symmetry. Heckbert [8] suggests:

$$
d=\max \left(\sqrt{\left(\frac{\partial u}{\partial x}\right)^{2}+\left(\frac{\partial v}{\partial x}\right)^{2}}, \sqrt{\left(\frac{\partial u}{\partial y}\right)^{2}+\left(\frac{\partial v}{\partial y}\right)^{2}}\right)
$$

where D is proportional to the "diameter" of the area in the texture to be filtered, and the partials of $U$ and $V$ (the texturemap coordinates) with respect to $X$ and $Y$ (the screen coordinates) can be calculated from the surface projection.

Illustrations of mapping performed by the mip technique are the subject of figures (2) through (10). The NYIT Test Frog in Figure (2) is magnified by simple point sampling in (3), and by interpolation in (4). The hapless amphibian is similarly


Figure (2)
Mip map of the flexible NYIT Test Frog.
compressed by point sampling in (5) and by mipping in (6).

The more general and interesting case -- continuously variable upsampling and downsampling of the original texture -- is illustrated in (7) on a variety of surfaces. Since the symmetry of mip filtering would be expected to show up badly when texture is compressed in only one dimension, figures (8) through (10) are of especial interest. These pictures, created by Ed Emshwiller at NYIT for his videotape, "Sunstone," were mapped using Alvy Ray Smith's TEXAS animation program, which in turn used MIP to antialias texture. As the panels rotate edge-on, the texture collapses to a line smoothly and without apparent artifacts.


Figure (7)
General mapping: interpolation and pyramidal compression.

Figure (3)
Upsampling the frog: magnification by
point sampling.


Figure (4)
Upsampling the frog: magnification by bilinear interpolation.


Figure (5)
Downsampling the frog: compression by point samolind (detail. rinht)


Downsampling: compression by pyramidal interpolation (detail, right).

## APPENDIX L



Figures (8)-(9)
"Sunstone" by Ed Emshwiller, segment animated by Alvy Ray Smith Pyramidal parametric texture mapping on polygons.

## APPENDIX L



Figures (10)-(11)
"Sunstone" by Ed Emshwiller, segment animated by Alvy Ray Smith Pyramidal parametric texture mapping on polygons.

## 4. Highlight Antialiasing

As small or highly curved objects move across a raster, their surface normails may beat erratically with the sampling grid. This causes the shading values to flash annoyingly in motion sequences, a symptom of illumination aliasing. The surface normals essentially point-sample the illumination function.

Figure (12) illustrates samples of the surface normals of a set of parallel cylinders. The cylinders in the diagram are depicted as if from the edge of the image plane; the regularly-spaced vertical line segments are the samples along a single axis. The arrows at the sample points indicate the directions of the surface normals. Depending on the shading formula invoked, there may be very high contrast between samples where the normal is nearly parallel to the sample axis, and samples where the normal points directly at the observer's eye.

Figure (12)


The shading function depends not only on the shape of the surface, but its light reflection properties (characterized by the shading formula), the position of the light source, and the position of the observer's eye. Hanrahan [7] expresses it in honest Greek:

$$
\int_{X} \int_{Y} \varphi(E, N, L) \frac{\partial(u, v)}{\partial(x, y)} d x d y
$$

where the normal, $N$, the light sources, $L$, and the eye, $E$, are vectors which may each be functions of $U$ and $V$, and the limits of integration are the $X, Y$ boundaries of the pixel.

Figure (13) illustrates highlight aliasing on a perfectly flat surface. The viewing conventions of the diagram are the same as in Figure (12). "L" is the direction vector of the light source; the surface is a polygon at an angle to the image plane; the dotted bump is a graph of the reflected light, characteristic of a

specular surface reflection function. The highlight indicated by the bump falls entirely between the samples. (Note that this is only possible on a flat surface if either the eye or the light is local, a point in space rather than simply a direction vector. Some boring shading formulae exclude the possibility of highlight aliasing on polygons by requiring all flat surfaces to be flat in shading.)

A first attempt to overcome the limitations of point-sampling the illumination function is to integrate the function over the projected area represented by each sample point. This approach is illustrated in Figure (14). The brackets at each sample represent the area of the surface over which the illumination function is integrated. This procedure is analogous to area-averaging of sampled edges or texture [3].

In order to generalize this approach to curved surfaces, the "sample interval" over which illumination is integrated must be modified according to the local curvature of the surface at a sample. In Figure (15), the area of a surface represented by a pixel has been projected onto a curved surface. The solid angle over which illumination must be integrated is approximated by the volume enclosed by the normals at the pixel corners. The distribution of light within this volume will sum to an estimate of the diffuse reflection over the pixel. If the surface exhibits undulations at the pixel level, however, aliasing will result.


Figure (15)


Figure (16)
Michael Chou (right) poses with an imaginary companion. Reflectance maps can enhance the realism of synthetic shading.


Figure (17)
A pyramidal parametric reflectance map, containing 9 light sources. The region outside the "snhera" ia unncod


Figure (18) Before

We might divide the surface up into regions of relatively low curvature (as is done in some patch rendering algorithms), and rely on "edge antialiasing" to integrate the different surfaces within a pixel. Alternatively, we may develop some mechanism for limiting the local curvature of surfaces before rendering. This possibility is explored in the next section.

If we represent the illumination of a scene as a two-dimensional map, highlights can be effectively antialiased in much the same way as textures. Blinn and Newell [1] demonstrated specular reflection using an illumination map. The map was an image of the environment (a spherical projection of the scene, indexed by the $X$ and $Y$ components of the surface normals) which could be used to cast reflections onto specular surfaces. The impression of mirrored facets and chrome objects which can be achieved with this method is striking; Figure (16) provides an illustration. Reflectance mapping is not, however, accurate for local reflections. To achieve similar results with three dimensional accuracy requires ray-tracing.

A pyramidal parametric illumination map permits convenient antialiasing of highlights as long as a good measure of local surface curvature is available. The value of "D" used to index the map is proportional to the solid angle subtended by the surface over the pixel being computed; this may be estimated by the same formula used to compute $D$ for ordinary texture mapping. Nine light sources of varying brightness glint raggedly from the test object in Figure (18); the reflectance map in Figure (17) provided the illumination. In Figure (19), convincing highıight antialiasing results from the full pyramidal parametric treatment.


Figure (19) After


Figures (20-23) Different resolution meshes.

## 5. Levels of Detail in Surface Representation

In addition to bandlimiting texture and illumination functions for mapping onto a surface, pyramidal parametrics may be used to limit the level of detail with which the surface itself is represented. The goal is to represent an object for graphic display as economically as its projection on the image plane permits, without boiling and sparkling aliasing artifacts as the projection changes.

The expense of computing and shading each pixel dominates the cost of many algorithms for rendering higher-order surfaces. For meshes of polygons or patch control points which project onto a small portion of the image, however, the vertex (or control-point) expense dominates. In these situations it is desirable to reduce the number of points used to represent the object.

A pyramidal parametric data structure the components of which are spatial coordinates (the $X-Y-Z$ of the vertices of $a$ rectangular mesh, for example, as opposed to the $R-G-B$ of a texture or illumination map) provides a continuously-variable filtered instance of the surface for sampling at any desired degree of resolution.

Figures (20) through (23) illustrate a simple surface based on a human face model developed by Fred Parke at the University of Utah. As the sampling density varies, so does the filtering of the surface. These faces are filtered and sampled by the same methods previously discussed for texture and reflectance maps. Pyramidal parametric representations such as these appear promising for reducing aliasing effects as well as systematically sampling very large data bases over a wide range of scales and viewing angles.

## 6. Conclusions

Pyramidal data structures are of proven value in image analysis and have interesting application to image bandwidth compression and transmission. "Pyramidal parametrics," pyramidal data structures with intra- and inter-level interpolation, are here proposed for use in image synthesis. By continuously varying the detail with which data are resolved, pyramidal parametrics provide economical approximate solutions to filtering problems in mapping texture and illumination onto surfaces, and preliminary experiments suggest they may provide flexible surface representations as well.

## 7. Acknowledgments

I would like to acknowledge Ed Catmull, the first (to my knowledge) to apply multiple prefiltered images to texture mapping: the method was applied to the bicubic patches in his thesis, although it was not described. Credit is also due Tom Duff, who wrote both recursive and scanorder routines for creating mip maps which preserved numerical precision over all map instances; Dick Lundin, who wrote the first assembly-coded mip map accessing routines; Ephraim Cohen, who wrote the second; Rick Ace, who translated Ephraim's PDP-ll versions for the VAX assembler; Paul Heckbert, for refining and speeding up both creation and accessing routines, and investigating various estimates of "D"; Michael Chou, for implementing highlight antialiasing and high-resolution reflectance mapping on quadric surfaces.

## I owe special thanks to Jules

 Bloomenthal, Michael Chou, Pat Hanrahan, and Paul Heckbert for critical reading and numerous helpful suggestions in the course of preparing this text. Photographic support was provided by Michael Lehman.
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## Mipmapping

TEXTURE_MIN_FILTER values NEAREST_MIPMAP_NEAREST, NEAREST_MIPMAP_LINEAR, LINEAR_MIPMAP_NEAREST, and LINEAR_MIPMAP_LINEAR each require the use of a mipmap. A mipmap is an ordered set of arrays representing the same image; each array has a resolution lower than the previous one. If the texture has dimensions $2^{n} \times 2^{m}$, then there are $\max \{n, m\}+1$ mipmap arrays. The first array is the original texture with dimensions $2^{n} \times 2^{m}$. Each subsequent array has dimensions $2^{(k-1)} \times 2^{(l-1)}$ where $2^{k} \times 2^{l}$ are the dimensions of the previous array. This is the case as long as both $\mathbf{k}>\mathbf{0}$ and $\mathbf{l}>\mathbf{0}$. Once either $\mathbf{k}=\mathbf{0}$ or $\mathbf{l}=\mathbf{0}$, each subsequent array has dimension $1 \times 2^{(t-1)}$ or $2^{(k-1)} \times 1$, respectively, until the last array is reached with dimension $1 \times 1$.

Each array in a mipmap is transmitted to the GL using TexImage2D or TexImage1D ; the array being set is indicated with the level-of-detail argument. Level-of-detail numbers proceed from $\mathbf{0}$ for the original texture array through $\boldsymbol{P}=\max \{n, m\}$ with each unit increase indicating an array of half the dimensions of the previous one as already described. If texturing is enabled (and TEXTURE_MIN_FILTER is one that requires a mipmap) at the time a primitive is rasterized and if the set of arrays $\mathbf{0}$ through $\mathbf{p}$ is incomplete, based on the dimensions of array $\mathbf{0}$, then it is as if texture mapping were disabled. The set of arrays $\mathbf{0}$ through $\mathbf{p}$ is incomplete if the internal formats of all the mipmap arrays were not specified with the same symbolic constant, or if the border widths of the mipmap arrays are not the same, or if the dimensions of the mipmap arrays do not follow the sequence described above. Arrays indexed greater than $\mathbf{p}$ are insignificant.

The mipmap is used in conjunction with the level of detail to approximate the application of an appropriately filtered texture to a fragment. Let $P=\max \{n, m\}$ and let $\mathbf{c}$ be the value of $\lambda$ at which the transition from minification to magnification occurs (since this discussion pertains to minification, we are concerned only with values of $\boldsymbol{\lambda}$ where $\boldsymbol{\lambda} \boldsymbol{\lambda} \boldsymbol{c}$ ). For NEAREST_MIPMAP_NEAREST, if $c<\lambda \leq 0.5$ then the mipmap array with level-of-detail of 0 is selected. Otherwise, the dth mipmap array is selected when $d-\frac{1}{2}<\lambda \leq d+\frac{1}{2}$ as long as $1 \leq d \leq p$. If $\lambda>p+\frac{1}{2}$, then the pth mipmap array is selected. The rules for neArest are then applied to the selected array.

The same mipmap array selection rules apply for LINEAR_MIPMAP_NEAREST as for NEAREST_MIPMAP_NEAREST, but the rules for LINEAR are applied to the selected array.

For neArest mipmap_Linear, the level d-1 and the level d mipmap arrays are selected, where $d-1 \leq \lambda<d$, unless $\lambda \geq P$, in which case the pth mipmap array is used for both arrays. The rules
for NEAREST are then applied to each of these arrays, yielding two corresponding texture values $\boldsymbol{\tau}_{\mathbb{I}} \boldsymbol{- 1}$ and $\boldsymbol{\tau}_{\boldsymbol{I}}$. The final texture value is then found as

$$
\tau=[1-\operatorname{frac}(\lambda)] \tau_{I-1}+\operatorname{frac}(\lambda) \tau_{I-}
$$

LINEAR_MIPMAP_LINEAR has the same effect as NEAREST_MIPMAP_LINEAR except that the rules for LINEAR are applied for each of the two mipmap arrays to generate $\boldsymbol{\tau}_{\boldsymbol{d}} \mathbf{I}$ and $\boldsymbol{\tau}_{\boldsymbol{d}}$.

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## David Blythe

Sat Mar 29 02:23:21 PST 1997

# Progressive Meshes 

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#### Abstract

Highly detailed geometric models are rapidly becoming commonplace in computer graphics. These models, often represented as complex triangle meshes, challenge rendering performance, transmission bandwidth, and storage capacities. This paper introduces the progressive mesh (PM) representation, a new scheme for storing and transmitting arbitrary triangle meshes. This efficient, lossless, continuous-resolution representation addresses several practical problems in graphics: smooth geomorphing of level-of-detail approximations, progressive transmission, mesh compression, and selective refinement. In addition, we present a new mesh simplification procedure for constructing a PM representation from an arbitrary mesh. The goal of this optimization procedure is to preserve not just the geometry of the original mesh, but more importantly its overall appearance as defined by its discrete and scalar appearance attributes such as material identifiers, color values, normals, and texture coordinates. We demonstrate construction of the PM representation and its applications using several practical models.


CR Categories and Subject Descriptors: I.3.5 [Computer Graphics]: Computational Geometry and Object Modeling - surfaces and object representations.
Additional Keywords: mesh simplification, level of detail, shape interpolation, progressive transmission, geometry compression.

## 1 INTRODUCTION

Highly detailed geometric models are necessary to satisfy a growing expectation for realism in computer graphics. Within traditional modeling systems, detailed models are created by applying versatile modeling operations (such as extrusion, constructive solid geometry, and freeform deformations) to a vast array of geometric primitives. For efficient display, these models must usually be tessellated into polygonal approximations-meshes. Detailed meshes are also obtained by scanning physical objects using range scanning systems [5]. In either case, the resulting complex meshes are expensive to store, transmit, and render, thus motivating a number of practical problems:

[^11][^12]- Mesh simplification: The meshes created by modeling and scanning systems are seldom optimized for rendering efficiency, and can frequently be replaced by nearly indistinguishable approximations with far fewer faces. At present, this process often requires significant user intervention. Mesh simplification tools can hope to automate this painstaking task, and permit the porting of a single model to platforms of varying performance.
- Level-of-detail (LOD) approximation: To further improve rendering performance, it is common to define several versions of a model at various levels of detail [3, 8]. A detailed mesh is used when the object is close to the viewer, and coarser approximations are substituted as the object recedes. Since instantaneous switching between LOD meshes may lead to perceptible "popping", one would like to construct smooth visual transitions, geomorphs, between meshes at different resolutions.
- Progressive transmission: When a mesh is transmitted over a communication line, one would like to show progressively better approximations to the model as data is incrementally received. One approach is to transmit successive LOD approximations, but this requires additional transmission time.
- Mesh compression: The problem of minimizing the storage space for a model can be addressed in two orthogonal ways. One is to use mesh simplification to reduce the number of faces. The other is mesh compression: minimizing the space taken to store a particular mesh.
- Selective refinement: Each mesh in a LOD representation captures the model at a uniform (view-independent) level of detail. Sometimes it is desirable to adapt the level of refinement in selected regions. For instance, as a user flies over a terrain, the terrain mesh need be fully detailed only near the viewer, and only within the field of view.

In addressing these problems, this paper makes two major contributions. First, it introduces the progressive mesh (PM) representation. In PM form, an arbitrary mesh $\hat{M}$ is stored as a much coarser mesh $M^{0}$ together with a sequence of $n$ detail records that indicate how to incrementally refine $M^{0}$ exactly back into the original mesh $\hat{M}=M^{n}$. Each of these records stores the information associated with a vertex split, an elementary mesh transformation that adds an additional vertex to the mesh. The PM representation of $\hat{M}$ thus defines a continuous sequence of meshes $M^{0}, M^{1}, \ldots, M^{n}$ of increasing accuracy, from which LOD approximations of any desired complexity can be efficiently retrieved. Moreover, geomorphs can be efficiently constructed between any two such meshes. In addition, we show that the PM representation naturally supports progressive transmission, offers a concise encoding of $\hat{M}$ itself, and permits selective refinement. In short, progressive meshes offer an efficient, lossless, continuous-resolution representation.

The other contribution of this paper is a new simplification procedure for constructing a PM representation from a given mesh $\hat{M}$. Unlike previous simplification methods, our procedure seeks to preserve not just the geometry of the mesh surface, but more importantly its overall appearance, as defined by the discrete and scalar attributes associated with its surface.

## 2 MESHES IN COMPUTER GRAPHICS

Models in computer graphics are often represented using triangle meshes. ${ }^{1}$ Geometrically, a triangle mesh is a piecewise linear surface consisting of triangular faces pasted together along their edges. As described in [9], the mesh geometry can be denoted by a tuple $(K, V)$, where $K$ is a simplicial complex specifying the connectivity of the mesh simplices (the adjacency of the vertices, edges, and faces), and $V=\left\{\mathbf{v}_{1}, \ldots, \mathbf{v}_{m}\right\}$ is the set of vertex positions defining the shape of the mesh in $\mathbf{R}^{3}$. More precisely (cf. [9]), we construct a parametric domain $|K| \subset \mathbf{R}^{m}$ by identifying each vertex of $K$ with a canonical basis vector of $\mathbf{R}^{m}$, and define the mesh as the image $\phi_{V}(|K|)$ where $\phi_{V}: \mathbf{R}^{m} \rightarrow \mathbf{R}^{3}$ is a linear map.

Often, surface appearance attributes other than geometry are also associated with the mesh. These attributes can be categorized into two types: discrete attributes and scalar attributes.

Discrete attributes are usually associated with faces of the mesh. A common discrete attribute, the material identifier, determines the shader function used in rendering a face of the mesh [18]. For instance, a trivial shader function may involve simple look-up within a specified texture map.

Many scalar attributes are often associated with a mesh, including diffuse color $(r, g, b)$, normal ( $n_{x}, n_{y}, n_{z}$ ), and texture coordinates $(u, v)$. More generally, these attributes specify the local parameters of shader functions defined on the mesh faces. In simple cases, these scalar attributes are associated with vertices of the mesh. However, to represent discontinuities in the scalar fields, and because adjacent faces may have different shading functions, it is common to associate scalar attributes not with vertices, but with corners of the mesh [1]. A corner is defined as a (vertex,face) tuple. Scalar attributes at a corner $(v, f)$ specify the shading parameters for face $f$ at vertex $v$. For example, along a crease (a curve on the surface across which the normal field is not continuous), each vertex has two distinct normals, one associated with the corners on each side of the crease.

We express a mesh as a tuple $M=(K, V, D, S)$ where $V$ specifies its geometry, $D$ is the set of discrete attributes $d_{f}$ associated with the faces $f=\{j, k, l\} \in K$, and $S$ is the set of scalar attributes $s_{(v, f)}$ associated with the corners $(v, f)$ of $K$.

The attributes $D$ and $S$ give rise to discontinuities in the visual appearance of the mesh. An edge $\left\{v_{j}, v_{k}\right\}$ of the mesh is said to be sharp if either (1) it is a boundary edge, or (2) its two adjacent faces $f_{l}$ and $f_{r}$ have different discrete attributes (i.e. $d_{f_{l}} \neq d_{f_{r}}$ ), or (3) its adjacent corners have different scalar attributes (i.e. $s_{\left(v_{j}, f_{l}\right)} \neq s_{\left(v_{j}, f_{r}\right)}$ or $\left.s_{\left(v_{k}, f_{l}\right)} \neq s_{\left(v_{k}, f_{r}\right)}\right)$. Together, the set of sharp edges define a set of discontinuity curves over the mesh (e.g. the yellow curves in Figure 12).

## 3 PROGRESSIVE MESH REPRESENTATION

### 3.1 Overview

Hoppe et al. [9] describe a method, mesh optimization, that can be used to approximate an initial mesh $\hat{M}$ by a much simpler one. Their optimization algorithm, reviewed in Section 4.1, traverses the space of possible meshes by successively applying a set of 3 mesh transformations: edge collapse, edge split, and edge swap.

We have discovered that in fact a single one of those transformations, edge collapse, is sufficient for effectively simplifying meshes. As shown in Figure 1, an edge collapse transformation $\operatorname{ecol}\left(\left\{v_{s}, v_{t}\right\}\right)$

[^13]

Figure 1: Illustration of the edge collapse transformation.

(a)

(b)

Figure 2: (a) Sequence of edge collapses; (b) Resulting vertex correspondence.
unifies 2 adjacent vertices $v_{s}$ and $v_{t}$ into a single vertex $v_{s}$. The vertex $v_{t}$ and the two adjacent faces $\left\{v_{s}, v_{t}, v_{l}\right\}$ and $\left\{v_{t}, v_{s}, v_{r}\right\}$ vanish in the process. A position $\mathbf{v}_{s}$ is specified for the new unified vertex.

Thus, an initial mesh $\hat{M}=M^{n}$ can be simplified into a coarser mesh $M^{0}$ by applying a sequence of $n$ successive edge collapse transformations:

$$
\left(\hat{M}=M^{n}\right) \xrightarrow{\text { ecol }_{n-1}} \ldots \xrightarrow{\text { ecol }_{1}} M^{1} \xrightarrow{\text { ecol }_{0}} M^{0} .
$$

The particular sequence of edge collapse transformations must be chosen carefully, since it determines the quality of the approximating meshes $M^{i}, i<n$. A scheme for choosing these edge collapses is presented in Section 4.

Let $m_{0}$ be the number of vertices in $M^{0}$, and let us label the vertices of mesh $M^{i}$ as $V^{i}=\left\{v_{1}, \ldots, v_{m_{0}+i}\right\}$, so that edge $\left\{v_{s_{i}}, v_{m_{0}+i+1}\right\}$ is collapsed by ecol ${ }_{i}$ as shown in Figure 2a. As vertices may have different positions in the different meshes, we denote the position of $v_{j}$ in $M^{i}$ as $\mathbf{v}_{j}^{i}$.

A key observation is that an edge collapse transformation is invertible. Let us call that inverse transformation a vertex split, shown as vsplit in Figure 1. A vertex split transformation $\operatorname{vsplit}(s, l, r, t, A)$ adds near vertex $v_{s}$ a new vertex $v_{t}$ and two new faces $\left\{v_{s}, v_{t}, v_{l}\right\}$ and $\left\{v_{t}, v_{s}, v_{r}\right\}$. (If the edge $\left\{v_{s}, v_{t}\right\}$ is a boundary edge, we let $v_{r}=0$ and only one face is added.) The transformation also updates the attributes of the mesh in the neighborhood of the transformation. This attribute information, denoted by $A$, includes the positions $\mathbf{v}_{s}$ and $\mathbf{v}_{t}$ of the two affected vertices, the discrete attributes $d_{\left\{v_{s}, v_{t}, v_{l}\right\}}$ and $d_{\left\{v_{t}, v_{s}, v_{r}\right\}}$ of the two new faces, and the scalar attributes of the affected corners $\left(s_{\left(v_{s}, \cdot\right)}, s_{\left(v_{t}, \cdot\right)}, s_{\left(v_{l},\left\{v_{s}, v_{t}, v_{l}\right\}\right)}\right.$, and $\left.s_{\left(v_{r},\left\{v_{t}, v_{s}, v_{r}\right\}\right)}\right)$.

Because edge collapse transformations are invertible, we can therefore represent an arbitrary triangle mesh $\hat{M}$ as a simple mesh $M^{0}$ together with a sequence of $n v$ split records:

$$
M^{0} \xrightarrow{\text { vsplit }}{ }^{\text {P }} M^{1} \xrightarrow{\text { vsplit }} \ldots \xrightarrow{\text { vsplit }_{n}-1}\left(M^{n}=\hat{M}\right)
$$

where each record is parametrized as $\operatorname{vsplit}_{i}\left(s_{i}, l_{i}, r_{i}, A_{i}\right)$. We call $\left(M^{0},\left\{v s p l i t_{0}, \ldots\right.\right.$, vsplit $\left.\left._{n-1}\right\}\right)$ a progressive mesh $(\mathrm{PM})$ representation of $\hat{M}$.

As an example, the mesh $\hat{M}$ of Figure 5 d (13,546 faces) was simplified down to the coarse mesh $M^{0}$ of Figure 5 ( 150 faces) using

6,698 edge collapse transformations. Thus its PM representation consists of $M^{0}$ together with a sequence of $n=6698$ vsplit records. From this PM representation, one can extract approximating meshes with any desired number of faces (actually, within $\pm 1$ ) by applying to $M^{0}$ a prefix of the vsplit sequence. For example, Figure 5 shows approximating meshes with 150,500 , and 1000 faces.

### 3.2 Geomorphs

A nice property of the vertex split transformation (and its inverse, edge collapse) is that a smooth visual transition (a geomorph) can be created between the two meshes $M^{i}$ and $M^{i+1}$ in $M^{i} \xrightarrow{\text { vspliti }} M^{i+1}$. For the moment let us assume that the meshes contain no attributes other than vertex positions. With this assumption the vertex split record is encoded as $\operatorname{vsplit} t_{i}\left(s_{i}, l_{i}, r_{i}, A_{i}=\left(\mathbf{v}_{s_{i}}^{i+1}, \mathbf{v}_{m_{0}+i+1}^{i+1}\right)\right)$. We construct a geomorph $M^{G}(\alpha)$ with blend parameter $0 \leq \alpha \leq 1$ such that $M^{G}(0)$ looks like $M^{i}$ and $M^{G}(1)$ looks like $M^{i+1}$-in fact $M^{G}(1)=M^{i+1}$-by defining a mesh

$$
M^{G}(\alpha)=\left(K^{i+1}, V^{G}(\alpha)\right)
$$

whose connectivity is that of $M^{i+1}$ and whose vertex positions linearly interpolate from $v_{s_{i}} \in M^{i}$ to the split vertices $v_{s_{i}}, v_{m_{0}+i+1} \in M^{i+1}$ :

$$
\mathbf{v}_{j}^{G}(\alpha)= \begin{cases}(\alpha) \mathbf{v}_{j}^{i+1}+(1-\alpha) \mathbf{v}_{s_{i}}^{i} & , j \in\left\{s_{i}, m_{0}+i+1\right\} \\ \mathbf{v}_{j}^{i+1}=\mathbf{v}_{j}^{i} & , j \notin\left\{s_{i}, m_{0}+i+1\right\}\end{cases}
$$

Using such geomorphs, an application can smoothly transition from a mesh $M^{i}$ to meshes $M^{i+1}$ or $M^{i-1}$ without any visible "snapping" of the meshes.

Moreover, since individual ecol transformations can be transitioned smoothly, so can the composition of any sequence of them. Geomorphs can therefore be constructed between any two meshes of a PM representation. Indeed, given a finer mesh $M^{f}$ and a coarser mesh $M^{c}, 0 \leq c<f \leq n$, there exists a natural correspondence between their vertices: each vertex of $M^{f}$ is related to a unique ancestor vertex of $M^{c}$ by a surjective map $A^{c}$ obtained by composing a sequence of ecol transformations (Figure 2b). More precisely, each vertex $v_{j}$ of $M^{f}$ corresponds with the vertex $v_{A^{c}(j)}$ in $M^{c}$ where

$$
A^{c}(j)=\left\{\begin{array}{cl}
j & , j \leq m_{0}+c \\
A^{c}\left(s_{j-m_{0}-1}\right) & , j>m_{0}+c
\end{array} .\right.
$$

(In practice, this ancestor information $A^{c}$ is gathered in a forward fashion as the mesh is refined.) This correspondence allows us to define a geomorph $M^{G}(\alpha)$ such that $M^{G}(0)$ looks like $M^{c}$ and $M^{G}(1)$ equals $M^{f}$. We simply define $M^{G}(\alpha)=\left(K^{f}, V^{G}(\alpha)\right)$ to have the connectivity of $M^{f}$ and the vertex positions

$$
\mathbf{v}_{j}^{G}(\alpha)=(\alpha) \mathbf{v}_{j}^{f}+(1-\alpha) \mathbf{v}_{A^{c}(j)}^{c} .
$$

So far we have outlined the construction of geomorphs between PM meshes containing only position attributes. We can in fact construct geomorphs for meshes containing both discrete and scalar attributes.
Discrete attributes by their nature cannot be smoothly interpolated. Fortunately, these discrete attributes are associated with faces of the mesh, and the "geometric" geomorphs described above smoothly introduce faces. In particular, observe that the faces of $M^{c}$ are a proper subset of the faces of $M^{f}$, and that those faces of $M^{f}$ missing from $M^{c}$ are invisible in $M^{G}(0)$ because they have been collapsed to degenerate (zero area) triangles. Other geomorphing schemes [10, 11, 17] define well-behaved (invertible) parametrizations between meshes at different levels of detail, but these do not permit the construction of geomorphs between meshes with different discrete attributes.
Scalar attributes defined on corners can be smoothly interpolated much like the vertex positions. There is a slight complication in that a corner $(v, f)$ in a mesh $M$ is not naturally associated with
any "ancestor corner" in a coarser mesh $M^{c}$ if $f$ is not a face of $M^{c}$. We can still attempt to infer what attribute value ( $v, f$ ) would have in $M^{c}$ as follows. We examine the mesh $M^{i+1}$ in which $f$ is first introduced, locate a neighboring corner ( $v, f^{\prime}$ ) in $M^{i+1}$ whose attribute value is the same, and recursively backtrack from it to a corner in $M^{c}$. If there is no neighboring corner in $M^{i+1}$ with an identical attribute value, then the corner $(v, f)$ has no equivalent in $M^{c}$ and we therefore keep its attribute value constant through the geomorph.

