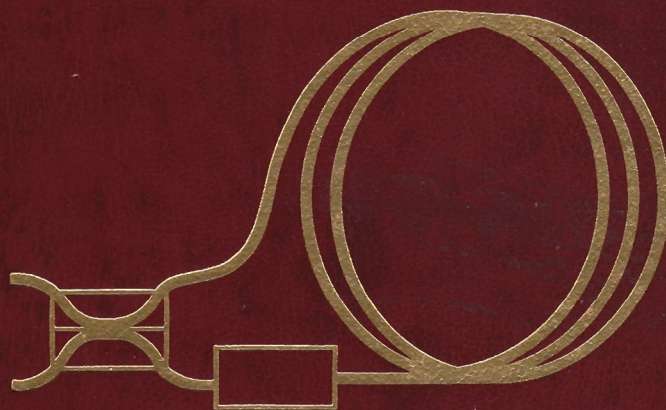


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# *Guided-Wave Photonics*



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**BUCKMAN**

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such as the one shown in Figure 1.2. This allows a degree of parallel processing that is exploited in each of the devices described below.

### 7.3.2 Guided-Wave Real-Time Spectrum Analyzer (13)

With electronic computation, obtaining the power spectrum of a received signal requires sampling a large number of points and then calculating a different integral for each frequency at which a value for the power spectrum is desired. Since each calculation occurs in sequence in a conventional electronic computer, the entire spectrum of a wideband signal takes a long time to generate. The device shown in Figure 7.13 generates the power spectrum much faster. Light from a CW laser is butt-coupled into the slab waveguide, before entering the two-dimensional lens, L1, which collimates the guided wave into a "beam" in the slab, with a width  $W$ . This beam interacts with the surface acoustic wave produced at the transducer. The geometry of this interaction is the same as that in Figure 7.10(a). Neglecting any Doppler shift in the light frequency in Equation (7-71) requires that

$$\omega_i = \omega_D \tag{7-76}$$

which means that the incident and diffracted modes will differ only in direction and not in propagation constant, or

$$|\beta_i| = |\beta_D| \tag{7-77}$$

in Equation (7-70). The vector momentum conservation diagram in Figure 7.10(b) is thus an isosceles triangle, with the diffraction angle  $\theta$  given by

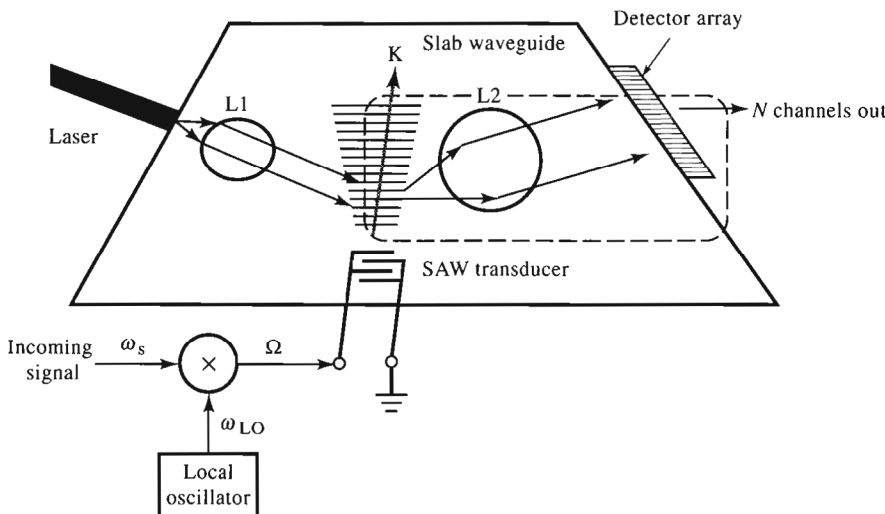


Figure 7.13 Schematic of a guided-wave real time spectrum analyzer.

In view of Equation (7-78). The surface acoustic frequency

which is just the general wave. Solving Equation (7-78) produces the angle

Before being applied is mixed with a signal that the SAW frequency

Actually, the incoming yielding diffracted gr lens, L2, collimates detector in the array signal component a calculated by substituting guided mode power the corresponding a the array that is produced centered at  $\omega_s$ .

