

# A Method for Obtaining Digital Signatures and Public- Key Cryptosystems

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**An encryption method is presented with the novel property that publicly revealing an encryption key does not thereby reveal the corresponding decryption key. This has two important consequences:**

- (1) Couriers or other secure means are not needed to transmit keys, since a message can be enciphered using an encryption key publicly revealed by the intended recipient. Only he can decipher the message, since only he knows the corresponding decryption key.**
- (2) A message can be "signed" using a privately held decryption key. Anyone can verify this signature using the corresponding publicly revealed encryption key. Signatures cannot be forged, and a signer cannot later deny the validity of his signature. This has obvious applications in "electronic mail" and "electronic funds transfer" systems. A message is encrypted by representing it as a number  $M$ , raising  $M$  to a publicly specified power  $e$ , and then taking the remainder when the result is divided by the publicly specified product,  $n$ , of two large secret prime numbers  $p$  and  $q$ . Decryption is similar; only a different, secret, power  $d$  is used, where  $e * d \equiv 1 \pmod{(p - 1) * (q - 1)}$ . The security of the system rests in part on the difficulty of factoring the published divisor,  $n$ .**

**Key Words and Phrases:** digital signatures, public-key cryptosystems, privacy, authentication, security, factorization, prime number, electronic mail, message-passing, electronic funds transfer, cryptography.

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## I. Introduction

The era of "electronic mail" [10] may soon be upon us; we must ensure that two important properties of the current "paper mail" system are preserved: (a) messages are *private*, and (b) messages can be *signed*. We demonstrate in this paper how to build these capabilities into an electronic mail system.

At the heart of our proposal is a new encryption method. This method provides an implementation of a "public-key cryptosystem", an elegant concept invented by Diffie and Hellman [1]. Their article motivated our research, since they presented the concept but not any practical implementation of such a system. Readers familiar with [1] may wish to skip directly to Section V for a description of our method.

## II. Public-Key Cryptosystems

In a "public-key cryptosystem" each user places in a public file an encryption procedure  $E$ . That is, the public file is a directory giving the encryption procedure of each user. The user keeps secret the details of his corresponding decryption procedure  $D$ . These procedures have the following four properties:

- (a) Deciphering the enciphered form of a message  $M$  yields  $M$ . Formally,

$$D(E(M)) = M. \quad (1)$$

- (b) Both  $E$  and  $D$  are easy to compute.
- (c) By publicly revealing  $E$  the user does not reveal an easy way to compute  $D$ . This means that in practice only he can decrypt messages encrypted with  $E$ , or compute  $D$  efficiently.
- (d) If a message  $M$  is first deciphered and then enciphered,  $M$  is the result. Formally,

$$E(D(M)) = M. \quad (2)$$

An encryption (or decryption) procedure typically consists of a *general method* and an *encryption key*. The general method, under control of the key, enciphers a message  $M$  to obtain the enciphered form of the message, called the *ciphertext*  $C$ . Everyone can use the same general method; the security of a given procedure will rest on the security of the key. Revealing an encryption algorithm then means revealing the key.

When the user reveals  $E$  he reveals a very *inefficient* method of computing  $D(C)$ : testing all possible messages  $M$  until one such that  $E(M) = C$  is found. If property (c) is satisfied the number of such messages to test will be so large that this approach is impractical.

A function  $E$  satisfying (a)–(c) is a "trap-door one-way function;" if it also satisfies (d) it is a "trap-door one-way permutation." Diffie and Hellman [1] introduced the concept of trap-door one-way functions but

did not present any examples. These functions are called “one-way” because they are easy to compute in one direction but (apparently) very difficult to compute in the other direction. They are called “trap-door” functions since the inverse functions are in fact easy to compute once certain private “trap-door” information is known. A trap-door one-way function which also satisfies (d) must be a permutation: every message is the ciphertext for some other message and every ciphertext is itself a permissible message. (The mapping is “one-to-one” and “onto”). Property (d) is needed only to implement “signatures”.