The interpolating function on the scalar attributes need not be linear; for instance, normals are best interpolated over the unit sphere, and colors may be interpolated in a color space other than RGB.

Figure 6 demonstrates a geomorph between two meshes $M^{175}$ (500 faces) and $M^{425}$ (1000 faces) retrieved from the PM representation of the mesh in Figure 5d.

### 3.3 Progressive transmission

Progressive meshes are a natural representation for progressive transmission. The compact mesh $M^{0}$ is transmitted first (using a conventional uni-resolution format), followed by the stream of $v^{v p l i t} t_{i}$ records. The receiving process incrementally rebuilds $\hat{M}$ as the records arrive, and animates the changing mesh. The changes to the mesh can be geomorphed to avoid visual discontinuities. The original mesh $\hat{M}$ is recovered exactly after all $n$ records are received, since PM is a lossless representation.

The computation of the receiving process should be balanced between the reconstruction of $\hat{M}$ and interactive display. With a slow communication line, a simple strategy is to display the current mesh whenever the input buffer is found to be empty. With a fast communication line, we find that a good strategy is to display meshes whose complexities increase exponentially. (Similar issues arise in the display of images transmitted using progressive JPEG.)

### 3.4 Mesh compression

Even though the PM representation encodes both $\hat{M}$ and a continuous family of approximations, it is surprisingly space-efficient, for two reasons. First, the locations of the vertex split transformations can be encoded concisely. Instead of storing all three vertex indices ( $s_{i}, l_{i}, r_{i}$ ) of $v s p l i t_{i}$, one need only store $s_{i}$ and approximately 5 bits to select the remaining two vertices among those adjacent to $v_{s_{i}}{ }^{2}$ Second, because a vertex split has local effect, one can expect significant coherence in mesh attributes through each transformation. For instance, when vertex $v_{s_{i}}^{i}$ is split into $v_{s_{i}}^{i+1}$ and $v_{m_{0}+i+1}^{i+1}$, we can predict the positions $\mathbf{v}_{s_{i}}^{i+1}$ and $\mathbf{v}_{m_{0}+i+1}^{i+1}$ from $\mathbf{v}_{s_{i}}^{i}$, and use delta-encoding to reduce storage. Scalar attributes of corners in $M^{i+1}$ can similarly be predicted from those in $M^{i}$. Finally, the material identifiers $d_{\left\{v_{s}, v_{t}, v_{l}\right\}}$ and $d_{\left\{v_{t}, v_{s}, v_{r}\right\}}$ of the new faces in mesh $M^{i+1}$ can often be predicted from those of adjacent faces in $M^{i}$ using only a few control bits.

As a result, the size of a carefully designed PM representation should be competitive with that obtained from methods for compressing uni-resolution meshes. Our current prototype implementation was not designed with this goal in mind. However, we analyze the compression of the connectivity $K$, and report results on the compression of the geometry $V$. In the following analysis, we assume for simplicity that $m_{0}=0$ since typically $m_{0} \ll n$.

A common representation for the mesh connectivity $K$ is to list the three vertex indices for each face. Since the number of vertices is $n$ and the number of faces approximately $2 n$, such a list requires $6\left\lceil\log _{2}(n)\right\rceil n$ bits of storage. Using a buffer of 2 vertices, generalized triangle strip representations reduce this number to about

[^14]$\left(\left\lceil\log _{2}(n)\right\rceil+2 k\right) n$ bits, where vertices are back-referenced once on average and $k \simeq 2$ bits capture the vertex replacement codes [6]. By increasing the vertex buffer size to 16, Deering's generalized triangle mesh representation [6] further reduces storage to about $\left(\frac{1}{8}\left[\log _{2}(n)\right\rceil+8\right) n$ bits. Turan [16] shows that planar graphs (and hence the connectivity of closed genus 0 meshes) can be encoded in $12 n$ bits. Recent work by Taubin and Rossignac [15] addresses more general meshes. With the PM representation, each vspliti requires specification of $s_{i}$ and its two neighbors, for a total storage of about $\left(\left\lceil\log _{2}(n)\right\rceil+5\right) n$ bits. Although not as concise as $[6,15]$, this is comparable to generalized triangle strips.
A traditional representation of the mesh geometry $V$ requires storage of $3 n$ coordinates, or $96 n$ bits with IEEE single-precision floating point. Like Deering [6], we assume that these coordinates can be quantized to 16 -bit fixed precision values without significant loss of visual quality, thus reducing storage to $48 n$ bits. Deering is able to further compress this storage by delta-encoding the quantized coordinates and Huffman compressing the variable-length deltas. For 16-bit quantization, he reports storage of $35.8 n$ bits, which includes both the deltas and the Huffman codes. Using a similar approach with the PM representation, we encode $V$ in $31 n$ to $50 n$ bits as shown in Table 1. To obtain these results, we exploit a property of our optimization algorithm (Section 4.3): when considering the collapse of an edge $\left\{v_{s}, v_{t}\right\}$, it considers three starting points for the resulting vertex position $\mathbf{v}_{n}:\left\{\mathbf{v}_{s}, \mathbf{v}_{t}, \frac{\mathbf{v}_{s}+\mathbf{v}_{t}}{2}\right\}$. Depending on the starting point chosen, we delta-encode either $\left\{\mathbf{v}_{s}-\mathbf{v}_{n}, \mathbf{v}_{t}-\mathbf{v}_{n}\right\}$ or $\left\{\frac{\mathbf{V}_{s}+\mathbf{V}_{t}}{2}-\mathbf{v}_{n}, \frac{\mathbf{V}_{t}-\mathbf{V}_{s}}{2}\right\}$, and use separate Huffman tables for all four quantities.
To further improve compression, we could alter the construction algorithm to forego optimization and let $\mathbf{v}_{n} \in\left\{\mathbf{v}_{s}, \mathbf{v}_{t}, \frac{\mathbf{v}_{s}+\mathbf{V}_{t}}{2}\right\}$. This would degrade the accuracy of the approximating meshes somewhat, but allows encoding of $V$ in $30 n$ to $37 n$ bits in our examples. Arithmetic coding [19] of delta lengths does not improve results significantly, reflecting the fact that the Huffman trees are well balanced. Further compression improvements may be achievable by adapting both the quantization level and the delta length models as functions of the vsplit record index $i$, since the magnitude of successive changes tends to decrease.

### 3.5 Selective refinement

The PM representation also supports selective refinement, whereby detail is added to the model only in desired areas. Let the application supply a callback function REFINE $(v)$ that returns a Boolean value indicating whether the neighborhood of the mesh about $v$ should be further refined. An initial mesh $M^{c}$ is selectively refined by iterating through the list $\left\{\right.$ vsplit $_{c}, \ldots$, vsplit $\left._{n-1}\right\}$ as before, but only performing $v \operatorname{vsplit}_{i}\left(s_{i}, l_{i}, r_{i}, A_{i}\right)$ if
(1) all three vertices $\left\{v_{s_{i}}, v_{l_{i}}, v_{r_{i}}\right\}$ are present in the mesh, and
(2) $\operatorname{REFINE}\left(v_{s_{i}}\right)$ evaluates to TRUE.
(A vertex $v_{j}$ is absent from the mesh if the prior vertex split that would have introduced it, $v$ split $_{j-m_{0}-1}$, was not performed due to the above conditions.)

As an example, to obtain selective refinement of the model within a view frustum, $\operatorname{REFINE}(v)$ is defined to be TRUE if either $v$ or any of its neighbors lies within the frustum. As seen in Figure 7a, condition (1) described above is suboptimal. The problem is that a vertex $v_{s_{i}}$ within the frustum may fail to be split because its expected neighbor $v_{l_{i}}$ lies just outside the frustum and was not previously created. The problem is remedied by using a less stringent version of condition (1). Let us define the closest living ancestor of a vertex $v_{j}$ to be the vertex with index

$$
A^{\prime}(j)=\left\{\begin{array}{cl}
j & , \text { if } v_{j} \text { exists in the mesh } \\
A^{\prime}\left(s_{j-m_{0}-1}\right) & , \text { otherwise }
\end{array}\right.
$$

The new condition becomes:
(1') $v_{s_{i}}$ is present in the mesh (i.e. $\left.A^{\prime}\left(s_{i}\right)=s_{i}\right)$ and the vertices $v_{A^{\prime}}\left(l_{i}\right)$ and $v_{A^{\prime}\left(r_{i}\right)}$ are both adjacent to $v_{s_{i}}$.
As when constructing the geomorphs, the ancestor information $A^{\prime}$ is carried efficiently as the vsplit records are parsed. If conditions (1') and (2) are satisfied, $v \operatorname{split}\left(s_{i}, A^{\prime}\left(l_{i}\right), A^{\prime}\left(r_{i}\right), A_{i}\right)$ is applied to the mesh. A mesh selectively refined with this new strategy is shown in Figure 7b. This same strategy was also used for Figure 10. Note that it is still possible to create geomorphs between $M^{c}$ and selectively refined meshes thus created.

An interesting application of selective refinement is the transmission of view-dependent models over low-bandwidth communication lines. As the receiver's view changes over time, the sending process need only transmit those vsplit records for which REFINE evaluates to TRUE, and of those only the ones not previously transmitted.

## 4 PROGRESSIVE MESH CONSTRUCTION

The PM representation of an arbitrary mesh $\hat{M}$ requires a sequence of edge collapses transforming $\hat{M}=M^{n}$ into a base mesh $M^{0}$. The quality of the intermediate approximations $M^{i}, i<n$ depends largely on the algorithm for selecting which edges to collapse and what attributes to assign to the affected neighborhoods, for instance the positions $\mathbf{v}_{s_{i}}^{i}$.

There are many possible PM construction algorithms with varying trade-offs of speed and accuracy. At one extreme, a crude and fast scheme for selecting edge collapses is to choose them completely at random. (Some local conditions must be satisfied for an edge collapse to be legal, i.e. manifold preserving [9].) More sophisticated schemes can use heuristics to improve the edge selection strategy, for example the "distance to plane" metric of Schroeder et al. [14]. At the other extreme, one can attempt to find approximating meshes that are optimal with respect to some appearance metric, for instance the $E_{\text {dist }}$ geometric metric of Hoppe et al. [9].

Since PM construction is a preprocess that can be performed offline, we chose to design a simplification procedure that invests some time in the selection of edge collapses. Our procedure is similar to the mesh optimization method introduced by Hoppe et al. [9], which is outlined briefly in Section 4.1. Section 4.2 presents an overview of our procedure, and Sections 4.3-4.6 present the details of our optimization scheme for preserving both the shape of the mesh and the scalar and discrete attributes which define its appearance.

### 4.1 Background: mesh optimization

The goal of mesh optimization [9] is to find a mesh $M=(K, V)$ that both accurately fits a set $X$ of points $\mathbf{x}_{i} \in \mathbf{R}^{3}$ and has a small number of vertices. This problem is cast as minimization of an energy function

$$
E(M)=E_{\text {dist }}(M)+E_{\text {rep }}(M)+E_{\text {spring }}(M) .
$$

The first two terms correspond to the two goals of accuracy and conciseness: the distance energy term

$$
E_{d i s t}(M)=\sum_{i} d^{2}\left(\mathbf{x}_{i}, \phi_{V}(|K|)\right)
$$

measures the total squared distance of the points from the mesh, and the representation energy term $E_{\text {rep }}(M)=c_{\text {rep }} m$ penalizes the number $m$ of vertices in $M$. The third term, the spring energy $E_{\text {spring }}(M)$ is introduced to regularize the optimization problem. It corresponds to placing on each edge of the mesh a spring of rest length zero and tension $\kappa$ :

$$
E_{\text {spring }}(M)=\sum_{\{j, k\} \in K} \kappa\left\|\mathbf{v}_{j}-\mathbf{v}_{k}\right\|^{2} .
$$



Figure 3: Illustration of the paths taken by mesh optimization using three different settings of $c_{\text {rep }}$.

The energy function $E(M)$ is minimized using a nested optimization method:

- Outer loop: The algorithm optimizes over $K$, the connectivity of the mesh, by randomly attempting a set of three possible mesh transformations: edge collapse, edge split, and edge swap. This set of transformations is complete, in the sense that any simplicial complex $K$ of the same topological type as $\hat{K}$ can be reached through a sequence of these transformations. For each candidate mesh transformation, $K \rightarrow K^{\prime}$, the continuous optimization described below computes $E_{K^{\prime}}$, the minimum of $E$ subject to the new connectivity $K^{\prime}$. If $\Delta E=E_{K^{\prime}}-E_{K}$ is found to be negative, the mesh transformation is applied (akin to a zero-temperature simulated annealing method).
- Inner loop: For each candidate mesh transformation, the algorithm computes $E_{K^{\prime}}=\min _{V} E_{\text {dist }}(V)+E_{\text {spring }}(V)$ by optimizing over the vertex positions $V$. For the sake of efficiency, the algorithm in fact optimizes only one vertex position $\mathbf{v}_{s}$, and considers only the subset of points $X$ that project onto the neighborhood affected by $K \rightarrow K^{\prime}$. To avoid surface self-intersections, the edge collapse is disallowed if the maximum dihedral angle of edges in the resulting neighborhood exceeds some threshold.

Hoppe et al. [9] find that the regularizing spring energy term $E_{\text {spring }}(M)$ is most important in the early stages of the optimization, and achieve best results by repeatedly invoking the nested optimization method described above with a schedule of decreasing spring constants $\kappa$.
Mesh optimization is demonstrated to be an effective tool for mesh simplification. Given an initial mesh $\hat{M}$ to approximate, a dense set of points $X$ is sampled both at the vertices of $\hat{M}$ and randomly over its faces. The optimization algorithm is then invoked with $\hat{M}$ as the starting mesh. Varying the setting of the representation constant $c_{\text {rep }}$ results in optimized meshes with different trade-offs of accuracy and size. The paths taken by these optimizations are shown illustratively in Figure 3.

### 4.2 Overview of the simplification algorithm

As in mesh optimization [9], we also define an explicit energy metric $E(M)$ to measure the accuracy of simplified meshes $M=(K, V, D, S)$ with respect to the original $\hat{M}$, and we also modify the mesh $M$ starting from $\hat{M}$ while minimizing $E(M)$.

Our energy metric has the following form:

$$
E(M)=E_{d i s t}(M)+E_{\text {spring }}(M)+E_{\text {scalar }}(M)+E_{\text {disc }}(M)
$$

The first two terms, $E_{\text {dist }}(M)$ and $E_{\text {spring }}(M)$ are identical to those in [9]. The next two terms of $E(M)$ are added to preserve attributes associated with $M: E_{\text {scalar }}(M)$ measures the accuracy of its scalar attributes (Section 4.4), and $E_{d i s c}(M)$ measures the geometric accuracy of its discontinuity curves (Section 4.5). (To achieve scale invariance of the terms, the mesh is uniformly scaled to fit in a unit cube.)


Figure 4: Illustration of the path taken by the new mesh simplification procedure in a graph plotting accuracy vs. mesh size.

Our scheme for optimizing over the connectivity $K$ of the mesh is rather different from [9]. We have discovered that a mesh can be effectively simplified using edge collapse transformations alone. The edge swap and edge split transformations, useful in the context of surface reconstruction (which motivated [9]), are not essential for simplification. Although in principle our simplification algorithm can no longer traverse the entire space of meshes considered by mesh optimization, we find that the meshes generated by our algorithm are just as good. In fact, because of the priority queue approach described below, our meshes are usually better. Moreover, considering only edge collapses simplifies the implementation, improves performance, and most importantly, gives rise to the PM representation (Section 3).

Rather than randomly attempting mesh transformations as in [9], we place all (legal) candidate edge collapse transformations into a priority queue, where the priority of each transformation is its estimated energy cost $\Delta E$. In each iteration, we perform the transformation at the front of the priority queue (with lowest $\Delta E$ ), and recompute the priorities of edges in the neighborhood of this transformation. As a consequence, we eliminate the need for the awkward parameter $c_{r e p}$ as well as the energy term $E_{r e p}(M)$. Instead, we can explicitly specify the number of faces desired in an optimized mesh. Also, a single run of the optimization can generate several such meshes. Indeed, it generates a continuous-resolution family of meshes, namely the PM representation of $\hat{M}$ (Figure 4).

For each edge collapse $K \rightarrow K^{\prime}$, we compute its cost $\Delta E=$ $E_{K^{\prime}}-E_{K}$ by solving a continuous optimization

$$
E_{K^{\prime}}=\min _{V, S} E_{\text {dist }}(V)+E_{\text {spring }}(V)+E_{\text {scalar }}(V, S)+E_{\text {disc }}(V)
$$

over both the vertex positions $V$ and the scalar attributes $S$ of the mesh with connectivity $K^{\prime}$. This minimization is discussed in the next three sections.

### 4.3 Preserving surface geometry ( $E_{\text {dist }}+E_{\text {spring }}$ )

As in [9], we "record" the geometry of the original mesh $\hat{M}$ by sampling from it a set of points $X$. At a minimum, we sample a point at each vertex of $\hat{M}$. If requested by the user, additional points are sampled randomly over the surface of $\hat{M}$. The energy terms $E_{\text {dist }}(M)$ and $E_{\text {spring }}(M)$ are defined as in Section 4.1.

For a mesh of fixed connectivity, our method for optimizing the vertex positions to minimize $E_{\text {dist }}(V)+E_{\text {spring }}(V)$ closely follows that of [9]. Evaluating $E_{\text {dist }}(V)$ involves computing the distance of each point $\mathbf{x}_{i}$ to the mesh. Each of these distances is itself a minimization problem

$$
\begin{equation*}
d^{2}\left(\mathbf{x}_{i}, \phi_{V}(|K|)\right)=\min _{\mathbf{b}_{i} \in|K|}\left\|\mathbf{x}_{i}-\phi_{V}\left(\mathbf{b}_{i}\right)\right\|^{2} \tag{1}
\end{equation*}
$$

where the unknown $\mathbf{b}_{i}$ is the parametrization of the projection of $\mathbf{x}_{i}$ on the mesh. The nonlinear minimization of $E_{\text {dist }}(V)+E_{\text {spring }}(V)$ is performed using an iterative procedure alternating between two steps:

1. For fixed vertex positions $V$, compute the optimal parametrizations $B=\left\{\mathbf{b}_{1}, \ldots, \mathbf{b}_{|X|}\right\}$ by projecting the points $X$ onto the mesh.
2. For fixed parametrizations $B$, compute the optimal vertex positions $V$ by solving a sparse linear least-squares problem.
As in [9], when considering $\operatorname{ecol}\left(\left\{v_{s}, v_{t}\right\}\right)$, we optimize only one vertex position, $\mathbf{v}_{s}^{i}$. We perform three different optimizations with different starting points, $\mathbf{v}_{s}^{i}=(1-\alpha) \mathbf{v}_{s}^{i+1}+(\alpha) \mathbf{v}_{t}^{i+1}$ for $\alpha=\left\{0, \frac{1}{2}, 1\right\}$, and accept the best one.

Instead of defining a global spring constant $\kappa$ for $E_{\text {spring }}$ as in [9], we adapt $\kappa$ each time an edge collapse transformation is considered. Intuitively, the spring energy is most important when few points project onto a neighborhood of faces, since in this case finding the vertex positions minimizing $E_{\text {dist }}(V)$ may be an under-constrained problem. Thus, for each edge collapse transformation considered, we set $\kappa$ as a function of the ratio of the number of points to the number of faces in the neighborhood. ${ }^{3}$ With this adaptive scheme, the influence of $E_{\text {spring }}(M)$ decreases gradually and adaptively as the mesh is simplified, and we no longer require the expensive schedule of decreasing spring constants.

### 4.4 Preserving scalar attributes ( $E_{\text {scalar }}$ )

As described in Section 2, we represent piecewise continuous scalar fields by defining scalar attributes $S$ at the mesh corners. We now present our scheme for preserving these scalar fields through the simplification process. For exposition, we find it easier to first present the case of continuous scalar fields, in which the corner attributes at a vertex are identical. The generalization to piecewise continuous fields is discussed shortly.
Optimizing scalar attributes at vertices Let the original mesh $\hat{M}$ have at each vertex $v_{j}$ not only a position $\mathbf{v}_{j} \in \mathbf{R}^{3}$ but also a scalar attribute $\underline{\mathbf{v}}_{j} \in \mathbf{R}^{d}$. To capture scalar attributes, we sample at each point $\mathbf{x}_{i} \in X$ the attribute value $\underline{\mathbf{x}}_{i} \in \mathbf{R}^{d}$. We would then like to generalize the distance metric $E_{\text {dist }}$ to also measure the deviation of the sampled attribute values $\underline{X}$ from those of $M$.

One natural way to achieve this is to redefine the distance metric to measure distance in $\mathbf{R}^{3+d}$ :

$$
d^{2}\left(\left(\mathbf{x}_{i} \underline{\mathbf{x}}_{i}\right), M(K, V, \underline{V})\right)=\min _{\mathbf{b}_{i} \in|K|}\left\|\left(\mathbf{x}_{i} \underline{\mathbf{x}}_{i}\right)-\left(\phi_{V}\left(\mathbf{b}_{i}\right) \phi_{\underline{V}}\left(\mathbf{b}_{i}\right)\right)\right\|^{2} .
$$

This new distance functional could be minimized using the iterative approach of Section 4.3. However, it would be expensive since finding the optimal parametrization $\mathbf{b}_{i}$ of each point $\mathbf{x}_{i}$ would require projection in $\mathbf{R}^{3+d}$, and would be non-intuitive since these parametrizations would not be geometrically based.

Instead we opted to determine the parametrizations $\mathbf{b}_{i}$ using only geometry with equation (1), and to introduce a separate energy term $E_{\text {scalar }}$ to measure attribute deviation based on these parametrizations:

$$
E_{\text {scalar }}(\underline{V})=\left(c_{\text {scalar }}\right)^{2} \sum_{i}\left\|\underline{\mathbf{x}}_{i}-\phi_{\underline{V}}\left(\mathbf{b}_{i}\right)\right\|^{2}
$$

where the constant $c_{s c a l a r}$ assigns a relative weight between the scalar attribute errors $\left(E_{\text {scalar }}\right)$ and the geometric errors $\left(E_{\text {dist }}\right)$.

Thus, to minimize $E(V, \underline{V})=E_{\text {dist }}(V)+E_{\text {spring }}(V)+E_{\text {scalar }}(\underline{V})$, our algorithm first finds the vertex position $\mathbf{v}_{s}$ minimizing $E_{\text {dist }}(V)+$ $E_{\text {spring }}(V)$ by alternately projecting the points onto the mesh (obtaining the parametrizations $\mathbf{b}_{i}$ ) and solving a linear least-squares problem (Section 4.1). Then, using those same parametrizations

[^15]$\mathbf{b}_{i}$, it finds the vertex attribute $\underline{\mathbf{v}}_{s}$ minimizing $E_{s c a l a r}$ by solving a single linear least-squares problem. Hence introducing $E_{\text {scalar }}$ into the optimization causes negligible performance overhead.

Since $\Delta E_{\text {scalar }}$ contributes to the estimated cost $\Delta E$ of an edge collapse, we obtain simplified meshes whose faces naturally adapt to the attribute fields, as shown in Figures 8 and 11.

Optimizing scalar attributes at corners Our scheme for optimizing the scalar corner attributes $S$ is a straightforward generalization of the scheme just described. Instead of solving for a single unknown attribute value $\underline{\mathbf{v}}_{s}$, the algorithm partitions the corners around $v_{s}$ into continuous sets (based on equivalence of corner attributes) and for each continuous set solves independently for its optimal attribute value.

Range constraints Some scalar attributes have constrained ranges. For instance, the components $(r, g, b)$ of color are typically constrained to lie between 0 and 1 . Least-squares optimization may yield color values outside this range. In these cases we clip the optimized values to the given range. For least-squares minimization of a Euclidean norm at a single vertex, this is in fact optimal.
Normals Surface normals ( $n_{x}, n_{y}, n_{z}$ ) are typically constrained to have unit length, and thus their domain is non-Cartesian. Optimizing over normals would therefore require minimization of a nonlinear functional with nonlinear constraints. We decided to instead simply carry the normals through the simplification process. Specifically, we compute the new normals at vertex $v_{s i}^{i}$ by interpolating between the normals at vertices $v_{s_{i}}^{i+1}$ and $v_{m_{0}+i+1}^{i+1}$ using the $\alpha$ value that resulted in the best vertex position $\mathbf{v}_{s_{i}}^{i}$ in Section 4.3. Fortunately, the absolute directions of normals are less visually important than their discontinuities, and we have a scheme for preserving such discontinuities, as described in the next section.

### 4.5 Preserving discontinuity curves ( $E_{\text {disc }}$ )

Appearance attributes give rise to a set of discontinuity curves on the mesh, both from differences between discrete face attributes (e.g. material boundaries), and from differences between scalar corner attributes (e.g. creases and shadow boundaries). As these discontinuity curves form noticeable features, we have found it useful to preserve them both topologically and geometrically.

We can detect when a candidate edge collapse would modify the topology of the discontinuity curves using some simple tests on the presence of sharp edges in its neighborhood. Let $\operatorname{sharp}\left(v_{j}, v_{k}\right)$ denote that an edge $\left\{v_{j}, v_{k}\right\}$ is sharp, and let \#sharp $\left(v_{j}\right)$ be the number of sharp edges adjacent to a vertex $v_{j}$. Then, referring to Figure 1, $\operatorname{ecol}\left(\left\{v_{s}, v_{t}\right\}\right)$ modifies the topology of discontinuity curves if either:

- $\operatorname{sharp}\left(v_{s}, v_{l}\right)$ and $\operatorname{sharp}\left(v_{t}, v_{l}\right)$, or
- $\operatorname{sharp}\left(v_{s}, v_{r}\right)$ and $\operatorname{sharp}\left(v_{t}, v_{r}\right)$, or
- $\# \operatorname{sharp}\left(v_{s}\right) \geq 1$ and $\# \operatorname{sharp}\left(v_{t}\right) \geq 1$ and not $\operatorname{sharp}\left(v_{s}, v_{t}\right)$, or
- \#sharp $\left(v_{s}\right) \geq 3$ and $\# \operatorname{sharp}\left(v_{t}\right) \geq 3$ and $\operatorname{sharp}\left(v_{s}, v_{t}\right.$ ), or
- $\operatorname{sharp}\left(v_{s}, v_{t}\right)$ and $\# \operatorname{sharp}\left(v_{s}\right)=1$ and $\# \operatorname{sharp}\left(v_{t}\right) \neq 2$, or
- $\operatorname{sharp}\left(v_{s}, v_{t}\right)$ and $\# \operatorname{sharp}\left(v_{t}\right)=1$ and $\# \operatorname{sharp}\left(v_{s}\right) \neq 2$.

If an edge collapse would modify the topology of discontinuity curves, we either disallow it, or penalize it as discussed in Section 4.6.

To preserve the geometry of the discontinuity curves, we sample an additional set of points $X_{\text {disc }}$ from the sharp edges of $\hat{M}$, and define an additional energy term $E_{\text {disc }}$ equal to the total squared distances of each of these points to the discontinuity curve from which it was sampled. Thus $E_{\text {disc }}$ is defined just like $E_{\text {dist }}$, except that the points $X_{\text {disc }}$ are constrained to project onto a set of sharp edges in the mesh. In effect, we are solving a curve fitting problem embedded within the surface fitting problem. Since all boundaries of the surface are defined to be discontinuity curves, our procedure preserves bound-
ary geometry more accurately than [9]. Figure 9 demonstrates the importance of using the $E_{\text {disc }}$ energy term in preserving the material boundaries of a mesh with discrete face attributes.

### 4.6 Permitting changes to topology of discontinuity curves

Some meshes contain numerous discontinuity curves, and these curves may delimit features that are too small to be visible when viewed from a distance. In such cases we have found that strictly preserving the topology of the discontinuity curves unnecessarily curtails simplification. We have therefore adopted a hybrid strategy, which is to permit changes to the topology of the discontinuity curves, but to penalize such changes. When a candidate edge collapse $\operatorname{ecol}\left(\left\{v_{s}, v_{t}\right\}\right)$ changes the topology of the discontinuity curves, we add to its cost $\Delta E$ the value $\left|X_{d i s c,\left\{v_{s}, v_{t}\right\}}\right| \cdot\left\|\mathbf{v}_{s}-\mathbf{v}_{t}\right\|^{2}$ where $\left|X_{\text {disc, }\left\{v_{s}, v_{t}\right\}}\right|$ is the number of points of $X_{\text {disc }}$ projecting onto $\left\{v_{s}, v_{t}\right\}$. That simple strategy, although ad hoc, has proven very effective. For example, it allows the dark gray window frames of the "cessna" (visible in Figure 9) to vanish in the simplified meshes (Figures 5a-c).

