ELECTRONIC & ELECTRICAL ENGINEERING RESEARCH STUDIES

COMMUNICATIONS SYSTEMS, TECHNIQUES AND APPLICATIONS SERIES

Series Editor: Professor P. G. Farrell, The University of Lancaster, UK

Coding, Communications and Broadcasting focuses on research topics in three important and related areas of digital communication theory and practice. The section on coding for error control provides the latest results on turbo and low-density parity check codes, iterative and low complexity decoding, source coding and cryptography. Coverage of communications systems and techniques includes chapters on equalisation, image transmission, sequence design and synchronisation. Finally the section on digital broadcasting describes the exciting possibilities for development at transmission frequencies below 30 MHz and includes a review of current and future developments in digital video broadcasting.

This book provides revised versions of presentations made by outstanding and well-known international researchers from academia and industry at the International Symposium on Communication Theory and Applications held in July 1999.

Also in the Series:

P. Fan & M. Darnell: Sequence Design for Communications Applications

Edited by B. Honary, Communications Coding and Signal Processing, Third Volume on Communication Theory and Applications

RESEARCH STUDIES PRESS LTD.
Baldock, Hertfordshire, England



FARRELL DARNELL HONARY

oding, Communications

Stanford University Libraries
361050285132

ENCODER-

Con

TK 5103.7 .C63 2000 ENG

and Broadcastir



ELECTRONIC & ELECTRICAL ENGINEERING RESEARCH STUDIES COMMUNICATIONS SYSTEMS, TECHNIQUES AND APPLICATIONS SERIES

Series Editor:

Professor P. G. Farrell

University of Lancaster, UK

- Sequence Design for Communications Applications Pingzhi Fan and Michael Darnell
- 2. Communications Coding and Signal Processing
 THIRD VOLUME ON COMMUNICATION THEORY AND APPLICATIONS
 Edited by Bahram Honary, Michael Darnell and Paddy Farrell
- 3. Coding, Communications and Broadcasting FOURTH VOLUME ON COMMUNICATION THEORY AND APPLICATIONS Edited by Paddy Farrell, Michael Darnell and Bahram Honary

Coding, Com Broadcasting

FOURTH VOLUME THEORY AND APP

Edited by

Paddy Farrell
University of Lancaster,
Michael Darnell
University of Leeds, UK
Bahram Honary
University of Lancaster,





RESEARCH STUDIES PRESS LTD.

15/16 Coach House Cloisters, 10 Hitchin Street, Baldock, Hertfordshire, England, SG7 6AE

325 Chestnut Street, Philadelphia, PA 19106, USA

Copyright © 2000, by Research Studies Press Ltd.

No part of this book may be reproduced by any means, nor transmitted, nor translated into a machine language without the written permission of the publisher.

Marketing:

UK, EUROPE & REST OF THE WORLD

Research Studies Press Ltd.

15/16 Coach House Cloisters, 10 Hitchin Street, Baldock, Hertfordshire, England, SG7 6AE

Distribution:

NORTH AMERICA

Taylor & Francis Inc.

47 Runway Road, Suite G. Levittown, PA 19057 - 4700, USA

ASIA-PACIFIC

Hemisphere Publication Services

Golden Wheel Building, 41 Kallang Pudding Road #04-03, Singapore

UK, EUROPE & REST OF THE WORLD

John Wiley & Sons Ltd.

Shripney Road, Bognor Regis, West Sussex, England, PO22 9SA

Library of Congress Cataloging-in-Publication Data

Coding, communications, and broadcasting / edited by Paddy Farrell, Bahram Honary, and Michael Darnell.

p. cm. -- (Electronic & electrical engineering research studies. Communications

systems, techniques, and applications series; 3)

Includes bibliographical references and index.

ISBN 0-86380-259-1 (alk. paper)

1. Digital communications. 2. Coding theory. 3. Digital audio broadcasting. I. Farrell, Paddy. II. Honary, Bahram. III. Darnell, Michael. IV. Series.

TK5103.7, C63 2000

621.382--dc21

00-020868

British Library Cataloguing in Publication Data

A catalogue record for this book is available from the British Library.

ISBN 0 86380 259 1

Printed in Great Britain by SRP Ltd., Exeter

Editorial Preface

It is with great pleasure that I intro Research Studies Press on Applications. The aim of the ser featuring subjects in Communicati have interacted beneficially. The Most chapters in the three sect Communications Techniques, and bands, are concerned with topics v

of the beneficial and close synergy

This third book in the Series is a emerged from the International Applications, held regularly at a Symposium held in July 1999 achi programme, from which key prese volume, for the benefit of all those event! The Editors are to be cong material which will inform ar community. On behalf of Research possible to include this outstanding



Gallager Codes -

David J. C. MacKay (m Cavendish Laboratory, Cambri

•

Abs

In 1948, Claude Shannon posed problems of information theory. The to communicate reliably over noise He defined a theoretical limit, no to which communication is possible is not possible. Since 1948, coding error-correcting codes capable of g

In the last decade remarkable that are defined in terms of sparse coded by a simple probability-base

This paper reviews low-density repeat-accumulate codes, and turb Some previously unpublished resul experiments on Gallager codes wit rule for decoding of repeat-accum time and allows block decoding err (c) the empirical power-laws obeye codes.