To see this more Figure 7.13, magnifying incoming signal beam angle  $\theta_c$  shown in Figure from the interaction at one detector of width  $L$

Differentiating Equation gives

$$\theta = \sin^{-1} \left[ \frac{|\mathbf{K}|}{2|\beta|} \right] \quad (7-78)$$

In view of Equation (7-77), the *i* and *D* subscripts have been dropped in Equation (7-78). The surface acoustic wave propagation velocity is constant over a wide acoustic frequency range, and obeys the relation

$$v_{\text{SAW}} = \frac{\Omega}{|\mathbf{K}|} \quad (7-79)$$

which is just the general wave property (Eq. 1-11), written for the surface acoustic wave. Solving Equation (7-79) for  $|\mathbf{K}|$  and substituting the result into Equation (7-78) produces the desired relation between acoustic frequency and diffraction angle

$$\theta = \sin^{-1} \left[ \frac{\Omega}{2v_{\text{SAW}} |\beta|} \right] \quad (7-80)$$

Before being applied to the SAW transducer in Figure 7.12, the incoming signal is mixed with a single-frequency sinusoid at  $\omega_{\text{LO}}$  from the local oscillator, so that the SAW frequency is related to the incoming signal frequency,  $\omega_s$ , by

$$\Omega = \omega_{\text{LO}} + \omega_s \quad (7-81)$$

Actually, the incoming signal consists of multiple components at different  $\omega_s$ , yielding diffracted guided modes at multiple values of  $\theta$ . The second waveguide lens, L2, collimates light diffracted into a particular direction onto a particular detector in the array at the right side of the slab waveguide in Figure 7.13. Each signal component at a different  $\omega_s$  corresponds to a different diffraction angle calculated by substituting Equation (7-81) into Equation (7-80). Assuming the guided mode power diffracted into any  $\theta$  is proportional to the signal power at the corresponding  $\omega_s$ , this device yields a set of currents from each detector in the array that is proportional to the signal power in a narrow frequency band centered at  $\omega_s$ .

To see this more clearly, consider the region enclosed by the dashed line in Figure 7.13, magnified to yield Figure 7.14. Let the center frequency of the incoming signal be  $\omega_c$ , and the diffraction angle corresponding to  $\omega_c$  be the angle  $\theta_c$  shown in Figure 7.14. If the lens L2 is situated a focal length,  $f$ , away from the interaction region, all diffracted energy in the angular range  $\Delta\theta$  arrives at one detector of width  $L$ . For small  $\theta_1$ , the range of angles incident on a single detector of width  $L$  is given by

$$\Delta\theta = \frac{L}{f} \quad (7-82)$$

Differentiating Equation (7-80) with respect to  $\Omega$ , and using Equation (7-81) gives

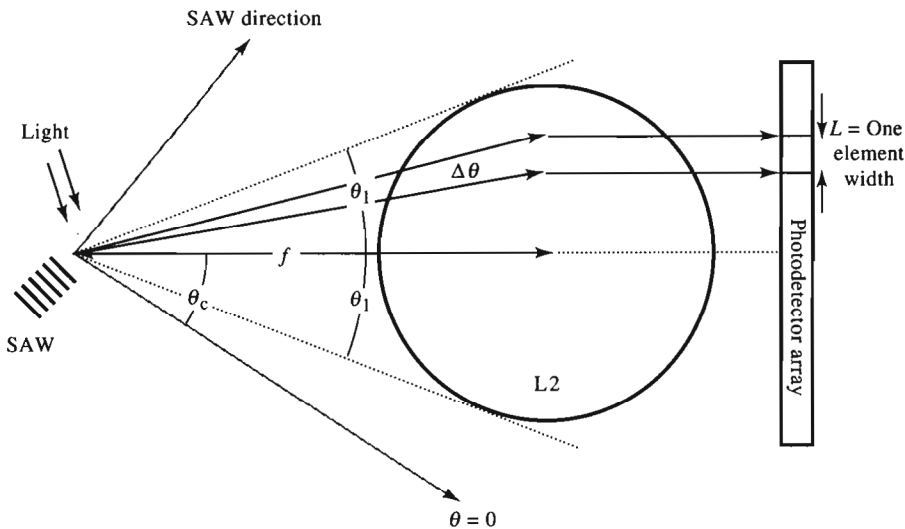


Figure 7.14 Diffraction and focusing on the detector array in the guided-wave real time spectrum analyzer.