Table 1: Parameter settings and quantitative results.

| Object | Original $\hat{M}$ |  | Base $M^{0}$ |  | User param. |  | $\left\|X_{\text {disc }}\right\|$ | $$ | Timemins |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $m_{0}+n$ | \#faces | $m_{0}$ | \#faces | ${ }^{\|X\|-\left(m_{0}+n\right)}$ | $c_{\text {color }}$ |  |  |  |
| cessna | 6,795 | 13,546 | 97 | 150 | 100,000 |  | 46,811 | 46 | 23 |
| terrain | 33 | 0 | 3 |  | 0 |  | 96 | 46 | 16 |
| mandri | 40,000 | 79,202 | 3 | 1 | 0 | 0.1 | 4,776 | 31 | 19 |
| radiosity | 78,923 | 150,983 | 1,192 | 1,191 | 200,000 | 0.01 | 74,316 | 37 | 06 |
| fandisk | 6,475 | 12,946 | 27 | 50 | 10,000 |  | 5,924 | 50 | 19 |

## 5 RESULTS

Table 1 shows, for the meshes in Figures 5-12, the number of vertices and faces in both $\hat{M}$ and $M^{0}$. In general, we let the simplification proceed until no more legal edge collapse transformations are possible. For the "cessna", we stopped at 150 faces to obtain a visually aesthetic base mesh. As indicated, the only user-specified parameters are the number of additional points (besides the $m_{0}+n$ vertices of $\hat{M}$ ) sampled to increase fidelity, and the $c_{\text {scalar }}$ constants relating the scalar attribute accuracies to the geometric accuracy. The only scalar attribute we optimized is color, and its $c_{\text {scalar }}$ constant is denoted as $c_{\text {color }}$. The number $\left|X_{\text {disc }}\right|$ of points sampled from sharp edges is set automatically so that the densities of $X$ and $X_{\text {disc }}$ are proportional. ${ }^{4}$ Execution times were obtained on a 150 MHz Indigo2 with 128 MB of memory.

Construction of the PM representation proceeds in three steps. First, as the simplification algorithm applies a sequence ecol $_{n-1} \ldots$ ecol $_{0}$ of transformations to the original mesh, it writes to a file the sequence vsplit $n_{n-1} \ldots$ vsplit $0_{0}$ of corresponding inverse transformations. When finished, the algorithm also writes the resulting base mesh $M^{0}$. Next, we reverse the order of the vsplit records. Finally, we renumber the vertices and faces of ( $M^{0}$, vsplit $0_{0} \ldots v^{2} p l i t_{n-1}$ ) to match the indexing scheme of Section 3.1 in order to obtain a concise format.

Figure 6 shows a single geomorph between two meshes $M^{175}$ and $M^{425}$ of a PM representation. For interactive LOD, it is useful to select a sequence of meshes from the PM representation, and to construct successive geomorphs between them. We have obtained

[^16]good results by selecting meshes whose complexities grow exponentially, as in Figure 5. During execution, an application can adjust the granularity of these geomorphs by sampling additional meshes from the PM representation, or freeing some up.

In Figure 10, we selectively refined a terrain (grid of $181 \times 187$ vertices) using a new $\operatorname{REFINE}(v)$ function that keeps more detail near silhouette edges and near the viewer. More precisely, for the faces $F_{v}$ adjacent to $v$, we compute the signed projected screen areas $\left\{a_{f}: f \in F_{v}\right\}$. We let REFINE $(v)$ return TRUE if
(1) any face $f \in F_{v}$ lies within the view frustum, and either
(2a) the signs of $a_{f}$ are not all equal (i.e. $v$ lies near a silhouette edge) or
(2b) $\sum_{f \in F_{v}} a_{f}>$ thresh for a screen area threshold thresh $=0.16^{2}$ (where total screen area is 1 ).

## 6 RELATED WORK

Mesh simplification methods A number of schemes construct a discrete sequence of approximating meshes by repeated application of a simplification procedure. Turk [17] sprinkles a set of points on a mesh, with density weighted by estimates of local curvature, and then retriangulates based on those points. Both Schroeder et al. [14] and Cohen et al. [4] iteratively remove vertices from the mesh and retriangulate the resulting holes. Cohen et al. are able to bound the maximum error of the approximation by restricting it to lie between two offset surfaces. Hoppe et al. [9] find accurate approximations through a general mesh optimization process (Section 4.1). Rossignac and Borrel [12] merge vertices of a model using spatial binning. A unique aspect of their approach is that the topological type of the model may change in the process. Their method is extremely fast, but since it ignores geometric qualities like curvature, the resulting approximations can be far from optimal. Some of the above methods [12,17] permit the construction of geomorphs between successive simplified meshes.

Multiresolution analysis (MRA) Lounsbery et al. [10, 11] generalize the concept of multiresolution analysis to surfaces of arbitrary topological type. Eck et al. [7] describe how MRA can be applied to the approximation of an arbitrary mesh. Certain et al. [2] extend MRA to capture color, and present a multiresolution Web viewer supporting progressive transmission. MRA has many similarities with the PM scheme, since both store a simple base mesh together with a stream of detail records, and both produce a continuous-resolution representation. It is therefore worthwhile to highlight their differences:

## Advantages of PM over MRA:

- MRA requires that the detail terms (wavelets) lie on a domain with subdivision connectivity, and as a result an arbitrary initial mesh $\hat{M}$ can only be recovered to within an $\epsilon$ tolerance. In contrast, the PM representation is lossless since $M^{n}=\hat{M}$.
- Because the approximating meshes $M^{i}, i<n$ in a PM may have arbitrary connectivity, they can be much better approximations than their MRA counterparts (Figure 12).
- The MRA representation cannot deal effectively with surface creases, unless those creases lie parametrically along edges of the base mesh (Figure 12). PM's can introduce surface creases anywhere and at any level of detail.
- PM's capture continuous, piecewise-continuous, and discrete appearance attributes. MRA schemes can represent discontinuous functions using a piecewise-constant basis (such as the Haar basis as used in [2, 13]), but the resulting approximations have too many discontinuities since none of the basis functions meet continuously. Also, it is not clear how MRA could be extended to capture discrete attributes.


## Advantages of MRA over PM:

- The MRA framework provides a parametrization between meshes at various levels of detail, thus making possible multiresolution surface editing. PM's also offer such a parametrization, but it is not smooth, and therefore multiresolution editing may be non-intuitive.
- Eck et al. [7] construct MRA approximations with guaranteed maximum error bounds to $\hat{M}$. Our PM construction algorithm does not provide such bounds, although one could envision using simplification envelopes [4] to achieve this.
- MRA allows geometry and color to be compressed independently [2].

Other related work There has been relatively little work in simplifying arbitrary surfaces with functions defined over them. One special instance is image compression, since an image can be thought of as a set of scalar color functions defined on a quadrilateral surface. Another instance is the framework of Schröder and Sweldens [13] for simplifying functions defined over the sphere. The PM representation, like the MRA representation, is a generalization in that it supports surfaces of arbitrary topological type.

## 7 SUMMARY AND FUTURE WORK

We have introduced the progressive mesh representation and shown that it naturally supports geomorphs, progressive transmission, compression, and selective refinement. In addition, as a PM construction method, we have presented a new mesh simplification procedure designed to preserve not just the geometry of the original mesh, but also its overall appearance.
There are a number of avenues for future work, including:

- Development of an explicit metric and optimization scheme for preserving surface normals.
- Experimentation with PM editing.
- Representation of articulated or animated models.
- Application of the work to progressive subdivision surfaces.
- Progressive representation of more general simplicial complexes (not just 2-d manifolds).
- Addition of spatial data structures to permit efficient selective refinement.

We envision many practical applications for the PM representation, including streaming of 3D geometry over the Web, efficient storage formats, and continuous LOD in computer graphics applications. The representation may also have applications in finite element methods, as it can be used to generate coarse meshes for multigrid analysis.

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(a) Base mesh $M^{0}$ (150 faces) (b) Mesh $M^{1 / 5}$ (500 faces)
(c) Mesh $M^{425}$ (1,000 faces)
(d) Original $M=M^{n}$ (13,546 faces)

Figure 5: The PM representation of an arbitrary mesh $\hat{M}$ captures a continuous-resolution family of approximating meshes $M^{0} \ldots M^{n}=\hat{M}$.


Figure 6: Example of a geomorph $M^{G}(\alpha)$ defined between $M^{G}(0) \doteq M^{175}$ (with 500 faces) and $M^{G}(1)=M^{425}$ (with 1,000 faces).

(a) Using conditions (1) and (2); 9,462 faces

(b) Using conditions (1') and (2); 12,169 faces ew frustum (indicated in orange).


Figure 8: Demonstration of minimizing $E_{\text {scalar }}$ : simplification of a mesh with trivial geometry (a square) but complex scalar attribute field. ( $M$ is a mesh with regular connectivity whose vertex colors correspond to the pixels of an image.)


Figure 9: (a) Simplification without $E_{\text {disc }}$


Figure 10: Selective refinement of a terrain mesh taking into account view frustum, silhouette regions, and projected screen size of faces (7,438 faces).


Figure 11: Simplification of a radiosity solution; left: original mesh ( 150,983 faces); right: simplified mesh ( 10,000 faces).

(d) $\epsilon=9.0$ (192 faces)
(e) $\epsilon=2.75$ ( 1,070 faces)
(f) $\epsilon=0.1$ ( 15,842 faces)

Figure 12: Approximations of a mesh $\hat{M}$ using (b-c) the PM representation, and (d-f) the MRA scheme of Eck et al. [7]. As demonstrated, MRA cannot recover $\hat{M}$ exactly, cannot deal effectively with surface creases, and produces approximating meshes of inferior quality.

## Baldwin

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[45] Date of Patent:
Aug. 25, 1998
[54] GRAPHICS RENDERING SYSTEM WITH RECONFIGURABLE PIPELINE SEQUENCE
[75] Inventor: David Robert Baldwin. Weybridge. United Kingdom
[73] Assignee: 3DLabs Inc. Ltd.. Hamilton. Bermuda
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[22] Filed: May 1, 1996

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Int. $\mathrm{Cl}^{6}{ }^{6}$ $\qquad$ G06T 1/20
[52] U.S. Cl. .......................... 345/506; 345/519; 345/509
[58] Field of Search
395/507, 509, 519, 122, 130, 132, 125. $503 ; 345 / 506,507,502,509,519,422$.
$430-432,425.503$

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ABSTRACT
The preferred embodiment discloses a pipelined graphics processor in which the sequence can be dynamically reconfigured (e.g. between primitives) in a rendering sequence. The pipeline sequence can be configured for compliance with specifications such as OpenGL, but may also be optimized by reconfiguring the pipeline sequence to eliminate unnecessary processing. In a preferred embodiment. pixel elimination sequences such as depth and stencil tests are performed before texturing calculations are performed. so that unneeded pixel data is discarded before said texturing calculations are performed.

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| :--- | :--- | :--- |
| $5,392,391$ | 2/1995 Caulk, Jr. et al. ................ $395 / 503$ |  |

## 26 Claims, 12 Drawing Sheets




FIG. $1 B$


APPENDIX O



Microsoft Corp. Exhibit 1009

$$
F I G . \quad 2 C
$$




## APPENDIX 0



FIG. 2E


## FIG. $3 A$



## FIG. $3 B$



FIG. $3 C$


FIG. 3D


Microsoft Corp. Exhibit 1009

## APPENDIX 0

$$
F I G . \quad 4 A
$$



APPENDIX 0



FIG. $5 B$


FIG. 5C

# APPENDIX 0 

## GRAPHICS RENDERING SYSTEM WITH RECONFIGURABLE PIPELINE SEQUENCE

## CROSS-REFERENCE TO RELATED APPLICATION

This application is a continuation-in-part of $08 / 410.345$ filed Mar. 24, 1995, and claims priority from provisional 60/008.803 filed Dec. 18, 1995, which is hereby incorporated by reference.

## BACKGROUND AND SUMMARY OF THE INVENTION

The present application relates to computer graphics and animation systems, and particularly to 3D graphics rendering hardware. Background of the art and the prior embodiment, according to the parent application. is described below. Some of the distinctions of the presently preferred embodiment are particularly noted beginning on page 8.

## COMPUTER GRAPHICS AND RENDERING

Modern computer systems normally manipulate graphical objects as high-level entities. For example, a solid body may be described as a collection of triangles with specified vertices, or a straight line segment may be described by listing its two endpoints with three-dimensional or twodimensional coordinates. Such high-level descriptions are a necessary basis for high-level geometric manipulations, and also have the advantage of providing a compact format which does not consume memory space unnecessarily.

Such higher-level representations are very convenient for performing the many required computations. For example, ray-tracing or other lighting calculations may be performed. and a projective transformation can be used to reduce a three-dimensional scene to its two-dimensional appearance from a given viewpoint. However, when an image containing graphical objects is to be displayed, a very low-level description is needed. For example, in a conventional CRT display, a "flying spot" is moved across the screen (one line at a time), and the beam from each of three electron guns is switched to a desired level of intensity as the flying spot passes each pixel location. Thus at some point the image model must be translated into a data set which can be used by a conventional display. This operation is known as "rendering."
The graphics-processing system typically interfaces to the display controller through a "frame store" or "frame buffer" of special two-port memory, which can be written to randomly by the graphics processing system, but also provides the synchronous data output needed by the video output driver. (Digital-to-analog conversion is also provided after the frame buffer.) Such a frame buffer is usually implemented using VRAM memory chips (or sometimes with DRAM and special DRAM controllers). This interface relieves the graphics processing system of most of the burden of synchronization for video output. Nevertheless, the amounts of data which must be moved around are very sizable, and the computational and data-transfer burden of placing the correct data into the frame buffer can still be very large.

Even if the computational operations required are quite simple, they must be performed repeatedly on a large number of data points. For example, in a typical 1995 high-end configuration. a display of $1280 \times 1024$ elements may need to be refreshed at 72 Hz , with a color resolution
of 24 bits per pixel. If blending is desired. additional bits (e.g. another 8 bits per pixel) will be required to store an "alpha" or transparency value for each pixel. This implies manipulation of more than 3 billion bits per second, without allowing for any of the actual computations being performed. Thus it may be seen that this is an environment with unique data manipulation requirements.

If the display is unchanging, no demand is placed on the rendering operations. However, some common operations (such as zooming or rotation) will require every object in the image space to be re-rendered. Slow rendering will make the rotation or zoom appear jerky. This is highly undesirable. Thus efficient rendering is an essential step in translating an image representation into the correct pixel values. This is particularly true in animation applications. where newly rendered updates to a computer graphics display must be generated at regular intervals.

The rendering requirements of three-dimensional graphics are particularly heavy. One reason for this is that. even after the three-dimensional model has been translated to a two-dimensional model, some computational tasks may be bequeathed to the rendering process. (For example, color values will need to be interpolated across a triangle or other primitive.) These computational tasks tend to burden the rendering process. Another reason is that since threedimensional graphics are much more lifelike, users are more likely to demand a fully rendered image. (By contrast. in the two-dimensional images created e.g. by a GUI or simple game, users will learn not to expect all areas of the scene to be active or filled with information.)

FIG. 1A is a very high-level view of other processes performed in a 3D graphics computer system. A three dimensional image which is defined in some fixed 3D coordinate system (a "world" coordinate system) is transformed into a viewing volume (determined by a view position and direction), and the parts of the image which fall outside the viewing volume are discarded. The visible portion of the image volume is then projected onto a viewing plane, in accordance with the familiar rules of perspective. This produces a two-dimensional image, which is now mapped into device coordinates. It is important to understand that all of these operations occur prior to the operations performed by the rendering subsystem of the present invention. FIG. 1B is an expanded version of FIG. 1A, and shows the flow of operations defined by the OpenGL standard.

A vast amount of engineering effort has been invested in computer graphics systems, and this area is one of increasing activity and demands. Numerous books have discussed the requirements of this area; see, e.g., Advances in Compuier Graphics (ed. Enderle 1990-); Chellappa and Sawchuk. Digital Image Processing and analysis (1985); Computer Graphics Hardware (ed. Reghbati and Lee 1988); Computer Graphics: Image Synthesis (ed. Joy et al.); Foley et al., Fundamentals of Interactive Computer Graphics (2.ed. 1984); Foley, Computer Graphics Principles \& Practice (2.ed. 1990); Foley, Introduction to Computer Graphics (1994); Giloi, Interactive Computer Graphics (1978); Hearn and Baker. Computer Graphics (2.ed. 1994); Hill. COMpUIER Graphics (1990); Latham, Dictionary of Computer Graphics (1991); MagnenatThalma. Image Synthesis Theory \& Practice (1988); Newman and Sproull, Principles of Interactive ComPuter Graphics (2.ed. 1979); Picture Engineering (ed. Fu and Kunii 1982); Picture Processing \& Digital Flltering (2.ed. Huang 1979); Prosise, How Computer Graphics WORK (1994); Rimmer. Brt Mapped Graphics (2.ed. 1993); Salmon. Computer Graphics Systems \& Concepts
(1987): Schachter. Computer Image Generation (1990); Watt. Three-Dimensional Computer Graphics (2.ed. 1994): Scott Whitman, Multiprocessor Methods for Computer Graphics Rendering; the SIGGRaph ProCEEDINGS for the years 1980-1994; and the IEEE Computer Graphics and Applications magazine for the years 1990-1994.
Background: Graphics Animation
In many areas of computer graphics a succession of slowly changing pictures are displayed rapidly one after the other, to give the impression of smooth movement, in much the same way as for cartoon animation. In general the higher the speed of the animation. the smoother (and better) the result.
When an application is generating animation images. it is normally necessary not only to draw each picture into the frame buffer, but also to first clear down the frame buffer. and to clear down auxiliary buffers such as depth ( Z ) buffers. stencil buffers, alpha buffers and others. A good treatment of the general principles may be found in Computer Graphics: Principles and Practice. James D. Foley et al., Reading Mass.: Addison-Wesley. A specific description of the various auxiliary buffers may be found in The OpenGL Graphics System: A Specification (Version 1.0), Mark Segal and Kurt Akeley, SGI.
In most applications the value written, when clearing any given buffer, is the same at every pixel location. though different values may be used in different auxiliary buffers. Thus the frame buffer is often cleared to the value which corresponds to black, while the depth (Z) buffer is typically cleared to a value corresponding to infinity.
The time taken to clear down the buffers is often a significant portion of the total time taken to draw a frame, so it is important to minimize it. Background: Parallelism in Graphics Processing
Due to the large number of at least partially independent operations which are performed in rendering, many proposals have been made to use some form of parallel architecture for graphics (and particularly for rendering). See, for example, the special issue of Computer Graphics on parallel rendering (September 1994). Other approaches may be found in earlier patent filings by the assignee of the present application and its predecessors, e.g. U.S. Pat. No. 5,195, 186, and published PCT applications PCT/GB90/00987, PCT/GB90/01209. PCT/GB90/01210, PCT/GB90/01212. PCT/GB90/01213. PCT/GB90/01214. PCT/GB90/01215. and PCT/GB90/01216.

## Background: Pipelined Processing Generally

There are several general approaches to parallel processing. One of the basic approaches to achieving parallelism in computer processing is a technique known as pipelining. In this technique the individual processors are, in effect, connected in series in an assembly-line configuration: one processor performs a first set of operations on one chunk of data, and then passes that chunk along to another processor which performs a second set of operations, while at the same time the first processor performs the first set operations again on another chunk of data. Such architectures are generally discussed in Kogge. The architecture of Pipelined Computers (1981).

## Background: The OpenGL ${ }^{\text {Tm }}$ Standard

The "OpenGL" standard is a very important software standard for graphics applications. In any computer system which supports this standard. the operating system(s) and application software programs can make calls according to the OpenGL standards, without knowing exactly what the hardware configuration of the system is.

The OpenGL standard provides a complete library of low-level graphics manipulation commands. which can be used to implement three-dimensional graphics operations. This standard was originally based on the proprietary standards of Silicon Graphics, Inc.. but was later transformed into an open standard. It is now becoming extremely important. not only in high-end graphics-intensive workstations, but also in high-end PCs. OpenGL is supported by Windows NT™ which makes it accessible to many PC applications.

The OpenGL specification provides some constraints on the sequence of operations. For instance, the color DDA operations must be performed before the texturing operations. which must be performed before the alpha operations. (A "DDA" or digital differential analyzer, is a conventional piece of hardware used to produce linear gradation of color (or other) values over an image area.)

Other graphics interfaces (or "APIs"), such as PHIGS or XGL. are also current as of 1995; but at the lowest level. OpenGL is a superset of most of these.
The OpenGL standard is described in the OPENGL Programming GUIDE (1993), the OpenGL Reference Manual (1993), and a book by Segal and Akeley (of SGI) entitled The Opengl Graphics System: A Specification (Version 1.0).

FIG. 1B is an expanded version of FIG. 1A. and shows the flow of operations defined by the OpenGL standard. Note that the most basic model is carried in terms of vertices, and these vertices are then assembled into primitives (such as triangles. lines, etc.). After all manipulation of the primitives has been completed, the rendering operations will translate each primitive into a set of "fragments." (A fragment is the portion of a primitive which affects a single pixel.) Again, it should be noted that all operations above the block marked "Rasterization" would be performed by a host processor, or possibly by a "geometry engine" (i.e. a dedicated processor which performs rapid matrix multiplies and related data manipulations), but would normally not be performed by a dedicated rendering processor such as that of the presently preferred embodiment.

One disadvantage of standards such as OpenGL is that they require that texturing or other processor-intensive operations be performed on data before pixel elimination tests, e.g. depth testing, is performed, which wastes processor time by performing costly texturing calculations on pixels which will be eliminated later in the pipeline. When the OpenGL specification is not required or when the current OpenGI state vector cannot eliminate pixels as a result of the alpha test. however, it would be much more efficient to eliminate as many pixels as possible before doing these calculations. The present application discloses a method and device for reordering the processing steps in the rendering pipeline to either accommodate order-specific specifications such as OpenGL. or to provide for an optimized throughput by only performing processor-intensive operations on pixels which will actually be displayed.
Background: Texturing
Texture patterns are commonly used as a way to apply realistic visual detail at the sub-polygon level. See Foley et 60 al., Computer Graphics: Princifles and Practice (2.ed. 1990. corr. 1995), especially at pages 741-744; Paul S. Heckbert. "Fundamentals of Texture Mapping and Image Warping." Thesis submitted to Dept. of EE and Computer Science. University of California. Berkeley, Jun. 17. 1994; Heckbert. "Survey of Computer Graphics," IEEE Computer Graphics. November 1986, pp.56ff. Since the surfaces are transformed (by the host or geometry engine) to produce a

2D view, the textures will need to be similarly transformed by a linear transform (normally projective or "affine"). (In conventional terminology, the coordinates of the object surface, i.e. the primitive being rendered. are referred to as an $(s, t)$ coordinate space, and the map of the stored texture is referred to a (u,v) coordinate space.) The transformation in the resulting mapping means that a horizontal line in the (x.y) display space is very likely to correspond to a slanted line in the (u.v) space of the texture map, and hence many page breaks will occur, due to the texturing operation, as rendering walks along a horizontal line of pixels.

## Innovative System and Methods

The preferred embodiment discloses a pipelined graphics processor in which the sequence can be dynamically reconfigured (e.g. between primitives) in a rendering sequence. The pipeline sequence can be configured for compliance with specifications such as OpenGL. but may also be optimized by reconfiguring the pipeline sequence to eliminate unnecessary processing. In a preferred embodiment, pixel elimination sequences such as depth and stencil tests are performed before texturing calculations are performed, so that unneeded pixel data is discarded before said texturing calculations are performed.

It is noted that the texturing operations become more computation-intense, early elimination of unneeded pixels becomes even more valuable. For example, Phong shading and bump mapping both require many more operations than more common shading and texture mapping techniques, thus making the system of the present application even more valuable in real-time rendering systems.

An overhead cost is that the reconfigurable portion of the pipeline must be flushed at each reconfiguration-but since reconfiguration is normally done only on a per-primitive basis, or even less frequently, this is a relatively small cost.

## BRIEF DESCRIPTION OF THE DRAWING

The disclosed inventions will be described with reference to the accompanying drawings, which show important sample embodiments of the invention and which are incorporated in the specification hereof by reference, wherein:

FIG. 1A, described above, is an overview of key elements and processes in a 3D graphics computer system.

FIG. 1B is an expanded version of FIG. 1A, and shows the flow of operations defined by the OpenGL standard.
FIG. 2A is an overview of the graphics rendering chip of the preferred embodiment of the parent case.
FIG. 2B is an overview of the graphics rendering chip of the presently preferred embodiment.

FIG. 2C is a more schematic view of the sequence of operations performed in the graphics rendering chip of FIG. 2B. when operating in a first mode.

FIG. 2D is a different view of the graphics rendering chip of FIG. 2B, showing the connections of a readback bus which provides a diagnostic pathway.

FIG. 2E is yet another view of the graphics rendering chip of FIG. 2B, showing how the functions of the core pipeline of FIG. 2C are combined with various external interface functions.

FIG. 2F is yet another view of the graphics rendering chip of FIG. 2B, showing how the details of FIFO depth and lookahead are implemented, in the presently preferred embodiment.

FIG. 3A shows a sample graphics board which incorporates the chip of FIG. 2B.

FIG. 3B shows another sample graphics board implementation, which differs from the board of FIG. 3A in that more memory and an additional component is used to achieve higher performance.
of FIG. 2 B accelerator chip.

FIG. 3D shows another graphics board, in which the chip of FIG. 2B shares access to a common frame store with a playback functions.

FIG. 4A illustrates the definition of the dominant side and the subordinate sides of a triangle.

FIG. 4B illustrates the sequence of rendering an Antialiased Line primitive.

FIG. 5 A is a detailed view of the router unit of the presently preferred embodiment.

FIG. 5B is a detailed view of the data path through the 20 router unit of the presently preferred embodiment when operating in a first mode.

FIG. 5C is a detailed view of the data path through the router unit of the presently preferred embodiment when operating in a second mode.

## DETAILED DESCRIPTION OF THE PREFERRED EMBODIMENTS

The numerous innovative teachings of the present applipresently preferred embodiment (by way of example. and not of limitation). The presently preferred embodiment is a GLINT ${ }^{\text {m }} 400$ TX $^{\text {TM }}$ 3D rendering chip. The Hardware Reference Manual and Programmer's Reference Manual for this chip describe further details of this sample embodiment. Both are available, as of the effective filing date of this application, from 3Dlabs Inc. Ltd., 181 Metro Drive. Suite 520, San Jose Calif. 95110.

## Definitions

The following definitions may help in understanding the exact meaning of terms used in the text of this application: application: a computer program which uses graphics animation.
depth (Z) buffer: A memory buffer containing the depth component of a pixel. Used to, for example. eliminate hidden surfaces.
blt double-buffering: A technique for achieving smooth animation, by rendering only to an undisplayed back buffer. and then copying the back buffer to the front once drawing is complete.
FrameCount Planes: Used to allow higher animation rates by enabling DRAM local buffer pixel data, such as depth ( $Z$ ), to be cleared down quickly.
55 frame buffer: An area of memory containing the displayable color buffers (front, back. left, right, overlay, underlay). This memory is typically separate from the local buffer.
local buffer: An area of memory which may be used to store non-displayable pixel information: depth(Z), stencil. FrameCount and GID planes. This memory is typically separate from the framebuffer.
pixel: Picture element. A pixel comprises the bits in all the buffers (whether stored in the local buffer or framebuffer). corresponding to a particular location in the framebuffer. stencil buffer: A buffer used to store information about a pixel which controls how subsequent stencilled pixels at the same location may be combined with the current value

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in the framebuffer. Typically used to mask complex two-dimensional shapes.

## Preferred Chip Embodiment-Overview

The GLINT ${ }^{\text {TM }}$ high performance graphics processors combine workstation class 3D graphics acceleration. and state-of-the-art 2D performance in a single chip. All 3D rendering operations are accelerated by GLINT. including Gouraud shading. texture mapping. depth buffering, antialiasing, and alpha blending.
The scalable memory architecture of GLINT makes it ideal for a wide range of graphics products. from PC boards to high-end workstation accelerators.
There will be several of the GLINT family of graphics processors: the GLINT 300SXTM is the embodiment of the parent case, and the GLINT $400 \mathrm{TX}{ }^{\text {TM }}$ is a presently preferred embodiment which is which is described herein in great detail. The two devices are generally compatible, with the 400TX adding local texture storage and texel address generation for all texture modes.

FIG. 2B is an overview of the graphics rendering chip of the presently preferred embodiment (i.e. the GLINT $400 \mathrm{TX}^{\mathrm{mi}}$ ).

## General Concept

The overall architecture of the GLINT chip is best viewed using the software paradigm of a message passing system. In this system all the processing blocks are connected in a long pipeline with communication with the adjacent blocks being done through message passing. Between each block there is a small amount of buffering, the size being specific to the local communications requirements and speed of the two blocks.
The message rate is variable and depends on the rendering mode. The messages do not propagate through the system at a fixed rate typical of a more traditional pipeline system. If the receiving block can not accept a message, because its input buffer is full. then the sending block stalls until space is available.

The message structure is fundamental to the whole system as the messages are used to control, synchronize and inform each block about the processing it is to undertake. Each message has two fields-a 32 bit data field and a 9 bit tag field. (This is the minimum width guaranteed, but some local block to block connections may be wider to accommodate more data.) The data field will hold color information, coordinate information, local state information. etc. The tag field is used by each block to identify the message type so it knows how to act on it.
Each block on receiving a message, can do one of several things:

Not recognize the message so it just passes it on to the next block.
Recognize it as updating some local state (to the block) so the local state is updated and the message terminated, i.e. not passed on to the next block.