The reader is encouraged to read Diffie and Hellman’s excellent article [1] for further background, for elaboration of the concept of a public-key cryptosystem, and for a discussion of other problems in the area of cryptography. The ways in which a public-key cryptosystem can ensure privacy and enable “signatures” (described in Sections III and IV below) are also due to Diffie and Hellman.

For our scenarios we suppose that A and B (also known as Alice and Bob) are two users of a public-key cryptosystem. We will distinguish their encryption and decryption procedures with subscripts:  $E_A$ ,  $D_A$ ,  $E_B$ ,  $D_B$ .

### III. Privacy

Encryption is the standard means of rendering a communication private. The sender enciphers each message before transmitting it to the receiver. The receiver (but no unauthorized person) knows the appropriate deciphering function to apply to the received message to obtain the original message. An eavesdropper who hears the transmitted message hears only “garbage” (the ciphertext) which makes no sense to him since he does not know how to decrypt it.

The large volume of personal and sensitive information currently held in computerized data banks and transmitted over telephone lines makes encryption increasingly important. In recognition of the fact that efficient, high-quality encryption techniques are very much needed but are in short supply, the National Bureau of Standards has recently adopted a “Data Encryption Standard” [13, 14], developed at IBM. The new standard does not have property (c), needed to implement a public-key cryptosystem.

All classical encryption methods (including the NBS standard) suffer from the “key distribution problem.” The problem is that before a private communication can begin, *another* private transaction is necessary to distribute corresponding encryption and decryption keys to the sender and receiver, respectively. Typically a private courier is used to carry a key from the sender to the receiver. Such a practice is not feasible if an electronic mail system is to be rapid and inexpensive. A public-key cryptosystem needs no private couriers; the keys can be distributed over the insecure communications channel.

How can Bob send a private message  $M$  to Alice in

a public-key cryptosystem? First, he retrieves  $E_A$  from the public file. Then he sends her the enciphered message  $E_A(M)$ . Alice decipheres the message by computing  $D_A(E_A(M)) = M$ . By property (c) of the public-key cryptosystem only she can decipher  $E_A(M)$ . She can encipher a private response with  $E_B$ , also available in the public file.

Observe that no private transactions between Alice and Bob are needed to establish private communication. The only “setup” required is that each user who wishes to receive private communications must place his enciphering algorithm in the public file.

Two users can also establish private communication over an insecure communications channel without consulting a public file. Each user sends his encryption key to the other. Afterwards all messages are enciphered with the encryption key of the recipient, as in the public-key system. An intruder listening in on the channel cannot decipher any messages, since it is not possible to derive the decryption keys from the encryption keys. (We assume that the intruder cannot modify or insert messages into the channel.) Ralph Merkle has developed another solution [5] to this problem.

A public-key cryptosystem can be used to “bootstrap” into a standard encryption scheme such as the NBS method. Once secure communications have been established, the first message transmitted can be a key to use in the NBS scheme to encode all following messages. This may be desirable if encryption with our method is slower than with the standard scheme. (The NBS scheme is probably somewhat faster if special-purpose hardware encryption devices are used; our scheme may be faster on a general-purpose computer since multiprecision arithmetic operations are simpler to implement than complicated bit manipulations.)

### IV. Signatures

If electronic mail systems are to replace the existing paper mail system for business transactions, “signing” an electronic message must be possible. The recipient of a signed message has proof that the message originated from the sender. This quality is stronger than mere authentication (where the recipient can verify that the message came from the sender); the recipient can convince a “judge” that the signer sent the message. To do so, he must convince the judge that he did not forge the signed message himself! In an authentication problem the recipient does not worry about this possibility, since he only wants to satisfy *himself* that the message came from the sender.

An electronic signature must be *message-dependent*, as well as *signer-dependent*. Otherwise the recipient could modify the message before showing the message-signature pair to a judge. Or he could attach the signature to any message whatsoever, since it is impossible to detect electronic “cutting and pasting.”

To implement signatures the public-key cryptosys-

tem must be implemented with trap-door one-way permutations (i.e. have property (d)), since the decryption algorithm will be applied to unenciphered messages.