1 Introduction

The central problem of communication a decoding system that make it possible channel. The encoding system uses from a set of codewords. The decode output of the channel, which codeword been transmitted; for an appropriate of codeword to the received signal. A go are well spaced apart, so that codeword to the codeword to the codeword to the received signal.

Designing a good and practical en (a) it is hard to find an explicit set of generic code, decoding, *i.e.*, finding the is intractable.

However, a simple method for desi (1962), has recently been rediscovered



fined in terms of sparse random graphs. Because the graphs are constructed randomly, the codes are likely to have well–spaced codewords. And because the codes' constraints are defined by a sparse graph, the decoding problem can be solved — almost optimally — by message–passing on the graph. The practical performance of Gallager's codes and their modern cousins is vastly better than the performance of the codes with which textbooks have been filled in the intervening years.

2 Sparse Graph Codes

In a sparse graph code, the nodes in the graph represent the transmitted bits and the constraints they satisfy. For a linear code with a codeword length N and rate R = K/N, the number of constraints is of order M = N - K. [There could be more constraints, if they happen to be redundant.] Any linear code can be described by a graph, but what makes a sparse graph code special is that each constraint involves only a small number of variables in the graph: the number of edges in the graph scales roughly linearly with N, rather than as N^2 .

The graph defining a low-density parity-check code, or Gallager code (Gallager 1962; Gallager 1963; MacKay 1999), contains two types of node: codeword bits, and parity constraints. In a regular (j,k) Gallager code (figure 1a), each codeword bit is connected to j parity constraints and each constraint is connected to k bits. The connections in the graph are made at random.

Repeat—accumulate codes (Divsalar *et al.* 1998) can be represented by a graph with four types of node (figure 1b): equality constraints __, intermediate binary variables (black circles), parity constraints __, and the transmitted bits (white circles). The encoder sets each group of intermediate bits to values read from the source. These bits are put through a fixed random permutation. The transmitted stream is the accumulated sum (modulo 2) of the permuted intermediate bits.

In a **turbo code** (Berrou and Glavieux 1996), the K source bits drive two linear feedback shift registers, which emit parity bits (figure 1c).

All these codes can be decoded by a local message–passing algorithm on the graph, the sum–product algorithm (MacKay and Neal 1996; McEliece et al. 1998), and, while this algorithm is not the optimal decoder, the empirical results are record–breaking. Figure 2 shows the performance of various sparse graph codes on a Gaussian channel. In figure 2(a) turbo codes with rate 1/4 are compared with regular and irregular Gallager codes over GF(2), GF(8) and GF(16). In figure 2(b) the performance of repeat–accumulate codes of various blocklengths and rate 1/3 is shown.

THE BEST SPARSE GRAPH CODES

Which of the three types of sparse graph code is 'best' depends on the chosen rate and blocklength, the permitted encoding and decoding complexity, and

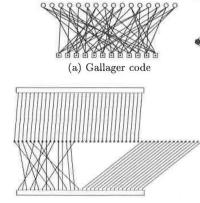


Figure 1. Graphs of three sparse graph of

(c1) Turbo code

Graphs of three sparse graph α (a) A rate 1/4 low-density blocklength N=16, and M resents a transmitted bit. Early represented by + squares. If k=4 bits to which it is connected.

(b) A repeat—accumulate of resents a transmitted bit. Each binary variable. Each connected to be equal.

(c) A turbo code with rate word bits. The two rectangle (c2), with the systematic bits angle and the parity bits $\{t^{(b)}\}$

140

DOCKET

Explore Litigation Insights



Docket Alarm provides insights to develop a more informed litigation strategy and the peace of mind of knowing you're on top of things.

Real-Time Litigation Alerts



Keep your litigation team up-to-date with **real-time** alerts and advanced team management tools built for the enterprise, all while greatly reducing PACER spend.

Our comprehensive service means we can handle Federal, State, and Administrative courts across the country.

Advanced Docket Research



With over 230 million records, Docket Alarm's cloud-native docket research platform finds what other services can't. Coverage includes Federal, State, plus PTAB, TTAB, ITC and NLRB decisions, all in one place.

Identify arguments that have been successful in the past with full text, pinpoint searching. Link to case law cited within any court document via Fastcase.

Analytics At Your Fingertips



Learn what happened the last time a particular judge, opposing counsel or company faced cases similar to yours.

Advanced out-of-the-box PTAB and TTAB analytics are always at your fingertips.

API

Docket Alarm offers a powerful API (application programming interface) to developers that want to integrate case filings into their apps.

LAW FIRMS

Build custom dashboards for your attorneys and clients with live data direct from the court.

Automate many repetitive legal tasks like conflict checks, document management, and marketing.

FINANCIAL INSTITUTIONS

Litigation and bankruptcy checks for companies and debtors.

E-DISCOVERY AND LEGAL VENDORS

Sync your system to PACER to automate legal marketing.