Recognize it as a processing action, and if appropriate to the unit, the processing work specific to the unit is done. This may entail sending out new messages such as Color and/or modifying the initial message before sending it on. Any new messages are injected into the message stream before the initial message is forwarded on. Some examples will clarify this.
When the Depth Block receives a message 'new fragment', it will calculate the corresponding depth and do the depth test. If the test passes then the 'new fragment' message is passed to the next unit. If the test fails then the
message is modified and passed on. The temptation is not to pass the message on when the test fails (because the pixel is not going to be updated), but other units downstream need to keep their local DDA units in step.
(In the present application, the messages are being described in general terms so as not to be bogged down in detail at this stage. The details of what a 'new fragment' message actually specifies (i.e. coordinate. color information) is left till later. In general. the term "pixel" is used to describe the picture element on the screen or in memory. The term "fragment" is used to describe the part of a polygon or other primitive which projects onto a pixel. Note that a fragment may only cover a part of a pixel.) When the Texture Read Unit (if enabled) gets a 'new fragment' message. it will calculate the texture map addresses, and will accordingly provide 1, 2, 4 or 8 texels to the next unit together with the appropriate number of interpolation coefficients.
Each unit and the message passing are conceptually running asynchronous to all the others. However, in the presently preferred embodiment there is considerable synchrony because of the common clock.

How does the host process send messages? The message data field is the 32 bit data written by the host. and the message tag is the bottom 9 bits of the address (excluding the byte resolution address lines). Writing to a specific address causes the message type associated with that address to be inserted into the message queue. Alternatively, the on-chip DMA controller may fetch the messages from the host's memory.

The message throughput, in the presently preferred embodiment, is 50 M messages per second and this gives a fragment throughput of up to 50 M per second, depending on what is being rendered. Of course, this rate will predictably be further increased over time, with advances in process technology and clock rates.

## Linkage

The block diagram of FIG. 2A shows how the units are connected together in the GLINT 300SX embodiment, and the block diagram of FIG. 2B shows how the units are connected together in the presently preferred embodiment. Some general points are:

The following functionality is present in the 400TX. but missing from the 300SX: The Texture Address (TAddr) and Texture Read (TRd) Units are missing. Also. the router and multiplexer are missing from this section, so the unit ordering is Scissor/Stipple, Color DDA, Texture Fog Color, Alpha Test, LB Rd, etc.
In the embodiment of FIG. 2B, the order of the units can be configured in two ways. The most general order (Router, Color DDA, Texture Unit, Alpha Test. LB Rd, GID/Z/Stencil, LB Wr, Multiplexer) and will work in all modes of OpenGL. However, when the alpha test is disabled it is much better to do the Graphics ID. depth and stencil tests before the texture operations rather than after. This is because the texture operations have a high processing cost and this should not be spent on fragments which are later rejected because of window, depth or stencil tests.
The loop back to the host at the bottom provides a simple synchronization mechanism. The host can insert a Sync command and when all the preceding rendering has finished the sync command will reach the bottom host interface which will notify the host the sync event has occurred.
Benefits
The very modular nature of this architecture gives great benefits. Each unit lives in isolation from all the others and

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has a very well defined set of input and output messages. This allows the internal structure of a unit (or group of units) to be changed to make algorithmic/speed/gate count tradeoffs.
The isolation and well defined logical and behavioral interface to each unit allows much better testing and verification of the correctness of a unit.
The message passing paradigm is easy to simulate with software, and the hardware design is nicely partitioned. The architecture is self synchronizing for mode or primitive changes.
The host can mimic any block in the chain by inserting messages which that block would normally generate. These message would pass through the earlier blocks to the mimicked block unchanged and from then onwards to the rest of the blocks which cannot tell the message did not originate from the expected block. This allows for an easy work around mechanism to correct any flaws in the chip. It also allows other rasterization paradigms to be implemented outside of the chip, while still using the chip for the low level pixel operations.

## "A Day in the Life of a Triangle"

Before we get too detailed in what each unit does it is worth while looking in general terms at how a primitive (e.g. triangle) passes through the pipeline, what messages are generated, and what happens in each unit. Some simplifications have been made in the description to avoid detail which would otherwise complicate what is really a very simple process. The primitive we are going to look at is the familiar Gouraud shaded Z buffered triangle, with dithering. It is assumed any other state (i.e. depth compare mode) has been set up, but (for simplicity) such other states will be mentioned as they become relevant.
The application generates the triangle vertex information and makes the necessary OpenGL calls to draw it.
The OpenGL server/library gets the vertex information. transforms, clips and lights it. It calculates the initial values and derivatives for the values to interpolate ( $\mathrm{X}_{\text {lefr }}$ $\mathrm{X}_{\text {righr }}$ red. green. blue and depth) for unit change in dx and $d x d y{ }_{k e f}$. All these values are in fixed point integer and have unique message tags. Some of the values (the depth derivatives) have more than 32 bits to cope with the dynamic range and resolution so are sent in two halves Finally, once the derivatives, start and end values have been sent to GLINT the 'render triangle' message is sent.
On GLINT: The derivative. start and end parameter messages are received and filter down the message stream to the appropriate blocks. The depth parameters and derivatives to the Depth Unit; the RGB parameters and derivative to the Color DDA Unit; the edge values and derivatives to the Rasterizer Unit.
The 'render triangle' message is received by the rasterizer unit and all subsequent messages (from the host) are blocked until the triangle has been rasterized (but not necessarily written to the frame store). A 'prepare to render' message is passed on so any other blocks can prepare themselves.
The Rasterizer Unit walks the left and right edges of the triangle and fills in the spans between. As the walk progresses messages are send to indicate the direction of the next step: StepX or StepYDomEdge. The data field holds the current ( $\mathrm{x}, \mathrm{y}$ ) coordinate. One message is sent per pixel within the triangle boundary. The step messages are duplicated into two groups: an active group and a passive group. The messages always start off in the active group but may be changed to the passive group if this pixel fails one of the tests (e.g. depth) on its path down the
message stream. The two groups are distinguished by a single bit in the message tag. The step messages (in either form) are always passed throughout the length of the message stream, and are used by all the DDA units to keep their interpolation values in step. The step message effectively identifies the fragment and any other messages pertaining to this fragment will always precede the step message in the message stream.
The Scissor and Stipple Unit. This unit does 4 tests on the fragment (as embodied by the active step message). The screen scissor test takes the coordinates associated with the step message, converts them to be screen relative (if necessary) and compares them against the screen boundaries. The other three tests (user scissor. line stipple and area stipple) are disabled for this example. If the enabled tests pass then the active step is forwarded onto the next unit. otherwise it is changed into a passive step and then forwarded.
The Color DDA unit responds to an active step message by generating a Color message and sending this onto the next unit. The active step message is then forwarded to the next unit. The Color message holds, in the data field. the current RGBA value from the DDA. If the step message is passive then no Color message is generated. After the Color message is sent (or would have been sent) the step message is acted on to increment the DDA in the correct direction, ready for the next pixel.
Texturing, Fog and Alpha Tests Units are disabled so the messages just pass through these blocks.
In general terms the Local Buffer Read Unit reads the Graphic ID, Stencil and Depth information from the Local Buffer and passes it onto the next unit. More specifically it does:

1. If the step message is passive then no further action occurs.
2. On an active step message it calculates the linear address in the local buffer of the required data. This is done using the ( $\mathrm{X}, \mathrm{Y}$ ) position recorded in the step message and locally stored information on the 'screen width' and window base address. Separate read and write addresses are calculated.
3. The addresses are passed to the Local Buffer Interface Unit and the identified local buffer location read. The write address is held for use later.
4. Sometime later the local buffer data is returned and is formatted into a consistent internal format and inserted into a 'Local Buffer Data' message and passed on to the next unit.
The message data field is made wider to accommodate the maximum Local Buffer width of 52 bits ( 32 depth, 8 stencil, 4 graphic ID, 8 frame count) and this extra width just extends to the Local Buffer Write block.
The actual data read from the local buffer can be in several formats to allow narrower width memories to be used in cost sensitive systems. The narrower data is formatted into a consistent internal format in this block.
The Graphic ID. Stencil and Depth Unit just passes the Color message through and stores the LBData message until the step message arrives. A passive step message would just pass straight through. When the active step message is received the internal Graphic ID, stencil and depth values are compared with the ones in the LBData message as specified by this unit's mode information. If the enabled tests pass then the new local buffer data is sent in the LBWriteData message to the next unit and the

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active step message forwarded. If any of the enabled tests fail then an LBCancelWrite message is sent followed by the equivalent passive step message. The depth DDA is stepped to update the local depth value.
The Local Buffer Write Unit performs any writes which are necessary. The LBWriteData message has its data formatted into the external local buffer format and this is posted to the Local Buffer Interface Unit to be written into the memory (the write address is already waiting in the Local Buffer Interface Unit). The LBWriteCancel message just informs the Local Buffer Interface Unit that the pending write address is no longer needed and can be discarded. The step message is just passed through.
In general terms the Framebuffer Read Unit reads the color information from the framebuffer and passes it onto the next unit. More specifically it does:

1. If the step message is passive then no further action occurs.
2. On an active step message it calculates the linear address in the framebuffer of the required data. This is done using the ( $\mathbf{X} . \mathbf{Y}$ ) position recorded in the step message and locally stored information on the 'screen width' and window base address. Separate read and write addresses are calculated.
3. The addresses are passed to the Framebuffer Interface Unit and the identified framebuffer location read. The write address is held for use later.
4. Sometime later the color data is returned and inserted into a 'Frame Buffer Data' message and passed on to the next unit.
The actual data read from the framestore can be in several formats to allow narrower width memories to be used in cost sensitive systems. The formatting of the data is deferred until the Alpha Blend Unit as it is the only unit which needs to match it up with the internal formats. In this example no alpha blending or logical operations are taking place, so reads are disabled and hence no read address is sent to the Framebuffer Interface Unit. The Color and step messages just pass through.
The Alpha Blend Unit is disabled so just passes the messages through.
The Dither Unit stores the Color message internally until an active step is received. On receiving this it uses the least significant bits of the (X,Y) coordinate information to dither the contents of the Color message. Part of the dithering process is to convert from the internal color format into the format of the framebuffer. The new color is inserted into the Color message and passed on, followed by the step message.
The Logical Operations are disabled so the Color message is just converted into the FBWriteData message (just the tag changes) and forwarded on to the next unit. The step message just passes through.
The Framebuffer Write Unit performs any writes which are necessary.
The FBWriteData message has its data posted to the Framebuffer Interface Unit to be written into the memory (the write address is already waiting in the Framebuffer Interface Unit).
The step message is just passed through.
The Host Out Unit is mainly concerned with synchronization with the host so for this example will just consume any messages which reach this point in the message stream.
This description has concentrated on what happens as one fragment flows down the message stream. It is important to
remember that at any instant in time there are many fragments flowing down the message stream and the further down they reach the more processing has occurred.
Interfacing Between Blocks FIG. 2B shows the FIFO buffering and lookahead connections which are used in the presently preferred embodiment. The FIFOs are used to provide an asynchronous interface between blocks, but are expensive in terms of gate count. Note that most of these FIFOs are only one stage deep (except where indicated). which reduces their area. To maintain performance. lookahead connections are used to accelerate the "startup" of the pipeline. For example, when the Local-Buffer-Read block issues a data request. the Texture/Fog/Color blocks also receive this, and begin to transfer data accordingly. Normally a single-entry deep FIFO cannot be read and written in the same cycle. as the writing side doesn't know that the FIFO is going to be read in that cycle (and hence become eligible to be written). The look-ahead feature give the writing side this insight, so that single-cycle transfer can be achieved. This accelerates the throughput of the pipeline.

## Programming Model

The following text describes the programming model for GLINT.

## GLINT as a Register file

The simplest way to view the interface to GLINT is as a flat block of memory-mapped registers (i.e. a register file). This register file appears as part of Region 0 of the PCI address map for GLINT. See the GLINT Hardware Reference Manual for details of this address map.

When a GLINT host software driver is initialized it can map the register file into its address space. Each register has an associated address tag. giving its offset from the base of the register file (since all registers reside on a 64-bit boundary, the tag offset is measured in multiples of 8 bytes). The most straightforward way to load a value into a register is to write the data to its mapped address. In reality the chip interface comprises a 16 entry deep FIFO, and each write to a register causes the written value and the register's address tag to be written as a new entry in the FIFO.

Programming GLINT to draw a primitive consists of writing initial values to the appropriate registers followed by a write to a command register. The last write triggers the start of rendering.

GLINT has approximately 200 registers. All registers are 32 bits wide and should be 32 -bit addressed. Many registers are split into bit fields, and it should be noted that bit 0 is the least significant bit.
Register Types
GLINT has three main types of register:
Control Registers
Command Registers
Internal Registers
Control Registers are updated only by the host-the chip effectively uses them as read-only registers. Examples of control registers are the Scissor Clip unit min and max registers. Once initialized by the host. the chip only reads these registers to determine the scissor clip extents.

Command Registers are those which. when written to, typically cause the chip to start rendering (some command registers such as ResetPickResult or Sync do not initiate rendering). Normally, the host will initialize the appropriate control registers and then write to a command register to initiate drawing. There are two types of command registers: begin-draw and continue-draw. Begin-draw commands cause rendering to start with those values specified by the
control registers. Continue-draw commands cause drawing to continue with internal register values as they were when the previous drawing operation completed. Making use of continue-draw commands can significantly reduce the amount of data that has to be loaded into GLINT when drawing multiple connected objects such as polylines. Examples of command registers include the Render and ContinueNewLine registers.
For convenience this application will usually refer to "sending a Render command to GLINT" rather than saying (more precisely) "the Render Command register is written to. which initiates drawing".
Internal Registers are not accessible to host software. They are used internally by the chip to keep track of changing values. Some control registers have corresponding internal registers. When a begindraw command is sent and before rendering starts, the internal registers are updated with the values in the corresponding control registers. If a continue-draw command is sent then this update does not happen and drawing continues with the current values in the internal registers. For example. if a line is being drawn then the StartXDom and StartY control registers specify the (x. y) coordinates of the first point in the line. When a begin-draw command is sent these values are copied into internal registers. As the line drawing progresses these internal registers are updated to contain the ( $x, y$ ) coordinates of the pixel being drawn. When drawing has completed the internal registers contain the ( $\mathrm{x}, \mathrm{y}$ ) coordinates of the next point that would have been drawn. If a continue-draw command is now given these final ( $\mathrm{x}, \mathrm{y}$ ) internal values are not modified and further drawing uses these values. If a begin-draw command had been used the internal registers would have been reloaded from the StartXDom and StartY registers.
For the most part internal registers can be ignored. It is helpful to appreciate that they exist in order to understand the continue-draw commands.

## GLINT I/O Interface

There are a number of ways of loading GLINT registers for a given context:
The host writes a value to the mapped address of the register
The host writes address-tag/data pairs into a host memory buffer and uses the on-chip DMA to transfer this data to the FIFO.
The host can perform a Block Command Transfer by writing address and data values to the FIFO interface registers.
In all cases where the host writes data values directly to the chip (via the register file) it has to worry about FIFO overflow. The InFIFOSpace register indicates how many free entries remain in the FIFO. Before writing to any register the host must ensure that there is enough space left in the FIFO. The values in this register can be read at any time. When using DMA, the DMA controller will automatically ensure that there is room in the FIFO before it performs further transfers. Thus a buffer of any size can be passed to the DMA controller.

## FIFO Control

The description above considered the GLINT interface to be a register file. More precisely, when a data value is written to a register this value and the address tag for that register are combined and put into the FIFO as a new entry. The actual register is not updated until GLINT processes this entry. In the case where GLINT is busy performing a time consuming operation (e.g. drawing a large texture mapped polygon), and not draining the FIFO very quickly, it is possible for the FIFO to become full. If a write to a register
is performed when the FIFO is full no entry is put into the FIFO and that write is effectively lost.
The input FIFO is 16 entries deep and each entry consists of a tag/data pair. The InFIFOSpace register can be read to determine how many entries are free. The value returned by this register will never be greater than 16.

To check the status of the FIFO before every write is very inefficient. so it is preferably checked before loading the data for each rectangle. Since the FIFO is 16 entries deep. a further optimization is to wait for all 16 entries to be free after every second rectangle. Further optimizations can be made by moving dXDom, dXSub and dY outside the loop (as they are constant for each rectangle) and doing the FIFO wait after every third rectangle.
The InFIFOSpace FIFO control register contains a count of the number of entries currently free in the FIFO. The chip increments this register for each entry it removes from the FIFO and decrements it every time the host puts an entry in the FIFO.
The DMA Interface
Loading registers directly via the FIFO is often an inefficient way to download data to GLINT. Given that the FIFO can accommodate only a small number of entries, GLINT has to be frequently interrogated to determine how much space is left. Also, consider the situation where a given API function requires a large amount of data to be sent to GLINT. If the FIFO is written directly then a return from this function is not possible until almost all the data has been consumed by GLINT. This may take some time depending on the types of primitives being drawn.

To avoid these problems GLINT provides an on-chip DMA controller which can be used to load data from arbitrary sized ( $<64 \mathrm{~K} 32$-bit words) host buffers into the FIFO. In its simplest form the host software has to prepare 5 a host buffer containing register address tag descriptions and data values. It then writes the base address of this buffer to the DMAAddress register and the count of the number of words to transfer to the DMACount register. Writing to the DMACount register starts the DMA transfer and the host can now perform other work. In general. if the complete set of rendering commands required by a given call to a driver function can be loaded into a single DMA buffer then the driver function can return. Meanwhile, in parallel. GLINT is reading data from the host buffer and loading it into its FIFO. FIFO overfiow never occurs since the DMA controller automatically waits until there is room in the FIFO before doing any transfers.
The only restriction on the use of DMA control registers is that before attempting to reload the DMACount register the host software must wait until previous DMA has completed. It is valid to load the DMAAddress register while the previous DMA is in progress since the address is latched internally at the start of the DMA transfer.

Using DMA leaves the host free to return to the 55 application. while in parallel. GLINT is performing the DMA and drawing. This can increase performance significantly over loading a FIFO directly. In addition, some algorithms require that data be loaded multiple times (e.g. drawing the same object across multiple clipping rectangles). Since the GLINT DMA only reads the buffer data, it can be downloaded many times simply by restarting the DMA. This can be very beneficial if composing the buffer data is a time consuming task.
The host can use this hardware capability in various ways. 65 For example, a further optional optimization is to use a double buffered mechanism with two DMA buffers. This allows the second buffer to be filled before waiting for the

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previous DMA to complete, thus further improving the parallelism between host and GLINT processing. Thus, this optimization is dependent on the allocation of the host memory. If there is only one DMA host buffer then either it is being filled or it is being emptied-it cannot be filled and emptied at the same time, since there is no way for the host and DMA to interact once the DMA transfer has started. The host is at liberty to allocate as many DMA buffers as it wants; two is the minimum to do double buffering, but allocating many small buffers is generally better, as it gives the benefits of double buffering together with low latency time, so GLINT is not idle while large buffer is being filled up. However, use of many small buffers is of course more complicated.
In general the DMA buffer format consists of a 32-bit address tag description word followed by one or more data words. The DMA buffer consists of one or more sets of these formats. The following paragraphs describe the different types of tag description words that can be used.

## DMA Tag Description Format

There are 3 different tag addressing modes for DMA: hold, increment and indexed. The different DMA modes are provided to reduce the amount of data which needs to be transferred, hence making better use of the available DMA bandwidth. Each of these is described in the following sections.

## Hold Format

In this format the 32 -bit tag description contains a tag value and a count specifying the number of data words following in the buffer. The DMA controller writes each of the data words to the same address tag. For example, this is useful for image download where pixel data is continuously written to the Color register. The bottom 9 bits specify the register to which the data should be written; the high-order 16 bits specify the number of data words (minus 1) which follow in the buffer and which should be written to the address tag (note that the 2 -bit mode field for this format is zero so a given tag value can simply be loaded into the low order 16 bits).

A special case of this format is where the top 16 bits are zero indicating that a single data value follows the tag (i.e. the 32-bit tag description is simply the address tag value itself). This allows simple DMA buffers to be constructed which consist of tag/data pairs. Increment Format

This format is similar to the hold format except that as each data value is loaded the address tag is incremented (the value in the DMA buffer is not changed; GLINT updates an internal copy). Thus, this mode allows contiguous GLINT registers to be loaded by specifying a single 32-bit tag value followed by a data word for each register. The low-order 9 bits specify the address tag of the first register to be loaded. The 2 bit mode field is set to 1 and the high-order 16 bits are set to the count (minus 1) of the number of registers to update. To enable use of this format, the GLINT register file has been organized so that registers which are frequently loaded together have adjacent address tags. For example, the 32 AreaStipplePattern registers can be loaded as follows:

| AreaStipplePattern0, Count=31, Mode=1 |
| :--- |
| row 0 bits |
| row 1 bits |

row 31 bits
groups and within each group there are up to 16 tags. The low-order 4 bits of a tag give its offset within the group. The high-order 5 bits give the major group number.

The following Register Table lists the individual registers with their Major Group and Offset in the presently preferred embodiment:

## Register Table

The following table lists registers by group. giving their tag values and indicating their type. The register groups may be used to improve data transfer rates to GLINT when using DMA.

The following types of register are distinguished:

| Unit | Register | Major Group (hex) | $\begin{aligned} & \text { Off- } \\ & \text { set } \\ & \text { (hex) } \end{aligned}$ | Type |
| :---: | :---: | :---: | :---: | :---: |
| Rasterizer | StartXDom | $\infty$ | 0 | Control |
|  | dXDom | 00 | 1 | Control |
|  | StartXSub | 00 | 2 | Control |
|  | dXSub | 00 | 3 | Control |
|  | StartY | 00 | 4 | Control |
|  | dY | 00 | 5 | Control |
|  | Count | $\infty$ | 6 | Control |
|  | Render | 00 | 7 | Command |
|  | ContinueNewLine | 00 | 8 | Command |
|  | ContinueNewDom | 00 | 9 | Connmand |
|  | ContinueNewSub | 00 | A | Command |
|  | Continue | 00 | B | Command |
|  | FlushSpan | 00 | C | Command |
|  | BitMaskPattern | 00 | D | Mixed |
| Rasterizer | PointTable[0-3] | 01 | 0-3 | Control |
|  | RasterizerMode | 01 | 4 | Control |
| Scissor Stipple | ScissorMode | 03 | 0 | Control |
|  | ScissorMinXY | 03 | 1 | Control |
|  | ScissorMaxXY | 03 | 2 | Control |
|  | ScreenSize | 03 | 3 | Control |
|  | AreaStippleMode | 03 | 4 | Control |
|  | LineStippleMode | 03 | 5 | Control |
|  | LoadLineStipple | 03 | 6 | Control |
|  | Counters |  |  |  |
|  | UpdateLimeStipple <br> Counters | 03 | 7 | Command |
|  | SaveLineStipple | 03 | 8 | Command |
|  | State |  |  |  |
|  | WindowOrigin | 03 | 9 | Control |
| Scissor <br> Stipple <br> Texture <br> Color/Fog | AreaStipplePat- | 04 | O-F | Control |
|  | tern[0-31] | 05 | O-F |  |
|  | Texe 10 | OC | 0 | Control |
|  | Texe 11 | 0 C | 1 | Control |
|  | Texe 12 | 0 C | 2 | Control |
|  | Texe 13 | 0 C | 3 | Control |
|  | Texe 14 | 0 C | 4 | Control |
|  | Texe 15 | 0 C | 5 | Control |
|  | Texe 16 | OG | 6 | Control |
|  | Texe 17 | 0 C | 7 | Control |
|  | Interp0 | 0 C | 8 | Control |
|  | Interpl | OC | 9 | Control |
|  | Interp2 | OC | A | Control |
|  | Interp3 | 0 C | B | Control |
|  | Interp4 | ${ }^{0 C}$ | C | Control |
|  | TextureFilter | OC | D | Control |
| Texture/Fog <br> Color | TextureColor | OD | 0 | Control |
|  | Mode |  |  |  |
|  | TextureEnvColor | OD | 1 | Control |
|  | FogMode | OD | 2 | Control |
|  | FogColor | OD | 3 | Control |
|  | FStart | OD | 4 | Control |
|  | dFds | OD | 5 | Control |
|  | dFdyDom | OD | 6 | Control |
| Color DDA | RStart | OF | 0 | Control |
|  | dRdx | OF | 1 | Control |
|  | dRdyDom | OF | 2 | Control |
|  | GStart | OF | 3 | Control |
|  | dGdr | OF |  | Control |
|  | dGdyDom | OF | 5 | Control |

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-continued

| Unit | Register | Major <br> Group <br> (hex) | $\begin{aligned} & \text { Off- } \\ & \text { set } \\ & \text { (hex) } \end{aligned}$ | Type |
| :---: | :---: | :---: | :---: | :---: |
|  | BStart | 0 F | 6 | Control |
|  | dBdx | OF | 7 | Control |
|  | dBdyDom | OF | 8 | Control |
|  | AStart | OF | 9 | Control |
|  | dAds | OF | A | Control |
|  | dAdyDom | OF | B | Control |
|  | ColorDDAMode | OF | C | Control |
|  | ConstantColor | OF | D | Control |
|  | Color | OF | E | Mixed |
| Alpha Test | AlphaTestMode | 10 | 0 | Control |
|  | AntialiasMode | 10 | 1 | Control |
| Alpha Blend | AlphaBlendMode | 10 | 2 | Control |
| Dither | DitherMode |  | 3 | Control |
| Logical Ops | FBSofwareWrite Mask | 10 | 4 | Control |
|  | LogicalOpMode | 10 | 5 | Control |
|  | FBWriteData | 10 | 6 | Control |
| LB Read | LBReadMode | 11 | 0 | Control |
|  | LBReadFormat | 11 | 1 | Control |
|  | LBSourceOffset | 11 | 2 | Control |
|  | LBStencil | 11 | 5 | Output |
|  | LBDepth | 11 | 6 | Output |
|  | LBWindowBase | 11 | 7 | Control |
| LB Write | LBWriteMode | 11 | 8 | Control |
|  | LBWriteFormat | 11 | 9 | Control |
| GID/Stencil/ <br> Depth | Window | 13 | 0 | Control |
|  | StencilMode | 13 | 1 | Control |
|  | Stencilibata | 13 | 2 | Control |
|  | Stencil | 13 | 3 | Mixed |
|  | DepthMode | 13 | 4 | Control |
|  | Depth | 13 | 5 | Mixed |
|  | ZStartU | 13 | 6 | Control |
|  | ZStart | 13 | 7 | Control |
|  | dZdxU | 13 | 8 | Control |
|  | dZdxL | 13 | 9 | Control |
|  | dZdy DomU | 13 | A | Control |
|  | dZdy DomL | 13 | B | Control |
|  | FastClearDepth | 13 | C | Control |
| FB Read | FBReadMode | 15 | 0 | Control |
|  | FBSourceOffiset | 15 |  | Control |
|  | FBPixeloffet | 15 | 2 | Control |
|  | FBColor | 15 | 3 | Output |
|  | FBWindowBase | 15 | 6 | Control |
| FB Write | FBWriteMode | 15 | 7 | Control |
|  | FBHardware Write Mask | 15 | 8 | Control |
|  | FBBlockColor | 15 | 9 | Control |
| Host Out | FilterMode | 18 | 0 | Control |
|  | StatisticMode | 18 | 1 | Control |
|  | MinRegion | 18 | 2 | Control |
|  | MaxRegion | 18 | 3 | Control |
|  | ResetPickResult | 18 | 4 | Command |
|  | MinHitRegion | 18 | 5 | Command |
|  | MaxHitRegion | 18 | 6 | Command |
|  | PickResult | 18 | 7 | Command |
|  | Sync | 18 | 8 | Command |

This format allows up to 16 registers within a group to be loaded while still only specifying a single address tag description word.
If the Mode of the address tag description word is set to indexed mode, then the high-order 16 bits are used as a mask to indicate which registers within the group are to be used. The bottom 4 bits of the address tag description word are unused. The group is specified by bits 4 to 8 . Each bit in the mask is used to represent a unique tag within the group. If a bit is set then the corresponding register will be loaded. The number of bits set in the mask determines the number of data words that should be following the tag description word in the DMA buffer. The data is stored in order of increasing corresponding address tag.

## DMA Buffer Addresses

Host software must generate the correct DMA buffer address for the GLINT DMA controller. Normally, this means that the address passed to GLINT must be the physical address of the DMA buffer in host memory. The buffer must also reside at contiguous physical addresses as accessed by GLINT. On a system which uses virtual memory for the address space of a task. some method of allocating contiguous physical memory, and mapping this into the address space of a task must be used

If the virtual memory buffer maps to non-contiguous physical memory. then the buffer must be divided into sets of contiguous physical memory pages and each of these sets transferred separately. In such a situation the whole DMA buffer cannot be transferred in one go; the host software must wait for each set to be transferred. Often the best way to handle these fragmented transfers is via an interrupt handler.

## DMA Interrupts

GLINT provides interrupt support. as an alternative means of determining when a DMA transfer is complete. If enabled. the interrupt is generated whenever the DMACount register changes from having a non-zero to having a zero value. Since the DMACount register is decremented every time a data item is transferred from the DMA buffer this happens when the last data item is transferred from the DMA buffer.

To enable the DMA interrupt. the DMAInterruptEnable bit must be set in the IntEnable register. The interrupt handler should check the DMAFlag bit in the IntFlags register to determine that a DMA interrupt has actually occurred. To clear the interrupt a word should be written to the IntFlags register with the DMAFlag bit set to one.