$$\frac{d\theta}{d\Omega} = \frac{d\theta}{d\omega_s} = \frac{1}{2v_{SAW} |\beta|} \left\{ 1 - \left[ \frac{\omega_{LO} + \omega_s}{2v_{SAW} |\beta|} \right]^2 \right\}^{-1/2} \quad (7-83)$$

Solving Equation (7-83) for  $d\omega_s$  and substituting Equation (7-82) for  $\Delta\theta$  gives the channel bandwidth associated with each detector in the array as

$$d\omega_s = 2v_{SAW} |\beta| \left\{ 1 - \left[ \frac{\omega_{LO} + \omega_s}{2v_{SAW} |\beta|} \right]^2 \right\}^{1/2} \frac{L}{f} \quad (7-84)$$

If the array contains  $N$  detectors, the device in Figure 7.13 computes a power spectrum of the incoming signal over the range of  $\omega_s$  corresponding to the range of diffracted angles

$$\theta_c - \theta_1 < \theta < \theta_c + \theta_1 \quad (7-85)$$

with  $N$ -point resolution along the frequency axis. This power spectrum is computed in the time it takes for the light in the waveguide to propagate from the laser to the detector array. Conventional methods for computing a power spectrum require many successive summations and/or integrations, each of which can involve considerable computation time.

### 7.3.3 The Integrated Optic Spatial Light Modulator (IOSLM)

Like the real-time spectrum analyzer, the integrated optic spatial light modulator (abbreviated IOSLM) operates on the principle of diffraction of a guided mode

by a controllable grating. In the structure like the one shown in Figure 7.15, the grating is a linear array of gratings. The grating period, in the IOSLM is the same as the grating period in Figure 7.15. In the guided mode waveguide, the light is

Each cell of the array is modeled in Section 7.3.1. The electro-optic modulator is assembled into an array. The output of each cell must be controlled from that cell do not

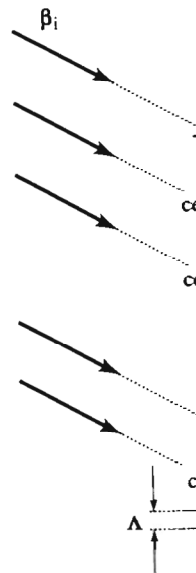
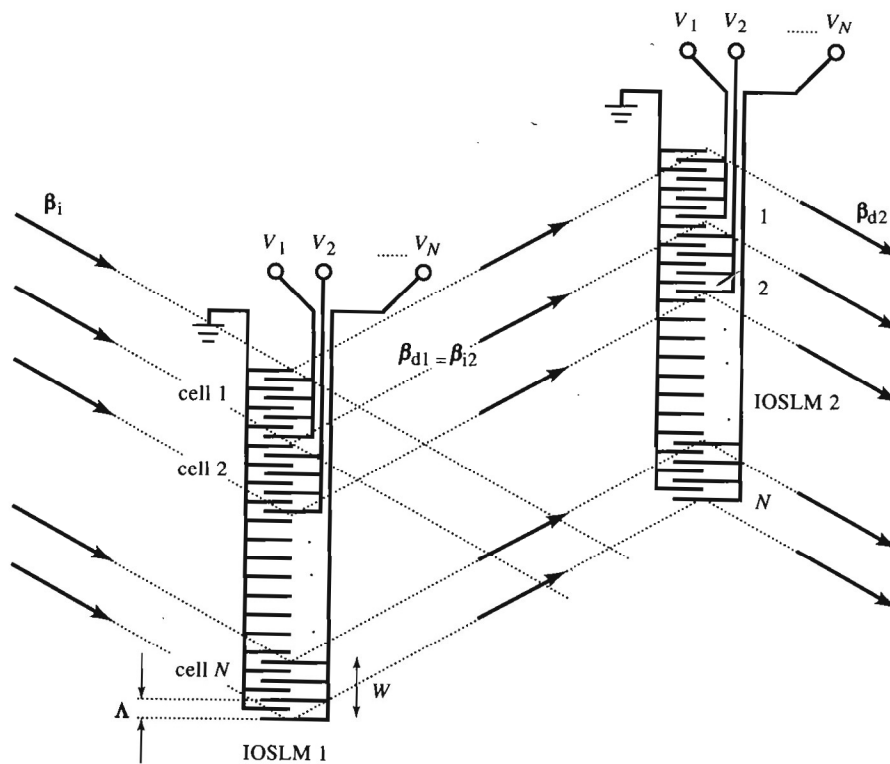


