[54] CRYPTOGRAPHIC COMMUNICATIONS SYSTEM AND METHOD
[75] Inventors: Ronald L. Rivest, Belmont; Adi Shamir, Cambridge; Leonard M. Adleman, Arlington, all of Mass.
[73] Assignee:
Massachusetts Institute of Technology, Cambridge, Mass.

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Primary Examiner-Sal Cangialosi
Attorney, Agent, or Firm—Arthur A. Smith, Jr.; Robert J. Horn, Jr.

## [57]

ABSTRACT
A cryptographic communications system and method. The system includes a communications channel coupled to at least one terminal having an encoding device and to at least one terminal having a decoding device. A message-to-be-transferred is enciphered to ciphertext at the encoding terminal by first encoding the message as a number M in a predetermined set, and then raising that number to a first predetermined power (associated with the intended receiver) and finally computing the remainder, or residue, C , when the exponentiated number is divided by the product of two predetermined prime numbers (associated with the intended receiver). The residue $\mathbf{C}$ is the ciphertext. The ciphertext is deciphered to the original message at the decoding terminal in a similar manner by raising the ciphertext to a second predetermined power (associated with the intended receiver), and then computing the residue, $\mathbf{M}^{\prime}$, when the exponentiated ciphertext is divided by the product of the two predetermined prime numbers associated with the intended receiver. The residue $\mathbf{M}^{\prime}$ corresponds to the original encoded message M .

40 Claims, 7 Drawing Figures



FIG. I


FIG. 2


FIG. 3 cipher text c



FIG. 6


FIG. 7

## CRYPTOGRAPHIC COMMUNICATIONS SYSTEM AND METHOD

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## BACKGROUND OF THE DISCLOSURE

This invention relates to communications, and more particularly to cryptographic communications systems and methods.
With the development of computer technology, the transfer of information in digital form has rapidly increased. There are many applications, including electronic mail systems, bank systems and data processing systems, where the transferred information must pass over communications channels which may be monitored by electronic eavesdroppers. While the degree of security required may vary for various applications, it is generally important for all of these examples that the substance of particular communications pass directly from a sender to an intended receiver without intermediate parties being able to interpret the transferred message. In addition, there are further instances where information in cumputer memory banks must be protected from snoopers who have access to the memory through data processing networks.
In addition to these privacy requirements, authentication of the source of a message must often be insured along with the verification and security of the message content. For example, in banking applications, it is required that a signed document, such as a bank draft, be authenticated as being actually signed by the indicated signator. Furthermore, in many applications, it is desirable to further require safeguards against signature forgery by a message recipient.
In the prior art, a number of cryptographic encoding and decoding techniques are readily available to provide some degree of privacy and authentication for digital communications, for example, the data encryption standards adopted by the National Bureau of Standards, see Federal Register, Mar. 17, 1975, Volume 40, No. 52 and Aug. 1, 1975, Yolume 40, No. 149.

In general, cryptographic systems are adapted to transfer a message between remote locations. Such systems include at least one encoding device at a first location and at least one decoding device at a second location, with the encoding and decoding devices all being coupled to a communication channel. For digital systems, the message is defined to be a digital message, $M$, that is, a sequence of symbols from some alphabet. In practice, the alphabet is generally chosen to be the binary alphabet consisting of the symbols 0 and 1 .

Each encoding device is an apparatus which accepts two inputs: a message-to-be-encoded, $M$, and an encoding key or operator, $E$. Each encoding device transforms the message M in accordance with the encryption operator to produce an encoded version $C$ of the message (which is denoted as the ciphertext) where $\mathrm{C}=\mathrm{E}(\mathrm{M})$. The encoding key and the ciphertext are also digital sequences.
Each decoding device is an apparatus which accepts two inputs: a ciphertext-to-be-decoded C and a decoding key or operator, D. Each decoding device transforms the ciphertext in accordance with the decryption operator to produce a decoded version $\mathbf{M}^{\prime}$ of the cipher-
for any message M. In order for the public key system to be practical, both $\mathrm{E}_{A}$ and $\mathrm{D}_{A}$ must be efficiently computable. Furthermore, user A must not compromise $\mathrm{D}_{A}$ when revealing $\mathrm{E}_{A}$. That is, it should not be computationally feasible for an eavesdropper to find an efficient way of computing $\mathrm{D}_{A}$, given only a specification of the enciphering key $\mathrm{E}_{A}$ (even though a very inefficient way exists: to compute $\mathrm{D}_{A}(\mathrm{C})$, just enumerate all possible messages $M$ until one such that $\mathrm{E}_{A}(\mathrm{M})=\mathrm{C}$ is found. Then $\mathrm{D}_{A}(\mathrm{C})=\mathrm{M}$.). In a public key system, a judicious selection of keys ensures that only user $A$ is able to compute $\mathrm{D}_{A}$ efficiently.
Whenever another user (e.g. user B) wishes to send a message M to A , he looks up $\mathrm{E}_{A}$ in the public file and then sends the enciphered message $\mathrm{E}_{A}(\mathrm{M})$ to user A . User A deciphers the message by computing $\mathrm{D}_{A}$ $\left(E_{A}(M)\right)=M$. Since $D_{A}$ is not derivable from $E_{A}$ in a practical way, only user A can decipher the message

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