This scheme frees the processor for other work while DMA is being completed. Since the overhead of handling an interrupt is often quite high for the host processor, the scheme should be tuned to allow a period of polling before sleeping on the interrupt.

## Output FIFO and Graphics Processor FIFO Interface

To read data back from GLINT an output FIFO is provided. Each entry in this FIFO is 32 -bits wide and it can hold tag or data values. Thus its format is unlike the input FIFO whose entries are always tag/data pairs (we can think of each entry in the input FIFO as being 41 bits wide: 9 bits for the tag and 32 bits for the data). The type of data written by GLINT to the output FIFO is controlled by the FilterMode register. This register allows filtering of output data in various categories including the following:

Depth: output in this category results from an image upload of the Depth buffer.
Stencil: output in this category results from an image upload of the Stencil buffer.
Color: output in this category results from an image upload of the framebuffer.
Synchronization: synchronization data is sent in response to a Sync command.
The data for the FilterMode register consists of 2 bits per category. If the least significant of these two bits is set ( $0 \times 1$ ) then output of the register tag for that category is enabled; if the most significant bit is set $(0 \times 2)$ then output of the data for that category is enabled. Both tag and data output can be

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enabled at the same time. In this case the tag is written first to the FIFO followed by the data.

For example, to perform an image upload from the framebuffer, the FilterMode register should have data output enabled for the Color category. Then, the rectangular area to be uploaded should be described to the rasterizer. Each pixel that is read from the framebuffer will then be placed into the output FIFO. If the output FIFO becomes full, then GLINT will block internally until space becomes available. It is the programmer's responsibility to read all data from the output FIFO. For example, it is important to know how many pixels should result from an image upload and to read exactly this many from the FIFO.
To read data from the output FIFO the OutputFIFOWords register should first be read to determine the number of entries in the FIFO (reading from the FIFO when it is empty returns undefined data). Then this many 32 -bit data items are read from the FIFO. This procedure is repeated until all the expected data or tag items have been read. The address of the output FIFO is described below.

Note that all expected data must be read back GLINT will block if the FIFO becomes full. Programmers must be careful to avoid the deadlock condition that will result if the host is waiting for space to become free in the input FIFO while GLINT is waiting for the host to read data from the output FIFO.

## Graphics Processor FIFO Interface

GLINT has a sequence of $1 \mathrm{~K} \times 32$ bit addresses in the PCI Region 0 address map called the Graphics Processor FIFO Interface. To read from the output FIFO any address in this range can be read (normally a program will choose the first address and use this as the address for the output FIFO). All 32-bit addresses in this region perform the same function: the range of addresses is provided for data transfer schemes which force the use of incrementing addresses.
Writing to a location in this address range provides raw access to the input FIFO. Again, the first address is normally chosen. Thus the same address can be used for both input and output FIFOs. Reading gives access to the output FIFO; writing gives access to the input FIFO.

Writing to the input FIFO by this method is different from writing to the memory mapped register file. Since the register file has a unique address for each register, writing to this unique address allows GLINT to determine the register for which the write is intended. This allows a tag/data pair to be constructed and inserted into the input FIFO. When writing to the raw FIFO address an address tag description must first be written followed by the associated data. In fact. the format of the tag descriptions and the data that follows is identical to that described above for DMA buffers. Instead of using the GLINT DMA it is possible to transfer data to GLINT by constructing a DMA-style buffer of data and then copying each item in this buffer to the raw input FIFO address. Based on the tag descriptions and data written GLINT constructs tag/data pairs to enter as real FIFO entries. The DMA mechanism can be thought of as an automatic way of writing to the raw input FIFO address.
Note, that when writing to the raw FIFO address the FIFO full condition must still be checked by reading the InFIFOSpace register. However, writing tag descriptions does not cause any entries to be entered into the FIFO: such a write simply establishes a set of tags to be paired with the subsequent data. Thus. free space need be ensured only for actual data items that are written (not the tag values). For example, in the simplest case where each tag is followed by a single data item, assuming that the FIFO is empty, then 32 writes are possible before checking again for free space.

Other Interrupts
GLINT also provides interrupt facilities for the following:
Sync: If a Sync command is sent and the Sync interrupt has been enabled then once all rendering has been completed. a data value is entered into the Host Out FIFO. and a Sync interrupt is generated when this value reaches the output end of the FIFO. Synchronization is described further in the next section.
External: this provides the capability for external hardware on a GLINT board (such as an external video timing generator) to generate interrupts to the host processor.
Error: if enabled the error interrupt will occur when GLINT detects certain error conditions. such as an attempt to write to a full FIFO.
Vertical Retrace: if enabled a vertical retrace interrupt is generated at the start of the video blank period.
Each of these are enabled and cleared in a similar way to the DMA interrupt. Synchronization
There are three main cases where the host must synchronize with GLINT: before reading back from registers
before directly accessing the framebuffer or the localbuffer via the bypass mechanism
framebuffer management tasks such as double buffering Synchronizing with GLINT implies waiting for any pending DMA to complete and waiting for the chip to complete any processing currently being performed. The following pseudo-code shows the general scheme:

```
GLINTData data;
// wait for DMA to complete
while (*DMACount != 0) {
    poll or wait for internupt
}
while (*InFIFOSpace < 2) {
    ;// wait for free space in the FIFO
f
// enable sync output and send the Sync command
data.Word = 0;
data.FiterMode.Synchronization = 0x1;
FilterMode(data. Word);
Sync(0x0);
/* wait for the sync outpur data */
do {
    while (*OutFIFOWords = 0)
            ;// poll waiting for data in output
FIFO
} while (*OutpurFFFO != Symc__tag);
```

Initially, we wait for DMA to complete as normal. We then have to wait for space to become free in the FIFO (since the DMA controller actually loads the FIFO). We need space for 2 registers: one to enable generation of an output sync value, and the Sync command itself. The enable flag can be set at initialization time. The output value will be generated only when a Sync command has actually been sent, and GLINT has then completed all processing.

Rather than polling it is possible to use a Sync interrupt as mentioned in the previous section. As well as enabling the interrupt and setting the filter mode, the data sent in the Sync command must have the most significant bit set in order to generate the interrupt. The interrupt is generated when the tag or data reaches the output end of the Host Out FIFO. Use of the Sync interrupt has to be considered carefully as GLINT will generally empty the FIFO more quickly than it takes to set up and handle the interrupt.
Host Framebuffer Bypass
Normally, the host will access the framebuffer indirectly via commands sent to the GLINT FIFO interface. However.

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GLINT does provide the whole framebuffer as part of its address space so that it can be memory mapped by an application. Access to the framebuffer via this memory mapped route is independent of the GLINT FIFO.
Drivers may choose to use direct access to the framebuffer for algorithms which are not supported by GLINT. The framebuffer bypass supports big-endian. little-endian and GIB-endian formats.
A driver making use of the framebuffer bypass mechanism should synchronize framebuffer accesses made through the FIFO with those made directly through the memory map. If data is written to the FIFO and then an access is made to the framebuffer, it is possible that the framebuffer access will occur before the commands in the FIFO have been fully processed. This lack of temporal ordering is generally not desirable.
Framebuffer Dimensions and Depth
At reset time the hardware stores the size of the framebuffer in the FBMemoryControl register. This register can be read by software to determine the amount of VRAM on the display adapter. For a given amount of VRAM, software can configure different screen resolutions and off-screen memory regions.
The framebuffer width must be set up in the FBReadMode register. The first 9 bits of this register define 3 partial products which determine the offset in pixels from one scanline to the next. Typically, these values will be worked out at initialization time and a copy kept in software. When this register needs to be modified the software copy is retrieved and any other bits modified before writing to the register.

Once the offset from one scanline to the next has been established, determining the visible screen width and height becomes a clipping issue. The visible screen width and height are set up in the ScreenSize register and enabled by setting the ScreenScissorEnable bit in the ScissorMode register.
The framebuffer depth (8, 16 or 32 -bit) is controlled by the FBModeSel register. This register provides a 2 bit field to control which of the three pixel depths is being used. The pixel depth can be changed at any time but this should not be attempted without first synchronizing with GLINT. The FBModeSel register is not a FIFO register and is updated immediately it is written. If GLINT is busy performing rendering operations, changing the pixel depth will corrupt that rendering.
Normally, the pixel depth is set at initialization time. To optimize certain 2 D rendering operations it may be desirable to change it at other times. For example, if the pixel depth is normally 8 (or 16 ) bits, changing the pixel depth to 32 bits for the duration of a bitblt can quadruple (or double) the blt speed, when the bit source and destination edges are aligned on 32 bit boundaries. Once such a blt sequence has been set up the host software must wait and synchronize with GLINT and then reset the pixel depth before continuing with further rendering. It is not possible to change the pixel depth via the FIFO, thus explicit synchronization must always be used.

## Host Localbuffer Bypass

As with the framebuffer. the localbuffer can be mapped in and accessed directly. The host should synchronize with GLINT before making any direct access to the localbuffer.
At reset time the hardware saves the size of the localbuffer in the LBMemoryControl register (localbuffer visible region size). In bypass mode the number of bits per pixel is either 32 or 64. This information is also set in the LBMemoryControl register (localbuffer bypass packing). This pixel packing defines the memory off set between one pixel and the
next. A further set of 3 bits (localbuffer width) in the LBMemoryControl register defines the number of valid bits per pixel. A typical localbuffer configuration might be 48 bits per pixel but in bypass mode the data for each pixel starts on a 64 -bit boundary. In this case valid pixel data will be contained in bits 0 to 47 . Software must set the LBReadFormat register to tell GLINT how to interpret these valid bits.

Host software must set the width in pixels of each scanline of the localbuffer in the LBReadMode FIFO register. The first 9 bits of this register define 3 partial products which determine the offset in pixels from one scanline to the next. As with the framebuffer partial products, these values will usually be worked out at initialization time and a copy kept in software. When this register needs to be modified the software copy is retrieved and any other bits modified before writing to the register. If the system is set up so that each pixel in the framebuffer has a corresponding pixel in the localbuffer then this width will be the same as that set for the framebuffer.

The localbuffer is accessible via Regions 1 and 3 of the PCI address map for GLINT. The localbuffer bypass supports big-endian and little-endian formats. These are described in a later section.

## Register Read Back

Under some operating environments, multiple tasks will want access to the GLINT chip. Sometimes a server task or driver will want to arbitrate access to GLINT on behalf of multiple applications. In these circumstances. the state of the GLINT chip may need to be saved and restored on each context switch. To facilitate this, the GLINT control registers can be read back. (However, internal and command registers cannot be read back.)

To perform a context switch the host must first synchronize with GLINT. This means waiting for outstanding DMA to complete, sending a Sync command and waiting for the sync output data to appear in the output FIFO. After this the registers can be read back.

To read a GLINT register the host reads the same address which would be used for a write, i.e. the base address of the register file plus the offset value for the register.

Note that since internal registers cannot be read back care must be taken when context switching a task which is making use of continue-draw commands. Continue-draw commands rely on the internal registers maintaining previous state. This state will be destroyed by any rendering work done by a new task. To prevent this. continue-draw commands should be performed via DMA since the context switch code has to wait for outstanding DMA to complete. Alternatively, continue-draw commands can be performed in a non-preemptable code segment.

Normally, reading back individual registers should be avoided. The need to synchronize with the chip can adversely affect performance. It is usually more appropriate to keep a software copy of the register which is updated when the actual register is updated.

Byte Swapping
Internally GLINT operates in little-endian mode. However, GLINT is designed to work with both big- and little-endian host processors. Since the PCIBus specification defines that byte ordering is preserved regardless of the size of the transfer operation. GLINT provides facilities to handle byte swapping. Each of the Configuration Space, Control Space. Framebuffer Bypass and Localbuffer Bypass memory areas have both big and little endian mappings available. The mapping to use typically depends on the endian ordering of the host processor.

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The Configuration Space may be set by a resistor in the board design to be either little endian or big endian.

The Control Space in PCI address region 0 . is 128 K bytes in size, and consists of two 64 K sized spaces. The first 64 K provides little endian access to the control space registers; the second 64 K provides big endian access to the same registers.
The framebuffer bypass consists of two PCI address regions: Region 2 and Region 4. Each is independently configurable to by the Aperture0 and Aperture 1 control registers respectively, to one of three modes: no byte swap. 16-bit swap. full byte swap. Note that the 16 bit mode is needed for the following reason. If the framebuffer is configured for 16 -bit pixels and the host is big-endian then simply byte swapping is not enough when a 32 -bit access is made (to write two pixels). In this case, the required effect is that the bytes are swapped within each 16 -bit word, but the two 16 -bit halves of the 32 -bit word are not swapped. This preserves the order of the pixels that are written as well as the byte ordering within each pixel. The 16 bit mode is referred to as GIB-endian in the PCI Multimedia Design Guide, version 1.0.
The localbuffer bypass consists of two PCI address regions: Region 1 and Region 3. Each is independently configurable to by the Aperture 0 and Aperture 1 control registers respectively, to one of two modes: no byte swap. full byte swap.
To save on the size of the address space required for GLINT. board vendors may choose to turn off access to the big endian regions ( 3 and 4) by the use of resistors on the board.
There is a bit available in the DMAControl control register to enable byte swapping of DMA data. Thus for big-endian hosts, this control bit would normally be enabled. Red and Blue Swapping
For a given graphics board the RAMDAC and/or API will usually force a given interpretation for true color pixel values. For example, 32 -bit pixels will be interpreted as either ARGB (alpha at byte 3, red at byte 2 , green at byte 1 and blue at byte 0 ) or ABGR (blue at byte 2 and red at byte 0). The byte position for red and blue may be important for software which has been written to expect one byte order or the other, in particular when handling image data stored in a file.
GLINT provides two registers to specify the byte positions of blue and red internally. In the Alpha Blend Unit the AlphaBlendMode register contains a 1 -bit field called ColorOrder. If this bit is set to zero then the byte ordering is ABGR; if the bit is set to one then the ordering is ARGB. As well as setting this bit in the Alpha Blend unit, it must also be set in the Color Formatting unit. In this unit the DitherMode register contains a Color Order bit with the same interpretation. The order applies to all of the true color pixel formats, regardless of the pixel depth.

## Hardware Data Structures

Some of the hardware data structure implementations used in the presently preferred embodiment will now be described in detail. Of course these examples are provided merely to illustrate the presently preferred embodiment in great detail, and do not necessarily delimit any of the claimed inventions.

## Localbuffer

The localbuffer holds the per pixel information corresponding to each displayed pixel and any texture maps. The per pixel information held in the localbuffer are Graphic ID (GID). Depth, Stencil and Frame Count Planes (FCP). The possible formats for each of these fields, and their use are covered individually in the following sections.

The maximum width of the localbuffer is 48 bits, but this can be reduced by changing the external memory configuration. albeit at the expense of reducing the functionality or dynamic range of one or more of the fields.

The localbuffer memory can be from 16 bits (assuming a depth buffer is always needed) to 48 bits wide in steps of 4 bits. The four fields supported in the localbuffer, their allowed lengths and positions are shown in the following table:

| Field | Lengths | Start bit positions |
| :--- | :--- | :--- |
| Depth | $16,24,32$ | 0 |
| Stencil | $0,4,8$ | $16,20,24,28,32$ |
| FrameCount | $0,4,8$ | $16,20,24,28,32,36,40$ |
| GID | 0,4 | $16,20,24,28,32,36,40,44,48$ |

The order of the fields is as shown with the depth field at the least significant end and GID field at the most significant end. The GID is at the most significant end so that various combinations of the Stencil and FrameCount field widths can be used on a per window basis without the position of the GID fields moving. If the GID field is in a different positions in different windows then the ownership tests become impossible to do.
The GID. FrameCount. Stencil and Depth fields in the localbuffer are converted into the internal format by right justification if they are less than their internal widths, i.e. the unused bits are the most significant bits and they are set to 0.

The format of the localbuffer is specified in two places: the LBReadFormat register and the LBWriteFormat register.

It is still possible to part populate the localbuffer so other combinations of the field widths are possible (i.e. depth field width of 0 ), but this may give problems if texture maps are to be stored in the localbuffer as well.

Any non-bypass read or write to the localbuffer always reads or writes all 48 bits simultaneously.

## GID field

The 4 bit GID field is used for pixel ownership tests to allow per pixel window clipping. Each window using this facility is assigned one of the GID values, and the visible pixels in the window have their GID field set to this value. If the test is enabled the current GID (set to correspond with the current window) is compared with the GID in the localbuffer for each fragment. If they are equal this pixel belongs to the window so the localbuffer and framebuffer at this coordinate may be updated.

Using the GID field for pixel ownership tests is optional and other methods of achieving the same result are:
clip the primitive to the window's boundary (or rectangular tiles which make up the window's area) and render only the visible parts of the primitive
use the scissor test to define the rectangular tiles which make up the window's visible area and render the primitive once per tile (This may be limited to only those tiles which the primitive intersects).
Depth Field
The depth field holds the depth (Z) value associated with a pixel and can be 16,24 or 32 bits wide.

## Stencil Field

The stencil field holds the stencil value associated with a pixel and can be 0.4 or 8 bits wide.

The width of the stencil buffer is also stored in the StencilMode register and is needed for clamping and masking during the update methods. The stencil compare mask should be set up to exclude any absent bits from the stencil compare operation.

FrameCount Field
The Frame Count Field holds the frame count value associated with a pixel and can be 0.4 or 8 bits wide. It is used during animation to support a fast clear mechanism to aid the rapid clearing of the depth and/or stencil fields needed at the start of each frame.

In addition to the fast clear mechanism the extent of all updates to the localbuffer and framebuffer can be recorded (MinRegion and MaxRegion registers) and read back (MinHitRegion and MaxHitRegion commands) to give the bounding box of the smallest area to clear. For some applications this will be significantly smaller than the whole window or screen, and hence faster.

The fast clear mechanism provides a method where the cost of clearing the depth and stencil buffers can be amortized over a number of clear operations issued by the application. This works as follows:

The window is divided up into n regions. where n is the range of the frame counter ( 16 or 256 ). Every time the application issues a clear command the reference frame counter is incremented (and allowed to roll over if it exceeds its maximum value) and the $\mathrm{n}^{\text {th }}$ region is cleared only. The clear updates the depth and/or stencil buffers to the new values and the frame count buffer with the reference value. This region is much smaller than the full window and hence takes less time to clear.

When the localbuffer is subsequently read and the frame count is found to be the same as the reference frame count (held in the Window register) the localbuffer data is used directly. However, if the frame count is found to be different from the reference frame count (held in the Window register) the data which would have been written, if the localbuffer had been cleared properly, is substituted for the stale data returned from the read. Any new writes to the localbuffer will set the frame count to the reference value so the next read on this pixel works normally without the substitution. The depth data to substitute is held in the FastClearDepth register and the stencil data to substitute is held in the StencilData register (along with other stencil information).

The fast clear mechanism does not present a total solution as the user can elect to clear just the stencil planes or just the depth planes. or both. The situation where the stencil planes only are 'cleared' using the fast clear method, then some rendering is done and then the depth planes are 'cleared' using the fast clear will leave ambiguous pixels in the localbuffer. The driver software will need to catch this situation. and fall back to using a per pixel write to do the second clear. Which field(s) the frame count plane refers to is recorded in the Window register.

When clear data is substituted for real memory data (during normal rendering operations) the depth write mask and stencil write masks are ignored to mimic the OpenGL operation when a buffer is cleared.

Localbuffer Coordinates
The coordinates generated by the rasterizer are 16 bit 2 's complement numbers, and so have the range +32767 to -32768 . The rasterizer will produce values in this range. but any which have a negative coordinate, or exceed the screen width or height (as programmed into the ScreenSize register) are discarded.

Coordinates can be defined window relative or screen relative and this is only relevant when the coordinate gets converted to an actual physical address in the localbuffer. In general it is expected that the windowing system will use absolute coordinates and the graphics system will use relative coordinates (to be independent of where the window really is).

GUI systems (such as Windows, Windows NT and X) usually have the origin of the coordinate system at the top left corner of the screen but this is not true for all graphics systems. For instance OpenGL uses the bottom left corner as its origin. The WindowOrigin bit in the LBReadMode register selects the top left ( 0 ) or bottom left (1) as the origin.

The actual equations used to calculate the localbuffer address to read and write are:

```
Bottom left origin:
    Destination address \(=\mathrm{LB}\) WindowBase \(-\mathrm{Y} * \mathrm{~W}+\mathrm{X}\)
    Source address =
        LBWindowBase \(-Y * W+X+\) LBSourceOffset
Top left origin:
    Destination address \(=\) LBWindowBase \(+\mathrm{Y} * \mathrm{~W}+\mathrm{X}\)
    Source address =
        LBWindowBase \(+\mathrm{Y} * \mathrm{~W}+\mathrm{X}+\) LBSourceOffset
```

where:
x is the pixel's X coordinate.
$\mathbf{Y}$ is the pixel's $\mathbf{Y}$ coordinate.
LBWindowBase holds the base address in the localbuffer of the current window.
LBSourceOffset is normally zero except during a copy operation where data is read from one address and written to another address. The offset between source and destination is held in the LBSourceOffset register.
W is the screen width. Only a subset of widths are supported and these are encoded into the PP0. PP1 and PP2 fields in the LBReadMode register.
These address calculations translate a 2 D address into a linear address.

The Screen width is specified as the sum of selected partial products so a full multiply operation is not needed. The partial products are selected by the fields PP0. PP1 and PP2 in the LBReadMode register.

For arbitrary width screens. for instance bitmaps in "off screen' memory, the next largest width from the table must be chosen. The difference between the table width and the bitmap width will be an unused strip of pixels down the right hand side of the bitmap.

Note that such bitmaps can be copied to the screen only as a series of scanlines rather than as a rectangular block. However, often windowing systems store offscreen bitmaps in rectangular regions which use the same stride as the screen. In this case normal bitblts can be used.

Texture Memory
The localbuffer is used to hold textures in the GLINT 400TX variant. In the GLINT 300SX variant the texture information is supplied by the host.

## Framebuffer

The framebuffer is a region of memory where the information produced during rasterization is written prior to being displayed. This information is not restricted to color but can include window control data for LUT management and double buffering.
The framebuffer region can hold up to 32 MBytes and there are very few restrictions on the format and size of the individual buffers which make up the video stream. Typical buffers include:

True color or color index main planes,
Overlay planes.
Underlay planes.
Window ID planes for LUT and double buffer management.
Cursor planes.

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Any combination of these planes can be supported up to a maximum of 32 MBytes. but usually it is the video level processing which is the limiting factor. The following text examines the options and choices available from GLINT for rendering, copying, etc. data to these buffers.

To access alternative buffers either the FBPixelOffset register can be loaded. or the base address of the window held in the FBWindow-Base register can be redefined. This is described in more detail below.
Buffer Organization
Each buffer resides at an address in the framebuffer memory map. For rendering and copying operations the actual buffer addresses can be on any pixel boundary. Display hardware will place some restrictions on this as it will need to access the multiple buffers in parallel to mix the buffers together depending on their relative priority, opacity and double buffer selection. For instance, visible buffers (rather than offscreen bitmaps) will typically need to be on a page boundary.

Consider the following highly configured example with a $1280 \times 1024$ double buffered system with 32 bit main planes (RGBA). 8 bit overlay and 4 bits of window control information (WID).

Combining the WID and overlay planes in the same 32 bit pixel has the advantage of reducing the amount of data to copy when a window moves. as only two copies are required-one for the main planes and one for the overlay and WID planes.

Note the position of the overlay and WID planes. This was not an arbitrary choice but one imposed by the (presumed) desire to use the color processing capabilities of GLINT (dither and interpolation) in the overlay planes. The conversion of the internal color format to the external one stored in the framebuffer depends on the size and position of the component. Note that GLINT does not support all possible configurations. For example; if the overlay and WID bits were swapped, then eight bit color index starting at bit 4 would be required to render to the overlay, but this is not supported.

## Framebuffer Coordinates

Coordinate generation for the framebuffer is similar to that for the localbuffer. but there are some key differences.

As was mentioned before. the coordinates generated by the rasterizer are 16 bit 2 's complement numbers. Coordinates can be defined as window relative or screen relative. though this is only relevant when the coordinate gets converted to an actual physical address in the framebuffer. The WindowOrigin bit in the FBReadMode register selects top left (0) or bottom left (1) as the origin for the framebuffer.
The actual equations used to calculate the framebuffer address to read and write are:

```
Bottom left origin:
Destination address \(=\) FBWindowBase \(-\mathbf{Y} * W+\mathbb{X}+\) FBPixelOffset
Source address \(=\) FBWindowBase \(-\mathbf{Y} * \mathbf{W}+\mathbf{X}+\) FBPixelOffset + FBSourceOffset
Top left Origin:
Destination address \(=\) FBWindowBase \(+\mathrm{Y} * \mathrm{~W}+\mathrm{X}+\) FBPixelOffset
Source address \(=\) FBWindowBase \(+\mathbf{Y} \mathbf{W}+\mathbf{X}+\) FBPixelOffset + FBSourceOffset
```

These address calculations translate a 2D address into a linear address, so non power of two framebuffer widths (i.e. 1280) are economical in memory.

The width is specified as the sum of selected partial products so a full multiply operation is not needed. The
partial products are selected by the fields PP0. PP1 and PP2 in the FBReadMode register. This is the same mechanism as is used to set the width of the localbuffer. but the widths may be set independently.
For arbitrary screen sizes, for instance when rendering to 'off screen' memory such as bitmaps the next largest width from the table must be chosen. The difference between the table width and the bitmap width will be an unused strip of pixels down the right hand side of the bitmap.

Note that such bitmaps can be copied to the screen only as a series of scanlines rather than as a rectangular block However, often windowing systems store offscreen bitmaps in rectangular regions which use the same stride as the screen. In this case normal bitblts can be used.

## Color Formats

The contents of the framebuffer can be regarded in two ways:
As a collection of fields of up to 32 bits with no meaning or assumed format as far as GLINT is concerned. Bit planes may be allocated to control cursor. LUT, multi-buffer visibility or priority functions. In this case GLINT will be used to set and clear bit planes quickly but not perform any color processing such as interpolation or dithering. All the color processing can be disabled so that raw reads and writes are done and the only operations are write masking and logical ops. This allows the control planes to be updated and modified as necessary. Obviously this technique can also be used for overlay buffers, etc. providing color processing is not required.
As a collection of one or more color components. All the processing of color components, except for the final write mask and logical ops are done using the internal color format of 8 bits per red, green, blue and alpha color channels. The final stage before write mask and logical ops processing converts the internal color format to that required by the physical configuration of the framebuffer and video logic. The nomenclature n@m means this component is $n$ bits wide and starts at bit position $m$ in the framebuffer. The least significant bit position is 0 and a dash in a column indicates that this component does not exist for this mode. The ColorOrder is specified by a bit in the DitherMode register.
Some important points to note:
The alpha channel is always associated with the RGB color channels rather than being a separate buffer. This allows it to be moved in parallel and to work correctly in multi-buffer updates and double buffering. If the framebuffer is not configured with an alpha channel (e.g. 24 bit framebuffer width with $8: 8: 8: 8 \mathrm{RGB}$ format) then some of the rendering modes which use the retained alpha buffer cannot be used. In these cases the NoAlphaBuffer bit in the AlphaBlendMode register should be set so that an alpha value of 255 is substituted. For the RGB modes where no alpha channel is present (e.g. 3:3:2) then this substitution is done automatically.
For the Front and Back modes the data value is replicated into both buffers.
All writes to the framebuffer try to update all 32 bits irrespective of the color format. This may not matter if the memory planes don't exist. but if they are being used (as overlay planes, for example) then the write masks (FBSoftwareWriteMask or FBHardwareWriteMask) must be set up to protect the alternative planes.
When reading the framebuffer RGBA components are scaled to their internal width of 8 bits, if needed for alpha blending.
CI values are left justified with the unused bits (if any) set to zero and are subsequently processed as the red compo-
nent. The result is replicated into each of the streams G.B and A giving four copies for CI8 and eight copies for CI4.