How can user Bob send Alice a “signed” message  $M$  in a public-key cryptosystem? He first computes his “signature”  $S$  for the message  $M$  using  $D_B$ :

$$S = D_B(M).$$

(Deciphering an unenciphered message “makes sense” by property (d) of a public key cryptosystem: each message is the ciphertext for some other message.) He then encrypts  $S$  using  $E_A$  (for privacy), and sends the result  $E_A(S)$  to Alice. He need not send  $M$  as well; it can be computed from  $S$ .

Alice first decrypts the ciphertext with  $D_A$  to obtain  $S$ . She knows who is the presumed sender of the signature (in this case, Bob); this can be given if necessary in plain text attached to  $S$ . She then extracts the message with the encryption procedure of the sender, in this case  $E_B$  (available on the public file):

$$M = E_B(S).$$

She now possesses a message-signature pair  $(M, S)$  with properties similar to those of a signed paper document.

Bob cannot later deny having sent Alice this message, since no one else could have created  $S = D_B(M)$ . Alice can convince a “judge” that  $E_B(S) = M$ , so she has proof that Bob signed the document.

Clearly Alice cannot modify  $M$  to a different version  $M'$ , since then she would have to create the corresponding signature  $S' = D_B(M')$  as well.

Therefore Alice has received a message “signed” by Bob, which she can “prove” that he sent, but which she cannot modify. (Nor can she forge his signature for any other message.)

An electronic checking system could be based on a signature system such as the above. It is easy to imagine an encryption device in your home terminal allowing you to sign checks that get sent by electronic mail to the payee. It would only be necessary to include a unique check number in each check so that even if the payee copies the check the bank will only honor the first version it sees.

Another possibility arises if encryption devices can be made fast enough: it will be possible to have a telephone conversation in which every word spoken is signed by the encryption device before transmission.

When encryption is used for signatures as above, it is important that the encryption device not be “wired in” between the terminal (or computer) and the communications channel, since a message may have to be successively enciphered with several keys. It is perhaps more natural to view the encryption device as a “hardware subroutine” that can be executed as needed.

We have assumed above that each user can always access the public file reliably. In a “computer network” this might be difficult; an “intruder” might forge

messages purporting to be from the public file. The user would like to be sure that he actually obtains the encryption procedure of his desired correspondent and not, say, the encryption procedure of the intruder. This danger disappears if the public file “signs” each message it sends to a user. The user can check the signature with the public file’s encryption algorithm  $E_{PF}$ . The problem of “looking up”  $E_{PF}$  itself in the public file is avoided by giving each user a description of  $E_{PF}$  when he first shows up (in person) to join the public-key cryptosystem and to deposit his public encryption procedure. He then stores this description rather than ever looking it up again. The need for a courier between every pair of users has thus been replaced by the requirement for a single secure meeting between each user and the public-file manager when the user joins the system. Another solution is to give each user, when he signs up, a book (like a telephone directory) containing all the encryption keys of users in the system.

## V. Our Encryption and Decryption Methods

To encrypt a message  $M$  with our method, using a public encryption key  $(e, n)$ , proceed as follows. (Here  $e$  and  $n$  are a pair of positive integers.)

First, represent the message as an integer between 0 and  $n - 1$ . (Break a long message into a series of blocks, and represent each block as such an integer.) Use any standard representation. The purpose here is not to encrypt the message but only to get it into the numeric form necessary for encryption.

Then, encrypt the message by raising it to the  $e$ th power modulo  $n$ . That is, the result (the ciphertext  $C$ ) is the remainder when  $M^e$  is divided by  $n$ .

To decrypt the ciphertext, raise it to another power  $d$ , again modulo  $n$ . The encryption and decryption algorithms  $E$  and  $D$  are thus:

$$C \equiv E(M) \equiv M^e \pmod{n}, \text{ for a message } M.$$

$$D(C) \equiv C^d \pmod{n}, \text{ for a ciphertext } C.$$

Note that encryption does not increase the size of a message; both the message and the ciphertext are integers in the range 0 to  $n - 1$ .

