

Google's PageRank and Beyond: The Science of Search Engine Rankings

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Google's PageRank and Beyond: The Science of Search Engine Rankings

Amy N. Langville and Carl D. Meyer

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