The 4:4:4:4 Front and Back formats are designed to support 12 bit double buffering with 4 bit Alpha, in a 32 bit system.
The 3:3:2 Front and Back formats are designed to support 8 bit double buffering in a 16 bit system.
The $1: 2: 1$ Front and Back formats are designed to support 4 bit double buffering in an 8 bit system.
It is possible to have a color index buffer at other positions as long as reduced functionality is acceptable. For example a 4 bit CI buffer at bit position 16 can be achieved using write masking and 4:4:4:4 Front format with color interpolation, but dithering is lost.
The format information needs to be stored in two places: the DitherMode register and the AlphaBlendMode register.

|  | Format | Name | Internal Color Channel |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | R | G | B | A |
| Color <br> Onder: <br> RGB | 0 | 8:8:8:8 | $8 @ 0$ | 8 88 | 8 816 | 8 824 |
|  | 1 | 5:5:5:5 | $5 @ 0$ | $5 @ 5$ | 5 (4) 10 | $5 @ 15$ |
|  | 2 | 4:4:4:4 | 4@0 | 404 | 4@8 | 4 @12 |
|  | 3 | 4:4:4:4 | 4@0 | $4 @ 8$ | 4016 | 4 @ 24 |
|  |  | Front | 4 49 | $4 @ 12$ | 4 920 | $4 @ 28$ |
|  | 4 | 4:4:4:4 | 4@0 | $4 @ 8$ | $4 @ 16$ | 4 @ 24 |
|  |  | Back | 4@4 | 4912 | 4920 | 4928 |
|  | 5 | 3:3:2 | 3 @0 | 393 | 2 26 | - |
|  |  | Front | 3@8 | 3@11 | 2 214 |  |
|  | 6 | 3:3:2 | 3@0 | $3 \times 3$ | 296 | - |
|  |  | Back | 3 (1)8 | 3@11 | 2 1914 |  |
|  | 7 | 1:2:1 | 1 @0 | 2@1 | 193 | - |
|  |  | Front | 1 @ 4 | 2 ¢5 | 1 197 |  |
|  | 8 | 1:2:1 | $1 @ 0$ | 2 11 | 193 | - |
|  |  | Back | 104 | 2 @ 5 | $1 @ 7$ |  |
| Color Order: BGR | 0 | 8:8:8:8 | $8 @ 16$ | 8 ¢88 | 8 90 | 8 @ 24 |
|  | 1 | 5:5:5:5 | $5 @ 10$ | 5 ¢5 | 5 50 | $5 @ 15$ |
|  | 2 | 4:4:4:4 | 4@8 | 4 @4 | 4@0 | 4 412 |
|  | 3 | 4:4:4:4 | 4016 | $4{ }^{61} 8$ | 4@0 | 4 ¢ 24 |
|  |  | Front | 4 @ 20 | 4@12 | 4@4 | 4 ¢28 |
|  | 4 | 4:4:4:4 | $4 @ 16$ | 4 @8 | 40 | $4 @ 24$ |
|  |  | Back | 4 @ 20 | 4@12 | 4 ¢ 4 | 4@28 |
|  | 5 | 3:3:2 | 3@5 | $3{ }^{\text {d } 2}$ | 2@0 | - |
|  |  | Front | $3 @ 13$ | $3 @ 10$ | 2 ¢8 |  |
|  | 6 | 3:3:2 | 305 | $3{ }^{\text {@ } 2}$ | 2@0 | - |
|  |  | Back | 3@13 | 3@10 | 2 ¢8 |  |
|  | 7 | 1:2:1 | 1 @3 | 2@1 | 1@0 | - |
|  |  | Front | 1 (6) | 2 (9)5 | 1 ¢ 4 |  |
|  | 8 | 1:2:1 | 103 | 2 al | 1 @0 | - |
|  |  | Back | 107 | 2@5 | $1 @ 4$ |  |
| CI | 14 | CI8 | 8 @0 | 0 | 0 | 0 |
|  | 15 | C14 | 4@0 | 0 | 0 | 0 |

Overlays and Underlays
In a GUI system there are two possible relationships between the overlay planes (or underlay) and the main planes.

The overlay planes are fixed to the main planes, so that if the window is moved then both the data in the main planes and overlay planes move together.
The overlay planes are not fixed to the main planes but floating, so that moving a window only moves the associated main or overlay planes.
In the fixed case both planes can share the same GID. The pixel offset is used to redirect the reads and writes between the main planes and the overlay (underlay) buffer. The pixel ownership tests using the GID field in the localbuffer work as expected.
In the floating case different GIDs are the best choice, because the same GID planes in the localbuffer can not be used for pixel ownership tests. The alternatives are not to use
the GID based pixel ownership tests for one of the buffers but rely on the scissor clipping, or to install a second set of GID planes so each buffer has it's own set. GLINT allows either approach.
If rendering operations to the main and overlay planes both need the depth or stencil buffers, and the windows in each overlap then each buffer will need its own exclusive depth and/or stencil buffers. This is easily achieved with GLINT by assigning different regions in the localbuffer to 10 each of the buffers. Typically this would double the local buffer memory requirements.
One scenario where the above two considerations do not cause problems. is when the overlay planes are used exclusively by the GUI system, and the main planes are used for the 3D graphics.

## VRAM Modes

High performance systems will typically use VRAM for the framebuffer and the extended functionality of VRAM over DRAM can be used to enhance performance for many rendering tasks.
Hardware Write Masks.
These allow write masking in the framebuffer without incurring a performance penalty. If hardware write masks
25 are not available. GLINT must be programmed to read the memory, merge the value with the new value using the write mask, and write it back.
To use hardware write masking, the required write mask is written to the FBHardwareWriteMask register, the FBSoftwareWriteMask register should be set to all I's. and the number of framebuffer reads is set to 0 (for normal rendering). This is achieved by clearing the ReadSource and ReadDestination enables in the FBReadMode register.

To use software write masking. the required write mask is
35 written to the FBSoftwareWriteMask register and the number of framebuffer reads is set to 1 (for normal rendering). This is achieved by setting the ReadDestination enable in the FBReadMode register.
Block Writes Block writes cause consecutive pixels in the
40 framebuffer to be written simultaneously. This is useful when filling large areas but does have some restrictions:

No pixel level clipping is available;
No depth or stencil testing can be done;
All the pixels must be written with the same value so no color interpolation. blending, dithering or logical ops can be done; and
The area is defined in screen relative coordinates.
Block writes are not restricted to rectangular areas and can be used for any trapezoid. Hardware write masking is available during block writes.

The following registers need to be set up before block fills can be used:

FBBlockColor register with the value to write to each pixel; and
FBWriteMode register with the block width field.
Sending a Render command with the PrimitiveType field set to "trapezoid" and the FastFillEnable and FastFillincrement fields set up will then cause block filling of the area.
Note that during a block fill of a trapezoid any inappropriate state is ignored so even if color interpolation, depth testing and logical ops, for example, are enabled they have no effect.

The block sizes supported are 8.16 and 32 pixels. GLINT takes care of filling any partial blocks at the end of spans. 5 Graphics Programming

GLINT provides a rich variety of operations for 2D and 3D graphics supported by its Pipelined architecture.

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The Graphics Pipeline
This section describes each of the units in the graphics Pipeline. FIG. 2C shows a schematic of the pipeline. In this diagram, the localbuffer contains the pixel ownership values (known as Graphic IDs). the FrameCount Planes (FCP). Depth (Z) and Stencil buffer. The framebuffer contains the Red. Green. Blue and Alpha bitplanes. The operations in the Pipeline include:
Rasterizer scan converts the given primitive into a series of fragments for processing by the rest of the pipeline.
Scissor Test clips out fragments that lie outside the bounds of a user defined scissor rectangle and also performs screen clipping to stop illegal access outside the screen memory.
Stipple Test masks out certain fragments according to a specified pattern. Line and area stipples are available.
Color DDA is responsible for generating the color information (True Color RGBA or Color Index(CI)) associated with a fragment.
Texture is concerned with mapping a portion of a specified image (texture) onto a fragment. The process involves filtering to calculate the texture color, and application which applies the texture color to the fragment color.
Fog blends a fog color with a fragment's color according to a given fog factor. Fogging is used for depth cuing images and to simulate atmospheric fogging.
Antialias Application combines the incoming fragment's alpha value with its coverage value when anti aliasing is enabled.
Alpha Test conditionally discards a fragment based on the outcome of a comparison between the fragments alpha value and a reference alpha value.
Pixel Ownership is concerned with ensuring that the location in the framebuffer for the current fragment is owned by the current visual. Comparison occurs between the given fragment and the Graphic ID value in the localbuffer, at the corresponding location, to determine whether the fragment should be discarded.
Stencil Test conditionally discards a fragment based on the outcome of a test between the given fragment and the value in the stencil buffer at the corresponding location. The stencil buffer is updated dependent on the result of the stencil test and the depth test.
Depth Test conditionally discards a fragment based on the outcome of a test between the depth value for the given fragment and the value in the depth buffer at the corresponding location. The result of the depth test can be used to control the updating of the stencil buffer.
Alpha Blending combines the incoming fragment's color with the color in the framebuffer at the corresponding location.
Color Formatting converts the fragment's color into the format in which the color information is stored in the framebuffer.
This may optionally involve dithering.
The Pipeline structure of GLINT is very efficient at processing fragments, for example, texture mapping calculations are not actually performed on fragments that get clipped out by scissor testing. This approach saves substantial computational effort. The pipelined nature does however mean that when programming GLINT one should be aware of what all the pipeline stages are doing at any time. For example, many operations require both a read and/or write to the localbuffer and framebuffer; in this case it is not sufficient to set a logical operation to XOR and enable logical operations, but it is also necessary to enable the reading/writing of data from/to the framebuffer.

A Gouraud Shaded Triangle
We may now revisit the "day in the life of a triangle" example given above, and review the actions taken in greater detail. Again, the primitive being rendered will be a Gouraud shaded depth buffered triangle. For this example assume that the triangle is to be drawn into a window which has its colormap set for RGB as opposed to color index operation. This means that all three color components; red. green and blue, must be handled. Also. assume the coordinate origin is 10 bottom left of the window and drawing will be from top to bottom. GLINT can draw from top to bottom or bottom to top.

Consider a triangle with vertices, $v_{1}, v_{2}$ and $v_{3}$ where each vertex comprises X. Y and $Z$ coordinates. Each vertex has a different color made up of red, green and blue ( $R, G$ and $B$ ) components. The alpha component will be omitted for this example.
Initialization
GLINT requires many of its registers to be initialized in a particular way, regardless of what is to be drawn, for instance, the screen size and appropriate clipping must be set up. Normally this only needs to be done once and for clarity this example assumes that all initialization has already been done.

Other state will change occasionally, though not usually on a per primitive basis, for instance enabling Gouraud shading and depth buffering.
Dominant and Subordinate Sides of a Triangle
As shown in FIG. 4A, the dominant side of a triangle is 30 that with the greatest range of $Y$ values. The choice of dominant side is optional when the triangle is either flat bottomed or flat topped.

GLINT always draws triangles starting from the dominant edge towards the subordinate edges. This simplifies the calculation of set up parameters as will be seen below.

These values allow the color of each fragment in the triangle to be determined by linear interpolation. For example, the red component color value of a fragment at XN, Ym could be calculated by
adding $\mathrm{dRdy}_{13}$, for each scanline between $Y_{1}$ and $Y_{n}$, to $\mathbf{R}_{1}$.
then adding $d R d x$ for each fragment along scanline $Y_{n}$ from the left edge to $X_{n}$.
The example chosen has the 'knee,' i.e. vertex 2. on the right hand side, and drawing is from left to right. If the knee were on the left side (or drawing was from right to left), then the Y deltas for both the subordinate sides would be needed to interpolate the start values for each color component (and the depth value) on each scanline. For this reason GLINT always draws triangles starting from the dominant edge and towards the subordinate edges. For the example triangle, this means left to right.
Register Set Up for Color Interpolation
For the example triangle, the GLINT registers must be set as follows, for color interpolation. Note that the format for color values is 24 bit, fixed point 2 's complement.
// Load the color start and delta values to draw
// a triangle
RStart ( $\mathbf{R}_{\mathbf{1}}$ )
GStart ( $\mathrm{G}_{1}$ )
BStart ( $\mathbf{B}_{\mathbf{1}}$ )
$\mathrm{dRdyDom}\left(\mathrm{dRdy}_{19}\right) \quad$ ) To walk up the dominant edge
dGdyDom (dGdy ${ }_{13}$ )
dBdyDom (dBdy ${ }^{13}$ )
dRdx (dRdx)
/ To walk along the scanline
-continued

```
dGdx (dGdx)
dBdx (dBdx)
```


## Calculating Depth Gradient Values

To draw from left to right and top to bottom, the depth gradients or deltas) required for interpolation are:

$$
d Z d y_{13}=\frac{Z_{3}-Z_{1}}{Y_{3}-Y_{1}}
$$

And from the plane equation:

$$
\begin{aligned}
& d Z d x=\left\{\left(Z_{1}-Z_{3}\right) \frac{\left(Y_{2}-Y_{3}\right)}{c}\right\}-\left\{\left(Z_{2}-Z_{3}\right) \frac{\left(Y_{3}-Y_{1}\right)}{c}\right\} \\
& \text { where } \\
& c=\|\left(X_{3}-X_{3}\right)\left(Y_{2}-Y_{3}\right)-\left(X_{2}-X_{3}\right)\left(Y_{1}-Y_{1}\right) \mid
\end{aligned}
$$

The divisor, shown here as $c$. is the same as for color gradient values. The two deltas $\mathrm{dZdyl}_{13}$ and dZdx allow the $Z$ value of each fragment in the triangle to be determined by linear interpolation. just as for the color interpolation.
Register Set Up for Depth Testing
Internally GLINT uses fixed point arithmetic. Each depth value must be converted into a 2 's complement 32.16 bit fixed point number and then loaded into the appropriate pair of 32 bit registers. The 'Upper' or 'U' registers store the integer portion. whilst the 'Lower' or ' $L$ ' registers store the 16 fractional bits, left justified and zero filled.

For the example triangle. GLINT would need its registers set up as follows:
// Load the depth stant and delta values
// to draw a triangle
ZStartU (Z1_MS)
ZStartL (Z1_LS)
dZdyDomU (dZdy 13_MS)
dZdyDomL (dZdy13_LS)
dZdxU (dZat_MS)
dZ dxL ( $\mathrm{dZdx} \_\mathrm{LS}$ )

Calculating the Slopes for each Side
GLINT draws filled shapes such as triangles as a series of spans with one span per scanline. Therefore it needs to know the start and end X coordinate of each span. These are determined by 'edge walking'. This process involves adding one delta value to the previous span's start X coordinate and another delta value to the previous span's end $x$ coordinate to determine the X coordinates of the new span. These delta values are in effect the slopes of the triangle sides. To draw from left to right and top to bottom. the slopes of the three sides are calculated as:

$$
\begin{aligned}
& d X_{13}=\frac{X_{3}-X_{1}}{Y_{3}-Y_{1}} \\
& d X_{12}=\frac{X_{2}-X_{1}}{Y_{2}-Y_{1}} \\
& d X_{23}=\frac{X_{3}-X_{2}}{Y_{3}-Y_{2}}
\end{aligned}
$$

This triangle will be drawn in two parts, top down to the 'knee' (i.e. vertex 2), and then from there to the bottom. The dominant side is the left side so for the top half:
$\mathrm{dXDom}=\mathrm{dX} \mathrm{X}_{13}$
$\mathrm{dXSub}=\mathrm{dX}_{12}$
The start $\mathrm{X}, \mathrm{Y}$, the number of scanlines, and the above deltas give GLINT enough information to edge walk the top half of the triangle. However. to indicate that this is not a flat topped triangle (GLINT is designed to rasterize screen aligned trapezoids and flat topped triangles). the same start position in terms of X must be given twice as StartXDom and StartXSub.
To edge walk the lower half of the triangle, selected additional information is required. The slope of the dominant edge remains unchanged, but the subordinate edge slope needs to be set to:
dXSub $=\mathrm{dX}_{23}$
Also the number of scanlines to be covered from $\mathrm{Y}_{2}$ to $\mathrm{Y}_{3}$ needs to be given. Finally to avoid any rounding errors accumulated in edge walking to $\mathrm{X}_{2}$ (which can lead to pixel errors). StartXSub must be set to $\mathbf{X}_{2}$.

## Rasterizer Mode

The GLINT rasterizer has a number of modes which have effect from the time they are set until they are modified and can thus affect many primitives. In the case of the Gouraud shaded triangle the default value for these modes are suitable.
Subpixel Correction
GLINT can perform subpixel correction of all interpolated values when rendering aliased trapezoids. This correction ensures that any parameter (color/depth/texture/fog) is correctly sampled at the center of a fragment. Subpixel correction will generally always be enabled when rendering any trapezoid which is smooth shaded, textured. fogged or depth buffered. Control of subpixel correction is in the Render command register described in the next section, and is selectable on a per primitive basis.

## Rasterization

GLINT is almost ready to draw the triangle. Setting up the registers as described here and sending the Render command will cause the top half of the example triangle to be drawn.

For drawing the example triangle, all the bit fields within the Render command should be set to 0 except the PrimitiveType which should be set to trapezoid and the SubPixelCorrectionEnable bit which should be set to TRUE.

```
// Draw triangle with knee
// Set deltas
StartXDom ( \(\mathrm{X}_{1} \ll 16\) ) // Converted to 16.16 fixed
point
dXDom \(\left.\left(\left(\mathrm{X}_{3}-\mathrm{X}_{1}\right) \ll 16\right)\left(\mathrm{Y}_{3}-\mathrm{Y}_{1}\right)\right)\)
StartXSub ( \(\mathrm{X}_{1} \ll 16\) )
\(\left.\mathrm{dXSub}\left(\left(\mathrm{X}_{2}-\mathrm{X}_{\mathrm{t}}\right) \ll 16\right)\left(\mathrm{Y}_{2}-\mathrm{Y}_{1}\right)\right)\)
Start \(\mathrm{Y}\left(\mathrm{Y}_{1} \ll 16\right)\)
dY ( \(-1 \ll 16\) )
Count ( \(\mathbf{Y}_{1}-Y_{2}\) )
// Set the render command mode
render.PrimitiveType = GLINT_TRAPEZOID_PRIMITIVE
render.SubPixelCorrectionEnable \(=\) TRUE
// Draw the top half of the triangle
Render(render)
```

After the Render command has been issued. the registers in GLINT can immediately be altered to draw the lower half of the triangle. Note that only two registers need be loaded and the command ContinueNewSub sent. Once GLINT has received ContinueNewSub, drawing of this sub-triangle will begin.

# APPENDIX 0 

// Setup the delta and start for the new edge
StartXSub $\left(\mathrm{X}_{2} \ll 16\right)$
dXSub $\left.\left(\left(X_{3}-X_{2}\right) \ll 16\right)\left(Y_{3}-Y_{2}\right)\right)$
// Draw sub-triangle
ContinueNewSub $\left(Y_{2}-Y_{3}\right)$ // Draw lower half

## Rasterizer Unit

The rasterizer decomposes a given primitive into a series of fragments for processing by the rest of the Pipeline.

GLINT can directly rasterize:
aliased screen aligned trapezoids
aliased single pixel wide lines
aliased single pixel points
antialiased screen aligned trapezoids
antialiased circular points
All other primitives are treated as one or more of the above. for example an antialiased line is drawn as a series of antialiased trapezoids.
Trapezoids GLINT's basic area primitives are screen aligned trapezoids. These are characterized by having top and bottom edges parallel to the $\mathbf{X}$ axis. The side edges may be vertical (a rectangle). but in general will be diagonal. The top or bottom edges can degenerate into points in which case we are left with either flat topped or flat bottomed triangles. Any polygon can be decomposed into screen aligned trapezoids or triangles. Usually, polygons are decomposed into triangles because the interpolation of values over nontriangular polygons is ill defined. The rasterizer does handle flat topped and flat bottomed 'bow tie' polygons which are a special case of screen aligned trapezoids.

To render a triangle, the approach adopted to determine which fragments are to be drawn is known as 'edge walking'. Suppose the aliased triangle shown in FIG. 4A was to be rendered from top to bottom and the origin was bottom left of the window. Starting at (X1, Y1) then decrementing $Y$ and using the slope equations for edges 1-2 and 1-3, the intersection of each edge on each scanline can be calculated. This results in a span of fragments per scanline for the top trapezoid. The same method can be used for the bottom trapezoid using slopes 2-3 and 1-3.

It is usually required that adjacent triangles or polygons which share an edge or vertex are drawn such that pixels which make up the edge or vertex get drawn exactly once. This may be achieved by omitting the pixels down the left or the right sides and the pixels along the top or lower sides. GLINT has adopted the convention of omitting the pixels down the right hand edge. Control of whether the pixels along the top or lower sides are omitted depends on the start $Y$ value and the number of scanlines to be covered. With the example, if Start $\mathrm{Y}=\mathrm{Y} 1$ and the number of scanlines is set to Y1-Y2, the lower edge of the top half of the triangle will be excluded. This excluded edge will get drawn as part of the lower half of the triangle.

To minimize delta calculations, triangles may be scan converted from left to right or from right to left. The direction depends on the dominant edge, that is the edge which has the maximum range of $Y$ values. Rendering always proceeds from the dominant edge towards the relevant subordinate edge. In the example above, the dominant edge is $\mathbf{1 - 3}$ so rendering will be from right to left.

The sequence of actions required to render a triangle (with a 'knee') is:

Load the edge parameters and derivatives for the dominant edge and the first subordinate edges in the first triangle.

Send the Render command. This starts the scan conversion of the first triangle, working from the dominant edge. This means that for triangles where the knee is on the left we are scanning right to left, and vice versa for triangles where the knee is on the right.
Load the edge parameters and derivatives for the remaining subordinate edge in the second triangle.
Send the ContinueNewSub command. This starts the scan conversion of the second triangle.
Pseudocode for the above example is:

```
// Set the rasterizer mode to the default
RasterizerMode (0)
I/ Setup the start values and the deltas.
// Note that the X and Y coordinates are converted
// to 16.16 format
StartXDom (Xl<<16)
dXDom (( \(\mathrm{X} 3-\mathrm{X} 1 \lll 16)(\mathrm{Y} 3-\mathrm{Y} 1))\)
StartXSub (X1<<16)
dXSub \(((\) (X2 \(2-\mathrm{X} 1) \ll 16)(\mathbf{Y} 2-Y 1))\)
StartY (Y1<<16)
dY \((-1<16) / /\) Down the screen
Count (Y1 - Y2)
" Set the render mode to aliased primitive with
/" subpixel correction.
render.PrimitiveType \(=\) GLINT_TRAPEZOID_PRIMITIVE
render.SubpixelCorrectionEnable \(=\) GLINT_TRUE
render.AntialiasEnable = GLINT_DISABLE
// Draw top half of the triangle
Render(render)
// Set the start and delta for the second half of
\(/ /\) the triangle.
StartXSub (X2<<16)
dXSub \(((\) (X3- X2) \(\ll 16)(\mathrm{Y} 3-\mathrm{Y} 2))\)
// Draw lower half of triangle
ContinueNewSub (abs(Y2 - Y3))
```

After the Render command has been sent, the registers in GLINT can immediately be altered to draw the second half of the triangle. For this, note that only two registers need be loaded and the command ContinueNewSub be sent. Once drawing of the first triangle is complete and GLINT has received the ContinueNewSub command, drawing of this sub-triangle will start. The ContinueNewSub command register is loaded with the remaining number of scanlines to be rendered.
Lines
Single pixel wide aliased lines are drawn using a DDA algorithm, so all GLINT needs by way of input data is StartX. StartY, dX. dY and length.
For polylines, a ContinueNewLine command (analogous to the Continue command used at the knee of a triangle) is used at vertices.
When a Continue command is issued some error will be propagated along the line. To minimize this, a choice of actions are available as to how the DDA units are restarted on the receipt of a Continue command. It is recommended that for OpenGL rendering the ContinueNewLine command is not used and individual segments are rendered.

Antialiased lines, of any width, are rendered as antialiased screen-aligned trapezoids.
Points
GLINT supports a single pixel aliased point primitive. For points larger than one pixel trapezoids should be used. In this case the PrimitiveType field in the Render command should be set to equal GLINT_POINT_PRIMITIVE.
Anti aliasing
GLINT uses a subpixel point sampling algorithm to antialias primitives. GLINT can directly rasterize antialiased trapezoids and points. Other primitives are composed from these base primitives.

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The rasterizer associates a coverage value with each fragment produced when antialiasing. This value represents the percentage coverage of the pixel by the fragment. GLINT supports two levels of antialiasing quality:
normal, which represents $4 \times 4$ pixel subsampling
high, which represents $8 \times 8$ pixel subsampling
Selection between these two is made by the AntialiasingQuality bit within the Render command register.
When rendering antialiased primitives with GLINT the FlushSpan command is used to terminate rendering of a primitive. This is due to the nature of GLINT antialiasing. When a primitive is rendered which does not happen to complete on a scanline boundary. GLINT retains antialiasing information about the last sub-scanline(s) it has processed. but does not generate fragments for them unless a FlushSpan command is received. The commands ContinueNewSub ContinueNewDom or Continue can then be used, as appropriate, to maintain continuity between adjacent trapezoids. This allows complex antialiased primitives to be built up from simple trapezoids or points.
To illustrate this consider using screen aligned trapezoids to render an antialiased line. The line will in general consist of three screen aligned trapezoids as shown in FIG. 4B. This FIG. illustrates the sequence of rendering an Antialiased Line primitive. Note that the line has finite width.
The procedure to render the line is as follows:

```
// Setup the blend and coverage application units
// as appropriate - not shown
// In this example only the edge deltas are shown
// loaded into registers for clarity. In reality
// start \(X\) and \(Y\) values are required
// Render Trapezoid A
\(\mathrm{dY}(1 \ll 16)\)
dXDom(dXDom1<<16)
dXSub(dXSub1<<<16)
Count(countl)
render.PrimitiveType \(=\) GLINT_TRAPEZOID
remder.AntialiasEnable \(=\) GLINT_TRUE
render.AntialiasQuality \(=\) GLINT_MIN_ANTIALIAS
render.CoverageEnable \(=\) GLINT_TRUE
Render(render)
// Render Trapezoid B
dXSub(dXSub2<<16)
ContinueNewSub(count2)
// Render Trapezoid C
dXDom(dXDom2 \(\ll 16\) )
ContinueNewDom(count3)
// Now we have finished the primitive flush out
// the last scanline
FlushSpan( )
```

Note that when rendering antialiased primitives, any count values should be given in subscanlines, for example if the quality is $4 \times 4$ then any scanline count must be multiplied by 4 to convert it into a subscanline count. Similarly, any delta yalue must be divided by 4.

When rendering. AntialiasEnable must be set in the Antialias-Mode register to scale the fragments color by the coverage value. An appropriate blending function should also be enabled.

Note, when rendering antialiased bow-ties, the coverage value on the cross-over scanline may be incorrect

GLINT can render small antialiased points. Antialiased points are treated as circles, with the coverage of the boundary fragments ranging from $0 \%$ to $100 \%$. GLINT supports:
point radii of 0.5 to 16.0 in steps of 0.25 for $4 \times 4$ antialiasing
point radii of 0.25 to 8.0 in steps of 0.125 for $8 \times 8$ antialiasing

To scan convert an antialiased point as a circle. GLINT traverses the boundary in sub scanline steps to calculate the coverage value. For this, the sub-scanline intersections are calculated incrementally using a small table. The table holds the change in X for a step in Y. Symmetry is used so the table only holds the delta values for one quadrant.

StartXDom. StartXSub and StartY are set to the top or bottom of the circle and dY set to the subscanline step. In the case of an even diameter, the last of the required entries in the table is set to zero.

Since the table is configurable, point shapes other than circles can be rendered. Also if the StartXDom and StartXSub values are not coincident then horizontal thick lines with rounded ends, can be rendered.

## Block Write Operation

GLINT supports VRAM block writes with block sizes of 8.16 and 32 pixels. The block write method does have some restrictions: None of the per pixel clipping, stipple, or fragment operations are available with the exception of write masks. One subtle restriction is that the block coordinates will be interpreted as screen relative and not window relative when the pixel mask is calculated in the Framebuffer Units

Any screen aligned trapezoid can be filled using block writes, not just rectangles.

The use of block writes is enabled by setting the FastFilIEnable and FastFillincrement fields in the Render command register. The framebuffer write unit must also be configured.

Note only the Rasterizer, Framebuffer Read and Framebuffer Write units are involved in block filling. The other units will ignore block write fragments, so it is not necessary to disable them.

## Sub Pixel Precision and Correction

As the rasterizer has 16 bits of fraction precision, and the screen width used is typically less than $2^{16}$ wide a number of bits called subpixel precision bits, are available. Consider a screen width of 4096 pixels. This figure gives a subpixel precision of 4 bits $\left(4096=2^{12}\right)$. The extra bits are required for a number of reasons:
antialiasing (where vertex start positions can be supplied to subpixel precision)
when using an accumulation buffer (where scans are rendered multiple times with jittered input vertices)
for correct interpolation of parameters to give high quality shading as described below
GLINT supports subpixel correction of interpolated values when rendering aliased trapezoids. Subpixel correction ensures that all interpolated parameters associated with a fragment (color, depth, fog, texture) are correctly sampled at the fragment's center. This correction is required to ensure consistent shading of objects made from many primitives. It should generally be enabled for all aliased rendering which uses interpolated parameters.

Subpixel correction is not applied to antialiased primitives.

## Bitmaps

A Bitmap primitive is a trapezoid or line of ones and zeros which control which fragments are generated by the rasterizer. Only fragments where the corresponding Bitmap bit is set are submitted for drawing. The normal use for this is in drawing characters, although the mechanism is available for all primitives. The Bitmap data is packed contiguously into 32 bit words so that rows are packed adjacent to each other. Bits in the mask word are by default used from the least significant end towards the most significant end and are applied to pixels in the order they are generated in.

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The rasterizer scans through the bits in each word of the Bitmap data and increments the X.Y coordinates to trace out the rectangle of the given width and height. By default. any set bits (1) in the Bitmap cause a fragment to be generated. any reset bits ( 0 ) cause the fragment to be rejected.
The selection of bits from the BitMaskPattern register can be mirrored. that is, the pattern is traversed from MSB to LSB rather than LSB to MSB. Also. the sense of the test can be reversed such that a set bit causes a fragment to be rejected and vice versa. This control is found in the RasterizerMode register.
When one Bitmap word has been exhausted and pixels in the rectangle still remain then rasterization is suspended until the next write to the BitMaskPattern register. Any unused bits in the last Bitmap word are discarded. Image Copy/Upload/Download
GLINT supports three "pixel rectangle" operations: copy. upload and download. These can apply to the Depth or Stencil Buffers (held within the localbuffer) or the framebuffer.