The *encryption key* is thus the pair of positive integers  $(e, n)$ . Similarly, the *decryption key* is the pair of positive integers  $(d, n)$ . Each user makes his encryption key public, and keeps the corresponding decryption key private. (These integers should properly be subscripted as in  $n_A, e_A$ , and  $d_A$ , since each user has his own set. However, we will only consider a typical set, and will omit the subscripts.)

How should you choose your encryption and decryption keys, if you want to use our method?

You first compute  $n$  as the product of two primes  $p$  and  $q$ :

$$n = p * q.$$

These primes are very large, “random” primes. Al-

though you will make  $n$  public, the factors  $p$  and  $q$  will be effectively hidden from everyone else due to the enormous difficulty of factoring  $n$ . This also hides the way  $d$  can be derived from  $e$ .

You then pick the integer  $d$  to be a large, random integer which is relatively prime to  $(p - 1) * (q - 1)$ . That is, check that  $d$  satisfies:

$$\gcd(d, (p - 1) * (q - 1)) = 1$$

("gcd" means "greatest common divisor").

The integer  $e$  is finally computed from  $p$ ,  $q$ , and  $d$  to be the "multiplicative inverse" of  $d$ , modulo  $(p - 1) * (q - 1)$ . Thus we have

$$e * d \equiv 1 \pmod{(p - 1) * (q - 1)}.$$

We prove in the next section that this guarantees that (1) and (2) hold, i.e. that E and D are inverse permutations. Section VII shows how each of the above operations can be done efficiently.

The aforementioned method should not be confused with the "exponentiation" technique presented by Diffie and Hellman [1] to solve the key distribution problem. Their technique permits two users to determine a key in common to be used in a normal cryptographic system. It is not based on a trap-door one-way permutation. Pohlig and Hellman [8] study a scheme related to ours, where exponentiation is done modulo a prime number.

## VI. The Underlying Mathematics

We demonstrate the correctness of the deciphering algorithm using an identity due to Euler and Fermat [7]: for any integer (message)  $M$  which is relatively prime to  $n$ ,

$$M^{\varphi(n)} \equiv 1 \pmod{n}. \quad (3)$$

Here  $\varphi(n)$  is the Euler totient function giving the number of positive integers less than  $n$  which are relatively prime to  $n$ . For prime numbers  $p$ ,

$$\varphi(p) = p - 1.$$

In our case, we have by elementary properties of the totient function [7]:

$$\begin{aligned} \varphi(n) &= \varphi(p) * \varphi(q), \\ &= (p - 1) * (q - 1) \\ &= n - (p + q) + 1. \end{aligned} \quad (4)$$

Since  $d$  is relatively prime to  $\varphi(n)$ , it has a multiplicative inverse  $e$  in the ring of integers modulo  $\varphi(n)$ :

$$e * d \equiv 1 \pmod{\varphi(n)}. \quad (5)$$

We now prove that equations (1) and (2) hold (that is, that deciphering works correctly if  $e$  and  $d$  are chosen as above). Now

$$D(E(M)) \equiv (E(M))^d \equiv (M^e)^d \equiv M^{e*d} \pmod{n}$$

$$E(D(M)) \equiv (D(M))^e \equiv (M^d)^e \equiv M^{d*e} \pmod{n}$$

and

$$M^{e*d} \equiv M^{k*\varphi(n)+1} \pmod{n} \quad (\text{for some integer } k).$$

From (3) we see that for all  $M$  such that  $p$  does not divide  $M$

$$M^{p-1} \equiv 1 \pmod{p}$$

and since  $(p - 1)$  divides  $\varphi(n)$

$$M^{k*\varphi(n)+1} \equiv M \pmod{p}.$$

This is trivially true when  $M \equiv 0 \pmod{p}$ , so that this equality actually holds for all  $M$ . Arguing similarly for  $q$  yields

$$M^{k*\varphi(n)+1} \equiv M \pmod{q}.$$

Together these last two equations imply that for all  $M$ ,

$$M^{e*d} \equiv M^{k*\varphi(n)+1} \equiv M \pmod{n}.$$

This implies (1) and (2) for all  $M$ ,  $0 \leq M < n$ . Therefore E and D are inverse permutations. (We thank Rich Schroepel for suggesting the above improved version of the authors' previous proof.)

