

(12) United States Patent Kamvar et al.

### (54) ADAPTIVE COMPUTATION OF RANKING

- (75) Inventors: Sepandar D. Kamvar, Palo Alto, CA (US); Taher H. Haveliwala, Mountain View, CA (US); Gene H. Golub, Stanford, CA (US)
- (73) Assignee: Google Inc., Mountain View, CA (US)
- (\*) Notice: Subject to any disclaimer, the term of this patent is extended or adjusted under 35 U.S.C. 154(b) by 0 days.
- (21) Appl. No.: 10/925,189
- (22) Filed: Aug. 23, 2004

### (65) Prior Publication Data

US 2005/0027685 A1 Feb. 3, 2005

### **Related U.S. Application Data**

- (63) Continuation-in-part of application No. 10/646,331, filed on Aug. 22, 2003.
- (60) Provisional application No. 60/458,921, filed on Mar. 28, 2003.
- (51) Int. Cl.

DOCKF

- G06F 17/30 (2006.01)
- (52)
   U.S. Cl.
   707/5; 3/7; 715/501.1

   (58)
   Field of Classification Search
   707/3, 707/100, 5, 101, 10; 706/15; 715/500
- 707/100, 5, 101, 10; 706/15; 715/500 See application file for complete search history.

### (56) References Cited

### U.S. PATENT DOCUMENTS

 6,112,202
 A
 8/2000
 Kleinberg

 6,285,999
 B1\*
 9/2001
 Page
 707/5



6,560,600 B1*	5/2003	Broder 707/7
6,584,468 B1*	6/2003	Gabriel et al 707/10
6,799,176 B1*	9/2004	Page 707/5
6,871,202 B1*	3/2005	Broder 707/7
003/0204502 A1*	10/2003	Tomlin et al 707/5
003/0208478 A1*	11/2003	Harvey 707/3
003/0208482 A1*	11/2003	Kim et al 707/3
004/0024752 A1*	2/2004	Manber et al 707/3
2004/0111412 A1*	6/2004	Broder 707/7

### OTHER PUBLICATIONS

Arasu, A., et al., "PageRank Computation and the Structure of the Web: Experiments and Algorithms," *Proceedings of the 11th Int'l World Wide Web Conf., Poster Track*, 2002. Bharat, K., et al., "Improved Algorithms for Topic Distillation in a Hyperlinked Environment," *Proceedings of the ACM-SIGIR*, 1998.

#### (Continued)

Primary Examiner—Jean M. Corrielus (74) Attorney, Agent, or Firm—Morgan, Lewis & Bockius LLP

### (57) ABSTRACT

A system and method is disclosed in which a ranking function for a set of document rank values is iteratively solved with respect to a set of linked documents until a first stability condition is satisfied. After such condition is satisfied, some of the ranks will have converged. The ranking function is modified to take into account these converged ranks so as to reduce the ranking function's computation cost. The modified ranking function is then solved until a second stability condition is satisfied. After such condition is satisfied more of the ranks will have converged. The ranking function is again modified and process continues until complete.

### 31 Claims, 5 Drawing Sheets



EXHIBIT 2104 Facebook, Inc. et al. v. Software Rights Archive, LLC

Find authenticated court documents without watermarks at docketalarm.com.

### OTHER PUBLICATIONS

Haveliwala, T., "Efficient Computation of PageRank," Stanford University Technical Report, 1999.

Haveliwala, T., "Topic Sensitive PageRank," Proceedings of the 11th Int'l World Wide Web Conf., 2002.

Haveliwala, T., et al., "The Second Eigenvalue of the Google Matrix," *Stanford University Technical Report*, 2003.

Jeh, G., et al., "Scaling Personalized Web Search," Proceedings of the 12th Int'l World Wide Web Conf., 2003. Kamvar, S., et al., "Exploiting the Block Structure of the Web for Computing PageRank," *Stanford University Technical Report*, 1999.

Kamvar, S., et al., "Extrapolation Methods for Accelerating PageRank Computations," *Proceedings of the 12th Int'l World Wide Web Conf.*, 2003.

Page, L., et al., "The PageRank Citation Ranking: Bringing Order to the Web," *Stanford Digital Libraries Working Paper*, 1998.

\* cited by examiner

Α

R

M

Δ



Find authenticated court documents without watermarks at docketalarm.com.

Δ



Fig. 2

**OCKET LARM** Find authenticated court documents without watermarks at <u>docketalarm.com</u>.



Fig. 3

# DOCKET



## Explore Litigation Insights

Docket Alarm provides insights to develop a more informed litigation strategy and the peace of mind of knowing you're on top of things.

## **Real-Time Litigation Alerts**



Keep your litigation team up-to-date with **real-time** alerts and advanced team management tools built for the enterprise, all while greatly reducing PACER spend.

Our comprehensive service means we can handle Federal, State, and Administrative courts across the country.

## **Advanced Docket Research**



With over 230 million records, Docket Alarm's cloud-native docket research platform finds what other services can't. Coverage includes Federal, State, plus PTAB, TTAB, ITC and NLRB decisions, all in one place.

Identify arguments that have been successful in the past with full text, pinpoint searching. Link to case law cited within any court document via Fastcase.

## **Analytics At Your Fingertips**



Learn what happened the last time a particular judge, opposing counsel or company faced cases similar to yours.

Advanced out-of-the-box PTAB and TTAB analytics are always at your fingertips.

## API

Docket Alarm offers a powerful API (application programming interface) to developers that want to integrate case filings into their apps.

### LAW FIRMS

Build custom dashboards for your attorneys and clients with live data direct from the court.

Automate many repetitive legal tasks like conflict checks, document management, and marketing.

## **FINANCIAL INSTITUTIONS**

Litigation and bankruptcy checks for companies and debtors.

## **E-DISCOVERY AND LEGAL VENDORS**

Sync your system to PACER to automate legal marketing.