It should be emphasized that the GLINT copy operation moves RAW blocks of data around buffers. To zoom or re-format data, in the presently preferred embodiment. external software must upload the data. process it and then download it again.
To copy a rectangular area. the rasterizer would be configured to render the destination rectangle, thus generating fragments for the area to be copied. GLINT copy works by adding a linear offset to the destination fragment's address to find the source fragment's address.
Note that the offset is independent of the origin of the buffer or window, as it is added to the destination address. Care must be taken when the source and destination overlap to choose the source scanning direction so that the overlapping area is not overwritten before it has been moved. This may be done by swapping the values written to the StartXDom and StartXSub, or by changing the sign of dY and setting StartY to be the opposite side of the rectangle.

Localbuffer copy operations are correctly tested for pixel ownership. Note that this implies two reads of the localbuffer. one to collect the source data, and one to get the destination GID for the pixel ownership test.

GLINT buffer upload/downloads are very similar to copies in that the region of interest is generated in the rasterizer. However, the localbuffer and framebuffer are generally configured to read or to write only, rather than both read and write. The exception is that an image load may use pixel ownership tests, in which case the localbuffer destination read must be enabled.

Units which can generate fragment values, the color DDA unit for example, should generally be disabled for any copy/upload/download operations. rasterizer in 2 's complement 16 bit integer. 16 bit fraction format. The following Table lists the command registers which control the rasterizer unit:

| Register Name $\quad$ Description |  |
| :--- | :--- |
| Render | Starts the rasterization process <br> ContinueNewDom <br> Allows the rasterization to continue with a new dominant <br> edge. The dominant edge DDA is reloaded with the new <br> parameters. The subordinate edge is carried on from the <br> previous trapezoid. This allows any convex polygon to be <br> broken down into a collection of trapezoids, with continuity <br> maintained across boundaries. |
|  | The data field holds the number of scanlines for sub scan- <br> limes) to fill. Note this count does not get loaded into the |
| ContinueNewSub register. |  |$\quad$| Count |
| :--- |
| Allows the rasterization to continue with a new subordinate |
| edge. The subordinate DDA is reloaded with the new |

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-continued

| Register Name | Description |
| :---: | :---: |
|  | parameters. The dominant edge is carried on from the previous trapezoid. This is useful when scan converting triangles with a 'knee' (i.e. two subordinate edges). The data field holds the number of scanlines (or sub scanlines) to fill. Note this count does not get loaded into the Count register. |
| Continue | Allows the rasterization to continue after new delta value(s) have beell loaded, but does not cause either of the trapezoid's edge DDAs to be reloaded. <br> The data field holds the number of scanlines (or sub scanlines) to fill. Note this count does not get loaded into the Count register. |
| ContinueNewLine | Allows the rasterization to continue for the next segment in a polyline. The XY position is carried on from the previous line, but the fraction bits in the DDAs can be: kept, set to zero, half, or nearly one half, under control of the RasterizerMode. <br> The data field holds the number of scanlines to fill. Note this count does not get loaded into the Count register. The use of ContimueNewLine is not recommended for OpenGL because the DDA units will start with a slight error as compared with the value they would have been loaded with for the second and subsequent segments. |
| FlushSpan | Used when antialiasing to force the last span out when not all sub spans may be defined. |

The following Table shows the control registers of the rasterizer, in the presently preferred embodiment:
$\left.\begin{array}{lll}\hline \text { RasterizerMod } & & \\ \text { e } & 30 \\ \hline \text { Defines the long term mode of operation of the rasterizer. }\end{array}\right\}$

For efficiency. the Render command register has a number of bit fields that can be set or cleared per render operation, and which qualify other state information within GLINT. These bits are AreaStippleEnable, LineStippleEnable. ResetLineStipple. TextureEnable FogEnable. CoverageEnable and SubpixelCorrection.

One use of this feature can occur when a window is cleared to a background color. For normal 3D primitives, stippling and fog operations may have been enabled. but these are to be ignored for window clears. Initially the FogMode. AreaStippleMode and LineStippleMode registers
are enabled through the UnitEnable bits. Now bits need only be set or cleared within the Render command to achieve the required result, removing the need for the FogMode. AreaStippleMode and LineStippleMode registers to be loaded for every render operation.

The bitfields of the Render command register. in the presently preferred embodiment, are detailed below:

| Bit | Name | Description |
| :---: | :---: | :---: |
| 0 | Area-StippleEnable | This bit, when set, enables area stippling of the fragments produced during rasterization. Note that area stipple in the Stipple Unit must be enabled as well for stippling to occur. When this bit is reset no area stippling occurs irrespective of the setting of the area stipple enable bit in the Stipple Unit. This bit is useful to temporarily force no area stippling for this primitive. |
| 1 | Line-StippleEnable | This bit, when set, enables line stippling of the fragments produced during rasterization in the Stipple Unit. Note that line stipple in the Stipple Unit must be enabled as well for stippling to occur. <br> When this bit is reset no line stippling occurs irrespective of the setting if the line stipple enable bit in the Stipple Unit. This bit is useful to temporarily force no line stippling for this primitive. |
| 2 | Reset- <br> Line- <br> Stipple | This bit, when set, causes the line stipple counters in the Stipple Unit to be reset to zero, and would typically be used for the first segment in a polyline. This action is also qualified by the LineStippleEnable bit and also the stipple enable bits in the Stipple Unit. <br> When this bit is reset the stipple counters carry on from where they left off (if line stippling is enabled) |
| 3 | FastFilie nable | This bit, when set, causes fast block filling of primitives. When this bit is reset the nommal rasterization process occurs. |
| 4,5 | Fast-FillIncremen t | This two bit field selects the block size the framebuffer supports. The sizes supported and the corresponding codes are: <br> $0=8$ pixels <br> $1=16$ pixels <br> $2=32$ pixels |
| 6.7 | Primitive- <br> Type | This two bit field selects the primitive type to rasterize. The primitives are: $\begin{aligned} & 0=\text { Line } \\ & 1=\text { Trapezoid } \\ & 2=\text { Point } \end{aligned}$ |
| 8 | AntialiasEnable | This bit, when set, causes the generation of sub scanline data and the coverage value to be calculated for each fragment. The number of sub pixel samples to use is controlled by the AntialiasingQuality bit. <br> When this bit is reset normal rasterization occurs. |
| 9 | An-tialiasingQuality | This bit, when set, sets the sub pixel resolution to be $8 \times 8$ When this bit is reset the sub pixel resolution is $4 \times 4$. |
| 10 | UsePointTable | When this bit and the AntialiasingEnable are set, the dx values used to remove from one scanline to the next are derived from the Point Table. |
| 11 | SynconBitMask | This bit, when set, causes a number of actions: The least significant bit or most significant bit (depending on the MirrorBitMask bit) in the Bit Mask register is extracted and optionally inverted (controlled by the InvertMask bit). If this bit is 0 then the corresponding fragment is culled from being drawn. <br> After every fragrant the Bit Mask register is rotated by one bit. <br> If all the bits in the Bit Mask register have been used then rasterization is suspended until a new BitMaskPattern is received. If any other register is written while the rasterization is suspended then the rasterization is aborted. The register write which caused the abort is then processed as nommal. Note the behavior is slightly different when the SyncOnHostData bit is set to prevent a deadlock from occurring. In this case the rasterization doesn't suspend when all the bits have been used and if new BitMaskPattern data words are not received in a timely manner then the subsequent fragments will just reuse the bitmask. |
| 12 | SyncOn HostData | When this bit is set a fragment is produced only when one of the following registers has been written by the host: Depth, FBColor, Stencil or Color. If SyncOnBitMask is reset, then if any register other than one of these four is written to, the rasterization is aborted. If SyncOnBitMask is set, then if any register other than one of these four or BitMaskPattem, is written to, the rasterization is aborted. The register write which caused the abort is then processed as normal. Writing to the BitMaskPattern register doesn't cause any fragments to be generated, but just updates the BitMask register. |
| 13 | TextureE nable | This bit, when set, enables texturing of the fragments produced during rasterization. Note that the Texture Units must be suitably enabled as well for any texturing to occur. |

-continued

| Bit | Name | Description |
| :--- | :--- | :--- |
| 14 | Fog- <br> Enable | When this bit is reset no texruring occurs irrespective of the <br> setting of the Texture Unit controls. <br> This bit is useful to temporarily force no texturing for this <br> primitive. <br> This bit, When set, enables fogging of the fragments produced <br> during rasterization. Note that the Fog Unit must be suitably <br> enabled as well for any fogging to occur. <br> When this bit is reset no fogging occurs imrespective of the <br> setting of the Fog Unit controls. |
| This bit is useful to temporarily force no fogging for this |  |  |
| primitive. |  |  |

A number of long-term rasterizer modes are stored in the RasterizerMode register as shown below:

| Bit | Name | Description |
| :---: | :---: | :---: |
| 0 | Mirror- <br> BitMask | When this bit is set the bitmask bits are consumed from the most significant end towards the least significant end. When this bit is reset the bitmask bits are consumed from the least significant end towards the most significant end. |
| 1 | InvertBitMask | When this bit is set the bitmask is inverted first before being tested. |
| 2,3 | FractionAdjust | These bits control the action of a ContinueNewLine command and specify how the fraction bits in the $Y$ and <br> XDom DDAs are adjusted <br> 0 : No adjustment is done <br> 1: Set the fraction bits to zero <br> 2. Set the fraction bits to half <br> 3. Set the fraction to nearly half, i.e. $0 \times 7$ fff |
| 4.5 | BiasCoordinates | These bits control how much is added onto the StartXDom, StartXSub and StartY values, when they are loaded into the DDA units. The original registers are not affected: <br> 0 : Zero is added <br> 1: Half is added <br> 2: Nearly half, i.e. Ox7fff is added |

## Scissor Unit

Two scissor tests are provided in GLINT, the User Scissor test and the Screen Scissor test. The user scissor checks each fragment against a user supplied scissor region; the screen scissor checks that the fragment lies within the screen.
This test may reject fragments if some part of a window has been moved off the screen. It will not reject fragments if part of a window is simply overlapped by another window (GID testing can be used to detect this).

## Stipple Unit

Stippling is a process whereby each fragment is checked against a bit in a defined pattern. and is rejected or accepted depending on the result of the stipple test. If it is rejected it undergoes no further processing; otherwise it proceeds down the pipeline. GLINT supports two types of stippling, line and area.

## Area Stippling

A $32 \times 32$ bit area stipple pattern can be applied to fragments. The least significant n bits of the fragment's (X.Y) coordinates. index into a 2D stipple pattern. If the selected bit in the pattern is set. then the fragment passes the test. otherwise it is rejected. The number of address bits used. allow regions of $1.2 .4,8.16$ and 32 pixels to be stippled. The
address selection can be controlled independently in the X and $Y$ directions. In addition the bit pattern can be inverted 25 or mirrored. Inverting the bit pattern has the effect of changing the sense of the accept/reject test. If the mirror bit is set the most significant bit of the pattern is towards the left of the window, the default is the converse.

In some situations window relative stippling is required but coordinates are only available screen relative. To allow window relative stippling, an offset is available which is added to the coordinates before indexing the stipple table. X and $Y$ offsets can be controlled independently.

## Line Stippling

In this test, fragments are conditionally rejected on the 35 outcome of testing a linear stipple mask. If the bit is zero then the test fails, otherwise it passes. The line stipple pattern is 16 bits in length and is scaled by a repeat factor $r$ (in the range 1 to 512 ). The stipple mask bit b which controls the acceptance or rejection of a fragment is deter40 mined using:
$\mathrm{b}=($ floor ( $\mathrm{s} / \mathrm{r}$ ) ) mod 16
where $s$ is the stipple counter which is incremented for every fragment (normally along the line). This counter may be reset at the start of a polyline, but between segments it 5 continues as if there were no break.

The stipple pattern can be optionally mirrored, that is the bit pattern is traversed from most significant to least significant bits. rather than the default, from least significant to most significant.

Color DDA Unit
The color DDA unit is used to associate a color with a fragment produced by the rasterizer. This unit should be enabled for rendering operations and disabled for pixel rectangle operations (i.e. copies, uploads and downloads). 35 Two color modes are supported by GLINT. true color RGBA and color index (CI).
Gouraud Shading
When in Gouraud shading mode, the color DDA unit performs linear interpolation given a set of start and incre60 ment values. Clamping is used to ensure that the interpolated value does not underflow or overflow the permitted color range.

For a Gouraud shaded trapezoid, GLINT interpolates from the dominant edge of a trapezoid to the subordinate edges. This means that two increment values are required per color component. one to move along the dominant edge and one to move across the span to the subordinate edge.

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Note that if one is rendering to multiple buffers and has initialized the start and increment values in the color DDA unit. then any subsequent Render command will cause the start values to be reloaded.

If subpixel correction has been enabled for a primitive. then any correction required will be applied to the color components.
Flat Shading
In flat shading mode, a constant color is associated with each fragment. This color is loaded into the ConstantColor register.

Texture Unit
The texture unit combines the incoming fragment's color (generated in the color DDA unit) with a value derived from interpolating texture map values (texels).

Texture application consists of two stages; derivation of the texture color from the texels (a filtering process) and then application of the texture color to the fragment's color. which is dependent on the application mode (Decal. Blend or Modulate).
GLINT 300SX compared with the GLINT 400TX
Both the GLINT 300SX and GLINT 300TX support all the filtering and application modes described in this section. However. when using the GLINT 300SX. texel values. interpolants and texture filter selections are supplied by the host. This implies that texture coordinate interpolation and texel extraction are performed by the host using texture maps resident on the host. The recommended technique for performing texture mapping using the GLINT 300SX is to scan convert primitives on the host and render fragments as GLINT point primitives.

The GLINT 400TX automatically generates all data required for texture application as textures are stored in the localbuffer and texture parameter interpolation with full perspective correction takes place within the processor. Thus the GLINT 400TX is the processor of choice when full texture mapping acceleration is desired. the GLINT 300SX is more suitable in applications where the performance of texture mapping is not critical.

Texture Color Generation.
Texture color generation supports all the filter modes of OpenGL. that is:

Minification:

## Nearest

Linear
NearestMipMapNearest
NearestMipMapLinear
LinearMipMapNearest
LinearMipMapLinear
Magnification:
Nearest
Linear
Minification is the name given to the filtering process used whereby multiple texels map to a fragment, while magnification is the name given to the filtering process whereby only a portion of a single texel maps to a single fragment.

Nearest is the simplest form of texture mapping where the nearest texel to the sample location is selected with no filtering applied.

Linear is a more sophisticated algorithm which is dependent on the type of primitive. For lines (which are 1D), it involves linear interpolation between the two nearest texels, for polygons and points which are considered to have finite area, linear is in fact bi-linear interpolation which interpolates between the nearest 4 texels.

Mip Mapping is a technique to allow the efficient filtering of texture maps when the projected area of the fragment covers more than one texel (ie, minification). A hierarchy of texture maps is held with each one being half the size (or one 5 quarter the area) of the preceding one. A pair of maps are selected, based on the projected area of the texture. In terms of filtering this means that three filter operations are performed: one on the first map, one on the second map and one between the maps. The first filter name (Nearest or Linear) 10 in the MipMap name specifies the filtering to do on the two maps, and the second filter name specifies the filtering to do between maps. So for instance. linear mapping between two maps. with linear interpolation between the results is supported (LinearMipMapLinear), but linear interpolation on 15 one map, nearest on the other map, and linear interpolation between the two is not supported.
The filtering process takes a number of texels and interpolants. and with the current texture filter mode produces a texture color.

## Fog Unit

The fog unit is used to blend the incoming fragment's color (generated by the color DDA unit. and potentially modified by the texture unit) with a predefined fog color. Fogging can be used to simulate atmospheric fogging. and also to depth cue images.

Fog application has two stages; derivation of the fog index for a fragment, and application of the fogging effect. The fog index is a value which is interpolated over the primitive using a DDA in the same way color and depth are interpolated. The fogging effect is applied to each fragment using one of the equations described below.

Note that although the fog values are linearly interpolated over a primitive the fog values can be calculated on the host using a linear fog function (typically for simple fog effects and depth cuing) or a more complex function to model atmospheric attenuation. This would typically be an exponential function.
Fog Index Calculation-The Fog DDA
The fog DDA is used to interpolate the fog index (f) 40 across a primitive. The mechanics are similar to those of the other DDA units, and horizontal scanning proceeds from dominant to subordinate edge as discussed above.

The DDA has an internal range of approximately +511 to -512. so in some cases primitives may exceed these bounds.
45 This problem typically occurs for very large polygons which span the whole depth of a scene. The correct solution is to tessellate the polygon until polygons lie within the acceptable range, but the visual effect is frequently negligible and can often be ignored.
The fog DDA calculates a fog index value which is clamped to lie in the range 0.0 to 1.0 before it is used in the appropriate fogging equation. (Fogging is applied differently depending on the color mode.)

Antialias Application Unit
Antialias application controls the combining of the coverage value generated by the rasterizer with the color generated in the color DDA units. The application depends on the color mode, either RGBA or Color Index (C1). Antialias Application
When antialiasing is enabled this unit is used to combine the coverage value calculated for each fragment with the fragment's alpha value. In RGBA mode the alpha value is multiplied by the coverage value calculated in the rasterizer (its range is $0 \%$ to $100 \%$ ). The RGB values remain unchanged and these are modified later in the Alpha Blend unit which must be set up appropriately. In CI mode the coverage value is placed in the lower 4 bits of the color field.

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The Color Look Up Table is assumed to be set up such that each color has 16 intensities associated with it, one per coverage entry.
Polygon Antialiasing
When using GLINT to render antialiased polygons. depth buffering cannot be used. This is because the order the fragments are combined in is critical in producing the correct final color. Polygons should therefore be depth sorted, and rendered front to back using the alpha blend modes: SourceAlphaSaturate for the source blend function and One for the destination blend function. In this way the alpha component of a fragment represents the percentage pixel coverage. and the blend function accumulates coverage until the value in the alpha buffer equals one, at which point no further contributions can made to a pixel.

For the antialiasing of general scenes. with no restrictions on rendering order. the accumulation buffer is the preferred choice. This is indirectly supported by GLINT via image uploading and downloading, with the accumulation buffer residing on the host.

When antialiasing, interpolated parameters which are sampled within a fragment (color. fog and texture), will sometimes be unrepresentative of a continuous sampling of a surface, and care should be taken when rendering smooth shaded antialiased primitives. This problem does not occur in aliased rendering, as the sample point is consistently at the center of a pixel.

Alpha Test Unit
The alpha test compares a fragment's alpha value with a reference value. Alpha testing is not available in color index (CI) mode. The alpha test conditionally rejects a fragment based on the comparison between a reference alpha value and one associated with the fragment.

Localbuffer Read/Write Unit
The localbuffer holds the Graphic ID, FrameCount. Stencil and Depth data associated with a fragment. The localbuffer read/write unit controls the operation of GID testing depth testing and stencil testing.
Localbuffer Read
The LBReadMode register can be configured to make 0 . 1 or 2 reads of the localbuffer. The following are the most common modes of access to the localbuffer:

Normal rendering without depth. stencil or GID testing. This requires no localbuffer reads or writes.
Normal rendering without depth or stencil testing and with GID testing. This requires a localbuffer read to get the GID from the localbuffer.
Normal rendering with depth and/or stencil testing required which conditionally requires the localbuffer to be updated. This requires localbuffer reads and writes to be enabled.
Copy operations. Operations which copy all or part of the localbuffer with or without GID testing. This requires reads and writes enabled.
Image upload/download operations. Operations which download depth or stencil information to the local buffer or read depth. stencil fast clear or GID from the localbuffer.
Localbuffer Write
Writes to the localbuffer must be enabled to allow any update of the localbuffer to take place. The LBWriteMode register is a single bit flag which controls updating of the buffer.

## Pixel Ownership (GID) Test Unit

Any fragment generated by the rasterizer may undergo a pixel ownership test. This test establishes the current fragment's write permission to the localbuffer and framebuffer

In addition a comparison bit mask is supplied in the StencilData register. This is used to establish which bits of the source and reference value are used in the stencil function test. In addition it should normally be set to exclude 35 the top four bits when the stencil width has been set to 4 bits in the StencilMode register.
The source stencil value can be from a number of places as controlled by a field in the StencilMode register:
$\left.\begin{array}{ll}\begin{array}{l}\text { LBWriteData } \\ \text { Stencil }\end{array} & \text { Use } \\ \hline \text { Test logic } & \begin{array}{l}\text { This is the normal mode. } \\ \text { Stencil }\end{array} \\ \text { This is used, for instance, in the OpenGL draw pixels } \\ \text { function where the host supplies the stencil values in the }\end{array}\right]$

Depth Test Unit
The depth (Z) test. if enabled. compares a fragment's depth against the corresponding depth in the depth buffer. The result of the depth test can effect the updating of the stencil buffer if stencil testing is enabled. This test is only performed if all the preceding tests (bitmask, scissor, stipple. alpha. pixel ownership. stencil) have passed. The source value can be obtained from a number of places as controlled by a field in the DepthMode register:

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| Source | Use |
| :--- | :--- |
| DDA (see | This is used for normal Depth buffered 3D rendering. |
| below) |  |
| Depth register | This is used, for instance, in the OpenGL draw pixels <br> function where the host supplies the depth values through <br> the Depth register. |
|  | Alternatively this is used when a constant depth value is <br> needed, for example, when clearing the depth buffer <br> (when fast clear planes are not available) or 2 D |
| rendering where the depth is held constant. |  |

When using the depth DDA for normal depth buffered rendering operations the depth values required are similar to those required for the color values in the color DDA unit: ZStart=Start Z Value
dZdYDom=Increment along dominant edge.
$\mathrm{dZdX}=$ Increment along the scan line.
The dZdX value is not required for Z-buffered lines.
The depth unit must be enabled to update the depth buffer If it is disabled then the depth buffer will only be updated if ForceL-BUpdate is set in the Window register.

## Framebuffer Read/Write Unit

Before rendering can take place GLINT must be configured to perform the correct framebuffer read and write operations. Framebuffer read and write modes effect the operation of alpha blending, logic ops, write masks, image upload/download operations and the updating of pixels in the framebuffer.

## Framebuffer Read

The FBReadMode register allows GLINT to be configured to make 0,1 or 2 reads of the framebuffer. The following are the most common modes of access to the framebuffer: Note that avoiding unnecessary additional reads will enhance performance.
Rendering operations with no logical operations, software write-masking or alpha blending. In this case no read of the framebuffer is required and framebuffer writes should be enabled.
Rendering operations which use logical ops, software write masks or alpha blending. In these cases the destination pixel must be read from the framebuffer and framebuffer writes must be enabled.
Image copy operations. Here setup varies depending on whether hardware or software write masks are used. For software write masks, the framebuffer needs two reads. one for the source and one for the destination. When hardware write masks are used (or when the software write mask allows updating of all bits in a pixel) then only one read is required.
Image upload. This requires reading of the destination framebuffer reads to be enabled and framebuffer writes to be disabled.
Image download. In this case no framebuffer read is required
(as long as software writemasking and logic ops are disabled) and the write must be enabled.
For both the read and the write operations, an offset is added to the calculated address. The source offset (FBSourceOffset) is used for copy operations. The pixel offset (FBPixelOffset) can be used to allow multi-buffer updates. The offsets should be set to zero for normal rendering.

The data read from the framebuffer may be tagged either FBDefault (data which may be written back into the framebuffer or used in some manner to modify the fragment color) or FBColor (data which will be uploaded to the host). The table below summarizes the framebuffer read/write control for common rendering operations:

| Read- <br> Source | ReadDes- <br> tination | Writes | Read Data <br> Type | Rendering Operation |
| :--- | :--- | :--- | :--- | :--- |

## Framebuffer Write

Framebuffer writes must be enabled to allow the framebuffer to be updated. A single 1 bit flag controls this operation.

The framebuffer write unit is also used to control the operation of fast block fills. if supported by the framebuffer. Fast fill rendering is enabled via the FastFillEnable bit in the Render command register, the framebuffer fast block size must be configured to the same value as the FastFillincrement in the Render command register. The FBBlockColor register holds the data written to the framebuffer during a block fill operation and should be formatted to the 'raw' framebuffer format. When using the framebuffer in 8 bit packed mode the data should be replicated into each byte. When using the framebuffer in packed 16 bit mode the data should be replicated into the top 16 bits.

When uploading images the UpLoadData bit can be set to allow color formatting (which takes place in the Alpha Blend unit).

It should be noted that the block write capability provided by the chip of the presently preferred embodiment is itself believed to be novel. According to this new approach. a graphics system can do masked block writes of variable length (e.g. 8. 16, or 32 pixels, in the presently preferred embodiment). The rasterizer defines the limits of the block to be written, and hardware masking logic in the framebuffer interface permits the block to be filled in, with a specified primitive, only up to the limits of the object being rendered. Thus the rasterizer can step by the Block Fill increment. This permits the block-write capabilities of the VRAM chips to be used optimally, to minimize the length which must be written by separate writes per pixel.

Alpha Blend Unit
Alpha blending combines a fragment's color with those of the corresponding pixel in the framebuffer. Blending is supported in RGBA mode only.

## Alpha Blending

The alpha blend unit combines the fragment's color value with that stored in the framebuffer. using the blend equation:

$$
C_{0}=C_{S} S+C_{d} D
$$

where: $\mathrm{C}_{o}$ is the output color; $\mathrm{C}_{s}$ is the source color (calculated internally); $\mathrm{C}_{d}$ is the destination color read from

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the framebuffer; S is the source blending weight; and D is the destination blending weight. S and D are not limited to linear combinations; lookup functions can be used to implement other combining relations.

If the blend operations require any destination color components then the framebuffer read mode must be set appropriately.

## Image Formatting

The alpha blend and color formatting units can be used to format image data into any of the supported GLINT framebuffer formats.
Consider the case where the framebuffer is in RGBA 4:4:4:4 mode, and an area of the screen is to be uploaded and stored in an 8 bit RGB 3:3:2 format. The sequence of operations is:
Set the rasterizer as appropriate
Enable framebuffer reads
Disable framebuffer writes and set the UpLoadData bit in the FBWriteMode register
Enable the alpha blend unit with a blend function which passes the destination value and ignores the source value (source blend Zero, destination blend One) and set the color mode to RGBA 4:4:4:4
Set the color formatting unit to format the color of incoming fragments to an 8 bit RGB 3:3:2 framebuffer format.
The upload now proceeds as normal. This technique can be used to upload data in any supported format.
The same technique can be used to download data which is in any supported framebuffer format, in this case the rasterizer is set to sync with FBColor, rather than Color. In this case framebuffer writes are enabled, and the UpLoadData bit cleared.
Color Formatting Unit
The color formatting unit converts from GLINT's internal color representation to a format suitable to be written into the framebuffer. This process may optionally include dithering of the color values for framebuffers with less than 8 bits width per color component. If the unit is disabled then the color is not modified in any way.
As noted above, the framebuffer may be configured to be RGBA or Color Index (CI).

## Color Dithering

GLINT uses an ordered dither algorithm to implement color dithering. Several types of dithering can be selected.
If the color formatting unit is disabled. the color components RGBA are not modified and will be truncated when placed in the framebuffer. In CI mode the value is rounded to the nearest integer. In both cases the result is clamped to a maximum value to prevent overflow.
In some situations only screen coordinates are available, but window relative dithering is required. This can be implemented by adding an optional offset to the coordinates before indexing the dither tables. The offset is a two bit number which is supplied for each coordinate, X and Y . The XOffset. YOffset fields in the DitherMode register control this operation, if window relative coordinates are used they should be set to zero.

## Logical Op Unit

The logical op unit performs two functions; logic operations between the fragment color (source color) and a value from the framebuffer (destination color); and. optionally, control of a special GLINT mode which allows high performance flat shaded rendering. High Speed Flat Shaded Rendering
A special GLINT rendering mode is available which allows high speed rendering of unshaded images. To use the mode the following constraints must be satisfied: that the ReadDestination bit must be enabled in the FBReadMode register when using software write masks, in which some of the bits are zero.

## Hardware Write Masks

Hardware write masks, if available. are controlled using 65 the FBHardwareWriteMask register. If the framebuffer supports hardware write masks, and they are to be used. then software write masking should be disabled (by setting all the

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bits in the FBSoftwareWriteMask register). This will result in fewer framebuffer reads when no logical operations or alpha blending is needed.
If the framebuffer is used in 8 bit packed mode. then an 8 bit hardware write mask must be replicated to all 4 bytes of the FBHardwareWriteMask register. If the framebuffer is in 16 bit packed mode then the 16 bit hardware write mask must be replicated to both halves of the FBHardware WriteMask register.
Host Out Unit
Host Out Unit controls which registers are available at the output FIFO. gathering statistics about the rendering operations (picking and extent testing) and the synchronization of GLINT via the Sync register. These three functions are as follows:
Message filtering. This unit is the last unit in the core so any message not consumed by a preceding unit will end up here. These messages will fall in to three classifications: Rasterizer messages which are never consumed by the earlier units, messages associated with image uploads. and finally programmer mistakes where an invalid message was written to the input FIFO. Synchronization messages are a special category and are dealt with later. Any messages not filtered out are passed on the output FIFO.
Statistic Collection. Here the active step messages are used to record the extent of the rectangular region where rasterization has been occurring, or if rasterization has occurred inside a specific rectangular region. These facilities are useful for picking and debug activities.
Synctronization. It is often useful for the controlling software to find out when some rendering activity has finished, to allow the timely swapping or sharing of buffers, reading back of state, etc. To achieve this the software would send a Sync message and when this reached this unit any preceding messages or their actions are guaranteed to have finished. On receiving the Sync message it is entered into the FIFO and optionally generates an interrupt.