## VII. Algorithms

To show that our method is practical, we describe an efficient algorithm for each required operation.

### A. How to Encrypt and Decrypt Efficiently

Computing  $M^e \pmod{n}$  requires at most  $2 * \log_2(e)$  multiplications and  $2 * \log_2(e)$  divisions using the following procedure (decryption can be performed similarly using  $d$  instead of  $e$ ):

*Step 1.* Let  $e_k e_{k-1} \dots e_1 e_0$  be the binary representation of  $e$ .

*Step 2.* Set the variable C to 1.

*Step 3.* Repeat steps 3a and 3b for  $i = k, k - 1, \dots, 0$ :

*Step 3a.* Set C to the remainder of  $C^2$  when divided by  $n$ .

*Step 3b.* If  $e_i = 1$ , then set C to the remainder of  $C * M$  when divided by  $n$ .

*Step 4.* Halt. Now C is the encrypted form of M.

This procedure is called "exponentiation by repeated squaring and multiplication." This procedure is half as good as the best; more efficient procedures are known. Knuth [3] studies this problem in detail.

The fact that the enciphering and deciphering are identical leads to a simple implementation. (The whole operation can be implemented on a few special-purpose integrated circuit chips.)

A high-speed computer can encrypt a 200-digit message  $M$  in a few seconds; special-purpose hardware would be much faster. The encryption time per block increases no faster than the cube of the number of digits in  $n$ .

### B. How to Find Large Prime Numbers

Each user must (privately) choose two large ran-

dom prime numbers  $p$  and  $q$  to create his own encryption and decryption keys. These numbers must be large so that it is not computationally feasible for anyone to factor  $n = p * q$ . (Remember that  $n$ , but not  $p$  or  $q$ , will be in the public file.) We recommend using 100-digit (decimal) prime numbers  $p$  and  $q$ , so that  $n$  has 200 digits.

To find a 100-digit "random" prime number, generate (odd) 100-digit random numbers until a prime number is found. By the prime number theorem [7], about  $(\ln 10^{100})/2 = 115$  numbers will be tested before a prime is found.

To test a large number  $b$  for primality we recommend the elegant "probabilistic" algorithm due to Solovay and Strassen [12]. It picks a random number  $a$  from a uniform distribution on  $\{1, \dots, b - 1\}$ , and tests whether

$$\gcd(a, b) = 1 \text{ and } J(a, b) \equiv a^{(b-1)/2} \pmod{b}, \quad (6)$$

where  $J(a, b)$  is the Jacobi symbol [7]. If  $b$  is prime (6) is always true. If  $b$  is composite (6) will be false with probability at least  $1/2$ . If (6) holds for 100 randomly chosen values of  $a$  then  $b$  is almost certainly prime; there is a (negligible) chance of one in  $2^{100}$  that  $b$  is composite. Even if a composite were accidentally used in our system, the receiver would probably detect this by noticing that decryption didn't work correctly. When  $b$  is odd,  $a \leq b$ , and  $\gcd(a, b) = 1$ , the Jacobi symbol  $J(a, b)$  has a value in  $\{-1, 1\}$  and can be efficiently computed by the program:

```
J(a, b) = if a = 1 then 1 else
           if a is even then J(a/2, b) * (-1)(b2-1)/8
           else J(b(mod a), a) * (-1)(a-1)(b-1)/4
```

(The computations of  $J(a, b)$  and  $\gcd(a, b)$  can be nicely combined, too.) Note that this algorithm does *not* test a number for primality by trying to factor it. Other efficient procedures for testing a large number for primality are given in [6, 9, 11].

To gain additional protection against sophisticated factoring algorithms,  $p$  and  $q$  should differ in length by a few digits, both  $(p - 1)$  and  $(q - 1)$  should contain large prime factors, and  $\gcd(p - 1, q - 1)$  should be small. The latter condition is easily checked.