Figure 7.15 Geometry of the IOSLM devices are shown in the second.

by a controllable grating structure formed in a slab waveguide in response to an electrical signal. Instead of a surface acoustic wave, an interdigital electrode structure like the one in Figure 7.9 forms the grating in the IOSLM, by means of the electro-optic effect described in Section 7.2.1. The IOSLM consists of a linear array of grating modulators based on Figure 7.9 with a geometry shown in Figure 7.15. The angle of diffraction is not adjustable in the IOSLM, since the grating period,  $\Lambda$ , is fixed when the device is fabricated. However, each cell in the IOSLM is individually addressable using the appropriate drive line in Figure 7.15. In this way, the intensity in each section of the broad, incident guided mode wavefront is modulated individually.

Each cell of the IOSLM is an electro-optic Bragg modulator like the one modeled in Section 7.2.1 and can be evaluated using the criteria developed for electro-optic modulators earlier in this chapter. When an array of such cells is assembled into an IOSLM, some additional constraints apply. The width,  $W$ , of each cell must be large enough so that the transmitted and diffracted beams from that cell do not spread out appreciably from diffraction over the propagation



**Figure 7.15** Geometry for an integrated optic spatial light modulator (IOSLM). Two devices are shown, with the diffracted output from the first serving as the input for the second.

instances to the next elements (detectors or other devices) in the system. Thus  $W$  should be much larger than the wavelength of the guided mode in the slab.

Two or more IOSLMs placed in optical series with each other, as shown in Figure 7.15, are capable of a number of computational functions. For example, suppose that no light is diffracted by a cell with no applied voltage and that, at an applied voltage  $V_{max}$ , the cell diffracts essentially all of the guided mode incident on it. Some diffraction is present for all applied cell voltages in the range

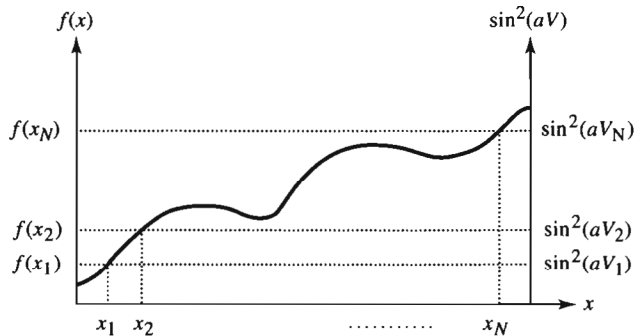
$$0 < V_c < V_{max} \tag{7-86}$$

Let the cell voltages in modulator 1 in Figure 7.15 be chosen to represent  $N$  sampled values of a function  $f(x)$ , as represented in Figure 7.16. Since the diffracted power from any cell is always positive,  $f(x)$  must be restricted to positive values only. For scaling purposes, let the maximum value of  $f(x)$  be one. As pointed out in Section 7.2.1, the diffracted intensity is not linear with  $V_c$ , but instead proportional to  $\sin^2(aV_c)$ , where  $a$  is a constant dependent on electrode geometry and waveguide properties. Therefore, the diffracted power from each cell will be linear with  $f(x)$  if the voltage corresponding to the value of  $f$  is

$$V = \frac{1}{a} \sin^{-1} f \tag{7-87}$$

Returning again to Figure 7.15, suppose that a second function  $g(x)$  is sampled using the same procedure employed with  $f(x)$  and the resulting voltages placed on the cells of the second IOSLM. From Figure 7.15, the diffracted output from the  $M$ th cell of the second IOSLM is clearly the product of  $f(M)g(M)$ . Thus, the intensity profile of the diffracted output of the second IOSLM is a sampled product of  $f(x)g(x)$ .

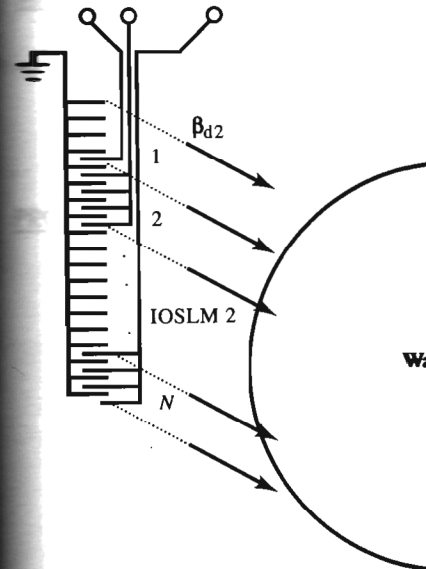
The device in Figure 7.15 extracts an analog product of two positive functions very rapidly by operating on all the samples simultaneously. As such, it is another