## Sample Board-Level Embodiment

A sample board incorporating the GLINT chip may include simply:
the GLINT chip itself, which incorporates a PCI interface; Video RAM (VRAM), to which the chip has read-write access through its frame buffer (FB) port;
DRAM. which provides a local buffer then made for such purposes as Z buffering; and
a RAMDAC, which provides analog color values in accordance with the color values read out from the VRAM.
Thus one of the advantages of the chip of the presently 50 preferred embodiment is that a minimal board implementation is a trivial task.
FIG. 3A shows a sample graphics board which incorporates the chip of FIG. 2B.
FIG. 3B shows another sample graphics board implementation. which differs from the board of FIG. 3A in that more memory and an additional component is used to achieve higher performance.
FIG. 3C shows another graphics board. in which the chip of FIG. 2B shares access to a common frame store with GUI 60 accelerator chip.
FIG. 3D shows another graphics board. in which the chip of FIG. 2B shares access to a common frame store with a video coprocessor (which may be used for video capture and playback functions (e.g. frame grabbing).
Alternative Board Embodiment with Additional Video Processor combined with an additional chip for management to the graphics produced by the graphical user interface. This provides a migration path for users and applications who need to take advantage of the existing software investment and device drivers for various other graphics chips.

FIG. 3C shows another graphics board. in which the chip of FIG. 2B shares access to a common frame store with a of FIG. $2 B$ shares access to a common frame store with a
GUI accelerator chip (such as an S 3 chip). This provides a path for software migration. and also provides a way to separate 3D rendering tasks from 2D rendering.

In this embodiment. a shared framebuffer is used to enable
In this embodiment, a shared framebuffer is used to enable framebuffer memory. Example applications using the GLINT 300SX:

Using a video device as a coprocessor to GLINT, to grab live video into the framebuffer. for displaying video in a window or acquiring a video sequence;
Using GLINT as a 3D coprocessor to a 2D GUI accelerator, preserving an existing investment in 2D driver software.
25 In a coprocessor system. the framebuffer is a shared resource, and so access to the resource needs to be arbitrated. There are also other aspects of sharing a framebuffer that need to be considered:

## Memory refreshing;

Transfer of data from the memory cells into the shift registers of the VRAM;
Control of writemasks and color registers.
GLINT uses the S3 Shared Frame Buffer Interface (SFBI) to 5 share a framebuffer. This interface is able to handle all of the above aspects for two devices sharing a frame buffer, with the GLINT acting as an arbitration master or slave.

## Timing Considerations in Shared Frame-Buffer Interface

The Control Signals used in the Shared Framebuffer interface, in the presently preferred embodiment. are as follows

In the presently preferred embodiment, the frame buffer interface of the GLINT chip contains additional simple interface logic, so that two chips can both access the same frame buffer memory. This permits the GLINT chip to be gropides produced by the graphical user inticace. This

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Framebuffer Refresh and VRAM transfer cycles by GLINT are turned off when GLINT is a secondary framebuffer controller.
GLINT asserts FBReqN whenever is requires a framebuffer access.
FBGntN is internally re-synchronized to system clock.
When FBGntN is asserted. GLINT drives FBselOEN to enable any external buffers used to drive the control signals, and then drives the framebuffer address, data and control lines to perform the memory access. FBReqN remains asserted while FBGntN is asserted.
When FBGntN is negated. GLINT finishes any outstanding memory cycles. drives the control lines inactive, negates FBselOEN and then tri-states the address, data and control lines. then releases FBReqN. GLINT guarantees to release FBReqN within 500 ns of FBGntN being negated.
GLINT will not reassert FBReqN within 4 system clock cycles ( $80 \mathrm{~ns} @ 50 \mathrm{MHz}$ ).
Considerations for Board-Level Implementations
The following are some points to be noted when implementing a shared framebuffer design with a GLINT 300SX:

Some 2D GUIAccelerators such as the S3 Vision964, and GLINT use configuration resistors on the framebuffer databus at reset. In this case care should be taken with the configuration setup where it effects read only registers inside either device. If conflicts exist that can not be resolved by the board initialization software, then the conflicts should be resolved by isolating the two devices from each other at reset so they can read the correct configuration information. This isolation need only be done for the framebuffer databus lines that cause problems;
GLINT should be configured as the secondary controller when used with an S3 GUI accelerator, as the S3 devices can only be primary controllers;
GLINT cannot be used on the daughter card interface as described in the $\mathbf{S 3}$ documentation, because this gives no access to the PCI bus. A suitable PCI bridge should be used in a design with a PCI 2D GUI accelerator and GLINT so they can both have access to the PCI bus;
The use of ribbon cable to carry the framebuffer signals between two PCI boards is not recommended, because of noise problems and the extra buffering required would impact performance;
The GLINT 300SX does not provide a way of sharing its localbuffer.
The 400TX also allows grabbing of live video into the localbuffer and real-time texture mapping of that video into the framebuffer for video manipulation effects.

## Alternative Board Embodiments with Multiple Rendering Accelerator Chips

This technical note describes some system design issues on how multiple GLINT devices can be used in parallel to achieve higher performance. The main driving force for higher performance is the simulation market which, at the low end. demands somewhere between $25-30 \mathrm{M}$ texture mapped pixels per second.

There are some key points before we look at different parallel organizations:
To gain any benefit from running multiple GLINTs in parallel. the overall system must be rendering bound. If the system is host bound or geometry bound. then adding in more GLINTs will not improve the systems performance.

The memory systems (i.e. local buffer and framebuffer) are duplicated for each GLINT. Recall that the texture maps are stored in the local buffer. A single GLINT places very high demands on the memory systems, and it would be very difficult to share them between multiple GLINTs. In the presently preferred embodiment there are no provisions for sharing the local buffer. so if this is necessary it would have to be done behind GLINT's back and transparently. The framebuffer can be shared (since GLINT has a SFB interface), but this is likely to be a bottle neck if shared between GLINTs.
Broadcast. In some parallel systems each GLINT will get the same (or mostly the same) primitive data and just render those pixels assigned to it. It is very desirable that this data is written by the host only once, or fetched from the host address space once if DMA is being used. This presents two issues: Firstly the PCI bus does not have any concept of broadcasting to multiple devices. and secondly GLINT does not have a dedicated FIFO status signal pin an external controller can use. Neither of these issues are insurmountable, but will require hardware to solve. However, if the application only uses a 'few' large texture mapped primitives so repeatedly sending or fetching the parameters for each GLINT will not be a problem.
To avoid problems with Antialiasing, Bitmasks for characters. or Line stipple, the area stipple table can be used to reserve scanlines to a processor.
Parallel Configurations
This section looks at some of the common ways of applying parallelism to the rendering operation. The list is not exhaustive and an interested reader is directed to the book by Whitman cited above. No one paradigm is best and the choice is very application or market dependent.
Frame Interleaving
Frame Interleaving is where a GLDTT works on frame n , the next GLINT works on frame $\mathrm{n}+1$, etc. Each GLINT does everything for its own frame and the video is sourced from each GLINT's framebuffer in turn. This paradigm is perhaps the simplest one with very little hardware overhead and none of the above complications regarding antialiasing. block copies, bitmasks and line stipples.

This scheme only works when the image is double buffered (normal for simulation systems) and where the increase in transport delay is acceptable. Transport delay is the time it takes for a user to see a visual change after new input stimulus to the system has occurred. With 4 GLINTs this will be 4 frame times attributable to the rendering system. plus whatever else the whole system adds.

The cost of this method is also one of the highest. as ALL the memory has to be duplicated. By contrast, the schemes where the screen is divided up can save depth and color buffer memory (but not texture memory).

Sequential frames will usually have very similar amounts of rendering, unless there is a discontinuity in the viewing position and/or orientation, so load balancing is generally good.
Frame Merging or Primitive Parallelism
Frame merging is a similar technique to frame interleaving where each GLINT has a full local buffer and framebuffer. In this case the primitives are distributed amongst the GLINTs and the resultant partial images composited using the depth information to control which fragment from the multiple buffers is displayed in each pixel position.

GLINT has not been designed to share the local buffer (where the depth information is held) so the compositing is not readily supported. Also the composition frequently needs to be done at video rate so requires some fast hardware.

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Alpha blending and Antialiasing presents some problems but the bitmask. block copies and line stipple are easily accommodated. Good load balancing depends on even distribution of primitives. Not all primitives will take the same amount of time to process so a round robin distribution scheme. or a heuristic one with takes into account the expected processing time for each primitive will be needed. Screen Subdivision-Blocks
Here the screen is divided up into large contiguous regions and a GLINT looks after each region. Primitives which overlap between regions are sent to both regions and scissor clipping used. Primitives contained wholly in one region are ideally just sent to the one GLINT.
The number of regions and the horizontal and/or vertical division of the screen can be chosen as appropriate, but horizontal bands are usually easier for the video hardware to cope with. Each GLINT only needs enough local buffer and frame buffer to cover the pixels in its own region. but texture maps are duplicated in full. Block copies are a problem when the block. or part block is moved between regions. Bit masking and line stipples can be solved with some careful clipping.

Load balancing is very poor in this paradigm, since most of the scene complexity can be concentrated into one region. Dynamically changing the size of the regions based on expected scene complexity (maybe measured from the previous frame) can alleviate the poor load balancing to some extent.

## Screen Subdivision-Interleaved Scanlines

The interleave factor is every other $\mathrm{n}^{\text {th }}$ scanline where n is the number of GLINTs. Vertical interleaves are possible, but not supported by the GLINT rasterizer. Nearly all primitives will overlap multiple scanlines so are ideally broadcast to all GLINTs. Each GLINT will have different start values for the rasterization and interpolation parameters.
Each GLINT only needs enough local buffer and frame buffer to cover the pixels in its own region, but texture maps are duplicated in full.
Some block copies are a problem when the block is moved between non nth scanlines, but horizontal moves are available with any alignment. Bit masking can be solved with some careful clipping, but line stipples have no easy solution. Antialiasing is not normally a problem but with GLINT 300SX there is no provision for sub scanline steps as well as nth scanline steps. Load balancing is excellent in this paradigm which is the main reason it features prominently in the literature.
Thus the simplest and lowest risk method of using multiple GLINTs is Frame Interleaving. but if this is not an option. e.g. because of the transport delay or the amount of memory needed, then the next best choice is the Interleaved Scanline. Linkage

FIG. 2B shows how the units are connected together Some general points are:
The order of the units can be configured in two ways. The most general order (Router, Colour DDA. Texture Units. Fog Unit. Alpha Test. LB Rd. GID/Z/Stencil, LB Wr, Multiplexer) and will work in all modes of OpenGL. However. when the alpha test is disabled it is much better to do the Graphics ID, depth and stencil tests before the texture operations rather than after. This is because the texture operations have a high processing cost and this should not be spent on fragments which are later rejected because of window, depth or stencil tests. received; wherein said first set of graphics processes requires a longer processing time than said second set of graphics processes.

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Among the disclosed classes of preferred embodiments. there is also provided: A method for processing graphics data through a data path comprising the steps of: (a) receiving a routing command from a data bus input; (b) stalling further input from said data bus input until previous data has exited said data path; (c) resuming said input from said data bus input; (d) if said routing command has a first value. thenperforming a set of texturing processes on said data, and thenperforming a set of pixel elimination processes on said data; (e) if said routing command has a second value. thenperforming said set of pixel elimination processes on said data, and thenperforming said set of texturing processes on said data, wherein some portion of said data may be eliminated by said set of pixel elimination processes according to the results of said processes; wherein steps (d) and (e) are repeated until a new routing command is received; wherein said first set of graphics processes requires a longer processing time than said second set of graphics processes.

Among the disclosed classes of preferred embodiments. there is also provided: A method for rendering graphics data comprising the steps of: (a) receiving a routing command from a data bus input; (b) stalling further input from said data bus input until previous data has exited said data path; (c) resuming said input from said data bus input; (d) if said routing command has a first value, thenperforming a set of texturing processes on said data, and thenperforming a set of pixel elimination processes on said data; (e) if said routing command has a second value, thenperforming said set of pixel elimination processes on said data, and thenperforming said set of texturing processes on said data. wherein some portion of said data may be eliminated by said set of pixel elimination processes according to the results of said processes; (f) rendering said data and writing the results to a memory; (g) displaying the contents of said memory; wherein steps (d) and (e) are repeated until a new routing command is received; wherein said set of texturing processes requires a longer processing time than said set of pixel elimination processes.

Among the disclosed classes of preferred embodiments. there is also provided: A method for processing graphics data through a data path comprising the steps of: (a) receiving a routing command from a data bus input; (b) stalling further input from said data bus input until previous data has exited said data path; (c) resuming said input from said data bus input; (d) if said routing command has a first value, thenreading said graphics data from said data bus input; performing a color DDA process on said data;performing a texturing process on said data;performing an alpha test on said data; if the data has passed the previous test, then performing a graphics ID test on said data; if the data has passed the previous tests, then performing a stencil test on said data;if the data has passed the previous tests, then performing a depth test on said data; and if the data has passed the previous tests. then writing said data to a local bus; (e) if said routing command has a second value. thenreading said graphics data from said data bus input; performing a graphics ID test on said data;if the data has passed the previous test, then performing a stencil test on said data; if the data has passed the previous tests, then performing a depth test on said data; if the data has passed the previous tests, then performing a color DDA process on said data; if the data has passed the previous tests. then performing a texturing process on said data; if the data has passed the previous tests. then performing an alpha test on said data; if the data has passed the previous tests. then writing said data to a local bus; wherein steps (d) and (e) are repeated until a new routing command is received.

Among the disclosed classes of preferred embodiments. there is also provided: A pipelined graphics processing device. comprising:a switching device connected to a data bus input and configured to route graphics data received on said data bus according to instruction data received on said data bus; a multiplexing device connected to said switching device and to a data bus output; a first processing block connected and configured to receive said graphics data from said switching device and pass processed graphics data to said multiplexing device; anda second processing block connected and configured to receive said graphics data from said switching device and pass processed graphics data to said multiplexing device; wherein said switching device routes said graphics data according to a first data path, wherein said graphics data is processed by said first processing block and then by said second processing block. or a second data path. wherein said graphics data is processed by said second processing block before said first processing block. according to said instruction data.

Among the disclosed classes of preferred embodiments. there is also provided: A pipelined graphics processing device, comprising: a routing device connected to a data bus input and data bus output and configured to route graphics data received on said data bus according to instruction data received on said data bus; a first processing block connected and configured to receive said graphics data from said routing device and pass processed graphics data back to said routing device; anda second processing block connected and configured to receive said graphics data from said routing device and pass processed graphics data back to said routing device; wherein said routing device routes data according to a first data path, wherein said graphics data is processed by said first processing block and then by said second processing block. or a second data path, wherein said graphics data is processed by said second processing block before said first processing block. according to said instruction data.

Among the disclosed classes of preferred embodiments, there is also provided: A graphics processing subsystem, comprising: at least four functionally distinct processing units, each including hardware elements which are customized to perform a rendering operation which is not performed by at least some others of said processing units; at least some ones of said processing units being connected to operate asynchronously to one another; a frame buffer. connected to be accessed by at least one of said processing units;said processing units being mutually interconnected in a pipeline relationship. with at least some successive ones of said processing units being interconnected through a FIFO buffer; and wherein at least one said processing unit is connected to look downstream, in said pipeline relationship, past the immediately succeeding one of said processors; and wherein at least two of said processing units may be dynamically reordered in said pipeline relationship; whereby the duty cycle of said processors is increased while permitting use of a reduced depth for said FIFO.

## Modifications and Variations

As will be recognized by those skilled in the art. the innovative concepts described in the present application can be modified and varied over a tremendous range of applications. and accordingly the scope of patented subject matter is not limited by any of the specific exemplary teachings given.

The foregoing text has indicated a large number of alternative implementations. particularly at the higher levels, but these are merely a few examples of the huge range of possible variations.

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For example, the preferred chip context can be combined with other functions, or distributed among other chips. as will be apparent to those of ordinary skill in the art.

For another example, the described graphics systems and subsystems can be used. in various adaptations. not only in high-end PC's. but also in workstations, arcade games, and high-end simulators.

For another example, the described graphics systems and subsystems are not necessarily limited to color displays, but can be used with monochrome systems.

For another example, the described graphics systems and subsystems are not necessarily limited to displays, but also can be used in printer drivers.

What is claimed is:

1. A method for processing graphics data through a data path comprising the steps of:
(a) receiving a routing command from a data bus input; 20
(b) stalling further input from said data bus input until previous data has exited said data path;
(c) resuming said input from said data bus input;
(d) if said routing command has a first value. then performing a first set of graphics processes on said data. and then
performing a second set of graphics processes on said data;
(e) if said routing command has a second value, then performing said second set of graphics processes on said data, and then
performing said first set of graphics processes on said data, wherein some portion of said data is selectively eliminated by said first or second sets of graphics process according to the results of said processes;
wherein steps (d) and (e) are repeated until a new routing command is received;
wherein said first set of graphics processes requires a longer processing time than said second set of graphics processes.
2. The method of claim 1. wherein said first set of graphics processes comprises the steps of:
reading said graphics data from said data bus input;
performing a color DDA process on said data;
performing a texturing process on said data; and
performing an alpha test on said data.
3. The method of claim 1, wherein said second set of graphics processes comprises the step of if the data has passed all previous tests, then performing a graphics ID test on said data.
4. The method of claim 1. wherein said second set of graphics processes comprises the step of if the data has passed the previous tests, then performing a stencil test on said data.
5. The method of claim 1 , wherein said second set of graphics processes comprises the steps of if the data has passed the previous tests, then performing a depth test on said data.
6. The method of claim 1 , wherein step (d) comprises steps according to the OpenGL standard.
7. The method of claim 1, wherein step (b) is performed by a switcher connected at said data bus input.
8. The method of claim 1, wherein a multiplexer at an 65 output of said data path indicates when said data path is clear and step (c) can begin.
9. A method for processing graphics data through a data path comprising the steps of:
(a) receiving a routing command from a data bus input;
(b) stalling further input from said data bus input until previous data has exited said data path;
(c) resuming said input from said data bus input;
(d) if said routing command has a first value. then
performing a set of texturing processes on said data. and then
performing a set of pixel elimination processes on said data;
(e) if said routing command has a second value, then
performing said set of pixel elimination processes on said data. and then
performing said set of texturing processes on said data. wherein some portion of said data is selectively eliminated by said set of pixel elimination processes according to the results of said processes;
wherein steps (d) and (e) are repeated until a new routing command is received;
wherein said first set of graphics processes requires a longer processing time than said second set of graphics processes.
10. A method for rendering graphics data comprising the steps of:
(a) receiving a routing command from a data bus input;
(b) stalling further input from said data bus input until previous data has exited said data path;
(c) resuming said input from said data bus input;
(d) if said routing command has a first value, then
performing a set of texturing processes on said data. and then
performing a set of pixel elimination processes on said data;
(e) if said routing command has a second value, then
performing said set of pixel elimination processes on said data, and then
performing said set of texturing processes on said data, wherein some portion of said data is selectively eliminated by said set of pixel elimination processes according to the results of said processes;
(f) rendering said data and writing the results to a memory;
(g) displaying the contents of said memory;
wherein steps (d) and (e) are repeated until a new routing command is received;
wherein said set of texturing processes requires a longer processing time than said set of pixel elimination processes.
11. A method for processing graphics data through a data path comprising the steps of:
(a) receiving a routing command from a data bus input;
(b) stalling further input from said data bus input until previous data has exited said data path;
(c) resuming said input from said data bus input;
(d) if said routing command has a first value. then reading said graphics data from said data bus input; performing a color DDA process on said data; performing a texturing process on said data; performing an alpha test on said data;
if the data has passed the previous test, then performing a graphics ID test on said data;
if the data has passed the previous tests, then performing a stencil test on said data;

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if the data has passed the previous tests, then performing a depth test on said data; and
if the data has passed the previous tests, then writing said data to a local bus;
(e) if said routing command has a second value. then reading said graphics data from said data bus input: performing a graphics ID test on said data;
if the data has passed the previous test. then performing a stencil test on said data;
if the data has passed the previous tests, then perform- 10 ing a depth test on said data;
if the data has passed the previous tests, then performing a color DDA process on said data;
if the data has passed the previous tests, then performing a texturing process on said data;
if the data has passed the previous tests, then performing an alpha test on said data;
if the data has passed the previous tests, then writing said data to a local bus;
wherein steps (d) and (e) are repeated until a new routing command is received.
12. The method of claim 11, wherein step (d) comprises steps according to the OpenGL standard.
13. The method of claim 11. wherein step (b) is performed by a switcher connected at said data bus input.
14. The method of claim 11. wherein a multiplexer at said local bus indicates when said data path is clear and step (c) can begin.
15. A pipelined graphics processing device, comprising:
a switching device connected to a data bus input and configured to route graphics data received on said data bus according to instruction data received on said data bus;
a multiplexing device connected to said switching device and to a data bus output;
a first processing block connected and configured to receive said graphics data from said switching device and pass processed graphics data to said multiplexing device; and
a second processing block connected and configured to receive said graphics data from said switching device and pass processed graphics data to said multiplexing device;
wherein said switching device routes said graphics data according to a first data path, wherein said graphics data is processed by said first processing block and then by said second processing block. or a second data path. wherein said graphics data is processed by said second processing block before said first processing block. according to said instruction data.
16. The device of claim 15, wherein said first data path processes said graphics data according to the OpenGL standard.
17. The device of claim 15. wherein said switching device halts all input data until the current data path is clear before switching data paths.
18. The device of claim 15 , wherein said multiplexing device is configured to determine when the current data path is clear and to allow said switching device to switch data paths.

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19. A pipelined graphics processing device, comprising: a routing device connected to a data bus input and data bus output and configured to route graphics data received on said data bus according to instruction data received on said data bus;
a first processing block connected and configured to receive said graphics data from said routing device and pass processed graphics data back to said routing device; and
a second processing block connected and configured to receive said graphics data from said routing device and pass processed graphics data back to said routing device;
wherein said routing device routes data according to a first data path, wherein said graphics data is processed by said first processing block and then by said second processing block, or a second data path, wherein said graphics data is processed by said second processing block before said first processing block, according to said instruction data.
20. A graphics processing subsystem, comprising:
at least four functionally distinct processing units. each including hardware elements which are customized to perform a rendering operation which is not performed by at least some others of said processing units; at least some ones of said processing units being connected to operate asynchronously to one another;
a frame buffer, connected to be accessed by at least one of said processing units;
said processing units being mutually interconnected in a pipeline relationship, with at least some successive ones of said processing units being interconnected through a FIFO buffer;
and wherein at least one said processing unit is connected to look downstream. in said pipeline relationship. past the immediately succeeding one of said processors;
and wherein at least two of said processing units are selectively dynamically reordered in said pipeline relationship;
whereby the duty cycle of said processors is increased while permitting use of a reduced depth for said FIFO.
21. The graphics processing subsystem of claim 20 , 5 wherein said processing units include a texturing unit.
22. The graphics processing subsystem of claim 20. wherein said processing units include a scissoring unit.
23. The graphics processing subsystem of claim 20. wherein said processing units include a memory access unit which reads and writes a local buffer memory.
24. The graphics processing subsystem of claim 20. wherein at least some ones of said processing units include internally paralleled data paths.
25. The graphics processing subsystem of claim 20 . wherein all of said processing units are integrated into a single integrated circuit.
26. The graphics processing subsystem of claim 20. wherein all of said processing units, but not said frame buffer, are integrated into a single integrated circuit.

[^0]:    ${ }^{1}$ Available online at
    https://www.opengl.org/documentation/specs/version1.1/glspec1.1/node84.html\#SECTION00681100000000000000

[^1]:    ${ }^{1}$ Alternatively we can say that the root node is at depth 0 while a node at depth $n$ corresponds to a single pixel in the image. In this book both concepts of level and depth are used to describe the relative position of nodes. The one that is chosen is context dependent.

[^2]:    ${ }^{2}$ A problem is in NP if it can be solved nondeterministically in polynomial time. A nondeterministic solution process proceeds by 'guessing' a solution and then verifying that the solution is correct. Assume that $n$ is the size of the problem (e.g., for sorting, $n$ is the number of records to be sorted). Intuitively, then. a problem is in NP if there is a polynomial $P(n)$ such that if one guesses a solution, it can be veritied in $O(P(n))$ time, whether the guess is indeed a correct solution. Thus the verification process is the hey to determining whether a problem is in NP, not the actual solution of the problem.

    A problem is NP-complete if it is 'at least as hard' as any other problem in NP. Somewhat more formally, a problem $P_{1}$ in NP is NP-complete if the following property holds: for all other problems $P^{\circ}$, ill Nr . il $P_{1}$ can be solved deterministically in $O(f(n))$ time, then $P_{i}$ can be solved in $O(P(f(n)))$ time tor vinlle: polynomial $P$. It has been conjectured that no Np-complete problem can be solved deterministicill: "II polynomial time. but this is not known for sure. The theory of Np-completeness is discussed in detal III [Gare79].

[^3]:    ${ }^{3}$ The Gray code is motivated by a desire to reduce errors in transitions between successive gray level values. Its one bit difference guarantee is achieved by the following encoding. Consider the binary representation of the integers from 0 to $2^{m \prime}-1$. This representation can be obtained by constructing a binary tree, say $T$. of height $m$ where each left branch is labeled 0 while each right branch is labeled 1 . Each leaf node, say $P$. is given the label formed by concatenating the labels of the branches taken by the path from the root to $P$. Enumerating the leaf nodes from left to right yields the binary integers 0 to $2^{m}-1$. The Gray codes of the integers are obtained by constructing a new binary tree, say $r^{\prime}$. such that the labels of some of the branches in $T^{\prime}$ are the reverse of what they were in $T$. The algorithm is as follows. Initially, $T^{\prime}$ is a copy of $T$. Next, traverse $T$ in preorder (i.e.. visit the root node, followed by the left and right subtrees). For each branch in $T$ labeled I, exchange the labels of the two descendant branches of its corresponding branch in $T^{\prime}$. No action is taken for descendants of branches in $T$ labeled 0 . Enumerating the leaf nodes in $T^{\prime}$ from left to right yields the Gray codes of the integers 0 to $2^{m}-1$. For example, for 8 gray levels (i.e., $m=3$ ), we have 000.001, 011, 010, 110, $111.101,100$.
    ${ }^{4}$ In a one-dimensional trie structure, each data item or key is treated as a sequence of characters where each character has $M$ possible values. A node at depth $i$ in the trie represents an $M$-way branch depending on the $i^{t h}$ character. The data are stored in the leaf nodes, and the shape of the trie is independent of the order in which the data are processed. Such a structure is also known as a digital tree [Knut73b].
    ${ }^{5}$ The correspondence between coordinate values and city names is not geographically correct. This liberty has been taken so that the same example can be used throughout the text to illustrate a variety of concepts.

[^4]:    ${ }^{6}$ Refer to Figure 2.5 to see how the point quadtree is constructed in an incremental fashion for Chicago, Mobile, Toronto, and Buffalo.

[^5]:    ${ }^{7}$ The Manhattan distance between points $\left(x_{1}, y_{1}\right)$ and $\left(x_{2}, y_{2}\right)$ is $\left|x_{1}-x_{2}\right|+\left|y_{1}-y_{2}\right|$ (for more details, see Section 9.1 of [Same90b]).

[^6]:    ${ }^{8}$ Recall the statement in Section 1.2 that hierarchical data structures are often differentiated on the basis of whether they specify the boundaries of regions or organize their interiors.

[^7]:    ${ }^{9}$ A (linear) halfspace in $d$-space is defined by the inequality $\sum_{i=0}^{d} a_{i} \cdot x_{i} \geq 0$ on the $d+1$ homogeneous coordinates ( $x_{0}=1$ ). The halfspace is represented by a column vector $a$. In vector notation, the inequality is written as $a \cdot x \geq 0$. In the case of equality, it defines a hyperplane with $a$ as its normal. It is important to note that halfspaces are volume, not boundary, elements.

[^8]:    ${ }^{10}$ Of course, the storage used by runlength codes is also proportional to the perimeter of the regions. However, runlength codes do not facilitate access to different parts of the regions (i.e., they have poor spatial indexing properties).

[^9]:    ${ }^{1}$ These organizations were funded by ARPA.

[^10]:    ${ }^{2}$ These numerical values were obtained from a version of this diagram with an expanded timescale.

[^11]:    Email: hhoppe@microsoft.com
    Web: http://www.research.microsoft.com/research/graphics/hoppe/

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    © 1996 ACM-0-89791-746-4/96/008_..\$3.50

[^13]:    ${ }^{1}$ We assume in this paper that more general meshes, such as those containing $n$-sided faces and faces with holes, are first converted into triangle meshes by triangulation. The PM representation could be generalized to handle the more general meshes directly, at the expense of more complex data structures.

[^14]:    ${ }^{2}$ On average, $v_{s_{i}}$ has 6 neighbors, and the number of permutations $P_{2}^{6}=30$ can be encoded in $\left\lceil\log _{2}\left(P_{2}^{6}\right)\right\rceil=5$ bits.

[^15]:    ${ }^{3}$ The neighborhood of an edge collapse transformation is the set of faces shown in Figure 1. Using C notation, we set $\kappa=r<4 ? 10^{-2}: r<$ $8 ? 10^{-4}: 10^{-8}$ where $r$ is the ratio of the number of points to faces in the neighborhood.

[^16]:    ${ }^{4}$ We set $\left|X_{\text {disc }}\right|$ such that $\left|X_{\text {disc }}\right| /$ perim $=c(|X| / \text { area })^{\frac{1}{2}}$ where perim is the total length of all sharp edges in $\hat{M}$, area is total area of all faces, and the constant $c=4.0$ is chosen empirically.