To find a prime number  $p$  such that  $(p - 1)$  has a large prime factor, generate a large random prime number  $u$ , then let  $p$  be the first prime in the sequence  $i * u + 1$ , for  $i = 2, 4, 6, \dots$  (This shouldn't take too long.) Additional security is provided by ensuring that  $(u - 1)$  also has a large prime factor.

A high-speed computer can determine in several seconds whether a 100-digit number is prime, and can find the first prime after a given point in a minute or two.

Another approach to finding large prime numbers is to take a number of known factorization, add one to it, and test the result for primality. If a prime  $p$  is found it is possible to *prove* that it really is prime by

using the factorization of  $p - 1$ . We omit a discussion of this since the probabilistic method is adequate.

### C. How to Choose $d$

It is very easy to choose a number  $d$  which is relatively prime to  $\varphi(n)$ . For example, any prime number greater than  $\max(p, q)$  will do. It is important that  $d$  should be chosen from a large enough set so that a cryptanalyst cannot find it by direct search.

### D. How to Compute $e$ from $d$ and $\varphi(n)$

To compute  $e$ , use the following variation of Euclid's algorithm for computing the greatest common divisor of  $\varphi(n)$  and  $d$ . (See exercise 4.5.2.15 in [3].) Calculate  $\gcd(\varphi(n), d)$  by computing a series  $x_0, x_1, x_2, \dots$ , where  $x_0 = \varphi(n)$ ,  $x_1 = d$ , and  $x_{i+1} \equiv x_{i-1} \pmod{x_i}$ , until an  $x_k$  equal to 0 is found. Then  $\gcd(x_0, x_1) = x_{k-1}$ . Compute for each  $x_i$  numbers  $a_i$  and  $b_i$  such that  $x_i = a_i * x_0 + b_i * x_1$ . If  $x_{k-1} = 1$  then  $b_{k-1}$  is the multiplicative inverse of  $x_1 \pmod{x_0}$ . Since  $k$  will be less than  $2 * \log_2(n)$ , this computation is very rapid.

If  $e$  turns out to be less than  $\log_2(n)$ , start over by choosing another value of  $d$ . This guarantees that every encrypted message (except  $M = 0$  or  $M = 1$ ) undergoes some "wrap-around" (reduction modulo  $n$ ).

### VIII. A Small Example

Consider the case  $p = 47, q = 59, n = p * q = 47 * 59 = 2773$ , and  $d = 157$ . Then  $\varphi(2773) = 46 * 58 = 2668$ , and  $e$  can be computed as follows:

$$\begin{array}{lll} x_0 = 2668, & a_0 = 1, & b_0 = 0, \\ x_1 = 157, & a_1 = 0, & b_1 = 1, \\ x_2 = 156, & a_2 = 1, & b_2 = -16 \text{ (since } 2668 \\ & & = 157 * 16 + 156 \text{)}, \\ x_3 = 1, & a_3 = -1, & b_3 = 17 \text{ (since } 157 = 1 \\ & & * 156 + 1 \text{)}. \end{array}$$

Therefore  $e = 17$ , the multiplicative inverse (mod 2668) of  $d = 157$ .

With  $n = 2773$  we can encode two letters per block, substituting a two-digit number for each letter: blank = 00, A = 01, B = 02,  $\dots$ , Z = 26. Thus the message

ITS ALL GREEK TO ME  
(Julius Caesar, I, ii, 288, paraphrased) is encoded:

0920 1900 0112 1200 0718  
0505 1100 2015 0013 0500

Since  $e = 10001$  in binary, the first block ( $M = 920$ ) is enciphered:

$$M^{17} \equiv (((((1)^2 * M)^2)^2)^2 * M \equiv 948 \pmod{2773}.$$

The whole message is enciphered as:

0948 2342 1084 1444 2663  
2390 0778 0774 0219 1655.

The reader can check that deciphering works:  $948^{157} \equiv 920 \pmod{2773}$ , etc.

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