**Figure 7.16** Representing the sampled values of a positive function  $f(x)$  by a series of voltage levels.

example of the capability of IOSLMs. Since the sampled values of  $f(x)$  are represented by voltage levels, the IOSLM can be electronically used to perform operations on these values. For example, in Figure 7.15, a shift of  $f(x)$  by  $+P$  cells just means that in cell  $M$ . In convolution, the output of the IOSLM is integrated over the domain of  $f(x)$ . The integration of the IOSLM outputs is readily performed in Figure 7.17. The lens performs the integration from all cells of the IOSLM to produce the output  $h(x)$ , the integration is equal to

where  $N$  is the number of cells. In the IOSLM mode, the voltage levels. The values of  $f(x)$  of zero or one are operations on the zeroes of  $f(x)$  in Figure 7.16, in parallel.



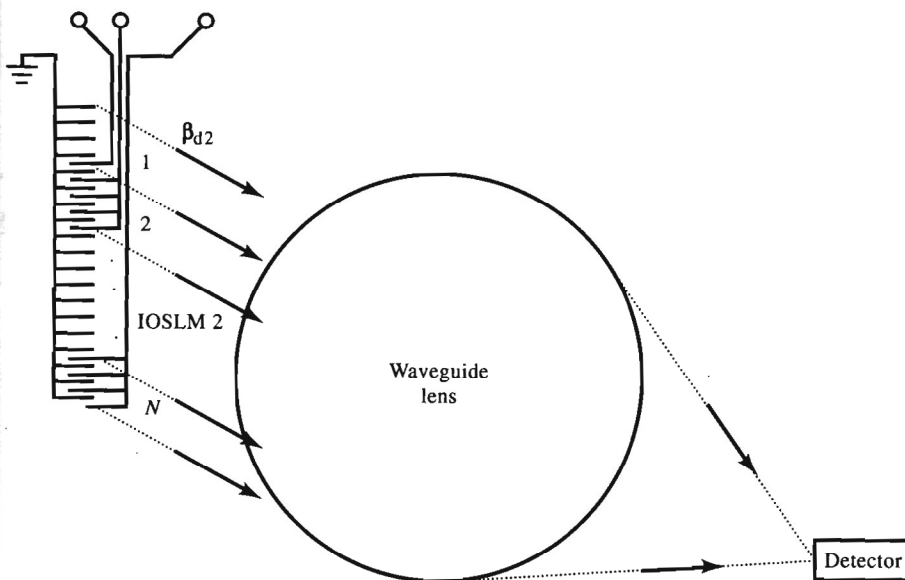
**Figure 7.17** Integration across the front detector.

example of the capability optical devices have for parallel computational operations. Since the sampled values of  $f(x)$  and  $g(x)$  can be shifted across each IOSLM electronically using shift registers, operations requiring multiplication of shifted functions, such as correlation and convolution, are also possible. In Figure 7.15, a shift would just reassign cell values so that, for example, a shift of  $f(x)$  by  $+P$  cells just means that the value of  $V_c$  in cell  $M + P$  is replaced by that in cell  $M$ . In convolution and correlation, the product of two shifted functions is integrated over the domain,  $x$ , of the functions of interest. This integration of IOSLM outputs is readily accomplished with a guided-wave lens, as shown in Figure 7.17. The lens performs the integration in Figure 7.17 by converging light from all cells of the IOSLM onto a single detector. For a sampled function,  $h(x)$ , the integration is equivalent to summing the outputs from all cells, or

$$\int h(x) dx = \sum_{q=1}^N h_q \quad (7-88)$$

where  $N$  is the number of samples or cells.

In the IOSLM model developed above, the  $V_c$  are assumed to be analog voltage levels. The values of  $V_c$  can also be restricted to correspond with values for  $f(x)$  of zero or one only. In this case, the IOSLM performs bit-level logic operations on the zeroes or ones in each corresponding cell of the two IOSLMs in Figure 7.16, in parallel. For example, the diffracted output of the second



**Figure 7.17** Integration across the front of an IOSLM using a lens and a single detector.



IOSLM is the result of a bit-by-bit logical AND of the strings of zeros and ones in the two IOSLMs.

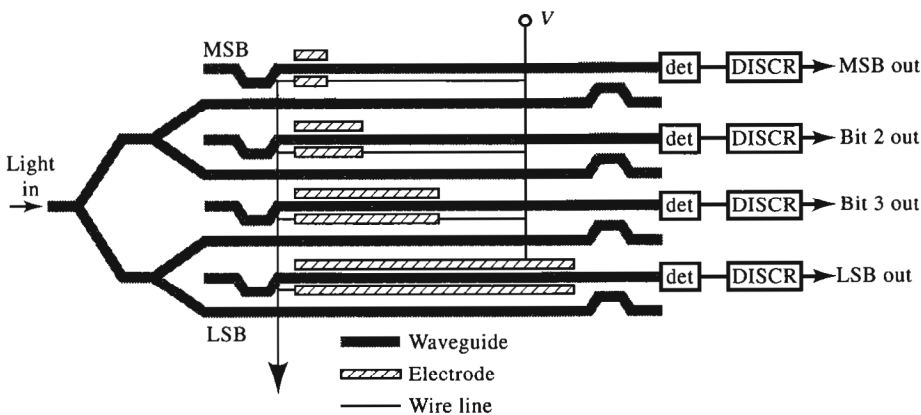
**7.3.4 Analog-to-Digital Conversion with Guided-Wave Optics (14)**

The final example of guided-wave information subsystems that exploit the inherent parallelism of optical processing is the analog-to-digital converter. In conceptual similarity to the IOSLM in the preceding section will be immediately apparent. The analog-to-digital converter described here is a parallel arrangement of electro-optic switches similar to the one in Figure 7.6. Each switch corresponds to one bit of precision in the A-to-D conversion. The analog voltage to be converted is applied simultaneously to all electro-optic switches in the converter. An example with four-bit precision is shown in Figure 7.18. The electrode length for the most-significant bit (MSB) is chosen such that the maximum voltage to be converted can cause a  $\pi$  phase shift in the switch for that bit. Moving down the structure of Figure 7.18, the electrode length doubles with each decrease in bit significance so that, for the 4-bit example shown, the electrode length of the least significant bit (LSB) is eight times that of the MSB. The discriminators (DISCR) that follow the detectors convert all detector outputs to discriminator outputs,  $V_D$ , which are logical zeros or ones according to the following rule:

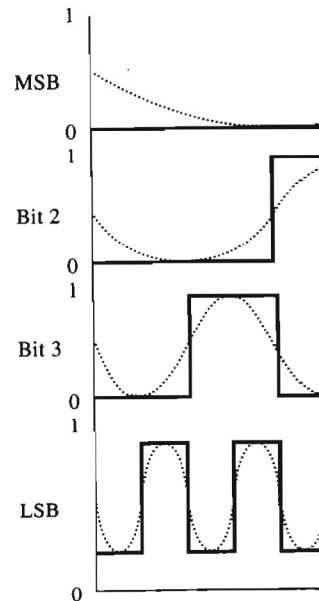
$$V_D = \begin{cases} 0 & ; \text{if } 0 < P < P_{\max}/2 \\ 1 & ; \text{if } P_{\max}/2 < P_{\max} \end{cases} \quad (7-89)$$

where  $P$  is the optical power incident on a detector and  $P_{\max}$  is the maximum optical power that can be transmitted through the switch.

Figure 7.19 illustrates the operation of the device in Figure 7.18 as an analog-



**Figure 7.18** A 4-bit guided-wave optical analog to digital converter based on four parallel Mach-Zehnder electro-optic switches.



**Figure 7.19** The optical transmission for each bit channel of the A-to-D converter.

to-digital converter, assuming the presence of discriminators. The optical transmission curve, while the corresponding discriminator outputs.

The speed of this A-to-D converter is extremely fast because the electro-optic switches are extremely fast.

**PROBLEMS**

7-1 A certain electro-optic waveguide is capable of a phase shift of  $10^{-4}$  when the maximum effective index is 3.4. The channel waveguide is on a substrate with an index of refraction of 1.5.

- a. A Mach-Zehnder interferometer is constructed using this waveguide. The phase difference between the two arms is  $10^{-4}$ .
- b. A coupler switch is constructed using this waveguide. The phase difference between the two arms is  $10^{-4}$ .

Use the analysis of the Mach-Zehnder interferometer. One waveguide has a length of  $10^4$  cm.